

Review problems

①

2.56

$$\Delta P = 5 \text{ kPa}$$

Energy Balance $\dot{V} \Delta P = \dot{W}$

$$\Delta P \dot{V} = \dot{W} = 5.2 \text{ kW}$$

$$\therefore \dot{V} = \frac{5.2}{5.0} = 1.04 \text{ m}^3/\text{sec}$$

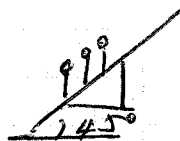
2.57

$$M = 30 \times 75 = 2250 \text{ kg}$$

$$\frac{\Delta PE}{\Delta t} = M g \frac{\Delta z}{\Delta t}$$

$$= M g \cdot \dot{V} \sin 45^\circ$$

$$= \frac{(2250)(0.8)(9.8)}{\sqrt{2}} = \underline{\underline{12.5 \text{ kW}}}$$



Note: Power Consumption results in people realizing Potential Energy

2.71

$$\dot{W}_{\text{shaft}} = \frac{\dot{m}(\Delta PE)}{1000} \text{ kW}$$

$$\frac{(1500)(9.81)(70)}{1000} = \underline{\underline{1031 \text{ kW}}}$$

If "generator" is efficient as well as the shaft assembly, then the power generated should be closer to this. This leads to

$$\eta_{\text{overall}} = \frac{\text{Desired output}}{\text{required input}} = \frac{750 \text{ kW}}{1031} = \underline{\underline{0.7274}} \approx \underline{\underline{0.73}}$$

Looking at generator, $\eta_{\text{gen}} = \frac{750}{800} = 0.94$

$$\eta_{\text{turbine}} = \frac{800}{1031} = 0.78$$

$$\boxed{\eta_{\text{overall}} = \eta_{\text{turbine}} \cdot \eta_{\text{gen}}}$$

(2)

2.80

$$\Delta E_{\text{mech}} = \dot{m} \left[\left(\frac{P_2}{\rho} + \frac{V_2^2}{2} \right) - \left(\frac{P_1}{\rho} + \frac{V_1^2}{2} \right) \right]$$

$$= \frac{\dot{m}}{\rho} \left[\left(P_2 + \rho \frac{V_2^2}{2} \right) - \left(P_1 + \rho \frac{V_1^2}{2} \right) \right]$$

$$\dot{m} = \rho \vec{V} \cdot \vec{A} \quad \dot{m} = \rho \dot{V} = \frac{\dot{V}}{G} \quad (\dot{V} = \text{vol. flow rate})$$

$\rho = \text{density constant (Incompressible)}$

$$= \dot{V} \left[(P_2 - P_1) + \frac{\rho (V_2^2 - V_1^2)}{2000} \right] \text{ kW}$$

$$= (\dot{V}) \left[(400) + \frac{860 (V_2^2 - V_1^2)}{2000} \right] \text{ kW}$$

$$V_1 = \frac{\dot{V}}{A_1} = \frac{0.1 \text{ m}^3/\text{s}}{\pi (0.08)^2} = 19.9 \text{ m/s}$$

$$V_2 = \frac{\dot{V}}{A_2} = \frac{0.1 \text{ m}^3/\text{s}}{\frac{\pi (0.12)^2}{4}} = 8.84 \text{ m/s}$$

From First law

$$\dot{W}_{\text{pump}} = \Delta E_{\text{mech}}$$

$$= (0.1) \left(400 + \frac{860 (8.84^2 - 19.9^2)}{2000} \right) \text{ kW}$$

$$= \underline{26.3 \text{ kW}}$$

$$\dot{W}_{\text{pump, shaft}} = \eta_{\text{motor}} \dot{W}_{\text{electric}} = 35 \times 0.9 = 31.5 \text{ kW}$$

$$\eta_{\text{pump}} = \frac{26.3 \text{ (output)}}{31.5 \text{ (input)}} = 0.836 \%$$

Note: Here efficiency defined as what is ideally required & what is provided

(3)

2.142

$$\dot{Q} = 100 \times 0.08$$

$$= 8 \text{ W}$$

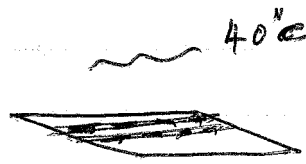
$$A = 0.02 \text{ m}^2$$

$$h = 10 \text{ W/m}^2 \text{ } ^\circ\text{C}$$

$$\dot{Q} = h A (T - T_{\text{amb}})$$

$$\frac{\dot{Q}}{hA} + T_{\text{amb}} = T \Rightarrow \frac{0.08}{(10)(0.02)} + 40^\circ\text{C}$$

$$= 40^\circ\text{C} + 40^\circ\text{C} = \underline{\underline{80^\circ\text{C}}}$$

2.78

$$\dot{\Delta E}_{\text{mech}} = \dot{m} \Delta e_{\text{mech}} = \dot{m} \Delta(P) = \dot{m} g (\Delta z)$$

$$(1000)(0.03)(9.81)(45) = \underline{\underline{13.2 \text{ kW}}}$$

$$\dot{W}_{\text{friction}} = \dot{W}_{\text{pump, actual}} - \dot{\Delta E}_{\text{mech}}$$

$$= 20 - 13.2 = \underline{\underline{6.8 \text{ kW}}}$$

$$\eta_{\text{pump}} = \frac{13.2}{20.0} \approx \underline{\underline{0.66}} \text{ or } \underline{\underline{66\%}}$$

2.72

$$\text{Sweeping Area} = \frac{\pi D^2}{4} = \frac{\pi (50)^2}{4}$$

$$\dot{m}_{\text{air}} = \rho A v = (1.25) \left(\frac{\pi 50^2}{4} \right) (12)$$

$$= \underline{\underline{29,450 \text{ kg/s}}}$$

$$\dot{W}_{\text{max}} = \dot{E}_{\text{mech}} = \dot{m} e_{\text{mech}}$$

$$e_{\text{mech}} = k_e = \frac{v^2}{2} = \frac{12^2}{2000} = 0.072 \frac{\text{kJ}}{\text{kg}}$$

$$\dot{W}_{\text{max}} = (29450)(0.072) = \underline{\underline{2121 \text{ kW}}}$$

$$\dot{W}_{\text{el}} = \eta \dot{W}_{\text{max}}$$