Process Heat Iransfer
Principles and applications


## Process Heat Transfer

## Dedication

This book is dedicated to C.C.S.

# Process Heat Transfer Principles and Applications 

R.W. Serth<br>Department of Chemical and Natural Gas Engineering, Texas A\&M University-Kingsville, Kingsville, Texas, USA

AMSTERDAM • BOSTON • HEIDELBERG • LONDON • NEW YORK • OXFORD PARIS • SAN DIEGO•SAN FRANCISCO•SINGAPORE •SYDNEY • TOKYO

Academic Press is an imprint of Elsevier
30 Corporate Drive, Suite 400, Burlington, MA 01803, USA
Linacre House, Jordan Hill, Oxford OX2 8DP, UK
The Boulevard, Langford Lane, Kidlington, Oxford OX5 1GB, UK
First edition 2007

Copyright © 2007, Elsevier Ltd. All rights reserved

No part of this publication may be reproduced, stored in a retrieval system or transmitted in any form or by any means electronic, mechanical, photocopying, recording or otherwise without the prior written permission of the publisher

Permissions may be sought directly from Elsevier's Science \& Technology Rights Department in Oxford, UK: phone (+44) (0) 1865 843830; fax (+44) (0) 1865853333 ; email: permissions@elsevier.com. Alternatively you can submit your request online by visiting the Elsevier web site at http://elsevier.com/locate/permissions, and selecting Obtaining permission to use Elsevier material

Notice
No responsibility is assumed by the publisher for any injury and/or damage to persons or property as a matter of products liability, negligence or otherwise, or from any use or operation of any methods, products, instructions or ideas contained in the material herein. Because of rapid advances in the medical sciences, in particular, independent verification of diagnoses and drug dosages should be made

## British Library Cataloguing in Publication Data

Serth, R. W.
Process heat transfer: principles and applications

1. Heat-Transmission 2. Heat exchangers 3. Heat exchangers-Design
2. Heat-Transmission - Computer programs
I. Title
$621.4^{\prime} 022$

## Library of Congress Catalog number: 2006940583

ISBN: 978-0-12-373588-1

For information on all Academic Press publications visit our web site at http://books.elsevier.com

Typeset by Charon Tec Ltd (A Macmillan Company), Chennai, India
www.charontec.com
Printed and bound in USA
$060708091011 \quad 10987654321$

## Working together to grow libraries in developing countries

www.elsevier.com | www.bookaid.org | www.sabre.org

## Contents

Preface viii
Conversion Factors ..... X
Physical Constants ..... xi
Acknowledgements ..... xii
1 Heat Conduction ..... 1
1.1 Introduction ..... 2
1.2 Fourier's Law of Heat Conduction ..... 2
1.3 The Heat Conduction Equation ..... 6
1.4 Thermal Resistance ..... 15
1.5 The Conduction Shape Factor ..... 19
1.6 Unsteady-State Conduction ..... 24
1.7 Mechanisms of Heat Conduction ..... 31
2 Convective Heat Transfer ..... 43
2.1 Introduction ..... 44
2.2 Combined Conduction and Convection ..... 44
2.3 Extended Surfaces ..... 47
2.4 Forced Convection in Pipes and Ducts ..... 53
2.5 Forced Convection in External Flow ..... 62
2.6 Free Convection ..... 65
3 Heat Exchangers ..... 85
3.1 Introduction ..... 86
3.2 Double-Pipe Equipment ..... 86
3.3 Shell-and-Tube Equipment ..... 87
3.4 The Overall Heat-Transfer Coefficient ..... 93
3.5 The LMTD Correction Factor ..... 98
3.6 Analysis of Double-Pipe Exchangers ..... 102
3.7 Preliminary Design of Shell-and-Tube Exchangers ..... 106
3.8 Rating a Shell-and-Tube Exchanger ..... 109
3.9 Heat-Exchanger Effectiveness ..... 114
4 Design of Double-Pipe Heat Exchangers ..... 127
4.1 Introduction ..... 128
4.2 Heat-Transfer Coefficients for Exchangers without Fins ..... 128
4.3 Hydraulic Calculations for Exchangers without Fins ..... 128
4.4 Series/Parallel Configurations of Hairpins ..... 131
4.5 Multi-tube Exchangers ..... 132
4.6 Over-Surface and Over-Design ..... 133
4.7 Finned-Pipe Exchangers ..... 141
4.8 Heat-Transfer Coefficients and Friction Factors for Finned Annuli ..... 143
4.9 Wall Temperature for Finned Pipes ..... 145
4.10 Computer Software ..... 152
5 Design of Shell-and-Tube Heat Exchangers ..... 187
5.1 Introduction ..... 188
5.2 Heat-Transfer Coefficients ..... 188
5.3 Hydraulic Calculations ..... 189
5.4 Finned Tubing ..... 192
5.5 Tube-Count Tables ..... 194
5.6 Factors Affecting Pressure Drop ..... 195
5.7 Design Guidelines ..... 197
5.8 Design Strategy ..... 201
5.9 Computer software ..... 218
6 The Delaware Method ..... 245
6.1 Introduction ..... 246
6.2 Ideal Tube Bank Correlations ..... 246
6.3 Shell-Side Heat-Transfer Coefficient ..... 248
6.4 Shell-Side Pressure Drop ..... 250
6.5 The Flow Areas ..... 254
6.6 Correlations for the Correction Factors ..... 259
6.7 Estimation of Clearances ..... 260
$7 \quad$ The Stream Analysis Method ..... 277
7.1 Introduction ..... 278
7.2 The Equivalent Hydraulic Network ..... 278
7.3 The Hydraulic Equations ..... 279
7.4 Shell-Side Pressure Drop ..... 281
7.5 Shell-Side Heat-Transfer Coefficient ..... 281
7.6 Temperature Profile Distortion ..... 282
7.7 The Wills-Johnston Method ..... 284
7.8 Computer Software ..... 295
8 Heat-Exchanger Networks ..... 327
8.1 Introduction ..... 328
8.2 An Example: TC3 ..... 328
8.3 Design Targets ..... 329
8.4 The Problem Table ..... 329
8.5 Composite Curves ..... 331
8.6 The Grand Composite Curve ..... 334
8.7 Significance of the Pinch ..... 335
8.8 Threshold Problems and Utility Pinches ..... 337
8.9 Feasibility Criteria at the Pinch ..... 337
8.10 Design Strategy ..... 339
8.11 Minimum-Utility Design for TC3 ..... 340
8.12 Network Simplification ..... 344
8.13 Number of Shells ..... 347
8.14 Targeting for Number of Shells ..... 348
8.15 Area Targets ..... 353
8.16 The Driving Force Plot ..... 356
8.17 Super Targeting ..... 358
8.18 Targeting by Linear Programming ..... 359
8.19 Computer Software ..... 361
$9 \quad$ Boiling Heat Transfer ..... 385
9.1 Introduction ..... 386
9.2 Pool Boiling ..... 386
9.3 Correlations for Nucleate Boiling on Horizontal Tubes ..... 387
9.4 Two-Phase Flow ..... 402
9.5 Convective Boiling in Tubes ..... 416
9.6 Film Boiling ..... 428
10 Reboilers ..... 443
10.1 Introduction ..... 444
10.2 Types of Reboilers ..... 444
10.3 Design of Kettle Reboilers ..... 449
10.4 Design of Horizontal Thermosyphon Reboilers ..... 467
10.5 Design of Vertical Thermosyphon Reboilers ..... 473
10.6 Computer Software ..... 488
11 Condensers ..... 539
11.1 Introduction ..... 540
11.2 Types of Condensers ..... 540
11.3 Condensation on a Vertical Surface: Nusselt Theory ..... 545
11.4 Condensation on Horizontal Tubes ..... 549
11.5 Modifications of Nusselt Theory ..... 552
11.6 Condensation Inside Horizontal Tubes ..... 562
11.7 Condensation on Finned Tubes ..... 568
11.8 Pressure Drop ..... 569
11.9 Mean Temperature Difference ..... 571
11.10 Multi-component Condensation ..... 590
11.11 Computer Software ..... 595
12 Air-Cooled Heat Exchangers ..... 629
12.1 Introduction ..... 630
12.2 Equipment Description ..... 630
12.3 Air-Side Heat-Transfer Coefficient ..... 637
12.4 Air-Side Pressure Drop ..... 638
12.5 Overall Heat-Transfer Coefficient ..... 640
12.6 Fan and Motor Sizing ..... 640
12.7 Mean Temperature Difference ..... 643
12.8 Design Guidelines ..... 643
12.9 Design Strategy ..... 644
12.10 Computer Software ..... 653
Appendix ..... 681
Appendix A Thermophysical Properties of Materials ..... 682
Appendix B Dimensions of Pipe and Tubing ..... 717
Appendix C Tube-Count Tables ..... 729
Appendix D Equivalent Lengths of Pipe Fittings ..... 737
Appendix E Properties of Petroleum Streams ..... 740
Index ..... 743

## Preface

This book is based on a course in process heat transfer that I have taught for many years. The course has been taken by seniors and first-year graduate students who have completed an introductory course in engineering heat transfer. Although this background is assumed, nearly all students need some review before proceeding to more advanced material. For this reason, and also to make the book self-contained, the first three chapters provide a review of essential material normally covered in an introductory heat transfer course. Furthermore, the book is intended for use by practicing engineers as well as university students, and it has been written with the aim of facilitating self-study.

Unlike some books in this field, no attempt is made herein to cover the entire panoply of heat transfer equipment. Instead, the book focuses on the types of equipment most widely used in the chemical process industries, namely, shell-and-tube heat exchangers (including condensers and reboilers), air-cooled heat exchangers and double-pipe (hairpin) heat exchangers. Within the confines of a single volume, this approach allows an in-depth treatment of the material that is most relevant from an industrial perspective, and provides students with the detailed knowledge needed for engineering practice. This approach is also consistent with the time available in a one-semester course.

Design of double-pipe exchangers is presented in Chapter 4. Chapters 5-7 comprise a unit dealing with shell-and-tube exchangers in operations involving single-phase fluids. Design of shell-and-tube exchangers is covered in Chapter 5 using the Simplified Delaware method for shell-side calculations. For pedagogical reasons, more sophisticated methods for performing shell-side heat-transfer and pressure-drop calculations are presented separately in Chapter 6 (full Delaware method) and Chapter 7 (Stream Analysis method). Heat exchanger networks are covered in Chapter 8. I normally present this topic at this point in the course to provide a change of pace. However, Chapter 8 is essentially self-contained and can, therefore, be covered at any time. Phase-change operations are covered in Chapters 9-11. Chapter 9 presents the basics of boiling heat transfer and two-phase flow. The latter is encountered in both Chapter 10, which deals with the design of reboilers, and Chapter 11, which covers condensation and condenser design. Design of air-cooled heat exchangers is presented in Chapter 12. The material in this chapter is essentially self-contained and, hence, it can be covered at any time.

Since the primary goal of both the book and the course is to provide students with the knowledge and skills needed for modern industrial practice, computer applications play an integral role, and the book is intended for use with one or more commercial software packages. HEXTRAN (SimSci-Esscor), HTRI Xchanger Suite (Heat Transfer Research, Inc.) and the HTFS Suite (Aspen Technology, Inc.) are used in the book, along with HX-Net (Aspen Technology, Inc.) for pinch calculations. HEXTRAN affords the most complete coverage of topics, as it handles all types of heat exchangers and also performs pinch calculations for design of heat exchanger networks. It does not perform mechanical design calculations for shell-and-tube exchangers, however, nor does it generate detailed tube layouts or setting plans. Furthermore, the methodology used by HEXTRAN is based on publicly available technology and is generally less refined than that of the other software packages. The HTRI and HTFS packages use proprietary methods developed by their respective research organizations, and are similar in their level of refinement. HTFS Suite handles all types of heat exchangers; it also performs mechanical design calculations and develops detailed tube layouts and setting plans for shell-and-tube exchangers. HTRI Xchanger Suite lacks a mechanical design feature, and the module for hairpin exchangers is not included with an academic license. Neither HTRI nor HTFS has the capability to perform pinch calculations.

As of this writing, Aspen Technology is not providing the TASC and ACOL modules of the HTFS Suite under its university program. Instead, it is offering the HTFS-plus design package. This package basically consists of the TASC and ACOL computational engines combined with slightly modified GUI's from the corresponding BJAC programs (HETRAN and AEROTRAN), and packaged with the BJAC TEAMS mechanical design program. This package differs greatly in appearance and to some extent in available features from HTFS Suite. However, most of the results presented in the text using TASC and ACOL can be generated using the HTFS-plus package.

Software companies are continually modifying their products, making differences between the text and current versions of the software packages unavoidable. However, many modifications involve only superficial changes in format that have little, if any, effect on results. More substantive changes occur less frequently, and even then the effects tend to be relatively minor. Nevertheless, readers should expect some divergence of the software from the versions used herein, and they should not be unduly concerned if their results differ somewhat from those presented in the text. Indeed, even the same version of a code, when run on different machines, can produce slightly different results due to differences in round-off errors. With these caveats, it is hoped that the detailed computer examples will prove helpful in learning to use the software packages, as well as in understanding their idiosyncrasies and limitations.

I have made a concerted effort to introduce the complexities of the subject matter gradually throughout the book in order to avoid overwhelming the reader with a massive amount of detail at any one time. As a result, information on shell-and-tube exchangers is spread over a number of chapters, and some of the finer details are introduced in the context of example problems, including computer examples. Although there is an obvious downside to this strategy, I nevertheless believe that it represents good pedagogy.

Both English units, which are still widely used by American industry, and SI units are used in this book. Students in the United States need to be proficient in both sets of units, and the same is true of students in countries that do a large amount of business with U.S. firms. In order to minimize the need for unit conversion, however, working equations are either given in dimensionless form or, when this is not practical, they are given in both sets of units.

I would like to take this opportunity to thank the many students who have contributed to this effort over the years, both directly and indirectly through their participation in my course. I would also like to express my deep appreciation to my colleagues in the Department of Chemical and Natural Gas Engineering at TAMUK, Dr. Ali Pilehvari and Mrs. Wanda Pounds. Without their help, encouragement and friendship, this book would not have been written.

## Conversion Factors

| Acceleration | $1 \mathrm{~m} / \mathrm{s}^{2}=4.2520 \times 10^{7} \mathrm{ft} / \mathrm{h}^{2}$ |
| :--- | ---: |
| Area | $1 \mathrm{~m}^{2}=10.764 \mathrm{ft}^{2}$ |
| Density | $1 \mathrm{~kg} / \mathrm{m}^{3}=0.06243 \mathrm{lbm} / \mathrm{ft}^{3}$ |
| Energy | $1 \mathrm{~J}=0.239 \mathrm{cal}=9.4787 \times 10^{-4} \mathrm{Btu}$ |
| Force | $1 \mathrm{~N}=0.22481 \mathrm{lbf}$ |
| Fouling factor | $1 \mathrm{~m}^{2} \cdot \mathrm{~K} / \mathrm{W}=5.6779 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ |
| Heat capacity flow rate | $1 \mathrm{~kW} / \mathrm{K}=1 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$ |
|  | $=1895.6 \mathrm{Btu} / \mathrm{h} \cdot{ }^{\circ} \mathrm{F}$ |
| Heat flux | $1 \mathrm{~W} / \mathrm{m}^{2}$ |$=0.3171 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.

lbf: pound force and lbm: pound mass.

## Physical Constants

| Quantity | Symbol | Value |
| :--- | :--- | :--- |
| Universal gas constant | $\widetilde{R}$ | $0.08205 \mathrm{~atm} \cdot \mathrm{~m}^{3} / \mathrm{kmol} \cdot \mathrm{K}$ |
|  |  | $0.08314 \mathrm{bar} \cdot \mathrm{m}^{3} / \mathrm{kmol} \cdot \mathrm{K}$ |
|  |  | $8314 \mathrm{~J} / \mathrm{kmol} \cdot \mathrm{K}$ |
|  |  | $1.986 \mathrm{cal} / \mathrm{mol} \cdot \mathrm{K}$ |
|  |  | $1.986 \mathrm{Btu} / \mathrm{lb} \mathrm{mole} \cdot{ }^{\circ} \mathrm{R}$ |
|  |  | $10.73 \mathrm{psia} \cdot \mathrm{ft}^{3} / \mathrm{lb} \mathrm{mole} \cdot{ }^{\circ} \mathrm{R}$ |
|  |  | $1545 \mathrm{ft} \cdot \mathrm{lbf} / \mathrm{lb} \mathrm{mole} \cdot{ }^{\circ} \mathrm{R}$ |
| Standard gravitational acceleration | g | $9.8067 \mathrm{~m} / \mathrm{s}^{2}$ |
|  |  | $32.174 \mathrm{ft} / \mathrm{s}^{2}$ |
|  |  | $4.1698 \times 10^{8} \mathrm{ft} / \mathrm{h}^{2}$ |
| Stefan-Boltzman constant | $\sigma_{S B}$ | $5.670 \times 10^{-8} \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}^{4}$ |
|  |  | $1.714 \times 10^{-9} \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{R}^{4}$ |

## Acknowledgements

## Item

## Special Credit Line

Figure 3.1 Reprinted, with permission, from Extended Surface Heat Transfer by D. Q. Kern and A. D. Kraus. Copyright © 1972 by The McGraw-Hill Companies, Inc.

Table 3.1 Reprinted, with permission, from Perry's Chemical Engineers' Handbook, 7th edn., R. H. Perry and D. W. Green, eds. Copyright © 1997 by The McGraw-Hill Companies, Inc.

Figure 3.6 Reprinted, with permission, from Extended Surface Heat Transfer by D. Q. Kern and A. D. Kraus. Copyright © 1972 by The McGraw-Hill Companies, Inc.

Figure 3.7 Reprinted, with permission, from Extended Surface Heat Transfer by D. Q. Kern and A. D. Kraus. Copyright © 1972 by The McGraw-Hill Companies, Inc.

Table 3.2 Reproduced, with permission, from J. W. Palen and J. Taborek, Solution of shell side flow pressure drop and heat transfer by stream analysis method, Chem. Eng. Prog. Symposium Series, 65, No. 92, 53-63, 1969. Copyright © 1969 by AIChE.

Table 3.5 Reprinted, with permission, from Perry's Chemical Engineers' Handbook, 7th edn., R. H. Perry and D. W. Green, eds. Copyright © 1997 by The McGraw-Hill Companies, Inc.

Figure 4.1 Copyright © 1998 from Heat Exchangers: Selection, Rating and Thermal Design by S. Kakac and H. Liu. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

Figure $4.2 \quad$ Copyright © 1998 from Heat Exchangers: Selection, Rating and Thermal Design by S. Kakac and H. Liu. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

Figure 4.4 Reprinted, with permission, from Extended Surface Heat Transfer by D. Q. Kern and A. D. Kraus. Copyright © 1972 by The McGraw-Hill Companies, Inc.

Figure 4.5 Reprinted, with permission, from Extended Surface Heat Transfer by D. Q. Kern and A. D. Kraus. Copyright © 1972 by The McGraw-Hill Companies, Inc.

Figure 5.3 Reproduced, with permission, from R. Mukherjee, Effectively design shell-and-tube heat exchangers, Chem. Eng. Prog., 94, No. 2, 21-37, 1998. Copyright © 1998 by AIChE.
Figure 5.4 Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-inChief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Figures 6.1-6.5 Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-inChief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Table 6.1 Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-inChief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Figure $6.10 \quad$ Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-inChief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

Figure 7.1 Reproduced, with permission, from J. W. Palen and J. Taborek, Solution of shell side flow pressure drop and heat transfer by stream analysis method, Chem. Eng. Prog. Symposium Series, 65, No. 92, 53-63, 1969. Copyright © 1969 by AIChE.
Table, p. 283 Reproduced, with permission, from R. Mukherjee, Effectively design shell-and-tube heat exchangers, Chem. Eng. Prog., 94, No. 2, 21-37, 1998. Copyright © 1998 by AIChE.
Figure 8.20 Reprinted from Computers and Chemical Engineering, Vol. 26, X. X. Zhu and X. R. Nie, Pressure Drop Considerations for Heat Exchanger Network Grassroots Design, pp. 16611676, Copyright © 2002, with permission from Elsevier.

## Item Special Credit Line

Figure 9.2

Figures 10.1-10.5 Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-in-Chief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

Figure 10.6

Table 10.1

Appendix 10.A

Figure 11.1

Figure 11.3

Figure 11.6 Copyright© 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-in-Chief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Figure 11.7 Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-in-Chief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Figure 11.8 Reprinted, with permission, from Distillation Operation by H.Z. Kister. Copyright © 1990 by The McGraw-Hill Companies, Inc.
Figure 11.11 Reprinted, with permission, from G. Breber, J. W. Palen and J. Taborek, Prediction of tubeside condensation of pure components using flow regime criteria, J. Heat Transfer, 102, 471-476, 1980. Originally published by ASME.
Figure $11.12 \quad$ Copyright © 1998 from Heat Exchangers: Selection, Rating and Thermal Design by S. Kakac and H. Liu. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

Figures 11.A1-11.A3 Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-in-Chief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Figure 12.5
Copyright © 1991 from Heat Transfer Design Methods by J. J. McKetta, Editor. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

Figures 12.A1-12.A5 Copyright © 1988 from Heat Exchanger Design Handbook by E. U. Schlünder, Editor-in-Chief. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Table A. 1
Copyright © 1972 from Handbook of Thermodynamic Tables and Charts by K. Raznjevič. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Table A. 3 Reprinted, with permission, from Heat Transfer, 7th edn., by J. P. Holman. Copyright © 1990 by The McGraw-Hill Companies, Inc.
Table A. 4 Copyright © 1972 from Handbook of Thermodynamic Tables and Charts by K. Raznjevič. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Table A. 7
Copyright © 1972 from Handbook of Thermodynamic Tables and Charts by K. Raznjevič. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

## Item Special Credit Line

Table A. 8 Reprinted, with permission, from ASME Steam Tables, American Society of Mechanical Engineers, New York, 1967. Originally published by ASME.
Table A. 9 Reprinted, with permission, from Flow of Fluids Through Valves, Fittings and Pipe, Technical Paper 410, 1988, Crane Company. All rights reserved.
Table A. 11 Copyright © 1975 from Tables of Thermophysical Properties of Liquids and Gases, 2nd edn., by N. B. Vargaftik. Reproduced by permission of Taylor \& Francis, a division of Informa plc.

Table A. 13 Copyright © 1972 from Handbook of Thermodynamic Tables and Charts by K. Raznjevič. Reproduced by permission of Taylor \& Francis, a division of Informa plc.
Table A. 15 Reprinted, with permission, from Chemical Engineers' Handbook, 5th edn., R. H. Perry and C. H. Chilton, eds. Copyright © 1973 by The McGraw-Hill Companies, Inc.

Table A. 17 Reprinted, with permission, from Chemical Engineers' Handbook, 5th edn., R. H. Perry and C. H. Chilton, eds. Copyright © 1973 by The McGraw-Hill Companies, Inc.

Figure A. 1 Reprinted, with permission, from Chemical Engineers' Handbook, 5th edn., R. H. Perry and C. H. Chilton, eds. Copyright © 1973 by The McGraw-Hill Companies, Inc.

Table A. 18 Reprinted, with permission, from Chemical Engineers' Handbook, 5th edn., R. H. Perry and C. H. Chilton, eds. Copyright © 1973 by The McGraw-Hill Companies, Inc.

Figure A. 2 Reprinted, with permission, from Chemical Engineers' Handbook, 5th edn., R. H. Perry and C. H. Chilton, eds. Copyright © 1973 by The McGraw-Hill Companies, Inc.

## HEAT CONDUCTION

Contents
1.1 Introduction ..... 2
1.2 Fourier's Law of Heat Conduction ..... 2
1.3 The Heat Conduction Equation ..... 6
1.4 Thermal Resistance ..... 15
1.5 The Conduction Shape Factor ..... 19
1.6 Unsteady-State Conduction ..... 24
1.7 Mechanisms of Heat Conduction ..... 31

### 1.1 Introduction

Heat conduction is one of the three basic modes of thermal energy transport (convection and radiation being the other two) and is involved in virtually all process heat-transfer operations. In commercial heat exchange equipment, for example, heat is conducted through a solid wall (often a tube wall) that separates two fluids having different temperatures. Furthermore, the concept of thermal resistance, which follows from the fundamental equations of heat conduction, is widely used in the analysis of problems arising in the design and operation of industrial equipment. In addition, many routine process engineering problems can be solved with acceptable accuracy using simple solutions of the heat conduction equation for rectangular, cylindrical, and spherical geometries.

This chapter provides an introduction to the macroscopic theory of heat conduction and its engineering applications. The key concept of thermal resistance, used throughout the text, is developed here, and its utility in analyzing and solving problems of practical interest is illustrated.

### 1.2 Fourier's Law of Heat Conduction

The mathematical theory of heat conduction was developed early in the nineteenth century by Joseph Fourier [1]. The theory was based on the results of experiments similar to that illustrated in Figure 1.1 in which one side of a rectangular solid is held at temperature $T_{1}$, while the opposite side is held at a lower temperature, $T_{2}$. The other four sides are insulated so that heat can flow only in the $x$-direction. For a given material, it is found that the rate, $q_{x}$, at which heat (thermal energy) is transferred from the hot side to the cold side is proportional to the cross-sectional area, $A$, across which the heat flows; the temperature difference, $T_{1}-T_{2}$; and inversely proportional to the thickness, $B$, of the material. That is:

$$
q_{x} \propto \frac{A\left(T_{1}-T_{2}\right)}{B}
$$

Writing this relationship as an equality, we have:

$$
\begin{equation*}
q_{x}=\frac{k A\left(T_{1}-T_{2}\right)}{B} \tag{1.1}
\end{equation*}
$$



Figure 1.1 One-dimensional heat conduction in a solid.

The constant of proportionality, $k$, is called the thermal conductivity. Equation (1.1) is also applicable to heat conduction in liquids and gases. However, when temperature differences exist in fluids, convection currents tend to be set up, so that heat is generally not transferred solely by the mechanism of conduction.
The thermal conductivity is a property of the material and, as such, it is not really a constant, but rather it depends on the thermodynamic state of the material, i.e., on the temperature and pressure of the material. However, for solids, liquids, and low-pressure gases, the pressure dependence is usually negligible. The temperature dependence also tends to be fairly weak, so that it is often acceptable to treat $k$ as a constant, particularly if the temperature difference is moderate. When the temperature dependence must be taken into account, a linear function is often adequate, particularly for solids. In this case,

$$
\begin{equation*}
k=a+b T \tag{1.2}
\end{equation*}
$$

where $a$ and $b$ are constants.
Thermal conductivities of a number of materials are given in Appendices 1.A-1.E. Many other values may be found in various handbooks and compendiums of physical property data. Process simulation software is also an excellent source of physical property data. Methods for estimating thermal conductivities of fluids when data are unavailable can be found in the authoritative book by Poling et al. [2].
The form of Fourier's law given by Equation (1.1) is valid only when the thermal conductivity can be assumed constant. A more general result can be obtained by writing the equation for an element of differential thickness. Thus, let the thickness be $\Delta x$ and let $\Delta T=T_{2}-T_{1}$. Substituting in Equation (1.1) gives:

$$
\begin{equation*}
q_{x}=-k A \frac{\Delta T}{\Delta x} \tag{1.3}
\end{equation*}
$$

Now in the limit as $\Delta x$ approaches zero,

$$
\frac{\Delta T}{\Delta x} \rightarrow \frac{d T}{d x}
$$

and Equation (1.3) becomes:

$$
\begin{equation*}
q_{x}=-k A \frac{d T}{d x} \tag{1.4}
\end{equation*}
$$

Equation (1.4) is not subject to the restriction of constant $k$. Furthermore, when $k$ is constant, it can be integrated to yield Equation (1.1). Hence, Equation (1.4) is the general one-dimensional form of Fourier's law. The negative sign is necessary because heat flows in the positive $x$-direction when the temperature decreases in the $x$-direction. Thus, according to the standard sign convention that $q_{x}$ is positive when the heat flow is in the positive $x$-direction, $q_{x}$ must be positive when $d T / d x$ is negative.
It is often convenient to divide Equation (1.4) by the area to give:

$$
\begin{equation*}
\hat{q}_{x} \equiv q_{x} / A=-k \frac{d T}{d x} \tag{1.5}
\end{equation*}
$$

where $\hat{q}_{x}$ is the heat flux. It has units of $\mathrm{J} / \mathrm{s} \cdot \mathrm{m}^{2}=\mathrm{W} / \mathrm{m}^{2}$ or $\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$. Thus, the units of $k$ are $\mathrm{W} / \mathrm{m} \cdot \mathrm{K}$ or $\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$.
Equations (1.1), (1.4), and (1.5) are restricted to the situation in which heat flows in the $x$-direction only. In the general case in which heat flows in all three coordinate directions, the total heat flux is
obtained by adding vectorially the fluxes in the coordinate directions. Thus,

$$
\begin{equation*}
\overrightarrow{\hat{q}}=\hat{q}_{x} \vec{i}+\hat{q}_{y} \vec{j}+\hat{q}_{z} \vec{k} \tag{1.6}
\end{equation*}
$$

where $\overrightarrow{\hat{q}}$ is the heat flux vector and $\vec{i}, \vec{j}, \vec{k}$ are unit vectors in the $x$-, $y$-, $z$-directions, respectively. Each of the component fluxes is given by a one-dimensional Fourier expression as follows:

$$
\begin{equation*}
\hat{q}_{x}=-k \frac{\partial T}{\partial x} \quad \hat{q}_{y}=-k \frac{\partial T}{\partial y} \quad \hat{q}_{z}=-k \frac{\partial T}{\partial z} \tag{1.7}
\end{equation*}
$$

Partial derivatives are used here since the temperature now varies in all three directions. Substituting the above expressions for the fluxes into Equation (1.6) gives:

$$
\begin{equation*}
\overrightarrow{\hat{q}}=-k\left(\frac{\partial T}{\partial x} \vec{i}+\frac{\partial T}{\partial y} \vec{j}+\frac{\partial T}{\partial z} \vec{k}\right) \tag{1.8}
\end{equation*}
$$

The vector in parenthesis is the temperature gradient vector, and is denoted by $\vec{\nabla} T$. Hence,

$$
\begin{equation*}
\overrightarrow{\hat{q}}=-k \vec{\nabla} T \tag{1.9}
\end{equation*}
$$

Equation (1.9) is the three-dimensional form of Fourier's law. It is valid for homogeneous, isotropic materials for which the thermal conductivity is the same in all directions.

Equation (1.9) states that the heat flux vector is proportional to the negative of the temperature gradient vector. Since the gradient direction is the direction of greatest temperature increase, the negative gradient direction is the direction of greatest temperature decrease. Hence, Fourier's law states that heat flows in the direction of greatest temperature decrease.

## Example 1.1

The block of 304 stainless steel shown below is well insulated on the front and back surfaces, and the temperature in the block varies linearly in both the $x$ - and $y$-directions, find:
(a) The heat fluxes and heat flows in the $x$ - and $y$-directions.
(b) The magnitude and direction of the heat flux vector.


## Solution

(a) From Table A.1, the thermal conductivity of 304 stainless steel is $14.4 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$. The crosssectional areas are:

$$
\begin{aligned}
& A_{x}=10 \times 5=50 \mathrm{~cm}^{2}=0.0050 \mathrm{~m}^{2} \\
& A_{y}=5 \times 5=25 \mathrm{~cm}^{2}=0.0025 \mathrm{~m}^{2}
\end{aligned}
$$

Using Equation (1.7) and replacing the partial derivatives with finite differences (since the temperature variation is linear), the heat fluxes are:

$$
\begin{aligned}
& \hat{q}_{x}=-k \frac{\partial T}{\partial x}=-k \frac{\Delta T}{\Delta x}=-14.4\left(\frac{-5}{0.05}\right)=1440 \mathrm{~W} / \mathrm{m}^{2} \\
& \hat{q}_{y}=-k \frac{\partial T}{\partial y}=-k \frac{\Delta T}{\Delta y}=-14.4\left(\frac{10}{0.1}\right)=-1440 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

The heat flows are obtained by multiplying the fluxes by the corresponding cross-sectional areas:

$$
\begin{aligned}
& q_{x}=\hat{q}_{x} A_{x}=1440 \times 0.005=7.2 \mathrm{~W} \\
& q_{y}=\hat{q}_{y} A_{y}=-1440 \times 0.0025=-3.6 \mathrm{~W}
\end{aligned}
$$

(b) From Equation (1.6):

$$
\begin{aligned}
& \overrightarrow{\hat{q}}=\hat{q}_{x} \vec{i}+\hat{q}_{y} \vec{j} \\
& \overrightarrow{\hat{q}}=1440 \vec{i}-1440 \vec{j} \\
& \mid \overrightarrow{\hat{q}}_{\mid}=\left[(1440)^{2}+(-1440)^{2}\right]^{0.5}=2036.5 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

The angle, $\theta$, between the heat flux vector and the $x$-axis is calculated as follows:

$$
\begin{aligned}
\tan \theta & =\hat{q}_{y} / \hat{q}_{x}=-1440 / 1440=-1.0 \\
\theta & =-45^{\circ}
\end{aligned}
$$

The direction of the heat flux vector, which is the direction in which heat flows, is indicated in the sketch below.


### 1.3 The Heat Conduction Equation

The solution of problems involving heat conduction in solids can, in principle, be reduced to the solution of a single differential equation, the heat conduction equation. The equation can be derived by making a thermal energy balance on a differential volume element in the solid. For the case of conduction only in the $x$-direction, such a volume element is illustrated in Figure 1.2. The balance equation for the volume element is:

$$
\begin{align*}
& \text { \{rate of thermal energy in }\}-\{\text { rate of thermal energy out }\}+\{\text { net rate of thermal } \\
& \text { energy generation }\}=\{\text { rate of accumulation of thermal energy }\} \tag{1.10}
\end{align*}
$$

The generation term appears in the equation because the balance is made on thermal energy, not total energy. For example, thermal energy may be generated within a solid by an electric current or by decay of a radioactive material.

The rate at which thermal energy enters the volume element across the face at $x$ is given by the product of the heat flux and the cross-sectional area, $\hat{q}_{x}{ }_{x} A$. Similarly, the rate at which thermal energy leaves the element across the face at $x+\Delta x$ is $\left.\hat{q}_{x}\right|_{x+\Delta x} A$. For a homogeneous heat source


Figure 1.2 Differential volume element used in derivation of conduction equation.
of strength $\dot{q}$ per unit volume, the net rate of generation is $\dot{q} A \Delta x$. Finally, the rate of accumulation is given by the time derivative of the thermal energy content of the volume element, which is $\rho c\left(T-T_{r e f}\right) A \Delta x$, where $T_{r e f}$ is an arbitrary reference temperature. Thus, the balance equation becomes:

$$
\left(\left.\hat{q}_{x}\right|_{x}-\left.\hat{q}_{x}\right|_{x+\Delta x}\right) A+\dot{q} A \Delta x=\rho c \frac{\partial T}{\partial t} A \Delta x
$$

It has been assumed here that the density, $\rho$, and heat capacity, $c$, are constant. Dividing by $A \Delta x$ and taking the limit as $\Delta x \rightarrow 0$ yields:

$$
\rho c \frac{\partial T}{\partial t}=-\frac{\partial \hat{q}_{x}}{\partial x}+\dot{q}
$$

Using Fourier's law as given by Equation (1.5), the balance equation becomes:

$$
\rho c \frac{\partial T}{\partial t}=\frac{\partial}{\partial x}\left(\frac{k \partial T}{\partial x}\right)+\dot{q}
$$

When conduction occurs in all three coordinate directions, the balance equation contains $y$ - and $z$-derivatives analogous to the $x$-derivative. The balance equation then becomes:

$$
\begin{equation*}
\rho c \frac{\partial T}{\partial t}=\frac{\partial}{\partial x}\left(\frac{k \partial T}{\partial x}\right)+\frac{\partial}{\partial y}\left(\frac{k \partial T}{\partial y}\right)+\frac{\partial}{\partial z}\left(\frac{k \partial T}{\partial z}\right)+\dot{q} \tag{1.11}
\end{equation*}
$$

Equation (1.11) is listed in Table 1.1 along with the corresponding forms that the equation takes in cylindrical and spherical coordinates. Also listed in Table 1.1 are the components of the heat flux vector in the three coordinate systems.

When $k$ is constant, it can be taken outside the derivatives and Equation (1.11) can be written as:

$$
\begin{equation*}
\frac{\rho c}{k} \frac{\partial T}{\partial t}=\frac{\partial^{2} T}{\partial x^{2}}+\frac{\partial^{2} T}{\partial y^{2}}+\frac{\partial^{2} T}{\partial z^{2}}+\frac{\dot{q}}{k} \tag{1.12}
\end{equation*}
$$

or

$$
\begin{equation*}
\frac{1}{\alpha} \frac{\partial T}{\partial t}=\nabla^{2} T+\frac{\dot{q}}{k} \tag{1.13}
\end{equation*}
$$

where $\alpha \equiv k / \rho c$ is the thermal diffusivity and $\nabla^{2}$ is the Laplacian operator. The thermal diffusivity has units of $\mathrm{m}^{2} / \mathrm{s}$ or $\mathrm{ft}^{2} / \mathrm{h}$.

## Table 1.1 The Heat Conduction Equation

A. Cartesian coordinates

$$
\rho c \frac{\partial T}{\partial t}=\frac{\partial}{\partial x}\left(k \frac{\partial T}{\partial x}\right)+\frac{\partial}{\partial y}\left(k \frac{\partial T}{\partial y}\right)+\frac{\partial}{\partial z}\left(k \frac{\partial T}{\partial z}\right)+\dot{q}
$$

The components of the heat flux vector, $\overrightarrow{\hat{q}}$, are:

$$
\hat{q}_{x}=-k \frac{\partial T}{\partial x} \quad \hat{q}_{y}=-k \frac{\partial T}{\partial y} \quad \hat{q}_{z}=-k \frac{\partial T}{\partial z}
$$

B. Cylindrical coordinates ( $\mathrm{r}, \phi, \mathrm{z}$ )


$$
\rho c \frac{\partial T}{\partial t}=\frac{1}{r} \frac{\partial}{\partial r}\left(k r \frac{\partial T}{\partial r}\right)+\frac{1}{r^{2}} \frac{\partial}{\partial \phi}\left(k \frac{\partial T}{\partial \phi}\right)+\frac{\partial}{\partial z}\left(k \frac{\partial T}{\partial z}\right)+\dot{q}
$$

The components of $\overrightarrow{\hat{q}}$ are:

$$
\hat{q}_{r}=-k \frac{\partial T}{\partial r} ; \quad \hat{q}_{\phi}=\frac{-k}{r} \frac{\partial T}{\partial \phi} ; \quad \hat{q}_{z}=-k \frac{\partial T}{\partial z}
$$

C. Spherical coordinates (r, $\theta, \phi$ )


$$
\begin{aligned}
\rho c \frac{\partial T}{\partial t}= & \frac{1}{r^{2}} \frac{\partial}{\partial r}\left(k r^{2} \frac{\partial T}{\partial r}\right)+\frac{1}{r^{2} \sin \theta} \frac{\partial}{\partial \theta}\left(k \sin \theta \frac{\partial T}{\partial \theta}\right) \\
& +\frac{1}{r^{2} \sin ^{2} \theta} \frac{\partial}{\partial \phi}\left(k \frac{\partial T}{\partial \phi}\right)+\dot{q}
\end{aligned}
$$

The components of $\overrightarrow{\hat{q}}$ are:

$$
\hat{q}_{r}=-k \frac{\partial T}{\partial r} ; \quad \hat{q}_{\theta}=-\frac{k}{r} \frac{\partial T}{\partial \theta} ; \quad \hat{q}_{\phi}=-\frac{k}{r \sin \theta} \frac{\partial T}{\partial \phi}
$$

The use of the conduction equation is illustrated in the following examples.

## Example 1.2

Apply the conduction equation to the situation illustrated in Figure 1.1.

## Solution

In order to make the mathematics conform to the physical situation, the following conditions are imposed:
(1) Conduction only in $x$-direction $\Rightarrow T=\mathrm{T}(\mathrm{x})$, so $\frac{\partial T}{\partial y}=\frac{\partial T}{\partial z}=0$
(2) No heat source $\Rightarrow \dot{q}=0$
(3) Steady state $\Rightarrow \frac{\partial T}{\partial t}=0$
(4) Constant $k$

The conduction equation in Cartesian coordinates then becomes:

$$
0=k \frac{\partial^{2} T}{\partial x^{2}} \quad \text { or } \quad \frac{d^{2} T}{d x^{2}}=0
$$

(The partial derivative is replaced by a total derivative because $x$ is the only independent variable in the equation.) Integrating on both sides of the equation gives:

$$
\frac{d T}{d x}=C_{1}
$$

A second integration gives:

$$
T=C_{1} x+C_{2}
$$

Thus, it is seen that the temperature varies linearly across the solid. The constants of integration can be found by applying the boundary conditions:
(1) At $x=0 \quad T=T_{1}$
(2) At $x=B \quad T=T_{2}$

The first boundary condition gives $T_{1}=C_{2}$ and the second then gives:

$$
T_{2}=C_{1} B+T_{1}
$$

Solving for $C_{1}$ we find:

$$
C_{1}=\frac{T_{2}-T_{1}}{B}
$$

The heat flux is obtained from Fourier's law:

$$
\hat{q}_{x}=-k \frac{d T}{d x}=-k C_{1}=-k \frac{\left(T_{2}-T_{1}\right)}{B}=k \frac{\left(T_{1}-T_{2}\right)}{B}
$$

Multiplying by the area gives the heat flow:

$$
q_{x}=\hat{q}_{x} A=\frac{k A\left(T_{1}-T_{2}\right)}{B}
$$

Since this is the same as Equation (1.1), we conclude that the mathematics are consistent with the experimental results.

## Example 1.3

Apply the conduction equation to the situation illustrated in Figure 1.1, but let $k=a+b T$, where $a$ and $b$ are constants.

## Solution

Conditions 1-3 of the previous example are imposed. The conduction equation then becomes:

$$
0=\frac{d}{d x}\left(k \frac{d T}{d x}\right)
$$

Integrating once gives:

$$
k \frac{d T}{d x}=C_{1}
$$

The variables can now be separated and a second integration performed. Substituting for $k$, we have:

$$
\begin{gathered}
(a+b T) d T=C_{1} d x \\
a T+\frac{b T^{2}}{2}=C_{1} x+C_{2}
\end{gathered}
$$

It is seen that in this case of variable $k$, the temperature profile is not linear across the solid.
The constants of integration can be evaluated by applying the same boundary conditions as in the previous example, although the algebra is a little more tedious. The results are:

$$
\begin{gathered}
C_{2}=a T_{1}+\frac{b T_{1}^{2}}{2} \\
C_{1}=a \frac{\left(T_{2}-T_{1}\right)}{B}+\frac{b}{2 B}\left(T_{2}^{2}-T_{1}^{2}\right)
\end{gathered}
$$

As before, the heat flow is found using Fourier's law:

$$
\begin{aligned}
q_{x} & =-k A \frac{d T}{d x}=-A C_{1} \\
q_{x} & =\frac{A}{B}\left[a\left(T_{1}-T_{2}\right)+\frac{b}{2}\left(T_{1}^{2}-T_{2}^{2}\right)\right]
\end{aligned}
$$

This equation is seldom used in practice. Instead, when $k$ cannot be assumed constant, Equation (1.1) is used with an average value of $k$. Thus, taking the arithmetic average of the conductivities at the two sides of the block:

$$
\begin{aligned}
k_{\text {ave }} & =\frac{k\left(T_{1}\right)+k\left(T_{2}\right)}{2} \\
& =\frac{\left(a+b T_{1}\right)+\left(a+b T_{2}\right)}{2} \\
k_{\text {ave }} & =a+\frac{b}{2}\left(T_{1}+T_{2}\right)
\end{aligned}
$$

Using this value of $k$ in Equation (1.1) yields:

$$
\begin{aligned}
q_{x} & =\frac{k_{\text {ave }} A\left(T_{1}-T_{2}\right)}{B} \\
& =\left[a+\frac{b\left(T_{1}+T_{2}\right)}{2}\right] \frac{A}{B}\left(T_{1}-T_{2}\right) \\
q_{x} & =\frac{A}{B}\left[a\left(T_{1}-T_{2}\right)+\frac{b}{2}\left(T_{1}^{2}-T_{2}^{2}\right)\right]
\end{aligned}
$$

This equation is exactly the same as the one obtained above by solving the conduction equation. Hence, using Equation (1.1) with an average value of $k$ gives the correct result. This is a consequence of the assumed linear relationship between $k$ and $T$.

## Example 1.4

Use the conduction equation to find an expression for the rate of heat transfer for the cylindrical analog of the situation depicted in Figure 1.1.

## Solution



As shown in the sketch, the solid is in the form of a hollow cylinder and the outer and inner surfaces are maintained at temperatures $T_{1}$ and $T_{2}$, respectively. The ends of the cylinder are insulated so that heat can flow only in the radial direction. There is no heat flow in the angular ( $\phi$ ) direction because the temperature is the same all the way around the circumference of the cylinder. The following conditions apply:
(1) No heat flow in $z$-direction $\Rightarrow \frac{\partial T}{\partial z}=0$
(2) Uniform temperature in $\phi$-direction $\Rightarrow \frac{\partial T}{\partial \phi}=0$
(3) No heat generation $\Rightarrow \dot{q}=0$
(4) Steady state $\Rightarrow \frac{\partial T}{\partial t}=0$
(5) Constant $k$

With these conditions, the conduction equation in cylindrical coordinates becomes:

$$
\frac{1}{r} \frac{\partial}{\partial r}\left(k r \frac{\partial T}{\partial r}\right)=0
$$

or

$$
\frac{d}{d r}\left(r \frac{d T}{d r}\right)=0
$$

Integrating once gives:

$$
r \frac{d T}{d r}=C_{1}
$$

Separating variables and integrating again gives:

$$
T=C_{1} \ln r+C_{2}
$$

It is seen that, even with constant $k$, the temperature profile in curvilinear systems is nonlinear.
The boundary conditions for this case are:
(1) At $r=R_{1} \quad T=T_{1} \Rightarrow T_{1}=C_{1} \ln R_{1}+C_{2}$
(2) At $r=R_{2} \quad T=T_{2} \Rightarrow T_{2}=C_{1} \ln R_{2}+C_{2}$

Solving for $C_{1}$ by subtracting the second equation from the first gives:

$$
C_{1}=\frac{T_{1}-T_{2}}{\ln R_{1}-\ln R_{2}}=-\frac{T_{1}-T_{2}}{\ln \left(R_{2} / R_{1}\right)}
$$

From Table 1.1, the appropriate form of Fourier's law is:

$$
\hat{q}_{r}=-k \frac{d T}{d r}=-k \frac{C_{1}}{r}=\frac{k\left(T_{1}-T_{2}\right)}{r \ln \left(R_{2} / R_{1}\right)}
$$

The area across which the heat flows is:

$$
A_{r}=2 \pi r L
$$

where $L$ is the length of the cylinder. Thus,

$$
q_{r}=\hat{q}_{r} A_{r}=\frac{2 \pi k L\left(T_{1}-T_{2}\right)}{\ln \left(R_{2} / R_{1}\right)}
$$

Notice that the heat-transfer rate is independent of radial position. The heat flux, however, depends on $r$ because the cross-sectional area changes with radial position.

## Example 1.5

The block shown in the diagram below is insulated on the top, bottom, front, back, and the side at $x=\mathrm{B}$. The side at $x=0$ is maintained at a fixed temperature, $T_{1}$. Heat is generated within the block at a rate per unit volume given by:

$$
\dot{q}=\Gamma e^{-\gamma x}
$$

where $\Gamma, \gamma>0$ are constants. Find the maximum steady-state temperature in the block. Data are as follows:

$$
\begin{array}{lll}
\Gamma & =10 \mathrm{~W} / \mathrm{m}^{3} & B=1.0 \mathrm{~m} \\
\gamma=0.1 \mathrm{~m}^{-1} & T_{1}=20^{\circ} \mathrm{C} &
\end{array}
$$



## Solution

The first step is to find the temperature profile in the block by solving the heat conduction equation. The applicable conditions are:

- Steady state
- Conduction only in $x$-direction
- Constant thermal conductivity

The appropriate form of the heat conduction equation is then:

$$
\begin{aligned}
& \frac{d(k d T / d x)}{d x}+\dot{q}=0 \\
& k \frac{d^{2} T}{d x^{2}}+\Gamma e^{-\gamma x}=0 \\
& \frac{d^{2} T}{d x^{2}}=-\frac{\Gamma e^{-\gamma x}}{k}
\end{aligned}
$$

Integrating once gives:

$$
\frac{d T}{d x}=\frac{\Gamma e^{-\gamma x}}{k \gamma}+C_{1}
$$

A second integration yields:

$$
T=-\frac{\Gamma e^{-\gamma x}}{k \gamma^{2}}+C_{1} x+C_{2}
$$

The boundary conditions are:
(1) At $x=0 \quad T=T_{1}$
(2) At $x=\mathrm{B} \frac{d T}{d x}=0$

The second boundary condition results from assuming zero heat flow through the insulated boundary (perfect insulation). Thus, at $x=L$ :

$$
q_{x}=-k A \frac{d T}{d x}=0 \quad \Rightarrow \quad \frac{d T}{d x}=0
$$

This condition is applied using the equation for $d T / d x$ resulting from the first integration:

$$
0=\frac{\Gamma e^{-\gamma B}}{k \gamma}+C_{1}
$$

Hence,

$$
C_{1}=-\frac{\Gamma e^{-\gamma B}}{k \gamma}
$$

Applying the first boundary condition to the equation for $T$ :

$$
T_{1}=-\frac{\Gamma e^{(0)}}{k \gamma^{2}}+C_{1}(0)+C_{2}
$$

Hence,

$$
C_{2}=T_{1}+\frac{\Gamma}{k \gamma^{2}}
$$

With the above values for $C_{1}$ and $C_{2}$, the temperature profile becomes:

$$
T=T_{1}+\frac{\Gamma}{k \gamma^{2}}\left(1-e^{-\gamma x}\right)-\frac{\Gamma e^{-\gamma B}}{k \gamma} x
$$

Now at steady state, all the heat generated in the block must flow out through the un-insulated side at $x=0$. Hence, the maximum temperature must occur at the insulated boundary, i.e., at $x=B$. (This intuitive result can be confirmed by setting the first derivative of $T$ equal to zero and solving for $x$.) Thus, setting $x=B$ in the last equation gives:

$$
T_{\max }=T_{1}+\frac{\Gamma}{k \gamma^{2}}\left(1-e^{-\gamma B}\right)-\frac{\Gamma B L e^{-\gamma B}}{k \gamma}
$$

Finally, the solution is obtained by substituting the numerical values of the parameters:

$$
\begin{aligned}
& T_{\max }=20+\frac{10}{0.5(0.1)^{2}}\left(1-e^{-0.1}\right)-\frac{10 \times 1.0 e^{-0.1}}{0.5 \times 0.1} \\
& T_{\max } \cong 29.4^{\circ} \mathrm{C}
\end{aligned}
$$

The procedure illustrated in the above examples can be summarized as follows:
(1) Write down the conduction equation in the appropriate coordinate system.
(2) Impose any restrictions dictated by the physical situation to eliminate terms that are zero or negligible.
(3) Integrate the resulting differential equation to obtain the temperature profile.
(4) Use the boundary conditions to evaluate the constants of integration.
(5) Use the appropriate form of Fourier's law to obtain the heat flux.
(6) Multiply the heat flux by the cross-sectional area to obtain the rate of heat transfer.

In each of the above examples there is only one independent variable so that an ordinary differential equation results. In unsteady-state problems and problems in which heat flows in more than one direction, a partial differential equation must be solved. Analytical solutions are often possible if the geometry is sufficiently simple. Otherwise, numerical solutions are obtained with the aid of a computer.

### 1.4 Thermal Resistance

The concept of thermal resistance is based on the observation that many diverse physical phenomena can be described by a general rate equation that may be stated as follows:

$$
\begin{equation*}
\text { Flow rate }=\frac{\text { Driving force }}{\text { Resistance }} \tag{1.14}
\end{equation*}
$$

Ohm's Law of Electricity is one example:

$$
\begin{equation*}
I=\frac{E}{R} \tag{1.15}
\end{equation*}
$$

In this case, the quantity that flows is electric charge, the driving force is the electrical potential difference, $E$, and the resistance is the electrical resistance, $R$, of the conductor.
In the case of heat transfer, the quantity that flows is heat (thermal energy) and the driving force is the temperature difference. The resistance to heat transfer is termed the thermal resistance, and is denoted by $R_{t h}$. Thus, the general rate equation may be written as:

$$
\begin{equation*}
q=\frac{\Delta T}{R_{t h}} \tag{1.16}
\end{equation*}
$$

In this equation, all quantities take on positive values only, so that $q$ and $\Delta T$ represent the absolute values of the heat-transfer rate and temperature difference, respectively.
An expression for the thermal resistance in a rectangular system can be obtained by comparing Equations (1.1) and (1.16):

$$
\begin{gather*}
q_{x}=\frac{k A\left(T_{1}-T_{2}\right)}{B}=\frac{\Delta T}{R_{t h}}=\frac{T_{1}-T_{2}}{R_{t h}}  \tag{1.17}\\
R_{t h}=\frac{B}{k A} \tag{1.18}
\end{gather*}
$$

Similarly, using the equation derived in Example 1.4 for a cylindrical system gives:

$$
\begin{equation*}
q_{r}=\frac{2 \pi k L\left(T_{1}-T_{2}\right)}{\ln \left(R_{2} / R_{1}\right)}=\frac{T_{1}-T_{2}}{R_{t h}} \tag{1.19}
\end{equation*}
$$

Table 1.2 Expressions for Thermal Resistance

| Configuration | $R_{t h}$ |
| :--- | :--- |
| Conduction, Cartesian <br> coordinates | $B / k A$ |
| Conduction, radial direction, <br> cylindrical coordinates | $\frac{\ln \left(R_{2} / R_{1}\right)}{2 \pi k L}$ |
| Conduction, radial direction, <br> spherical coordinates | $\frac{R_{2}-R_{1}}{4 \pi k R_{1} R_{2}}$ |
| Conduction, shape factor <br> Convection, un-finned surface | $1 / k S$ |
| Convection, finned surface | $1 / h A$ |
| $S=$ shape factor | $\frac{1}{h \eta_{w} A}$ |
| $h=$ heat-transfer coefficient |  |
| $\eta_{w}=$ weighted efficiency of finned surface $=\frac{A_{p}+\eta_{f} A_{f}}{A_{p}+A_{f}}$ |  |
| $A_{p}=$ prime surface area |  |
| $A_{f}=$ fin surface area |  |
| $\eta_{f}=$ fin efficiency |  |

$$
\begin{equation*}
R_{t h}=\frac{\ln \left(R_{2} / R_{1}\right)}{2 \pi k L} \tag{1.20}
\end{equation*}
$$

These results, along with a number of others that will be considered subsequently, are summarized in Table 1.2. When $k$ cannot be assumed constant, the average thermal conductivity, as defined in the previous section, should be used in the expressions for thermal resistance.

The thermal resistance concept permits some relatively complex heat-transfer problems to be solved in a very simple manner. The reason is that thermal resistances can be combined in the same way as electrical resistances. Thus, for resistances in series, the total resistance is the sum of the individual resistances:

$$
\begin{equation*}
R_{T o t}=\sum_{i} R_{i} \tag{1.21}
\end{equation*}
$$

Likewise, for resistances in parallel:

$$
\begin{equation*}
R_{T o t}=\left(\sum_{i} 1 / R_{i}\right)^{-1} \tag{1.22}
\end{equation*}
$$

Thus, for the composite solid shown in Figure 1.3, the thermal resistance is given by:

$$
\begin{equation*}
R_{t h}=R_{A}+R_{B C}+R_{D} \tag{1.23}
\end{equation*}
$$

where $R_{B C}$, the resistance of materials $B$ and $C$ in parallel, is:

$$
\begin{equation*}
R_{B C}=\left(1 / R_{B}+1 / R_{C}\right)^{-1}=\frac{R_{B} R_{C}}{R_{B}+R_{C}} \tag{1.24}
\end{equation*}
$$



Figure 1.3 Heat transfer through a composite material.

In general, when thermal resistances occur in parallel, heat will flow in more than one direction. In Figure 1.3, for example, heat will tend to flow between materials $B$ and $C$, and this flow will be normal to the primary direction of heat transfer. In this case, the one-dimensional calculation of $q$ using Equations (1.16) and (1.22) represents an approximation, albeit one that is generally quite acceptable for process engineering purposes.

## Example 1.6

A 5-cm (2-in.) schedule 40 steel pipe carries a heat-transfer fluid and is covered with a $2-\mathrm{cm}$ layer of calcium silicate insulation ( $k=0.06 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ) to reduce the heat loss. The inside and outside pipe diameters are 5.25 cm and 6.03 cm , respectively. If the inner pipe surface is at $150^{\circ} \mathrm{C}$ and the exterior surface of the insulation is at $25^{\circ} \mathrm{C}$, calculate:
(a) The rate of heat loss per unit length of pipe.
(b) The temperature of the outer pipe surface.

## Solution


(a)

$$
\begin{aligned}
q_{r} & =\frac{\Delta T}{R_{\text {th }}}=\frac{150-25}{R_{\text {th }}} \\
R_{\text {th }} & =R_{\text {pipe }}+R_{\text {insulation }} \\
R_{\text {th }} & =\frac{\ln \left(R_{2} / R_{1}\right)}{2 \pi k_{\text {steel }} L}+\frac{\ln \left(R_{3} / R_{2}\right)}{2 \pi k_{\text {ins }} L}
\end{aligned}
$$

$$
\begin{aligned}
R_{1} & =5.25 / 2=2.625 \mathrm{~cm} \\
R_{2} & =6.03 / 2=3.015 \mathrm{~cm} \\
R_{3} & =3.015+2=5.015 \mathrm{~cm} \\
k_{\text {steel }} & =43 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K} \text { (Table A.1) } \\
k_{\text {ins }} & =0.06 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K} \text { (given) } \\
L & =1 \mathrm{~m} \\
R_{t h} & =\frac{\ln \left(\frac{3.015}{2.625}\right)}{2 \pi \times 43}+\frac{\ln \left(\frac{5.015}{3.015}\right)}{2 \pi \times 0.06}=0.000513+1.349723 \\
& =1.350236 \mathrm{~K} / \mathrm{W} \\
q_{r} & =\frac{125}{1.350236} \cong 92.6 \mathrm{~W} / \mathrm{m} \text { of pipe }
\end{aligned}
$$

(b) Writing Equation (1.16) for the pipe wall only:

$$
\begin{aligned}
q_{r} & =\frac{150-T_{0}}{R_{p i p e}} \\
92.6 & =\frac{150-T_{0}}{0.000513} \\
T_{0} & =150-0.0475 \cong 149.95^{\circ} \mathrm{C}
\end{aligned}
$$

Clearly, the resistance of the pipe wall is negligible compared with that of the insulation, and the temperature difference across the pipe wall is a correspondingly small fraction of the total temperature difference in the system.

It should be pointed out that the calculation in Example 1.6 tends to overestimate the rate of heat transfer because it assumes that the insulation is in perfect thermal contact with the pipe wall. Since solid surfaces are not perfectly smooth, there will generally be air gaps between two adjacent solid materials. Since air is a very poor conductor of heat, even a thin layer of air can result in a substantial thermal resistance. This additional resistance at the interface between two materials is called the contact resistance. Thus, the thermal resistance in Example 1.5 should really be written as:

$$
\begin{equation*}
R_{t h}=R_{\text {pipe }}+R_{\text {insulation }}+R_{\text {contact }} \tag{1.25}
\end{equation*}
$$

The effect of the additional resistance is to decrease the rate of heat transfer according to Equation (1.16). Since the contact resistance is difficult to determine, it is often neglected or a rough approximation is used. For example, a value equivalent to an additional 5 mm of material thickness is sometimes used for the contact resistance between two pieces of the same material [3]. A more rigorous method for estimating contact resistance can be found in Ref. [4].

A slightly modified form of the thermal resistance, the $R$-value, is commonly used for insulations and other building materials. The $R$-value is defined as:

$$
\begin{equation*}
R \text {-value }=\frac{B(\mathrm{ft})}{k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)} \tag{1.26}
\end{equation*}
$$

where $B$ is the thickness of the material and $k$ is its thermal conductivity. Comparison with Equation (1.18) shows that the $R$-value is the thermal resistance, in English units, of a slab of material having a cross-sectional area of $1 \mathrm{ft}^{2}$. Since the $R$-value is always given for a specified thickness, the thermal conductivity of a material can be obtained from its $R$-value using Equation (1.26). Also, since $R$-values are essentially thermal resistances, they are additive for materials arranged in series.

## Example 1.7

Triple-glazed windows like the one shown in the sketch below are often used in very cold climates. Calculate the $R$-value for the window shown. The thermal conductivity of air at normal room temperature is approximately $0.015 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$.


Triple-pane window

## Solution

From Table A.3, the thermal conductivity of window glass is $0.78 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$. Converting to English units gives:

$$
k_{\text {glass }}=0.78 \times 0.57782=0.45 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}
$$

The $R$-values for one pane of glass and one air gap are calculated from Equation (1.26):

$$
\begin{gathered}
R_{\text {glass }}=\frac{0.08 / 12}{0.45} \cong 0.0148 \\
R_{\text {air }}=\frac{0.25 / 12}{0.015} \cong 1.3889
\end{gathered}
$$

The $R$-value for the window is obtained using the additive property for materials in series:

$$
\begin{aligned}
R \text {-value } & =3 R_{\text {glass }}+2 R_{\text {air }} \\
& =3 \times 0.0148+2 \times 1.3889 \\
R \text {-value } & \cong 2.8
\end{aligned}
$$

### 1.5 The Conduction Shape Factor

The conduction shape factor is a device whereby analytical solutions to multi-dimensional heat conduction problems are cast into the form of one-dimensional solutions. Although quite restricted

Table 1.3 Conduction Shape Factors (Source: Ref. [5])

## Case 1

Isothermal sphere buried in a semi-infinite medium


$$
z>D / 2 \quad S=\frac{2 \pi D}{1-D / 4 z}
$$

## Case 2

Horizontal isothermal cylinder of length $L$ buried in a semi-infinite medium

$L \gg D$
$S=\frac{2 \pi L}{\cosh ^{-1}(2 z / D)}$

Case 3
Vertical cylinder in a semi-infinite medium


$$
L \gg D \quad S=\frac{2 \pi L}{\ln (4 L / D)}
$$

## Case 4

Conduction between two cylinders of length $L$ in infinite medium

$L \gg D_{1}, D_{2}$
$S=\frac{2 \pi L}{\cosh ^{-1}\left(\frac{4 w^{2}-D_{1}^{2}-D_{2}^{2}}{2 D_{1} D_{1}}\right)}$

## Case 5

Horizontal circular cylinder of length $L$ midway between parallel planes of equal length and infinite width

$z \gg D / 2$

$$
S=\frac{2 \pi L}{\ln (8 z / \pi D)}
$$

## Case 6

Circular cylinder of length $L$ centered in a square solid of equal length

$w>D$
$L \gg w$
$S=\frac{2 \pi L}{\ln (1.08 w / D)}$

## Case 7

Eccentric circular cylinder of length $L$ in a cylinder of equal length


$$
S=\frac{2 \pi L}{\cosh ^{-1}\left(\frac{D^{2}+d^{2}-4 z^{2}}{2 D d}\right)}
$$

## Table 1.3 (Continued)

## Case 8

Conduction through the edge of adjoining walls


$$
D>L / 5 \quad S=0.54 D
$$

## Case 9

Conduction through corner of three walls with a temperature difference $\Delta T_{1}-T_{2}$ across the walls

$L \ll$ length and $\quad S=0.15 L$ width of wall

## Case 10

Disk of diameter $D$ and $T_{1}$ on a semi-finite medium of thermal conductivity $k$ and $T_{2}$


$$
S=2 D
$$

## Case 11

Square channel of length $L$


$$
\begin{aligned}
& \frac{W}{w}<1.4 \\
& \frac{W}{w}>1.4
\end{aligned}
$$

$$
S=\frac{2 \pi L}{0.785 \ln (W / w)}
$$

$$
S=\frac{2 \pi L}{0.930 \ln (W / w)-0.050}
$$

in scope, the shape factor method permits rapid and easy solution of multi-dimensional heattransfer problems when it is applicable. The conduction shape factor, $S$, is defined by the relation:

$$
\begin{equation*}
q=k S \Delta T \tag{1.27}
\end{equation*}
$$

where $\Delta T$ is a specified temperature difference. Notice that $S$ has the dimension of length. Shape factors for a number of geometrical configurations are given in Table 1.3. The solution of a problem involving one of these configurations is thus reduced to the calculation of $S$ by the appropriate formula listed in the table.

The thermal resistance corresponding to the shape factor can be found by comparing Equation (1.16) with Equation (1.27). The result is:

$$
\begin{equation*}
R_{t h}=1 / k S \tag{1.28}
\end{equation*}
$$

This is one of the thermal resistance formulas listed in Table 1.2. Since shape-factor problems are inherently multi-dimensional, however, use of the thermal resistance concept in such cases
will, in general, yield only approximate solutions. Nevertheless, these solutions are usually entirely adequate for process engineering calculations.

## Example 1.8

An underground pipeline transporting hot oil has an outside diameter of 1 ft and its centerline is 2 ft below the surface of the earth. If the pipe wall is at $200^{\circ} \mathrm{F}$ and the earth's surface is at $-50^{\circ} \mathrm{F}$, what is the rate of heat loss per foot of pipe? Assume $k_{\text {earth }}=0.5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$.

## Solution



From Table 1.3, the shape factor for a buried horizontal cylinder is:

$$
S=\frac{2 \pi L}{\cosh ^{-1}(2 z / D)}
$$

In this case, $z=2 \mathrm{ft}$ and $r=0.5 \mathrm{ft}$. Taking $L=1 \mathrm{ft}$ we have:

$$
\begin{aligned}
S & =\frac{2 \pi L}{\cosh ^{-1}(4)}=3.045 \mathrm{ft} \\
q & =k_{\text {earth }} S \Delta T \\
& =0.5 \times 3.045 \times[200-(-50)] \\
q & \cong 380 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \text { of pipe }
\end{aligned}
$$

Note: If necessary, the following mathematical identity can be used to evaluate $\cosh ^{-1}(x)$ :

$$
\cosh ^{-1}(x)=\ln \left(x+\sqrt{x^{2}-1}\right)
$$

## Example 1.9

Suppose the pipeline of the previous example is covered with 1 in . of magnesia insulation ( $k=0.07 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ). What is the rate of heat loss per foot of pipe?

## Solution



This problem can be solved by treating the earth and the insulation as two resistances in series. Thus,

$$
q=\frac{\Delta T}{R_{\text {th }}}=\frac{200-(-50)}{R_{\text {earth }}+R_{\text {insulation }}}
$$

The resistance of the earth is obtained by means of the shape factor for a buried horizontal cylinder. In this case, however, the diameter of the cylinder is the diameter of the exterior surface of the insulation. Thus,

$$
\begin{gathered}
z=2 \mathrm{ft}=24 \mathrm{in} \\
D=12+2=14 \mathrm{in} \\
2 z / D=\frac{48}{14}=3.4286
\end{gathered}
$$

Therefore,

$$
\begin{gathered}
S=\frac{2 \pi L}{\cosh ^{-1}(2 z / D)}=\frac{2 \pi \times 1}{\cosh ^{-1}(3.4286)}=3.3012 \mathrm{ft} \\
R_{\text {earth }}=\frac{1}{k_{\text {earth }} S}=\frac{1}{0.5 \times 3.3012}=0.6058 \mathrm{~h} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
\end{gathered}
$$

Converting the thermal conductivity of the insulation to English units gives:

$$
k_{i n s}=0.07 \times 0.57782=0.0404 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}
$$

Hence,

$$
\begin{aligned}
R_{\text {insulation }} & =\ln \frac{\left(R_{2} / R_{1}\right)}{2 \pi k_{\text {ins }} L}=\frac{\ln (7 / 6)}{2 \pi \times 0.0404 \times 1} \\
& =0.6073 \mathrm{~h} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
\end{aligned}
$$



Figure 1.4 Semi-infinite solid.
Then

$$
q=\frac{250}{0.6058+0.6073}=206 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \text { of pipe }
$$

### 1.6 Unsteady-State Conduction

The heat conduction problems considered thus far have all been steady state, i.e., time-independent, problems. In this section, solutions of a few unsteady-state problems are presented. Solutions to many other unsteady-state problems can be found in heat-transfer textbooks and monographs, e.g., Refs. [5-10].

We consider first the case of a semi-infinite solid illustrated in Figure 1.4. The rectangular solid occupies the region from $x=0$ to $x=\infty$. The solid is initially at a uniform temperature, $T_{0}$. At time $t=0$, the temperature of the surface at $x=0$ is changed to $T_{s}$ and held at that value. The temperature within the solid is assumed to be uniform in the $y$-and $z$-directions at all times, so that heat flows only in the $x$-direction. This condition can be achieved mathematically by allowing the solid to extend to infinity in the $\pm y$ - and $\pm z$-directions. If $T_{s}$ is greater that $T_{0}$, heat will begin to penetrate into the solid, so that the temperature at any point within the solid will gradually increase with time. That is, $T=T(x, t)$, and the problem is to determine the temperature as a function of position and time.

Assuming no internal heat generation and constant thermal conductivity, the conduction equation for this situation is:

$$
\begin{equation*}
\frac{1}{\alpha} \frac{\partial T}{\partial t}=\frac{\partial^{2} T}{\partial x^{2}} \tag{1.29}
\end{equation*}
$$

The boundary conditions are:
(1) At $t=0, \quad T=T_{0}$ for all $x \geq 0$
(2) At $x=0, \quad T=T_{s}$ for all $t>0$
(3) As $x \rightarrow \infty, \quad T \rightarrow T_{0}$ for all $t \geq 0$

The last condition follows because it takes an infinite time for heat to penetrate an infinite distance into the solid.

The solution of Equation (1.29) subject to these boundary conditions can be obtained by the method of combination of variables [11]. The result is:

$$
\begin{equation*}
\frac{T(x, t)-T_{s}}{T_{0}-T_{s}}=\operatorname{erf}\left(\frac{x}{2 \sqrt{\alpha t}}\right) \tag{1.30}
\end{equation*}
$$

The error function, erf, is defined by:

$$
\begin{equation*}
\operatorname{erf}\left(\frac{x}{2 \sqrt{\alpha t}}\right)=\frac{2}{\sqrt{\pi}} \int_{0}^{\frac{x}{2 \sqrt{\alpha t}}} e^{-z^{2}} d z \tag{1.31}
\end{equation*}
$$

This function, which occurs in many diverse applications in engineering and applied science, can be evaluated by numerical integration. Values are listed in Table 1.4.

Table 1.4 The Error Function

| $x$ | erf $x$ | $x$ | erf $x$ | $x$ | erf $x$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0.00 | 0.00000 | 0.76 | 0.71754 | 1.52 | 0.96841 |
| 0.02 | 0.02256 | 0.78 | 0.73001 | 1.54 | 0.97059 |
| 0.04 | 0.04511 | 0.80 | 0.74210 | 1.56 | 0.97263 |
| 0.06 | 0.06762 | 0.82 | 0.75381 | 1.58 | 0.97455 |
| 0.08 | 0.09008 | 0.84 | 0.76514 | 1.60 | 0.97635 |
| 0.10 | 0.11246 | 0.86 | 0.77610 | 1.62 | 0.97804 |
| 0.12 | 0.13476 | 0.88 | 0.78669 | 1.64 | 0.97962 |
| 0.14 | 0.15695 | 0.90 | 0.79691 | 1.66 | 0.98110 |
| 0.16 | 0.17901 | 0.92 | 0.80677 | 1.68 | 0.98249 |
| 0.18 | 0.20094 | 0.94 | 0.81627 | 1.70 | 0.98379 |
| 0.20 | 0.22470 | 0.96 | 0.82542 | 1.72 | 0.98500 |
| 0.22 | 0.24330 | 0.98 | 0.83423 | 1.74 | 0.98613 |
| 0.24 | 0.26570 | 1.00 | 0.84270 | 1.76 | 0.98719 |
| 0.26 | 0.28690 | 1.02 | 0.85084 | 1.78 | 0.98817 |
| 0.28 | 0.30788 | 1.04 | 0.85865 | 1.80 | 0.98909 |
| 0.30 | 0.32863 | 1.06 | 0.86614 | 1.82 | 0.98994 |
| 0.32 | 0.34913 | 1.08 | 0.87333 | 1.84 | 0.99074 |
| 0.34 | 0.36936 | 1.10 | 0.88020 | 1.86 | 0.99147 |
| 0.36 | 0.38933 | 1.12 | 0.88079 | 1.88 | 0.99216 |
| 0.38 | 0.40901 | 1.14 | 0.89308 | 1.90 | 0.99279 |
| 0.40 | 0.42839 | 1.16 | 0.89910 | 1.92 | 0.99338 |
| 0.42 | 0.44749 | 1.18 | 0.90484 | 1.94 | 0.99392 |
| 0.44 | 0.46622 | 1.20 | 0.91031 | 1.96 | 0.99443 |
| 0.46 | 0.48466 | 1.22 | 0.91553 | 1.98 | 0.99489 |
| 0.48 | 0.50275 | 1.24 | 0.92050 | 2.00 | 0.995322 |
| 0.50 | 0.52050 | 1.26 | 0.92524 | 2.10 | 0.997020 |
| 0.52 | 0.53790 | 1.28 | 0.92973 | 2.20 | 0.998137 |
| 0.54 | 0.55494 | 1.30 | 0.93401 | 2.30 | 0.998857 |
| 0.56 | 0.57162 | 1.32 | 0.93806 | 2.40 | 0.999311 |
| 0.58 | 0.58792 | 1.34 | 0.94191 | 2.50 | 0.999593 |
| 0.60 | 0.60386 | 1.36 | 0.94556 | 2.60 | 0.999764 |
| 0.62 | 0.61941 | 1.38 | 0.94902 | 2.70 | 0.999866 |
| 0.64 | 0.63459 | 1.40 | 0.95228 | 2.80 | 0.999925 |
| 0.66 | 0.64938 | 1.42 | 0.95538 | 2.90 | 0.999959 |
| 0.68 | 0.66278 | 1.44 | 0.95830 | 3.00 | 0.999978 |
| 0.70 | 0.67780 | 1.46 | 0.96105 | 3.20 | 0.999994 |
| 0.72 | 0.69143 | 1.48 | 0.96365 | 3.40 | 0.999998 |
| 0.74 | 0.70468 | 1.50 | 0.96610 | 3.60 | 1.000000 |
|  |  |  |  |  |  |

The heat flux is given by:

$$
\begin{equation*}
\hat{q}_{x}=\frac{k\left(T_{s}-T_{0}\right)}{\sqrt{\pi \alpha t}} \exp \left(-x^{2} / 4 \alpha t\right) \tag{1.32}
\end{equation*}
$$

The total amount of heat transferred per unit area across the surface at $x=0$ in time $t$ is given by:

$$
\begin{equation*}
\frac{Q}{A}=2 k\left(T_{s}-T_{0}\right) \sqrt{\frac{t}{\pi \alpha}} \tag{1.33}
\end{equation*}
$$

Although the semi-infinite solid may appear to be a purely academic construct, it has a number of practical applications. For example, the earth behaves essentially as a semi-infinite solid. A solid of any finite thickness can be considered a semi-infinite solid if the time interval of interest is sufficiently short that heat penetrates only a small distance into the solid. The approximation is generally acceptable if the following inequality is satisfied:

$$
\begin{equation*}
\frac{\alpha t}{L^{2}}<0.1 \tag{1.34}
\end{equation*}
$$

where $L$ is the thickness of the solid. The dimensionless group $\alpha t / L^{2}$ is called the Fourier number and is designated $F o$.

## Example 1.10

The steel panel of a firewall is $5-\mathrm{cm}$ thick and is initially at $25^{\circ} \mathrm{C}$. The exterior surface of the panel is suddenly exposed to a temperature of $250^{\circ} \mathrm{C}$. Estimate the temperature at the center and at the interior surface of the panel after 20 s of exposure to this temperature. The thermal diffusivity of the panel is $0.97 \times 10^{-5} \mathrm{~m}^{2} / \mathrm{s}$.

## Solution

To determine if the panel can be approximated by a semi-infinite solid, we calculate the Fourier number:

$$
F o=\frac{\alpha t}{L^{2}}=\frac{0.97 \times 10^{-5} \times 20}{(0.05)^{2}} \cong 0.0776
$$

Since $F o<0.1$, the approximation should be acceptable. Thus, using Equation (1.30) with $x=0.025$ for the temperature at the center,

$$
\begin{aligned}
\frac{T-T_{s}}{T_{0}-T_{s}} & =\operatorname{erf}\left(\frac{x}{2 \sqrt{\alpha t}}\right) \\
\frac{T-250}{25-250} & =\operatorname{erf}\left(\frac{0.025}{2 \sqrt{0.97 \times 10^{-5} \times 20}}\right)=\operatorname{erf}(0.8974) \\
\frac{T-250}{-225} & =0.7969(\text { from Table 1.4) } \\
T & \cong 70.7^{\circ} \mathrm{C}
\end{aligned}
$$



Figure 1.5 Infinite solid of finite thickness.

For the interior surface, $x=0.05$ and Equation (1.30) gives:

$$
\begin{aligned}
\frac{T-250}{-225} & =\operatorname{erf}\left(\frac{0.05}{2 \sqrt{0.97 \times 10^{-5} \times 20}}\right)=\operatorname{erf}(1.795) \\
& =0.9891 \\
T & \cong 27.5^{\circ} \mathrm{C}
\end{aligned}
$$

Thus, the temperature of the interior surface has not changed greatly from its initial value of $25^{\circ} \mathrm{C}$, and treating the panel as a semi-infinite solid is therefore a reasonable approximation.

Consider now the rectangular solid of finite thickness illustrated in Figure 1.5. The configuration is the same as that for the semi-infinite solid except that the solid now occupies the region from $x=0$ to $x=2 s$. The solid is initially at uniform temperature $T_{0}$ and at time $t=0$ the temperature of the surfaces at $x=0$ and $x=2 s$ are changed to $T_{s}$. If $T_{s}>T_{0}$, then heat will flow into the solid from both sides. It is assumed that heat flows only in the $x$-direction, which again can be achieved mathematically by making the solid of infinite extent in the $\pm y$ - and $\pm z$-directions. This condition will be approximated in practice when the areas of the surfaces normal to the $y$-and $z$-directions are much smaller than the area of the surface normal to the $x$-direction, or when the former surfaces are insulated.

The mathematical statement of this problem is the same as that of the semi-infinite solid except that the third boundary condition is replaced by:

$$
\text { (3') } \quad \mathrm{At} x=2 s \quad T=T_{s}
$$

The solution for $T(x, t)$ can be found in the textbooks cited at the beginning of this section. Frequently, however, one is interested in determining the average temperature, $\bar{T}$, of the solid as a
function of time, where:

$$
\begin{equation*}
\bar{T}(t)=\frac{1}{2 s} \int_{0}^{2 s} T(x, t) d x \tag{1.35}
\end{equation*}
$$

That is, $\bar{T}$ is the temperature averaged over the thickness of the solid at a given instant of time. The solution for $\bar{T}$ is in the form of an infinite series [12]:

$$
\begin{equation*}
\frac{T_{s}-\bar{T}}{T_{s}-T_{0}}=\frac{8}{\pi^{2}}\left(e^{-a F o}+\frac{1}{9} e^{-9 a F o}+\frac{1}{25} e^{-25 a F o}+\cdots\right) \tag{1.36}
\end{equation*}
$$

where $a=(\pi / 2)^{2} \cong 2.4674$ and $F o=\alpha t / s^{2}$.
The solution given by Equation (1.36) is shown graphically in Figure 1.6. When the Fourier number, Fo, is greater than about 0.1 , the series converges very rapidly so that only the first term is significant. Under these conditions, Equation (1.36) can be solved for the time to give:

$$
\begin{equation*}
t=\frac{1}{\alpha}\left(\frac{2 s}{\pi}\right)^{2} \ln \left[\frac{8\left(T_{s}-T_{0}\right)}{\pi^{2}\left(T_{s}-\bar{T}\right)}\right] \tag{1.37}
\end{equation*}
$$



Figure 1.6 Average temperatures during unsteady-state heating or cooling of a rectangular solid, an infinitely long cylinder, and a sphere.

The total amount of heat, $Q$, transferred to the solid per unit area, $A$, in time $t$ is:

$$
\begin{equation*}
\frac{Q(t)}{A}=\frac{m c}{A}\left[\bar{T}(t)-T_{0}\right] \tag{1.38}
\end{equation*}
$$

where $m$, the mass of solid, is equal to $2 \rho s A$. Thus,

$$
\begin{equation*}
\frac{Q(t)}{A}=2 \rho c s\left[\bar{T}(t)-T_{0}\right] \tag{1.39}
\end{equation*}
$$

The analogous problem in cylindrical geometry is that of an infinitely long solid cylinder of radius, $R$, initially at uniform temperature, $T_{0}$. At time $t=0$ the temperature of the surface is changed to $T_{s .}$. This situation will be approximated in practice by a finite cylinder whose length is much greater than its diameter, or whose ends are insulated. The solutions corresponding to Equations (1.36), (1.37), and (1.39) are [12]:

$$
\begin{align*}
\frac{T_{s}-\bar{T}}{T_{s}-T_{0}}= & 0.692 e^{-5.78 F o}+0.131 e^{-30.5 F o} \\
& +0.0534 e^{-74.9 F o}+\cdots  \tag{1.40}\\
t= & \frac{R^{2}}{5.78 \alpha} \ln \left[\frac{0.692\left(T_{s}-T_{0}\right)}{T_{s}-\bar{T}}\right]  \tag{1.41}\\
\frac{Q(t)}{A}= & \frac{\rho c R}{2}\left[\bar{T}(t)-T_{0}\right] \tag{1.42}
\end{align*}
$$

where

$$
\begin{equation*}
F o=\frac{\alpha t}{R^{2}} \tag{1.43}
\end{equation*}
$$

Here $A$ is the circumferential area, which is equal to $2 \pi R$ times the length of the cylinder. Equation (1.40) is shown graphically in Figure 1.6.

The corresponding equations for a solid sphere of radius $R$ are [12]:

$$
\begin{gather*}
\frac{T_{s}-\bar{T}}{T_{s}-T_{0}}=0.608 e^{-9.87 F o}+0.152 e^{-39.5 F o} \\
+0.0676 e^{-88.8 F o}+\cdots  \tag{1.44}\\
t=\frac{R^{2}}{9.87 \alpha} \ln \left[\frac{0.608\left(T_{s}-T_{0}\right)}{T_{s}-\bar{T}}\right]  \tag{1.45}\\
Q(t)=\frac{4}{3} \pi R^{3} \rho c\left[T(t)-T_{0}\right] \tag{1.46}
\end{gather*}
$$

The Fourier number for this case is also given by Equation (1.43). Equation (1.44) is shown graphically in Figure 1.6.

## Example 1.11

A 12 -ounce can of beer initially at $80^{\circ} \mathrm{F}$ is placed in a refrigerator, which is at $36^{\circ} \mathrm{F}$. Estimate the time required for the beer to reach $40^{\circ} \mathrm{F}$.

## Solution

Application to this problem of the equations presented in this section requires a considerable amount of approximation, a situation that is not uncommon in practice. Since a 12 -ounce beer can has a diameter of 2.5 in . and a length of 4.75 in ., we have:

$$
L / D=\frac{4.75}{2.5}=1.9
$$

Hence, the assumption of an infinite cylinder will not be a particularly good one. In effect, we will be neglecting the heat transfer through the ends of the can. The effect of this approximation will be to overestimate the required time.

Next, we must assume that the temperature of the surface of the can suddenly drops to $36^{\circ} \mathrm{F}$ when it is placed in the refrigerator. That is, we neglect the resistance to heat transfer between the air in the refrigerator and the surface of the can. The effect of this approximation will be to underestimate the required time. Hence, there will be at least a partial cancellation of errors.

We must also neglect the heat transfer due to convection currents set up in the liquid inside the can by the cooling process. The effect of this approximation will be to overestimate the required time.

Finally, we will neglect the resistance of the aluminum can and will approximate the physical properties of beer by those of water. We thus take:

$$
\begin{array}{ll}
k=0.341 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F} & T_{s}=36^{\circ} \mathrm{F} \\
\rho=62.4 \mathrm{lbm} / \mathrm{ft}^{3} & T_{0}=80^{\circ} \mathrm{F} \\
c=1.0 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} & \bar{T}=40^{\circ} \mathrm{F}
\end{array}
$$

With these values we have:

$$
\begin{gathered}
\alpha=\frac{k}{\rho c}=0.0055 \mathrm{ft}^{2} / \mathrm{h} \\
\frac{T_{s}-\bar{T}}{T_{s}-T_{0}}=\frac{36-40}{36-80}=0.0909
\end{gathered}
$$

From Figure 1.6, we find a Fourier number of about 0.35 . Thus,

$$
\begin{gathered}
F o=\frac{\alpha t}{R^{2}}=0.35 \\
t=\frac{0.35 R^{2}}{\alpha}=\frac{0.35(1.25 / 12)^{2}}{0.0055} \cong 0.69 \mathrm{~h}
\end{gathered}
$$

Alternatively, since $F o>0.1$, we can use Equation (1.41):

$$
\begin{aligned}
t & =\frac{R^{2}}{5.78 \alpha} \ln \left[\frac{0.692\left(T_{s}-T_{0}\right)}{T_{s}-\bar{T}}\right] \\
& =\frac{(1.25 / 12)^{2}}{5.78 \times 0.0055} \quad \ln \left[\frac{0.629}{0.0909}\right] \\
t & =0.66 \mathrm{~h}
\end{aligned}
$$

This agrees with the previous calculation to within the accuracy with which one can read the graph of Figure 1.6. Experience suggests that this estimate is somewhat optimistic and, hence, that the error introduced by neglecting the thermal resistance between the air and the can is predominant. Nevertheless, if the answer is rounded to the nearest hour (a reasonable thing to do considering the many approximations that were made), the result is a cooling time of 1 h , which is essentially correct. In any event, the calculations show that the time required is more than a few minutes but less than a day, and in many practical situations this level of detail is all that is needed.

### 1.7 Mechanisms of Heat Conduction

This chapter has dealt with the computational aspects of heat conduction. In this concluding section we briefly discuss the mechanisms of heat conduction in solids and fluids. Although Fourier's law accurately describes heat conduction in both solids and fluids, the underlying mechanisms differ. In all media, however, the processes responsible for conduction take place at the molecular or atomic level.

Heat conduction in fluids is the result of random molecular motion. Thermal energy is the energy associated with translational, vibrational, and rotational motions of the molecules comprising a substance. When a high-energy molecule moves from a high-temperature region of a fluid toward a region of lower temperature (and, hence, lower thermal energy), it carries its thermal energy along with it. Likewise, when a high-energy molecule collides with one of lower energy, there is a partial transfer of energy to the lower-energy molecule. The result of these molecular motions and interactions is a net transfer of thermal energy from regions of higher temperature to regions of lower temperature.

Heat conduction in solids is the result of vibrations of the solid lattice and of the motion of free electrons in the material. In metals, where free electrons are plentiful, thermal energy transport by electrons predominates. Thus, good electrical conductors, such as copper and aluminum, are also good conductors of heat. Metal alloys, however, generally have lower (often much lower) thermal and electrical conductivities than the corresponding pure metals due to disruption of free electron movement by the alloying atoms, which act as impurities.

Thermal energy transport in non-metallic solids occurs primarily by lattice vibrations. In general, the more regular the lattice structure of a material is, the higher its thermal conductivity. For example, quartz, which is a crystalline solid, is a better heat conductor than glass, which is an amorphous solid. Also, materials that are poor electrical conductors may nevertheless be good heat conductors. Diamond, for instance, is an excellent conductor of heat due to transport by lattice vibrations.

Most common insulating materials, both natural and man-made, owe their effectiveness to air or other gases trapped in small compartments formed by fibers, feathers, hairs, pores, or rigid foam. Isolation of the air in these small spaces prevents convection currents from forming within the material, and the relatively low thermal conductivity of air (and other gases) thereby imparts a low effective thermal conductivity to the material as a whole. Insulating materials with effective thermal conductivities much less than that of air are available; they are made by incorporating evacuated layers within the material.

## References

1. Fourier, J. B., The Analytical Theory of Heat, translated by A. Freeman, Dover Publications, Inc., New York, 1955 (originally published in 1822).
2. Poling, B. E., J.M. Prausnitz and J. P. O'Connell, The Properties of Gases and Liquids, 5th edn, McGraw-Hill, New York, 2000.
3. White, F. M., Heat Transfer, Addison-Wesley, Reading, MA, 1984.
4. Irvine Jr., T. F. Thermal contact resistance, in Heat Exchanger Design Handbook, Vol. 2, Hemisphere Publishing Corp., New York, 1988.
5. Incropera, F. P. and D. P. DeWitt, Introduction to Heat Transfer, 4th edn, John Wiley \& Sons, New York, 2002.
6. Kreith, F. and W. Z. Black, Basic Heat Transfer, Harper \& Row, New York, 1980.
7. Holman, J. P., Heat Transfer, 7th edn, McGraw-Hill, New York, 1990.
8. Kreith, F. and M. S. Bohn, Principles of Heat Transfer, 6th edn, Brooks/Cole, Pacific Grove, CA, 2001.
9. Schneider, P. J., Conduction Heat Transfer, Addison-Wesley, Reading, MA, 1955.
10. Carslaw, H. S. and J. C. Jaeger, Conduction of Heat in Solids, 2nd edn, Oxford University Press, New York, 1959.
11. Jensen, V. G. and G. V. Jeffreys, Mathematical Methods in Chemical Engineering, 2nd edn, Academic Press, New York, 1977.
12. McCabe, W. L. and J. C. Smith, Unit Operations of Chemical Engineering, 3rd edn, McGraw-Hill, New York, 1976.

## Notations

| $A$ | Area |
| :--- | :--- |
| $A_{f}$ | Fin surface area (Table 1.2) |
| $A_{p}$ | Prime surface area (Table (1.2) |
| $A_{r}$ | $2 \pi r L$ |
| $A_{x}, A_{y}$ | Cross-sectional area perpendicular to $x$ - or $y$-direction |
| $a$ | Constant in Equation (1.2); constant equal to $(\pi / 2)^{2}$ in Equation (1.36) |
| $B$ | Thickness of solid in direction of heat flow |
| $b$ | Constant in Equation (1.2) |
| $c$ | specific heat of solid |
| $C_{1}, C_{2}$ | Constants of integration |
| $D$ | Diameter; distance between adjoining walls (Table 1.3) |
| $d$ | diameter of eccentric cylinder (Table 1.3) |
| $E$ | Voltage difference in Ohm's law |
| erf | Gaussian error function defined by Equation (1.31) |
| $F o$ | Fourier number |
| $h$ | Heat-transfer coefficient (Table 1.2) |
| $I$ | Electrical current in Ohm's law |
| $\vec{i}$ | Unit vector in $x$-direction |
| $\vec{j}$ | Unit vector in $y$-direction |
| $k$ | Thermal conductivity |
| $\vec{k}$ | Unit vector in $z$-direction |
| $L$ | Length; thickness of edge or corner of wall (Table 1.3) |
| $Q$ | Total amount of heat transferred |
| $q$ | Rate of heat transfer |
| $q_{x}, q_{y}, q_{r}$ | Rate of heat transfer in $x$-, $y$-, or $r$-direction |
| $\underset{q}{q}=q / A$ | Heat flux |
| $\vec{q}$ | Rate of heat generation per unit volume |
| $\vec{q}$ | Heat flow vector |


| $\overrightarrow{\hat{q}}$ | Heat flux vector |
| :--- | :--- |
| $R$ | Resistance; radius of cylinder or sphere |
| $R_{t h}$ | Thermal resistance |
| $R$-value | Ratio of a material's thickness to its thermal conductivity, in English units |
| $r$ | Radial coordinate in cylindrical or spherical coordinate system |
| $S$ | Conduction shape factor defined by Equation (1.27) |
| $s$ | Half-width of solid in Figure 1.5 |
| $T$ | Temperature |
| $\bar{T}$ | Average temperature |
| $t$ | Time |
| $W$ | Width |
| $w$ | Width or displacement (Table 1.3) |
| $x$ | Coordinate in Cartesian system |
| $y$ | Coordinate in Cartesian system |
| $z$ | Coordinate in Cartesian or cylindrical system; depth or displacement (Table 1.3) |

## Greek Letters

$\alpha=k / \rho c \quad$ Thermal diffusivity
$\Gamma \quad$ Constant in Example 1.5
$\gamma \quad$ Constant in Example 1.5
$\Delta T, \Delta x$, etc. Difference in $T, x$, etc.
$\eta \quad$ Efficiency
$\eta_{f} \quad$ Fin efficiency (Table 1.2)
$\eta_{w} \quad$ Weighted efficiency of a finned surface (Table 1.2)
$\theta \quad$ Angular coordinate in spherical system; angle between heat flux vector and $x$-axis (Example 1.1)
$\rho \quad$ Density
$\phi \quad$ Angular coordinate in cylindrical or spherical system

## Other Symbols

$\vec{\nabla} T$ Temperature gradient vector
$\nabla^{2} \quad$ Laplacian operator $=\frac{\partial^{2}}{\partial x^{2}}+\frac{\partial^{2}}{\partial y^{2}}+\frac{\partial^{2}}{\partial z^{2}}$ in Cartesian coordinates
$\rightarrow \quad$ Overstrike to denote a vector
$\left.\right|_{x} \quad$ Evaluated at $x$

## Problems

(1.1) The temperature distribution in a bakelite block $(k=0.233 \mathrm{~W} / \mathrm{m} \cdot \mathrm{k})$ is given by:

$$
T(x, y, z)=x^{2}-2 y^{2}+z^{2}-x y+2 y z
$$

where $T \propto^{\circ} \mathrm{C}$ and $x, y, z \propto \mathrm{~m}$. Find the magnitude of the heat flux vector at the point $(x, y, z)=(0.5,0,0.2)$.
Ans. $0.252 \mathrm{~W} / \mathrm{m}^{2}$.
(1.2) The temperature distribution in a Teflon $\operatorname{rod}(k=0.35 \mathrm{~W} / \mathrm{m} \cdot \mathrm{k})$ is:

$$
T(r, \phi, z)=r \sin \phi+2 z
$$

where
$T \propto{ }^{\circ} \mathrm{C}$
$r=$ radial position (m)
$\phi=$ circumferential position (rad)
$z=$ axial position (m)
Find the magnitude of the heat flux vector at the position $(r, \phi, z)=(0.1,0,0.5)$.
Ans. $0.78 \mathrm{~W} / \mathrm{m}^{2}$.
(1.3) The rectangular block shown below has a thermal conductivity of $1.4 \mathrm{~W} / \mathrm{m} \cdot \mathrm{k}$. The block is well insulated on the front and back surfaces, and the temperature in the block varies linearly from left to right and from top to bottom. Determine the magnitude and direction of the heat flux vector. What are the heat flows in the horizontal and vertical directions?


Ans. $313 \mathrm{~W} / \mathrm{m}^{2}$ at an angle of $26.6^{\circ}$ with the horizontal; 1.4 W and 5.76 W .
(1.4) The temperature on one side of a 6-in. thick solid wall is $200^{\circ} \mathrm{F}$ and the temperature on the other side is $100^{\circ} \mathrm{F}$. The thermal conductivity of the wall can be represented by:

$$
k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)=0.1+0.001 T\left({ }^{\circ} \mathrm{F}\right)
$$

(a) Calculate the heat flux through the wall under steady-state conditions.
(b) Calculate the thermal resistance for a $1 \mathrm{ft}^{2}$ cross-section of the wall.

Ans. (a) $50 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$. (b) $2 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$
(1.5) A long hollow cylinder has an inner radius of 1.5 in . and an outer radius of 2.5 in . The temperature of the inner surface is $150^{\circ} \mathrm{F}$ and the outer surface is at $110^{\circ} \mathrm{F}$. The thermal conductivity of the material can be represented by:

$$
k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)=0.1+0.001 T\left({ }^{\circ} \mathrm{F}\right)
$$

(a) Find the steady-state heat flux in the radial direction:
(i) At the inner surface
(ii) At the outer surface
(b) Calculate the thermal resistance for a 1 ft length of the cylinder.

Ans: (a) $144.1 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}, 86.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$. (b) $0.3535 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$.
(1.6) A rectangular block has thickness $B$ in the $x$-direction. The side at $x=0$ is held at temperature $T_{1}$ while the side at $x=B$ is held at $T_{2}$. The other four sides are well insulated. Heat is generated in the block at a uniform rate per unit volume of $\Gamma$.
(a) Use the conduction equation to derive an expression for the steady-state temperature profile, $T(x)$. Assume constant thermal conductivity.
(b) Use the result of part (a) to calculate the maximum temperature in the block for the following values of the parameters:

$$
\begin{array}{ll}
T_{1}=100^{\circ} \mathrm{C} & k=0.2 \mathrm{~W} / \mathrm{m} \cdot \mathrm{k} \quad B=1.0 \mathrm{~m} \\
T_{2}=0^{\circ} \mathrm{C} & \Gamma=100 \mathrm{~W} / \mathrm{m}^{3}
\end{array}
$$

Ans. (a) $T(x)=T_{1}+\left(\frac{T_{2}-T_{1}}{B}+\frac{\Gamma L}{2 k}\right) x-\frac{\Gamma x^{2}}{2 k} . \quad$ (b) $T_{\max }=122.5^{\circ} \mathrm{C}$ at $x=0.3 \mathrm{~m}$
(1.7) Repeat Problem 1.6 for the situation in which the side of the block at $x=0$ is well insulated.

Ans. (a) $T(x)=T_{2}+\frac{\Gamma}{2 k}\left(B^{2}-x^{2}\right)$. (b) $T_{\max }=250^{\circ} \mathrm{C}$
(1.8) Repeat Problem 1.6 for the situation in which the side of the block at $x=0$ is exposed to an external heat flux, $\hat{q}_{o}$, of $20 \mathrm{~W} / \mathrm{m}^{2}$. Note that the boundary condition at $x=0$ for this case becomes

$$
\frac{d T}{d x}=-\frac{\hat{q}_{o}}{k}
$$

Ans. (a) $T(x)=T_{2}+\frac{\hat{q}_{o}}{k}(B-x)+\frac{\Gamma}{2 k}\left(B^{2}-x^{2}\right) . \quad$ (b) $T_{\max }=350^{\circ} \mathrm{C}$
(1.9) A long hollow cylinder has inner and outer radii $R_{1}$ and $R_{2}$, respectively. The temperature of the inner surface at radius $R_{1}$ is held at a constant value, $T_{1}$, while that of the outer surface at radius $R_{2}$ is held constant at a value of $T_{2}$. Heat is generated in the wall of the cylinder at a rate per unit volume given by $\dot{q}=\Gamma r$, where $r$ is radial position and $\Gamma$ is a constant. Assuming constant thermal conductivity and heat flow only in the radial direction, derive expressions for:
(a) The steady-state temperature profile, $T(r)$, in the cylinder wall.
(b) The heat flux at the outer surface of the cylinder.

## Ans.

(a) $T(r)=T_{1}+(\Gamma / 9 k)\left(R_{1}^{3}-r^{3}\right)+\frac{\left\{T_{2}-T_{1}+\frac{\Gamma}{9 k}\left(R_{2}^{3}-R_{1}^{3}\right)\right\} \ln \left(r / R_{1}\right)}{\ln \left(R_{2} / R_{1}\right)}$.
(b) $\left.\hat{q}_{r}\right|_{r=R_{2}}=\frac{\Gamma R_{2}^{3}}{3}+\frac{k\left\{T_{1}-T_{2}-(\Gamma / 9 k)\left(R_{2}^{3}-R_{1}^{3}\right)\right\}}{R_{2} \ln \left(R_{2} / R_{1}\right)}$.
(1.10) Repeat Problem 1.9 for the situation in which the inner surface of the cylinder at $R_{1}$ is well insulated.

Ans. (a) $T(r)=T_{2}-(\Gamma / 9 k)\left(R_{2}^{3}-r^{3}\right)+\frac{\Gamma R_{1}^{3} \ln \left(r / R_{2}\right)}{3 k}$. (b) $\left.\hat{q}_{r}\right|_{r=R_{2}}=\frac{\Gamma\left(R_{2}^{3}-R_{1}^{3}\right)}{3 R_{2}}$.
(1.11) A hollow sphere has inner and outer radii $R_{1}$ and $R_{2}$, respectively. The inner surface at radius $R_{1}$ is held at a uniform temperature $T_{1}$, while the outer surface at radius $R_{2}$ is held at temperature $T_{2}$. Assuming constant thermal conductivity, no heat generation and steady-state conditions, use the conduction equation to derive expressions for:
(a) The temperature profile, $T(r)$.
(b) The rate of heat transfer, $q_{r}$, in the radial direction.
(c) The thermal resistance.

Ans.
(a) $T(r)=T_{1}+\frac{R_{1} R_{2}\left(T_{1}-T_{2}\right)\left(\frac{1}{r}-\frac{1}{R_{1}}\right)}{R_{2}-R_{1}}$.
(b) $q_{r}=\frac{4 \pi k R_{1} R_{2}\left(T_{1}-T_{2}\right)}{R_{2}-R_{1}}$.
(c) See Table 1.2.
(1.12) A hollow sphere with inner and outer radii $R_{1}$ and $R_{2}$ has fixed uniform temperatures of $T_{1}$ on the inner surface at radius $R_{1}$ and $T_{2}$ on the outer surface at radius $R_{2}$. Heat is generated in the wall of the sphere at a rate per unit volume given by $\dot{q}=\Gamma r$, where $r$ is radial position and $\Gamma$ is a constant. Assuming constant thermal conductivity, use the conduction equation to derive expressions for:
(a) The steady-state temperature profile, $T(r)$, in the wall.
(b) The heat flux at the outer surface of the sphere.

## Ans.

(a) $T(r)=T_{1}+(\Gamma / 12 k)\left(R_{1}^{3}-r^{3}\right)+\frac{R_{1} R_{2}\left\{T_{1}-T_{2}-(\Gamma / 12 k)\left(R_{2}^{3}-R_{1}^{3}\right)\right\}\left(\frac{1}{r}-\frac{1}{R_{1}}\right)}{R_{2}-R_{1}}$.
(b) $\left.\hat{q}_{r}\right|_{r=R_{2}}=\frac{\Gamma R_{2}^{2}}{4}+\left\{k R_{1} / R_{2}\left(R_{2}-R_{1}\right)\right\}\left\{T_{1}-T_{2}-(\Gamma / 12 k)\left(R_{2}^{3}-R_{1}^{3}\right)\right\}$.
(1.13) Repeat Problem 1.12 for the situation in which the inner surface at radial position $R_{1}$ is well insulated.

Ans.
(a) $T(r)=T_{2}+(\Gamma / 12 k)\left(R_{2}^{3}-r^{3}\right)+\left(\frac{\Gamma R_{1}^{4}}{4 k}\right)\left(\frac{1}{R_{2}}-\frac{1}{r}\right)$.
(b) $\left.\hat{q}_{r}\right|_{r=R_{2}}=\frac{\Gamma\left(R_{2}^{4}-R_{1}^{4}\right)}{4 R_{2}^{2}}$
(1.14) When conduction occurs in the radial direction in a solid rod or sphere, the heat flux must be zero at the center ( $r=0$ ) in order for a finite temperature to exist there. Hence, an appropriate boundary condition is:

$$
\frac{d T}{d r}=0 \quad \text { at } r=0
$$

Consider a solid sphere of radius $R$ with a fixed surface temperature, $T_{R}$. Heat is generated within the solid at a rate per unit volume given by $\dot{q}=\Gamma_{1}+\Gamma_{2} r$, where $\Gamma_{1}$ and $\Gamma_{2}$ are constants.
(a) Assuming constant thermal conductivity, use the conduction equation to derive an expression for the steady-state temperature profile, $T(r)$, in the sphere.
(b) Calculate the temperature at the center of the sphere for the following parameter values:

$$
\begin{array}{rll}
R=1.5 \mathrm{~m} & \Gamma_{1}=20 \mathrm{~W} / \mathrm{m}^{3} & T_{R}=20^{\circ} \mathrm{C} \\
k=0.5 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K} & \Gamma_{2}=10 \mathrm{~W} / \mathrm{m}^{4} &
\end{array}
$$

Ans. (a) $T(r)=T_{R}+\left(\Gamma_{1} / 6 k\right)\left(R^{2}-r^{2}\right)+\left(\Gamma_{2} / 12 k\right)\left(R^{3}-r^{3}\right) . \quad$ (b) $40.625^{\circ} \mathrm{C}$.
(1.15) A solid cylinder of radius $R$ is well insulated at both ends, and its exterior surface at $r=R$ is held at a fixed temperature, $T_{R}$. Heat is generated in the solid at a rate per unit volume given by $\dot{q}=\Gamma(1-r / R)$, where $\Gamma=$ constant. The thermal conductivity of the solid may be assumed constant. Use the conduction equation together with an appropriate set of boundary conditions to derive an expression for the steady-state temperature profile, $T(r)$, in the solid.

Ans. $T(r)=T_{R}+(\Gamma / 36 k)\left(5 R^{2}+4 r^{3} / R-9 r^{2}\right)$.
(1.16) A rectangular wall has thickness $B$ in the $x$-direction and is insulated on all sides except the one at $x=B$, which is held at a constant temperature, $T_{w}$. Heat is generated in the wall at a rate per unit volume given by $\dot{q}=\Gamma(B-x)$, where $\Gamma$ is a constant.
(a) Assuming constant thermal conductivity, derive an expression for the steady-state temperature profile, $T(x)$, in the wall.
(b) Calculate the temperature of the block at the side $x=0$ for the following parameter values:

$$
\begin{gathered}
\Gamma=0.3 \times 10^{6} \mathrm{~W} / \mathrm{m}^{4} \quad B=0.1 \mathrm{~m} \\
T_{w}=90^{\circ} \mathrm{C} \quad k=25 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K}
\end{gathered}
$$

Ans. (a) $T(x)=T_{w}+(\Gamma / k)\left(\frac{x^{3}}{6}-\frac{x^{2} B}{2}+\frac{B^{3}}{3}\right) . \quad$ (b) $94^{\circ} \mathrm{C}$.
(1.17) The exterior wall of an industrial furnace is to be covered with a 2 -in. thick layer of hightemperature insulation having an $R$-value of 2.8 , followed by a layer of magnesia (85\%) insulation. The furnace wall may reach $1200^{\circ} \mathrm{F}$, and for safety reasons, the exterior of the magnesia insulation should not exceed $120^{\circ} \mathrm{F}$. At this temperature, the heat flux from the insulation to the surrounding air has been estimated for design purposes to be $200 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(a) What is the thermal conductivity of the high-temperature insulation?
(b) What thickness of magnesia insulation should be used?
(c) Estimate the temperature at the interface between the high-temperature insulation and the magnesia insulation.

Ans. (a) $k=0.0595 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$. (c) $640^{\circ} \mathrm{F}$.
(1.18) A storage tank to be used in a chemical process is spherical in shape and is covered with a 3 -in. thick layer of insulation having an $R$-value of 12 . The tank will hold a chemical intermediate that must be maintained at $150^{\circ} \mathrm{F}$. A heating unit is required to maintain this temperature in the tank.
(a) What is the thermal conductivity of the insulation?
(b) Determine the duty for the heating unit assuming as a worst-case scenario that the exterior surface of the insulation reaches a temperature of $20^{\circ} \mathrm{F}$.
(c) What thermal resistances were neglected in your calculation?

Ans. (a) $k=0.02083 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$. (b) $q \cong 7900 \mathrm{Btu} / \mathrm{h}$.
(1.19) A 4 -in. schedule 80 steel pipe ( $\mathrm{ID}=3.826$ in., $\mathrm{OD}=4.5 \mathrm{in}$.) carries a heat-transfer fluid at $600^{\circ} \mathrm{F}$ and is covered with a $1 / 2$-in. thick layer of pipe insulation. The pipe is surrounded by air at $80^{\circ} \mathrm{F}$. The vendor's literature states that a $1-\mathrm{in}$. thick layer of the pipe insulation has an $R$-value of 3 . Neglecting convective resistances, the resistance of the pipe wall, and thermal radiation, estimate the rate of heat loss from the pipe per foot of length.
Ans. 453 Btu/h $\cdot \mathrm{ft}$ pipe
(1.20) A pipe with an OD of 6.03 cm and an ID of 4.93 cm carries steam at $250^{\circ} \mathrm{C}$. The pipe is covered with 2.5 cm of magnesia ( $85 \%$ ) insulation followed by 2.5 cm of polystyrene insulation $(k=0.025 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$. The temperature of the exterior surface of the polystyrene is $25^{\circ} \mathrm{C}$. The thermal resistance of the pipe wall may be neglected in this problem. Also neglect the convective and contact resistances.
(a) Calculate the rate of heat loss per meter of pipe length.
(b) Calculate the temperature at the interface between the two types of insulation.

Ans. (a) $63 \mathrm{~W} / \mathrm{m}$ of pipe. (b) $174.5^{\circ} \mathrm{C}$.
(1.21) It is desired to reduce the heat loss from the storage tank of problem 1.18 by $90 \%$. What additional thickness of insulation will be required?
(1.22) A steel pipe with an OD of 2.375 in . is covered with a $1 / 2$-in. thick layer of asbestos insulation ( $k=0.048 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) followed by a 1 -in. thick layer of fiberglass insulation ( $k=0.022 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ). The temperature of the pipe wall is $600^{\circ} \mathrm{F}$ and the exterior surface of the fiberglass insulation is at $100^{\circ} \mathrm{F}$. Calculate:
(a) The rate of heat loss per foot of pipe length.
(b) The temperature at the interface between the asbestos and fiberglass insulations.

Ans. (a) $110 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}$ pipe. (b) $471^{\circ} \mathrm{F}$.
(1.23) A building contains $6000 \mathrm{ft}^{2}$ of wall surface area constructed of panels shown in the sketch below. The interior sheathing is gypsum wallboard and the wood is yellow pine. Calculate the rate of heat loss through the walls if the interior wall surface is at $70^{\circ} \mathrm{F}$ and the exterior surface is at $30^{\circ} \mathrm{F}$.

Ans. 22,300 Btu/h

(1.24) A 6 in. schedule 80 steel pipe ( $\mathrm{OD}=6.62 \mathrm{in}$.) will be used to transport $450^{\circ} \mathrm{F}$ steam from a boiler house to a new process unit. The pipe will be buried at a depth of 3 ft (to the pipe centerline). The soil at the plant site has an average thermal conductivity of $0.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ and the minimum expected ground surface temperature is $20^{\circ} \mathrm{F}$. Estimate the rate of heat loss per foot of pipe length for the following cases:
(a) The pipe is not insulated.
(b) The pipe is covered with a 2 -in. thick layer of magnesia insulation.

Neglect the thermal resistance of the pipe wall and the contact resistance between the insulation and pipe wall.
Ans. (a) $350 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}$ of pipe. (b) $160 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}$ of pipe.
(1.25) The cross-section of an industrial chimney is shown in the sketch below. The flue has a diameter of 2 ft and the process waste gas flowing through it is at $400^{\circ} \mathrm{F}$. If the exterior surface of the brick is at $120^{\circ} \mathrm{F}$, calculate the rate of heat loss from the waste gas per foot of chimney height. Neglect the convective resistance between the waste gas and interior surface of the flue for this calculation.


Ans. 910 Btu/h $\cdot \mathrm{ft}$ of chimney height.
(1.26) A new underground pipeline at a chemical complex is to be placed parallel to an existing underground pipeline. The existing line has an OD of 8.9 cm , carries a fluid at 283 K and is not insulated. The new line will have an OD of 11.4 cm and will carry a fluid at 335 K . The center-to-center distance between the two pipelines will be 0.76 m . The ground at the plant site has an average thermal conductivity of $0.7 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$. In order to determine whether the new line will need to be insulated, calculate the rate of heat transfer between the two pipelines per meter of pipe length if the new line is not insulated. For the purpose of this
calculation, neglect the resistances of the pipe walls and the convective resistances between the fluids and pipe walls.

Ans. $42 \mathrm{~W} / \mathrm{m}$ of pipe length.
Hot waste gas at $350^{\circ} \mathrm{F}$ will be transported from a new process unit to a pollution control device via an underground duct. The duct will be rectangular in cross-section with a height of 3 ft and a width of 5 ft . The top of the duct will be 1.25 ft below the ground surface, which for design purposes has been assigned a temperature of $40^{\circ} \mathrm{F}$. The average thermal conductivity of the ground at the plant site is $0.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$. Calculate the rate of heat loss from the waste gas per foot of duct length. What thermal resistances are neglected in your calculation?

The following shape factor for a buried rectangular solid is available in the literature:

$$
\begin{aligned}
& S=2.756 L\left[\ln \left(1+\frac{h}{a}\right)\right]^{-0.59}\left(\frac{h}{b}\right)^{-0.078} \\
& L \gg h, a, b
\end{aligned}
$$


(1.28) An industrial furnace wall will be made of diatomaceous refractory brick ( $\alpha=1.3228 \times$ $10^{-7} \mathrm{~m}^{2} / \mathrm{s}$ ) and is to be designed so that the exterior surface will remain cool enough for safety purposes. The design criterion is that the mid-plane temperature in the wall will not exceed 400 K after 8 h of operation with an interior wall surface temperature of 1100 K .
(a) Assume that the furnace wall can be approximated as a semi-infinite solid. Calculate the wall thickness required to meet the design specification assuming that the wall is initially at a uniform temperature of 300 K .
(b) Using the wall thickness obtained in part (a), calculate the exterior wall surface temperature after 8 h of operation.
(c) Based on the above results, is the assumption that the furnace wall can be approximated as a semi-infinite solid justified, i.e., is the wall thickness calculated in part (a) acceptable for design purposes? Explain why or why not.

Ans. (a) 26.8 cm . (b) 301.7 K .
(1.29) The steel panel ( $\alpha=0.97 \times 10^{-5} \mathrm{~m}^{2} / \mathrm{s}$ ) of a firewall is 5 cm thick and its interior surface is insulated. The panel is initially at $25^{\circ} \mathrm{C}$ when its exterior surface is suddenly exposed to a temperature of $250^{\circ} \mathrm{C}$. Calculate the average temperature of the panel after 2 min of exposure to this temperature.

Note: A wall of width $s$ with the temperature of one side suddenly raised to $T_{s}$ and the opposite side insulated is mathematically equivalent to a wall of width 2 s with the temperature of both sides suddenly raised to $T_{s}$. In the latter case, $d T / d x=0$ at the mid-plane due to symmetry, which is the same condition that exists at a perfectly insulated boundary.
Ans. $192^{\circ}$ C.
(1.30) An un-insulated metal storage tank at a chemical plant is cylindrical in shape with a diameter of 4 ft and a length of 25 ft . The liquid in the tank, which has properties similar to those of water, is at a temperature of $70^{\circ} \mathrm{F}$ when a frontal passage rapidly drops the ambient temperature to $40^{\circ} \mathrm{F}$. Assuming that ambient conditions remain constant for an extended period of time, estimate:
(a) The average temperature of the liquid in the tank 12 h after the frontal passage.
(b) The time required for the average temperature of the liquid to reach $50^{\circ} \mathrm{F}$.

Ans. (a) $59^{\circ} \mathrm{F}$. (b) 92 h .
(1.31) Repeat Problem 1.30 for the situation in which the fluid in the tank is
(a) Methyl alcohol.
(b) Aniline.
(1.32) Repeat Problem 1.30 for the situation in which the tank is spherical in shape with a diameter of 4.2 ft .

Ans. (a) $63^{\circ} \mathrm{F}$. (b) 207 h (From Equation (1.44). Note that $F o<0.1$.).

This page intentionally left blank

## CONVECTIVE HEAT TRANSFER

## Contents

### 2.1 Introduction <br> 44

2.2 Combined Conduction and Convection 44
2.3 Extended Surfaces

47
2.4 Forced Convection in Pipes and Ducts 53
2.5 Forced Convection in External Flow

62
2.6 Free Convection 65

### 2.1 Introduction

Convective heat transfer occurs when a gas or liquid flows past a solid surface whose temperature is different from that of the fluid. Examples include an organic heat-transfer fluid flowing inside a pipe whose wall is heated by electrical heating tape, and air flowing over the outside of a tube whose wall is chilled by evaporation of a refrigerant inside the tube. Two broad categories of convective heat transfer are distinguished, namely, forced convection and natural (or free) convection. In forced convection, the fluid motion is caused by an external agent such as a pump or blower. In natural convection, the fluid motion is the result of buoyancy forces created by temperature differences within the fluid.

In contrast to conductive heat transfer, convective heat-transfer problems are usually solved by means of empirical correlations derived from experimental data and dimensional analysis. The reason is that in order to solve a convection problem from first principles, one must solve the equations of fluid motion along with the energy balance equation. Although many important results have been obtained by solving the fundamental equations for convection problems in which the flow is laminar, no method has yet been devised to solve the turbulent flow equations entirely from first principles.

The empirical correlations are usually expressed in terms of a heat-transfer coefficient, $h$, which is defined by the relation:

$$
\begin{equation*}
q=h A \Delta T \tag{2.1}
\end{equation*}
$$

In this equation, $q$ is the rate of heat transfer between the solid surface and the fluid, $A$ is the area over which the heat transfer occurs, and $\Delta T$ is a characteristic temperature difference between the solid and the fluid. Equation (2.1) is often referred to as Newton's Law of Cooling, even though Newton had little to do with its development, and it is not really a physical law. It is simply a definition of the quantity, $h$. Note that the units of $h$ are $\mathrm{W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ or Btu $/ \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.

Equation (2.1) may appear to be similar to Fourier's Law of heat conduction. However, the coefficient, $h$, is an entirely different kind of entity from the thermal conductivity, $k$, which appears as the constant of proportionality in Fourier's Law. In particular, $h$ is not a material property. It depends not only on temperature and pressure, but also on such factors as geometry, the hydrodynamic regime (laminar or turbulent), and in turbulent flow, the intensity of the turbulence and the roughness of the solid surface. Hence, the heat-transfer coefficient should not be regarded as a fundamental quantity, but simply as a vehicle through which the empirical methods are implemented.

From the standpoint of transferring heat, turbulent flow is highly desirable. In general, heattransfer rates can be ordered according to the mechanism of heat transfer as follows:
conduction $<$ natural convection $<$ laminar forced convection $<$ turbulent forced convection
The reason that turbulent flow is so effective at transferring heat is that the turbulent eddies can rapidly transport fluid from one area to another. When this occurs, the thermal energy of the fluid is transported along with the fluid itself. This eddy transport mechanism is much faster (typically, about two orders of magnitude) than the molecular transport mechanism of heat conduction.

The heat-transfer correlations presented in this chapter are valid for most common Newtonian fluids. They are not valid for liquid metals or for non-Newtonian fluids. Special correlations are required for these types of fluids.

### 2.2 Combined Conduction and Convection

Heat-transfer problems involving both conduction and convection can be conveniently handled by means of the thermal resistance concept. Equation (2.1) can be put into the form of a thermal resistance as follows:

$$
q=h A \Delta T=\Delta T / R_{t h}
$$

Thus,

$$
\begin{equation*}
R_{t h}=\frac{1}{h A} \tag{2.2}
\end{equation*}
$$

This expression for convective thermal resistance was given previously in Table 1.2. Convective resistances can be combined with other thermal resistances according to the rules for adding resistances in series and in parallel.

## Example 2.1

A 5 cm (2 in.) schedule 40 steel pipe carries a heat-transfer fluid and is covered with a 2 cm layer of calcium silicate insulation to reduce the heat loss. The inside and outside pipe diameters are 5.25 cm and 6.03 cm , respectively. The fluid temperature is $150^{\circ} \mathrm{C}$, and the temperature of the exterior surface of the insulation is $25^{\circ} \mathrm{C}$. The coefficient of heat transfer between the fluid and the inner pipe wall is $700 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. Calculate the rate of heat loss per unit length of pipe.

## Solution

$$
\begin{aligned}
q_{r} & =\frac{\Delta T}{R_{t h}}=\frac{150-25}{R_{\text {th }}} \\
R_{t h} & =R_{\text {convection }}+R_{\text {pipe }}+R_{\text {insulation }} \\
R_{\text {convection }} & =\frac{1}{h A}=\frac{1}{h \pi D L}=\frac{1}{700 \times \pi \times 0.0525 \times 1}=0.008661 \mathrm{~K} / \mathrm{W} \\
R_{\text {pipe }} & =0.000513 \mathrm{~K} / \mathrm{W} \quad(\text { from Example } 1.6) \\
R_{\text {insulation }} & =1.349723 \mathrm{~K} / \mathrm{W} \quad(\text { from Example } 1.6) \\
R_{t h} & =0.008661+0.000513+1.349723=1.358897 \mathrm{~K} / \mathrm{W} \\
q_{r} & =\frac{125}{1.358897} \cong 92.0 \mathrm{~W} / \mathrm{m} \text { of pipe }
\end{aligned}
$$

Another situation involving conduction and convection is the transient heating or cooling of a solid in contact with a fluid as depicted in Figure 2.1. For the special case in which the thermal resistance within the solid is small compared with the convective resistance between the fluid and solid, temperature variations in the solid are small and can be neglected. The temperature of the solid can then be approximated as a function of time only.


Figure 2.1 Transient heat transfer between a solid and a fluid.

A thermal energy balance on the solid gives:

$$
\begin{equation*}
\text { \{rate of accumulation of thermal energy }\}=\{\text { rate of heat transfer from fluid }\} \tag{2.3}
\end{equation*}
$$

$$
\begin{gather*}
\rho v c \frac{d T}{d t}=h A_{s}\left(T_{\infty}-T\right) \\
\frac{d T}{d t}=\frac{h A_{s}}{\rho v c}\left(T_{\infty}-T\right) \tag{2.4}
\end{gather*}
$$

where $\rho, c, v$, and $A_{s}$ are, respectively, the density, heat capacity, volume, and surface area of the solid.

The solution to this linear first-order differential equation subject to the initial condition that $T=T_{0}$ when $t=0$ is:

$$
\begin{equation*}
T(t)=T_{\infty}+\left(T_{0}-T_{\infty}\right) \exp \left(-\frac{h A_{s} t}{\rho v c}\right) \tag{2.5}
\end{equation*}
$$

The approximation $T=T(t)$ is generally acceptable when the following condition is satisfied [1]:

$$
\begin{equation*}
\frac{h\left(v / A_{s}\right)}{k_{\text {solid }}}<0.1 \tag{2.6}
\end{equation*}
$$

where $k_{\text {solid }}$ is the thermal conductivity of the solid. Equation (2.5) can also be applied to the transient heating or cooling of stirred process vessels. In this case, the fluid inside the vessel is maintained at a nearly uniform temperature by the mixing. The physical properties ( $\rho$ and $c$ ) of the fluid in the vessel are used in Equation (2.5).

## Example 2.2

A batch chemical reactor operates at 400 K and the contents are well mixed. The reactor volume is $0.8 \mathrm{~m}^{3}$ with a surface area of $4.7 \mathrm{~m}^{2}$. After the reaction is complete, the contents are cooled to 320 K before the reactor is emptied. The cooling is accomplished with ambient air at 300 K and $h=75 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The agitator continues to operate during cool down. The reactor contents have a density of $840 \mathrm{~kg} / \mathrm{m}^{3}$ and a heat capacity of $2200 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{K}$. Determine the cooling time required.

## Solution

Neglect the thermal capacity of the reactor vessel and heat loss by radiation. Also, neglect the thermal resistance of the vessel wall and the convective resistance between the wall and the fluid in the reactor. Equation (2.5) is then applicable since the reactor contents remain well mixed during cooling.

$$
\begin{aligned}
T(t) & =T_{\infty}+\left(T_{0}-T_{\infty}\right) \exp \left(-\frac{h A_{s} t}{\rho v c}\right) \\
320 & =300+(400-300) \exp \left(-\frac{75 \times 4.7 t}{840 \times 0.8 \times 2200}\right) \\
t & =6,750 s \cong 1.9 h
\end{aligned}
$$

### 2.3 Extended Surfaces

An important application involving both conduction and convection is that of heat-transfer fins, also referred to as extended surfaces. Although fins come in a variety of shapes, the two most frequently used in process heat exchangers are rectangular fins (Figure 2.2) and annular (radial or transverse) fins (Figure 2.3). The basic idea behind fins is to compensate for a low heat-transfer coefficient, $h$, by increasing the surface area, $A$. Thus, fins are almost always used when heat is transferred to or from air or other gases, because heat-transfer coefficients for gases are generally quite low compared with those for liquids. Since fins usually consist of very thin pieces of metal attached to the primary heat-transfer surface (the prime surface), a relatively large amount of additional surface area is achieved with a small amount of material.
All the heat transferred by convection from the fin surface must first be transferred by conduction through the fin from its base, which is generally taken to be at the same temperature as the prime


Figure 2.2 Rectangular fin attached to a flat surface.


Figure 2.3 Annular fin attached to a tube wall.
surface. Therefore, a temperature gradient must exist along the length of the fin, and as the distance from the base of the fin increases, the temperature of the fin becomes closer to the temperature of the surrounding fluid. As a result, the $\Delta T$ for convective heat transfer decreases along the length of the fin, and hence the extended surface is less effective in transferring heat than the prime surface.
In order to calculate the rate of heat transfer from a fin, it is necessary to determine the temperature profile along the length of the fin. We consider a rectangular fin attached to a flat surface as depicted in Figure 2.2, and make a thermal energy balance on a differential volume element. The following assumptions are made:

- Steady state
- Heat transfer from fin surface by convection only (no radiation)
- No heat generation in the fin
- Constant thermal conductivity in the fin
- Negligible temperature difference across the thickness of the fin
- Negligible edge effects

The last two assumptions are justified because the fin is assumed to be very thin (like a knife blade), and made of metal (a good heat conductor). Therefore, there is very little thermal resistance between the top and bottom of the fin, and hence little temperature difference. Furthermore, the fin width, $W$, is much greater than the thickness, $t$, and so nearly all the surface area resides on the top and bottom of the fin. Hence, nearly all the convective heat transfer occurs at the top and bottom surfaces, and very little occurs at the sides and tip of the fin. The upshot of all this is that the temperature in the fin can be considered a function only of $x$, i.e., $T=T(x)$.

With steady state and no heat generation, the thermal energy balance on the control volume is simply:

$$
\begin{equation*}
\{\text { rate of thermal energy in }\}-\{\text { rate of thermal energy out }\}=0 \tag{2.7}
\end{equation*}
$$

Heat enters the control volume by conduction at position $x$, and leaves by conduction at position $x+\Delta x$ and by convection at the surface of the control volume. Thus, the balance equation can be written:

$$
\begin{equation*}
\left.\hat{q}_{x}\right|_{x} ^{\prime} A-\left.\hat{q}_{x}\right|_{\left.\right|_{x+\Delta x}} A-\hat{q}_{c v} P \Delta x=0 \tag{2.8}
\end{equation*}
$$

where

$$
\begin{aligned}
& A=W \tau=\text { fin cross-sectional area } \\
& P=2(W+\tau)=\text { fin perimeter }
\end{aligned}
$$

Note that $P \Delta x$ is the total surface area of the differential element. Dividing by $\Delta x$ and taking the limit as $\Delta x \rightarrow 0$ yields:

$$
\begin{equation*}
-A \frac{d \hat{q}_{x}}{d x}-\hat{q}_{c v} P=0 \tag{2.9}
\end{equation*}
$$

Now from Fourier's Law,

$$
\hat{q}_{x}=-k \frac{d T}{d x}
$$

and from Equation (2.1), the convective heat flux is:

$$
\begin{equation*}
\hat{q}_{c v}=h \Delta T=h\left(T-T_{\infty}\right) \tag{2.10}
\end{equation*}
$$

Substituting and utilizing the fact that $k$ is constant gives:

$$
\begin{equation*}
k A \frac{d^{2} T}{d x^{2}}-h P\left(T-T_{\infty}\right)=0 \tag{2.11}
\end{equation*}
$$

or

$$
\begin{equation*}
\frac{d^{2} T}{d x^{2}}-\frac{h P}{k A}\left(T-T_{\infty}\right)=0 \tag{2.12}
\end{equation*}
$$

Equation (2.12) can be simplified by making the following definitions:

$$
\begin{gather*}
\theta \equiv T-T_{\infty}  \tag{2.13}\\
m^{2} \equiv \frac{h P}{k A}=\frac{2 h(W+\tau)}{k W \tau} \cong \frac{2 h}{k \tau}(\text { since } \tau \ll W) \tag{2.14}
\end{gather*}
$$

(Note: The above approximation for $m^{2}$ is frequently used in practice.)
Making these substitutions and assuming that the fluid temperature, $T_{\infty}$, is a constant yields:

$$
\begin{equation*}
\frac{d^{2} \theta}{d x^{2}}-m^{2} \theta=0 \tag{2.15}
\end{equation*}
$$

This equation is subject to the following boundary conditions:

$$
\begin{align*}
& \text { 1. At } x=0, \theta=T_{s}-T_{\infty} \\
& \text { 2. At } x=L, \frac{d \theta}{d x}=0 \tag{2.16}
\end{align*}
$$

The first condition results from the assumption that the temperature at the base of the fin is equal to the prime surface temperature, $T_{s}$. The second condition follows from the fact there is very little heat transfer from the tip of the fin. Setting the heat flux at the end of the fin to zero gives $d T / d x=d \theta / d x=0$.
The general solution to Equation (2.15) can be expressed either as a sum of exponential functions or as a sum of hyperbolic functions, but the latter is more convenient in this context:

$$
\begin{equation*}
\theta=C_{1} \sinh (m x)+C_{2} \cosh (m x) \tag{2.17}
\end{equation*}
$$

Applying the boundary conditions (2.16) gives:

$$
\begin{aligned}
& C_{1}=-\left(T_{s}-T_{\infty}\right) \tanh (m L) \\
& C_{2}=T_{s}-T_{\infty}
\end{aligned}
$$

With these results, the temperature profile along the fin becomes:

$$
\begin{equation*}
T=T_{\infty}-\left(T_{s}-T_{\infty}\right)[\tanh (m L) \sinh (m x)-\cosh (m x)] \tag{2.18}
\end{equation*}
$$

To find the rate of heat transfer from the fin, note that all the heat must enter the fin by conduction at the base, where $x=0$. Therefore,

$$
\begin{equation*}
q_{f i n}=-k A \frac{d T}{d x} I_{x=0} \tag{2.19}
\end{equation*}
$$

Differentiating Equation (2.18) and evaluating at $x=0$ gives:

$$
\begin{equation*}
\left.\frac{d T}{d x}\right|_{x=0}=-m\left(T_{s}-T_{\infty}\right) \tanh (m L) \tag{2.20}
\end{equation*}
$$

Substituting into Equation (2.19) gives:

$$
q_{f i n}=k A m\left(T_{s}-T_{\infty}\right) \tanh (m L)
$$

or

$$
\begin{equation*}
q_{f i n}=(h P k A)^{1 / 2}\left(T_{s}-T_{\infty}\right) \tanh (m L) \tag{2.21}
\end{equation*}
$$

Now the maximum possible rate of heat transfer occurs when the entire fin is at the prime surface temperature, $T_{s}$ :

$$
\begin{equation*}
q_{\max }=h P L\left(T_{s}-T_{\infty}\right) \tag{2.22}
\end{equation*}
$$

The fin efficiency, $\eta_{f}$, is defined as the ratio of $q_{f i n}$ to $q_{\text {max }}$ :

$$
\eta_{f}=\frac{q_{f i n}}{q_{\max }}=\frac{(h P k A)^{1 / 2}\left(T_{s}-T_{\infty}\right) \tanh (m L)}{h P L\left(T_{s}-T_{\infty}\right)}
$$

or

$$
\begin{equation*}
\eta_{f}=\frac{\tanh (m L)}{m L} \tag{2.23}
\end{equation*}
$$

The rate of heat transfer from the fin can now be expressed in terms of the fin efficiency as:

$$
q_{f i n}=\eta_{f} q_{\max }
$$

or

$$
\begin{equation*}
q_{f i n}=\eta_{f} h A_{f i n}\left|T_{s}-T_{\infty}\right| \tag{2.24}
\end{equation*}
$$

where the surface area, $A_{f i n}$, is equal to $P L$ for the rectangular fin, and absolute value signs have been added to make $q_{f i n}$ positive regardless of the direction of heat flow.

One further modification is made to the fin equations to account (approximately) for the heat transfer from the fin tip, which was neglected in the above analysis. This is accomplished by, in effect, adding the tip area to the periphery of the fin. To this end, the fin length is increased by an amount, $\Delta L$, determined as follows:

$$
\begin{align*}
P \Delta L & =\text { tip area }=W \tau \\
\Delta L & =\frac{W \tau}{P}=\frac{W \tau}{2(W+\tau)} \cong \frac{\tau}{2} \tag{2.25}
\end{align*}
$$

The corrected length, $L_{c}$, defined by:

$$
\begin{equation*}
L_{c}=L+\Delta L=L+\frac{\tau}{2} \tag{2.26}
\end{equation*}
$$

is then used in place of $L$ in Equations (2.23) and (2.24).

The analysis of an annular fin is somewhat more complicated and the equation for fin efficiency involves Bessel functions [1,2], making it inconvenient to use. However, the following simple modification of Equation (2.23) provides a very good approximation for annular fins [3]:

$$
\begin{equation*}
\eta_{f} \cong \frac{\tanh (m \psi)}{m \psi} \tag{2.27}
\end{equation*}
$$

where
$\psi=\left(r_{2 c}-r_{1}\right)\left[1+0.35 \ln \left(r_{2 c} / r_{1}\right)\right]$
$r_{1}=$ inner radius of fin $=$ external radius of tube (prime surface)
$r_{2}=$ outer radius of fin
$r_{2 c}=r_{2}+\tau / 2=$ corrected fin radius
The rate of heat transfer from the fin is given by

$$
\begin{equation*}
q_{f i n}=2 \eta_{f} h \pi\left(r_{2 c}^{2}-r_{1}^{2}\right)\left|T_{s}-T_{\infty}\right| \tag{2.28}
\end{equation*}
$$

The factor of two in Equation (2.28) results from the fact that heat is transferred from both sides of the fin.

The total rate of heat transfer from a finned surface is the sum of the heat-transfer rates from the prime surface and from all of the fins. Thus,

$$
\begin{align*}
q & =q_{\text {prime }}+q_{\text {fins }} \\
& =h A_{\text {prime }}\left|T_{s}-T_{\infty}\right|+\eta_{f} h A_{\text {fins }}\left|T_{s}-T_{\infty}\right| \\
& =h\left[\frac{A_{\text {prime }}+\eta_{f} A_{\text {fins }}}{A_{\text {Tot }}}\right] A_{T o t}\left|T_{s}-T_{\infty}\right|  \tag{2.29}\\
q & =h \eta_{w} A_{T o t}\left|T_{s}-T_{\infty}\right| \tag{2.30}
\end{align*}
$$

where

$$
\begin{align*}
A_{\text {Tot }} & =A_{\text {prime }}+A_{\text {fins }}=\text { total heat-transfer area } \\
\eta_{w} & =\text { weighted efficiency }=\frac{A_{\text {prime }}+\eta_{f} A_{\text {fins }}}{A_{\text {Tot }}} \tag{2.31}
\end{align*}
$$

It follows from Equation (2.30) that the thermal resistance of a finned surface is:

$$
\begin{equation*}
R_{t h}=\frac{1}{h \eta_{w} A_{T o t}} \tag{2.32}
\end{equation*}
$$

This result was previously listed in Table 1.1.

## Example 2.3

A rectangular aluminum alloy (Duralumin) fin is 2 in . long, 0.1 in . thick and 40 in . wide. It is attached to a prime surface at $150^{\circ} \mathrm{F}$ and is surrounded by a fluid at $100^{\circ} \mathrm{F}$ with a heat
transfer coefficient of $75 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Calculate the fin efficiency and the rate of heat transfer from the fin.

## Solution

$$
\begin{aligned}
k & =164 \times 0.57782=94.76 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}(\text { Table A.2) } \\
m^{2} & \cong \frac{2 h}{k \tau}=\frac{2 \times 75}{94.76(0.1 / 12)}=189.95 \\
m & =\sqrt{189.95}=13.78 \mathrm{ft}^{-1} \\
L_{c} & =L+\tau / 2=\frac{2+(0.1 / 2)}{12}=0.17083 \mathrm{ft} \\
m L_{c} & =13.78 \times 0.17083=2.354
\end{aligned}
$$

Using Equation (2.23) with $L$ replaced by $L_{c}$,

$$
\eta_{f}=\frac{\tanh \left(m L_{c}\right)}{m L_{c}}=\frac{\tanh (2.354)}{2.354} \cong 0.417
$$

The rate of heat transfer from the fin is computed from Equation (2.24).

$$
\begin{aligned}
q_{f i n} & =\eta_{f} h P L_{c}\left|T_{s}-T_{\infty}\right| \\
P & =2(W+\tau)=2(40+0.1) / 12=6.6833 \mathrm{ft} \\
q_{\text {fin }} & =0.417 \times 75 \times 6.6833 \times 0.17083(150-100) \\
q_{\text {fin }} & \cong 1785 \mathrm{Btu} / \mathrm{h}
\end{aligned}
$$

## Example 2.4

A 0.1-in. thick annular Duralumin fin with an external diameter of 3 in. is attached to a tube having an external diameter of 2 in . The tube wall temperature is $150^{\circ} \mathrm{F}$ and the tube is surrounded by a fluid at $100^{\circ} \mathrm{F}$ with a heat-transfer coefficient of $75 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$.
(a) Calculate the fin efficiency and the rate of heat transfer from the fin.
(b) If the total heat-transfer surface consists of $75 \%$ fin surface and $25 \%$ prime surface, calculate the weighted efficiency of the surface.

## Solution

(a)

Tube $O D=2 \mathrm{in} . \Rightarrow r_{1}=1 \mathrm{in}$. Fin $O D=3 \mathrm{in} . \Rightarrow r_{2}=1.5 \mathrm{in}$.

$$
\begin{aligned}
r_{2 c} & =r_{2}+\tau / 2=1.5+0.1 / 2=1.55 \mathrm{in} . \\
k & =94.76 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}(\text { from Example } 2.3) \\
m & =\left(\frac{2 h}{k \tau}\right)^{0.5}=\left(\frac{2 \times 75}{94.76(0.1 / 12)}\right)^{0.5}=13.782 \mathrm{ft}^{-1} \\
\psi & =\left(r_{2 c}-r_{1}\right)\left[1+0.35 \ln \left(r_{2 c} / r_{1}\right)\right]=(1.55-1.0)[1+\ln (1.55 / 1.0)]
\end{aligned}
$$

$$
\begin{aligned}
\psi & =0.63436 \mathrm{in} .=0.7258 \mathrm{ft} \\
m \psi & =13.782 \times 0.05286=0.7258
\end{aligned}
$$

From Equation (2.27), the fin efficiency is:

$$
\eta_{f}=\frac{\tanh (m \psi)}{m \psi}=\frac{\tanh (0.7258)}{0.7258}=0.855
$$

The rate of heat transfer from the fin is given by Equation (2.28):

$$
\begin{aligned}
q_{f i n} & =2 \eta_{f} h \pi\left(r_{2 c}^{2}-r_{1}^{2}\right)\left|T_{s}-T_{\infty}\right| \\
& =2 \times 0.855 \times 75 \pi\left[(1.55 / 12)^{2}-(1.0 / 12)^{2}\right](150-100) \\
q_{f i n} & \cong 196 \mathrm{Btu} / \mathrm{h}
\end{aligned}
$$

(b) The weighted efficiency is computed from Equation (2.31):

$$
\begin{aligned}
\eta_{w} & =\left(A_{\text {prime }} / A_{\text {Tot }}\right)+\eta_{f}\left(A_{\text {fins }} / A_{\text {Tot }}\right) \\
& =0.25+0.855 \times 0.75 \\
\eta_{w} & =0.89
\end{aligned}
$$

### 2.4 Forced Convection in Pipes and Ducts

Heat transfer to fluids flowing inside pipes and ducts is a subject of great practical importance. Consequently, many correlations for calculating heat-transfer coefficients in this type of flow have been proposed. However, the correlations presented below are adequate to handle the vast majority of process heat-transfer applications. Correlations are given for each of the three flow regimes; turbulent, transition, and laminar. The physical situation described by the correlations is depicted in Figure 2.4. Fluid enters the pipe at an average temperature $T_{b 1}$ and leaves at an average temperature $T_{b 2}$. ( $T_{b}$ stands for bulk temperature. It is the fluid temperature averaged over the flow area.) The pipe wall temperature is $T_{w 1}$ at the entrance and $T_{w 2}$ at the exit. The fluid is either heated or cooled as it flows through the pipe, depending on whether the wall temperature is greater or less than the fluid temperature.


Figure 2.4 Heat transfer in pipe flow.

With respect to heat transfer in circular pipes, fully developed turbulent flow is achieved at a Reynolds number of approximately $10^{4}$. For this flow regime ( $R e \geq 10^{4}$ ), the following correlation is widely used:

$$
\begin{equation*}
N u=0.027 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \tag{2.33}
\end{equation*}
$$

where

$$
\begin{aligned}
N u & \equiv \text { Nusselt Number } \equiv h D / k \\
\operatorname{Re} & \equiv \text { Reynolds } N u m b e r \equiv D V \rho / \mu \\
\operatorname{Pr} & \equiv \text { Prandtl Number }=C_{P} \mu / k \\
D & =\text { inside pipe diameter } \\
V & =\text { average fluid velocity } \\
C_{P}, \mu, \rho, k & =\text { fluid properties evaluated at the average bulk fluid temperature } \\
\mu_{w} & =\text { fluid viscosity evaluated at average wall temperature }
\end{aligned}
$$

The average bulk fluid temperature and average wall temperature are given by:

$$
\begin{align*}
T_{b, a v e} & =\frac{T_{b 1}+T_{b 2}}{2}  \tag{2.34}\\
T_{w, a v e} & =\frac{T_{w 1}+T_{w 2}}{2} \tag{2.35}
\end{align*}
$$

Equation (2.33) is generally attributed to Seider and Tate [4], although they did not explicitly formulate it. The equation is frequently written with the coefficient 0.027 replaced by 0.023 . The latter value gives a somewhat more conservative estimate for the heat-transfer coefficient, which is often desirable for design purposes. Both coefficients will be used in this book. Although this may cause some consternation, it does reflect current practice, as both values are in common use.

Equation (2.33) is valid for fluids with Prandtl numbers between 0.5 and 17,000 , and for pipes with $L / D>10$. However, for short pipes with $10<L / D<60$, the right-hand side of the equation is often multiplied by the factor $\left[1+(D / L)^{2 / 3}\right]$ to correct for entrance and exit effects. The correlation is generally accurate to within $\pm 20 \%$ to $\pm 40 \%$. It is most accurate for fluids with low to moderate Prandtl numbers ( $0.5 \leq \operatorname{Pr} \leq 100$ ), which includes all gasses and low-viscosity process liquids such as water, organic solvents, light hydrocarbons, etc. It is less accurate for highly viscous liquids, which have correspondingly large Prandtl numbers.
For laminar flow in circular pipes ( $R e<2100$ ), the Seider-Tate correlation takes the form:

$$
\begin{equation*}
N u=1.86[\operatorname{Re} \operatorname{Pr} D / L]^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \tag{2.36}
\end{equation*}
$$

This equation is valid for $0.5<\operatorname{Pr}<17,000$ and $(\operatorname{Re} \operatorname{Pr} D / L)^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14}>2$, and is generally accurate to within $\pm 25 \%$. Fluid properties are evaluated at $T_{b, \text { ave }}$ except for $\mu_{w}$, which is evaluated at $T_{w, a v e}$. For $(\operatorname{Re} \operatorname{Pr} D / L)^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14}<2$, the Nusselt number should be set to 3.66 , which is the theoretical value for laminar flow in an infinitely long pipe with constant wall temperature. Also, at low Reynolds numbers heat transfer by natural convection can be significant (see Section 2.6 below), and this effect is not accounted for in the Seider-Tate correlation.

For flow in the transition region ( $2100<R e<10^{4}$ ), the Hausen correlation is recommended [2,5]:

$$
\begin{equation*}
N u=0.116\left[\operatorname{Re}^{2 / 3}-125\right] \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14}\left[1+(D / L)^{2 / 3}\right] \tag{2.37}
\end{equation*}
$$

Heat-transfer calculations in the transition region are subject to a higher degree of uncertainty than those in the laminar and fully developed turbulent regimes. Although industrial equipment
is sometimes designed to operate in the transition region, it is generally recommended to avoid working in this flow regime if possible. Fluid properties in Equation (2.37) are evaluated in the same manner as with the Seider-Tate correlations.

An alternative equation for the transition and turbulent regimes has been proposed by Gnielinski [6]:

$$
\begin{equation*}
N u=\frac{(f / 8)(R e-1,000) P r}{1+12.7 \sqrt{f / 8}\left(\operatorname{Pr}^{2 / 3}-1\right)}\left[1+(D / L)^{2 / 3}\right] \tag{2.38}
\end{equation*}
$$

Here, $f$ is the Darcy friction factor, which can be computed from the following explicit approximation of the Colebrook equation [7]:

$$
\begin{equation*}
f=(0.782 \ln R e-1.51)^{-2} \tag{2.39}
\end{equation*}
$$

Equation (2.38) is valid for $2100<\operatorname{Re}<10^{6}$ and $0.6<\operatorname{Pr}<2000$. It is generally accurate to within $\pm 20 \%$.

For flow in ducts and conduits with non-circular cross-sections, Equations (2.33) and (2.37)(2.39), can be used if the diameter is everywhere replaced by the equivalent diameter, $D_{e}$, where

$$
\begin{equation*}
D_{e}=4 \times \text { hydraulic radius }=4 \times \text { flow area } / \text { wetted perimeter } \tag{2.40}
\end{equation*}
$$

This approximation generally gives reliable results for turbulent flow. However, it is not recommended for laminar flow.

The most frequently encountered case of laminar flow in non-circular ducts is flow in the annulus of a double-pipe heat exchanger. For laminar annular flow, the following equation given by Gnielinski [6] is recommended:

$$
\begin{equation*}
N u=3.66+1.2\left(D_{2} / D_{1}\right)^{0.8}+\frac{0.19\left[1+0.14\left(D_{2} / D_{1}\right)^{0.5}\right]\left[\operatorname{Re} \operatorname{Pr} D_{e} / L\right]^{0.8}}{1+0.117\left[\operatorname{Re} \operatorname{Pr} D_{e} / L\right]^{0.467}} \tag{2.41}
\end{equation*}
$$

where
$D_{1}=$ outside diameter of inner pipe
$D_{2}=$ inside diameter of outer pipe
$D_{e}=$ equivalent diameter $=D_{2}-D_{1}$
The Nusselt number in Equation (2.41) is based on the equivalent diameter, $D_{e}$.
All of the above correlations give average values of the heat-transfer coefficient over the entire length, $L$, of the pipe. Hence, the total rate of heat transfer between the fluid and the pipe wall can be calculated from Equation (2.1):

$$
q=h A \Delta T_{\ln }
$$

In this equation, $A$ is the total heat-transfer surface area ( $\pi D L$ for a circular pipe) and $\Delta T_{\text {ln }}$ is an average temperature difference between the fluid and the pipe wall. A logarithmic average is used; it is termed the logarithmic mean temperature difference (LMTD) and is defined by:

$$
\begin{equation*}
\Delta T_{\ln }=\frac{\Delta T_{1}-\Delta T_{2}}{\ln \left(\Delta T_{1} / \Delta T_{2}\right)} \tag{2.42}
\end{equation*}
$$

where

$$
\begin{aligned}
& \Delta T_{1}=\left|T_{w 1}-T_{b 1}\right| \\
& \Delta T_{2}=\left|T_{w 2}-T_{b 2}\right|
\end{aligned}
$$

Like any mean value, the LMTD lies between the extreme values, $\Delta T_{1}$ and $\Delta T_{2}$. Hence, when $\Delta T_{1}$ and $\Delta T_{2}$ are not greatly different, the LMTD will be approximately equal to the arithmetic mean temperature difference, by virtue of the fact that they both lie between $\Delta T_{1}$ and $\Delta T_{2}$. The arithmetic mean temperature difference, $\Delta T_{\text {ave }}$, is given by:

$$
\begin{equation*}
\Delta T_{a v e}=\frac{\Delta T_{1}+\Delta T_{2}}{2} \tag{2.43}
\end{equation*}
$$

The difference between $\Delta T_{\mathrm{ln}}$ and $\Delta T_{\text {ave }}$ is small when the flow is laminar and $\operatorname{Re} \operatorname{Pr} D / L>10$ [8].

## Example 2.5

Carbon dioxide at 300 K and 1 atm is to be pumped through a 5 cm ID pipe at a rate of $50 \mathrm{~kg} / \mathrm{h}$. The pipe wall will be maintained at a temperature of 450 K in order to raise the carbon dioxide temperature to 400 K . What length of pipe will be required?

## Solution

Equation (2.41) may be written as:

$$
q=h A \Delta T_{\ln }=h \pi D L \Delta T_{\ln }
$$

In order to solve the equation for the length, $L$, we must first determine $q, h$, and $\Delta T_{\ln }$. The required physical properties of $\mathrm{CO}_{2}$ are obtained from Table A.10.

| Property | At $T_{b, a v e}=350 \mathrm{~K}$ | At $T_{w, a v e}=450 \mathrm{~K}$ |
| :--- | :--- | :--- |
| $\mu\left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right)$ | $17.21 \times 10^{-6}$ | $21.34 \times 10^{-6}$ |
| $C_{P}(\mathrm{~J} / \mathrm{kg} \cdot \mathrm{K})$ | 900 |  |
| $k(\mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ | 0.02047 |  |
| $\operatorname{Pr}$ | 0.755 |  |

(i)

$$
R e=\frac{D V \rho}{\mu}=\frac{4 \dot{m}}{\pi D \mu}=\frac{4 \times(50 / 3600)}{\pi \times 0.05 \times 17.21 \times 10^{-6}}=2.06 \times 10^{4}
$$

Since $R e>10^{4}$, the flow is turbulent, and Equation (2.33) is applicable.
(ii)

$$
\begin{aligned}
N u & =0.027(\operatorname{Re})^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
N u & =0.027\left(2.06 \times 10^{4}\right)^{0.8}(0.755)^{1 / 3}\left(\frac{17.21}{21.34}\right)^{0.14}=67.41 \\
h & =(k / D) N u=(0.02047 / 0.05) \times 67.41 \\
h & =27.6 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

(iii)

$$
\begin{aligned}
\Delta T_{\ln } & =\frac{\Delta T_{1}-\Delta T_{2}}{\ln \left(\Delta T_{1} / \Delta T_{2}\right)} \\
& =\frac{(450-300)-(450-400)}{\ln \left(\frac{450-300}{450-400}\right)}=\frac{100}{\ln (3)} \\
\Delta T_{\ln } & =91.02 \mathrm{~K}
\end{aligned}
$$

(iv) The rate of heat transfer, $q$, is obtained from an energy balance on the $\mathrm{CO}_{2}$.

$$
\begin{aligned}
q & =\dot{m} C_{P}(\Delta T)_{\mathrm{CO}_{2}} \\
& =\left(\frac{50}{3600}\right) \times 900 \times(400-300) \\
q & =1250 \mathrm{~W}
\end{aligned}
$$

(v)

$$
\begin{aligned}
& q=h \pi D L \Delta T_{\mathrm{ln}} \\
& L=\frac{q}{\pi D h \Delta T_{\mathrm{ln}}}=\frac{1250}{\pi \times 0.05 \times 27.6 \times 91.02}=3.17 \mathrm{~m}
\end{aligned}
$$

Checking the length to diameter ratio,

$$
L / D=\frac{3.17}{0.05}=63.4>60
$$

Hence, the correction factor for short pipes is not required. Therefore, a length of about 3.2 m is required. However, if it is important that the outlet temperature be no less than 400 K , then it is advisable to provide additional heat-transfer area to compensate for the uncertainty in the SeiderTate correlation. Thus, if the actual heat-transfer coefficient turns out to be $20 \%$ lower than the calculated value (about the worst error to be expected with the given values of $R e$ and $P r$ ), then a length of

$$
L=\frac{3.17}{0.8}=3.96 \cong 4.0 \mathrm{~m}
$$

will be required to achieve the specified outlet temperature.
When the length of the pipe is known and the outlet temperature is required, an iterative solution is usually necessary. A general calculation sequence is as follows:
(1) Estimate or assume a value of $T_{b 2}$
(2) Calculate $T_{b, \text { ave }}=\frac{T_{b 1}+T_{b 2}}{2}$ and $T_{w, a v e}=\frac{T_{w 1}+T_{w 2}}{2}$
(3) Obtain fluid properties at $T_{b, \text { ave }}$ and $\mu_{w}$
(4) Calculate the Reynolds number ( $R e=4 \dot{m} / \pi D \mu$ for a circular duct)
(5) Calculate $h$ from appropriate correlation
(6) Calculate $\Delta T_{\ln }$
(7) Calculate $q=h A \Delta T_{\text {ln }}$
(8) Calculate new value of $T_{b 2}$ from $q=\dot{m} C_{P}\left(T_{b 2}-T_{b 1}\right)$
(9) Go to Step 2 and iterate until two successive values of $T_{b 2}$ agree to within the desired accuracy.

## Example 2.6

$1000 \mathrm{lbm} / \mathrm{h}$ of oil at $100^{\circ} \mathrm{F}$ enters a 1-in. ID heated copper tube. The tube is 12 ft long and its inner surface is maintained at $215^{\circ} \mathrm{F}$. Determine the outlet temperature of the oil. The following physical property data are available for the oil:

$$
\begin{aligned}
C_{P} & =0.5 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} \\
\rho & =55 \mathrm{lbm} / \mathrm{ft}^{3} \\
\mu & =1.5 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~h} \\
k & =0.10 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

## Solution

Since the temperature dependencies of the fluid properties are not given, the properties will be assumed constant. In this case, the heat-transfer coefficient is independent of the outlet temperature, and can be computed at the outset.

$$
\begin{align*}
R e & =\frac{4 \dot{m}}{\pi D \mu}=\frac{4 \times 1000}{\pi \times 1 / 12 \times 1.5}=10,186 \Rightarrow \text { turbulent flow } \\
h & =\frac{k}{D} \times 0.027 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
h & =\frac{0.1}{(1 / 12)} \times 0.027(10,186)^{0.8}\left(\frac{0.5 \times 1.5}{0.1}\right)^{1 / 3}(1.0)  \tag{1.0}\\
h & =102 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{align*}
$$

In order to obtain a first approximation for the outlet temperature, $T_{b 2}$, we assume $\Delta T_{\ln } \cong \Delta T_{\text {ave }}$. Then,

$$
\begin{gathered}
q=\dot{m} C_{P} \Delta T_{\text {oil }}=h \pi D L \Delta T_{\text {ave }} \\
\dot{m} C_{P}\left(T_{b 2}-100\right)=h \pi D L\left[\frac{115+\left(215-T_{b 2}\right)}{2}\right]
\end{gathered}
$$

Solving for $T_{b 2}$,

$$
\begin{aligned}
1000 \times 0.05\left(T_{b 2}-100\right) & =102 \times \pi \times \frac{1}{12} \times 12 \times\left[\frac{330-T_{b 2}}{2}\right] \\
500 T_{b 2}-50,000 & =52,873-160.2 T_{b 2} \\
660.2 T_{b 2} & =102,873 \\
T_{b 2} & =155.8^{\circ} \mathrm{F}
\end{aligned}
$$

To obtain a second approximation for $T_{b 2}$, we next calculate the LMTD:

$$
\Delta T_{\ln }=\frac{115-(215-155.8)}{\ln \left(\frac{115}{215-155.8}\right)}=84^{\circ} \mathrm{F}
$$

Then,

$$
\begin{aligned}
q & =h \pi D L \Delta T_{\mathrm{ln}} \\
& =102 \times \pi \times \frac{1}{12} \times 12 \times 84 \\
q & =26,917 \mathrm{Btu} / \mathrm{h}
\end{aligned}
$$

But,

$$
\begin{aligned}
q & =\dot{m} C_{P}\left(T_{b 2}-100\right) \\
26,917 & =1000 \times 0.5\left(T_{b 2}-100\right) \\
T_{b 2} & =154^{\circ} \mathrm{F}
\end{aligned}
$$

This value is sufficiently close to the previous approximation that no further iterations are necessary.
Convergence of the iterative procedure, as given above, is often very slow, and it is then necessary to use a convergence accelerator. Wegstein's method for solving a nonlinear equation of the form $x=f(x)$ is well suited for this purpose. The new value of $T_{b 2}$ calculated in Step 8 of the iterative procedure depends on the old value of $T_{b 2}$ used in Step 2, i.e.,

$$
T_{b 2, \text { new }}=F\left(T_{b 2, o l d}\right)
$$

where the function, $F$, consists of Steps 2 through 8 . When the solution is reached, $T_{b 2 \text {,new }}=T_{b 2, o l d}$, so that:

$$
T_{b 2, \text { new }}=F\left(T_{b 2, \text { new }}\right)
$$

or

$$
T=F(T)
$$

which is the form to which Wegstein's method applies. The Wegstein iteration formula is:

$$
\begin{equation*}
T_{i+1}=T_{i}+\frac{\left(T_{i}-T_{i-1}\right)}{\left(\frac{T_{i-1}-F\left(T_{i-1}\right)}{T_{i}-F\left(T_{i}\right)}-1\right)} \tag{2.44}
\end{equation*}
$$

where $T_{i-1}, T_{i}$ and $T_{i+1}$ are three successive approximations to the outlet temperature, $T_{b 2}$.

## Example 2.7

Calculate the outlet temperature of the oil stream of Example 2.6 using Wegstein's method and an initial guess of $T_{b 2}=120^{\circ} \mathrm{F}$.

## Solution

Designate the initial approximation to the solution as $T_{0}$ and set $T_{0}=120$. A second approximation is obtained by following the iterative procedure to get a new value of $T_{b 2}$.

$$
\begin{aligned}
h & =102 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \quad(\text { from Example } 2.6) \\
\Delta T_{\mathrm{ln}} & =\frac{115-(215-120)}{\ln [115 /(215-120)]}=104.68^{\circ} \mathrm{F} \\
q & =h \pi D L \Delta T_{\ln }=102 \times \pi \times 1 / 12 \times 12 \times 104.68=33,544 \mathrm{Btu} / \mathrm{h} \\
33,544 & =q=\dot{m} C_{P}\left(T_{b 2}-T_{b 1}\right)=500\left(T_{b 2}-100\right) \\
T_{b 2} & =167.09^{\circ} \mathrm{F}
\end{aligned}
$$

Now this value becomes both $T_{1}$ and $F\left(T_{0}\right)$, i.e.,

$$
T_{1}=167.09 \text { and } F\left(T_{0}\right)=167.09
$$

To calculate $F\left(T_{1}\right)$, repeat the above calculations with $T_{1}$ as the initial guess for the outlet temperature.

$$
\begin{aligned}
\Delta T_{\ln } & =\frac{115-(215-167.09)}{\ln [115 / 215-167.09)]}=76.62^{\circ} \mathrm{F} \\
q & =h \pi D L \Delta T_{\mathrm{ln}}=102 \times \pi \times 1 / 12 \times 12 \times 76.62=24,552 \mathrm{Btu} / \mathrm{h} \\
24,552 & =q=500\left(T_{b 2}-100\right) \\
T_{b 2} & =149.10^{\circ} F=F\left(T_{1}\right)
\end{aligned}
$$

We now have the following values:

$$
\begin{array}{ll}
T_{0}=120 & F\left(T_{0}\right)=167.09 \\
T_{1}=167.09 & F\left(T_{1}\right)=149.10
\end{array}
$$

The next approximation, $T_{2}$, is obtained from Wegstein's formula:

$$
\begin{aligned}
& T_{2}=T_{1}+\frac{\left(T_{1}-T_{0}\right)}{\left[\frac{T_{0}-F\left(T_{0}\right)}{T_{1}-F\left(T_{1}\right)}-1\right]} \\
& T_{2}=167.09+\frac{(167.09-120)}{\left[\frac{120-167.09}{167.09-149.10}-1\right]}=154.07^{\circ} \mathrm{F}
\end{aligned}
$$

Next, $F\left(T_{2}\right)$ is calculated in the same manner as $F\left(\mathrm{~T}_{1}\right)$.

$$
\begin{aligned}
\Delta T_{\mathrm{ln}} & =\frac{115-(215-154.07)}{\ln [115 /(215-154.07)]}=85.12^{\circ} \mathrm{F} \\
q & =102 \times \pi \times 1 / 12 \times 12 \times 85.12=27,276 \mathrm{Btu} / \mathrm{h} \\
27,276 & =500\left(T_{b 2}-100\right) \\
T_{b 2} & =154.55^{\circ} \mathrm{F}=F\left(T_{2}\right)
\end{aligned}
$$

Applying Wegstein's formula again gives:

$$
\begin{aligned}
& T_{3}=T_{2}+\frac{\left(T_{2}-T_{1}\right)}{\left[\frac{T_{1}-F\left(T_{1}\right)}{T_{2}-F\left(T_{2}\right)}-1\right]} \\
& T_{3}=154.07+\frac{(154.07-167.09)}{\left[\frac{167.09-149.10}{154.07-154.55}-1\right]}=154.41^{\circ} \mathrm{F}
\end{aligned}
$$

Calculating $F\left(T_{3}\right)$ in the same manner as above:

$$
\begin{aligned}
\Delta T_{\mathrm{ln}} & =\frac{115-(215-154.41)}{\ln [115 /(215-154.41)]}=84.91^{\circ} \mathrm{F} \\
q & =102 \times \pi \times 1 / 12 \times 84.91=27,209 \mathrm{Btu} / \mathrm{h} \\
27,209 & =500\left(T_{b 2}-100\right) \\
T_{b 2} & =154.42^{\circ} \mathrm{F}=F\left(T_{3}\right)
\end{aligned}
$$

The results are summarized below.

| $i$ | $T_{i}$ | $F\left(T_{i}\right)$ |
| :--- | :--- | :--- |
| 0 | 120.00 | 167.09 |
| 1 | 167.09 | 149.10 |
| 2 | 154.07 | 154.55 |
| 3 | 154.41 | 154.42 |

Since $T_{3}=F\left(T_{3}\right)$ to four significant figures, the procedure has converged and the final result is $T_{b 2}=154.4^{\circ} \mathrm{F}$.

## Example 2.8

Carbon dioxide at 300 K and 1 atm is to be pumped through a duct with a $10 \mathrm{~cm} \times 10 \mathrm{~cm}$ square cross-section at a rate of $250 \mathrm{~kg} / \mathrm{h}$. The walls of the duct will be at a temperature of 450 K . What distance will the $\mathrm{CO}_{2}$ travel through the duct before its temperature reaches 400 K ?

## Solution

The required physical properties are tabulated in Example 2.5. The equivalent diameter is calculated from Equation (2.40):

$$
D_{e}=4 \times \frac{100}{40}=10 \mathrm{~cm}=0.1 \mathrm{~m}
$$

(i)

$$
\begin{gathered}
R e=\frac{D_{e} V \rho}{\mu}=\frac{D_{e} \dot{m}}{\mu A_{f}}=\frac{0.1 \times(250 / 3600)}{17.21 \times 10^{-6} \times 0.01} \text { where } A_{f}=\text { flow area }=0.01 \mathrm{~m}^{2} \\
R e=4.04 \times 10^{4} \Rightarrow \text { turbulent flow }
\end{gathered}
$$

Note that the Reynolds number is not equal to $4 \dot{m} / \pi D_{e} \mu$ for non-circular ducts. Rather the continuity equation ( $\dot{m}=\rho V A_{f}$ ) is used to express the Reynolds number in terms of mass flow rate.
(ii)

$$
\begin{aligned}
N u & =0.027 \operatorname{Re}^{0.8} P^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =0.027\left(4.04 \times 10^{4}\right)^{0.8}(0.755)^{1 / 3}\left(\frac{17.21}{21.34}\right)^{0.14} \\
N u & =115.5 \\
\frac{h D_{e}}{k} & =115.5 \\
h & =\frac{115.5 \times 0.02}{0.1}=23.1 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

(iii)

$$
\begin{aligned}
q & =\dot{m} C_{P} \Delta T_{\mathrm{co}_{2}} \\
& =(250 / 3600) \times 900 \times 100 \\
q & =6250 \mathrm{~W}
\end{aligned}
$$

(iv)

$$
\begin{aligned}
q & =h A \Delta T_{\ln }=h P L \Delta T_{\ln } \text { where } P=\text { perimeter of duct cross-section } \\
6250 & =23.1 \times 0.4 \times L \times 91.02 \\
L & =7.4 \mathrm{~m}
\end{aligned}
$$

Since $L / D_{e}=7.4 / 0.1=74>60$, no correction for entrance effects is required.

### 2.5 Forced Convection in External Flow

Many problems of engineering interest involve heat transfer to fluids flowing over objects such as pipes, tanks, buildings or other structures. In this section, correlations for several such systems are presented in order to illustrate the method of calculation. Many other correlations can be found in heat-transfer textbooks, e.g., [1,7,9-12], and in engineering handbooks.

Flow over a flat plate is illustrated in Figure 2.5. The undisturbed fluid velocity and temperature upstream of the plate are $V_{\infty}$ and $T_{\infty}$, respectively. The surface temperature of the plate is $T_{s}$ and $L$ is the length of the plate in the direction of flow. The fluid may flow over one or both sides of the plate. The heat-transfer coefficient is obtained from the following correlations [7]:

$$
\begin{equation*}
N u=0.664 R e^{l / 2} \mathrm{Pr}^{l / 3} \quad \text { for } \quad R e<5 \times 10^{5} \tag{2.45}
\end{equation*}
$$



Figure 2.5 Forced convection in flow over a flat plate.

$$
\begin{equation*}
N u=\left(0.037 R e^{0.8}-870\right) P r^{1 / 3} \text { for } R e>5 \times 10^{5} \tag{2.46}
\end{equation*}
$$

where

$$
N u=\frac{h L}{k} \quad \text { and } \quad R e=\frac{L V_{\infty} \rho}{\mu}
$$

Equation (2.45) is valid for Prandtl numbers greater than about 0.6. Equation (2.46) is applicable for Prandtl numbers between 0.6 and 60 , and Reynolds numbers up to $10^{8}$. In these equations all fluid properties are evaluated at the film temperature, $T_{f}$, defined by:

$$
\begin{equation*}
T_{f}=\frac{T_{\infty}+T_{s}}{2} \tag{2.47}
\end{equation*}
$$

The heat-transfer coefficients computed from Equations (2.45) and (2.46) are average values for the entire plate. Hence, the rate of heat transfer between the plate and the fluid is given by:

$$
\begin{equation*}
q=h A\left|T_{s}-T_{\infty}\right| \tag{2.48}
\end{equation*}
$$

where $A$ is the total surface area contacted by the fluid.
For flow perpendicular to a circular cylinder of diameter $D$, the average heat-transfer coefficient can be obtained from the correlation [13]:

$$
\begin{equation*}
N u=0.3+\frac{0.62 \operatorname{Re}^{1 / 2} \operatorname{Pr}^{1 / 3}}{\left[1+(0.4 / \operatorname{Pr})^{2 / 3}\right]^{1 / 4}}\left[1+\left(\frac{R e}{282,000}\right)^{5 / 8}\right]^{4 / 5} \tag{2.49}
\end{equation*}
$$

where

$$
N u=\frac{h D}{k}
$$

and

$$
R e=\frac{D V_{\infty} \rho}{\mu}
$$

The correlation is valid for $\operatorname{Re} \operatorname{Pr}>0.2$, and all fluid properties are evaluated at the film temperature, $T_{f}$. The rate of heat transfer is given by Equation (2.48) with $A=\pi D L$, where $L$ is the length of the cylinder.
For flow over a sphere of diameter $D$, the following correlation is recommended [14]:

$$
\begin{equation*}
N u=2+\left(0.4 R e^{1 / 2}+0.06 R e^{2 / 3}\right) \operatorname{Pr}^{0.4}\left(\frac{\mu_{\infty}}{\mu_{s}}\right)^{0.25} \tag{2.50}
\end{equation*}
$$

where

$$
N u=\frac{h D}{k}
$$

and

$$
R e=\frac{D V_{\infty} \rho}{\mu}
$$

All fluid properties, except $\mu_{s}$, are evaluated at the free-stream temperature, $T_{\infty}$. The viscosity, $\mu_{s}$, is evaluated at the surface temperature, $T_{s}$. Equation (2.50) is valid for Reynolds numbers between 3.5 and 80,000 , and Prandtl numbers between 0.7 and 380 .

For a gas flowing perpendicular to a cylinder having a square cross-section (such as an air duct), the following equation is applicable [1]:

$$
\begin{equation*}
N u=0.102 \operatorname{Re}^{0.675} \operatorname{Pr}^{1 / 3} \tag{2.51}
\end{equation*}
$$

The Nusselt and Reynolds numbers are calculated as for a circular cylinder but with the diameter, $D$, replaced by the length of a side of the square cross-section. All fluid properties are evaluated at the film temperature. Equation (2.51) is valid for Reynolds numbers in the range 5000 to $10^{5}$.

The equations presented in this (and the following) section, as well as similar correlations which appear in the literature, are not highly accurate. In general, one should not expect the accuracy of computed values to be better than $\pm 25 \%$ to $\pm 30 \%$ when using these equations. This limitation should be taken into consideration when interpreting the results of heat-transfer calculations.

## Example 2.9

Air at $20^{\circ} \mathrm{C}$ is blown over a 6 cm OD pipe that has a surface temperature of $140^{\circ} \mathrm{C}$. The free-stream air velocity is $10 \mathrm{~m} / \mathrm{s}$ What is the rate of heat transfer per meter of pipe?

## Solution

For forced convection from a circular cylinder, Equation (2.49) is applicable. The film temperature is:

$$
T_{f}=\frac{T_{s}+T_{\infty}}{2}=\frac{140+20}{2}=80^{\circ} \mathrm{C}
$$

From Table A.4, for air at $80^{\circ} \mathrm{C}$ :

$$
\begin{aligned}
v & =21.5 \times 10^{-6} \mathrm{~m}^{2} / \mathrm{s}=\text { kinematic viscosity } \\
k & =0.0293 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K} \\
\operatorname{Pr} & =0.71 \\
\operatorname{Re} & =D V_{\infty} / v=0.06 \times 10 /\left(21.5 \times 10^{-6}\right)=2.79 \times 10^{4}
\end{aligned}
$$

Substituting in Equation (2.49) gives:

$$
\begin{aligned}
N u & =0.3+\frac{0.62(27,900)^{1 / 2}(0.71)^{1 / 3}}{\left[1+\left(\frac{0.4}{0.71}\right)^{2 / 3}\right]^{1 / 4}}\left[1+\left(\frac{27,900}{282,000}\right)^{5 / 8}\right]^{4 / 5} \\
N u & =96.38 \\
h & =\frac{N u \times k}{D}=\frac{96.38 \times 0.0293}{0.06} \\
h & \cong 47 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

The rate of heat transfer is given by Equation (2.48). Taking a length of 1 m gives:

$$
\begin{aligned}
& q=h \pi D L\left(T_{s}-T_{\infty}\right) \\
& q=47 \times \pi \times 0.06 \times 1.0(140-20) \\
& q=1065 \cong 1100 \mathrm{~W} \text { per meter of pipe }
\end{aligned}
$$

## Example 2.10

A duct carries hot waste gas from a process unit to a pollution control device. The duct crosssection is $4 \mathrm{ft} \times 4 \mathrm{ft}$ and it has a surface temperature of $140^{\circ} \mathrm{C}$. Ambient air at $20^{\circ} \mathrm{C}$ blows
across the duct with a wind speed of $10 \mathrm{~m} / \mathrm{s}$. Estimate the rate of heat loss per meter of duct length.

## Solution

The film temperature is the same as in the previous example:

$$
T_{f}=\frac{140+20}{2}=80^{\circ} \mathrm{C}
$$

Therefore, the same values are used for the properties of air. The Reynolds number is based on the length of the side of the duct cross-section. Hence, we set:

$$
\begin{aligned}
D & =4 \mathrm{ft} \cong 1.22 \mathrm{~m} \\
R e & =\frac{D V_{\infty}}{v}=1.22 \times 10 /\left(21.5 \times 10^{-6}\right)=5.674 \times 10^{5}
\end{aligned}
$$

The Reynolds number is outside the range of Equation (2.51). However, the equation will be used anyway since no alternative is available. Thus,

$$
\begin{aligned}
N u & =0.102 \operatorname{Re}^{0.675} \mathrm{Pr}^{1 / 3} \\
& =0.102\left(5.674 \times 10^{5}\right)^{0.675}(0.71)^{1 / 3} \\
N u & =696.5 \\
h & =\frac{k}{D} \times 696.5 \\
h & =\frac{0.0293}{1.22} \times 696.5 \cong 16.7 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

The surface area of the duct per meter of length is:

$$
A=P L=4 \times 1.22 \times 1.0=4.88 \mathrm{~m}^{2}
$$

Finally, the rate of heat loss is:

$$
\begin{aligned}
q & =h A \Delta T \\
& =16.7 \times 4.88 \times(140-20) \\
q & \cong 9800 \mathrm{~W} / \mathrm{m} \text { of duct length }
\end{aligned}
$$

### 2.6 Free Convection

Engineering correlations for free convection heat transfer are similar in nature to those presented in the previous section for forced convection in external flows. However, in free-convection problems there is no free-stream velocity, $V_{\infty}$, upon which to base a Reynolds number. The dimensionless group that takes the place of the Reynolds number in characterizing free convection is called the Grashof number, $G r$, and is defined by:

$$
\begin{equation*}
G r=\frac{g \beta\left|T_{s}-T_{\infty}\right| L^{3}}{v^{2}} \tag{2.52}
\end{equation*}
$$

where
$g=$ gravitational acceleration;
$T_{s}=$ surface temperature;
$T_{\infty}=$ fluid temperature far from solid surface;
$L=$ characteristic length;
$\nu=\mu / \rho=$ kinematic viscosity;
$\beta=\frac{1}{\hat{v}}\left(\frac{\partial \hat{v}}{\partial T}\right)_{p}=$ coefficient of volume expansion;
$\hat{v}=$ specific volume.
For gases at low density, the ideal gas law may be used to evaluate $(\partial \hat{v} / \partial T)_{p}$ and show that:

$$
\begin{equation*}
\beta=1 / T \text { (ideal gas) } \tag{2.53}
\end{equation*}
$$

where
$T$ = absolute temperature.
For dense gases and liquids, $\beta$ can be approximated by:

$$
\begin{equation*}
\beta \cong \frac{1}{\hat{v}} \frac{\Delta \hat{v}}{\Delta T} \tag{2.54}
\end{equation*}
$$

if the specific volume (or density) is known at two different temperatures.
Free convection heat transfer from a heated vertical plate is illustrated in Figure 2.6. Fluid adjacent to the surface is heated and rises by virtue of its lower density relative to the bulk of the fluid. This rising layer of fluid entrains cooler fluid from the nearly quiescent region further from the heated surface, so that the mass flow rate of the rising fluid increases with distance along the plate. Near the bottom of the plate, the flow is laminar, but at some point, transition to turbulent flow may occur if the plate is long enough. The free-convection circulation is completed by a region of cold, sinking fluid far removed from the heated surface.


Figure 2.6 Free convection circulation pattern near a heated vertical plate.

Heat-transfer coefficients for free convection from a heated or cooled vertical plate of height $L$ can be obtained from the correlation [15]:

$$
\begin{equation*}
N u=\left\{0.825+\frac{0.387(G r P r)^{1 / 6}}{\left[1+(0.492 / P r)^{9 / 16}\right]^{8 / 27}}\right\}^{2} \tag{2.55}
\end{equation*}
$$

The characteristic length used in the Nusselt and Grashof numbers is the plate height, $L$. The fluid properties, including $\beta$, are evaluated at the film temperature, $T_{f}$, defined by Equation (2.47). Equation (2.55) is valid for $0.1 \leq G r \operatorname{Pr} \leq 10^{12}$, and is accurate to within about $\pm 30 \%$.

Equation (2.55) may also be used for free convection from vertical cylinders if the diameter-toheight ratio is greater than $\left(35 / G r^{0.25}\right)$. For smaller values of $D / L$, the effects of surface curvature become significant. However, a correction factor can be applied as follows [7]:

$$
\begin{equation*}
N u_{\text {cylinder }}=N u_{\text {plate }}\left[1+1.43\left(\frac{L}{D G r^{0.25}}\right)^{0.9}\right] \tag{2.56}
\end{equation*}
$$

where $N u_{\text {plate }}$ is the Nusselt number calculated from Equation (2.55).
For free convection from a horizontal cylinder, a correlation similar to Equation (2.55) can be used [16]:

$$
\begin{equation*}
N u=\left\{0.60+\frac{0.387(G r P r)^{1 / 6}}{\left[1+(0.559 / P r)^{9 / 16}\right]^{8 / 27}}\right\}^{2} \tag{2.57}
\end{equation*}
$$

In this case, however, the characteristic length used in the Nusselt and Grashof numbers is the diameter of the cylinder. Equation (2.57) is valid over the range $10^{-5} \leq \operatorname{Gr} \operatorname{Pr} \leq 10^{12}$. Fluid properties are evaluated at the film temperature.

For free convection from horizontal plates, the following correlations are available [17,18]:
Upper surface hot or lower surface cool:

$$
\begin{array}{ll}
N u=0.54(G r P r)^{1 / 4} & \text { for } 10^{4} \leq G r \operatorname{Pr} \leq 10^{7} \\
N u=0.15(G r P r)^{1 / 3} & \text { for } 10^{7} \leq G r \operatorname{Pr} \leq 10^{11} \tag{2.59}
\end{array}
$$

Upper surface cool or lower surface hot:

$$
\begin{equation*}
N u=0.27(G r P r)^{1 / 4} \quad \text { for } 10^{5} \leq G r P r \leq 10^{11} \tag{2.60}
\end{equation*}
$$

In these equations, fluid properties are again evaluated at the film temperature. The characteristic length used in both the Nusselt and Grashof numbers is the surface area of the plate divided by its perimeter.

For free convection from spheres, the following correlation is recommended [19]:

$$
\begin{equation*}
N u=2+\frac{0.598(G r P r)^{1 / 4}}{\left[1+(0.469 / P r)^{9 / 16}\right]^{4 / 9}}\left\{1+\frac{7.44 \times 10^{-8} G r P r}{\left[1+(0.469 / P r)^{9 / 16}\right]^{16 / 9}}\right\}^{1 / 12} \tag{2.61}
\end{equation*}
$$

The characteristic length is the sphere diameter and the correlation is valid for $\operatorname{Gr} \operatorname{Pr} \leq 10^{13}$ and $0.6 \leq \operatorname{Pr} \leq 100$. For larger values of the Prandtl number, better agreement with experimental data is
obtained by dropping the term in brackets raised to the $1 / 12$ th power. Fluid properties are evaluated at the film temperature.

Correlations for free convection heat transfer in other geometrical configurations can be found in the references cited at the end of the chapter. It should be noted that free convection effects can sometimes be significant in forced convection problems, especially in the case of laminar flow at low Reynolds numbers. The relative importance of forced and free convection effects can be determined by comparison of the Reynolds and Grashof numbers as follows:

$$
\begin{aligned}
R e^{2} / G r & \gg 1: \text { Forced convection predominates } \\
R e^{2} / G r & \cong 1: \text { Both modes of heat transfer are significant } \\
R e^{2} / G r & \ll 1: \text { Free convection predominates }
\end{aligned}
$$

Furthermore, in situations where free convection predominates, radiative heat transfer is often significant, even at relatively low temperatures. This is a consequence of the fact that heat-transfer rates in free convection are typically much lower than in forced convection.

## Example 2.11

A 12 -ounce can of beer at $80^{\circ} \mathrm{F}$ is placed on end in a refrigerator which is at $36^{\circ} \mathrm{F}$. Estimate the value of the external heat-transfer coefficient for this situation. A 12-ounce beer can has dimensions $D=2.5$ in. and $L=4.75$ in.

## Solution

It will be assumed that the refrigerator blower is not running and that the can is not in contact with any other item in the refrigerator. Under these conditions, the heat transfer will be by free convection from a vertical cylinder. We have:

$$
\begin{aligned}
T_{s} & =80^{\circ} \mathrm{F} \\
T_{\infty} & =36^{\circ} \mathrm{F} \\
T_{f} & =\frac{80+36}{2}=58^{\circ} \mathrm{F}=14.44^{\circ} \mathrm{C}
\end{aligned}
$$

From Table A.4, we find by interpolation for air at $14.44^{\circ} \mathrm{C}$ :

$$
\begin{aligned}
\frac{g \beta}{v^{2}} & =1.496 \times 10^{8} \mathrm{~K}^{-1} \mathrm{~m}^{-3} \\
k & =0.0247 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K} \\
\operatorname{Pr} & =0.71
\end{aligned}
$$

The characteristic length is the height of the cylinder, i.e.,

$$
L=4.75 \mathrm{in} .=0.1207 \mathrm{~m}
$$

Thus,

$$
\begin{aligned}
G r & =\frac{g \beta}{v^{2}}\left|T_{s}-T_{\infty}\right| L^{3} \\
& =1.496 \times 10^{8}\left(\frac{80-36}{1.8}\right)(0.1207)^{3} \\
G r & =6.430 \times 10^{6} \\
G r P r & =6.430 \times 10^{6} \times 0.71=4.566 \times 10^{6}
\end{aligned}
$$

Substituting in Equation (2.53) gives:

$$
\begin{aligned}
& N u=\left\{0.825+\frac{0.387\left(4.566 \times 10^{6}\right)^{1 / 6}}{\left[1+(0.492 / 0.71)^{9 / 16}\right]^{8 / 27}}\right\}^{2} \\
& N u=25
\end{aligned}
$$

Now,

$$
\frac{D}{L}=\frac{2.5}{4.75}=0.5263
$$

and

$$
\frac{35}{G r^{0.25}}=\frac{35}{\left(6.430 \times 10^{6}\right)^{0.25}}=0.695
$$

Therefore, Equation (2.54) should be used to correct for the effects of surface curvature.

$$
\begin{aligned}
N u_{\text {cylinder }} & =N u_{\text {plate }}\left[1+1.43\left(\frac{L}{D G r^{0.25}}\right)^{0.9}\right] \\
& =25\left[1+1.43\left(\frac{4.75}{2.5\left(6.43 \times 10^{6}\right)^{0.25}}\right)^{0.9}\right]=25[1.0749] \\
N u_{\text {cylinder }} & =26.9 \\
\frac{h L}{k} & =26.9 \\
h & =\frac{26.9 \times k}{L}=\frac{26.9 \times 0.0247}{0.1207} \cong 5.5 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} \\
h & =5.5 \times 0.17612 \cong 0.97 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

## Example 2.12

A small holding tank in a chemical plant contains a corrosive liquid that is maintained at a temperature of $120^{\circ} \mathrm{F}$ by means of an electrical heater. The heating element consists of a refractory disk 2 ft in diameter situated at the bottom of the tank. Estimate the power
required to maintain the surface of the heating element at $160^{\circ} \mathrm{F}$. The liquid properties are as follows:

| Property | At $140^{\circ} \mathrm{F}$ | At $60^{\circ} \mathrm{F}$ |
| :--- | :--- | :---: |
| $v\left(\mathrm{ft}^{2} / \mathrm{h}\right)$ | 0.023 |  |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.4 |  |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 69.3 | 70.0 |
| $\operatorname{Pr}$ | 4.8 |  |

## Solution

The heat transfer is by free convection from a horizontal plate with the upper surface hot. We first use the density data to estimate $\beta$.

$$
\begin{aligned}
\hat{v} & =1 / \rho=1 / 70=0.014286 \mathrm{ft}^{3} / \mathrm{lbm} \text { at } 60^{\circ} \mathrm{F} \\
\hat{v} & =1 / \rho=1 / 69.3=0.014430 \mathrm{ft}^{3} / \mathrm{lbm} \text { at } 140^{\circ} \mathrm{F} \\
\hat{v}_{\text {ave }} & =0.5(0.014286+0.014430)=0.014358 \mathrm{ft}^{3} / \mathrm{lbm} \\
\beta & \cong \frac{1}{\hat{v}_{\text {ave }}} \frac{\Delta \hat{v}}{\Delta T}=\frac{1}{0.014358} \times \frac{(0.014430-0.014286)}{(140-60)} \\
\beta & =0.000125\left({ }^{\circ} R\right)^{-1}
\end{aligned}
$$

Next, the characteristic length is calculated as the ratio of surface area to perimeter of the heating element.

$$
L=A_{s} / P=\frac{\pi D^{2} / 4}{\pi D}=\frac{D}{4}=\frac{2}{4}=0.5 \mathrm{ft}
$$

The Grashof number is calculated using the fluid properties at the film temperature:

$$
\begin{aligned}
T_{f} & =\frac{T_{s}+T_{\infty}}{2}=\frac{160+120}{2}=140^{\circ} \mathrm{F} \\
G r & =\frac{g \beta\left|T_{s}-T_{\infty}\right| L^{3}}{v^{2}}=\frac{4.17 \times 10^{8} \times 0.000125|160-120|(.5)^{3}}{(0.023)^{2}} \\
G r & =4.9267 \times 10^{8} \\
G r P r & =4.9267 \times 10^{8} \times 4.8=2.3648 \times 10^{9}
\end{aligned}
$$

For this value of $G r \operatorname{Pr}$, Equation (2.57) is applicable:

$$
\begin{aligned}
N u & =0.15(G r P r)^{1 / 3}=0.15\left(2.3648 \times 10^{9}\right)^{1 / 3}=199.84 \\
h & =\frac{199.84 \times k}{L}=\frac{199.84 \times 0.4}{0.5} \cong 160 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
q & =h A \Delta T=h\left(\pi D^{2} / 4\right)\left|T_{s}-T_{\infty}\right|=160 \times \frac{\pi(2)^{2}}{4}(160-120) \\
q & =20,090 \mathrm{Btu} / \mathrm{h} \\
q & =20,090 / 3412 \cong 5.9 \mathrm{~kW}
\end{aligned}
$$

## References

1. Incropera, F. P. and D. P. DeWitt, Introduction to Heat Transfer, 4th edn, John Wiley \& Sons, New York, 2002.
2. Kern, D. Q. and A. D. Krause, Extended Surface Heat Transfer, McGraw-Hill, New York, 1972.
3. McQuiston, F. C. and D. R. Tree, Optimum space envelopes of the finned tube heat transfer surface, Trans. ASHRAE, 78, 144-152, 1972.
4. Seider, E. N. and C. E. Tate, Heat transfer and pressure drop of liquids in tubes, Ind. Eng. Chem., 28, 1429-1435, 1936.
5. Hausen, H., Darstellung des Wärmeuberganges in Rohren durch Verallgemeinert Potenzbeziehungen, Z. VDI, Beih Verfahrenstech, 4, 91, 1943.
6. Gnielinski, V., Forced convection in ducts, in Heat Exchanger Design Handbook, Vol. 2, Hemisphere Publishing Corp., New York, 1988.
7. White, F. M., Heat Transfer, Addison-Wesley, Reading, MA, 1984.
8. Taborek, J., Design methods for heat transfer equipment-A critical survey of the state-of the art, in Heat Exchangers: Design and Theory Sourcebook, N. Afgan and E. U. Schlünder, eds, McGraw-Hill, New York, 1974.
9. Holman, J. P., Heat Transfer, 7th edn, McGraw-Hill, New York, 1990.
10. Kreith, F. and W. Z. Black, Basic Heat Transfer, Harper \& Row, New York, 1980.
11. Kreith, F. and M. S. Bohn, Principles of Heat Transfer, Brooks/Cole, Pacific Grove, CA, 2001.
12. Mills, A. F., Heat Transfer, 2nd edn, Prentice-Hall, Upper Saddle River, NJ, 1999.
13. Churchill, S. W. and M. Bernstein, A correlating equation for forced convection from gases and liquids to a circular cylinder in crossflow, J. Heat Transfer, 99, 300-306, 1977.
14. Whitaker, S., Forced convection heat transfer correlations for flow in pipes, past flat plates, single cylinders, single spheres, and for flow in packed beds and tube bundles, AIChE J., 18, 361-371, 1972.
15. Churchill, S. W. and H. H. S. Chu, Correlating equations for laminar and turbulent free convection from a vertical plate, Int. J. Heat Mass Transfer, 18, 1323-1329, 1975.
16. Churchill, S. W. and H. H. S. Chu, Correlating equations for laminar and turbulent free convection from a horizontal cylinder, Int. J. Heat Mass Transfer, 18, 1049-1053, 1975.
17. Fujii, T. and H. Imura, Natural convection heat transfer from a plate with arbitrary inclination, Int. J. Heat Mass Transfer, 15, 755-764, 1972.
18. Goldstein, R. J., E.M. Sparrow and D. C. Jones, Natural convection mass transfer adjacent to horizontal plates, Int. J. Heat Mass Transfer, 16, 1025-1035, 1973.
19. Churchill, S. W., Free Convection around immersed bodies, in Heat Exchanger Design Handbook, Vol. 2, Hemisphere Publishing Corp., New York, 1988.

## Notations

A Area
$A_{f i n} \quad$ Surface Area of fin
$A_{\text {prime }}$ Prime surface area
$A_{\text {Tot }} \quad$ Total area of finned surface
$A_{s} \quad$ Surface area of solid
$C_{1}, C_{2}$ Constants of integration
$C_{P} \quad$ Constant pressure heat capacity of fluid
c Specific heat of solid
$D$ Diameter
$D_{e} \quad$ Equivalent diameter
$D_{1} \quad$ Outer diameter of inner pipe of an annulus
$D_{2} \quad$ Inner diameter of outer pipe of an annulus
$f \quad$ Darcy friction factor
$g \quad$ Gravitational acceleration
Gr Grashof number
$h \quad$ Heat-transfer coefficient
$k \quad$ Thermal conductivity

| $L$ | Length of fin |
| :--- | :--- |
| $L_{c}$ | Corrected fin length |
| $m$ | $(h P / k A)^{1 / 2} \cong(2 h / k \tau)^{1 / 2}=$ Fin parameter |
| $N u$ | Nusselt number |
| $P$ | Perimeter of fin |
| $P r$ | Prandtl number |
| $q$ | Rate of heat transfer |
| $q_{r}, q_{x}$ | Rate of heat transfer in $r$ - or $x$-direction |
| $q_{f n}$ | Rate of heat transfer from a single fin |
| $q_{f i n s}$ | Rate of heat transfer from all fins on a finned surface |
| $q_{\text {max }}$ | Maximum possible rate of heat transfer from a fin |
| $q_{p r i m e}$ | Rate of heat transfer from prime surface |
| $\hat{q}$ | Heat flux |
| $\hat{q}_{c v}$ | Convective heat flux |
| $R e$ | Reynolds number |
| $R_{t h}$ | Thermal resistance |
| $r_{1}, r_{2}$ | Inner and outer radii of annular fin |
| $r_{2 c}$ | $r_{2}+\tau / 2=$ Corrected fin radius |
| $T$ | Temperature |
| $T_{b}$ | Bulk fluid temperature |
| $T_{f}$ | Film temperature |
| $T_{0}$ | Initial temperature |
| $T_{s}$ | Surface temperature |
| $T_{w}$ | Temperature of pipe wall |
| $T_{\infty}$ | Fluid temperature far from solid surface |
| $t$ | Time |
| $V$ | Fluid velocity |
| $V$ | Fluid velocity far from solid surface |
| $v$ | Volume |
| $\hat{v}$ | $v / \rho=$ Specific volume |
| $W$ | Width of fin |
| $x$ | Coordinate in Cartesian coordinate system |

## Greek Letters

$\beta \quad$ Coefficient of volume expansion
$\Delta T, \Delta x$ Difference in $T$ or $x$
$\Delta T_{\text {ave }} \quad$ Arithmetic mean temperature difference
$\Delta T_{\mathrm{ln}} \quad$ Logarithmic mean temperature difference (LMTD)
$\eta_{f} \quad$ Fin efficiency
$\eta_{w} \quad$ Weighted efficiency of finned surface
$\theta \quad T-T_{\infty}$
$\mu \quad$ Fluid viscosity
$\mu_{w} \quad$ Fluid viscosity at average temperature of pipe wall
$\mu_{\infty} \quad$ Fluid viscosity at temperature $T_{\infty}$
$\nu \quad \mu / \rho=$ Kinematic viscosity
$\rho \quad$ Density
$\tau \quad$ Fin thickness
$\psi \quad$ Parameter in equation for efficiency of annular fins

## Problems

(2.1) A pipe with an OD of 6.03 cm and an ID of 4.93 cm carries steam at $250^{\circ} \mathrm{C}$ with a heat-transfer coefficient of $200 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The pipe is covered with 2.5 cm of magnesia ( $85 \%$ ) insulation
followed by 2.5 cm of polystyrene insulation $(k=0.025 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$. The outer surface of the polystyrene is exposed to air at a temperature of $20^{\circ} \mathrm{C}$ with a heat-transfer coefficient of $10 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. What is the rate of heat loss per meter of pipe length? The resistance of the pipe wall, contact resistances and thermal radiation effects may be neglected in this problem.

Ans. $60 \mathrm{~W} / \mathrm{m}$ of pipe.
(2.1) A plastic $(k=0.5 \mathrm{~W} / \mathrm{m} \cdot K)$ pipe carries a coolant at $-35^{\circ} \mathrm{C}$ with a heat-transfer coefficient of $300 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The pipe ID is 3 cm and the OD is 4 cm . The exterior pipe surface is exposed to air at $25^{\circ} \mathrm{C}$ with a heat-transfer coefficient of $20 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. Radiative heat transfer may be neglected in this problem.
(a) Calculate the rate of heat transfer to the coolant per meter of pipe length.
(b) Calculate the temperature of the exterior pipe surface.
(c) It is desired to reduce the rate of heat transfer by $90 \%$. Will a 2 cm layer of magnesia insulation be sufficient for this purpose?

Ans. (a) $114 \mathrm{~W} / \mathrm{m}$ per meter of pipe. (b) $-20.5^{\circ} \mathrm{C}$.
(2.3) A 2 in. schedule 40 steel pipe ( $\mathrm{ID}=2.067 \mathrm{in}$., $\mathrm{OD}=2.375 \mathrm{in}$.) carries steam at $350^{\circ} \mathrm{F}$ with a heat-transfer coefficient of $50 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. The pipe is exposed to air at $70^{\circ} \mathrm{F}$ with a heattransfer coefficient of $2.0 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$. For safety reasons, as well as to conserve energy, it is desired to insulate the pipe so that the temperature of the surface exposed to air will be no greater than $120^{\circ} \mathrm{F}$. A commercial insulation vendor claims that using just $1 / 2 \mathrm{in}$. of his "high-efficiency" insulation will do the job. Is his claim correct?

## Notes:

1. The vendor's literature states that a 6 -in. thick layer of "high-efficiency" insulation has an $R$-value of 23.7.
2. The thermal resistance of the pipe wall may be neglected in this calculation. Also neglect contact resistance and thermal radiation effects.
(2.4) Suppose the steam pipe of Problem 2.3 is a 4 -in. schedule 40 steel pipe (ID $=$ $4.026 \mathrm{in} ., \mathrm{OD}=4.5 \mathrm{in}$.). What thickness of "high-efficiency" insulation will be required in this case?
(2.5) A 4-in. schedule 80 steel pipe ( $\mathrm{ID}=3.826$ in., $\mathrm{OD}=4.5$-in.) carries a heat-transfer fluid ( $T=80^{\circ} \mathrm{F}, h=200 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ ) and is covered with a $1 / 2 \mathrm{in}$. thick layer of pipe insulation. The pipe is exposed to ambient air ( $T=80^{\circ} \mathrm{F}, h=10 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ ). The insulation vendor's literature states that a 1 -in. layer of the pipe insulation has an $R$-value of 3 . Neglecting the resistance of the pipe wall and thermal radiation effects, calculate the rate of heat loss from the pipe per foot of length. Compare your answer with the result from Problem 1.19 in which convective resistances were neglected.

Ans. 423 Btu/h •ft of pipe.
(2.6) A steel pipe ( $\mathrm{ID}=2.067 \mathrm{in}$., $\mathrm{OD}=2.375 \mathrm{in}$.) is covered with a $1 / 2 \mathrm{in}$. thick layer of asbestos insulation ( $k=0.048 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) followed by a 1 -in. thick layer of fiberglass insulation $\left(k=0.022 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$. The fluid inside the pipe is at $600^{\circ} \mathrm{F}$ with $h=100 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$, and the exterior surface of the fiberglass insulation is exposed to air at $100^{\circ} \mathrm{F}$ with $h=5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$. Calculate the rate of heat loss per foot of pipe length. How does your answer compare with the result from Problem 1.22 in which the convective resistances were neglected?
(2.7) Consider again the building wall of Problem 1.23. Suppose the interior surface is exposed to air at $70^{\circ} \mathrm{F}$ with $h=10 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ while the exterior surface is exposed to air at $30^{\circ} \mathrm{F}$ with $h=25 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Calculate the rate of heat loss for this situation and compare with the result from Problem 1.23 in which the convective resistances were neglected.

Ans. $21,300 \mathrm{Btu} / \mathrm{h}$.
(2.8) A consulting firm has designed a steam system for a new process unit at your plant. Superheated steam is delivered to the unit via a 3-in. steel pipe that has an ID of 3.068 in . and an OD of 3.5 in . The steam is at $800^{\circ} \mathrm{F}$ with a heat-transfer coefficient of $100 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. The pipe is covered with a $1 / 2$-in. thick layer of Type I insulation having an $R$-value of 1 , followed by a 1 -in. thick layer of Type II insulation having an $R$-value of 4 . The steam line will be exposed to ambient air at $80^{\circ} \mathrm{F}$ with a heat-transfer coefficient of $5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Design specifications call for the external surface temperature of the insulation to be no greater than $110^{\circ} \mathrm{F}$, and the manufacturer's literature states that Type I insulation is suitable for temperatures up to $1200^{\circ} \mathrm{F}$, while Type II insulation is suitable for temperatures up to $500^{\circ} \mathrm{F}$. Your job is to evaluate the consulting firm's design. Proceed as follows:
(a) Calculate the rate of heat loss from the steam line per foot of pipe length that will actually occur if the consulting firm's design is implemented.
(b) Calculate the appropriate temperatures needed to determine whether or not all design and material specifications have been met.
(c) State whether or not the consulting firm's design is acceptable and the reason(s) for your conclusion.

In these calculations, neglect the thermal resistance of the pipe wall, contact resistances, and radiation effects.
(2.9) Consider again the underground waste gas duct of Problem 1.27. If the heat-transfer coefficient for the waste gas is $25 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$, calculate the rate of heat loss from the waste gas per foot of duct length.

Ans. $880 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}$ of length.
(2.10) Consider again the industrial chimney of Problem 1.25. The heat-transfer coefficient for the flue gas is $25 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ and the ambient air surrounding the chimney is at $60^{\circ} \mathrm{F}$ with $h=10 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} . \circ \mathrm{F}$. Calculate the rate of heat loss from the flue gas per foot of chimney height.

Ans. $1100 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}$ of height.
(2.11) A graphite heat exchanger is constructed by drilling circular channels in a solid block of graphite. Consider a large graphite block ( $k=800 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ) containing two 1in. diameter channels spaced 2 in . apart (center-to-center). A highly corrosive liquid ( $T=350^{\circ} \mathrm{F}, h=120 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ ) flows through one channel and a coolant ( $T=170^{\circ} \mathrm{F}$, $h=200 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ ) flows in the other channel. Calculate the rate of heat transfer from the corrosive liquid to the coolant per foot of exchanger length.
Ans. $3470 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}$ of length.
(2.12) A highly corrosive liquid is cooled by passing it through a circular channel with a diameter of 5 cm drilled in a rectangular block of graphite $(k=800 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$. Ambient air is blown over the exterior of the block as shown in the sketch below. The heat-transfer coefficient for the air is $100 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$, based on the total exterior surface area of the block. Calculate the rate of heat loss from the liquid per meter of channel length.
Ans. 10,500 W.

(2.13) A pipeline to transport chilled water from the utility building to a process unit is being designed at a chemical plant. The steel pipe will have an ID of 7.8 cm , an OD of 8.9 cm , and will be buried with its centerline at a depth of 0.92 m . Chilled water will enter the pipe at 285 K with a flow rate of $1.2 \mathrm{~kg} / \mathrm{s}$. The rate of heat transfer to the water is to be calculated to determine if the pipe will require insulation. For design purposes, the ground surface temperature is assumed to be 335 K and the pipe is assumed to be uninsulated. The process unit is located 40 m from the utility building.
(a) Make a reasonable guess for the pipe wall temperature and use it to calculate the heat-transfer coefficient for the water.
(b) Use the heat-transfer coefficient found in part (a), together with the design value for ground surface temperature, to calculate the rate of heat transfer to the water per meter of pipe length. (Do not use the wall temperature assumed in part (a) for this calculation because it was just a guess. The correct value for $T_{w}$ is unknown.)
(c) Use the result of part (b) to find the temperature of the water delivered to the process unit.
(d) Check the value assumed for $T_{w}$ in part (a) by calculating the pipe wall temperature. Is the difference between assumed and calculated values large enough to warrant further iteration?
(2.14) Chromium steel ( $\rho=7836 \mathrm{~kg} / \mathrm{m}^{3}, c=520 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{K}, k=45 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ) ball bearings are to be heat treated by heating to $300^{\circ} \mathrm{C}$ followed by immersion in a quenching bath which is maintained at $40^{\circ} \mathrm{C}$. The heat-transfer coefficient between the bearings and the quenching fluid is estimated to be $300 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$, and the bearings are 4.0 cm in diameter.
(a) How long should the bearings be quenched to cool them to $80^{\circ} \mathrm{C}$ ?
(b) The quenching bath consists of unused engine oil. Is the value given for the heattransfer coefficient in the problem statement reasonable? Give calculations to support your answer.

Ans. (a) 170 s .
(2.15) At 7:15 PM a process upset at a chemical plant resulted in the accidental release of a hazardous material to the atmosphere. The process was shut down, and an inspection revealed a faulty heater on a holding tank in the process. The tank holds a chemical intermediate which is normally maintained at $300^{\circ} \mathrm{F}$ by the heater, and a mechanical agitator keeps the temperature uniform throughout the tank. It is known that if the temperature of the intermediate drops below $100^{\circ} \mathrm{F}$, the process will not operate properly. Hence, it is postulated that a failed heater is the cause of the accidental release. Plant records show that the heater was operating normally at the start of the second shift (4:00 PM). The ambient temperature
at the time of the accident was $50^{\circ} \mathrm{F}$, and the heat-transfer coefficient between the ambient air and the tank is estimated to have been $10 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Properties of the chemical intermediate and tank dimensions are given below. Are the data consistent with the hypothesis that the failed heater caused the process upset?

| Chemical intermediate properties | Cylindrical tank dimensions |
| :--- | :--- |
| $\rho=50 \mathrm{lbm} / \mathrm{ft}^{3}$ | $D=10 \mathrm{ft}$ |
| $C_{P}=0.5 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ | Height $=15 \mathrm{ft}$ |
| $k=0.1 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ |  |

Notes:
(1) The agitator did not fail, so the temperature in the tank remained uniform at all times.
(2) The bottom of the tank sits on a concrete pad, so assume heat transfer through the side and top of the tank only.
(2.16) A prilling tower is a device which converts a liquid into a granular solid. The liquid is formed into droplets by forcing it through nozzles at the top of the tower. As the droplets fall under gravity, they are contacted by air blown upward through the tower. The droplets cool and solidify as they fall, and the solid particles are collected at the bottom of the tower. A key design parameter for a prilling tower is the time required for a droplet to cool and solidify.

In a new chemical process, the liquid organic chemical product will be fed to a prilling tower at $130^{\circ} \mathrm{C}$. Preliminary design parameters include a droplet diameter of 6 mm , an air temperature of $30^{\circ} \mathrm{C}$, and a heat-transfer coefficient of $40 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ between air and droplet. The organic chemical has the following properties:

```
Melting point \(=122^{\circ} \mathrm{C}\)
Liquid density \(=1.3 \mathrm{~g} / \mathrm{cm}^{3}\)
Heat capacity \(=1,460 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{K}\)
Thermal conductivity \(=0.42 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}\)
Latent heat of melting \(=180 \mathrm{~J} / \mathrm{g}\)
```

(a) Calculate $h\left(v / A_{s}\right) / k$ for a droplet. Is $T=T(t)$ a valid approximation for a droplet?
(b) Determine the time required for a droplet to reach the melting point.
(c) After the droplet has reached the melting point, estimate the additional time required for complete solidification of the droplet. Neglect any effect of changes in physical properties as solidification occurs.
(d) Is the specified value of $40 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ for the heat-transfer coefficient reasonable? Assume a relative velocity of $10 \mathrm{~m} / \mathrm{s}$ between air and droplets, and give calculations to support your answer.

Ans. (a) 0.095 . (b) 4 s . (c) 64 s .
(2.17) A rectangular steel $(k=58.7 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ fin 25 mm thick and 150 mm long is attached to a wall that is at $250^{\circ} \mathrm{C}$. The ambient air around the fin is at $20^{\circ} \mathrm{C}$ and the heat-transfer coefficient is $26 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. Calculate:
(a) The fin efficiency.
(b) The rate of heat transfer from the fin per meter of fin width.

Ans. (a) $77.9 \%$. (b) $1456 \mathrm{~W} / \mathrm{m}$ of width.
(2.18) A rectangular fin 1.0 ft long, 1.0 ft wide and 2 in . thick loses heat to the atmosphere at $70^{\circ} \mathrm{F}$. The base of the fin is at $270^{\circ} \mathrm{F}$. If $h=2 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ and the thermal conductivity of the fin is $24 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$, find:
(a) The fin efficiency.
(b) The total rate of heat loss from the fin.

Ans. (a) $70.9 \%$. (b) $709 \mathrm{Btu} / \mathrm{h}$.
(2.19) An annular stainless steel $(k=16.6 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ fin of thickness 5 mm and outside diameter 3 cm is attached to a $1-\mathrm{cm}$ OD tube. The fin is surrounded by a fluid at $50^{\circ} \mathrm{C}$ with a heattransfer coefficient of $40 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The tube wall temperature is $150^{\circ} \mathrm{C}$. Calculate:
(a) The fin efficiency.
(b) The rate of heat transfer from the fin.

Ans. (a) $91 \%$ (b) 6.4 W .
(2.20) The inner pipe of a double-pipe heat exchanger has an OD of 1.9 in . and contains 36 rectangular fins of the type shown in the sketch below. The fins are made of steel ( $k=34.9 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) and are 0.5 in . high and $0.035-\mathrm{in}$. thick. The pipe wall temperature is $250^{\circ} \mathrm{F}$ and the fluid in the annulus surrounding the fins is at $150^{\circ} \mathrm{F}$ with a heat-transfer coefficient of $30 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Calculate:
(a) The fin efficiency.
(b) The rate of heat transfer from one fin per foot of pipe length.
(c) The prime surface area per foot of pipe length.
(d) The rate of heat transfer from the prime surface per foot of pipe length.
(e) The weighted efficiency of the finned surface.
(f) The total rate of heat transfer (from fins and prime surface).
(g) The heat duty for the exchanger is $390,000 \mathrm{Btu} / \mathrm{h}$. What length of pipe is required to satisfy this duty?

Ans. (a) $75 \%$.
(b) $194 \mathrm{Btu} / \mathrm{h}$.
(c) $0.3924 \mathrm{ft}^{2}$.
(d) $1177 \mathrm{Btu} / \mathrm{h}$.
(e) $77.8 \%$.
(f) $8.160 \mathrm{Btu} / \mathrm{h}$.
(g) 48 ft .
(2.21) A carbon steel $(k=45 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ heat exchanger tube has an outside diameter of 2.4 cm and contains 630 annular fins per meter of length. Each fin extends 0.16 cm beyond the exterior tube wall and has a thickness of 0.04 cm . The fluid surrounding the tube is at $25^{\circ} \mathrm{C}$ and the heat-transfer coefficient is $1200 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The tube wall temperature is $100^{\circ} \mathrm{C}$. Determine:
(a) The fin efficiency.
(b) The surface area of the fins per meter of tube length.
(c) The prime surface area per meter of tube length.
(d) The weighted efficiency of the finned surface.
(e) The rate of heat transfer from the fins per meter of tube length.
(f) The rate of heat transfer from the prime surface per meter of tube length.
(g) The total rate of heat transfer per meter of tube length.
Ans. (a) $86.7 \%$.
(b) $0.183828 \mathrm{~m}^{2}$.
(c) $0.056398 \mathrm{~m}^{2}$.
(d) $89.8 \%$.
(e) $14,344 \mathrm{~W}$.
(f) 5076 W .
(g) $19,420 \mathrm{~W}$.
(2.22) Annular steel fins ( $k=56.7 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ) are attached to a steel tube that is 30 mm in external diameter. The fins are 2 mm thick and 15 mm long. The tube wall temperature is 350 K and the surrounding fluid temperature is 450 K with a heat-transfer coefficient of $75 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. There are 200 fins per meter of tube length. Calculate:
(a) The fin efficiency.
(b) The fin surface area per meter of tube length.
(c) The prime surface area per meter of the tube length.
(d) The weighted efficiency of the finned surface.
(e) The rate of heat transfer per meter of tube length.

Ans. (a) $85 \%$.(b) $0.9248 \mathrm{~m}^{2}$. (c) $0.0565 \mathrm{~m}^{2}$. (d) $86 \%$. (e) 6330 W .
(2.23) A finned heat exchanger tube is made of aluminum alloy ( $k=186 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ) and contains 125 annular fins per meter of tube length. The bare tube between fins has an OD of 50 mm . The fins are 4 mm thick and extend 15 mm beyond the external surface of the tube. The outer surface of the tube will be at $200^{\circ} \mathrm{C}$ and the tube will be exposed to a fluid at $20^{\circ} \mathrm{C}$ with a heat-transfer coefficient of $40 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. Calculate:
(a) The rate of heat transfer per meter of tube length for a plain (un-finned) tube.
(b) The fin efficiency.
(c) The fin and prime surface areas per meter of tube length.
(d) The weighted efficiency of the finned surface.
(e) The rate of heat transfer per meter of tube length for a finned tube.
(f) If the cost per unit length of finned tubing is 25\% greater than for plain tubing, determine whether plain or finned tubing is more economical for this service.

Ans. (a) 1130 W.
$\begin{array}{lll}\text { (d) } 98.7 \% & \text { (b) } 98.6 \% & \text { (e) } 0.890 \mathrm{~W} .\end{array}$
(2.24) A stream of ethylene glycol having a flow rate of $1.6 \mathrm{~kg} / \mathrm{s}$ is to be cooled from 350 to 310 K by pumping it through a $3-\mathrm{cm}$ ID tube, the wall of which will be maintained at a temperature of 300 K . What length of tubing will be required?

Ans. 49 m .
(2.25) A small steam superheater will be made of $3 / 4$-in. schedule 80 stainless steel pipe which will be exposed to hot flue gas from a boiler. $50 \mathrm{lbm} / \mathrm{h}$ of saturated steam at $320^{\circ} \mathrm{F}$ will enter the pipe and be heated to $380^{\circ} \mathrm{F}$. Assuming that the pipe wall temperature will vary from $375^{\circ} \mathrm{F}$ at the steam inlet to $415^{\circ} \mathrm{F}$ at the outlet, calculate the length of pipe required for the superheater.

Ans. 6.1 ft .
(2.26) Suppose that the steam superheater of Problem 2.25 has a length of 10 ft and the wall temperature is constant at $415^{\circ} \mathrm{F}$ over the entire length of the pipe. Using the value of the heat-transfer coefficient calculated in Problem 2.24, estimate the temperature of the steam leaving the superheater.

Ans. $405^{\circ} \mathrm{F}$.
(2.27) A gas heater shown below in cross-section consists of a square sheet metal duct insulated on the outside. A 5 cm OD steel pipe passes through the center of the duct and the pipe wall is maintained at $250^{\circ} \mathrm{C}$ by condensing steam flowing through the pipe. Air at $20^{\circ} \mathrm{C}$ will be fed to the heater at a rate of $0.35 \mathrm{~kg} / \mathrm{s}$.
(a) Calculate the equivalent diameter for the heater.
(b) Calculate the length of the heater required to heat the air stream to $60^{\circ} \mathrm{C}$.

Ans. (a) $D_{e}=0.1083 \mathrm{~m}$. (b) 8.1 m .

(2.28) Water at $20^{\circ} \mathrm{C}$ with a mass flow rate of $1.0 \mathrm{~kg} / \mathrm{s}$ enters an annulus formed by an inner pipe having an OD of 2.5 cm and an outer pipe having an ID of 10 cm . The wall temperature of the inner pipe varies from $80^{\circ} \mathrm{C}$ at the inlet to $100^{\circ} \mathrm{C}$ at the outlet. The outer surface of the outer pipe is well insulated. Calculate the length of the annulus required to heat the water to $75^{\circ} \mathrm{C}$.

Ans. 75.3 m .
(2.29) A stream of ethylene glycol having a flow rate of $4000 \mathrm{lb} / \mathrm{h}$ is to be heated from $17^{\circ} \mathrm{C}$ to $37^{\circ} \mathrm{C}$ by passing it through a circular annular heater. The outer pipe of the annulus will have an ID of 5 cm and the inner pipe will have an OD of 4 cm . The exterior surface of the outer pipe will be well insulated, while the inner pipe wall temperature will vary from $67^{\circ} \mathrm{C}$ at the entrance to $87^{\circ} \mathrm{C}$ at the exit. The required length of the heater is desired. Assuming as a first approximation that $L=20 \mathrm{~m}$, calculate a second approximation for the length.

Ans. 20.8 m .
(2.30) $100 \mathrm{lbm} / \mathrm{h}$ of oil at $130^{\circ} \mathrm{F}$ is needed for a process modification. The oil will be available at $70^{\circ} \mathrm{F}$, so a plant engineer has designed a heater consisting of a $1-\mathrm{in}$. ID tube, 10 ft long, the wall of which will be maintained at $215^{\circ} \mathrm{F}$ by condensing steam. Will the heater work as required? Properties of the oil may be assumed constant at the following values:

$$
\begin{array}{rlrl}
C_{P} & =0.49 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} \quad \mu & =1.42 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~h} \\
k & =0.0825 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F} & \rho & =55 \mathrm{lbm} / \mathrm{ft}^{3}
\end{array}
$$

(2.31) A stream of Freon- 12 with a flow rate of $4000 \mathrm{lb} / \mathrm{h}$ is to be heated from $-20^{\circ} \mathrm{C}$ to $30^{\circ} \mathrm{C}$ for use in a chemical processing operation. Available for this service is an annular heater 3.05 m in length. The outer pipe of the annulus has an ID of 5 cm and an O.D. of 5.5 cm . The inner pipe has an ID of 3.75 cm and an OD of 4 cm . When in operation, the walls of both pipes are maintained at a constant temperature that can be set to any value between $30^{\circ} \mathrm{C}$ and $70^{\circ} \mathrm{C}$. Will the heater be suitable for this service?
(2.32) A feed stream to a chemical reactor consists of $0.2 \mathrm{~kg} / \mathrm{s}$ of ammonia vapor at 300 K . Prior to entering the reactor, the ammonia is preheated by passing it through a rectangular duct whose walls are heated to 500 K by hot process waste gas. The duct cross-section is 9 cm by 20 cm , and it is $2.5-\mathrm{m}$ long. At what temperature does the ammonia enter the reactor?
(2.33) An air preheater is required to heat $0.2 \mathrm{~kg} / \mathrm{s}$ of process air from $15^{\circ} \mathrm{C}$ to $115^{\circ} \mathrm{C}$. The preheater will be constructed from rectangular ducting having a cross-section of 7.5 cm by 15 cm . The air will flow inside the duct and the duct walls will be maintained at $250^{\circ} \mathrm{C}$ by hot flue gas. What length of ducting will be required?
(2.34) A cylindrical storage tank with a diameter of 4 m and a length of 10 m will hold a fluid whose temperature must be maintained at 347 K . In order to size the heater required for the tank, the following worst-case scenario is considered:

Ambient air temperature $=-20^{\circ} \mathrm{C}$
Wind speed $=20 \mathrm{~m} / \mathrm{s}$
Tank wall temperature $=347 \mathrm{~K}$
What size ( kW ) heater will be needed?
Ans. 400 kW .
(2.35) A viscous liquid is to be pumped between two buildings at a chemical plant in an aboveground pipe that has an OD of 22 cm and is 110 m long. To facilitate pumping, the liquid will be heated to $40^{\circ} \mathrm{C}$ in order to reduce its viscosity. The liquid flow rate will be $20 \mathrm{~kg} / \mathrm{s}$ and the specific heat of the liquid is $1300 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{K}$. Determine the temperature drop that the liquid will experience over the length of the pipe under the following worst-case conditions:

Ambient air temperature $=-10^{\circ} \mathrm{C}$
Wind speed $=14 \mathrm{~m} / \mathrm{s}$
Pipe surface temperature $=37^{\circ} \mathrm{C}$
Ans. $5.7^{\circ} \mathrm{C}$.
A surge tank to be used in a chemical process is spherical in shape with a diameter of 10 ft . The tank will hold a liquid that must be maintained at $180^{\circ} \mathrm{F}$ by means of a heating unit. The following parameters have been established for design purposes:

Ambient air temperature $=20^{\circ} \mathrm{F}$
Wind speed $=20$ miles $/ \mathrm{hr}$.
Tank wall temperature $=180^{\circ} \mathrm{F}$
(a) Estimate the duty $(\mathrm{Btu} / \mathrm{h})$ that the heater must supply.
(b) Comment on the probable accuracy of your estimate.

Ans. (a) $88,500 \mathrm{Btu} / \mathrm{h}$.
(2.37) A duct is being designed to transport waste gas from a processing unit to a pollution control device. The duct will be 5 ft high, 6 ft wide, and 100 ft long. In order to determine
whether the duct will need to be insulated, the rate of heat loss to the environment must be estimated. Based on the following design conditions, compute the rate of heat loss from the duct.

Average duct surface temperature $=250^{\circ} \mathrm{F}$
Ambient air temperature $=10^{\circ} \mathrm{F}$
Wind speed $=20 \mathrm{miles} / \mathrm{hr}$.
Ans. $1.4 \times 10^{6} \mathrm{Btu} / \mathrm{h}$.
(2.38) A pipeline at a chemical complex has an OD of 10 cm , an ID of 9.4 cm , and is covered with a layer of insulation ( $k=0.055 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ) that is $4-\mathrm{cm}$ thick. A process liquid at $50^{\circ} \mathrm{C}$ flows in the pipeline with a heat-transfer coefficient of $400 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$. The pipeline is exposed to the environment on a day when the air temperature is $-20^{\circ} \mathrm{C}$ and the wind speed is $15 \mathrm{~m} / \mathrm{s}$. What is the rate of heat loss from the pipeline per meter of length?
Ans. 40 W.
(2.39) Consider again the graphite heat exchanger of Problem 2.12. What air velocity is required to achieve the stated heat - transfer coefficient of $100 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ ?
(2.40) An energy recovery system is being considered to preheat process air using hot flue gas. The process requires air at $80^{\circ} \mathrm{C}$. In the proposed energy recovery system, air at $25^{\circ} \mathrm{C}$ will enter a rectangular duct with a flow rate of $2 \mathrm{~kg} / \mathrm{s}$. The duct dimensions are $1 \mathrm{~m} \times 2 \mathrm{~m} \times 6 \mathrm{~m}$ long. The duct walls will be maintained at a temperature of $250^{\circ} \mathrm{C}$ by hot flue gas flowing over the outside of the duct. Estimate the air temperature that will be achieved with this system and thereby determine whether or not the energy recovery system will satisfy the process requirement.
(2.41) The surface temperature of the electronic chip shown below is $75^{\circ} \mathrm{C}$ and it is surrounded by ambient air at $25^{\circ} \mathrm{C}$. Calculate the rate of heat loss by natural convection from the upper surface of the chip.
Ans. 0.178 W.

(2.42) A petrochemical storage tank is cylindrical in shape with a diameter of 6 m and a height of 10 m . The surface temperature of the tank is $10^{\circ} \mathrm{C}$ when, on a calm clear night, the air temperature drops rapidly to $-10^{\circ} \mathrm{C}$. Estimate the rate of heat loss from the tank under these conditions.
(2.43) A horizontal elevated pipeline in a chemical plant has an OD of 10 cm , an ID of 9.4 cm , and is covered with a layer of magnesia insulation that is $4-\mathrm{cm}$ thick. A process liquid at $50^{\circ} \mathrm{C}$ flows in the pipeline with a heat-transfer coefficient of $400 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The pipeline is exposed to the environment on a calm night when the air temperature is $-5^{\circ} \mathrm{C}$.
(a) Make a reasonable guess for the temperature of the exterior surface of the insulation and use it to calculate the heat-transfer coefficient between the insulation and the ambient air.
(b) Use the result of part (a) together with the other information given in the problem to calculate the rate of heat loss per meter of pipe length.
(c) Use the result of part (b) to calculate the temperature of the exterior surface of the insulation and compare it with the value that you assumed in part (a).
(2.44) A spherical storage tank has a diameter of 5 m . The temperature of the exterior surface of the tank is $10^{\circ} \mathrm{C}$ when, on a calm clear night, the air temperature drops rapidly to $-10^{\circ} \mathrm{C}$. Estimate the rate of heat loss from the tank under these conditions.

Ans. 5550 W.
(2.45) At a convective boundary such as the one at $x=B$ in the sketch below, heat is transferred between a solid and a fluid. In order for a finite temperature to exist at the solid-fluid interface, the rate at which heat is transferred to the interface by conduction through the solid must equal the rate at which heat is transferred away from the interface by convection in the fluid. The reason is that the interface has no volume and no mass, and so has zero heat capacity. The boundary condition at $x=L$ is thus:

$$
\begin{aligned}
& \hat{q}_{\text {conduction }}=\hat{q}_{\text {convection }} \\
& -k \frac{d T}{d x}=h\left(T-T_{\infty}\right) \\
& h\left(T-T_{\infty}\right)+k \frac{d T}{d x}=0
\end{aligned}
$$

Expressions for both T and $d T / d x$ (obtained by integration of the conduction equation) are substituted into this equation to obtain a relationship between the constants of integration.


The rectangular solid shown above is insulated on all sides except the one at $x=B$, which is exposed to a fluid at temperature $T_{\infty}$ with heat-transfer coefficient, $h$. Heat is generated within the solid at a rate per unit volume given by $\dot{q}=\Gamma x$, where $\Gamma$ is a constant.
(a) Assuming constant thermal conductivity, derive an expression for the steady-state temperature distribution, $T(x)$, in the solid.
(b) Calculate the temperature of the insulated boundary at $x=0$ for the following parameter values:

$$
\begin{array}{rlrl}
T_{\infty} & =20^{\circ} \mathrm{C} & k & =1.5 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K} \quad \Gamma=50 \mathrm{~W} / \mathrm{m}^{4} \\
B & =2 \mathrm{~m} & \mathrm{~h} & =30 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{array}
$$

Ans. (a) $T(x)=T_{\infty}+\frac{\Gamma B^{2}}{2 h}+\frac{\Gamma}{6 k}\left(B^{3}-x^{3}\right) . \quad$ (b) $67.8^{\circ} \mathrm{C}$.
(2.46) Consider the rectangular solid shown below that is insulated on four sides. The side at $x=B$ is held at a fixed temperature, $T_{w}$, while the side at $x=0$ is exposed to a fluid at temperature $T_{\infty}$. Heat is generated within the wall at a rate per unit volume given by $\dot{q}=\Gamma x$, where $\Gamma$ is a constant. The thermal conductivity of the solid may be assumed constant.
(a) Formulate an appropriate set of boundary conditions for this configuration.
(b) Use the conduction equation to derive an expression for the steady-state heat flux, $\hat{q}_{x}$, in the solid.


Ans. (b) $\hat{q}_{x}=\frac{\Gamma x^{2}}{2}+\frac{h\left\{k\left(T_{\infty}-T_{w}\right)-\Gamma B^{3} / 6\right\}}{(k+B h)}$.
(2.47) A long solid cylindrical rod of radius R contains a heat source that generates heat per unit volume at a rate $\dot{q}=\Gamma r$, where $\Gamma$ is a constant and $r$ is radial position measured from the centerline. The rod is completely surrounded by a fluid at temperature $T_{\infty}$ with heat-transfer coefficient, $h$. Assuming heat flow only in the radial direction:
(a) Formulate an appropriate set of boundary conditions to be used with the heat conduction equation.
(b) Derive an expression for the steady-state temperature profile, $T(r)$, in the rod. State any assumptions that you make in your derivation.
(c) Obtain an expression for the maximum temperature in the rod at steady state.

Ans. (b) $T(r)=T_{\infty}+\frac{\Gamma R^{2}}{3 h}+\frac{\Gamma\left(R^{3}-r^{3}\right)}{9 k}$.
(2.48) Repeat Problem 2.47 for a heat source of the form $\dot{q}=\Gamma / r$.

Ans. (b) $T(r)=T_{\infty}+\Gamma / h+(\Gamma / k)(R-r)$.
(2.49) A long hollow cylinder has inner and outer radii $R_{1}$ and $R_{2}$, respectively. Heat is generated in the cylinder wall at a uniform rate, $\Gamma$, per unit volume. The outer surface of the cylinder is well insulated. A fluid flows through the inside of the cylinder to provide cooling. The
fluid temperature is $T_{\infty}$ and the heat-transfer coefficient is $h$. Assuming constant thermal conductivity, $k$, derive an expression for the steady-state temperature profile, $T(r)$, in the cylinder wall.
Ans. $T(r)=T_{\infty}+\frac{\Gamma\left(R_{2}^{2}-R_{1}^{2}\right)}{2 h R_{1}}+\frac{\Gamma\left(R_{1}^{2}-r^{2}\right)}{4 k}+\frac{\Gamma R_{2}^{2} \ln \left(r / R_{1}\right)}{2 k}$.
(2.50) A solid sphere of radius $R$ is immersed in a fluid with temperature $T_{\infty}$ and heat-transfer coefficient $h$. Heat is generated within the sphere at a rate per unit volume given by $\dot{q}=\Gamma r$, where $\Gamma$ is a constant and $r$ is radial position measured from the center of the sphere. Assuming constant thermal conductivity, k:
(a) Derive an expression for the steady-state temperature profile, $T(r)$, in the sphere.
(b) Calculate the maximum temperature in the sphere under steady-state conditions for the following parameter values:

$$
\begin{aligned}
R & =1.5 \mathrm{~m} \quad \Gamma=100 \mathrm{~W} / \mathrm{m}^{4} \quad h \\
k & =100 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} \\
& =0.5 \mathrm{~W} / \mathrm{m} \cdot \mathrm{~K} \quad T_{\infty}
\end{aligned}=20^{\circ} \mathrm{C} \text {. }
$$

Ans. (a) $T(r)=T_{\infty}+\frac{\Gamma R^{2}}{4 h}+\frac{\Gamma\left(R^{3}-r^{3}\right)}{12 k}$. (b) $76.8^{\circ} \mathrm{C}$.

## HEAT EXCHANGERS

Contents
3.1 Introduction ..... 86
3.2 Double-Pipe Equipment ..... 86
3.3 Shell-and-Tube Equipment ..... 87
3.4 The Overall Heat-Transfer Coefficient ..... 93
3.5 The LMTD Correction Factor ..... 98
3.6 Analysis of Double-Pipe Exchangers ..... 102
3.7 Preliminary Design of Shell-and-Tube Exchangers ..... 106
3.8 Rating a Shell-and-Tube Exchanger ..... 109
3.9 Heat-Exchanger Effectiveness ..... 114

### 3.1 Introduction

In this chapter, we consider some of the techniques that are used in the analysis of industrial heatexchange equipment. Of the many types of commercially available heat exchangers, the discussion will be limited to two, namely, the double pipe exchanger and the shell-and-tube exchanger. The double pipe is the simplest type of heat exchanger, while the shell-and-tube is the most widely used type of exchanger in the chemical process industries. For information on other types of heat-transfer equipment, the reader is referred to Refs. [1-3], as well as Chapter 12.

Heat-exchanger calculations can be divided into two distinct categories, namely, thermal and hydraulic calculations on the one hand and mechanical design calculations on the other. Thermal and hydraulic calculations are made to determine heat-transfer rates and pressure drops needed for equipment sizing. Mechanical design calculations are concerned with detailed equipment specifications, and include considerations such as stress and tube vibration analyses. In this chapter we will be concerned with thermal calculations only. Hydraulic calculations are considered in subsequent chapters, as is software that performs mechanical design calculations.

Heat-exchanger problems may also be categorized as rating problems or design problems. In a rating problem, one must determine whether a given, fully specified exchanger will perform a given heat-transfer duty satisfactorily. It is immaterial whether the exchanger physically exists or whether it is specified only on paper. In a design problem, one must determine the specifications for a heat exchanger that will handle a given heat-transfer duty. A rating calculation is generally an integral part of a design calculation. However, a rating problem also arises when it is desired to use an existing exchanger in a new or modified application. In this chapter we will be primarily concerned with rating calculations, although some aspects of the design problem will also be considered. Design procedures are covered in greater detail in the following chapters.

### 3.2 Double-Pipe Equipment

A simple double-pipe exchanger consists of two pairs of concentric pipes arranged as shown in Figure 3.1. Such a configuration is called a hairpin, for obvious reasons. Batteries of hairpins connected in series or in series-parallel arrangements are commonly employed to provide adequate surface area for heat transfer. The two fluids that are transferring heat flow in the inner and outer pipes, respectively. The fluids usually flow through the exchanger in opposite directions as shown in Figure 3.1. Such a flow pattern is called counter flow or counter-current flow. In some special-purpose applications, parallel (or co-current) flow is employed in which the two streams flow in the same direction. The outer pipe may be insulated to minimize heat transfer to or from the environment. Also, nozzles may be provided on the inner-pipe (tube) side as well as on the annulus side to facilitate connection to process piping. The maximum nozzle size is generally equal to the size of the outer heat-exchanger pipe.

Multi-tube exchangers are also available in which the inner pipe is replaced by a bundle of U -tubes, as shown in Figure 3.2. The tubes may be either plain or equipped with longitudinal fins.

Simple double-pipe exchangers are commercially available with outer-pipe sizes ranging from 2 to 8 in . and inner pipes from $3 / 4$ to 6 in . Multi-tube exchangers typically have outer pipes ranging


Figure 3.1 Simple double-pipe exchanger (Source: Ref. [4]).


Figure 3.2 Multi-tube hairpin exchanger (Source: Koch Heat Transfer Company, LP).


Figure 3.3 Schematic illustration of a shell-and-tube heat exchanger with one shell pass and two tube passes.
in size from 3 to 16 in . with tubing of various sizes. However, multi-tube units with outer-pipe sizes as large as 36 in. are commercially available.

Double-pipe exchangers are commonly used in applications involving relatively low flow rates and high temperatures or pressures, for which they are well suited. Other advantages include low installation cost, ease of maintenance, and flexibility. Hairpins can easily be added to or removed from an existing battery, or arranged in different series-parallel combinations to accommodate changes in process conditions. Simple unfinned double-pipe exchangers tend to become unwieldy, however, when heat-transfer areas greater than about $1000 \mathrm{ft}^{2}$ are required. They are also relatively expensive per unit of heat-transfer surface. Much larger heat-transfer areas are practical using multi-tube units with finned tubes. In fact, multi-tube hairpin exchangers with heat-transfer areas in excess of $12,000 \mathrm{ft}^{2}$ have been built and are commercially available.

### 3.3 Shell-and-Tube Equipment

A shell-and-tube exchanger (Figure 3.3) consists of a bundle of tubes contained in a cylindrical shell. The tubes may be permanently positioned inside the shell (fixed tube-sheet exchanger) or
may be removable for ease of cleaning and replacement (floating-head or U-tube exchanger). In addition, a number of different head and shell designs are commercially available as shown in Figure 3.4.
The Tubular Exchanger Manufacturers Association (TEMA) employs a three-letter code to specify the front-end, shell, and rear-end types. For example, a fixed tube-sheet type BEM exchanger is


Figure 3.4 TEMA designations for shell-and-tube exchangers (Source: Ref. [5]).
shown in Figure 3.5(b). An internal-floating-head type AES exchanger is shown in Figure 3.5(a). Shells are available with inside diameters in discrete sizes up to 120 in . Shells up to 24 in . in diameter are generally made from steel pipes, while larger sizes are made from rolled steel plate. Some key features of shell-and-tube exchangers are summarized in Table 3.1.
Heat exchanger and condenser tubing is available in a wide range of metals in sizes from $1 / 4$ to 2 in . outside diameter. Finned tubing is also available. The dimensions of plain tubing are listed in Table B.1. Notice that the size designations for tubing are different from those of pipe (Table B.2). The nominal outside diameter of a heat-exchanger tube is the actual diameter. Also, the wall thickness is specified by the Birmingham Wire Gage (BWG) rather than by schedule number.

The tubes are arranged in the bundle according to specific patterns. The most common are square $\left(90^{\circ}\right)$, rotated square $\left(45^{\circ}\right)$, and equilateral triangle $\left(30^{\circ}\right)$, as shown in Figure 3.6. The square and rotated square layouts permit mechanical cleaning of the outsides of the tubes. The center-to-center distance between tubes is called the tube pitch. The minimum distance between adjacent tubes is the clearance. From Figure 3.6, it can be seen that the pitch is equal to the clearance plus the outside diameter.

The tube bundle is usually supported against bending and vibrations by segmental baffles, as shown in Figure 3.7. The baffle cut is the ratio of the height of the cutout segment to the inner diameter (ID) of the shell. Thus, a $25 \%$ cut segmental baffle is one for which the height of the cutout segment is one-fourth of the shell ID. The baffles also serve the function of directing the flow of the shell-side fluid across the tube bundle, thereby enhancing the rate of heat transfer. Sealing strips


Figure 3.5 (a) Type AES floating-head exchanger; (b) type BEM fixed-tubesheet exchanger with conical rear head (Source: Ref. [5]).

(c)

(d)

1. Stationary Head-Channel
2. Stationary Head-Bonnet
3. Stationary Head Flange-Channel or Bonnet
4. Channel Cover
5. Stationary Head Nozzle
6. Stationary Tubesheet
7. Tubes
8. Shell
9. Shell Cover
10. Shell Flange-Stationary Head End
11. Shell Flange-Rear Head End
12. Shell Nozzle
13. Shell Cover Flange
14. Expansion Joint
15. Floating Tubesheet
16. Floating Head Cover
17. Floating Head Cover Flange
18. Floating Head Backing Device
19. Split Shear Ring
20. Slip-on Backing Flange
21. Floating Head Cover-External
22. Floating Tubesheet Skirt
23. Packing Box
24. Packing
25. Packing Gland
26. Omitted
27. Tierods and Spacers
28. Transverse Baffles or Support Plates
29. Impringement Plate
30. Longitudinal Baffle
31. Pass Partition
32. Vent Connection
33. Drain Connection
34. Instrument Connection
35. Support Saddle
36. Lifting Lug
37. Support Bracket
38. Weir
39. Liquid Level Connection
40. Floating Head Support

Figure 3.5 (c) Type AEP floating-head exchanger; (d) type CFU U-tube exchanger with two-pass shell (Source: Ref. [5]).

Table 3.1 Features of Shell-and-Tube Heat Exchangers ${ }^{\text {a }}$


Note: Relative costs A and B are not significantly different and interchange for long lengths of tubing.
${ }^{\text {a }}$ Modified from page a-8 of the Patterson-Kelley Co. Manual No. 700A, Heat Exchangers.
${ }^{\mathrm{b}}$ U-tube bundles have been built with tube supports which permit the U-bends to be spread apart and tubes inside of the bundle replaced.
${ }^{c}$ Normal triangular pitch does not permit mechanical cleaning. With a wide triangular pitch, which is equal to 2 (tube diameter plus cleaning lane) $/ \sqrt{3}$, mechanical cleaning is possible on removable bundles. This wide spacing is infrequently used.
${ }^{\mathrm{d}}$ For odd number of tube-side passes floating head requires packed joint or expansion joint.
Source: Ref. [1].
are used to minimize the channeling of fluid between the outer row of tubes and the shell. They usually consist of metal strips attached to the baffles and running between the shell and the outer tubes. Other types of baffles, such as disk and doughnut or window-cut baffles, are also used in some exchangers [1,2].


Figure 3.6 Commonly used tube layouts. (a) Square pitch (90 ); (b) rotated square pitch (45 ); and (c) triangular pitch (30 ) (Source: Ref. [4]).


Figure 3.7 Segmental baffles (Source: Ref. [4]).

Table 3.2 Shell-Side Bypass Flows

| Stream | Percentage in <br> turbulent flow | Percentage in <br> laminar flow |
| :--- | :---: | :---: |
| Cross flow | $30-65$ | $10-50$ |
| Bundle bypass | $15-35$ | $30-80$ |
| Baffle-shell leakage | $6-21$ | $6-48$ |
| Tube-baffle leakage | $9-23$ | $0-10$ |

Source: Ref. [6].

Either the tube-side fluid, the shell-side fluid, or both may make more than one pass through the heat exchanger. On the tube side, multiple passes are achieved by means of U-tubes or by partitioning the headers. The number of tube-side passes is usually one, two, four, or six, but may be as high as 16. Multiple passes on the shell side are achieved by partitioning the shell with a longitudinal baffle (type F-shell) or by connecting two or more single-pass shells together. The number of shell-side passes is usually between one and six.

The primary flow pattern in the shell is a sinuous motion both transverse and parallel to the tubes. However, the situation is complicated by the fact that part of the fluid bypasses the main heat-transfer surface as a result of various leakages. The bypass streams include the tube-to-baffle leakage stream, the tube bundle-to-shell bypass stream, and the baffle-to-shell leakage stream. The amounts of these bypass streams can be substantial as shown in Table 3.2, which gives typical values for well-designed heat exchangers [6]. As a result, the main stream flowing across the tube bundle may comprise less than $50 \%$ of the total shell-side flow. It is the presence of these bypass streams that greatly complicates the analysis of shell-side heat transfer and pressure drop.

The main advantage of shell-and-tube exchangers is that they provide a relatively large amount of heat-transfer surface per unit of volume and weight, and require a minimum number of connections.


Figure 3.8 Section of a double-pipe exchanger.

They are also extremely versatile, and can be designed to meet almost any heat-transfer service. As a result, they are commonly used in a wide variety of applications.

### 3.4 The Overall Heat-Transfer Coefficient

Consider the section of a double-pipe exchanger shown in Figure 3.8, in which the hot fluid is arbitrarily assumed to flow through the inner pipe.

Heat is transferred by convection from the hot fluid to the wall of the inner pipe, by conduction through the pipe wall, and then by convection from the pipe wall to the cold fluid. The driving force for the heat transfer is the difference in temperature between the hot and the cold streams. To describe this overall process, an overall heat-transfer coefficient, $U$, is defined by:

$$
\begin{equation*}
q=U A \Delta T_{m} \tag{3.1}
\end{equation*}
$$

The heat-transfer area, $A$, is the surface area of the inner pipe, and may be based on either the inside or outside diameter. In practice, however, the outside diameter is virtually always used, so that:

$$
\begin{equation*}
A=A_{o}=\pi D_{o} L \tag{3.2}
\end{equation*}
$$

The temperature difference, $\Delta T_{m}$, is the mean temperature difference between the two fluid streams. It can be shown (see Appendix 3.A) that when $U$ is independent of position along the exchanger, $\Delta T_{m}$ is the logarithmic mean temperature difference, i.e.,

$$
\begin{equation*}
\Delta T_{m}=\Delta T_{\ln }=\frac{\Delta T_{2}-\Delta T_{1}}{\ln \left(\Delta T_{2} / \Delta T_{1}\right)} \tag{3.3}
\end{equation*}
$$

where $\Delta T_{1}$ and $\Delta T_{2}$ are the temperature differences at the two ends of the exchanger. Equation (3.3) is valid regardless of whether counter flow or parallel flow is employed.

Now, according to Equation (3.1), the thermal resistance is:

$$
\begin{equation*}
R_{t h}=\frac{1}{U A} \tag{3.4}
\end{equation*}
$$

But this resistance is made up of three resistances in series, namely, the convective resistance between the hot fluid and the pipe wall, the conductive resistance of the pipe wall, and the convective resistance between the pipe wall and the cold fluid. Hence,

$$
\begin{equation*}
\frac{1}{U A_{o}}=\frac{1}{h_{i} A_{i}}+\frac{\ln \left(D_{o} / D_{i}\right)}{2 \pi k L}+\frac{1}{h_{o} A_{0}} \tag{3.5}
\end{equation*}
$$

where $h_{i}$ and $h_{o}$ are the heat-transfer coefficients for flow in the inner and outer pipes, respectively, and $A_{i}$ is the surface area of the inner pipe based on the inside diameter, i.e.,

$$
\begin{equation*}
A_{i}=\pi D_{i} L \tag{3.6}
\end{equation*}
$$

Multiplying Equation (3.5) by $A_{o}$ and inverting yields:

$$
\begin{equation*}
U=\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}\right]^{-1} \tag{3.7}
\end{equation*}
$$

Equation (3.7) is correct when the heat exchanger is new and the heat-transfer surfaces are clean. With most fluids, however, a film of dirt or scale will build up on the heat-transfer surfaces over a period of time. This process is called fouling and results in decreased performance of the heat exchanger due to the added thermal resistances of the dirt films. Fouling is taken into account by means of empirically determined fouling factors, $R_{D i}$ and $R_{D o}$, which represent the thermal resistances of the dirt films on the inside and outside of the inner pipe multiplied by the respective surface areas. Thus, for the inner dirt film:

$$
\begin{equation*}
R_{D t h}=\frac{R_{D i}}{A_{i}} \tag{3.8}
\end{equation*}
$$

Adding these two additional resistances to Equation (3.5) and proceeding as before yields:

$$
\begin{equation*}
U_{D}=\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}+\frac{R_{D i} D_{o}}{D_{i}}+R_{D o}\right]^{-1} \tag{3.9}
\end{equation*}
$$

where $U_{D}$ is the overall coefficient after fouling has occurred. Design calculations are generally made on the basis of $U_{D}$ since it is necessary that the exchanger be operable after fouling has occurred. More precisely, the fouling factors should be chosen so that the exchanger will have a reasonable operating period before requiring cleaning. The operating period must be sufficient to ensure that exchanger cleanings coincide with scheduled process shutdowns. It should be noted that the effect of the fouling factors in Equation (3.9) is to decrease the value of the overall heattransfer coefficient, which increases the heat-transfer area calculated from Equation (3.1). Hence, fouling factors can be viewed as safety factors in the design procedure. In any case, it is necessary to provide more heat-transfer area than is actually required when the exchanger is clean. As a result, outlet temperatures will exceed design specifications when the exchanger is clean, unless bypass streams are provided.

Fouling factors are best determined from experience with similar units in the same or similar service. When such information is not available, recourse may be had to published data. The most comprehensive tabulation of fouling factors is the one developed by TEMA, which is available in Refs. [3,5]. The values given below in Table 3.3 are representative of the data available in the public domain. It should be realized that there are very significant uncertainties associated with all such data. Fouling is a complex process that can be influenced by many variables that are not specifically accounted for in these tabulations.

Fouling can occur by a number of mechanisms operating either alone or in combination. These include:

## - Corrosion

Corrosion products such as rust can gradually build up on tube walls, resulting in reduced heat transmission and eventual tube failure. This type of fouling can be minimized or eliminated by the proper choice of corrosion-resistant materials of construction in the design process.

- Crystallization

Crystallization typically occurs with cooling water streams containing dissolved sulfates and carbonates. Since the solubility of these salts decreases with increasing temperature, they tend to precipitate on heat-transfer surfaces when the water is heated, forming scale. This type of fouling can be minimized by restricting the outlet water temperature to a maximum of $110-125^{\circ} \mathrm{F}$.

Table 3.3 Typical Values of Fouling Factors (h.ff $\cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ )

## Cooling water streams ${ }^{a}$

- Seawater
- Brackish water
- Treated cooling tower water
0.001
- Municipal water supply
- River water
- Engine jacket water
- Distilled or demineralized water
- Treated boiler feedwater
- Boiler blowdown
0.001-0.002

Service gas streams

- Ambient air (in air-cooled units)

0-0.0005

- Compressed air
- Steam (clean)
- Steam (with oil traces)
- Refrigerants (with oil traces)
0.001-0.002
- Ammonia

0-0.0005

- Carbon dioxide
0.001-0.002
- Flue gases
0.002

Service liquid streams

- Fuel oil
- Lubrication oil
0.002-0.005
- Transformer oil
0.001
- Hydraulic fluid
0.001
- Organic heat-transfer fluids
0.001
- Refrigerants
0.001-0.002
- Brine
0.001
0.003


## Process gas streams

- Hydrogen 0.001
- Organic solvent vapors
0.001
- Acid gases
- Stable distillation overhead products
0.002-0.003

Process liquid streams

- Amine solutions 0.002
- Glycol solutions $\quad 0.002$
- Caustic solutions 0.002
- Alcohol solutions 0.002
- Ammonia 0.001
- Vegetable oils 0.003
- Stable distillation side-draw and bottom products 0.001-0.002


## Natural gas processing streams

- Natural gas 0.001
- Overhead vapor products
0.001-0.002
- $\mathrm{C}_{3}$ or $\mathrm{C}_{4}$ vapor (condensing)
0.001
- Lean oil
0.002
- Rich oil
- LNG and LPG


## Table 3.3 (Continued)

## Oil refinery streams

- Crude oil ${ }^{\text {b }}$
- Temperature less than $250^{\circ} \mathrm{F} \quad 0.002-0.003$
- Temperature between $250^{\circ} \mathrm{F}$ and $350^{\circ} \mathrm{F} \quad 0.003-0.004$
- Temperature between $350^{\circ} \mathrm{F}$ and $450^{\circ} \mathrm{F} \quad 0.004-0.005$
- Temperature greater than $450^{\circ} \mathrm{F} \quad 0.005-0.006$
- Liquid product streams
- Gasoline $\quad 0.001-0.002$
- Naphtha and light distillates 0.001-0.003
- Kerosene 0.001-0.003
- Light gas oil 0.002-0.003
- Heavy gas oil
0.003-0.005
- Heavy fuel oils
- Asphalt and residuum
0.003-0.007
- Other oil streams
- Refined lube oil 0.001
- Cycle oil 0.002-0.004
- Coker gas oil $0.003-0.005$
- Absorption oils 0.002
${ }^{\text {a }}$ Assumes water velocity greater than $3 \mathrm{ft} / \mathrm{s}$. Lower values of ranges correspond to water temperature below about $120^{\circ} \mathrm{F}$ and hot stream temperature below about $250^{\circ} \mathrm{F}$.
${ }^{\mathrm{b}}$ Assumes desalting at approximately $250^{\circ} \mathrm{F}$ and a minimum oil velocity of $2 \mathrm{ft} / \mathrm{s}$.
Source: Refs. [7,8] and www.engineeringpage.com.


## - Decomposition

Some organic compounds may decompose when they are heated or come in contact with a hot surface, forming carbonaceous deposits such as coke and tar. In cracking furnaces, partial decomposition of the hydrocarbon feedstock is the objective and coke formation is an undesired but unavoidable result.

- Polymerization

Polymerization reactions can be initiated when certain unsaturated organic compounds are heated or come in contact with a hot metal tube wall. The resulting reaction products can form a very tough plastic-like layer that can be extremely difficult to remove from heat-transfer surfaces.

- Sedimentation

Sedimentation fouling results from the deposition of suspended solids entrained in many process streams such as cooling water and flue gases. High fluid velocities tend to minimize the accumulation of deposits on heat-transfer surfaces.

## - Biological activity

Biological fouling is most commonly caused by micro-organisms, although macroscopic marine organisms can sometimes cause problems as well. Cooling water and some other process streams may contain algae or bacteria that can attach and grow on heat-transfer surfaces, forming slimes that are very poor heat conductors. Metabolic products of these organisms can also cause corrosion of metal surfaces. Biocides and copper-nickel alloy tubing can be used to inhibit the growth of micro-organisms and mitigate this type of fouling.

It can be seen from Table 3.3 that the range of values of fouling factors spans more than an order of magnitude. For very clean streams, values of $0.0005 h \cdot f^{2} \cdot{ }^{\circ} F / B t u$ or less are appropriate, whereas very dirty streams require values of $0.005-0.01 h \cdot f^{2} \cdot{ }^{\circ} F / B t u$. However, values in the range $0.001-$ $0.003 h \cdot f^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ are appropriate for the majority of cases.

## Example 3.1

A double-pipe heat exchanger will be used to cool a hot stream from $350^{\circ} \mathrm{F}$ to $250^{\circ} \mathrm{F}$ by heating a cold stream from $80^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$. The hot stream will flow in the inner pipe, which is 2 -in. schedule 40 carbon steel with a thermal conductivity of $26 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Fouling factors of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ should be provided for each stream. The heat-transfer coefficients are estimated to be $h_{i}=200$ and $h_{o}=350 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$, and the heat load is $3.5 \times 10^{6} \mathrm{Btu} / \mathrm{h}$.
(a) For counter-current operation, what surface area is required?
(b) For co-current operation, what surface area is required?

## Solution

(a) Counter-current operation

From Equation (3.1) we have,

$$
\begin{aligned}
& A=\frac{q}{U_{D} \Delta T_{\mathrm{ln}}} \\
& A=\frac{3.5 \times 10^{6}}{U_{D} \Delta T_{\mathrm{ln}}}
\end{aligned}
$$

Clearly, we must compute values of $U_{D}$ and $\Delta T_{\mathrm{ln}}$ in order to solve the problem. Counter flow can be represented schematically as follows:

$$
\begin{gathered}
\Delta T=230^{\circ} \mathrm{F}\left\{\begin{array}{c}
350^{\circ} \mathrm{F} \longrightarrow 80^{\circ} \mathrm{F} \\
120^{\circ} \mathrm{F} \longleftrightarrow 80^{\circ} \mathrm{F}
\end{array}\right\} \Delta T=170^{\circ} \mathrm{F} \\
\Delta T_{\ln }=\frac{\Delta T_{2}-\Delta T_{1}}{\ln \left(\Delta T_{2} / \Delta T_{1}\right)}=\frac{230-170}{\ln (230 / 170)}=198.5^{\circ} \mathrm{F}
\end{gathered}
$$

In order to compute $U_{D}$ from Equation (3.9), we first find $D_{o}$ and $D_{i}$ for 2-in. schedule 40 pipe. From Table B.2, $D_{i}=2.067 \mathrm{in}$. and $D_{o}=2.375 \mathrm{in}$. Then,

$$
\begin{aligned}
U_{D}= & {\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}+\frac{R_{D i} D_{o}}{D_{i}}+R_{D o}\right]^{-1} } \\
U_{D}= & {\left[\frac{2.375}{200 \times 2.067}+\frac{(2.375 / 12) \times \ln (2.375 / 2.067)}{2 \times 26}\right.} \\
& \left.\quad+\frac{1}{350}+\frac{0.001 \times 2.375}{2.067}+0.001\right]^{-1} \\
U_{D}= & {[0.0057+0.0005+0.0029+0.0011+0.001]^{-1} } \\
U_{D}= & 88.65 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Therefore,

$$
A=\frac{3.5 \times 10^{6}}{88.65 \times 198.5}=198.9 \mathrm{ft}^{2} \cong 199 \mathrm{ft}^{2}
$$

(b) Co-current operation

For parallel flow, the value of $\Delta T_{\ln }$ will be different.

$$
\begin{aligned}
& \Delta T=270^{\circ} \mathrm{F}\left\{\begin{array}{c}
350^{\circ} \mathrm{F} \longrightarrow 250^{\circ} \mathrm{F} \\
80^{\circ} \mathrm{F} \longrightarrow 120^{\circ} \mathrm{F}
\end{array}\right\} \Delta T=130^{\circ} \mathrm{F} \\
& \Delta T_{\ln }=\frac{\Delta T_{2}-\Delta T_{1}}{\ln \left(\Delta T_{2} / \Delta T_{1}\right)}=\frac{270-130}{\ln (270 / 130)}=191.5^{\circ} \mathrm{F} \\
& A=\frac{3.5 \times 10^{6}}{88.65 \times 191.5}=206.2 \cong 206 \mathrm{ft}^{2}
\end{aligned}
$$

This example illustrates the advantage of counter-current operation as opposed to co-current operation. Although the difference between the modes of operation is small in this case, it is not always so. In fact, if the outlet temperature of the cold stream were required to be $260^{\circ} \mathrm{F}$ instead of $120^{\circ} \mathrm{F}$, parallel flow would be impossible.

### 3.5 The LMTD Correction Factor

In multi-pass shell-and-tube exchangers, the flow pattern is a mixture of co-current and countercurrent flow, as the two streams flow through the exchanger in the same direction on some passes and in the opposite direction on others. For this reason, the mean temperature difference is not equal to the logarithmic mean. However, it is convenient to retain the LMTD by introducing a correction factor, $F$, which is appropriately termed the LMTD correction factor:

$$
\begin{equation*}
\Delta T_{m}=F\left(\Delta T_{\ln }\right)_{c f} \tag{3.10}
\end{equation*}
$$

Note that in this relationship, the LMTD is computed as if the flow were counter current. The LMTD correction factor can be computed analytically for any number of shell-side passes and any even number of tube-side passes as follows [9]:

Let

$$
\begin{align*}
N & =\text { number of shell-side passes } \\
R & =\frac{T_{a}-T_{b}}{t_{b}-t_{a}}  \tag{3.11}\\
P & =\frac{t_{b}-t_{a}}{T_{a}-t_{a}} \tag{3.12}
\end{align*}
$$

where
$T_{a}=$ inlet temperature of shell-side fluid
$T_{b}=$ outlet temperature of shell-side fluid
$t_{a}=$ inlet temperature of tube-side fluid
$t_{b}=$ outlet temperature of tube-side fluid

For $R \neq 1$, compute:

$$
\begin{gather*}
\alpha=\left(\frac{1-R P}{1-P}\right)^{1 / N}  \tag{3.13}\\
F=\frac{\alpha-1}{\alpha-R}  \tag{3.14}\\
(R-1) \ln \left[\frac{2-S\left(R+1-\sqrt{R^{2}+1}\right)}{2-S\left(R+1+\sqrt{R^{2}+1}\right)}\right] \tag{3.15}
\end{gather*}
$$

For $R=1$, compute:

$$
\begin{gather*}
S=\frac{P}{N-(N-1) P}  \tag{3.16}\\
F=\frac{S \sqrt{2}}{(1-S) \ln \left[\frac{2-S(2-\sqrt{2})}{2-S(2+\sqrt{2})}\right]} \tag{3.17}
\end{gather*}
$$

Although not readily apparent, these equations are symmetric with respect to fluid placement, i.e., switching the two fluids between tubes and shell changes the values of $R$ and $P$, but leaves $F$ unchanged. Also, $F=1.0$ if either fluid is isothermal. The above relations are available in the form of graphs that are convenient for making quick estimates [2,5,8,10]. The graphs corresponding to one and two shell passes are given in Figures 3.9 and 3.10, respectively.

Configurations for which the calculated value of $F$ is less than about 0.8 should not be used in practice for several reasons. First, the heat transfer in such a case is relatively inefficient, being less than $80 \%$ of that for a counter-flow exchanger. More importantly, the restriction on $F$ is intended to avoid the steeply sloping parts of the curves in Figures 3.9 and 3.10. There, small deviations from simplifying assumptions (such as no heat loss and constant $U$ ) upon which the equations for $F$ are based, can result in an actual $F$-value much lower than the calculated value. Also, in these regions large changes in $F$ can result from small changes in $P$, making exchanger performance very sensitive to any deviations from design temperatures. Examination of Figures 3.9 and 3.10 shows that the value of 0.8 is approximate; higher values of $F$ are required at very large and small $R$-values, for example. The value of $F$ can be increased by increasing the number of shell passes, up to a practical limit of about six. (Note, however, that the curves become steeper with increasing number of shell passes, requiring still higher values of $F$.) In extreme cases, true counter flow, for which $F=1.0$, may be the only practical configuration.

## Example 3.2

A fluid is to be heated from $100^{\circ} \mathrm{F}$ to $160^{\circ} \mathrm{F}$ by heat exchange with a hot fluid that will be cooled from $230^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$. The heat-transfer rate will be $540,000 \mathrm{Btu} / \mathrm{h}$ and the hot fluid will flow in the tubes. Will a 1-2 exchanger (i.e., an exchanger with one shell pass and a multiple of two tube passes) be suitable for this service? Find the mean temperature difference in the exchanger.

## Solution

$$
\begin{aligned}
& R=\frac{T_{a}-T_{b}}{t_{b}-t_{a}}=\frac{100-160}{150-230}=0.75 \\
& P=\frac{t_{b}-t_{a}}{T_{a}-t_{a}}=\frac{150-230}{100-230}=0.615
\end{aligned}
$$

From Figure 3.9 (or Equation (3.15)), $F \cong 0.72$. Since $F$ is less than 0.8 , a $1-2$ exchanger should not be used. However, with two shell passes, it is found from Figure 3.10 that $F \cong 0.94$. Hence, an exchanger with two shell passes and a multiple of four tube passes will be suitable. Such an exchanger is called a $2-4$ exchanger. The mean temperature difference in the exchanger is easily


Figure 3.9 LMTD correction factor for 1-2 exchangers (Source: Ref. [8]).


Figure 3.10 LMTD correction factor for 2-4 exchangers (Source: Ref. [8]).
computed as follows:

$$
\begin{aligned}
\Delta T & =50^{\circ} \mathrm{F}\left\{\begin{array}{l}
100^{\circ} \mathrm{F} \longrightarrow 160^{\circ} \mathrm{F} \\
150^{\circ} \mathrm{F} \longleftrightarrow 230^{\circ} \mathrm{F}
\end{array}\right\} \quad \Delta T=70^{\circ} \mathrm{F} \\
\left(\Delta T_{\ln }\right)_{c f} & =\frac{\Delta T_{2}-\Delta T_{1}}{\ln \left(\Delta T_{2} / \Delta T_{1}\right)}=\frac{70-50}{\ln (70 / 50)}=59.6^{\circ} \mathrm{F} \\
\Delta T_{m} & =F\left(\Delta T_{\ln }\right)_{c f}=0.94 \times 59.6=56^{\circ} \mathrm{F}
\end{aligned}
$$

### 3.6 Analysis of Double-Pipe Exchangers

The detailed thermal analysis of a double-pipe heat exchanger involves the calculation of the overall heat-transfer coefficient according to Equation (3.9). The inside coefficient, $h_{i}$, can be computed using the equations for flow in circular pipes presented in Chapter 2, i.e., Equation (2.33), (2.36), (2.37), or (2.38), depending on the flow regime. The outside coefficient, $h_{o}$, can be computed using the equivalent diameter in Equation (2.33), (2.37), or (2.38) if the flow is turbulent or in the transition region. If the flow in the outer pipe is laminar, then Equation (2.41) should be used.

Use of the Seider-Tate or Hausen equations requires the calculation of the viscosity correction factor, $\phi=\left(\mu / \mu_{w}\right)^{0.14}$, which, in turn, requires that the average wall temperature of the inner pipe be determined. An equation for the wall temperature can be derived by assuming that all the heat is transferred between the streams at their average temperatures. Since $h_{i}$ and $h_{o}$ are calculated on the basis of a clean exchanger, the temperature drop across the pipe wall is normally very small and can be neglected. In the derivation, it will be assumed that the hot fluid is in the inner pipe, but the final equation is independent of this assumption. The configuration is indicated schematically in Figure 3.11, in which $T_{\text {ave }}$ and $t_{\text {ave }}$ are the average temperatures of the fluids in the outer and inner pipes, respectively, and $T_{w}$ is the average wall temperature.
An energy balance gives:

$$
q=h_{i} A_{i}\left(t_{\text {ave }}-T_{w}\right)=h_{o} A_{o}\left(T_{w}-T_{\text {ave }}\right)
$$

Solving for $\mathrm{T}_{w}$ yields:

$$
T_{w}=\frac{h_{i} A_{i} t_{\text {ave }}+h_{o} A_{o} T_{\text {ave }}}{h_{i} A_{i}+h_{0} A_{o}}
$$

Substituting $A=\pi D L$ for the areas and rearranging, we obtain:

$$
\begin{equation*}
T_{w}=\frac{h_{i} t_{\text {ave }}+h_{o}\left(D_{o} / D_{i}\right) T_{\text {ave }}}{h_{i}+h_{o}\left(D_{o} / D_{i}\right)} \tag{3.18}
\end{equation*}
$$

Use of Equation (3.18) involves an iterative procedure since $T_{w}$ is required for the calculation of $h_{i}$ and $h_{o}$, and vice versa. However, a single iteration is usually sufficient. The values of $h_{i}$ and $h_{o}$ are first computed by assuming that $\phi_{i}$ and $\phi_{o}$ are both unity. These preliminary values are used in Equation (3.18) to compute $T_{w}$. The values of $\mu_{w}$ for the two fluids are then obtained, and the viscosity correction factors are calculated. These factors are then multiplied by the preliminary values of $h_{i}$ and $h_{o}$ to obtain the final values of the film coefficients.

The thermal analysis of a double-pipe exchanger is illustrated in the following example.


Figure 3.11 Configuration for derivation of equation to estimate pipe-wall temperature.

## Example 3.3

$10,000 \mathrm{lb} / \mathrm{h}$ of benzene is to be heated from $60^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$ by heat exchange with an aniline stream that will be cooled from $150^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$. A number of 16 ft hairpins consisting of 2 in . by 1.25 in . schedule 40 stainless steel pipe (type $316, k=9.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) are available and will be used for this service. Assuming that the benzene flows in the inner pipe, how many hairpins will be required?

## Solution

(a) Fluid properties at the average stream temperatures are obtained from Figures A.1 and A.2, and Table A. 15.

| Fluid property | Benzene $\left(t_{\text {ave }}=90^{\circ} \mathrm{F}\right)$ | Aniline $\left(T_{\text {ave }}=125^{\circ} \mathrm{F}\right)$ |
| :--- | :--- | :--- |
| $\mu(\mathrm{cp})$ | 0.55 | 2.0 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.42 | 0.52 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.092 | 0.100 |

(b) Determine the heat load and aniline flow rate by energy balances on the two streams.

$$
\begin{aligned}
q & =\left(\dot{m} C_{P} \Delta T\right)_{B}=10,000 \times 0.42 \times 60=252,000 \mathrm{Btu} / \mathrm{h} \\
252,000 & =\left(\dot{m} C_{P} \Delta T\right)_{A}=\dot{m}_{A} \times 0.52 \times 50 \\
\dot{m}_{A} & =9692 \mathrm{lb} / \mathrm{h}
\end{aligned}
$$

(c) Calculate the LMTD. (Counter-current flow is assumed.)

$$
\begin{aligned}
& \Delta T=40^{\circ} \mathrm{F}\left\{\begin{array}{l}
60^{\circ} \mathrm{F} \longrightarrow 120^{\circ} \mathrm{F} \\
100^{\circ} \mathrm{F} \longleftrightarrow 150^{\circ} \mathrm{F}
\end{array}\right\} \Delta T=30^{\circ} \mathrm{F} \\
& \Delta T_{\ln }=\frac{40-30}{\ln (40 / 30)}=34.76^{\circ} \mathrm{F}
\end{aligned}
$$

(d) Calculate $\mathrm{h}_{\mathrm{i}}$ assuming $\phi_{i}=1.0$.

$$
\begin{aligned}
D_{i} & =\frac{1.38}{12}=0.115 \mathrm{ft} \quad(\text { From Table B.2) } \\
R e & =\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 10,000}{\pi \times 0.115 \times 0.55 \times 2.419}=83,217 \Rightarrow \text { turbulent flow } \\
N u & =\frac{h_{i} D_{i}}{k}=0.027 \operatorname{Re}^{0.8} \mathrm{Pr}^{1 / 3} \\
h_{i} & =\frac{k}{D_{i}} \times 0.027 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3} \\
h_{i} & =\frac{0.092}{0.115} \times 0.027(83,217)^{0.8}\left(\frac{0.42 \times 0.55 \times 2.419}{0.092}\right)^{1 / 3} \\
h_{i} & =340 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Note: The correction factor for entrance effects can usually be omitted from the Seider-Tate and Hausen equations when working with industrial heat-transfer equipment. For the inner pipe,
the effect of the return bends on the heat transfer is minor, so it is reasonable (and conservative) to use the entire length of the flow path in the correction term. Although this length is unknown in the present instance, the exchanger will have at least one hairpin containing 32 ft of pipe. Hence,

$$
\bar{D}_{i} \geq \frac{32}{0.115}=278>60
$$

Therefore, entrance effects are negligible in this case.
(e) Calculate $h_{o}$ assuming $\phi_{o}=1.0$.

$$
\begin{gathered}
\left.\begin{array}{r}
D_{2}=2.067 \mathrm{in} . \\
D_{1}=1.660 \mathrm{in} .
\end{array}\right\} \quad \text { (From Table B.2) } \\
D_{e}=D_{2}-D_{1}=\frac{(2.067-1.660)}{12}=0.0339 \mathrm{ft}
\end{gathered}
$$

Flow area $\equiv A_{f}=\frac{\pi}{4}\left(D_{2}^{2}-D_{1}^{2}\right)=0.00826 \mathrm{ft}^{2}$

$$
\begin{aligned}
& R e=\frac{D_{e}\left(\dot{m} / A_{f}\right)}{\mu}=\frac{0.0339 \times(9692 / 0.00826)}{2.0 \times 2.419}=8222 \Rightarrow \text { transition flow } \\
& N u=\frac{h_{o} D_{e}}{k}=0.116\left[R e^{2 / 3}-125\right] \operatorname{Pr}^{1 / 3}\left[1+\left(D_{e} / L\right)^{2 / 3}\right]
\end{aligned}
$$

Neglecting entrance effects,

$$
\begin{aligned}
h_{o} & =\frac{k}{D_{e}} \times 0.116\left[\mathrm{Re}^{2 / 3}-125\right] \operatorname{Pr}^{1 / 3} \\
& =\frac{0.1}{0.0339} \times 0.116 \times\left[(8222)^{2 / 3}-125\right]\left(\frac{0.52 \times 2.0 \times 2.419}{0.1}\right)^{1 / 3} \\
h_{o} & =283 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Note: In the annulus the flow is disrupted at the return bends, so it is appropriate to use the length of pipe in one leg of a hairpin to estimate entrance effects. Thus,

$$
L / D_{e}=16 / 0.0339=472>60
$$

Hence, entrance effects are negligible. (Including the correction term in the Hausen equation gives $h_{o}=288 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$, and this does not alter the solution.)
(f) Calculate the pipe-wall temperature.

$$
\begin{aligned}
& T_{w}=\frac{h_{i} t_{\text {ave }}+h_{o}\left(D_{o} / D_{i}\right) T_{\text {ave }}}{h_{i}+h_{o}\left(D_{o} / D_{i}\right)} \\
& T_{w}=\frac{340 \times 90+283 \times(1.66 / 1.38) \times 125}{340+283 \times(1.66 / 1.38)} \\
& T_{w}=108^{\circ} \mathrm{F}
\end{aligned}
$$

(g) Calculate $\phi_{i}$ and $\phi_{0}$, and corrected values of $h_{i}$ and $h_{0}$.

At $108^{\circ} \mathrm{F}$,

$$
\begin{aligned}
\mu_{B} & =0.47 \mathrm{cp} \text { and } \mu_{A}=2.4 \mathrm{cp} \quad(\text { from Figure A.1) } \\
\phi_{i} & =\left(\frac{0.55}{0.47}\right)^{0.14}=1.0222 \\
\phi_{o} & =\left(\frac{2.0}{2.4}\right)^{0.14}=0.9748 \\
h_{i} & =340(1.0222)=348 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
h_{o} & =283(0.9748)=276 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(h) Obtain fouling factors. A check of Table 3.3 shows no appropriate listings. However, these organic process chemicals are expected to exhibit low fouling tendencies. Hence, we take

$$
R_{D i}=R_{D o}=0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
$$

(i) Compute the overall heat-transfer coefficient.

$$
\begin{aligned}
& U_{D}=\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}+\frac{R_{D i} D_{o}}{D_{i}}+R_{D o}\right]^{-1} \\
& U_{D}=\left[\frac{1.66}{348 \times 1.38}+\frac{(1.66 / 12) \ln (1.66 / 1.38)}{2 \times 9.4}+\frac{1}{276}+\frac{0.001 \times 1.66}{1.38}+0.001\right]^{-1} \\
& U_{D}=94 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(j) Calculate the required surface area and number of hairpins.

$$
\begin{aligned}
q & =U_{D} A \Delta T_{\mathrm{ln}} \\
A & =\frac{q}{U_{D} \Delta T_{\mathrm{ln}}} \\
A & =\frac{252,000}{94 \times 34.76}=77.12 \mathrm{ft}^{2}
\end{aligned}
$$

From Table B.2, the external surface area per foot of $1.25-\mathrm{in}$. schedule 40 pipe is $0.435 \mathrm{ft}^{2}$. Therefore,

$$
L=\frac{77.12}{0.435}=177.3 \mathrm{ft}
$$

Since each 16 - ft hairpin contains 32 ft of pipe,

$$
\text { Number of hairpins }=\frac{177.3}{32}=5.5 \Rightarrow 6
$$

Thus, six hairpins will be required.

Table 3.4 Criteria for Fluid Placement, in Order of Priority

| Tube-side fluid | Shell-side fluid |
| :--- | :--- |
| Corrosive fluid | Condensing vapor (unless corrosive) |
| Cooling water | Fluid with large $\Delta T\left(>100^{\circ} \mathrm{F}\right)$ |
| Fouling fluid |  |
| Less viscous fluid |  |
| Higher-pressure stream |  |
| Hotter fluid |  |

The preceding example constitutes a design problem in which all of the design parameters are specified except one, namely, the total length of the heat exchanger. Design problems frequently include specifications of maximum allowable pressure drops on the two streams. In that case, pressure drops for both streams would have to be calculated in order to determine the suitability of the exchanger. A more complete analysis of the above problem will be given in the next chapter.

In the above example, benzene was specified as the tube-side fluid. Some guidelines for positioning the fluids are given in Table 3.4. It should be understood that these general guidelines, while often valid, are not ironclad rules, and optimal fluid placement depends on many factors that are service specific.

For the example problem, neither fluid is corrosive to stainless steel or highly fouling, so the first applicable criterion on the list for tube-side fluid is viscosity. Benzene has a significantly lower viscosity than aniline, indicating that it should be placed in the inner pipe. However, this criterion has relatively low priority and is actually relevant to finned-pipe or shell-and-tube exchangers where the fins or tubes act as turbulence generators for the shell-side fluid. The next criterion is stream pressure, which was not specified in the example. The last criterion for tube-side fluid is the hotter fluid, which is aniline. Neither criterion for the shell-side fluid is applicable. The upshot is that either fluid could be placed in the inner pipe, and both options should be investigated to determine which results in the better design.

### 3.7 Preliminary Design of Shell-and-Tube Exchangers

The complete thermal design of a shell-and-tube heat exchanger is a complex and lengthy process, and is usually performed with the aid of a computer program [2]. Frequently, however, one requires only a rough approximation of the heat-transfer area for the purpose of making a preliminary cost estimate of the exchanger. Tabulations of overall heat-transfer coefficients such as the one presented in Table 3.5 are used for this purpose. One simply estimates a value for the overall coefficient based on the tabulated values and then computes the required heat-transfer area from Equation (3.1). A somewhat better procedure is to estimate the individual film coefficients, $h_{i}$ and $h_{o}$, and use them to compute the overall coefficient by Equation (3.9). A table of film coefficients can be found in Ref. [11].

## Example 3.4

In a petroleum refinery, it is required to $\operatorname{cool} 30,000 \mathrm{lb} / \mathrm{h}$ of kerosene from $400^{\circ} \mathrm{F}$ to $250^{\circ} \mathrm{F}$ by heat exchange with $75,000 \mathrm{lb} / \mathrm{h}$ of gas oil, which is at $110^{\circ} \mathrm{F}$. A shell-and-tube exchanger will be used, and the following data are available:

| Fluid property | Kerosene | Gas oil |
| :--- | :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.6 | 0.5 |
| $\mu(\mathrm{cp})$ | 0.45 | 3.5 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.077 | 0.08 |

Table 3.5 Typical Values of Overall Heat-Transfer Coefficients in Tubular Heat Exchangers.
$\mathrm{U}=\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$
Shell side
Liquid-liquid media

Aroclor 1248
Cutback asphalt
Demineralized water
Ethanol amine (MEA or
DEA) 10-25\% solutions
Fuel oil
Fuel oil
Gasoline
Heavy oils
Heavy oils
Hydrogen-rich reformer
stream
Kerosene or gas oil
Kerosene or gas oil
Kerosene or jet fuels
Jacket water
Lube oil (low viscosity)
Lube oil (high viscosity)
Lube oil
Naphtha
Naphtha
Organic solvents
Organic solvents
Organic solvents
Tall oil derivatives, vegetable oil, etc.
Water

Water
Wax distillate
Wax distillate

Jet fuels
Water
Water
Water or DEA, or
MEA solutions

| Water | $15-25$ | 0.007 |
| :--- | :--- | :--- |
| Oil | $10-15$ | 0.008 |

Wate
Heavy oils
Water
Hydrogen-rich reformer
stream
Water $\quad 25-50 \quad 0.005$
Oil 20-35 0.005
Trichloroethylene $40-50 \quad 0.0015$
Water 230-300 0.002
Water $25-50 \quad 0.002$
Water $40-80 \quad 0.003$
Oil $11-20$ 0.006
Water 50-70 0.005
Oil 25-35 0.005
Water 50-150 0.003
Brine $35-90 \quad 0.003$

Organic solvents 20-60 0.002
Water 20-50 0.004

| Caustic soda | $100-250$ | 0.003 |
| :--- | :---: | :---: |
| solutions $(10-30 \%)$ |  |  |
| Water | $200-250$ | 0.003 |
| Water | $15-25$ | 0.005 |
| Oil | $13-23$ | 0.005 |

Condensing vapor-liquid media
Alcohol vapor
Asphalt ( $450^{\circ} \mathrm{F}$.)
Dowtherm vapor
Dowtherm vapor
Gas-plant tar
High-boiling hydrocarbons V
Low-boiling hydrocarbons A
Hydrocarbon vapors
(partial condenser)
Organic solvents A
Organic solvents high NC, A
Organic solvents low NC, V
Kerosene
Kerosene
Naphtha

Water

| $100-200$ | 0.002 |
| :--- | :--- |
| $40-60$ | 0.006 |
| $60-80$ | 0.004 |
| $80-120$ | 0.0015 |
| $40-50$ | 0.0055 |
| $20-50$ | 0.003 |
| $80-200$ | 0.003 |
| $25-40$ | 0.004 |

Oil

| Water | $100-200$ | 0.003 |
| :--- | :---: | :---: |
| Water or brine | $20-60$ | 0.003 |
| Water or brine | $50-120$ | 0.003 |
| Water | $30-65$ | 0.004 |
| Oil | $20-30$ | 0.005 |
| Water | $50-75$ | 0.005 |

Table 3.5 (Continued)

| Shell side | Tube side | Design $U$ | Includes total dirt |
| :---: | :---: | :---: | :---: |
| Naphtha | Oil | 20-30 | 0.005 |
| Stabilizer reflux vapors | Water | 80-120 | 0.003 |
| Steam | Feed water | 400-1000 | 0.0005 |
| Steam | No. 6 fuel oil | 15-25 | 0.0055 |
| Steam | No. 2 fuel oil | 60-90 | 0.0025 |
| Sulfur dioxide | Water | 150-200 | 0.003 |
| Tall-oil derivatives, vegetable oils (vapor) | Water | 20-50 | 0.004 |
| Water | Aromatic vapor-stream azeotrope | 40-80 | 0.005 |
| Gas-liquid media |  |  |  |
| Air, $\mathrm{N}_{2}$, etc. (compressed) | Water or brine | 40-80 | 0.005 |
| Air, $\mathrm{N}_{2}$, etc., A | Water or brine | 10-50 | 0.005 |
| Water or brine | Air, $\mathrm{N}_{2}$ (compressed) | 20-40 | 0.005 |
| Water or brine | Air, $\mathrm{N}_{2}$, etc., A | 5-20 | 0.005 |
| Water | Hydrogen containing natural-gas mixtures | 80-125 | 0.003 |
| Vaporizers |  |  |  |
| Anhydrous ammonia | Steam condensing | 150-300 | 0.0015 |
| Chlorine | Steam condensing | 150-300 | 0.0015 |
| Chlorine | Light heat-transfer oil | 40-60 | 0.0015 |
| Propane, butane, etc. | Steam condensing | 200-300 | 0.0015 |
| Water | Steam condensing | 250-400 | 0.0015 |

NC : non-condensable gas present; V : vacuum; A : atmospheric pressure.
Dirt (or fouling factor) units are (h) ( $\mathrm{ft}^{2}$ ) $\left({ }^{\circ} \mathrm{F}\right) / \mathrm{Btu}$
Source: Ref. [1].
For the purpose of making a preliminary cost estimate, determine the required heat-transfer area of the exchanger.

## Solution

(a) Calculate the heat load and outlet oil temperature by energy balances on the two streams.

$$
\begin{aligned}
q & =\left(\dot{m} C_{P} \Delta T\right)_{K}=30,000 \times 0.6 \times(400-250) \\
q & =2.7 \times 10^{6} \mathrm{Btu} / \mathrm{h} \\
q & =2.7 \times 10^{6}=\left(\dot{m} C_{P} \Delta T\right)_{o i l}=75,000 \times 0.05 \times(T-110) \\
T & =182^{\circ} \mathrm{F}
\end{aligned}
$$

(b) Calculate the LMTD.

$$
\begin{gathered}
\Delta T=140^{\circ} \mathrm{F}\left\{\begin{array}{l}
110^{\circ} \mathrm{F} \longrightarrow 182^{\circ} \mathrm{F} \\
250^{\circ} \mathrm{F} \longleftrightarrow 400^{\circ} \mathrm{F}
\end{array}\right\} \Delta T=218^{\circ} \mathrm{F} \\
\left(\Delta T_{1 \mathrm{n}}\right)_{c f}=\frac{218-140}{\ln (218 / 140)}=176^{\circ} \mathrm{F}
\end{gathered}
$$

(c) Calculate the LMTD correction factor.

For the purpose of this calculation, assume that the kerosene will flow in the shell. This assumption will not affect the result since the value of $F$ is the same, regardless of which fluid is in the shell.

$$
\begin{aligned}
& R=\frac{T_{b}-T_{a}}{t_{b}-t_{a}}=\frac{400-250}{182-110}=2.08 \\
& P=\frac{t_{b}-t_{a}}{T_{a}-t_{a}}=\frac{182-110}{400-110}=0.25
\end{aligned}
$$

From Figure 3.9, for a 1-2 exchanger, $F \cong 0.93$.
(d) Estimate $U_{D}$.

From Table 3.5, a kerosene-oil exchanger should have an overall coefficient in the range $20-35 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Therefore, take

$$
U_{D}=25 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(e) Calculate the required area.

$$
\begin{aligned}
q & =U_{D} A F\left(\Delta T_{\ln }\right)_{c f} \\
A & =\frac{q}{U_{D} F\left(\Delta T_{\ln }\right)_{c f}} \\
A & =\frac{2.7 \times 10^{6}}{25 \times 0.93 \times 176} \cong 660 \mathrm{ft}^{2}
\end{aligned}
$$

### 3.8 Rating a Shell-and-Tube Exchanger

The thermal analysis of a shell-and-tube heat exchanger is similar to the analysis of a double-pipe exchanger in that an overall heat-transfer coefficient is computed from individual film coefficients, $h_{i}$ and $h_{o}$. However, since the flow patterns in a shell-and-tube exchanger differ from those in a double-pipe exchanger, the procedures for calculating the film coefficients also differ. The shell-side coefficient presents the greatest difficulty due to the very complex nature of the flow in the shell, as discussed in Section 3.3. In addition, if the exchanger employs multiple tube passes, then the LMTD correction factor must be used in calculating the mean temperature difference in the exchanger.

In computing the tube-side coefficient, $h_{i}$, it is assumed that all tubes in the exchanger are exposed to the same thermal and hydraulic conditions. The value of $h_{i}$ is then the same for all tubes, and the calculation can be made for a single tube. Equation (2.33), (2.36), (2.37), or (2.38) is used, depending on the flow regime. In computing the Reynolds number, however, the mass flow rate per tube must be used, where

$$
\begin{equation*}
\dot{m}_{\text {per tube }}=\frac{\dot{m}_{t} n_{p}}{n_{t}} \tag{3.19}
\end{equation*}
$$

and

$$
\begin{aligned}
\dot{m}_{t} & =\text { total mass flow rate of tube-side fluid } \\
n_{p} & =\text { number of tube-side passes } \\
n_{t} & =\text { number of tubes }
\end{aligned}
$$

Equation (3.19) simply states that the flow rate in a single tube is the total flow rate divided by the number of fluid circuits, which is $n_{t} / n_{p}$. With the exception of this minor modification, the calculation of $h_{i}$ is the same as for a double-pipe exchanger.


Figure 3.12 Correlation for shell-side heat-transfer coefficient. For rotated square tube layouts, use the parameter values for square pitch and replace $P_{T}$ with $P_{T} / \sqrt{2}$ in the equation for $a_{S}$ (Source: Wolverine Tube, Inc. Originally published in Ref. [4]).

The most rigorous method available for computing the shell-side coefficient, $h_{o}$, is the stream analysis method developed by Heat Transfer Research, Inc. (HTRI) [6]. The method utilizes an iterative procedure to compute the various leakage streams in the shell, and therefore must be implemented on a computer. Although the method has been described in the open literature [6], some of the data needed to implement the method remain proprietary. The most accurate method available in the public domain is the Delaware method [12,13]. Although the method is conceptually simple, it is quite lengthy and involved, and will be presented in a later chapter.

The method that will be used here is a simplified version of the Delaware method presented in Ref. [4]. Although not highly accurate, the method is very straightforward and allows us to present the overall rating procedure without being bogged down in a mass of details. Also, the method has a built-in safety factor, and therefore errors are generally on the safe side. The method utilizes the graph of modified Colburn factor, $j_{H}$, versus shell-side Reynolds number shown in Figure 3.12. All symbols used on the graph are defined in the key. The graph is valid for segmental baffles with a $20 \%$ cut, which is approximately the optimum cut [4]. It is also based on TEMA standards for tube-to-baffle and baffle-to-shell clearances [5]. To use Figure 3.12, one simply reads $j_{H}$ from the graph and then computes $h_{o}$ from

$$
\begin{equation*}
h_{o}=j_{H}\left(\frac{k}{D_{e}}\right) \operatorname{Pr}^{1 / 3}\left(\frac{\mu}{\mu_{w}}\right)^{0.14} \tag{3.20}
\end{equation*}
$$

An approximate curve fit to Figure 3.12, which is convenient for implementation on a programmable calculator or computer, is:

$$
\begin{equation*}
j_{H}=0.5\left(1+B / d_{s}\right)\left(0.08 R e^{0.6821}+0.7 R e^{0.1772}\right) \tag{3.21}
\end{equation*}
$$

A general algorithm for thermal rating of a shell-and-tube heat exchanger is presented in Figure 3.13. The algorithm is also applicable to other types of heat-exchange equipment with minor modifications. The decision as to whether or not the exchanger is thermally suitable for a given service is based on
a comparison of calculated versus required overall heat-transfer coefficients. The exchanger is suitable if the calculated value of the design coefficient, $U_{D}$, is greater than or equal to the value, $U_{\text {req }}$, that is needed to provide the required rate of heat transfer. If the converse is true, the exchanger is "not suitable". The quotation marks are to indicate that the final decision to reject the exchanger should be tempered by engineering judgment. For example, it may be more economical to utilize an existing exchanger that is slightly undersized, and therefore may require more frequent cleaning, than to purchase a larger exchanger. In principle, the rating decision can be based on a comparison of heattransfer areas, heat-transfer rates, or mean temperature differences as well as heat-transfer coefficients. In fact, all of these parameters are used as decision criteria in various applications. The algorithm presented here has the advantage that the fouling factors, which are usually the parameters with the greatest associated uncertainty, do not enter the calculation until the final step. Frequently, one can unambiguously reject an exchanger in Step 3 before the fouling factors enter the calculation.

It should again be noted that the rating procedure given in Figure 3.13 includes only the thermal analysis of the exchanger. A complete rating procedure must include a hydraulic analysis as well. That is, the pressure drops of both streams must be computed and compared with the specified maximum allowable pressure drops. The tube-side pressure drop is readily computed by the friction factor method for pipe flow with appropriate allowances for the additional losses in the headers and nozzles. The calculation of shell-side pressure drop is beset with the same difficulties as the heat-transfer coefficient. Each of the methods (Stream Analysis, Delaware, Simplified Delaware) discussed above includes an algorithm for calculation of the shell-side pressure drop. These procedures are presented in subsequent chapters.
(1) Calculate the required overall coefficient.

$$
U_{r e q}=\frac{q}{A F\left(\Delta T_{\ln }\right)_{c f}}
$$

(2) Calculate the clean overall coefficient.

$$
\begin{equation*}
U_{C}=\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}\right]^{-1} \tag{3}
\end{equation*}
$$


(4) Obtain required fouling factors, $R_{D i}$ and $R_{D o}$, from past experience or from Table 3.2. Then compute:

$$
R_{D}=R_{D i}\left(D_{o} / D_{i}\right)+R_{D o}
$$

(5) Calculate the design overall coefficient.
)

$$
\begin{equation*}
U_{D}=\left(1 / U_{C}+R_{D}\right)^{-1} \tag{6}
\end{equation*}
$$

Figure 3.13 Thermal rating procedure for a shell-and-tube heat exchanger.

The thermal rating procedure for a shell-and-tube heat exchanger is illustrated in the following example.

## Example 3.5

$30,000 \mathrm{lb} / \mathrm{h}$ of kerosene are to be cooled from $400^{\circ} \mathrm{F}$ to $250^{\circ} \mathrm{F}$ by heat exchange with $75,000 \mathrm{lb} / \mathrm{h}$ of gas oil which is at $110^{\circ} \mathrm{F}$. Available for this duty is a shell-and-tube exchanger having 156 tubes in a $21 \frac{1}{4}-\mathrm{in}$. ID shell. The tubes are $1-\mathrm{in}$. OD, $14 \mathrm{BWG}, 16 \mathrm{ft}$ long on a $1 \frac{1}{4}-\mathrm{in}$. square pitch. There is one pass on the shell side and six passes on the tube side. The baffles are $20 \%$ cut segmental type and are spaced at 5 -in. intervals. Both the shell and tubes are carbon steel having $k=26 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$. Fluid properties are given in Example 3.4. Will the exchanger be thermally suitable for this service?

## Solution

Neither fluid is corrosive, but the oil stream may cause fouling problems so it should be placed in the tubes for ease of cleaning. Also, the kerosene should be placed in the shell due to its large $\Delta T$.

Step 1: Calculate $U_{\text {req }}$.
From Example 3.4, we have:

$$
\begin{aligned}
q & =2.7 \times 10^{6} \mathrm{Btu} / \mathrm{h} \\
F & =0.93 \\
\left(\Delta T_{\ln }\right)_{c f} & =176^{\circ} \mathrm{F}
\end{aligned}
$$

The surface area is obtained from the dimensions of the exchanger:

$$
A=156 \text { tubes } \times 16 \mathrm{ft} \times 0.2618 \frac{\mathrm{ft}^{2}}{\mathrm{ft} \text { of tube }}=653 \mathrm{ft}^{2}
$$

Thus,

$$
\begin{aligned}
U_{\text {req }} & =\frac{q}{A F\left(\Delta T_{\ln }\right)_{c f}}=\frac{2.7 \times 10^{6}}{653 \times 0.93 \times 176} \\
U_{\text {req }} & =25.3 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .^{\circ} \mathrm{F}
\end{aligned}
$$

Step 2: Calculate the clean overall coefficient, $U_{C}$.
(a) Calculate the tube-side Reynolds number.

$$
\begin{aligned}
\dot{m}_{\text {per tube }} & =\frac{75,000 \times 6}{156}=2885 \mathrm{lb} / \mathrm{h} \\
R e & =\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 2885}{\pi \times \frac{0.834}{12} \times 3.5 \times 2.419}=6243 \Rightarrow \text { transition region }
\end{aligned}
$$

(b) Calculate $h_{i}$.

$$
\begin{aligned}
N u & =\frac{h_{i} D_{i}}{k}=0.116\left[R e^{2 / 3}-125\right] \operatorname{Pr}^{1 / 3}(\mu / \mu w)^{0.14}\left[1+\left(D_{i} / L\right)^{2 / 3}\right] \\
h_{i} & =\frac{0.08}{(0.834 / 12)} \times 0.116\left[(6243)^{2 / 3}-125\right]\left(\frac{0.5 \times 3.5 \times 2.419}{0.08}\right)^{1 / 3}(1)\left[1+\left(\frac{0.834}{12 \times 16}\right)^{2 / 3}\right] \\
h_{i} & =110 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

In this calculation, the viscosity correction factor was assumed to be unity since no data were given for the temperature dependence of the oil viscosity.
(c) Calculate the shell-side Reynolds number.

From Figure 3.12, $d_{e}=0.99 \mathrm{in}$. and $C^{\prime}=0.250 \mathrm{in}$.

$$
\begin{aligned}
D_{e} & =d_{e} / 12=0.99 / 12=0.0825 \mathrm{ft} \\
a_{s} & =\frac{d_{s} C^{\prime} B}{144 P_{T}}=\frac{21.25 \times 0.250 \times 5}{144 \times 1.25}=0.1476 \mathrm{ft}^{2} \\
G & =\frac{\dot{m}}{a_{s}}=\frac{30,000}{0.1476}=203,294 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =\frac{D_{e} G}{\mu}=\frac{0.0825 \times 203,294}{0.45 \times 2.419}=15,407
\end{aligned}
$$

(d) Calculate $h_{o}$.

$$
B / d_{s}=5 / 21.25=0.235
$$

From Figure 3.12, $j_{H} \cong 40$. [Equation (3.21) gives $j_{H}=37.9$.]

$$
\begin{align*}
& h_{o}=j_{H} \frac{k}{D_{e}} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14}=\frac{40 \times 0.077}{0.0825}\left(\frac{0.60 \times 0.45 \times 2.419}{0.077}\right)^{1 / 3}  \tag{1}\\
& h_{o}=76 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{align*}
$$

(e) Calculate $U_{C}$.

$$
\begin{aligned}
U_{C} & =\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}\right]^{-1}=\left[\frac{1.0}{110 \times 0.834}+\frac{(1.0 / 12) \ln (1.0 / 0.834)}{2 \times 26}+\frac{1}{76}\right]^{-1} \\
U_{C} & =41.1 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Since $U_{C}>U_{\text {req }}$, proceed to Step 3.

Step 3: Obtain the required fouling factors.
In the absence of other information, Table 3.3 indicates fouling factors of 0.002$0.003 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ for kerosene and $0.002-0.005 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ for gas oil. Taking 0.0025 for kerosene and 0.0035 for gas oil gives:

$$
R_{D}=\frac{R_{D i} D_{o}}{D_{i}}+R_{D o}=\frac{0.0035 \times 1.0}{0.834}+0.0025=0.0067 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
$$

Step 4: Calculate $U_{D}$.

$$
U_{D}=\left(1 / U_{C}+R_{D}\right)^{-1}=(1 / 41.1+0.0067)^{-1} \cong 32 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

Since this value is greater than the required value of $25.3 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$, the exchanger is thermally suitable. In fact, a smaller exchanger would be adequate.

In the above example, the average tube-wall temperature was not required because the variation of fluid properties with temperature was ignored. In general, however, the wall temperature is required and is calculated using Equation (3.18) in the same manner as illustrated for a double-pipe exchanger in Example 3.3.

### 3.9 Heat-Exchanger Effectiveness

When the area of a heat exchanger is known and the outlet temperatures of both streams are to be determined, an iterative calculation using Equation (3.1) and the energy balance equations for the two streams is generally required. Since the calculations required for each iteration are quite lengthy, the procedure is best implemented on a computer or programmable calculator. However, in those situations in which the overall coefficient is known or can be estimated a priori, the iterative procedure can be avoided by means of a quantity called the heat-exchanger effectiveness.

The effectiveness is defined as the ratio of the actual rate of heat transfer in a given exchanger to the maximum possible rate of heat transfer. The latter is the rate of heat transfer that would occur in a counter-flow exchanger having infinite heat-transfer area. In such an exchanger, one of the fluid streams will gain or lose heat until its outlet temperature equals the inlet temperature of the other stream. The fluid that experiences this maximum temperature change is the one having the smaller value of $C \equiv \dot{m} C_{P}$, as can be seen from the energy balance equations for the two streams. Thus, if the hot fluid has the lower value of $C$, we will have $T_{h, \text { out }}=T_{c, i n}$, and:

$$
q_{\max }=\dot{m}_{h} C_{P h}\left(T_{h, i n}-T_{c, i n}\right)=C_{\min }\left(T_{h, i n}-T_{c, i n}\right)
$$

On the other hand, if the cold fluid has the lower value of $C$, then $T_{c, \text { out }}=T_{h, i n}$, and:

$$
q_{\max }=\dot{m}_{c} C_{P c}\left(T_{h, i n}-T_{c, i n}\right)=C_{\min }\left(T_{h, i n}-T_{c, i n}\right)
$$

Thus, in either case we can write:

$$
\begin{equation*}
q_{\max }=C_{\min }\left(T_{h, i n}-T_{c, i n}\right)=C_{\min } \Delta T_{\max } \tag{3.22}
\end{equation*}
$$

where $\Delta T_{m a x}=T_{h, i n}-T_{c, i n}$ is the maximum temperature difference that can be formed from the terminal stream temperatures.

Now, by definition the effectiveness, $\varepsilon$, is given by:

$$
\begin{equation*}
\varepsilon=\frac{q}{q_{\max }}=\frac{q}{C_{\min } \Delta T_{\max }} \tag{3.23}
\end{equation*}
$$

Thus, the actual heat-transfer rate can be expressed as:

$$
\begin{equation*}
q=\varepsilon C_{\min } \Delta T_{\max } \tag{3.24}
\end{equation*}
$$

It can be shown (see, e.g., Ref. [14]) that for a given type of exchanger the effectiveness depends on only two parameters, $r$ and $N T U$, where:

$$
\begin{gather*}
r \equiv C_{\min } / C_{\max }  \tag{3.25}\\
N T U \equiv U A / C_{\min } \tag{3.26}
\end{gather*}
$$

Here, NTU stands for number of transfer units, a terminology derived by analogy with continuouscontacting mass-transfer equipment. Equations for the effectiveness are available in the literature (e.g., Ref. [14]) for various types of heat exchangers. Equations for the heat exchanger configurations considered in this chapter are given in Table 3.6. Their use is illustrated in the following example.

## Example 3.6

Determine the outlet temperature of the kerosene and gas oil streams when the exchanger of Example 3.5 is first placed in service.

Table 3.6 Effectiveness Relations for Various Heat Exchangers
$r \equiv C_{\text {min }} / C_{\text {max }} \quad N T U \equiv U A / C_{\text {min }}$

| Exchanger type | Effectiveness equation |
| :--- | :--- |
| Counter flow | $\varepsilon=\frac{1-\exp [-N T U(1-r)]}{1-r \exp [-N T U(1-r)]} \quad(r<1)$ |
| $\varepsilon=\frac{N T U}{1+N T U} \quad(r=1)$ |  |
| Parallel flow | $\varepsilon=\frac{1-\exp [-N T U(1+r)]}{1+r}$ |
| $1-2$ | $\varepsilon=2\left[1+r+\beta\left(\frac{1+\exp [-\beta \times N T U]}{1-\exp [-\beta \times N T U]}\right)\right]^{-1}$ |
|  | where $\beta=\sqrt{1+r^{2}}$ |
| $N-2 N$ | $\varepsilon=\left[\left(\frac{1-\varepsilon^{*} r}{1-\varepsilon^{*}}\right)^{N}-1\right] \times\left[\left(\frac{1-\varepsilon^{*} r}{1-\varepsilon^{*}}\right)^{N}-r\right]^{-1} \quad(r<1)$ |
| (For a 2-4 exchanger, | $\varepsilon=\frac{N \varepsilon^{*}}{1+(N-1) \varepsilon^{*}} \quad(r=1)$ |
| $N=2 ;$ etc.) | where $\varepsilon^{*}$ is the effectiveness for a $1-2$ <br> exchanger with the same value of $r$ but with $(1 / N)$ <br> times the NTU value |

## Solution

We have:

$$
\begin{aligned}
C_{k e r} & =\left(\dot{m} C_{P}\right)_{k e r}=30,000 \times 0.6=18,000 \mathrm{Btu} / \mathrm{h} \cdot{ }^{\circ} \mathrm{F} \\
C_{o i l} & =\left(\dot{m} C_{P}\right)_{\text {oil }}=75,000 \times 0.5=37,500 \mathrm{Btu} / \mathrm{h} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
& C_{\text {min }}=18,000 \\
& C_{\text {max }}=37,500 \\
& r=C_{\text {min }} / C_{\text {max }}=18,000 / 37,500=0.48
\end{aligned}
$$

When the exchanger is first placed in service, the overall coefficient will be the clean coefficient computed in Example 3.5 (neglecting the effect of different average stream temperatures on the overall coefficient). Thus,

$$
N T U=U A / C_{\min }=\frac{41.1 \times 653}{18,000}=1.4910
$$

From Table 3.6, for a 1-2 exchanger:

$$
\varepsilon=2\left[1+r+\beta\left(\frac{1+\exp [-\beta \times N T U]}{1-\exp [-\beta \times N T U]}\right)\right]^{-1}
$$

where

$$
\beta=\sqrt{1+r^{2}}=\sqrt{1+(0.48)^{2}}=1.1092
$$

Thus,

$$
\begin{aligned}
& \varepsilon=2 \times\left[1+0.48+1.1092\left(\frac{1+\exp [-1.1092 \times 1.4910]}{1-\exp [-1.1092 \times 1.4910]}\right)\right]^{-1} \\
& \varepsilon=0.6423
\end{aligned}
$$

From Equation (3.24) we have:

$$
\begin{aligned}
& q=\varepsilon C_{\min } \Delta T_{\max } \\
& q=0.6423 \times 18,000 \times(400-110) \\
& q=3.35 \times 10^{6} \mathrm{Btu} / \mathrm{h}
\end{aligned}
$$

The outlet temperatures can now be computed from the energy balances on the two streams.

$$
\begin{aligned}
& q=3.35 \times 10^{6}=\left(\dot{m} C_{P} \Delta T\right)_{k e r}=18,000 \times \Delta T_{k e r} \\
& \Delta T_{k e r}=186^{\circ} \mathrm{F} \\
& T_{\text {ker }, \text { out }}=400-186=214^{\circ} \mathrm{F} \\
& \\
& q=3.35 \times 10^{6}=\left(\dot{m} C_{P} \Delta T\right)_{o i l}=37,500 \times \Delta T_{\text {oil }} \\
& \Delta T_{\text {oil }}=89^{\circ} \mathrm{F} \\
& T_{\text {oil,out }}=110+89=199^{\circ} \mathrm{F}
\end{aligned}
$$

Thus, as expected, the exchanger will initially far exceed the design specification of $250^{\circ} \mathrm{F}$ for the kerosene outlet temperature.

## References

1. R. H. Perry and D. W. Green, eds, Perry's Chemical Engineers' Handbook, 7th edn, McGraw-Hill, New York, 1997.
2. Heat Exchanger Design Handbook, Hemisphere Publishing Corp., New York, 1988.
3. Kakac, S. and H. Liu, Heat Exchangers: Selection, Rating and Thermal Design, CRC Press, Boca Raton, FL, 1997.
4. Kern, D. Q. and A. D. Kraus, Extended Surface Heat Transfer, McGraw-Hill, New York, 1972.
5. Standards of the Tubular Exchanger Manufacturers Association, 8th edn, Tubular Exchanger Manufacturers Association, Inc., Tarrytown, NY, 1999.
6. Palen, J. W. and J. Taborek, Solution of shell side flow pressure drop and heat transfer by stream analysis method, Chem. Eng. Prog. Symposium Series, 65, No. 92, 53-63, 1969.
7. Chenoweth, J., Final report of HTRI/TEMA joint committee to review the fouling section of TEMA Standards, Heat Transfer Research, Inc., Alhambra, CA, 1988.
8. Anonymous, Engineering Data Book, 11th edn, Gas Processors Suppliers Association, Tulsa, OK, 1998.
9. Bowman, R. A., A. C. Mueller and W. M. Nagle, Mean temperature difference in design, Trans. ASME, 62, 283-294, 1940.
10. Kern, D. Q., Process Heat Transfer, McGraw-Hill, New York, 1950.
11. Bell, K. J., Approximate sizing of shell-and-tube heat exchangers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
12. Bell, K. J., Exchanger design based on the Delaware research program, Pet. Eng., 32, No. 11, C26, 1960.
13. Taborek, J., Shell-and-tube heat exchangers: single phase flow, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
14. Holman, J. P., Heat Transfer, 7th edn, McGraw-Hill, New York, 1990.

## Appendix 3.A Derivation of the Logarithmic Mean Temperature Difference

Use of the logarithmic mean temperature difference and the LMTD correction factor for the thermal analysis of heat exchangers under steady-state conditions involves the following simplifying assumptions:

- The overall heat-transfer coefficient is constant throughout the heat exchanger.
- The specific enthalpy of each stream is a linear function of temperature. For a single-phase fluid, this implies that the heat capacity is constant.
- There is no heat transfer between the heat exchanger and its surroundings, i.e., no heat losses.
- For co-current and counter-current flow, the temperature of each fluid is uniform over any crosssection in the exchanger. For multi-tube exchangers, this implies that the conditions in every tube are identical.
- For multi-tube, multi-pass exchangers, the conditions in every tube within a given pass are identical.
- There is an equal amount of heat-transfer surface area in each pass of a multi-pass heat exchanger. Although not strictly necessary, the equations and graphs commonly used to calculate the LMTD correction factor for shell-and-tube exchangers are based on this assumption.
- There is no heat generation or consumption within the exchanger due to chemical reaction or other causes.
- There is no heat transfer in the axial direction along the length of the heat exchanger.

Now consider a counter-flow heat exchanger for which the temperatures of both streams increase as one moves along the length of the exchanger from the cold end (1) to the hot end (2). The rate of heat transfer between the fluids in a differential section of the exchanger is:

$$
\begin{equation*}
d q=U d A\left(T_{h}-T_{c}\right)=U d A \Delta T \tag{3.A.1}
\end{equation*}
$$

where $\Delta T=T_{h}-T_{c}$ is the local driving force for heat transfer and subscripts $h$ and $c$ denote the hot and cold streams, respectively. For single-phase operation, the differential energy balances on
the two streams are:

$$
\begin{equation*}
d q=C_{h} d T_{h}=C_{c} d T_{c} \tag{3.A.2}
\end{equation*}
$$

where $C \equiv \dot{m} C_{P}$. The stream energy balances over the entire exchanger are:

$$
\begin{equation*}
q=C_{h}\left(T_{h, a}-T_{h, b}\right)=C_{c}\left(T_{c, b}-T_{c, a}\right) \tag{3.A.3}
\end{equation*}
$$

where subscripts $a$ and $b$ denote inlet and outlet, respectively. Using Equation (3.A.2), the differential of the driving force can be written as follows:

$$
\begin{equation*}
d(\Delta T)=d T_{h}-d T_{c}=\frac{d q}{C_{h}}-\frac{d q}{C_{c}}=d q\left(\frac{1}{C_{h}}-\frac{1}{C_{c}}\right) \tag{3.A.4}
\end{equation*}
$$

Using this relationship along with Equation (3.A.1) gives:

$$
\begin{equation*}
\frac{d(\Delta T)}{\Delta T}=\frac{d q\left(\frac{1}{C_{h}}-\frac{1}{C_{c}}\right)}{d q / U d A}=U d A\left(\frac{1}{C_{h}}-\frac{1}{C_{c}}\right) \tag{3.A.5}
\end{equation*}
$$

Integrating this equation over the length of the heat exchanger we obtain:

$$
\begin{align*}
& \int_{\Delta T_{1}}^{\Delta T_{2}} \frac{d(\Delta T)}{\Delta T}=U\left(\frac{1}{C_{h}}-\frac{1}{C_{c}}\right) \int_{0}^{A} d A \\
& \ln \left(\Delta T_{2} / \Delta T_{1}\right)=U\left(\frac{1}{C_{h}}-\frac{1}{C_{c}}\right) A \tag{3.A.6}
\end{align*}
$$

where

$$
\begin{aligned}
& \Delta T_{1}=T_{h, b}-T_{c, a}=\text { driving force at cold end of exchanger } \\
& \Delta T_{2}=T_{h, a}-T_{c, b}=\text { driving force at hot end of exchanger }
\end{aligned}
$$

Substituting for $C_{h}$ and $C_{c}$ from Equation (3.A.3) gives:

$$
\begin{aligned}
\ln \left(\Delta T_{2} / \Delta T_{1}\right) & =U A\left\{\frac{T_{h, a}-T_{h, b}}{q}-\frac{T_{c, b}-T_{c, a}}{q}\right\} \\
& =\frac{U A}{q}\left\{\left(T_{h, a}-T_{c, b}\right)-\left(T_{h, b}-T_{c, a}\right)\right\} \\
& =\frac{U A}{q}\left\{\Delta T_{2}-\Delta T_{1}\right\}
\end{aligned}
$$

It follows from this result that:

$$
\begin{equation*}
q=U A\left\{\frac{\Delta T_{2}-\Delta T_{1}}{\ln \left(\Delta T_{2} / \Delta T_{1}\right)}\right\}=U A \Delta T_{\ln } \tag{3.A.7}
\end{equation*}
$$

Equation (3.A.7) is the desired result, demonstrating that the mean temperature difference in the exchanger is the LMTD. The derivation for co-current flow is similar and requires only minor modifications of the foregoing analysis.

| Notations |  |
| :---: | :---: |
| A | Surface area |
| $A_{i}$ | $\pi D_{i} L=$ Interior surface area of pipe or tube |
| $A_{0}$ | $\pi D_{0} L=$ Exterior surface area of pipe or tube |
| $a_{s}$ | Flow area across tube bundle |
| $B$ | Baffle spacing |
| C | $\dot{m} C_{P}$ |
| $C_{c}, C_{h}$ | Value of $C$ for cold and hot stream, respectively |
| $C_{\text {max }}$ | Larger of the values of $\dot{m} C_{P}$ for hot and cold streams |
| $C_{\text {min }}$ | Smaller of the values of $\dot{m} C_{P}$ for hot and cold streams |
| $C^{\prime}$ | $P_{T}-D_{o}=$ Clearance between tubes in tube bundle |
| $C_{P}$ | Heat capacity at constant pressure |
| $C_{P c}, C_{P h}$ | Heat capacity of cold and hot streams, respectively |
| D | Diameter |
| $D_{e}$ | Equivalent diameter |
| $D_{i}$ | Inside diameter of pipe or tube |
| $D_{0}$ | Outside diameter of pipe or tube |
| $D_{1}$ | Outside diameter of inner pipe of double-pipe heat exchanger |
| $D_{2}$ | Inside diameter of outer pipe of double-pipe heat exchanger |
| $d_{e}$ | Equivalent diameter expressed in inches |
| $d_{s}$ | Inside diameter of shell |
| $F$ | LMTD correction factor |
| $G$ | Mass flux |
| $h$ | Heat-transfer coefficient |
| $h_{i}$ | Heat-transfer coefficient for inner (tube-side) fluid |
| $h_{o}$ | Heat-transfer coefficient for outer (shell-side) fluid |
| $j_{H}$ | $\left(h_{o} D_{e} / k\right) \operatorname{Pr}^{-1 / 3}\left(\mu / \mu_{w}\right)^{-0.14}=$ Modified Colburn factor for shell-side heat transfer |
| $k$ | Thermal conductivity |
| $L$ | Length of pipe or tube |
| $\dot{m}$ | Mass flow rate |
| $\dot{m}_{t}$ | Total mass flow rate of tube-side fluid |
| $N$ | Number of shell-side passes |
| $n_{p}$ | Number of tube-side passes |
| $n_{t}$ | Number of tubes in tube bundle |
| NTU | $U A / C_{\text {min }}=$ Number of transfer units |
| $N u$ | Nusselt number |
| $P$ | Parameter used to calculate LMTD correction factor; defined by Equation (3.12) |
| $P_{T}$ | Tube pitch |
| Pr | Prandtl number |
| $q$ | Rate of heat transfer |
| $q_{\text {max }}$ | Maximum possible rate of heat transfer in a counter-flow heat exchanger |
| $R$ | Parameter used to calculate LMTD correction factor; defined by Equation (3.11) |
| $R_{D}$ | Fouling factor |
| $R_{\text {Di }}$ | Fouling factor for inner (tube-side) fluid |
| $R_{\text {Do }}$ | Fouling factor for outer (shell-side) fluid |
| $R_{\text {th }}$ | Thermal resistance |
| $R e$ | Reynolds number |
| $r$ | $C_{\text {min }} / C_{\text {max }}=$ Parameter used to calculate heat-exchanger effectiveness |
| $S$ | Parameter used in calculating LMTD correction factor; defined by Equation (3.16) |
| $T$ | Temperature |
| $T_{a}$ | Inlet temperature of shell-side fluid |
| $T_{b}$ | Outlet temperature of shell-side fluid |
| $T_{\text {ave }}$ | Average temperature of shell-side fluid |

$T_{c} \quad$ Cold fluid temperature
$T_{c, a}, T_{c, b}$ Inlet and outlet temperatures of cold stream
$T_{h} \quad$ Hot fluid temperature
$T_{h, a}, T_{h, b}$ Inlet and outlet temperatures of hot stream
$T_{w} \quad$ Average temperature of tube wall
$t_{a} \quad$ Inlet temperature of tube-side fluid
$t_{b} \quad$ Outlet temperature of tube-side fluid
$t_{\text {ave }} \quad$ Average temperature of tube-side fluid
$U \quad$ Overall heat-transfer coefficient
$U_{C} \quad$ Clean overall heat-transfer coefficient
$U_{D} \quad$ Design overall heat-transfer coefficient
$U_{\text {req }} \quad$ Required overall heat-transfer coefficient

## Greek Letters

Parameter used to calculate LMTD correction factor; defined by Equation (3.13)
$\beta \quad \sqrt{1-r^{2}}=$ Parameter used in calculating heat-exchanger effectiveness
$\Delta T \quad$ Temperature difference
$\Delta T_{m} \quad$ Mean temperature difference in a heat exchanger
$\Delta T_{\ln } \quad$ Logarithmic mean temperature difference
$\left(\Delta T_{\ln }\right)_{c f} \quad$ Logarithmic mean temperature difference for counter-current flow
$\Delta T_{\max } \quad T_{h, i n}-T_{c, \text { in }}=$ Temperature difference between inlet streams to a heat exchanger
$\Delta T_{1}, \Delta T_{2}$ Temperature differences between the fluids at the two ends of a heat exchanger
$\varepsilon \quad$ Heat-exchanger effectiveness
$\varepsilon^{*} \quad$ Parameter defined in Table 3.6 and used to calculate effectiveness of shell-and-tube heat exchanger having multiple shell passes
$\mu \quad$ Viscosity
$\mu_{w} \quad$ Fluid viscosity at average tube-wall temperature
$\phi \quad$ Viscosity correction factor
$\phi_{i} \quad$ Viscosity correction factor for inner (tube-side) fluid
$\phi_{0} \quad$ Viscosity correction factor for outer (shell-side) fluid

## Problems

(3.1) In a double-pipe heat exchanger, the cold fluid will enter at $30^{\circ} \mathrm{C}$ and leave at $60^{\circ} \mathrm{C}$, while the hot fluid will enter at $100^{\circ} \mathrm{C}$ and leave at $70^{\circ} \mathrm{C}$. Find the mean temperature difference in the heat exchanger for:
(a) Co-current flow.
(b) Counter-current flow.

Ans. (a) $30.83^{\circ} \mathrm{C}$.
(3.2) In Problem 3.1 the inner pipe is made of $3-\mathrm{in}$. schedule 40 carbon steel ( $k=45 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ). The cold fluid flows through the inner pipe with a heat-transfer coefficient of $600 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$, while the hot fluid flows in the annulus with a heat-transfer coefficient of $1000 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The exchanger duty is 140 kW . Calculate:
(a) The average wall temperature of the inner pipe.
(b) The clean overall heat-transfer coefficient.
(c) The design overall heat-transfer coefficient using a fouling factor of $0.002 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ for each stream. (Note the units.)
(d) The total length of pipe required in the heat exchanger for counter-current flow.
(e) The total length of pipe required in the heat exchanger for co-current flow.

Ans. (a) $71.2^{\circ} \mathrm{C}$. (b) $330 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. (c) $264 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. (d) 149 m .
(3.3) A brine cooler in a chemical plant consists of a 1-2 shell-and-tube heat exchanger containing 80 tubes, each of which is $1-\mathrm{in}$. OD, 16 BWG and 15 ft long. $90,000 \mathrm{lb} / \mathrm{h}$ of brine flows through the tubes and is cooled from $16^{\circ} \mathrm{F}$ to $12^{\circ} \mathrm{F}$. Ammonia enters the shell as a saturated liquid at $5^{\circ} \mathrm{F}$ and leaves as a saturated vapor at $5^{\circ} \mathrm{F}$. The heat capacity of the brine is $0.7 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$. Refrigeration equipment is commonly rated in tons of refrigeration, where by definition, 1 ton of refrigeration is equal to $12,000 \mathrm{Btu} / \mathrm{h}$.
(a) How many tons of refrigeration does the brine cooler deliver?
(b) How many square feet of heat-transfer surface does the cooler contain?
(c) Use Equations (3.11)-(3.17) to show that $F=1.0$ for the brine cooler.
(d) Determine the value of the overall heat-transfer coefficient that is achieved in the brine cooler.

Ans. (a) 21. (b) 314. (d) $91 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(3.4) The gas heater shown below in cross-section consists of a square sheet-metal duct insulated on the outside and a steel pipe ( 5 cm OD, 4.85 cm ID, $k=56 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ ) that passes through the center of the duct. A heat-transfer fluid will flow in the pipe, entering at 500 K and leaving at 450 K , with a heat-transfer coefficient of $200 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. Process air will enter the heater at 300 K with a flow rate of $0.35 \mathrm{~kg} / \mathrm{s}$, leave at 350 K , and flow counter currently to the heattransfer fluid. The heat-transfer coefficient for the air has been calculated and its value is $55 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. Fouling factors of $0.00018 \mathrm{~m}^{2} \cdot \mathrm{~K} / \mathrm{W}$ for the air stream and $0.00035 \mathrm{~m}^{2} \cdot \mathrm{~K} / \mathrm{W}$ for the heat-transfer fluid are specified.
(a) Calculate the value of the overall heat-transfer coefficient to be used for designing the heater.
(b) What is the mean temperature difference in the heater?
(c) Calculate the required length of the heater.


Ans. (a) $42 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. (c) 18 m .
(3.5) In a refinery $100,000 \mathrm{lb} / \mathrm{h}$ of fuel oil is to be cooled from $200^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$ by heat exchange with $70,000 \mathrm{lb} / \mathrm{h}$ of cooling water that is available at $60^{\circ} \mathrm{F}$. A shell-and-tube exchanger will be used. The heat capacities are $0.6 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ for the oil and $1.0 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ for the water.
(a) Use stream energy balances to calculate the duty for the exchanger and the outlet temperature of the cooling water.
(b) Determine whether or not a 1-2 exchanger can be used for this service. If not, how many shell passes will be needed?
(c) Refer to Table 3.5 and obtain an approximate value for the overall heat-transfer coefficient. Use this value to calculate the heat-transfer surface area for the exchanger.
(d) If $3 / 4-\mathrm{in}$., 16 BWG tubes with a length of 20 ft are used in the heat exchanger, how many tubes will be required to supply the surface area calculated in part (c)?

Ans. (a) $5.4 \times 10^{6} \mathrm{Btu} / \mathrm{h} ; 137.1^{\circ} \mathrm{F}$.
(3.6) A shell-and-tube heat exchanger will be used to cool $200,000 \mathrm{lb} / \mathrm{h}$ of gasoline from $152^{\circ} \mathrm{F}$ to $80^{\circ} \mathrm{F}$. Cooling water with a range of $60-100^{\circ} \mathrm{F}$ will be used. Heat capacities are $0.6 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ for gasoline and $10 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ for water.
(a) What flow rate of cooling water will be needed?
(b) How many E-shells will be required for the heat exchanger?
(c) Make a preliminary design calculation to estimate the heat-transfer surface area required in the heat exchanger.
(d) If 1-in. 14 BWG tubes 25 ft long are used, how many tubes will be needed to supply the heat-transfer area computed in part (c)?

Ans. (a) $216,000 \mathrm{lb} / \mathrm{h}$. (b) 2.
(3.7) In a petrochemical complex $150,000 \mathrm{lb} / \mathrm{h}$ of trichloroethylene is to be heated from $60^{\circ} \mathrm{F}$ to $140^{\circ} \mathrm{F}$ using $90,000 \mathrm{lb} / \mathrm{h}$ of kerosene that is available at $200^{\circ} \mathrm{F}$. Heat capacities are $0.35 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ for trichloroethylene and $0.6 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ for kerosene. A shell-and-tube heat exchanger will be used for this service.
(a) Will a 1-2 heat exchanger be satisfactory? If not, how many shell-side passes should be used?
(b) Make a preliminary design calculation to estimate the heat-transfer surface area required in the heat exchanger.
(c) If the tube bundle is to consist of 1.25 -in. 16 BWG tubes with a length of 16 ft , how many tubes will the bundle contain?
(3.8) A counter-flow heat exchanger was designed to cool $13,000 \mathrm{lb} / \mathrm{h}$ of $100 \%$ acetic acid from $250^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ by heating $19,000 \mathrm{lb} / \mathrm{h}$ of butyl alcohol from $100^{\circ} \mathrm{F}$ to $157^{\circ} \mathrm{F}$. An overall heat-transfer coefficient of $85 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ was used for the design. When first placed in service, the acetic acid outlet temperature was found to be $117^{\circ} \mathrm{F}$. It gradually rose to $135^{\circ} \mathrm{F}$ over a period of several months and then remained essentially constant, indicating that the exchanger was over-sized.
(a) Use the design data to calculate the amount of heat-transfer surface area in the heat exchanger.
(b) Use the initial operating data to calculate the value of the clean overall heat-transfer coefficient.
(c) Use the final operating data to calculate the value of the overall heat-transfer coefficient after fouling has occurred.
(d) Use the values of $U_{C}$ and $U_{D}$ found in parts (b) and (c) to obtain the correct (experimental) value of the total fouling factor, $R_{D} \equiv R_{D i}\left(D_{o} / D_{i}\right)+R_{D o}$, for the system.

Ans. (a) $121 \mathrm{ft}^{2}$. (b) $196 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (c) $121 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (d) $0.0032 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$.
(3.9) A heat exchanger consists of two E-shells connected in series and contains a total of 488 tubes arranged for four passes (two per shell). The tubes are 1-in. OD, 16 BWG with a length of 10 ft . The heat exchanger was designed to cool a hot fluid from $250^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ using a cold fluid entering at $100^{\circ} \mathrm{F}$. When the exchanger was first placed in service, the hot fluid outlet
temperature was $130^{\circ} \mathrm{F}$, but it gradually increased to $160^{\circ} \mathrm{F}$ over several months and then remained essentially constant. Fluid data are as follows:

| Property | Hot fluid (tubes) | Cold fluid (shell) |
| :--- | :--- | :--- |
| $\dot{m}(\mathrm{lbm} / \mathrm{h})$ | 130,000 | 190,000 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.55 | 0.66 |
| Inlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 250 | 100 |

(a) To the nearest square foot, how much heat-transfer surface does the heat exchanger contain?
(b) Use the initial operating data to calculate the clean overall heat-transfer coefficient, $U_{C}$.
(c) Use the final operating data to calculate the fouled overall heat-transfer coefficient, $U_{D}$.
(d) Use the results of parts (b) and (c) to determine the experimental value of the total fouling factor, $R_{D} \equiv R_{D i}\left(D_{o} / D_{i}\right)+R_{D o}$.

Ans. (a) $1,278 \mathrm{ft}^{2}$. (b) $153 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (c) $66 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (d) $0.0086 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$.
(3.10) A hydrocarbon stream is to be cooled from $200^{\circ} \mathrm{F}$ to $130^{\circ} \mathrm{F}$ using $10,800 \mathrm{lb} / \mathrm{h}$ of water with a range of $75-125^{\circ} \mathrm{F}$. A double-pipe heat exchanger comprised of 25 ft long carbon steel hairpins will be used. The inner and outer pipes are $1.5-$ and $3.5-\mathrm{in}$. schedule 40 , respectively. The hydrocarbon will flow through the inner pipe and the heat-transfer coefficient for this stream has been determined: $h_{i}=200 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Fouling factors of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ for water and $0.002 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ for the hydrocarbon are specified. How many hairpins will be required?
(3.11) An oil stream is to be cooled from $200^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$ by heating a kerosene stream from $80^{\circ} \mathrm{F}$ to $160^{\circ} \mathrm{F}$. A fouling factor of $0.002 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for each stream, and fluid properties may be assumed constant at the values given below. Ten carbon steel hairpins are available on the company's used equipment lot. Each hairpin is 20 ft long with inner and outer pipes being $\frac{3}{4}$ - and $1.5-\mathrm{in}$. schedule 40 , respectively. Will these hairpins be adequate for this service?

| Property | Oil | Kerosene |
| :--- | :--- | :--- |
| $\dot{m}(\mathrm{lb} / \mathrm{h})$ | 10,000 | 12,500 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.6 | 0.6 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.08 | 0.077 |
| $\mu(\mathrm{cp})$ | 3.2 | 0.45 |
| $\operatorname{Pr}$ | 58.1 | 8.49 |

(3.12) For the double-pipe heat exchanger of Problem 3.10, calculate the outlet temperatures of the two streams when the unit is first placed in service.
(3.13) Available on the used equipment lot at a petrochemical complex is a shell-and-tube heat exchanger configured for one shell pass and one tube pass, and containing $1500 \mathrm{ft}^{2}$ of heattransfer surface. Suppose this unit is used for the trichloroethylene/kerosene service of Problem 3.7, and that an overall heat-transfer coefficient of $100 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ is attained in the exchanger. Compute the outlet temperatures of the two streams if they flow:
(a) Counter-currently.
(b) Co-currently.

Ans. (a) $165^{\circ} \mathrm{F}$ (trichloroethylene), $98^{\circ} \mathrm{F}$ (kerosene).
(3.14) An organic liquid at $185^{\circ} \mathrm{F}$ is to be cooled with water that is available at $80^{\circ} \mathrm{F}$. A double-pipe heat exchanger consisting of six hairpins connected in series will be used. Each hairpin is 20 ft long and is made with 2 - and $1-\mathrm{in}$. stainless steel ( $k=9.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) pipes. Flow rates and fluid properties, which may be assumed constant, are given below. The organic liquid will flow through the inner pipe, and its heat-transfer coefficient has been determined: $h_{i}=250 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. The streams will flow counter-currently through the exchanger.

| Property | Organic liquid | Water |
| :--- | :--- | :--- |
| $\dot{m}(\mathrm{lb} / \mathrm{h})$ | 11,765 | 7000 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.51 | 1.0 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | - | 0.38 |
| $\mu(\mathrm{cp})$ | - | 0.65 |
| $\operatorname{Pr}$ | - | 4.14 |

(a) Calculate the heat-transfer coefficient, $h_{o}$, for the water.
(b) Calculate the clean overall heat-transfer coefficient.
(c) Determine the outlet temperatures of the two streams that will be achieved when the heat exchanger is first placed in service.
(d) Calculate the average wall temperature of the inner pipe when the heat exchanger is clean.

Ans. (a) $727 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (b) $130 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}{ }^{2} \cdot{ }^{\circ} \mathrm{F}$. (c) $105^{\circ} \mathrm{F}$ (organic), $149^{\circ} \mathrm{F}$ (water). (d) $121^{\circ} \mathrm{F}$.
(3.15) A shell-and-tube heat exchanger consists of an E-shell that contains 554 tubes. The tubes are $1-\mathrm{in}$. OD, 16 BWG with a length of 20 ft , and the tube bundle is arranged for two passes. Suppose that this heat exchanger is used for the gasoline/water service of Problem 3.6, and that an overall heat-transfer coefficient of $100 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ is realized in the exchanger. Calculate the outlet temperatures of the two streams and the exchanger duty under these conditions.

Ans. $87.5^{\circ} \mathrm{F}$ (gasoline), $96^{\circ} \mathrm{F}$ (water), $q=7.738 \times 10^{6} \mathrm{Btu} / \mathrm{h}$.
(3.16) For the gasoline/water service of Problem 3.6, it is proposed to use a heat exchanger consisting of two E-shells connected in series. Each shell contains 302 tubes arranged for two passes. The tubes are $1-\mathrm{in}$. OD, 16 BWG with a length of 20 ft . Assuming that an overall heat-transfer coefficient of $100 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ is realized in the exchanger, what outlet temperature and exchanger duty will be attained with this unit?

Ans. $79^{\circ} \mathrm{F}$ (gasoline), $101^{\circ} \mathrm{F}$ (water), $q=8.803 \times 10^{6} \mathrm{Btu} / \mathrm{h}$.
(3.17) $18,000 \mathrm{lb} / \mathrm{h}$ of a petroleum fraction are to be cooled from $250^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ using cooling water with a range of $85-120^{\circ} \mathrm{F}$. Properties of the petroleum fraction may be assumed constant at the following values:

| Property | Value |
| :--- | :---: |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.52 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.074 |
| $\mu(\mathrm{cp})$ | 2.75 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 51.2 |

A shell-and-tube heat exchanger with the following configuration is available:

Type: AES
Shell ID: 15.25 in.
Baffle type: segmental
Baffle cut: 20\%
Number of baffles: 50
Shell material: carbon steel

Tubes: $3 / 4 \mathrm{in}$. OD, $16 \mathrm{BWG}, 20 \mathrm{ft}$ long
Number of tubes: 128
Number of tube passes: 4
Tube pitch: 1.0 in. (square)
Sealing strips: 1 pair
Tube material: Admirality brass ( $k=64 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ )

Fouling factors of 0.001 and $0.002 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ are required for the cooling water and petroleum fraction, respectively. Is the heat exchanger thermally suitable for this service?
(3.18) For the heat exchanger of Problem 3.17, calculate the outlet temperatures of the two streams that will be attained when the exchanger is clean.
(3.19) $72,500 \mathrm{lb} / \mathrm{h}$ of crude oil are to be heated from $250^{\circ} \mathrm{F}$ to $320^{\circ} \mathrm{F}$ by cooling a lube oil from $450^{\circ} \mathrm{F}$ to $340^{\circ} \mathrm{F}$. Physical properties of the two streams may be assumed constant at the following values:

| Property | Crude oil | Lube oil |
| :--- | :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.59 | 0.62 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.073 | 0.067 |
| $\mu(\mathrm{cp})$ | 0.83 | 1.5 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 47.4 | 48.7 |

It is proposed to use a carbon steel heat exchanger having the following configuration:
Type: AES Tubes: 1.0 in . OD, $14 \mathrm{BWG}, 24 \mathrm{ft}$ long
Shell ID: 29 in. Number of tubes: 314
Baffle type: segmental Number of tube passes: 6
Baffle cut: 20\% Tube pitch: 1.25 in. (square)
Number of baffles: 30 Sealing strips: one pair per 10 tube rows
The crude oil will flow in the tubes, and published fouling factors for oil refinery streams should be used. Is the proposed unit thermally suitable for this service?
(3.20) For the heat exchanger of Problem 3.19, calculate the outlet temperatures of the two streams that will be attained when the exchanger is clean.
(3.21) Repeat Example 3.3 with the fluids switched, i.e., with aniline in the inner pipe and benzene in the annulus.

This page intentionally left blank

## DESIGN OF DOUBLE-PIPE HEAT EXCHANGERS

## Contents

4.1 Introduction 128
4.2 Heat-Transfer Coefficients for Exchangers without Fins 128
4.3 Hydraulic Calculations for Exchangers without Fins 128
4.4 Series/Parallel Configurations of Hairpins 131
4.5 Multi-tube Exchangers 132
4.6 Over-Surface and Over-Design 133
4.7 Finned-Pipe Exchangers 141
4.8 Heat-Transfer Coefficients and Friction Factors for Finned Annuli 143
4.9 Wall Temperature for Finned Pipes 145
4.10 Computer Software 152

### 4.1 Introduction

The basic calculations involved in the thermal analysis of double-pipe heat exchangers were presented in the previous chapter. In the present chapter we consider the design of double-pipe units in more detail. In particular, the hydraulic analysis alluded to in Chapter 3 is presented, and procedures for handling finned-tube and multi-tube exchangers are given. Series-parallel configurations of hairpins are also considered.

Design of heat-transfer equipment involves a trade-off between the two conflicting goals of low capital cost (high overall heat-transfer coefficient, small heat-transfer area) and low operating cost (small stream pressure drops). Optimal design thus involves capital and energy costs, which are constantly changing. A simpler, albeit sub-optimal, procedure is to specify a reasonable pressuredrop allowance for each stream and design the exchanger within these constraints. The pressuredrop allowances determine (approximately) the trade-off between capital and operating costs. For low-viscosity liquids such as water, organic solvents, light hydrocarbons, etc., an allowance in the range of $7-20 \mathrm{psi}$ is commonly used. For gases, a value in the range of $1-5 \mathrm{psi}$ is often specified.

### 4.2 Heat-Transfer Coefficients for Exchangers without Fins

Heat-transfer correlations for pipes and annuli were presented in Section 2.4 and their application to the analysis of double-pipe exchangers was illustrated in Section 3.6. The correlations that are used in this chapter are repeated here for convenience.

For turbulent flow $\left(R e \geq 10^{4}\right)$, the Seider-Tate equation is used in the form:

$$
\begin{equation*}
N u=0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \tag{4.1}
\end{equation*}
$$

This is the same as Equation (2.33) except that a coefficient of 0.023 is used here rather than 0.027 . As noted in Chapter 2, a coefficient of 0.023 is often preferred for design work.

For the transition region $\left(2100<R e<10^{4}\right)$, the Hausen equation is used:

$$
\begin{equation*}
N u=0.116\left[\operatorname{Re}^{2 / 3}-125\right] \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14}\left[1+\left(D_{i} / L\right)^{2 / 3}\right] \tag{2.37}
\end{equation*}
$$

Equations (4.1) and (2.37) are used for both pipes and annuli, with the equivalent diameter replacing $D_{i}$, the pipe ID, in the case of an annulus.

For laminar flow ( $R e \leq 2100$ ) in pipes, the Seider-Tate equation is used:

$$
\begin{equation*}
N u=1.86\left[\operatorname{Re} \operatorname{Pr} D_{i} / L\right]^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \tag{2.36}
\end{equation*}
$$

For laminar flow in annuli, Equation (2.41) should be used. Also, Equation (2.38) may be used for the turbulent and transition regions in place of the Seider-Tate and Hausen correlations. However, these equations are not used in this chapter.

### 4.3 Hydraulic Calculations for Exchangers without Fins

The main contribution to pressure drop in double-pipe exchangers is from fluid friction in the straight sections of pipe. For isothermal flow, this pressure drop can be expressed in terms of the Darcy friction factor, $f$, as:

$$
\begin{equation*}
\Delta P_{f}=\frac{f L \rho V^{2}}{2 g_{c} D_{i}} \tag{4.2}
\end{equation*}
$$

where
$L=$ pipe length
$D_{i}=$ pipe I D
$\rho=$ fluid density
$V=$ average fluid velocity

This equation can be written in terms of the mass flux, $G$, and the specific gravity, $s$, of the fluid by making the substitutions $V=G / \rho$ and $\rho=s \rho_{\text {water }}$ to give:

$$
\begin{equation*}
\Delta P_{f}=\frac{f L G^{2}}{2 g_{c} \rho_{\text {water }} D_{i} s} \tag{4.3}
\end{equation*}
$$

The specific gravity of liquids is usually referenced to water at $4^{\circ} \mathrm{C}$, which has a density of $62.43 \mathrm{lbm} / \mathrm{ft}^{3}$. (The petroleum industry uses a reference temperature of $60^{\circ} \mathrm{F}$, at which $\rho_{\text {water }}=62.37 \mathrm{lbm} / \mathrm{ft}^{3}$; the difference in reference densities is insignificant in the present context.) Also, in English units,

$$
g_{c}=32.174 \frac{\mathrm{lbm} \cdot \mathrm{ft} / \mathrm{s}^{2}}{\mathrm{lbf}}=4.16975 \times 10^{8} \frac{\mathrm{lbm} \cdot \mathrm{ft} / \mathrm{h}^{2}}{\mathrm{lbf}}
$$

With these numerical values, Equation (4.3) becomes:

$$
\begin{equation*}
\Delta P_{f}=\frac{f L G^{2}}{5.206 \times 10^{10} D_{i} s} \tag{4.4}
\end{equation*}
$$

When $L$ and $D_{i}$ are expressed in ft and $G$ in $\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$, the units of $\Delta P_{f}$ are $\mathrm{lbf} / \mathrm{ft}^{2}$.
A minor modification is made to this basic hydraulic equation by dividing the right side by $144 \phi$, where

$$
\begin{array}{ll}
\phi=\left(\mu / \mu_{w}\right)^{0.14} & \text { for turbulent flow } \\
\phi=\left(\mu / \mu_{w}\right)^{0.25} & \text { for laminar flow }
\end{array}
$$

The viscosity correction factor accounts for the effect of variable fluid properties on the friction factor in non-isothermal flow, while the factor of 144 converts the pressure drop from $\mathrm{lbf} / \mathrm{ft}^{2}$ to psi . With this modification, Equation (4.4) becomes:

$$
\begin{equation*}
\Delta P_{f}=\frac{f L G^{2}}{7.50 \times 10^{12} D_{i} s \phi} \tag{4.5}
\end{equation*}
$$

where
$\Delta P_{f} \propto \mathrm{psi}$
$L, D_{i} \propto \mathrm{ft}$
$G \propto \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$
$s, f, \phi$ are dimensionless
See Appendix 4.A for the corresponding equation in terms of SI units. Equation (4.5) is also applicable to flow in the annulus of a double-pipe exchanger if the pipe diameter, $D_{i}$, is replaced by the equivalent diameter, $D_{e}$.
The friction factor to be used with Equation (4.5) can be computed as follows. For laminar flow in the inner pipe,

$$
\begin{equation*}
f=64 / R e \tag{4.6}
\end{equation*}
$$

For laminar flow in the annulus,

$$
\begin{equation*}
f=\left(\frac{64}{R e}\right)\left[\frac{(1-\kappa)^{2}}{1+\kappa^{2}+\left(1-\kappa^{2}\right) / \ln \kappa}\right] \tag{4.7}
\end{equation*}
$$

where

$$
\begin{aligned}
\kappa & =D_{1} / D_{2} \\
D_{1} & =\text { OD of inner pipe } \\
D_{2} & =\text { ID of outer pipe }
\end{aligned}
$$

For practical configurations, the term in square brackets in Equation (4.7) is approximately 1.5.
For commercial pipe and turbulent flow with $R e \geq 3000$, the following equation can be used for both the pipe and the annulus:

$$
\begin{equation*}
f=0.3673 R e^{-0.2314} \tag{4.8}
\end{equation*}
$$

Minor pressure losses due to entrance and exit effects and return bends are usually expressed in terms of velocity heads. The grouping $\left(V^{2} / 2 g\right)$ has dimensions of length and is called a velocity head. The change in pressure equivalent to one velocity head is:

$$
\begin{equation*}
\Delta P=\rho\left(g / g_{c}\right)\left(V^{2} / 2 g\right)=\rho V^{2} / 2 g_{c} \tag{4.9}
\end{equation*}
$$

Expressing $\rho$ and $V$ in terms of s and $G$ as above and dividing by 144 to convert to psi gives:

$$
\begin{array}{r}
\Delta P=\left(\frac{1}{2 g_{c} \rho_{\text {water }} \times 144}\right)\left(\frac{G^{2}}{s}\right) \\
\Delta P=1.334 \times 10^{-13} G^{2} / \mathrm{s} \tag{4.11}
\end{array}
$$

where $\Delta P$ has units of psi and $G$ has units of $\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$. These units apply in the remainder of this section. See Appendix 4.A for the corresponding results in terms of SI units.

In the return bend of a hairpin, the fluid experiences a $180^{\circ}$ change of direction. The pressure loss for turbulent flow in a long-radius $180^{\circ}$ bend is given as 1.2 velocity heads in Ref. [1]. In laminar flow, the number of velocity heads depends on the Reynolds number [2], but for Re between 500 and 2100, a reasonable approximation is 1.5 velocity heads. Kern and Kraus [3] recommend an allowance of one velocity head per hairpin for the return-bend losses, which agrees fairly well with the above value for turbulent flow.

When hairpins are connected in series as shown in Figure 4.1, both fluids make an additional $180^{\circ}$ change of direction between the outlet of one hairpin and the inlet of the next. It follows that for $N_{H P}$ hairpins connected in series, the total number of direction changes experienced by each fluid is $\left(2 N_{H P}-1\right)$. The total pressure drop resulting from these direction changes is thus:

$$
\begin{array}{ll}
\Delta P_{r}=1.6 \times 10^{-13}\left(2 N_{H P}-1\right) G^{2} / s & \text { (turbulent flow) } \\
\Delta P_{r}=2.0 \times 10^{-13}\left(2 N_{H P}-1\right) G^{2} / s & \text { (laminar flow, } R e \geq 500) \tag{4.13}
\end{array}
$$

Entrance and exit losses for flow through the inner pipes of double-pipe exchangers are generally negligible because connections to process piping are inline and losses are mainly due to size mismatches, which are usually minor, between process and heat-exchanger pipes. An exception occurs in multi-tube exchangers, where the fluid experiences a significant contraction as it enters the individual tubes and a corresponding expansion as it exits the tubes at the outlet tubesheet. In turbulent flow, the sum of these losses can be approximated by 1 tube velocity head per hairpin. In laminar flow, the number of velocity heads varies with the Reynolds number [4].

On the annulus side, the fluid enters and leaves through standard nozzles where it experiences a sudden expansion (entering) and contraction (leaving). These losses can be approximated using the standard formulas for a sudden expansion and sudden contraction [4]. However, for turbulent flow in the nozzles, the sum of the entrance and exit losses can be estimated as 1.5 nozzle velocity


Figure 4.1 Two hairpins connected in series (Source: Ref. [1]).
heads [4], apportioned roughly as one velocity head for the entrance nozzle and 0.5 velocity head for the exit nozzle. In laminar flow, the number of velocity heads depends on the Reynolds number, but for $R e \geq 100$, a reasonable approximation is 3 nozzle velocity heads for the sum of the entrance and exit losses. Thus, for exchangers with internal return bends, we have the following relations for nozzle losses:

$$
\begin{array}{ll}
\Delta P_{n}=2.0 \times 10^{-13} N_{H P} G_{n}^{2} / s & \text { (turbulent flow) } \\
\Delta P_{n}=4.0 \times 10^{-13} N_{H P} G_{n}^{2} / s & \text { (laminar flow, } \left.R e_{n} \geq 100\right) \tag{4.15}
\end{array}
$$

where $G_{n}$ and $R e_{n}$ are the mass flux and Reynolds number, respectively, for the nozzle, and $N_{H P}$ is the number of hairpins connected in series. For exchangers with external return bends, the fluid in the annulus experiences another sudden contraction and expansion at the return bends. Hence, in this case the above pressure drop should be doubled.

### 4.4 Series/Parallel Configurations of Hairpins

Double-pipe exchangers are extremely flexible with respect to configuration of hairpins, since both the inner pipes and annuli can be connected either in series or in parallel. In order to meet pressuredrop constraints, it is sometimes convenient to divide one stream into two or more parallel branches while leaving the other stream intact. Such a case is shown in Figure 4.2, where the inner pipes are connected in parallel, while the annuli are connected in series. Although the flow is countercurrent in each hairpin of Figure 4.2, the overall flow pattern is not true counterflow. This fact can be appreciated by comparing Figure 4.1 (true counterflow) and Figure 4.2. Note in particular that the temperature of the fluid entering the inner pipe of the top hairpin is different in the two cases.

To account for the departure from true counterflow in series-parallel configurations, the counterflow logarithmic mean temperature difference (LMTD) is multiplied by a correction factor, $F$, given by the following equations:

$$
\begin{equation*}
F=\left[\frac{(R-x)}{x(R-1)}\right] \frac{\ln [(1-P) /(1-P R)]}{\ln \left[\frac{(R-x)}{R(1-P R)^{1 / x}}+\frac{x}{R}\right]} \quad(R \neq 1) \tag{4.16}
\end{equation*}
$$



Figure 4.2 Hairpins with annuli connected in series and inner pipes connected in parallel (Source:
Ref. [1]).

$$
\begin{gather*}
F=\frac{P(1-x)}{x(1-P) \ln \left[\frac{(1-x)}{(1-P)^{1 / x}}+x\right]} \quad(R=1)  \tag{4.17}\\
P=\left(t_{b}-t_{a}\right) /\left(T_{a}-t_{a}\right)  \tag{4.18}\\
R=\left(T_{a}-T_{b}\right) /\left(t_{b}-t_{a}\right) \tag{4.19}
\end{gather*}
$$

where
$x=$ number of parallel branches
$T_{a}, T_{b}=$ inlet and outlet temperatures of series stream
$t_{a}, t_{b}=$ inlet and outlet temperatures of parallel stream

### 4.5 Multi-tube Exchangers

Un-finned multi-tube hairpin exchangers can be handled using the methods presented above with an appropriate value of the equivalent diameter. For an outer pipe with an ID of $D_{2}$ containing $n_{t}$ tubes, each with OD of $D_{1}$, the flow area and wetted perimeter are:

$$
\begin{equation*}
A_{f}=(\pi / 4)\left(D_{2}^{2}-n_{t} D_{1}^{2}\right) \tag{4.20}
\end{equation*}
$$

$$
\begin{equation*}
\text { Wetted perimeter }=\pi\left(D_{2}+n_{t} D_{1}\right) \tag{4.21}
\end{equation*}
$$

Therefore, the equivalent diameter is given by:

$$
\begin{align*}
& D_{e}=4 A_{f} / \text { wetted perimeter } \\
& D_{e}=\left(D_{2}^{2}-n_{t} D_{1}^{2}\right)\left(D_{2}+n_{t} D_{1}\right) \tag{4.22}
\end{align*}
$$

Note that for $n_{t}=1$, this reduces to $D_{e}=D_{2}-D_{1}$.

### 4.6 Over-Surface and Over-Design

Over-surface is a measure of the safety factor incorporated in the design of a heat exchanger through fouling factors and the use of standard equipment sizes. Since it deals directly with exchanger surface area, it is easier to visualize than fouling factors and calculated versus required heat-transfer coefficients. The percentage over-surface is defined as follows:

$$
\begin{equation*}
\% \text { over-surface }=\frac{A-A_{C}}{A_{C}} \times 100 \tag{4.23}
\end{equation*}
$$

where
$A=$ actual heat-transfer surface area in the exchanger
$A_{C}=$ calculated heat-transfer surface area based on $U_{C}$
Over-surface depends on the relative magnitudes of the total fouling allowance and the film and wall resistances. While values of $20-40 \%$ may be considered typical, higher values are not unusual. Equation (4.23) is often applied with the surface area calculated using the design coefficient, $U_{D}$, rather than the clean coefficient. In this case the computed quantity is referred to as the overdesign; it represents the extra surface area beyond that required to compensate for fouling. Some over-design (typically about $10 \%$ or less) is considered acceptable and (often) desirable, since it provides an additional safety margin in the final design.

The design procedure for an un-finned double-pipe exchanger is illustrated by reconsidering the benzene-aniline exchanger of Example 3.3. For completeness, the problem is restated here and worked in its entirety. However, the reader may wish to refer to Example 3.3 for additional details. (Note that a coefficient of 0.027 was used in the Seider-Tate equation in Example 3.3, whereas a value of 0.023 is used here.)

## Example 4.1

$10,000 \mathrm{lb} / \mathrm{h}$ of benzene will be heated from $60^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$ by heat exchange with an aniline stream that will be cooled from $150^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$. A number of $16-\mathrm{ft}$ hairpins consisting of $2-\mathrm{in}$. by $1.25-\mathrm{in}$. schedule 40 stainless steel pipe (type $316, k=9.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) are available and will be used for this service. A maximum pressure drop of 20 psi is specified for each stream. The specific gravity of benzene is 0.879 and that of aniline is 1.022 . Determine the number and configuration of hairpins that are required.

## Solution

We begin by assuming that the hairpins are connected in series on both sides, since this is the simplest configuration, and that the flow pattern is counter-current. We also place the benzene in the inner pipe for the sake of continuity with Example 3.3. As discussed at the end of that example, however, either fluid could be placed in the inner pipe.

## First trial

(a) Fluid properties at the average stream temperatures are obtained from Figures A. 1 and A.2, and Table A. 15.

| Fluid property | Benzene $\left(t_{\text {ave }}=90^{\circ} \mathrm{F}\right)$ | Aniline $\left(T_{\text {ave }}=125^{\circ} \mathrm{F}\right)$ |
| :--- | :--- | :--- |
| $\mu(\mathrm{cp})$ | 0.55 | 2.0 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.42 | 0.52 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.092 | 0.100 |

(b) Determine the heat load and aniline flow rate by energy balances on the two streams.

$$
\begin{aligned}
& q=\left(\dot{m} C_{P} \Delta T\right)_{B}=10,000 \times 0.42 \times 60=252,000 \mathrm{Btu} / \mathrm{h} \\
& 252,000=\left(\dot{m} C_{P} \Delta T\right)_{A}=\dot{m}_{A} \times 0.52 \times 50 \\
& \dot{m}_{A}=9692 \mathrm{lb} / \mathrm{h}
\end{aligned}
$$

(c) Calculate the LMTD.

$$
\Delta T_{\ln }=\frac{40-30}{\ln (40 / 30)}=34.76^{\circ} \mathrm{F}
$$

(d) Calculate $h_{i}$ assuming $\phi_{i}=1.0$.

$$
\begin{aligned}
D_{i} & =1.38 / 12=0.115 \mathrm{ft} \quad(\text { from Table B.2 }) \\
R e & =\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 10,000}{\pi \times 0.115 \times 0.55 \times 2.419}=83,217 \Rightarrow \text { turbulent flow } \\
h_{i} & =\frac{k}{D_{i}} \times 0.023 \operatorname{Re}^{0.8} \mathrm{Pr}^{1 / 3} \\
h_{i} & =\frac{0.092}{0.115} \times 0.023(83,217)^{0.8}\left(\frac{0.42 \times 0.55 \times 2.419}{0.092}\right)^{1 / 3} \\
h_{i} & =290 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(e) Calculate $h_{o}$ assuming $\phi_{o}=1.0$.

$$
\begin{aligned}
& \left.\begin{array}{l}
D_{2}=2.067 \mathrm{in} . \\
D_{1}=1.660 \mathrm{in.}
\end{array}\right\} \quad(\text { from Table B.2) } \\
& D_{e}=D_{2}-D_{1}=\frac{2.067-1.660}{12}=0.0339 \mathrm{ft} \\
& \text { flow area } \equiv A_{f}=\frac{\pi}{4}\left(D_{2}^{2}-D_{1}^{2}\right)=0.00827 \mathrm{ft}^{2} \\
& R e=\frac{D_{e}\left(\dot{m} / A_{f}\right)}{\mu}=\frac{0.0339 \times(9692 / 0.00827)}{2.0 \times 2.419}=8212 \Rightarrow \text { transition flow }
\end{aligned}
$$

Using the Hausen equation with $\left[1+\left(D_{e} / L\right)^{2 / 3}\right]=1.0$ gives:

$$
\begin{aligned}
h_{o} & =\frac{k}{D_{e}} \times 0.116\left[\mathrm{Re}^{2 / 3}-125\right] \mathrm{Pr}^{1 / 3} \\
& =\frac{0.1}{0.0339} \times 0.116 \times\left[(8212)^{2 / 3}-125\right]\left(\frac{0.52 \times 2.0 \times 2.419}{0.1}\right)^{1 / 3} \\
h_{o} & =283 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(f) Calculate the pipe wall temperature.

$$
\begin{aligned}
T_{w} & =\frac{h_{i} t_{\text {ave }}+h_{o}\left(D_{o} / D_{i}\right) T_{\text {ave }}}{h_{i}+h_{o}\left(D_{o} / D_{i}\right)} \\
T_{w} & =\frac{290 \times 90+283(1.66 / 1.38) \times 125}{290+283 \times(1.66 / 1.38)} \\
T_{w} & =108.9^{\circ} \mathrm{F}
\end{aligned}
$$

(g) Calculate $\phi_{i}$ and $\phi_{0}$, and corrected values of $h_{i}$ and $h_{0}$.

From Figure A.1, at $108.9^{\circ} \mathrm{F}, \mu_{B}=0.47 \mathrm{cp}$ and $\mu_{A}=2.4 \mathrm{cp}$. Therefore,

$$
\begin{aligned}
\phi_{i} & =(0.55 / 0.47)^{0.14}=1.0222 \\
\phi_{o} & =(20 / 2.4)^{0.14}=0.9748 \\
h_{i} & =290(1.0222)=296 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
h_{o} & =283(0.9748)=276 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(h) Obtain fouling factors. For liquid organic process chemicals such as benzene and aniline, a value of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} / \mathrm{B}$ tu is appropriate.
(i) Compute the overall heat-transfer coefficient.

$$
\begin{aligned}
& U_{D}=\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}+\frac{R_{D i} D_{o}}{D_{i}}+R_{D o}\right]^{-1} \\
& U_{D}=\left[\frac{1.66}{296 \times 1.38}+\frac{(1.66 / 12) \ln (1.66 / 1.38)}{2 \times 9.4}+\frac{1}{276}+\frac{0.001 \times 1.66}{1.38}+0.001\right]^{-1} \\
& U_{D}=89 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(j) Calculate the required surface area and number of hairpins.

$$
\begin{aligned}
q & =U_{D} A \Delta T_{\mathrm{ln}} \\
A & =\frac{q}{U_{D} \Delta T_{\mathrm{ln}}} \\
A & =\frac{252,000}{89 \times 34.76}=81.5 \mathrm{ft}^{2}
\end{aligned}
$$

From Table B.2, the external surface area per foot of $1.25-\mathrm{in}$. schedule 40 pipe is $0.435 \mathrm{ft}^{2}$. Therefore,

$$
L=\frac{81.5}{0.435}=187.4 \mathrm{ft}
$$

Since each 16 - ft hairpin contains 32 ft of pipe,

$$
\text { Number of hairpins }=\frac{187.4}{32}=5.9 \Rightarrow 6
$$

Thus, six hairpins are required.
(k) Calculate the pressure drop for the benzene stream (inner pipe).

The friction factor is calculated from Equation (4.8):

$$
\begin{aligned}
f & =0.3673 \mathrm{Re}^{-0.2314}=0.3673(83,217)^{-0.2314} \\
f & =0.0267 \\
A_{f} & =0.0104 \mathrm{ft}^{2} \quad(\text { Table B.2) } \\
G & =\dot{m} / A_{f}=10,000 / 0.0104=961,538 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The pressure drop in the straight sections of pipe is calculated using Equation (4.5):

$$
\begin{aligned}
\Delta P_{f} & =\frac{f L G^{2}}{7.50 \times 10^{12} D_{i} s \phi} \\
& =\frac{0.0267(6 \times 32)(961,538)^{2}}{7.50 \times 10^{12}(1.38 / 12) \times 0.879 \times 1.022} \\
\Delta P_{f} & =6.1 \mathrm{psi}
\end{aligned}
$$

The pressure drop in the return bends is obtained from Equation (4.12):

$$
\begin{aligned}
\Delta P_{r} & =1.6 \times 10^{-13}\left(2 N_{H P}-1\right) G^{2} / s \\
& =1.6 \times 10^{-13}(2 \times 6-1)(961,538)^{2} / 0.879 \\
\Delta P_{r} & =1.85 \mathrm{psi}
\end{aligned}
$$

Since the nozzle losses associated with the inner pipes are negligible, the total pressure drop, $\Delta P_{i}$, is:

$$
\Delta P_{i}=\Delta P_{f}+\Delta P_{r}=6.1+1.85=7.95 \cong 8.0 \mathrm{psi}
$$

(l) Calculate the pressure drop for the aniline stream (annulus).

The friction factor is calculated from Equation (4.8):

$$
\begin{aligned}
& f=0.3673 R e^{-0.2314}=0.3673(8212)^{-0.2314} \\
& f=0.0456 \\
& G=\dot{m} / A_{f}=9692 / 0.00827=1,171,947 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The pressure drop in the straight sections of pipe is again calculated using Equation (4.5) with the pipe diameter replaced by the equivalent diameter:

$$
\begin{aligned}
\Delta P_{f} & =\frac{f L G^{2}}{7.50 \times 10^{12} D_{e} s \phi} \\
& =\frac{0.0456(6 \times 32)(1,171,947)^{2}}{7.50 \times 10^{12} \times 0.0339 \times 1.022 \times 0.9748} \\
\Delta P_{f} & =47.5 \mathrm{psi}
\end{aligned}
$$

Since this value greatly exceeds the allowed pressure drop, the minor losses will not be calculated. This completes the first trial.

In summary, there are two problems with the initial configuration of the heat exchanger:
(1) The pressure drop on the annulus side is too large.
(2) The Reynolds number in the annulus is less than 10,000 .

Since the dimensions of the hairpins are fixed in this problem, there are relatively few options for modifying the design. Two possibilities are:
(1) Switch the fluids, i.e., put the aniline in the inner pipe and the benzene in the annulus.
(2) Connect the annuli in parallel.

The effects of these changes on the Reynolds numbers and pressure drops can be estimated as follows:
(1) Switch the fluids. Since the flow rates of the two streams are approximately the same, the Reynolds numbers are essentially inversely proportional to the viscosity. Thus,

$$
\begin{aligned}
& R e_{i} \rightarrow 83,217(0.55 / 2.0) \cong 23,000 \\
& R e_{o} \rightarrow 8212(2.0 / 0.55) \cong 30,000
\end{aligned}
$$

Hence, switching the fluids will result in fully turbulent flow on both sides of the exchanger.
To estimate the effect on pressure drops, assume that the number of hairpins does not change. Then the main factors affecting $\Delta P$ are $f$ and $s$. Hence,

$$
\begin{aligned}
& \Delta P \sim f / s \sim R e^{-0.2314} s^{-1} \\
& \Delta P_{f, i} \rightarrow 6.1(23,000 / 83,000)^{-0.2314}(1.022 / 0.879)^{-1} \cong 7 \mathrm{psi} \\
& \Delta P_{f, o} \rightarrow 47.5(30,000 / 8200)^{-0.2314}(0.879 / 1.022)^{-1} \cong 41 \mathrm{psi}
\end{aligned}
$$

Clearly, switching the fluids does not reduce the annulus-side pressure drop nearly enough to meet the design specification (unless the number of hairpins is reduced by a factor of at least two, which is very unlikely).
(2) Connect the annuli in two parallel banks. This change will have no effect on the fluid flowing in the inner pipe. For the fluid in the annulus, however, both the flow rate and the length of the flow path will be halved. Therefore,

$$
R e_{o} \rightarrow 8212 \times 1 / 2 \cong 4100
$$

Assuming that the number of hairpins does not change,

$$
\begin{aligned}
& \Delta P_{f, o} \sim f G^{2} L \\
& \Delta P_{f, o} \rightarrow 47.5(4100 / 8200)^{-0.2314}(1 / 2)^{2}(1 / 2) \cong 7 \mathrm{psi}
\end{aligned}
$$

Apparently this modification will take care of the pressure-drop problem, but will push the Reynolds number further into the transition region.

Although neither modification by itself will correct the problems with the initial design, in combination they might. Hence, we consider a third alternative.
(3) Switch the fluids and connect the annuli in two parallel banks. The Reynolds numbers will become:

$$
\begin{aligned}
& R e_{i} \cong 23,000 \\
& R e_{o} \cong 15,000
\end{aligned}
$$

The pressure drops will become (assuming no change in the number of hairpins):

$$
\begin{aligned}
& \Delta P_{f, i} \cong 7 \mathrm{psi} \\
& \Delta P_{f, o} \rightarrow 47.5(15,000 / 8200)^{-0.2314}(1 / 2)^{2}(1 / 2)(0.879 / 1.022) \cong 6 \mathrm{psi}
\end{aligned}
$$

It appears that this alternative will meet all design requirements. However, it is necessary to perform the detailed calculations because $h_{i}, h_{o}$ and the mean temperature difference will all change, and hence the number of hairpins can be expected to change as well.

## Second trial

(a) Calculate the LMTD correction factor for the series/parallel configuration. Aniline in the inner pipe is the series stream and benzene in the annulus is the parallel stream. Therefore,

$$
\begin{aligned}
T_{a} & =150^{\circ} \mathrm{F} \quad t_{a}=60^{\circ} \mathrm{F} \\
T_{b} & =100^{\circ} \mathrm{F} \quad t_{b}=120^{\circ} \mathrm{F} \\
P & =\left(t_{b}-t_{a}\right) /\left(T_{a}-t_{a}\right)=(120-60) /(150-60)=0.6667 \\
R & =\left(T_{a}-T_{b}\right) /\left(t_{b}-t_{a}\right)=(150-100) /(120-60)=0.8333 \\
x & =2 \text { (number of parallel branches) }
\end{aligned}
$$

Substituting into Equation (4.16) gives:

$$
\begin{aligned}
F & =\left[\frac{(0.8333-2)}{2(0.8333-1)}\right] \frac{\ln [(1-0.6667) /(1-0.6667 \times 0.8333)]}{\ln \left[\frac{(0.8333-2)}{0.8333(1-0.6667 \times 0.8333)^{1 / 2}}+\left(\frac{2}{0.8333}\right)\right]} \\
F & =0.836
\end{aligned}
$$

(b) Calculate $h_{i}$ assuming $\phi_{i}=1.0$.

$$
\begin{aligned}
R e & =\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 9692}{\pi \times 0.115 \times 2.0 \times 2.419}=22,180 \Rightarrow \text { turbulent flow } \\
h_{i} & =\frac{k}{D_{i}} \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3} \\
& =\frac{0.1}{0.115} \times 0.023(22,180)^{0.8}(25.158)^{1 / 3} \\
h_{i} & =176 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(c) Calculate $h_{o}$ assuming $\phi_{o}=1.0$.

$$
\begin{aligned}
R e & =\frac{D_{e}\left(\dot{m} / A_{f}\right)}{\mu}=\frac{0.0339(5000 / 0.00827)}{0.55 \times 2.419}=15,405 \Rightarrow \text { turbulent flow } \\
h_{o} & =\frac{k}{D_{e}} \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3} \\
& =\frac{0.092}{0.0339} \times 0.023(15,405)^{0.8}(6.0764)^{1 / 3} \\
h_{o} & =255 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(d) Calculate the pipe wall temperature.

$$
T_{w}=\frac{176 \times 125+255(1.66 / 1.38) \times 90}{176+255(1.66 / 1.38)} \cong 103^{\circ} \mathrm{F}
$$

(e) Calculate $\phi_{i}$ and $\phi_{0}$, and corrected values of $h_{i}$ and $h_{o}$.

$$
\begin{aligned}
& \text { At } 103^{\circ} \mathrm{F}, \mu_{A}=2.6 \mathrm{cp} \text { and } \mu_{B}=0.5 \mathrm{cp} \quad \text { (Figure A.1) } \\
& \qquad \begin{aligned}
\phi_{i} & =(2.0 / 2.6)^{0.14}=0.9639 \\
\phi_{o} & =(0.55 / 0.5)^{0.14}=1.0134 \\
h_{i} & =176 \times 0.9639=170 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
h_{o} & =255 \times 1.0134=258 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
\end{aligned}
$$

(f) Calculate $U_{D}$.

$$
\begin{aligned}
U_{D} & =\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k}+\frac{1}{h_{o}}+\frac{R_{D i} D_{o}}{D_{i}}+R_{D_{o}}\right]^{-1} \\
& =\left[\frac{1.66}{170 \times 1.38}+\frac{(1.66 / 12) \ln (1.66 / 1.38)}{2 \times 9.4}+\frac{1}{258}+\frac{0.001 \times 1.66}{1.38}+0.001\right]^{-1} \\
U_{D} & =69 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(g) Calculate the required surface area and number of hairpins.

$$
\begin{aligned}
q & =U_{D} A F \Delta T_{\mathrm{ln}} \\
A & =\frac{q}{U_{D} F \Delta T_{\mathrm{ln}}}=\frac{252,000}{69 \times 0.836 \times 34.76}=125.7 \mathrm{ft}^{2} \\
L & =\frac{125.7}{0.435}=289 \mathrm{ft} \\
\text { Number of hairpins } & =\frac{289}{32}=9.0 \Rightarrow 9
\end{aligned}
$$

Thus, nine hairpins are required. However, the equation for the LMTD correction factor is based on the assumption that both parallel branches are identical. Therefore, use two banks of five hairpins, for a total of ten hairpins.
(h) Calculate the pressure drop for the aniline stream (inner pipe).

$$
\begin{aligned}
f & =0.3673 R e^{-0.2314}=0.3673(22,180)^{-0.2314}=0.03625 \\
G & =\dot{m} / A_{f}=9692 / 0.0104=931,923 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{0.03625(10 \times 32)(931,923)^{2}}{7.50 \times 10^{12}(1.38 / 12) \times 1.022 \times 0.9639}=11.9 \mathrm{psi} \\
\Delta P_{r} & =1.6 \times 10^{-13}\left(2 N_{H P}-1\right) G^{2} / \mathrm{s} \\
& =1.6 \times 10^{-13}(2 \times 10-1)(931,923)^{2} / 1.022
\end{aligned}
$$

$$
\begin{aligned}
& \Delta P_{r}=2.6 \mathrm{psi} \\
& \Delta P_{i}=\Delta P_{f}+\Delta P_{r}=11.9+2.6=14.5 \mathrm{psi}
\end{aligned}
$$

(i) Calculate the pressure drop for the benzene stream (annulus).

$$
\begin{aligned}
f & =0.3673 R e^{-0.2314}=0.3673(15,405)^{-0.2314}=0.03945 \\
G & =\dot{m} / A_{f}=5000 / 0.00827=604,595 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{f L G^{2}}{7.50 \times 10^{12} D_{e} s \phi} \\
& =\frac{0.03945(5 \times 32)(604,595)^{2}}{7.50 \times 10^{12} \times 0.0339 \times 0.879 \times 1.0134} \\
\Delta P_{f} & =10.2 \mathrm{psi} \\
\Delta P_{r} & =1.6 \times 10^{-13}\left(2 N_{H P}-1\right) G^{2} / \mathrm{s} \\
& =1.6 \times 10^{-13}(2 \times 5-1)(604,595)^{2} / 0.879 \\
\Delta P_{r} & =0.6 \mathrm{psi}
\end{aligned}
$$

Assume the nozzles are made from 1-in. schedule 40 pipe having a flow area of $0.006 \mathrm{ft}^{2}$ (Table B.2). Then,

$$
G_{n}=\dot{m} / A_{f}=5000 / 0.006=833,333 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

Assuming internal return bends, Equation (4.14) gives:

$$
\begin{aligned}
& \Delta P_{n}=2.0 \times 10^{-13} N_{H P} G_{n}^{2} / s=2.0 \times 10^{-13} \times 5(833,333)^{2} / 0.879 \\
& \Delta P_{n}=0.79 \mathrm{psi}
\end{aligned}
$$

The total pressure drop for the benzene is:

$$
\begin{aligned}
\Delta P_{o} & =\Delta P_{f}+\Delta P_{r}+\Delta P_{n} \\
& =10.2+0.6+0.79 \\
\Delta P_{o} & \cong 11.6 \mathrm{psi}
\end{aligned}
$$

(j) Calculate the over-surface and over-design.

$$
\begin{aligned}
U_{C} & =\left[\frac{1}{U_{D}}-R_{D, t o t}\right]^{-1}=\left[\frac{1}{69}-0.001(1+1.66 / 1.38)\right]^{-1}=81.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
A_{C} & =\frac{q}{U_{C} F \Delta T_{\mathrm{ln}}}=\frac{252,000}{81.4 \times 0.836 \times 34.76} \cong 107 \mathrm{ft}^{2} \\
A & =\pi D_{o} L=0.435 \times(10 \times 32)=139 \mathrm{ft}^{2} \\
\text { over-surface } & =\left(A-A_{C}\right) / A_{C}=(139-107) / 107 \cong 30 \%
\end{aligned}
$$

The required surface area is $125.7 \mathrm{ft}^{2}$ from Step (g). Therefore, the over-design is:

$$
\text { over-design }=(139-125.7) / 125.7=10.6 \%
$$



Figure 4.3 (a) Rectangular fins on heat-exchanger pipes. (b) Cross-section of a finned-pipe exchanger (Source: (a) Koch Heat Transfer Company, LP and (b) Ref. [5]).

All design criteria are satisfied and the over-surface and over-design are reasonable; therefore, the exchanger is acceptable. The final design consists of ten hairpins with inner pipes connected in series and annuli connected in two parallel banks of five hairpins each. Aniline flows in the inner pipe and benzene flows in the annulus.

### 4.7 Finned-Pipe Exchangers

### 4.7.1 Finned-pipe characteristics

The inner pipe of a double-pipe exchanger can be equipped with rectangular fins as shown in Figure 4.3. Although fins can be attached to both the internal and external pipe surfaces, external fins are most frequently used. Pairs of fins are formed from U-shaped channels that are welded or soldered onto the pipe, depending on the materials involved. An alternative method of attaching the fins consists of cutting grooves in the pipe surface, inserting the fin material, and then peening the pipe metal back to secure the fins. The fin material need not be the same as the pipe material; for example, carbon steel fins can be attached to stainless steel pipes. Combinations of this type are used when a corrosion resistant alloy is needed for the inner fluid but not for the fluid in the annulus.

Dimensions of standard finned exchangers are given in Tables 4.1 and 4.2. The data are for units employing schedule 40 pipe. Data for exchangers intended for high-pressure service and employing schedule 80 pipe can be found in Ref. [6]. For units with a single inner pipe, the number of fins varies from 20 to 48, with fin heights, which are dictated by the clearance between the inner and outer pipes, from 0.375 to 1.0 in . The fin thickness is $0.035 \mathrm{in} .(0.889 \mathrm{~mm})$ for weldable metals. For soldered fins, the thickness is 0.0197 in . $(0.5 \mathrm{~mm})$ for heights of 0.5 in . or less, and $0.0315 \mathrm{in} .(0.8 \mathrm{~mm})$ for heights greater than $0.5 \mathrm{in} .(7 \mathrm{~mm})$. For multi-tube units, the number of fins per tube is either 16 or 20 , and the fin height is generally less than in units with a single inner pipe. The fin thickness is the same in both single and multi-tube units.

### 4.7.2 Fin Efficiency

Heat-transfer fins were discussed in Chapter 2, where the fin height was referred to as the fin length, denoted by the symbol, $L$. Since $L$ is used in the present chapter to denote pipe length, the symbol, $b$, will be used for fin height. Equation (2.23) for the efficiency of a rectangular fin becomes:

$$
\begin{equation*}
\eta_{f}=\frac{\tanh \left(m b_{c}\right)}{m b_{c}} \tag{4.24}
\end{equation*}
$$

Table 4.1 Standard Configurations for Exchangers with a Single Finned Inner Pipe; Standard Pressure (Schedule 40) Units

| Nominal <br> diameter <br> (in.) | Outer pipe <br> thickness <br> $(\mathrm{mm})$ | Outer <br> pipe OD <br> $(\mathrm{mm})$ | Maximum <br> number of <br> fins | Inner <br> pipe <br> OD $(\mathrm{mm})$ | Inner pipe <br> thickness <br> $(\mathrm{mm})$ | Fin <br> height <br> $(\mathrm{mm})$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 3.91 | 60.3 | 20 | 25.4 | 2.77 | 11.1 |
| 3 | 5.49 | 88.9 | 20 | 25.4 | 2.77 | 23.8 |
| 3 | 5.49 | 88.9 | 36 | 48.3 | 3.68 | 12.7 |
| $31 / 2$ | 5.74 | 101.6 | 36 | 48.3 | 3.68 | 19.05 |
| $3^{1 / 2}$ | 5.74 | 101.6 | 40 | 60.3 | 3.91 | 12.7 |
| 4 | 6.02 | 114.3 | 36 | 48.3 | 3.68 | 25.4 |
| 4 | 6.02 | 114.3 | 40 | 60.3 | 3.91 | 19.05 |
| 4 | 6.02 | 114.3 | 48 | 73.0 | 5.16 | 12.7 |

Source: Ref. [7].

Table 4.2 Standard Configurations for Multi-tube Exchangers; Standard Pressure (Schedule 40) Units

| Nominal <br> diameter <br> (in.) | Pipe <br> thickness <br> $(\mathrm{mm})$ | Pipe <br> OD <br> $(\mathrm{mm})$ | Number <br> of tubes | Number <br> of fins | Tube <br> OD <br> $(\mathrm{mm})$ | Tube <br> thickness <br> $(\mathrm{mm})$ | Fin <br> height <br> $(\mathrm{mm})$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| 4 | 6.02 | 114.3 | 7 | 16 | 19.02 | 2.11 | 5.33 |
| 4 | 6.02 | 114.3 | 7 | 20 | 22.2 | 2.11 | 5.33 |
| 6 | 7.11 | 168.3 | 19 | 16 | 19.02 | 2.11 | 5.33 |
| 6 | 7.11 | 168.3 | 14 | 16 | 19.02 | 2.11 | 5.33 |
| 6 | 7.11 | 168.3 | 7 | 20 | 20.04 | 2.77 | 12.7 |
| 8 | 8.18 | 219.1 | 19 | 16 | 19.02 | 2.11 | 8.64 |
| 8 | 8.18 | 219.1 | 19 | 20 | 22.2 | 2.11 | 7.11 |
| 8 | 8.18 | 219.1 | 19 | 20 | 25.4 | 2.77 | 5.33 |
| 8 | 8.18 | 219.1 | 19 | 16 | 19.02 | 2.11 | 7.11 |
| 8 | 8.18 | 219.1 | 19 | 20 | 22.2 | 2.11 | 5.33 |

Source: Ref. [7].
where
$b_{c}=b+\tau / 2=$ corrected fin height
$m=\left(2 h_{o} / k \tau\right)^{1 / 2}$
$\tau=$ fin thickness
$k=$ fin thermal conductivity
$h_{o}=$ heat-transfer coefficient in annulus
The weighted efficiency of the entire finned surface is given by:

$$
\begin{equation*}
\eta_{w}=\frac{A_{\text {prime }}+\eta_{f} A_{\text {fins }}}{A_{T o t}} \tag{2.31}
\end{equation*}
$$

where

$$
\begin{aligned}
A_{\text {fins }} & =2 n_{t} N_{f} b_{c} L \\
A_{\text {prime }} & =\left(\pi D_{o}-N_{f} \tau\right) n_{t} L \\
A_{\text {Tot }} & =A_{\text {prime }}+A_{\text {fins }}
\end{aligned}
$$

$n_{t}=$ number of finned pipes
$N_{f}=$ number of fins on each pipe
$D_{o}=$ pipe OD
$L=$ pipe length

### 4.7.3 Overall heat-transfer coefficient

The overall coefficient is based on the total external surface area, $A_{T o t}$, of the inner pipe. The overall resistance to heat transfer is thus $1 / U A_{T o t}$, and is the sum of the inner and outer convective resistances, the conductive resistance of the pipe wall, and the resistances of the fouling layers (if present). The outer convective resistance in a finned annulus is:

$$
\begin{equation*}
R_{t h}=\frac{1}{h_{o} \eta_{w} A_{T o t}} \tag{2.32}
\end{equation*}
$$

Therefore, viewing $R_{D o}$ as a reciprocal heat-transfer coefficient, we have:

$$
\begin{gather*}
\frac{1}{U_{D} A_{T o t}}=\frac{1}{h_{i} A_{i}}+\frac{R_{D i}}{A_{i}}+\frac{\ln \left(D_{o} / D_{i}\right)}{2 \pi k_{p i p e} L}+\frac{1}{h_{o} \eta_{w} A_{T o t}}+\frac{R_{D o}}{\eta_{w} A_{T o t}}  \tag{4.25}\\
U_{D}=\left[\frac{A_{T o t}}{h_{i} A_{i}}+\frac{R_{D i} A_{T o t}}{A_{i}}+\frac{A_{T o t} \ln \left(D_{o} / D_{i}\right)}{2 \pi k_{p i p e} L}+\frac{1}{h_{o} \eta_{w}}+\frac{R_{D o}}{\eta_{w}}\right]^{-1} \tag{4.26}
\end{gather*}
$$

where $A_{i}=\pi D_{i} L$.
The equation for the clean overall coefficient is obtained by dropping the fouling terms:

$$
\begin{equation*}
U_{C}=\left[\frac{A_{T o t}}{h_{i} A_{i}}+\frac{A_{T o t} \ln \left(D_{o} / D_{i}\right)}{2 \pi k_{p i p e} L}+\frac{1}{h_{o} \eta_{w}}\right]^{-1} \tag{4.27}
\end{equation*}
$$

### 4.7.4 Flow area and equivalent diameter

Consider a finned annulus comprised of an outer pipe with ID of $D_{2}$ and $n_{t}$ inner pipes, each with OD of $D_{1}$ and containing $N_{f}$ rectangular fins of height $b$ and thickness $\tau$. The flow area and wetted perimeter are:

$$
\begin{align*}
& \qquad A_{f}=\frac{\pi}{4}\left(D_{2}^{2}-n_{t} D_{1}^{2}\right)-n_{t} N_{f} b \tau  \tag{4.28}\\
& \text { wetted perimeter } \tag{4.29}
\end{align*}=\pi\left(D_{2}+n_{t} D_{1}\right)+2 n_{t} N_{f} b
$$

In the case of welded or soldered fins, these equations neglect the thickness of the channels where they overlay the pipe surface.

The equivalent diameter is obtained in the usual way as 4 times the flow area divided by the wetted perimeter:

$$
\begin{equation*}
D_{e}=\frac{\pi\left(D_{2}^{2}-n_{t} D_{1}^{2}\right)-4 n_{t} N_{f} b \tau}{\pi\left(D_{2}+n_{t} D_{1}\right)+2 n_{t} N_{f} b} \tag{4.30}
\end{equation*}
$$

### 4.8 Heat-Transfer Coefficients and Friction Factors for Finned Annuli

Heat-transfer coefficients and friction factors were determined experimentally in commercial double-pipe fin-tube exchangers by DeLorenzo and Anderson [5]. Their data were re-plotted by Kern and Kraus [3], whose graphs are reproduced in Figures 4.4 and 4.5. Note that the quantity plotted in Figure 4.5 is a Fanning friction factor that has been modified by dividing by the conversion factor, $144 \mathrm{in} .{ }^{2} / \mathrm{ft}^{2}$. Therefore, the value from Figure 4.5 must be multiplied by a factor of


Figure 4.4 Heat-transfer coefficients for finned annuli (Source: Ref. [3]).


Figure 4.5 Friction factors for finned annuli (Source: Ref. [3]).
$4 \times 144=576$ to convert to a dimensionless Darcy friction factor for use in Equation (4.5). This factor of 576 is included in the curve fits to the graphs given below:

$$
\begin{align*}
j_{H} & =\left(0.0263 R e^{0.9145}+4.9 \times 10^{-7} R e^{2.618}\right)^{1 / 3} \quad(\text { for } 24 \text { fins) }  \tag{4.31}\\
j_{H} & =\left(0.0116 R e^{1.032}+4.9 \times 10^{-7} R e^{2.618}\right)^{1 / 3} \quad \text { (for } 36 \text { fins) }  \tag{4.32}\\
f & =\frac{64}{R e} \quad(R e \leq 400)  \tag{4.33}\\
f=576 & \exp \left[0.08172(\ln R e)^{2}-1.7434 \ln R e-0.6806\right] \quad(R e>400) \tag{4.34}
\end{align*}
$$

It should also be noted that the fins act to destabilize the laminar flow field, and as a result, the critical Reynolds number is approximately 400 in the finned annulus. Therefore, if the annulus is treated as an equivalent pipe with a critical Reynolds number of approximately 2100, both the heat-transfer coefficient and friction factor will be underestimated for $400<R e<2100$. It is also remarkable to note that the friction factor in the laminar region follows the Fanning equation for pipe flow ( $f=16 / R e$ ) rather than annular flow ( $f \cong 24 / R e$ ).
The exchangers used by DeLorenzo and Anderson contained 24, 28, or 36 fins per tube, and at low Reynolds numbers the correlation for $j_{H}$ depends on the fin number. The effect is most likely due to the fact that $L / D_{e}$ varied from 574 for the exchangers with 24 fins to 788 for the exchangers with 36 fins. For $R e \leq 1000$, the difference between the two curves in Figure 4.4 is well accounted for by a factor of $\left(L / D_{e}\right)^{-1 / 3}$. Therefore, it is suggested that Figure 4.4 (or Equations (4.31) and (4.32)) be used in the following way. Use the curve (or equation) for 24 or 36 fins, whichever has the $L / D_{e}$ value closest to the exchanger being calculated. Then, for $R e \leq 1000$ scale the computed value of $j_{H}$ by a factor of $\left(L / D_{e}\right)^{-1 / 3}$, i.e.,

$$
\begin{equation*}
j_{H}=\left(j_{H}\right)_{F i g .4 .4}\left[\frac{\left(L / D_{e}\right)_{\text {Fig.4.4 }}}{\left(L / D_{e}\right)}\right]^{1 / 3} \tag{4.35}
\end{equation*}
$$

where

$$
\begin{aligned}
\left(L / D_{e}\right)_{\text {Fig. } 4.4} & =788 \quad \text { (for } 36 \text { fins) } \\
& =574 \quad \text { (for } 24 \text { fins) }
\end{aligned}
$$

For Reynolds numbers above 1000, the effect of fin number diminishes and the correction factor in Equation (4.35) can be omitted. Note that the length used in this calculation is the length of a hairpin, i.e., the length of pipe in one leg of one hairpin.

### 4.9 Wall Temperature for Finned Pipes

The heat-transfer correlation of DeLorenzo and Anderson contains a viscosity correction factor that is calculated using a weighted average temperature, $T_{w t d}$, of the extended and prime surfaces. The temperature, $T_{p}$, of the prime surface is used to calculate the viscosity correction factor for the fluid in the inner pipe. The derivation of the equations for the two pipe wall temperatures is similar to the derivation of the wall temperature presented in Chapter 3. All of the heat is assumed to be transferred between the streams at their average temperatures, $t_{\text {ave }}$ for the fluid in the inner pipe and $T_{\text {ave }}$ for the fluid in the annulus. An energy balance gives:

$$
\begin{equation*}
q=h_{i} A_{i}\left(t_{a v e}-T_{p}\right)=h_{o} \eta_{w} A_{T o t}\left(T_{p}-T_{a v e}\right) \tag{4.36}
\end{equation*}
$$

The weighted average temperature, $T_{w t d}$, is defined by:

$$
\begin{equation*}
q=h_{o} A_{T o t}\left(T_{w t d}-T_{a v e}\right) \tag{4.37}
\end{equation*}
$$

Solving these equations for $T_{p}$ and $T_{w t d}$ yields:

$$
\begin{gather*}
T_{p}=\frac{h_{i} t_{a v e}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right) T_{a v e}}{h_{i}+h_{o} \eta_{w}\left(A_{\text {Tot }} / A_{i}\right)}  \tag{4.38}\\
T_{w t d}=\frac{h_{i} \eta_{w} t_{a v e}+\left[h_{i}\left(1-\eta_{w}\right)+h_{o} \eta_{w}\left(A_{\text {Tot }} / A_{i}\right)\right] T_{a v e}}{h_{i}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right)} \tag{4.39}
\end{gather*}
$$

To reiterate, $T_{p}$ is used to find $\phi_{i}$ and $T_{w t d}$ is used for $\phi_{0}$.

The calculation of a finned-pipe exchanger is illustrated by the following example that involves the design of an oil cooler [3]. Services, such as the one in this example, that transfer heat between an organic stream and water (usually cooling water), are good candidates for finned exchangers. The reason is that heat-transfer coefficients for water streams are often substantially higher than those for organics.

## Example 4.2

Design a heat exchanger to cool $18,000 \mathrm{lb} / \mathrm{h}$ of a petroleum distillate oil from $250^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ using water with a temperature range of $85-120^{\circ} \mathrm{F}$. A maximum pressure drop of 20 psi for each stream is specified and a fouling factor of $0.002 \mathrm{~h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for each stream. The exchanger will use 25 -ft long carbon steel hairpins with 3 -in. schedule 40 outer pipes, 1.5 -in schedule 40 inner pipes, and internal return bends. Each inner pipe contains 24 carbon steel fins $0.5-\mathrm{in}$. high and $0.035-\mathrm{in}$. thick. Physical properties at the average stream temperatures are given in the following table. Note that the oil viscosity is calculated from the equation:

$$
\mu_{\text {oil }}(\mathrm{cp})=0.003024 \exp \left[\frac{4495.5}{T\left({ }^{\circ} \mathrm{R}\right)}\right]
$$

This result is obtained by fitting the relation:

$$
\mu=\alpha e^{\beta / T}
$$

using the two data points $\mu=4.8 \mathrm{cp}$ at $150^{\circ} \mathrm{F}$ and $\mu=1.7 \mathrm{cp}$ at $250^{\circ} \mathrm{F}$.

| Fluid property | Oil at $200^{\circ} \mathrm{F}$ | Water at $102.5^{\circ} \mathrm{F}$ |
| :--- | :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lb} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.52 | 1.0 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.074 | 0.37 |
| $\mu(\mathrm{cp})$ | 2.75 | 0.72 |
| Specific gravity | 0.82 | 0.99 |
| $P r$ | 46.75 | 4.707 |

## Solution

For the first trial, assume that the hairpins will be connected in series on both sides. Since the oil stream is expected to have the lower heat-transfer coefficient, it must flow in the annulus where the fins are located. Counter-flow is assumed.
(a) Energy balances.

$$
\begin{aligned}
q & =\left(\dot{m} C_{P} \Delta T\right)_{\text {oil }}=18,000 \times 0.52 \times 100=936,000 \mathrm{Btu} / \mathrm{h} \\
936,000 & =\left(\dot{m} C_{P} \Delta T\right)_{\text {water }}=\dot{m}_{\text {water }} \times 1.0 \times 35 \\
\dot{m}_{\text {water }} & =26,743 \mathrm{lb} / \mathrm{h}
\end{aligned}
$$

(b) LMTD.

$$
\Delta T_{\ln }=\frac{130-65}{\ln (130 / 65)}=93.8^{\circ} \mathrm{F}
$$

(c) Calculate $h_{i}$ assuming $\phi_{i}=1.0$.

For $1.5-\mathrm{in}$. schedule 40 pipe,

$$
\begin{aligned}
D_{i} & =1.61 \mathrm{in}=0.1342 \mathrm{ft}(\text { Table B.2) } \\
R e & =\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 26,743}{\pi \times 0.1342 \times 0.72 \times 2.419}=145,680 \Rightarrow \text { turbulent flow } \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 R e^{0.8} \operatorname{Pr}^{1 / 3} \\
& =(0.37 / 0.1342) \times 0.023(145,680)^{0.8}(4.707)^{1 / 3} \\
h_{i} & =1436 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(d) Calculate $h_{o}$ assuming $\phi_{o}=1.0$.

From Table B.2,

$$
\begin{aligned}
& D_{2}=3.068 \text { in. (ID of } 3 \text {-in. schedule } 40 \text { pipe) } \\
& D_{1}=1.9 \mathrm{in} .(\text { OD of } 1.5-\mathrm{in} . \text { schedule } 40 \text { pipe })
\end{aligned}
$$

For the finned annulus, the flow area and wetted perimeter are calculated from Equations (4.28) and (4.29), respectively, with $n_{t}=1$ :

$$
\begin{aligned}
& \qquad \begin{aligned}
A_{f} & =(\pi / 4)\left(D_{2}^{2}-D_{1}^{2}\right)-n_{t} N_{f} b \tau \\
& =(\pi / 4)\left[(3.068)^{2}-(1.9)^{2}\right]-1 \times 24 \times 0.5 \times 0.035 \\
A_{f} & =4.1374 \mathrm{in.}^{2}=0.0287 \mathrm{ft}^{2} \\
\text { wetted perimeter } & =\pi\left(D_{2}+n_{t} D_{1}\right)+2 n_{t} N_{f} b \\
& =\pi(3.068+1 \times 1.9)+2 \times 1 \times 24 \times 0.5
\end{aligned}
\end{aligned}
$$

wetted perimeter $=39.6074 \mathrm{in} .=3.3006 \mathrm{ft}$

$$
\begin{aligned}
D_{e} & =4 \times A_{f} / \text { wetted perimeter } \\
D_{e} & =4 \times 0.0287 / 3.3006=0.03478 \mathrm{ft} \\
G & =\dot{m} / A_{f}=18,000 / 0.0287=627,178 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =D_{e} G / \mu=0.03478 \times 627,178 /(2.75 \times 2.419)=3279
\end{aligned}
$$

From Figure 4.4, $j_{H} \cong 9.2$. (Equations (4.31) and (4.32) both give $j_{H}=9.4$.) Therefore,

$$
\begin{aligned}
& h_{o}=j_{H}\left(k / D_{e}\right) \operatorname{Pr}^{1 / 3}=9.2(0.074 / 0.03478)(46.75)^{1 / 3} \\
& h_{o}=70.5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(e) Fin efficiency.

The fin efficiency is calculated from Equation (4.24) with $k=26 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ for carbon steel fins:

$$
\begin{aligned}
m & =\left(\frac{2 h_{o}}{k \tau}\right)^{1 / 2}=\left(\frac{2 \times 70.5}{26 \times(0.035 / 12)}\right)^{1 / 2}=43.12 \mathrm{ft} \\
b_{c} & =b+\tau / 2=(0.5+0.035 / 2) / 12=0.04313 \mathrm{ft} \\
m b_{c} & =43.12 \times 0.04313=1.8598 \\
\eta_{f} & =\frac{\tanh \left(m b_{c}\right)}{m b_{c}}=\frac{\tanh (1.8598)}{1.8598}=0.5122
\end{aligned}
$$

The weighted efficiency of the finned surface is given by Equation (2.31):

$$
\begin{aligned}
\eta_{w} & =\frac{A_{\text {prime }}+\eta_{f} A_{\text {fins }}}{A_{\text {Tot }}} \\
A_{\text {fins }} & =2 n_{t} N_{f} b_{c} L=2 \times 1 \times 24 \times 0.04313 \times L=2.07 L \mathrm{ft}^{2} \\
A_{\text {prime }} & =\left(\pi D_{o}-N_{f} \tau\right) n_{t} L \\
& =\left(\frac{\pi \times 1.9-24 \times 0.035}{12}\right) \times 1 \times L=0.43 L \mathrm{ft}^{2} \\
A_{\text {Tot }} & =A_{\text {fins }}+A_{\text {prime }}=2.50 L \mathrm{ft}^{2}
\end{aligned}
$$

The total length of pipe in the heat exchanger is unknown, but since $L$ cancels in Equation (2.31), the areas per unit length can be used. Thus,

$$
\eta_{w}=\frac{0.43+0.5122 \times 2.07}{2.50} \cong 0.60
$$

(f) Wall temperatures.

The wall temperatures used to obtain viscosity correction factors are given by Equations (4.38) and (4.39). The inside surface area of the inner pipe is:

$$
A_{i}=\pi D_{i} L=\pi \times 0.1342 \times L=0.4216 L \mathrm{ft}^{2}
$$

Hence,

$$
\begin{aligned}
A_{T o t} / A_{i} & =2.50 / 0.4216=5.93 \\
T_{p} & =\frac{h_{i} t_{\text {ave }}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right) T_{\text {ave }}}{h_{i}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right)} \\
& =\frac{1436 \times 102.5+70.5 \times 0.6 \times 5.93 \times 200}{1436+70.5 \times 0.6 \times 5.93} \\
T_{p} & =117^{\circ} \mathrm{F} \\
T_{w t d} & =\frac{h_{i} \eta_{w} t_{\text {ave }}+\left[h_{i}\left(1-\eta_{w}\right)+h_{o} \eta_{w}\left(A_{\text {Tot }} / A_{i}\right)\right] T_{\text {ave }}}{h_{i}+h_{o} \eta_{w}\left(A_{\text {Tot }} / A_{i}\right)} \\
& =\frac{1436 \times 0.6 \times 102.5+[1436 \times 0.4+70.5 \times 0.6 \times 5.93] \times 200}{1436+70.5 \times 0.6 \times 5.93} \\
T_{w t d} & =150^{\circ} \mathrm{F}
\end{aligned}
$$

(g) Viscosity correction factors and corrected heat-transfer coefficients.

From Figure A.1, the viscosity of water at $117^{\circ} \mathrm{F}$ is approximately 0.62 cp . Hence,

$$
\phi_{i}=(0.72 / 0.62)^{0.14}=1.021
$$

The oil viscosity at $150^{\circ} \mathrm{F}=610^{\circ} \mathrm{R}$ is:

$$
\mu_{\text {oil }}=0.003024 \exp (4495.5 / 610)=4.8 \mathrm{cp}
$$

Therefore,

$$
\phi_{o}=(2.75 / 4.8)^{0.14}=0.925
$$

The corrected heat-transfer coefficients are:

$$
\begin{aligned}
& h_{i}=1436 \times 1.021=1466 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
& h_{o}=70.5 \times 0.925=65 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Steps (e)-(g) could be repeated using the new values of $h_{i}$ and $h_{o}$, but iteration is usually unnecessary. In the present case, recalculation yields $\eta_{w}=0.61, T_{p}=116^{\circ} \mathrm{F}$, and $T_{w t d}=149^{\circ} \mathrm{F}$, which leaves $h_{i}$ and $h_{o}$ essentially unchanged.
(h) Overall coefficient.

The overall coefficient for design is calculated from Equation (4.26):

$$
\begin{aligned}
U_{D} & =\left[\frac{A_{T o t}}{h_{i} A_{i}}+\frac{R_{D i} A_{T o t}}{A_{i}}+\frac{A_{T o t} \ln \left(D_{o} / D_{i}\right)}{2 \pi k_{p i p e} L}+\frac{1}{h_{o} \eta_{w}}+\frac{R_{D o}}{\eta_{w}}\right]^{-1} \\
& =\left[\frac{5.93}{1466}+0.002 \times 5.93+\frac{2.50 \times L \ln (1.9 / 1.61)}{2 \times \pi \times 26 \times L}+\frac{1}{65 \times 0.6}+\frac{0.002}{0.6}\right]^{-1} \\
U_{D} & =21.1 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(i) Required heat-transfer surface and number of hairpins.

$$
A=\frac{q}{U_{D} \Delta T_{\mathrm{ln}}}=\frac{936,000}{21.1 \times 93.8}=473 \mathrm{ft}^{2}
$$

Area per hairpin $=2.50 L=2.50(25 \times 2)=125 \mathrm{ft}^{2}$
Number of hairpins $=473 / 125=3.78 \Rightarrow 4$
(j) Pressure drop for water (inner pipe).

$$
\begin{aligned}
A_{f} & =0.01414 \mathrm{ft}^{2} \text { for } 1.5 \text {-in. schedule } 40 \text { pipe (Table B.2) } \\
G & =\dot{m} / A_{f}=26,743 / 0.01414=1,891,301 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =145,680 \text { from Step (c) } \\
f & =0.3673 R e^{-0.2314}=0.3673(145,680)^{-0.2314} \\
f & =0.02345
\end{aligned}
$$

$$
\begin{aligned}
\Delta P_{f} & =\frac{f G^{2} L}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.02345(1,891,301)^{2} \times 4 \times 50}{7.50 \times 10^{12} \times 0.1342 \times 0.99 \times 1.021} \\
\Delta P_{f} & =16.50 \mathrm{psi} \\
\Delta P_{r} & =1.6 \times 10^{-13}\left(2 N_{H P}-1\right) G^{2} / \mathrm{s} \\
& =1.6 \times 10^{-13}(2 \times 4-1)(1,891,301)^{2} / 0.99 \\
\Delta P_{r} & =4.05 \mathrm{psi} \\
\Delta P_{i} & =\Delta P_{f}+\Delta P_{r}=16.50+4.05 \cong 20.6 \mathrm{psi}
\end{aligned}
$$

(k) Pressure drop for oil (annulus).

From Step (d) we have:

$$
\begin{aligned}
R e & =3279 \\
G & =627,178 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
D_{e} & =0.03478 \mathrm{ft}
\end{aligned}
$$

The friction factor is calculated using Equation (4.34):

$$
\begin{aligned}
f & =576 \exp \left[0.08172(\ln R e)^{2}-1.7434 \ln R e-0.6806\right] \\
& =576 \exp \left[0.08172(\ln 3278)^{2}-1.7434 \ln (3278)-0.6806\right]=0.04585 \\
\Delta P_{f} & =\frac{f G^{2} L}{7.50 \times 10^{12} D_{e} s \phi}=\frac{0.04585(627,178)^{2} \times 4 \times 50}{7.50 \times 10^{12} \times 0.03478 \times 0.82 \times 0.925} \\
\Delta P_{f} & =18.24 \mathrm{psi} \\
\Delta P_{r} & =1.6 \times 10^{-13}\left(2 N_{H P}-1\right) G^{2} / s \\
& =1.6 \times 10^{-13}(2 \times 4-1)(627,178)^{2} / 0.82 \\
\Delta P_{r} & =0.54 \mathrm{psi}
\end{aligned}
$$

Assuming 2 -in. schedule 40 nozzles having a cross-sectional area of $0.0233 \mathrm{ft}^{2}$,

$$
G_{n}=18,000 / 0.0233=772,532 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

For the outlet nozzle, where the viscosity is highest, $\mu=4.8 \mathrm{cp}$. Hence,

$$
R e_{n}=D G_{n} / \mu=(2.067 / 12) \times 772,532 /(4.8 \times 2.419)=11,460
$$

Thus, the flow will be turbulent in both nozzles and Equation (4.14) is applicable.

$$
\begin{aligned}
& \Delta P_{n}=2.0 \times 10^{-13} N_{H P} G_{n}^{2} / s=2.0 \times 10^{-13} \times 4(772,532)^{2} / 0.82 \\
& \Delta P_{n}=0.58 \mathrm{psi}
\end{aligned}
$$

Hence, the total pressure drop for the annulus is:

$$
\Delta P_{o}=18.24+0.54+0.58=19.4 \mathrm{psi}
$$

All design criteria are met, with the exception of $\Delta P_{i}=20.6 \mathrm{psi}$, which is slightly above the specified maximum pressure drop of 20 psi . This discrepancy is not large enough to be a concern in most situations. If necessary, however, it could be eliminated by using hairpins of length 24 ft rather than 25 ft .
Over-surface and over-design.

$$
\begin{align*}
U_{C} & =\left[\frac{A_{\text {Tot }}}{h_{o} A_{i}}+\frac{A_{\text {Tot }} \ln \left(D_{o} / D_{i}\right)}{2 \pi k_{p i p e} L}+\frac{1}{h_{o} \eta_{w}}\right]^{-1}  \tag{l}\\
& =\left[\frac{5.93}{1466}+\frac{2.50 \ln (1.9 / 1.61)}{2 \times \pi \times 26}+\frac{1}{65 \times 0.6}\right]^{-1} \\
U_{C} & =31.0 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
A_{C} & =\frac{q}{U_{C} \Delta T_{\mathrm{ln}}}=\frac{936,000}{31.0 \times 93.8}=322 \mathrm{ft}^{2} \\
A & =2.50 L=2.50 \times 200=500 \mathrm{ft}^{2} \\
\text { over-surface } & =\left(A-A_{C}\right) / A_{C}=(500-322) / 322 \cong 55 \%
\end{align*}
$$

The required surface area is $473 \mathrm{ft}^{2}$ from Step (i). Therefore, the over-design is:

$$
\text { over-design }=(500-473) / 473=5.7 \%
$$

The over-surface is relatively high and suggests that the exchanger may be over-sized. The reason lies in the large value of the total fouling allowance:

$$
\begin{aligned}
& R_{D}=R_{D i} A_{T o t} / A_{i}+R_{D o} / \eta_{w}=0.002 \times 5.93+0.002 / 0.6 \\
& R_{D}=0.01519 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
\end{aligned}
$$

The high over-surface is simply a reflection of the large effect that internal fouling has on the design overall heat-transfer coefficient. The effect is much greater in finned exchangers because the ratio of external to internal surface area is so high ( 5.93 in this case versus 1.18 for an un-finned $1.5-\mathrm{in}$. schedule 40 pipe). With the fouling factors specified in this example, the two fouling resistances account for $30 \%$ of the total thermal resistance. Clearly, in the design of finned exchangers, care must be exercised to ensure that an appropriate value is selected for the inner fouling factor.

To summarize, for the problem as given, the final design consists of four hairpins connected in series on both sides with water in the inner pipe and oil in the annulus.

In the preceding example it will be noticed that the fin efficiency was calculated based on a clean surface. The effect of fouling on $\eta_{f}$ can be accounted for by using an effective heat-transfer coefficient, $h_{o}^{\prime}[3,6-8]$ :

$$
\begin{equation*}
h_{o}^{\prime}=\left(1 / h_{o}+R_{D o}\right)^{-1} \tag{4.40}
\end{equation*}
$$

Since $h_{o}^{\prime}<h_{o}$, the effect of fouling is to increase the fin efficiency. Therefore, neglecting the effect of fouling on $\eta_{f}$ gives a somewhat conservative estimate of $U_{D}$. Furthermore, using $h_{o}^{\prime}$ requires a separate calculation using $h_{o}$ in order to obtain $U_{C}$. In addition, if $h_{o}^{\prime}$ is used in calculating $U_{D}$, consistency then dictates that the temperatures used to obtain the viscosity correction factors should be those at the exterior surfaces of the fouling layers. Finding those temperatures involves a rather lengthy iterative calculation [3,7]. Thus, for hand calculations, it is justifiable to neglect these complications and use the fin efficiency based on clean conditions.

### 4.10 Computer Software

### 4.10.1 HEXTRAN

Essentially all heat-transfer equipment is designed using commercial and/or in-house computer software packages. In this section we consider one such package, HEXTRAN, by SimSci-Esscor (www.simsci-esscor.com), a division of Invensys Systems, Inc. This program is available as part of the Process Engineering Suite that includes the PRO II chemical process simulator. Unique among software packages devoted exclusively to heat-transfer operations, HEXTRAN is a flowsheet simulator that employs the same extensive physical property data banks and thermodynamic routines developed for PRO II. The program also interfaces with the widely used HTRI Xchanger Suite software package, allowing the HTRI computational engines to be accessed and used to simulate heat exchangers on a HEXTRAN flowsheet.

The double-pipe heat-exchanger module (DPE) in HEXTRAN handles exchangers with a single inner pipe, either plain or finned. A separate module (MTE) is used for multi-tube hairpin exchangers. Both of these modules operate only in rating mode. Therefore, design must be done wholly by a trial-and-error procedure. Other HEXTRAN modules can operate in either design or rating mode. The following examples explore some of the attributes of the double-pipe exchanger module in HEXTRAN, version 9.1.

## Example 4.3

Use HEXTRAN to rate the initial configuration (six hairpins in series) for the benzene-aniline exchanger of Example 4.1, and compare the results with those obtained previously by hand.

## Solution

After program startup, login is achieved by entering simsci for both the User Name and Password. A new problem is then opened by entering flowsheet and database names. The flowsheet (shown below) is easily constructed using the mouse to drag and drop icons from the palette at the right of the screen to the drawing area. The items required for this problem are one double-pipe heat exchanger and four process streams (two feeds and two products). The streams are connected to the inlet and outlet ports of the heat exchanger by clicking and scrolling with the mouse. Right-clicking on any object (a stream or unit) on the flowsheet brings up the edit menu with options that include deleting or renaming the object, changing its configuration, and editing the data for the object. After renaming the streams, the flowsheet for this problem appears as shown on the next page.

In order to facilitate comparison with the hand calculations, the physical property values from Example 4.1 are used. Since the viscosity correction factors are close to unity in this problem, the temperature variation of viscosity is neglected. The two feed streams are first defined as bulk property streams by right-clicking on each stream in turn and selecting Change Configuration from the pop-up edit menu. There are five types of streams in HEXTRAN:

- Compositional
- Assay
- Bulk Property
- Water/Steam
- Utility

A compositional stream (the default type) is one having a defined composition. For this type of stream, methods must be chosen for generating thermodynamic and transport properties. An assay stream is a petroleum stream for which a complete assay is available. A bulk property stream is either one for which the average properties are known or a hydrocarbon stream for which the properties can be estimated from known values of specific gravity and Watson characterization factor (see Appendix E). A water/steam stream consists of pure water in the liquid and/or vapor state, for which the thermodynamic properties are obtained from steam tables. Utility streams in


HEXTRAN are used only in pinch calculations (see Chapter 8). For this problem, the Bulk Property option is selected.

The properties of the two feed streams are entered by selecting Edit Properties from the pop-up edit menu or by double-clicking on the stream. The flow rate, feed temperature, and feed pressure are entered on the Specifications form as shown below for benzene:


HEXTRAN requires pressures as well as temperatures for the two feed streams. Since these pressures were not specified in Example 4.1 (they are not needed for the calculations), a convenient (albeit rather high for this service) value of 100 psia is arbitrarily assigned to each stream. On the External Property Sets/Average Values form, the average stream values of specific heat, thermal conductivity, viscosity, and density are entered by selecting each property name, in turn, from the list box as shown below. Values of the first three properties for each stream are entered exactly as given in Example 4.1. The densities ( $54.876 \mathrm{lbm} / \mathrm{ft}^{3}$ for benzene and $63.803 \mathrm{lbm} / \mathrm{ft}^{3}$ for aniline) are obtained from the specific gravities given in Example 4.1. The densities, not the specific gravities, must be entered here. Otherwise, HEXTRAN will assume that stream properties are to be estimated using correlations for hydrocarbons as discussed in Appendix E.


The parameters of the heat exchanger are specified by right-clicking on the unit and selecting Edit Properties from the pop-up menu. This brings up the required forms and data are entered for the tube side (inner pipe), shell side (annulus), and nozzles as shown below. A hairpin is modeled as a single HEXTRAN shell with a length of 32 ft , the total length of pipe in both legs of the hairpin. Thus, six shells in series are specified. One-inch schedule 40 nozzles having an ID of 1.049 in . are assumed for the annulus, and no nozzles are specified for the inner pipe by un-checking the box labeled Perform Nozzle Sizing and Pressure Drop Calculations.

On the materials form, type 316 stainless steel is selected from the list boxes for shell material and tube material. Finally, on the Film Options form the tube-side and shell-side fouling factors (both $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ ) are entered under Fouling Resistances.

When all required data have been entered for a stream or unit, the color of the corresponding label on the flowsheet changes from red to black. The program is executed by clicking either Run or the right-pointing arrowhead on the top toolbar.

The input (keyword) file generated by the graphical user interface (GUI) is given below. Many of the items in this file are superfluous for this simulation, but are automatically included by the GUI in every case. The main items are the STREAM DATA section, where the properties of the two inlet streams are specified, and the UNIT OPERATIONS section, where the characteristics of the heat


exchanger are specified. The online help file contains a detailed explanation of the keyword code used by HEXTRAN, much of which is self-evident. Note that dollar signs are used for comment statements (which are ignored by the program) while an asterisk indicates that a statement is continued on the next line. The input file is echo printed at the top of the output file along with any warnings or error messages. The output file is accessed by selecting View Report from the Output menu. (To access the files directly, go to C: $\backslash$ Program Files $\backslash$ SIMSCI $\backslash$ SIM4ME11 $\backslash$ Server $\backslash$ Model Apps, open the folder bearing the name of the database followed by the folder bearing the flowsheet name. The input and output files have the same name as the flowsheet with extensions .inp and .out, respectively.)

Results of the calculations are summarized in the Double Pipe Exchanger Data Sheet and Extended Data Sheet, which are given below following the input file. This information was extracted from the HEXTRAN output file and used to prepare the following comparison between computer and hand calculations:

| Item | Hand calculation | HEXTRAN |
| :---: | :---: | :---: |
| $R e_{i}$ | 83,217 | 83,202 |
| $R e_{0}$ | 8212 | 8211 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 290 * | 289.8 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 283 * | 248.7 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 89* | 85.2 |
| $\Delta P_{i}(\mathrm{psi})$ | 8.09* | 8.02 |
| $\Delta P_{o}$ (excluding nozzles, psi ) | 48.7** | 43.7 |

It can be seen that the HEXTRAN results for the inner pipe are in close agreement with the hand calculations, but significant differences exist for the annulus, where the flow is in the transition region. For Reynolds numbers between 2000 and 10,000 HEXTRAN uses linear interpolation to calculate heat-transfer coefficients and friction factors. The heat-transfer coefficient (or friction factor) is calculated for $R e=2000$ and $R e=10,000$ using the appropriate correlations for laminar and turbulent flow, respectively. Linear interpolation between these two values is then used to obtain $h$ (or $f$ ) at the actual Reynolds number for the flow. In the present instance this procedure gives lower values of $h$ and $f$ compared with the hand calculations. As a result, the target temperatures for the two streams were not quite achieved in the simulation. For example, it can be seen from the output data that the benzene outlet temperature was $119.6^{\circ} \mathrm{F}$ versus $120^{\circ} \mathrm{F}$ as required by the design specifications.

Actually, the close agreement between the pressure drops for the inner pipe is fortuitous. Details of the methods used for pressure-drop calculations for double-pipe exchangers are not specified in the HEXTRAN documentation. However, by running additional simulations in which a hairpin was modeled as two or more HEXTRAN shells connected in series, it was possible to separate the pressure drop in the straight sections of pipe from that in the return bends. It was found that for shells connected in series, HEXTRAN uses 2 velocity heads per shell for the return-bend losses in the annulus and $4 \times$ (number of shells -1 ) velocity heads for the inner pipe return losses. For the present problem, this results in the following values for the inner pipe:

| Item | Hand | HEXTRAN |
| :--- | :--- | :--- |
| $\Delta P_{f}(\mathrm{psi})$ | 6.24 | 5.21 |
| $\Delta P_{r}(\mathrm{psi})$ | 1.85 | 2.81 |
| $\Delta P_{i}(\mathrm{psi})$ | 8.09 | 8.02 |

Clearly, the differences in $\Delta P_{f}$ and $\Delta P_{r}$ will result in greater differences in $\Delta P_{i}$ for different lengths of pipe. In the present case with six hairpins in series, the $\Delta P_{i}$ values calculated by HEXTRAN were within $10 \%$ of the values calculated by hand for hairpins ranging in length from 8 to 32 ft .

## HEXTRAN Input File for Example 4.3

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=EX4-3, PROBLEM=Benzene Heater, SITE=
$
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
    ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
    PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
    UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=CP, WT=LB, *
    XDENSITY=API, STDVAPOR=379.490
$
PRINT ALL, *
    RATE=M
$
CALC PGEN=New, WATER=Saturated
$
```


## HEXTRAN Input File for Example 4.3 (continued)

\$ Component Data Section
\$
\$
\$ Thermodynamic Data Section
$\$$
\$
\$Stream Data Section
\$
STREAM DATA

```
$
    PROP STRM=BENZENE, NAME=BENZENE, TEMP=60.00, PRES=100.000, *
        LIQUID (W)=10000.000, LCP (AVG) =0.42, Lcond (AVG) =0.092, *
        Lvis(AVG) =0.55, Lden (AVG) =54.876
$
    PROP STRM=3, NAME=3
$
    PROP STRM=4, NAME=4
$
    PROP STRM=ANILINE, NAME=ANILINE, TEMP=150.00, PRES=100.000, *
        LIQUID (W)=9692.000, LCP (AVG) =0.52, LCond (AVG)=0.1, *
        Lvis (AVG) =2, Lden(AVG)=63.803
$
$ Calculation Type Section
$
SIMULATION
$
    TOLERANCE TTRIAL=0.01
$
    LIMITS AREA=200.00, 6000.00, SERIES=1, 10, PDAMP=0.00, *
        TTRIAL=30
$
    CALC TWOPHASE=New, DPSMETHOD=Stream, MINFT=0.80
$
PRINT UNITS, ECONOMICS, STREAM, STANDARD, *
    EXTENDED, ZONES
$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR
$
    UTCOST OIL=3.50, GAS=3.50, ELECTRICITY=0.10, *
        WATER=0.03, HPSTEAM=4.10, MPSTEAM=3.90, *
        LPSTEAM=3.60, REFRIGERANT=0.00, HEATINGMEDIUM=0.00
$
    HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        EXPONENT=0.60, CONSTANT=0.00, UNIT
$
$ Unit Operations Data
```

```
HEXTRAN Input File for Example 4.3 (continued)
$
UNIT OPERATIONS
$
DPE UID=DPE1
    TYPE Old, HOTSIDE=Shellside, ORIENTATION=Horizontal, *
        FLOW=Countercurrent, *
        UESTIMATE=50.00, USCALER=1.00
    TUBE FEED=BENZENE, PRODUCT=3, *
        LENGTH=32.00, *
        NPS=1.25, SCHEDULE=40, *
        MATERIAL=9, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
    SHELL FEED=ANILINE, PRODUCT=4, *
        NPS=2.0, SCHEDULE=40, *
        SERIES=6, PARALLEL=1, *
        MATERIAL=9, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
    TNOZZ NONE
$
    SNOZZ ID=1.049, 1.049
$
    CALC TWOPHASE=New, *
        MINFT=0.80
$
    PRINT STANDARD, *
        EXTENDED, *
        ZONES
$
COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
    CONSTANT=0.00, EXPONENT=0.60, Unit
$
$ End of keyword file. . .
```


## HEXTRAN Output Data for Example 4.3



HEXTRAN Output Data for Example 4.3 (continued)


## Example 4.4

Use HEXTRAN to rate the final configuration (10 hairpins with inner pipes connected in series and annuli connected in two parallel banks) for the benzene-aniline exchanger of Example 4.1, and compare the results with those obtained previously by hand.

## Solution

The modeling is done as in the previous example using bulk stream properties and one HEXTRAN shell per hairpin. In order to accommodate the series-parallel configuration, however, each parallel bank of hairpins is represented as a separate double-pipe heat exchanger, as shown in the diagram
below. The flowsheet contains nine streams and four units (two heat exchangers, a stream divider and a mixer). Each heat exchanger consists of five hairpins connected in series. Aniline flows through the inner pipes and benzene flows through the annuli.


The input file generated by the HEXTRAN GUI is given below, followed by the data sheets for the two exchangers from the HEXTRAN output file. The data sheets were used to prepare the following comparison between computer and hand calculations:

| Item | Hand calculation | HEXTRAN |
| :--- | :---: | ---: |
| $R e_{i}$ | 22,180 | 22,176 |
| $R e_{o}$ | 15,405 | 15,403 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | $176^{\star}$ | 175.6 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | $255^{\star}$ | 254.9 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | $69.8^{\star}$ | 69.8 |
| $\Delta P_{i}(\mathrm{psi})$ | $14.0^{\star}$ | 13.6 |
| $\Delta P_{o}(\mathrm{psi})$ | $11.7^{*}$ | 10.5 |

$$
\text { *For } \phi=1.0
$$

It can be seen that the heat-transfer coefficients computed by HEXTRAN agree exactly with the hand calculations, and the two sets of pressure drops are also in reasonable agreement, although the difference on the shell side is about $10 \%$. Note that since the two exchangers are connected in series on the tube side, the total pressure drop for the aniline stream is the sum of the pressure drops in the two units.

Finally, note that the benzene outlet temperature (after mixing) is the arithmetic average of the outlet temperatures from the two exchangers. Thus,

$$
T_{\text {Benzene out }}=(134.7+108.9) / 2=121.8^{\circ} \mathrm{F}
$$

Since this temperature exceeds the design specification of $120^{\circ} \mathrm{F}$, the rating procedure indicates that the series-parallel configuration is thermally and hydraulically suitable, in agreement with the hand calculations.

## HEXTRAN Input File for Example 4.4

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=EX4-4, PROBLEM=Benzene Heater, SITE=
$
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
    ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
    PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
    UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=CP, WT=LB, *
    XDENSITY=API, STDVAPOR=379.490
$
PRINT ALL, *
    RATE=M
$
CALC PGEN=New, WATER=Saturated
$
$ Component Data Section
$
$
$ Thermodynamic Data Section
$
$
$Stream Data Section
$
STREAM DATA
$
    PROP STRM=1, NAME=1, TEMP=60.00, PRES=100.000, *
        LIQUID (W)=10000.000, LCP (AVG) =0.42, Lcond (AVG) =0.092, *
    Lvis(AVG)=0.55, Lden(AVG) =54.876
$
    PROP STRM=7, NAME=7, TEMP=150.00, PRES=100.000, *
        LIQUID (W)=9692.000, LCP (AVG)=0.52, Lcond (AVG)=0.1, *
        Lvis(AVG)=2, Lden(AVG) =63.803
$
    PROP STRM=9, NAME=9
$
    PROP STRM=2, NAME=2
$
    PROP STRM=3, NAME=3
$
    PROP STRM=6, NAME=6
$
    PROP STRM=4, NAME=4
$
    PROP STRM=5, NAME=5
$
    PROP STRM=8, NAME=8
$
```


## HEXTRAN Input File for Example 4.4 (continued)

```
$ Calculation Type Section
$
SIMULATION
$
    TOLERANCE TTRIAL=0.01
$
    LIMITS AREA=200.00, 6000.00, SERIES=1, 10, PDAMP=0.00, *
                TTRIAL=30
$
    CALC TWOPHASE=New, DPSMETHOD=Stream, MINFT=0.80
$
    PRINT UNITS, ECONOMICS, STREAM, STANDARD, *
        EXTENDED, ZONES
$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR
$
    UTCOST OIL=3.50, GAS=3.50, ELECTRICITY=0.10, *
        WATER=0.03, HPSTEAM=4.10, MPSTEAM=3.90, *
        LPSTEAM=3.60, REFRIGERANT=0.00, HEATINGMEDIUM=0.00
$
    HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
                EXPONENT=0.60, CONSTANT=0.00, UNIT
$
$ Unit Operations Data
$
UNIT OPERATIONS
$
SPLITTER UID=SP1
    STRMS FEED=1, PROD=2, 3
    OPERATION FRAC=0.5, 0.5
$
DPE UID=DPE1
    TYPE Old, HOTSIDE=Tubeside, ORIENTATION=Horizontal, *
                        FLOW=Countercurrent, *
                        UESTIMATE=50.00, USCALER=1.00
    TUBE FEED=7, PRODUCT=8, *
        LENGTH=32.00, *
        NPS=1.25, SCHEDULE=40, *
        MATERIAL=9, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
    SHELL FEED=2, PRODUCT=4, *
        NPS=2.0, SCHEDULE=40, *
        SERIES=5, PARALLEL=1, *
        MATERIAL=9, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
    TNOZZ NONE
$
```


## HEXTRAN Input File for Example 4.4 (continued)

```
    SNOZZ ID=1.049, 1.049
$
CALC TWOPHASE=New, *
    MINFT=0.80
$
    PRINT STANDARD, *
                EXTENDED, *
        ZONES
$
    COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        CONSTANT=0.00, EXPONENT=0.60, Unit
$
DPE UID=DPE2
    TYPE Old, HOTSIDE=Tubeside, ORIENTATION=Horizontal, *
        FLOW=Countercurrent, *
        UESTIMATE=50.00, USCALER=1.00
    TUBE FEED=8, PRODUCT=9, *
        LENGTH=32.00, *
        NPS=1.25, SCHEDULE=40, *
        MATERIAL=9, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
    SHELL FEED=3, PRODUCT=5, *
        NPS=2.0, SCHEDULE=40, *
        SERIES=5, PARALLEL=1, *
        MATERIAL=9, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
    TNOZZ NONE
$
    SNOZZ ID=1.049, 1.049
$
    CALC TWOPHASE=New, *
        MINFT=0.80
$
    PRINT STANDARD, *
        EXTENDED, *
        ZONES
$
    COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        CONSTANT=0.00, EXPONENT=0.60, Unit
$
MIXER UID=M1
    STRMS FEED=4, 5, PROD=6
$
$ End of keyword file...
```


## HEXTRAN Output Data for Example 4.4



## HEXTRAN Output Data for Example 4.4 (continued)



## HEXTRAN Output Data for Example 4.4 (continued)



## HEXTRAN Output Data for Example 4.4 (continued)



### 4.10.2 HTFS/Aspen

The HTFS software was originally developed by the Heat Transfer and Fluid Flow Service Division of the Atomic Energy Research Establishment, UK. The organization was later privatized and eventually became a part of Hyprotech, Ltd., developer of the HYSYS chemical process simulator. Hyprotech was subsequently assimilated by Aspen Technology, Inc. (www.aspentech.com), which now markets the software as part of the Aspen Engineering Suite. The software interfaces with HYSYS and the Aspen Plus process simulator so that the extensive thermodynamics and physical properties (including petroleum properties) packages available in the simulators can be utilized. When used on a stand-alone basis, the COMThermo package developed by Hyprotech, which is also used in HYSYS, is implemented. It contains a full range of thermodynamic routines and a database that includes over 1400 components.

The HTFS program called TASC handles both double-pipe and shell-and-tube exchangers. It consists of two parts, TASC Thermal, which performs thermal and hydraulic design and rating calculations, and TASC Mechanical, which performs mechanical design calculations. TASC Mechanical is restricted to shell-and-tube exchangers, however. TASC thermal can handle both standard and multi-tube hairpin units. Because the module is structured for shell-and-tube exchangers, many of the input data items are irrelevant for double-pipe exchangers, making it somewhat confusing to use. Also, some care must be taken to correctly interpret those parameters that do pertain to double-pipe units. Use of the TASC module is illustrated by the following examples. Version 5.01 of the software is used here; later versions exhibit only minor, superficial changes in format and produce nearly identical results.

## Example 4.5

Use TASC to rate the initial configuration (six hairpins in series) for the benzene-aniline exchanger of Example 4.1, and compare the results with those obtained previously using HEXTRAN.

## Solution

The modeling is done using the physical property data from Example 4.1 to facilitate comparison with the HEXTRAN results. English units are invoked by selecting Preferences on the File menu, then clicking the Units tab and choosing US/British for all input blocks. Input data for this problem are grouped into the following categories found on the Input menu:

- Start up
- Exchanger Geometry
- Bundle Geometry
- Nozzles
- Process
- Physical Properties

On the Start up form, Calculation Mode is set to either Checking or Simulation for a rating calculation; Simulation mode is used for this example. Checking the Basic Input Mode option simplifies the data entry process by suppressing many of the input data items that are not relevant to double-pipe exchangers.

On the Exchanger Geometry form (shown on the next page), the following settings are made:

Shell Type: Double Pipe
No. of Exchangers in Series: 6
No. of Exchangers in Parallel: 1

Shell Inside Diameter: 2.067 in.
Side for Hot Stream: Shell-side Hot
Tube Material: 316 Stainless

The entries for front and rear head types on this form are left at the default settings. Also, note that the number of exchangers in series and parallel refers to the number of hairpins. TASC sometimes uses Type D and Type $M$ shells in reference to standard and multi-tube hairpins; these are not TEMA designations, however.


On the Bundle Geometry form, the following settings are made as shown below:
Tube Length: 384 in .
Tube Outside Diameter: 1.66 in.
Tube Wall Thickness : 0.14 in .
The remaining input parameters are ignored as they are irrelevant for double-pipe exchangers. Note that the tube length is the total length of pipe in both legs of one hairpin.


On the Nozzles form, the shell-side nozzle functions are set to Inlet, Outlet, and Intermediate, respectively, for nozzles 1,2 , and 3 . The ID of each is set to 1.049 in . Intermediate nozzles are those connecting pairs of hairpins, whereas inlet and outlet nozzles refer to the entrance and exit of the heat exchanger as a whole. TASC does not have an option for omitting nozzles on the tube side. Therefore, the ID of the tube-side nozzles (inlet, outlet, and intermediate) is set to 2.067 in. , the largest value allowed by the program, in order to minimize the nozzle pressure drop calculated by the program.


Data are entered on the Process form as shown below:


Note that the inlet stream pressures are (arbitrarily) set to 60 psia. Since constant physical properties are used, stream pressure should have no effect on the calculations. However, when the inlet pressures are set to 100 psia as in previous examples, the calculations fail to converge. Also, note that the stream outlet temperatures are not specified here. In simulation mode, TASC calculates the outlet temperatures and pressures.

Finally, under the Physical Properties input category, the properties of the two streams are entered on the Thermo-Properties Input form as shown below. First, under Stream Data Source, the option <Direct Input> is clicked. This option allows the user to enter the fluid properties directly on the spreadsheet. In this problem, only one pressure and one temperature level are needed since constant properties are assumed. Therefore, the first pressure level is set to the inlet pressure ( 60 psia ), and the appropriate stream inlet temperature and physical properties ( $\rho, C_{P}, k, \mu$ ) are entered on the spreadsheet under Point 1. The procedure is then repeated for the other stream.


After completing the data entry, clicking on Run and then Calculate All executes the program, and the results summary form is shown on the screen. More detailed results are available in the full output file. The results summary generated by TASC is given below. Note that the value of 277 listed for the tube-side heat-transfer coefficient is referenced to the external surface of the pipe, i.e., it is actually $h_{i} D_{i} / D_{0}$. Hence, the value of $h_{i}$ is $277(1.66 / 1.38)=$ $333 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.

## TASC Results Summary for Example 4.5

| TASC Version 5.01 - SIMULATION |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Shell type/series/parallel | -D- |  | 6 |  | 1 |  |
| Shell diam/tube length/total area | 2.1 | in | 384.0 | in | 83.4 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 1 |  | 1 |  |  |  |
| Tube id/od/pitch (pattern) | 1.38 | in | 1.66 | in | 1.764(30) | in |
| No of baffles/pitch/cut | 0 |  |  | in |  | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 9692.0 | $\mathrm{lb} / \mathrm{h}$ | 10000.0 | $\mathrm{lb} / \mathrm{h}$ |  |  |
| Inlet temperature shell/tube | 150.0 | ${ }^{\circ} \mathrm{F}$ | 60.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 96.28 | ${ }^{\circ} \mathrm{F}$ | 122.06 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 0.0/0.0 |  | 0.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 41.956 | psi | 5.822 | psi |  |  |
| Velocity highest shell xflow/tube |  | $\mathrm{ft} / \mathrm{s}$ | 4.97 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 334 | $\mathrm{Btu} / \mathrm{hft}{ }^{2}{ }^{\circ} \mathrm{F}$ | 277 | $\mathrm{Btu} / \mathrm{hft}{ }^{2}{ }^{\circ} \mathrm{F}$ | 613 | $\mathrm{Btu} / \mathrm{hft}{ }^{2} \mathrm{~F}$ |
| Fouling coeff shell/tube | 1000 | $\mathrm{Btu} / \mathrm{hft}{ }^{2} \mathrm{~F}$ | 831 | Btu/hft ${ }^{\circ}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/ service | 121.3 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ | 95.8 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ | 95.8 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 261 | kBtu/h | 32.84 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.002 |  | 1.034 |  |  |  |

The results are compared with those from HEXTRAN in the table below. The greatest differences (about 30\%) are in the values of $h_{o}$ and $\Delta P_{i}$.

| Item | HEXTRAN | TASC |
| :--- | :---: | :---: |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 290 | 333 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{\circ} \cdot{ }^{\circ} \mathrm{F}\right)$ | 249 | 334 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 85.2 | 95.8 |
| $\Delta P_{i}(\mathrm{psi})$ | 8.0 | 5.8 |
| $\Delta P_{o}(\mathrm{psi})$ | 47 | 42 |
| Benzene outlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 119.6 | 122.1 |
| Aniline outlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 100.4 | 98.3 |

The full TASC output shows that the return-bend losses are zero. The reason is that TASC calculates these losses only if a Type U rear head is specified. (The tube length is halved in this case.) For the inner pipe, the pressure drop breakdown is as follows:

|  | HEXTRAN | TASC (L head) | TASC (U head) |
| :--- | :---: | :---: | :---: |
| $\Delta P_{f}$ (psi) | 5.2 | 5.4 | 5.4 |
| $\Delta P_{r}(\mathrm{psi})$ | 2.8 | 0 | 0.4 |
| $\Delta P_{n}(\mathrm{psi})$ | 0 | 0.4 | 0.4 |
| Total | 8.0 | 5.8 | 6.2 |

[Note: The current (2006) release of TASC uses axial tube-side nozzles for hairpin units. These have a lower pressure drop ( $<0.01 \mathrm{psi}$ ) than standard nozzles, giving $\Delta P_{i} \cong \Delta P_{f}+\Delta P_{r} \cong 5.8 \mathrm{psi}$.]

The differences in heat-transfer coefficients are obviously due to different computational methods in the two programs. The methods used by TASC are proprietary, and the program documentation provides no information about the correlations involved.

## Example 4.6

Repeat Example 4.5 using COMThermo to generate the physical properties of both streams.

## Solution

The input data for this problem are the same as for Example 4.5 with the exception of the physical property data. Clicking the Add button under Stream Data Source opens the COMThermo interface shown below. The appropriate component (benzene or aniline) is selected from the list of available components, and a suitable property package is then chosen from the list of available thermodynamic routines. For this problem, the NRTL-ideal package is chosen for both benzene and aniline. (Since each stream is a liquid consisting of a single component, the ideal-ideal property package, which treats the liquid phase as an ideal solution, will generate the same results for this problem. Additional thermodynamic routines can be accessed by checking the Advanced Views box.)

Returning to the TASC properties input screen, the Options button is clicked and the temperature range over which the properties are required is entered. For benzene, a range of $60-120^{\circ} \mathrm{F}$ is used; for aniline, $80-150^{\circ} \mathrm{F}$. The number of points in the given temperature range at which properties are to be calculated can also be specified here. For this problem, the default value of 11 points is used.

Next, the pressure levels at which the properties are required are entered. For benzene, two levels are used, 60 and 50 psia ; for aniline, three levels are entered, 60 , 30, and 15 psia. Finally, clicking the Get Properties button generates the physical property data, which are automatically entered on the spreadsheet.

The TASC results summary for this problem is given below, from which it can be seen that both the tube-side and shell-side heat-transfer coefficients are significantly lower than the corresponding values obtained in Example 4.5. The Heat-Exchanger Specification Sheet generated by TASC is given below and shows the physical properties of each stream at inlet and outlet conditions. It will be noted


that the heat capacities and thermal conductivities of both streams are lower than the values used in previous examples. Also, TASC performs a zone, or incremental, analysis (essentially a numerical integration of the design equations over the length of the heat exchanger; see Appendix 4.B) that takes into account the variation of physical properties along the length of the exchanger. The above differences notwithstanding, it is interesting to note that the overall coefficient of $84.8 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ obtained here is within $5 \%$ of the value calculated by hand in Example 4.1.

## TASC Results Summary for Example 4.6

| TASC Version 5.01 - SIMULATION |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Shell type/series/parallel | -D- |  | 6 |  | 1 |  |
| Shell diam/tube length/ total area | 2.1 | in | 384.0 | in | 83.4 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 1 |  | 1 |  |  |  |
| Tube id/od/pitch (pattern) | 1.38 | in | 1.66 | in | 1.764 (30) | in |
| No of baffles/pitch/cut | 0 |  |  | in |  |  |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 9692.0 | lb/h | 10000.0 | lb/h |  |  |
| Inlet temperature shell/tube | 150.0 | ${ }^{\circ} \mathrm{F}$ | 60.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 96.23 | ${ }^{\circ} \mathrm{F}$ | 119.22 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 0.0/0.0 |  | 0.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 44.461 | psi | 5.854 | psi |  |  |
| Velocity highest shell xflow/ tube |  | $\mathrm{ft} / \mathrm{s}$ | 5.16 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 264 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 240 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 614 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 1000 | Btu/hft ${ }^{\circ}{ }^{\circ} \mathrm{F}$ | 831 | Btu/hft ${ }^{\circ}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/ service | 104.3 | $\mathrm{Btu} / \mathrm{hft}{ }^{\circ}{ }^{\circ} \mathrm{F}$ | 84.8 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 84.8 | Btu/h $\mathrm{ft}^{2}{ }^{\text {F }}$ |
| Heat load/eff wtd mtd | 232 | kBtu/h | 33.3 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.010 |  | 0.922 |  |  |  |

## TASC Heat Exchanger Specification Sheet for Example 4.6



## References

1. Kakac, S. and H. Liu, Heat Exchangers: Selection, Rating and Thermal Design, CRC Press, Boca Raton, FL, 1998.
2. R. H. Perry and D. W. Green, eds, Perry's Chemical Engineers' Handbook, 7th edn, McGraw-Hill, New York, 1997.
3. Kern, D. Q. and A. D. Kraus, Extended Surface Heat Transfer, McGraw-Hill, New York, 1972.
4. Henry, J. A. R., Headers, nozzles and turnarounds, in Heat Exchanger Design Handbook, Vol. 2, Hemisphere Publishing Corp., New York, 1988.
5. DeLorenzo, B. and E. D. Anderson, Heat transfer and pressure drop of liquids in double-pipe fin-tube exchangers, Trans. ASME, 67, 697-702, 1945.
6. Guy, A. R., Applications of double-pipe heat exchangers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1983.
7. Kraus, A. D., A. Aziz and J. Welty, Extended Surface Heat Transfer, Wiley, New York, 2001.
8. Hewitt, G. F., G. L. Shires and T. R. Bott, Process Heat Transfer, CRC Press, Boca Raton, FL, 1994.

## Appendix 4.A. Hydraulic Equations in SI Units

For convenience in solving problems formulated in metric units, the working equations for hydraulic calculations are given below in terms of SI units. The starting point is Equation (4.3):

$$
\Delta P_{f}=\frac{f L G^{2}}{2 g_{c} \rho_{\text {water }} D_{i} s}
$$

In the SI unit system, $g_{c}=1.0$ and the density of water at $4^{\circ} \mathrm{C}$ is $1000 \mathrm{~kg} / \mathrm{m}^{3}$. With these numerical values, Equation (4.3) becomes:

$$
\begin{equation*}
\Delta P_{f}=\frac{f L G^{2}}{2000 D_{i} s} \tag{4.A.1}
\end{equation*}
$$

This equation is modified by inclusion of the viscosity correction factor to obtain the following equation for the friction loss in straight sections of pipe:

$$
\begin{equation*}
\Delta P_{f}=\frac{f L G^{2}}{2000 D_{i} s \phi} \tag{4.A.2}
\end{equation*}
$$

where

$$
\begin{aligned}
\Delta P_{f} & \propto P a \\
L, D_{i} & \propto m \\
G & \propto \mathrm{~kg} / \mathrm{s} \cdot \mathrm{~m}^{2} \\
s, f, \phi & \text { are dimensionless }
\end{aligned}
$$

The above units apply in all of the following equations.
The pressure drop associated with one velocity head is given by:

$$
\begin{equation*}
\Delta P=\left(\frac{1}{2 g_{c} \rho_{\text {water }}}\right)\left(\frac{G^{2}}{s}\right) \tag{4.A.3}
\end{equation*}
$$

Substituting $g_{c}=1.0$ and $\rho_{\text {water }}=1000 \mathrm{~kg} / \mathrm{m}^{3}$ yields:

$$
\begin{equation*}
\Delta P=5.0 \times 10^{-4} G^{2} / s \tag{4.A.4}
\end{equation*}
$$

The pressure drop in return bends is estimated using the following equations:

$$
\begin{array}{ll}
\Delta P_{r}=6.0 \times 10^{-4}\left(2 N_{H P}-1\right) G^{2} / s & \text { (turbulent flow) } \\
\Delta P_{r}=7.5 \times 10^{-4}\left(2 N_{H P}-1\right) G^{2} / s & \text { (laminar flow, } R e \geq 500) \tag{4.A.6}
\end{array}
$$

The following equations are used to estimate nozzle losses:

$$
\begin{array}{ll}
\Delta P_{n}=7.5 \times 10^{-4} N_{H P} G_{n}^{2} / s & \text { (turbulent flow) } \\
\Delta P_{n}=1.5 \times 10^{-3} N_{H P} G_{n}^{2} / s & \text { (laminar flow, } \left.R e_{n} \geq 100\right) \tag{4.A.8}
\end{array}
$$

In Equations (4.A.5-4.A.8), $N_{H P}$ represents the number of hairpins connected in series.

## Appendix 4.B. Incremental Analysis

It was noted in Appendix 3.A that the standard method for heat-exchanger analysis based on the LMTD depends on a number of simplifying assumptions, two of which are:
(1) The overall heat-transfer coefficient is constant throughout the heat exchanger.
(2) The stream enthalpies vary linearly with temperature. For single-phase operation, this implies constant heat capacities.

Although these conditions are never satisfied exactly in practice, analysis based on the LMTD is often sufficiently accurate for exchangers involving only single-phase flow. However, the above two assumptions are not generally applicable to operations involving a phase change, as in condensers, vaporizers, and reboilers. Even with single-phase operation, the overall coefficient sometimes varies greatly along the length of the exchanger. This may happen, for example, when the variation of fluid viscosity is large enough to cause a change in flow regime from turbulent at one end of the exchanger to laminar at the other end. In these situations an incremental (or zone) analysis is required.
The rate of heat transfer between the streams in a differential section of area $d A$ in the heat exchanger is:

$$
\begin{equation*}
d q=U d A\left(T_{h}-T_{c}\right) \tag{4.B.1}
\end{equation*}
$$

where $T_{h}$ and $T_{c}$ are the local temperatures of the hot and cold streams, respectively. This equation can be formally integrated over the heat-transfer area to obtain the total duty as follows:

$$
\begin{equation*}
q_{T o t}=\int_{0}^{A} U\left(T_{h}-T_{c}\right) d A \tag{4.B.2}
\end{equation*}
$$

Alternatively, the heat-transfer area required to achieve a given duty, $q_{T o t}$, is obtained by solving Equation (4.B.1) for $d A$ and integrating:

$$
\begin{equation*}
A=\int_{0}^{q_{T o t}} \frac{d q}{U\left(T_{h}-T_{c}\right)} \tag{4.B.3}
\end{equation*}
$$

In practice the integrals are evaluated numerically by discretizing the exchanger in terms of either area or duty. In the latter case, for example, Equation (4.B.3) is replaced by:

$$
\begin{equation*}
A \cong \sum_{i} \Delta A_{i}=\sum_{i} \frac{\Delta q_{i}}{U\left(T_{h, i}-T_{c, i}\right)} \tag{4.B.4}
\end{equation*}
$$

where

$$
\begin{equation*}
q_{T o t}=\sum_{i} \Delta q_{i} \tag{4.B.5}
\end{equation*}
$$

The stream energy balances are used to calculate the local stream temperatures. For a single-phase counter-flow exchanger in which the calculations are started at the cold end, the equations are:

$$
\begin{equation*}
\Delta q_{i}=C_{h, i}\left(T_{h, i+1}-T_{h, i}\right)=C_{c, i}\left(T_{c, i+1}-T_{c, i}\right) \tag{4.B.6}
\end{equation*}
$$

where $C \equiv \dot{m} C_{P}$. Similarly, the hydraulic equations are used to obtain local values of the stream pressures. Fluid properties are evaluated at the local stream conditions and used to calculate the local film and overall heat-transfer coefficients. For operations involving a phase change, additional thermodynamic calculations are performed to determine the local flow rate and composition of each phase. An example that illustrates the computational procedure for a condenser is given in Section 11.10.

Computer programs use the results of the incremental analysis to calculate mean values of the heat-transfer coefficients and temperature difference that are reported in the output summaries. Details of the incremental calculations are generally given in the full output files. It should be noted that for rating calculations involving counter-flow or multi-pass heat exchangers, the incremental analysis involves iteration. Since the output stream pressures (and possibly the outlet temperatures as well, depending on the input specifications) are unknown, at least one stream pressure (and possibly a stream temperature) is unknown at each end of the exchanger. In order to start the incremental calculations, however, the temperatures and pressures of both streams must be known at one end of the exchanger. Hence, the missing values must be assumed and subsequently updated iteratively until convergence is attained.

Many computer programs use the incremental method on all problems irregardless of whether it is really needed. Although this method undoubtedly provides the most accurate representation of the heat-transfer process, the overall accuracy is still limited by the engineering correlations used in the calculations. Furthermore, the incremental calculations sometimes fail to converge. This can lead to the seemingly paradoxical situation in which a very sophisticated computer program fails to solve a rather simple problem. Such was the case in Example 4.5 when the stream inlet pressures were set at 100 psia .

## Notations

$A \quad$ Heat-transfer surface area
$A_{C} \quad$ Calculated heat-transfer surface area based on clean overall heat-transfer coefficient
$A_{f} \quad$ Flow area
$A_{\text {fins }} \quad 2 n_{t} N_{f} b_{c} L=$ Surface area of all fins in a finned-pipe heat exchanger
$A_{i} \quad \pi D_{i} L=$ Internal surface area of inner pipe in a double-pipe heat exchanger
$A_{\text {prime }}$ Prime surface area in a finned-pipe heat exchanger
$A_{t o t} \quad A_{\text {prime }}+A_{\text {fins }}=$ Total heat-transfer surface area in a finned-pipe heat exchanger
$b \quad$ Fin height
$b_{c} \quad b+\tau / 2=$ Corrected fin height
$C_{c}, C_{h} \quad$ Value of $\dot{m} C_{P}$ for cold and hot streams, respectively
$C_{P} \quad$ Heat capacity at constant pressure
$D \quad$ Diameter
$D_{e} \quad$ Equivalent diameter
$D_{i} \quad$ Internal diameter of inner pipe in a double-pipe heat exchanger
$D_{o} \quad$ External diameter of inner pipe in a double-pipe heat exchanger
$D_{1} \quad$ External diameter of inner pipe in an annulus
$D_{2} \quad$ Internal diameter of outer pipe in an annulus
$F \quad$ LMTD correction factor for series-parallel arrangement of hairpins
$f$ Darcy friction factor
$G \quad \dot{m} / A_{f}=$ Mass flux
$G_{n} \quad$ Mass flux in a nozzle
$g$ Gravitational acceleration
$g_{c} \quad$ Unit conversion factor $=32.174 \frac{\mathrm{lbm} \cdot \mathrm{ft} / \mathrm{s}^{2}}{\mathrm{lbf}}=1.0 \frac{\mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}}{\mathrm{~N}}$
$h \quad$ Heat-transfer coefficient
$h_{i} \quad$ Heat-transfer coefficient for inner pipe in a double-pipe heat exchanger
$h_{o} \quad$ Heat-transfer coefficient for annulus in a double-pipe heat exchanger
$h_{o}^{\prime} \quad\left(h_{o}+R_{D o}\right)^{-1}$
$j_{H} \quad\left(h_{o} D_{e} / k\right) \times \operatorname{Pr}^{-1 / 3}\left(\mu / \mu_{w}\right)^{-0.14}=$ Modified Colburn factor for heat transfer in the annulus of a double-pipe heat exchanger
$k \quad$ Thermal conductivity
$L \quad$ Pipe length
$m \quad\left(2 h_{o} / k \tau\right)^{1 / 2}=$ Fin parameter
$\dot{m} \quad$ Mass flow rate
$N_{f} \quad$ Number of fins on a finned pipe
$N_{H P} \quad$ Number of hairpins connected in series
$N u \quad$ Nusselt Number
$n_{t} \quad$ Number of tubes in a multi-tube hairpin heat exchanger
$P \quad$ Pressure; parameter used to calculate LMTD correction factor
$\operatorname{Pr} \quad$ Prandtl number
$q \quad$ Rate of heat transfer
$q_{\text {Tot }} \quad$ Total duty for a heat exchanger
$R \quad$ Parameter used to calculate LMTD correction factor
$R_{D i} \quad$ Fouling factor for fluid in the inner pipe of a double-pipe heat exchanger
$R_{D o} \quad$ Fouling factor for fluid in the annulus of a double-pipe heat exchanger
Re Reynolds number
$R e_{i} \quad$ Reynolds number for fluid in the inner pipe of a double-pipe heat exchanger
$R e_{o} \quad$ Reynolds number for fluid in the annulus of a double-pipe heat exchanger
$R_{t h} \quad$ Thermal resistance
$s \quad$ Specific gravity
$T$ Temperature
$T_{a} \quad$ Inlet temperature of series stream for series-parallel configuration of hairpins
$T_{\text {ave }} \quad$ Average temperature of fluid in the annulus of a double-pipe heat exchanger
$T_{b} \quad$ Outlet temperature of series stream for series-parallel configuration of hairpins
$T_{c} \quad$ Temperature of cold stream
$T_{h} \quad$ Temperature of hot stream
$T_{p} \quad$ Average temperature of prime surface in a finned-pipe heat exchanger
$T_{w} \quad$ Average pipe wall temperature in an un-finned heat exchanger
$T_{w t d} \quad$ Weighted average temperature of finned surface in a finned-pipe heat exchanger
$t_{a} \quad$ Inlet temperature of parallel stream in a series-parallel configuration of hairpins
$t_{\text {ave }}$ Average temperature of fluid in the inner pipe of a double-pipe heat exchanger
$t_{b}$ Outlet temperature of parallel stream in a series-parallel configuration of hairpins
$U_{C} \quad$ Clean overall heat-transfer coefficient
$U_{D} \quad$ Design overall heat-transfer coefficient
$V \quad$ Average fluid velocity
$x \quad$ Number of parallel branches in a series-parallel configuration of hairpins

## Greek Letters

$\alpha \quad$ Parameter in exponential relationship for temperature dependence of liquid viscosity
$\beta \quad$ Parameter in exponential relationship for temperature dependence of liquid viscosity
$\Delta P \quad$ Pressure drop
$\Delta P_{f} \quad$ Pressure drop due to fluid friction in straight sections of pipe
$\Delta P_{f, i} \quad$ Frictional pressure drop in straight sections of inner pipe
$\Delta P_{f, o} \quad$ Frictional pressure drop in straight sections of annulus
$\Delta P_{i} \quad$ Total pressure drop for fluid flowing through inner pipe of double-pipe heat exchanger
$\Delta P_{n} \quad$ Pressure loss in nozzles
$\Delta P_{o} \quad$ Total pressure drop for fluid flowing through annulus of double-pipe heat exchanger
$\Delta P_{r} \quad$ Pressure loss in return bends of double-pipe heat exchanger
$\Delta T_{\ln } \quad$ Logarithmic mean temperature difference
$\eta_{f} \quad$ Fin efficiency
$\eta_{w} \quad$ Weighted efficiency of finned surface
$\kappa \quad D_{2} / D_{1}=$ Diameter ratio for annulus
$\mu \quad$ Viscosity
$\mu_{w} \quad$ Fluid viscosity evaluated at average temperature of pipe wall
$\rho \quad$ Fluid density
$\tau \quad$ Fin thickness
$\phi \quad$ Viscosity correction factor
$\phi_{i} \quad$ Viscosity correction factor for fluid in the inner pipe of a double-pipe heat exchanger
$\phi_{0} \quad$ Viscosity correction factor for fluid in the annulus of a double-pipe heat exchanger

## Problems

(4.1) In Example 4.1, repeat Steps (d)-(j) of the first trial using Equation (2.38) to calculate both $h_{i}$ and $h_{0}$. The correction for short pipes can be neglected, i.e., $1+(D / L)^{2 / 3} \cong 1.0$. Compared with Example 4.1, what are the percentage differences in the values of $h_{i}$ and $h_{0}$ ? Which procedure is more conservative for design purposes?
(4.2) A double-pipe heat exchanger consists of five hairpins connected in series. The hairpins are each $20-\mathrm{ft}$ long with $4-\mathrm{in}$. schedule 40 outer pipes, 2 -in. schedule 40 inner pipes and internal return bends. Nozzles are made of 2 -in. schedule 40 pipe. $40,000 \mathrm{lb} / \mathrm{h}$ of a petroleum fraction having the properties given below will flow in the annulus.

| Petroleum fraction property | Value |
| :--- | :---: |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.15 |
| $\mu(\mathrm{cp})$ | 2.0 |
| $s$ | 0.80 |
| $\operatorname{Pr}$ | 17.75 |

(a) Calculate the heat-transfer coefficient, $h_{o}$, for the annulus.
(b) Calculate the total pressure drop, $\Delta P_{o}$, for the annulus.
(c) What percentage of the total pressure loss occurs in the nozzles?
(d) If schedule 40 pipe is used, what size nozzles would be required to keep the pressure drop below 7 psi?
Ans. (a) $179 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. $\quad$ (b) 8.9 psi . $\quad$ (c) $41 \%$. (d) 3 -in. nozzles.
(4.3) A fluid with $k=0.173 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$ and $\operatorname{Pr}=6$ flows in a finned annulus having the following configuration:

| Length $=6.1 \mathrm{~m}$ | Number of fins $=48$ |
| :--- | :--- |
| Outer pipe ID $=102.26 \mathrm{~mm}$ | Fin height $=12.7 \mathrm{~mm}$ |
| Inner pipe OD $=73 \mathrm{~mm}$ | Fin thickness $=0.889 \mathrm{~mm}$ |

Calculate the heat-transfer coefficient and (Darcy) friction factor for a Reynolds number of: (a) 100 .
(b) 1000 .

Ans. (a) $h=45 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} ; f=0.64$. (b) $h=146 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} ; f=0.085$.
(4.4) The petroleum fraction of Example 4.2 flows at a rate of $1200 \mathrm{lb} / \mathrm{h}$ in the annulus of a $4-\mathrm{in}$. multi-tube hairpin exchanger having seven tubes, each with 20 fins. The fin thickness is 0.035 in . and the hairpin length is 15 ft . Other pipe and fin dimensions are given in Table 4.2.

Calculate the following:
(a) The flow area for the annulus.
(b) The equivalent diameter for the annulus.
(c) The Reynolds number for the oil.
(d) The heat-transfer coefficient for the oil.
(e) The friction factor for the oil.
(f) The friction loss per unit length in the annulus.

Ans. (a) $0.0521 \mathrm{ft}^{2}$. (b) 0.0276 ft . (c) 95.56 . (d) $11.9 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$.
(e) 0.670 (f) $0.0021 \mathrm{psi} / \mathrm{ft}$.
(4.5) A double-pipe heat exchanger consists of two hairpins connected in series. Each hairpin is 20 ft long with the following configuration:

Outer pipe: 4-in. schedule 40
Inner pipe: 2 -in. schedule 40 with 36 fins
Fin height: 0.75 in .
Fin thickness: 0.035 in.
Nozzles: 2-in. schedule 40
Return bends: Internal
The petroleum fraction of Problem 4.2 will flow in the annulus at a rate of $20,000 \mathrm{lb} / \mathrm{h}$.
(a) Calculate the heat-transfer coefficient, $h_{0}$, for the annulus.
(b) Calculate the total pressure drop, $\Delta P_{o}$, for the annulus.

Ans. (a) $94 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (b) 3.6 psi .
(4.6) An oil cooler will consist of three finned-pipe hairpins connected in series. The hairpins have the following dimensions:

Length of one hairpin: 20 ft
Outer pipe: 2-in. schedule 10
Inner pipe: $3 / 4$-in. schedule 40 with 30 fins
Fin height: 0.5 in .

Fin thickness: 0.035 in.
Nozzles: 1-in. schedule 40
Return bends: Internal
$12,000 \mathrm{lb} / \mathrm{h}$ of oil $\left(\rho=55.2 \mathrm{lbm} / \mathrm{ft}^{3}, \mu=7.5 \mathrm{cp}\right)$ will flow in the annulus. The maximum allowable pressure drop for the oil is 20 psi . Will the actual pressure drop be acceptable?
(4.7) An alternate design for the oil cooler of Problem 4.6 consists of two hairpins connected in series, each hairpin being 15 ft long. The outer pipes are 4 -in. schedule 10 , and each outer pipe contains two $3 / 4-\mathrm{in}$. schedule 40 pipes with fins as described in Problem 4.6. Nozzles and return bends are the same as in Problem 4.6. Will the oil pressure drop be acceptable for this configuration?
(4.8) A hot stream is to be cooled from $300^{\circ} \mathrm{F}$ to $275^{\circ} \mathrm{F}$ in a double-pipe heat exchanger by heating a cold stream from $100^{\circ} \mathrm{F}$ to $290^{\circ} \mathrm{F}$. In order to control pressure drops, the heat exchanger will be comprised of three parallel banks of hairpins with the hot stream flowing in series and the cold stream divided into three parallel branches. Calculate the mean temperature difference for the heat exchanger.
Ans. $37.6^{\circ} \mathrm{F}$.
(4.9) $72,500 \mathrm{lb} / \mathrm{h}$ of oil ( $s=0.75, \mu=0.83 \mathrm{cp}$ ) will be cooled using a double-pipe heat exchanger consisting of eight hairpins. Each hairpin is 20 ft long with $3.5-\mathrm{in}$. schedule 40 outer pipe, 2 -in. schedule 40 un-finned inner pipe, 2 -in. schedule 40 nozzles and internal return bend. The maximum allowable pressure drop for the oil is 8 psi . Determine whether the pressure drop will be acceptable if:
(a) The oil flows through the inner pipes, which are connected in two parallel banks of four hairpins each.
(b) The oil flows through the annuli, which are connected in two parallel banks of four hairpins each.
$50,000 \mathrm{lb} / \mathrm{h}$ of a fluid having a density of $53 \mathrm{lbm} / \mathrm{ft}^{3}$ and a viscosity of 1.5 cp will flow in the annulus of a double-pipe heat exchanger. The hairpins are 30 ft long with 3 -in. schedule 40 outer pipe, $1.5-\mathrm{in}$. schedule 40 inner pipe, internal return bends and $1.5-\mathrm{in}$. schedule 40 nozzles. A total of six hairpins will be used, and the maximum allowable pressure drop for the stream is 12 psi . Determine which of the following configurations should be used in connecting the annuli of the hairpins:

- Six hairpins in series
- Two parallel banks of three hairpins each
- Three parallel banks of two hairpins each
(4.11) In designing a double-pipe heat exchanger for a particular service it is found that the pressure drop for the stream flowing through the inner pipe is excessively high ( 35 psi ) compared with the allowable pressure drop ( 7 psi ). It is decided to remedy the problem by using a series-parallel configuration of hairpins. Assuming the same size and number of hairpins are used, how many parallel branches should the stream be divided into if:
(a) The flow is turbulent?
(b) The flow is laminar?
(4.12) $15,000 \mathrm{lb} / \mathrm{h}$ of benzene will be heated from $80^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$ by cooling a stream of orthotoluidine $\left(\mathrm{C}_{7} \mathrm{H}_{9} \mathrm{~N}\right)$ from $160^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$. Inlet pressures are 40 psia for ortho-toluidine and 50 psia for benzene. A maximum pressure drop of 15 psia is specified for each stream. A number of used carbon steel hairpins are available for this service. The hairpins are each 20 ft long with 3 -in. schedule 40 outer pipe, 1.5 -in. un-finned schedule 40 inner pipe, internal return bends and 2-in. schedule 40 nozzles. Properties of ortho-toluidine at $130^{\circ} \mathrm{F}$
are given below. Determine the number and configuration of hairpins required for this service.

| Ortho-toluidine property | Value at $130^{\circ} \mathrm{F}$ |
| :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.48 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.081 |
| $\mu(\mathrm{cp})$ | $1.85^{\star}$ |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 60.5 |
| $\operatorname{Pr}$ | 26.5 |
| ${ }^{*} \log _{10} \mu(\mathrm{cp})=1085.1\left(\frac{1}{T(\mathrm{~K})}-\frac{1}{356.46}\right)$. |  |

(4.13) $92,500 \mathrm{lb} / \mathrm{h}$ of oil will be cooled from $230^{\circ} \mathrm{F}$ to $200^{\circ} \mathrm{F}$ by heating a process water stream from $60^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$ in a stainless steel $\left(k=9.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ double-pipe heat exchanger. The hairpins to be used are each 20 ft long with 3.5 -in. schedule 40 outer pipe, 2 -in. schedule 40 un-finned inner pipe, 2 -in. schedule 40 nozzles and internal return bend. Maximum allowable pressure drops are 8 psi for the oil and 15 psi for the water. Inlet pressures are 50 psia for the oil and 60 psia for the water. Fouling factors of 0.002 and $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} . \circ \mathrm{F} / \mathrm{Btu}$ are required for the oil and water streams, respectively. Properties of the oil may be assumed constant at the values given below. Determine the number and configuration of hairpins to be used for this service.

| Oil property | Value |
| :--- | :---: |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.59 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.073 |
| $\mu(\mathrm{cp})$ | 0.83 |
| $s$ | 0.76 |
| $P r$ | 16.2 |

(4.14) An alternative design for the heat exchanger of Problem 4.13 is to be developed that utilizes finned hairpins. The hairpin dimensions are the same as in Problem 4.13 except that each inner pipe contains 24 fins of height 0.5 in . and thickness 0.035 in . Determine the number and configuration of hairpins to be used in this case.
(4.15) Use HEXTRAN or other suitable software to solve Problem 4.12.
(4.16) Use HEXTRAN or other suitable software to solve Problem 4.13.
(4.17) Use HEXTRAN, TASC or other suitable software to solve Problem 4.14.
(4.18) $30,000 \mathrm{lb} / \mathrm{h}$ of kerosene will be heated from $75^{\circ} \mathrm{F}$ to $110^{\circ} \mathrm{F}$ by cooling a gasoline stream from $160^{\circ} \mathrm{F}$ to $135^{\circ} \mathrm{F}$. For each stream the inlet pressure is 50 psia and a maximum pressure drop of 10 psi is specified. Published fouling factors for oil refinery streams should be used for this application. Use HEXTRAN, TASC, or other suitable software to design a double-pipe heat exchanger for this service.

Note: To begin, try using 3-in. by $1.5-\mathrm{in}$. schedule 40 hairpins. The dimensions of the hairpins may be changed as necessary during the design process. However, only standard sizes should be used.

| Property | Gasoline | Kerosene |
| :--- | :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.55 | 0.48 |
| $k(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot \mathrm{F})$ | 0.087 | 0.081 |
| $\mu(\mathrm{cp})$ | 0.42 | 1.60 |
| $s$ | 0.74 | 0.82 |
| $P r$ | 6.42 | 22.9 |

(4.19) $40,000 \mathrm{lb} / \mathrm{h}$ of a hydrocarbon liquid ( $30^{\circ} \mathrm{API}, K_{w}=11.5$ ) are to be cooled from $225^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ using water available from a municipal water system at $70^{\circ} \mathrm{F}$ and 65 psia . The inlet pressure of the hydrocarbon is 50 psia and a fouling factor of $0.0025 \mathrm{~h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for this stream. The maximum pressure drop for each stream is 10 psi . Carbon steel is acceptable for this application. Use HEXTRAN or other suitable software to design an un-finned hairpin heat exchanger for this service.
(4.20) Use HEXTRAN or other suitable software to design a finned-pipe hairpin heat exchanger for the service of Problem 4.19.
(4.21) $20,000 \mathrm{lb} / \mathrm{h}$ of lube oil $\left(26^{\circ} \mathrm{API}, K_{w}=12.2\right)$ will be cooled from $430^{\circ} \mathrm{F}$ to $350^{\circ} \mathrm{F}$ by heating a light gas oil ( $33^{\circ} \mathrm{API}, K_{w}=11.8$ ) from $310^{\circ} \mathrm{F}$ to $370^{\circ} \mathrm{F}$. The inlet pressure of each stream will be 50 psia and maximum pressure drops of 15 psi for the lube oil and 10 psi for the gas oil are specified. Design a double pipe heat exchanger for this service using:
(a) HEXTRAN.
(b) TASC with average stream properties generated by HEXTRAN or other software.
(4.22) $\quad 13,000 \mathrm{lb} / \mathrm{h}$ of amyl acetate ( $n$-pentyl acetate, $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ ) will be cooled from $150^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$ using $12,000 \mathrm{lb} / \mathrm{h}$ of amyl alcohol (l-pentanol, $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}$ ) which is available at $75^{\circ} \mathrm{F}$. Inlet pressures are 45 psia for the acetate and 55 psia for the alcohol. A maximum pressure drop of 10 psi is specified for each stream. Use HEXTRAN, TASC or other suitable software to design a double-pipe heat exchanger for this service.
(4.23) Use HEXTRAN, TASC, and/or other available software to rate the finned-pipe heat exchanger designed by hand in Example 4.2. Compare the results from the computer solution(s) with those from the hand calculations of Example 4.2.
(4.24) As noted in Example 4.3, HEXTRAN uses linear interpolation to compute heat-transfer coefficients in the transition region. This method yields reasonable results and has the additional advantage that the calculated coefficient is a continuous function of Reynolds number over all flow regimes. For the initial configuration in Example 4.1 (hairpins connected in series, aniline in annulus), use this method to calculate $h_{o}$ by proceeding as follows:
(a) Use Equation (2.41) to calculate the heat-transfer coefficient for the annulus at $R e=2000$. As noted in Example 3.3, the length, $L$, for the annulus should be taken as the length of pipe in one leg of one hairpin, or 16 ft in this case.
(b) Use the Seider-Tate correlation for turbulent flow to calculate the heat-transfer coefficient for the annulus at $R e=10,000$.
(c) Use linear interpolation between the values calculated in parts (a) and (b) to obtain the heat-transfer coefficient at the actual Reynolds number of 8218. Compare your result with the value of $248.7 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ obtained from HEXTRAN in Example 4.3.

## DESIGN OF SHELL-AND-TUBE HEAT EXCHANGERS

## Contents

### 5.1 Introduction <br> 188

5.2 Heat-Transfer Coefficients 188
5.3 Hydraulic Calculations 189
5.4 Finned Tubing 192
5.5 Tube-Count Tables 194
5.6 Factors Affecting Pressure Drop 195
5.7 Design Guidelines 197
5.8 Design Strategy 201
5.9 Computer Software 218

### 5.1 Introduction

Preliminary design- and thermal-rating calculations for shell-and-tube exchangers were presented in Chapter 3. Both are used, along with hydraulic calculations, in the complete design of shell-and-tube exchangers. As with double-pipe units, these exchangers are typically designed with specified pressure-drop constraints on the two streams. Due to the greater complexity and variety of shell-and-tube configurations, however, there are more design variables that must be taken into consideration. This complexity is also the source of computational difficulties on the shell side, which were alluded to in Chapter 3. The upshot is that design of shell-and-tube equipment is considerably more complicated than design of double-pipe exchangers.

In this chapter, the key aspects of shell-and-tube exchanger design are presented and illustrated with examples involving both plain and finned tubing. The Simplified Delaware method is used for shell-side calculations in order to keep the computations manageable. More sophisticated computational methods are considered separately in subsequent chapters.

### 5.2 Heat-Transfer Coefficients

The heat-transfer correlations used in this chapter were presented in Section 2.4, Section 3.8, and Section 4.2. They are repeated here for convenience.

For the tube-side heat-transfer coefficient, $h_{i}$, the Seider-Tate and Hausen equations are used as follows.

For $R e \geq 10^{4}$,

$$
\begin{equation*}
N u=0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \tag{4.1}
\end{equation*}
$$

For $2100<R e<10^{4}$,

$$
\begin{equation*}
N u=0.116\left[\operatorname{Re}^{2 / 3}-125\right] \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14}\left[1+(D / L)^{2 / 3}\right] \tag{2.37}
\end{equation*}
$$

For $R e \leq 2100$,

$$
\begin{equation*}
N u=1.86[\operatorname{RePr} D / L]^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \tag{2.36}
\end{equation*}
$$

Alternatively, Equation (2.38) may be used for the turbulent and transition regions. The Reynolds number in these correlations is calculated using the mass flow rate per tube:

$$
\begin{equation*}
\dot{m}_{\text {per tube }}=\frac{\dot{m}_{t} n_{p}}{n_{t}} \tag{3.19}
\end{equation*}
$$

where
$\dot{m}_{t}=$ total mass flow rate of tube-side fluid
$n_{p}=$ number of tube-side passes
$n_{t}=$ number of tubes
The shell-side heat-transfer coefficient, $h_{o}$, is computed using the following curve fit to Figure 3.12 (note that $j_{H}$ is dimensionless):

$$
\begin{equation*}
j_{H}=0.5\left(1+B / d_{S}\right)\left(0.08 R e^{0.6821}+0.7 R e^{0.1772}\right) \tag{3.21}
\end{equation*}
$$

where
$j_{H} \equiv\left(h_{o} D_{e} / k\right)\left(C_{P} \mu / k\right)^{-1 / 3}\left(\mu / \mu_{w}\right)^{-0.14}$
$B=$ baffle spacing
$d_{s}=$ shell ID
$D_{e}=$ equivalent diameter, in proper units, from Figure 3.12

The Reynolds number in Equation (3.21) is calculated using the equivalent diameter and flow area given in Figure 3.12. The correlation is valid for tube bundles employing plain or finned heatexchanger tubing, $20 \%$ cut segmental baffles, and one pair of sealing strips per 10 tube rows. It is also based on TEMA standards for tube-to-baffle and baffle-to-shell clearances. (See Section 6.7 for details regarding clearances.) Although the correlation was derived from results of the Delaware study, it contains a built-in safety factor of approximately $25 \%$ [1]. Therefore, it should generally yield lower values of the heat-transfer coefficient than the Delaware method itself.

### 5.3 Hydraulic Calculations

### 5.3.1 Tube-side pressure drop

The pressure drop due to fluid friction in the tubes is given by Equation (4.5) with the length of the flow path set to the tube length times the number of tube passes. Thus,

$$
\begin{equation*}
\Delta P_{f}=\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi} \tag{5.1}
\end{equation*}
$$

where
$f=$ Darcy friction factor (dimensionless)
$L=$ tube length (ft)
$G=$ mass flux $\left(\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}\right)$
$D_{i}=$ tube ID (ft)
$s=$ fluid specific gravity (dimensionless)
$\phi=$ viscosity correction factor (dimensionless)
$=\left(\mu / \mu_{w}\right)^{0.14}$ for turbulent flow
$=\left(\mu / \mu_{w}\right)^{0.25}$ for laminar flow
Here, $\Delta P_{f} \propto$ psi. (English units are used throughout this section; see Appendix 5.A for the hydraulic equations in terms of SI units.) For laminar flow, the friction factor is given by:

$$
\begin{equation*}
f=\frac{64}{R e} \tag{4.6}
\end{equation*}
$$

For turbulent flow in commercial heat-exchanger tubes, the following equation can be used for $R e \geq 3000$ :

$$
\begin{equation*}
f=0.4137 R e^{-0.2585} \tag{5.2}
\end{equation*}
$$

(Note the similarity between this equation and Equation (4.8) for commercial pipe. The surface roughness tends to be lower for heat-exchanger tubes than for pipes, resulting in somewhat smaller friction factors for tubing.)

The tube-side fluid experiences a sudden contraction when it enters the tubes from the header and a sudden expansion when it exits the tubes at the opposite header. The associated pressure losses can be calculated using standard hydraulic formulas [2], and depend on the tube diameter, pitch and layout. However, for commonly used tube configurations, the sum of the entrance and exit losses can be approximated by 0.5 tube velocity heads in turbulent flow [2]. For laminar flow the number of velocity heads depends on the Reynolds number, but for $R e \geq 500$ a reasonable approximation is one velocity head for the entrance loss and $3 / 4$ velocity head for the exit loss, giving a total of 1.75 velocity heads.

In the return header, the fluid experiences a $180^{\circ}$ change of direction. Henry [2] has suggested an allowance of 1.5 velocity heads for the associated pressure loss, similar to that for a pipe bend. Since the flow pattern in the header is complex regardless of whether the flow in the tubes is laminar or turbulent, this allowance is probably reasonable for both flow regimes.

Combining the tube entrance, tube exit, and return losses gives an allowance for minor losses of ( $2 n_{p}-1.5$ ) velocity heads for turbulent flow and ( $3.25 n_{p}-1.5$ ) velocity heads for laminar flow and $R e \geq 500$. (Note that the first pass involves only tube entrance and exit losses, and not a return loss.)

For exchangers employing U-tubes, the situation is somewhat different because the tube entrance and exit losses occur on alternate passes rather than on each pass. Furthermore, on even-numbered passes, the return header is replaced by a $180^{\circ}$ bend in the tubing. The pressure loss associated with the latter can be treated the same as in a double-pipe exchanger by allowing 1.2 velocity heads for turbulent flow and 1.5 velocity heads for laminar flow with $R e \geq 500$. This results in a minor loss allowance of (1.6 $n_{p}-1.5$ ) velocity heads for turbulent flow and ( $2.38 n_{p}-1.5$ ) velocity heads for laminar flow with $R e \geq 500$.

The rather untidy situation regarding minor losses is summarized in Table 5.1. These values can be compared with allowances reported elsewhere. The shell-and-tube module in the HEXTRAN software package uses two velocity heads per pass for the tube side minor losses, which agrees (except for the first pass) with the tabled value for turbulent flow and regular tubes. Bell and Mueller [3] recommend an allowance of three velocity heads per pass. Kern [4] stated without documentation that an allowance of four velocity heads per pass was appropriate for these losses, and this value has often been cited by others, e.g., Ref. [1, 5]. Although Table 5.1 indicates that Kern's allowance is conservative enough to cover nearly all situations, it appears to be excessive for turbulent flow.

Equation (4.11) gives the pressure drop associated with one velocity head. If we denote by $\alpha_{r}$ the number of velocity heads allocated for minor losses, then we obtain the following equation:

$$
\begin{equation*}
\Delta P_{r}=1.334 \times 10^{-13} \alpha_{r} G^{2} / s \tag{5.3}
\end{equation*}
$$

where $\alpha_{r}$ is obtained from Table 5.1. Alternatively, $\alpha_{r}$ may be selected in accordance with one of the other recommendations (Kern, Bell and Mueller, or HEXTRAN) cited above.

Each shell in a shell-and-tube exchanger contains an inlet and an outlet nozzle for the tube-side fluid. The nozzle pressure drop can be estimated in the same manner as was done for double-pipe exchangers in Chapter 4. In particular, Equations (4.14) and (4.15) are applicable if the number of hairpins is replaced by the number of shells. Thus,

$$
\begin{array}{ll}
\Delta P_{n}=2.0 \times 10^{-13} N_{s} G_{n}^{2} / s & \text { (turbulent flow) } \\
\left.\Delta P_{n}=4.0 \times 10^{-13} N_{s} G_{n}^{2} / s \quad \text { (laminar flow, } R e_{n} \geq 100\right) \tag{5.5}
\end{array}
$$

where $G_{n}$ and $R e_{n}$ are the mass flux and Reynolds number, respectively, for the nozzles, and $N_{s}$ is the number of shells connected in series. These equations give the total pressure drop, in psi, for all the nozzles, assuming they are all the same. When the inlet and outlet nozzles differ significantly in size and/or flow regime, each nozzle can be treated individually as discussed in Section 4.3.

Table 5.1 Number of Velocity Heads Allocated for Minor Losses on Tube Side

| Flow regime | Regular tubes | U-tubes |
| :--- | :--- | :--- |
| Turbulent | $2 n_{p}-1.5$ | $1.6 n_{p}-1.5$ |
| Laminar, $R e \geq 500$ | $3.25 n_{p}-1.5$ | $2.38 n_{p}-1.5$ |

### 5.3.2 Shell-side pressure drop

In the Simplified Delaware method the shell-side pressure drop is computed using the following equation [1], which is similar to Equation (5.1):

$$
\begin{equation*}
\Delta P_{f}=\frac{f G^{2} d_{s}\left(n_{b}+1\right)}{7.50 \times 10^{12} d_{e} s \phi} \tag{5.6}
\end{equation*}
$$

where
$f=$ friction factor (dimensionless)
$G=$ mass flux $=\dot{m} / a_{s}\left(\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}\right)$
$a_{s}=$ flow area across tube bundle $\left(\mathrm{ft}^{2}\right)$
$=d_{s} C^{\prime} B /\left(144 P_{T}\right)$
$d_{s}=$ shell ID (in.)
$C^{\prime}=$ clearance (in.)
$B=$ baffle spacing (in.)
$P_{T}=$ tube pitch (in.); replaced by $P_{T} / \sqrt{2}$ for $45^{\circ}$ tube layout
$n_{b}=$ number of baffles
$d_{e}=$ equivalent diameter from Figure 3.12 (in.)
$s=$ fluid specific gravity
$\phi=$ viscosity correction factor $=\left(\mu / \mu_{w}\right)^{0.14}$
$\Delta P_{f}=$ pressure drop (psi)
The shell-side friction factor is given in Figure 5.1 in dimensional form. For use in Equation (5.6), values from this figure must be multiplied by the factor $144 \mathrm{in} .^{2} / \mathrm{ft}^{2}$, which is included in the following linear interpolation formula:

$$
\begin{equation*}
f=144\left\{f_{1}-1.25\left(1-B / d_{s}\right)\left(f_{1}-f_{2}\right)\right\} \tag{5.7}
\end{equation*}
$$



Figure 5.1 Shell-side friction factors (Source: Wolverine Tube, Inc. Originally published in Ref. [1]).
where
$f_{1}=$ friction factor from graph for $B / d_{s}=1.0$
$f_{2}=$ friction factor from graph for $B / d_{s}=0.2$
Approximate curve fits for $f_{1}$ and $f_{2}$ are as follows, with $d_{s}$ in inches.
For $R e \geq 1000$,

$$
\begin{align*}
& f_{1}=\left(0.0076+0.000166 d_{s}\right) R e^{-0.125} \quad\left(8 \leq d_{s} \leq 42\right)  \tag{5.8}\\
& f_{2}=\left(0.0016+5.8 \times 10^{-5} d_{s}\right) R e^{-0.157} \quad\left(8 \leq d_{s} \leq 23.25\right) \tag{5.9}
\end{align*}
$$

For $R e<1000$,

$$
\begin{align*}
& f_{1}=\exp \left[0.092(\ln R e)^{2}-1.48 \ln R e-0.000526 d_{s}^{2}+0.0478 d_{s}-0.338\right] \quad\left(8 \leq d_{s} \leq 42\right)  \tag{5.10}\\
& f_{2}=\exp \left[0.123(\ln R e)^{2}-1.78 \ln R e-0.00132 d_{s}^{2}+0.0678 d_{s}-1.34\right] \quad\left(8 \leq d_{s} \leq 23.25\right) \tag{5.11}
\end{align*}
$$

Note: In Equations (5.9) and (5.11), set $d_{s}=23.25$ for shell diameters greater than 23.25 in .
The pressure drop due to the shell-side nozzles can be estimated in the same manner as for the tube-side nozzles using Equations (5.4) and (5.5).

### 5.4 Finned Tubing

The finned tubing used in shell-and-tube heat exchangers is often referred to as radial low-fin tubing. It is made by an extrusion process in which the wall of a plain tube is depressed by stacks of disks. The undisturbed portion of the tube wall between the disks forms the fins. The fins are actually helical rather that radial, but they can be approximated as radial (annular) fins of rectangular profile for computational purposes. Low-fin tubing is made in a variety of alloys and configurations. The number of fins per inch of tube length ranges from 11 to 43 ; fin height varies from about 0.02 to 0.125 in ., and fin thickness ranges from 0.01 in . to about 0.015 in .

A diagram of a section of low-fin tubing is given in Figure 5.2. The part of the tube underneath the fins is called the root tube. The OD of the finned section is somewhat less than the diameter of the plain tube from which it was formed, so finned tubes are interchangeable with plain tubes in tube bundles. Both the ID and wall thickness of the finned section are less than those of the original tube. The ends of the tubes are left un-finned so that they can be rolled into the tubesheets. Dimensions of selected low-fin tubing from two manufacturers are given in Appendix B (Tables B.3-B.5).

Equation (2.27) can be used to calculate the fin efficiency. The equation is repeated here for convenience.

$$
\begin{gather*}
\eta_{f}=\frac{\tanh (m \psi)}{m \psi}  \tag{2.27}\\
\psi=\left(r_{2 c}-r_{1}\right)\left[1+0.35 \ln \left(r_{2 c} / r_{1}\right)\right] \tag{5.12}
\end{gather*}
$$

where
where
$m=\left(2 h_{o} / k \tau\right)^{1 / 2}$
$r_{1}=$ external radius of root tube
$r_{2}=$ outer radius of fin
$r_{2 c}=r_{2}+\tau / 2=$ corrected fin radius
$k=$ thermal conductivity of fin
$\tau=$ fin thickness
$h_{o}=$ shell-side heat-transfer coefficient


Figure 5.2 Schematic illustration of a radial low-fin tube (Source: Ref. [6]).

The wall temperature of a finned tube can be estimated in the same manner as that of a finned pipe in a double-pipe exchanger. Two temperatures, $T_{p}$ and $T_{w t d}$, are calculated using Equations (4.38) and (4.39), which are repeated here for convenience.

$$
\begin{gather*}
T_{p}=\frac{h_{i} t_{a v e}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right) T_{\text {ave }}}{h_{i}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right)}  \tag{4.38}\\
T_{w t d}=\frac{h_{i} \eta_{w} t_{\text {ave }}+\left[h_{i}\left(1-\eta_{w}\right)+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right)\right] T_{a v e}}{h_{i}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right)} \tag{4.39}
\end{gather*}
$$

In these equations,
$\eta_{w}=$ weighted fin efficiency
$t_{\text {ave }}=$ average temperature of tube-side fluid
$T_{\text {ave }}=$ average temperature of shell-side fluid
$A_{i}=$ interior surface area of tube
$A_{\text {Tot }}=$ exterior surface (prime + fins) area of tube
$T_{p}$ is an estimate of the average temperature of the prime surface, i.e., the root tube, and is used to calculate the viscosity correction factor, $\phi_{i}$, for the tube-side fluid. $T_{w t d}$ represents a weighted average of the extended and prime surface temperatures, and is used to calculate the viscosity correction factor, $\phi_{0}$, for the shell-side fluid.

For tubing with 16 or 19 fins per inch, the clearance, $C^{\prime}$, and the equivalent diameter, $D_{e}$ (or $d_{e}$ ), that are used to calculate the shell-side heat-transfer coefficient and pressure drop are given in Figure 3.12. For other configurations these parameters must be calculated. They are based on an effective root-tube diameter obtained by adding to the root tube a cylinder whose volume is equal to the total volume of the fins. The relevant equations are as follows:

$$
\begin{equation*}
\hat{D}_{r}=\left[D_{r}^{2}+4 n_{f} b \tau\left(D_{r}+b\right)\right]^{1 / 2} \tag{5.13}
\end{equation*}
$$

where
$\hat{D}_{r}=$ effective root tube diameter
$D_{r}=$ diameter of root tube
$n_{f}=$ number of fins per unit length of tube
$b=r_{2}-r_{1}=$ fin height

$$
\begin{gather*}
C^{\prime}=P_{T}-\hat{D}_{r}  \tag{5.14}\\
D_{e}=\frac{4 \beta P_{T}^{2}-\pi \hat{D}_{r}^{2}}{\pi \hat{D}_{r}} \tag{5.15}
\end{gather*}
$$

where
$\beta=1.0$ for square and rotated square pitch
$=0.86$ for triangular pitch
A final comment concerns the "low-fin limit" indicated on Figure 3.12 at a Reynolds number of 500. The explanation of this notation is as follows [1]:
"When a low shell-side Reynolds number is the result of a high mass velocity and high viscosity as opposed to a low mass velocity and low viscosity some caution is suggested. Lube-oil coolers with oil on the shell side and water on the tube side illustrate the point. Often there is no temperature control on the cooling water so that in the wintertime water much below design temperature may be circulated. It might reduce the temperature of the fins below the cloud point or pour point of the oil. This may cause a viscous, insulating mass to set up at the tube circumference. The temperature of the wall, $T_{f w}$, will always be higher than the temperature of a plain tube for the same process conditions and equivalent coefficients. This is inherent in the difference in outside-to-inside-surface ratios between low-fin and plain tubes. Nevertheless, the low-fin tube is slightly more disposed toward insulating itself with liquids having high viscosities. The caution is intended to make mandatory a check of the viscosity $\mu_{w}$ against operating water temperatures as opposed to design temperatures which may be considerably higher."

### 5.5 Tube-Count Tables

The number of tubes of a given size that can be accommodated in a given shell depends on many factors, including number of tube passes, tube pattern and pitch, baffle cut, number of sealing strips, head type, pressure rating, and tie-rod location [7]. The actual number of tubes contained in a given shell also varies somewhat from one manufacturer to another. Although it is impractical to account for all of these factors, tables of approximate tube counts are useful in the design process for estimating the required shell size.

A set of tube-count tables is given in Appendix C. The values listed in the tables represent the number of tube holes in each tubesheet, which is equal to the number of tubes in the case of regular
tubes. For U-tubes, however, the number of tube holes is twice the actual number of tubes. The tables are based on the following criteria [7]:

- Tubes have been eliminated to provide entrance area for a nozzle with a diameter equal to $0.2 d_{s}$.
- Tube layouts are symmetrical about both horizontal and vertical axes.
- The distance from tube exterior surface to the centerline of pass partitions is $5 / 16$ in for shells with ID less that 22 in ., and $3 / 8 \mathrm{in}$. for larger shells.


### 5.6 Factors Affecting Pressure Drop

An important aspect of heat-exchanger design is the control of pressure losses to stay within the specifications on the two streams while achieving good heat transfer. In this section we consider the design parameters that can be adjusted to control tube-side and shell-side pressure drop.

### 5.6.1 Tube-side pressure drop

The friction loss on the tube side is given by Equation (5.1), which shows that:

$$
\begin{equation*}
\Delta P_{f} \sim \frac{f n_{p} L G^{2}}{D_{i}} \tag{5.16}
\end{equation*}
$$

Furthermore, the mass flux, $G$, is the mass flow rate per tube $\left(\dot{m} n_{p} / n_{t}\right)$ divided by the flow area per tube ( $\pi D_{i}^{2} / 4$ ). Substituting yields:

$$
\begin{equation*}
\Delta P_{f} \sim \frac{f L n_{p}^{3}}{n_{t}^{2} D_{i}^{5}} \tag{5.17}
\end{equation*}
$$

The friction factor is inversely proportional to Reynolds number in laminar flow and proportional to the -0.2585 power of Reynolds number in turbulent flow according to Equations (4.6) and (5.2). Since:

$$
\begin{equation*}
R e=\frac{4 \dot{m}_{\text {per tube }}}{\pi D_{i} \mu} \sim \frac{n_{p}}{n_{t} D_{i}} \tag{5.18}
\end{equation*}
$$

proportionality (5.17) becomes:

$$
\begin{align*}
& \Delta P_{f} \sim \frac{L n_{p}^{2.74}}{n_{t}^{1.74} D_{i}^{4.74} \quad \text { (turbulent flow) }}  \tag{5.19}\\
& \Delta p_{f} \sim \frac{L n_{p}^{2}}{n_{\mathrm{t}} D_{i}^{4}} \quad \text { (laminar flow) } \tag{5.20}
\end{align*}
$$

Now for a given amount of heat-transfer surface and a specified tube BWG,

$$
\begin{equation*}
A_{i}=n_{t} \pi D_{i} L=\mathrm{constant} \tag{5.21}
\end{equation*}
$$

If the tube diameter is also specified, then $n_{t}$ is inversely proportional to the tube length, and proportionalities (5.19) and (5.20) become:

$$
\begin{align*}
\Delta P_{f} & \sim n_{p}^{2.74} L^{2.74} \quad \text { (turbulent flow) }  \tag{5.22}\\
\Delta P_{f} & \sim n_{p}^{2} L^{2} \quad \text { (laminar flow) } \tag{5.23}
\end{align*}
$$

Thus, regardless of flow regime, the pressure drop is a strong function of both the tube length and the number of tube passes.

### 5.6.2 Shell-side pressure drop

According to Equation (5.6), for the shell-side pressure drop:

$$
\begin{equation*}
\Delta P_{f} \sim \frac{f G^{2} d_{s}\left(n_{b}+1\right)}{d_{e}} \tag{5.24}
\end{equation*}
$$

The number of baffle spaces is approximately equal to the tube length divided by the baffle spacing in consistent units, i.e.,

$$
\begin{equation*}
n_{b}+1 \sim L / B \tag{5.25}
\end{equation*}
$$

Also,

$$
\begin{equation*}
G=\frac{\dot{m}}{a_{s}}=\frac{\dot{m}}{\left[\frac{d_{s} C^{\prime} B}{144 P_{T}}\right]} \sim \frac{P_{T}}{d_{s} C^{\prime} B}=\frac{P_{T}}{d_{s} B\left(P_{T}-D_{o}\right)} \tag{5.26}
\end{equation*}
$$

The equivalent diameter, $d_{e}$, depends on the tube size and pitch. For plain tubes, the relationship is given by Equation (5.15) with $\hat{D}_{r}$ replaced by the tube OD. For square pitch,

$$
\begin{equation*}
d_{e}=4\left(P_{T}^{2}-\pi D_{o}^{2} / 4\right) /\left(\pi D_{o}\right) \tag{5.27}
\end{equation*}
$$

Combining Equations (5.24) to (5.27) yields:

$$
\begin{equation*}
\Delta P_{f} \sim \frac{f L P_{T}^{2} D_{o}^{2}}{B^{3} d_{s}^{2}\left(P_{T}-D_{o}\right)^{2}\left(P_{T}^{2}-\pi D_{o}^{2} / 4\right)} \tag{5.28}
\end{equation*}
$$

For given tube and shell diameters, this relation simplifies to:

$$
\begin{equation*}
\Delta P_{f} \sim \frac{f L P_{T}^{2}}{B^{3}\left(P_{T}-D_{o}\right)^{2}\left(P_{T}^{2}-\pi D_{o}^{2} / 4\right)} \tag{5.29}
\end{equation*}
$$

Shell-side pressure drop is thus a strong function of the baffle spacing. Increasing $B$ increases the flow area across the tube bundle, which lowers the pressure drop. The dependence is not as strong as might be inferred from the above relationship because the friction factor increases with baffle spacing. The dependence of $f$ on $B$ is complex since $f$ increases directly with the ratio $B / d_{s}$ and indirectly through the Reynolds number. Nevertheless, the baffle spacing is the main design parameter for controlling shell-side pressure drop.

Increasing the tube pitch also increases the flow area through the tube bundle and thereby lowers the pressure drop. However, this tactic has the disadvantage of increasing the required shell size and, hence, the cost of the heat exchanger. Therefore, the tube pitch is generally not used to control pressure drop except in situations where no alternative is available.

Shell-side pressure drop also varies directly with the tube length. However, for a specified tube diameter and a given amount of heat-transfer surface, reducing the tube length increases the number of tubes in the bundle, which may require a larger shell. It also has a major impact on the tube-side pressure drop.

There are additional ways to control shell-side pressure drop that are not accounted for in the Simplified Delaware method. Increasing the baffle cut reduces the length of the cross-flow path through the bundle, which reduces the pressure drop. In practice, however, this parameter is highly correlated with the baffle spacing because an appropriate ratio of these parameters is necessary for good flow distribution in the shell. (With the Simplified Delaware method, the baffle cut is fixed at $20 \%$ and cannot be varied.) A similar effect can be achieved by using double- or triple-segmental


Figure 5.3 Baffle designs for reduced pressure drop (Source: Ref. [9]).
baffles as shown in Figure 5.3. Another option is to use helical baffles [8], which can significantly lower the pressure drop while still providing a relatively high shell-side heat-transfer coefficient (see also www.kochheattransfer.com).

More drastic measures for reducing the pressure drop include eliminating the tubes in the baffle windows (the baffle-cut areas) and using rod baffles (Figure 5.3). The no-tubes-in-window option requires a larger, more expensive shell for a given amount of heat-transfer surface. However, it reduces window pressure drop and permits a larger baffle spacing without excessive tube vibration because each tube is supported by every baffle. Support plates can be placed between baffles (Figure 5.3) for added stability, thereby minimizing tube vibration problems. Rod baffles provide support for the tubes but do not force the flow across the bundle. The flow is parallel to the tubes, which greatly reduces both the pressure drop and the heat-transfer coefficient. For applications requiring very low shell-side pressure drops, a divided flow (type J) shell can be used.

### 5.7 Design Guidelines

### 5.7.1 Fluid placement

Guidelines for fluid placement were given in Table 3.4. The most important considerations here are corrosion and fouling. Corrosive fluids should be placed on the tube side so that only the tubes, tubesheets, and (possibly) headers need to be made of corrosion-resistant alloy. Fluids that are heavy foulers should be placed on the tube side because it is (usually) easier to clean deposits from the interior surfaces of the tubes than from the exterior surfaces. Cooling water is usually placed in the tubes due to its tendency to corrode carbon steel and to form scale, which is difficult to remove from the exterior tube surfaces. Also, in services involving cooling water and an organic stream, finned tubes are frequently used to offset the low heat-transfer coefficient of the organic stream relative to the water. This requires the organic stream on the shell side in contact with the fins. Copper alloys such as Admiralty brass ( $71 \% \mathrm{Cu}, 28 \% \mathrm{Zn}, 1 \% \mathrm{Sn}$ ) are frequently used as corrosion-resistant tubing materials for water services.

Stream pressure is another factor that may influence the fluid placement. The reason is that it is generally less expensive to confine a high-pressure stream in the tubes rather than in the shell. Due to their small diameters, tubes of standard wall thickness can withstand quite high pressures, and only tube-side headers and nozzles normally require more robust construction.

### 5.7.2 Tubing selection

The most frequently used tube sizes are $3 / 4$ and 1 in . For water service, $3 / 4 \mathrm{in}$., 16 BWG tubes are recommended. For oil (liquid hydrocarbon) service, $3 / 4 \mathrm{in}$., 14 BWG tubes are recommended if the fluid is non-fouling, while $1 \mathrm{in} ., 14 \mathrm{BWG}$ tubes should be used for fouling fluids. Tube lengths typically range from 8 to 30 ft , and sometimes longer depending on the type of construction and the tubing material. A good value to start with is 16 or 20 ft .

### 5.7.3 Tube layout

Triangular and square layouts are the most common, but rotated square pitch is also used. A fourth configuration, rotated triangular pitch, is seldom used. With triangular pitch the tubes are more closely packed in the bundle, which translates to more heat-transfer surface in a given shell and somewhat higher pressure drop and heat-transfer coefficient. However, the clearance between tubes is typically the larger of 0.25 in . and $0.25 D_{o}$, and with triangular pitch this is not sufficient to allow cleaning lanes between the tube rows. Although chemical cleaning may be possible, triangular pitch is usually restricted to services with clean shell-side fluids. Rotated square pitch provides some enhancement in the heat-transfer coefficient (along with higher pressure drop) compared with square pitch, while still providing cleaning lanes between the tubes. This configuration is especially useful when the shell-side Reynolds number is relatively low (less than about 2000).
To summarize, the most commonly used tube layouts are either triangular or square, with a pitch of 1.0 in . (for $3 / 4-\mathrm{in}$. tubes) or 1.25 in . (for $1-\mathrm{in}$. tubes).

### 5.7.4 Tube passes

For typical low-viscosity process streams, it is highly desirable to maintain fully developed turbulent flow in the tubes. Although this may not be practical with high viscosity liquids, turbulent flow provides the most effective heat transfer. Once the tube size and number of tubes have been determined, the number of tube passes can be chosen to give an appropriate Reynolds number, i.e.,

$$
\begin{equation*}
R e=\frac{4 \dot{m} n_{p}}{\pi D_{i} n_{t} \mu} \geq 10^{4} \tag{5.27}
\end{equation*}
$$

Except for single-pass exchangers, an even number of tube passes is almost always used so that the tube-side fluid enters and exits at the same header. With U-tubes, this is the only feasible arrangement, and accommodating nozzles on internal (typeS or T) floating heads in order to provide an odd number of passes is very cumbersome.
Fluid velocity can also be used as a criterion for setting the number of tube-side passes. It is desirable to maintain the liquid velocity in the tubes in the range of about $3-8 \mathrm{ft} / \mathrm{s}$. Too low a velocity can cause excessive fouling, while a very high velocity can cause erosion of the tube wall. Some material-specific maximum velocities are given in Appendix 5.B. Harder tubing materials, such as steel, can withstand somewhat higher velocities than softer metals such as copper or aluminum, for example. Maximum vapor velocities are also given in Appendix 5.B.

### 5.7.5 Shell and head types

Shell and head types were presented in Figure 3.3. The single pass type E shell is standard. If multiple shell passes are required, as indicated by the logarithmic mean temperature difference(LMTD) correction factor, E shells can be connected in series. Alternatively, a two-pass type F shell can be used, although the longitudinal baffle may be subject to leakage. An F Shell can also be used with two tube passes to obtain the equivalent of a 1-1 (true counter flow) exchanger. The other shell types listed in Figure 3.3 are used for more specialized applications, including reboilers (G, H, K, X ) and units, such as condensers and gas coolers, that require low shell-side pressure drops ( $\mathrm{J}, \mathrm{X}$ ).
The most important consideration with respect to head type is fixed tubesheet versus floating head. A fixed-tubesheet design is cheaper and less prone to leakage. However, the tube bundle cannot be removed to clean the exterior surfaces of the tubes. Therefore, fixed-tubesheet exchangers
are usually restricted to services with clean shell-side fluids. Also, if the temperature difference between the two inlet streams is greater than about $100^{\circ} \mathrm{F}$, an expansion joint is required in the shell of a fixed-tubesheet exchanger to accommodate the differential thermal expansion between the tubes and shell. The added cost of the expansion joint largely offsets the cost advantage of the fixed-tubesheet design.

With floating-head and U-tube exchangers, the entire tube bundle can be pulled out of the shell from the front (stationary head) end. This allows mechanical cleaning of the exterior tube surfaces, usually by high-pressure jets of water, steam or supercritical carbon dioxide. (Of course, square or rotated square pitch must be used to provide cleaning lanes.) Also, since only one tubesheet is attached to the shell (at the front end), the tubes are free to expand or contract relative to the shell due to temperature differences.

Another consideration with respect to head type is bonnet versus channel. Bonnets are cheaper and less prone to leakage. However, to gain access to the tubesheet for inspecting or cleaning the tubes, the stationary head must be disconnected from the process piping and removed from the shell. With a channel-type head, access to the tubesheet is obtained simply by unbolting and removing the channel cover. Thus, a channel-type stationary head is preferable if the tubes will require frequent cleaning.

Other factors that may affect the choice of head type are given in Appendix 5.D. The most widely used floating-head design in the process industries is the AES exchanger. U-tube exchangers are less expensive and are also widely used. The advent of equipment for cleaning the interiors of U-tubes using high-pressure water jets has mitigated the problem of cleaning the return bends, leading to increased use of these exchangers [10].

### 5.7.6 Baffles and tubesheets

Single segmental baffles are standard and by far the most widely used. In order to provide good flow distribution on the shell side, the spacing between baffles should be between 0.2 and 1.0 shell diameters (but not less than 2 in.). However, the maximum baffle spacing may be limited by tube support and vibration considerations to less than one shell diameter [11,12] (see also Appendix 5.C). As previously noted, the no-tubes-in-window option can be used to extend the baffle spacing in these situations. For good flow distribution, the baffle cut should be between $15 \%$ and $45 \%$. For single-phase flow, however, a range of $20-35 \%$ is recommended [9]. With the Simplified Delaware method, the baffle cut is fixed at $20 \%$.

Although baffle spacing and baffle cut are ostensibly independent parameters, in practice they are highly correlated. Figure 5.4 shows the recommendations given by Taborek [11], who states: "A sound design should not deviate substantially from the recommended values, which are based on a vast amount of practical experience as well as on studies of the shell-side flow patterns." If the baffle cut is set at 20\% for the Simplified Delaware method, then Figure 5.4 indicates that the baffle spacing should be in the range of 0.2 to about 0.4 shell diameters for single-phase flow.

Baffle thickness is not required for the Simplified Delaware method, but it is used in the Stream Analysis method and in commercial computer programs. It varies from $1 / 16$ to $3 / 4$ in., and generally increases with shell size and baffle spacing. If this parameter is not specified as input, most computer programs will default to the standard values given in Table 5.2.

Tubesheet thickness is another parameter used in commercial computer programs. It varies from about 1 to 6 in., and generally increases with shell size and operating pressure. As a rough approximation, a value equal to the larger of 1 in . and 0.1 times the shell ID can be used [11]. Detailed methods for calculating required tubesheet thickness based on bending and shear stresses are given in Ref. [12].

### 5.7.7 Nozzles

Nozzles can be sized to meet pressure drop limitations and/or to match process piping. The guidelines given by Kern [4] and reproduced in Table 5.3 are useful as a starting point.

Other considerations in sizing nozzles are tube vibration and erosion. The fluid entering the shell through the inlet nozzle impinges directly on the tube bundle. If the inlet velocity is too high, excessive tube vibration and/or erosion may result. TEMA specifications to prevent tube erosion


Figure 5.4 Recommended baffle cut, $B_{c}$, as a function of baffle spacing. $S B C$, for single-phase flow; $C V$, for condensing vapors (Source: Ref. [11]).

Table 5.2 Standard Values (Inches) for Baffle Thickness in Class R Heat Exchangers*

|  | Baffle spacing, inches |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| Shell ID, inches | $\leq 24$ | $24-36$ | $36-48$ | $48-60$ | $>60$ |  |
| $8-14$ | 0.125 | 0.1875 | 0.250 | 0.375 | 0.375 |  |
| $15-28$ | 0.1875 | 0.250 | 0.375 | 0.375 | 0.500 |  |
| $29-38$ | 0.250 | 0.3125 | 0.375 | 0.500 | 0.625 |  |
| $39-60$ | 0.250 | 0.375 | 0.500 | 0.625 | 0.625 |  |
| $61-100$ | 0.375 | 0.500 | 0.625 | 0.750 | 0.750 |  |

[^0]Table 5.3 Guidelines for Sizing Nozzles

| Shell size, inches | Nominal nozzle diameter, inches |
| :--- | :---: |
| $4-10$ | 2 |
| $12-17.25$ | 3 |
| $19.25-21.25$ | 4 |
| $23-29$ | 6 |
| $31-37$ | 8 |
| $39-42$ | 10 |

are given in terms of the product of density $\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ and nozzle velocity $(\mathrm{ft} / \mathrm{s})$ squared [12]:

$$
\begin{aligned}
\rho V_{n}^{2} \leq & 1500 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~s}^{2} \quad \text { for non-abrasive single-phase fluids } \\
& \leq 500 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~s}^{2} \quad \text { for all other liquids, including bubble-point liquids }
\end{aligned}
$$

Beyond these limits (and for all other gases, including saturated vapors and vapor-liquid mixtures regardless of the $\rho V_{n}^{2}$ value) an impingement plate is required to protect the tubes. This is a metal plate, usually about $1 / 4$-in. thick, placed beneath the nozzle to deflect the fluid and keep it from impinging directly on the tubes. With impingement protection, values of $\rho V_{n}^{2}$ up to twice the above values are acceptable [11]. For still higher nozzle velocities (or in lieu of an impingement plate) an annular distributor can be used to distribute the fluid more evenly around the shell periphery and thereby reduce the impingement velocity [11]. An impingement plate may not be adequate to prevent tube vibration problems, and a larger nozzle or a distributor may be needed for this purpose as well. Furthermore, impingement plates actually reduce the bundle entrance area, and as a result, tubes near plate edges may be exposed to very high velocities that can cause them to fail. Thus, impingement plates can sometimes be counterproductive. An alternative that can be used to avoid this problem is to replace the first two rows of tubes with solid rods of diameter equal to the tube OD. The rods serve to protect the tubes without reducing the bundle entrance area.

### 5.7.8 Sealing strips

The purpose of sealing strips is to reduce the effect of the bundle bypass stream that flows around the outside of the tube bundle. They are usually thin strips of metal that fit into slots in the baffles and extend outward toward the shell wall to block the bypass flow and force it back into the tube bundle. They are placed in pairs on opposite sides of the baffles running lengthwise along the bundle. Sealing strips are mainly used in floating-head exchangers, where the clearance between the shell and tube bundle is relatively large. Typically, one pair is used for every four to ten rows of tubes between the baffle tips. Increasing the number of sealing strips tends to increase the shellside heat-transfer coefficient at the expense of a somewhat larger pressure drop. In the Simplified Delaware method, the number of sealing strips is set at one pair per ten tube rows.

### 5.8 Design Strategy

Shell-and-tube design is an inherently iterative process, the main steps of which can be summarized as follows:
(a) Obtain an initial configuration for the heat exchanger. This can be accomplished by using the preliminary design procedure given in Section 3.7 to estimate the required heat-transfer surface area, along with the design guidelines and tube-count tables discussed above to completely specify the configuration.
(b) Rate the design to determine if it is thermally and hydraulically suitable.
(c) Modify the design, if necessary, based on the results of the rating calculations.
(d) Go to step (b) and iterate until an acceptable design is obtained.

The design procedure is illustrated in the following examples.

## Example 5.1

A kerosene stream with a flow rate of $45,000 \mathrm{lb} / \mathrm{h}$ is to be cooled from $390^{\circ} \mathrm{F}$ to $250^{\circ} \mathrm{F}$ by heat exchange with $150,000 \mathrm{lb} / \mathrm{h}$ of crude oil at $100^{\circ} \mathrm{F}$. A maximum pressure drop of 15 psi has been specified for each stream. Prior experience with this particular oil indicates that it exhibits significant fouling tendencies, and a fouling factor of $0.003 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is recommended. Physical properties of the two streams are given in the table below. Design a shell-and-tube heat exchanger for this service.

| Fluid property | Kerosene | Crude oil |
| :--- | :--- | :---: |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.59 | 0.49 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.079 | 0.077 |
| $\mu(\mathrm{lbm} / \mathrm{ft} \cdot \mathrm{h})$ | 0.97 | 8.7 |
| Specific gravity | 0.785 | 0.85 |
| $P r$ | 7.24 | 55.36 |

## Solution

(a) Make initial specifications.
(i) Fluid placement

Kerosene is not corrosive, but crude oil may be, depending on salt and sulfur contents and temperature. At the low temperature of the oil stream in this application, however, corrosion should not be a problem provided the oil has been desalted (if necessary). Nevertheless, the crude oil should be placed in the tubes due to its relatively high fouling tendency. Also, the kerosene should be placed in the shell due to its large $\Delta T$ of $140^{\circ} \mathrm{F}$ according to the guidelines given in Table 3.4.
(ii) Shell and head types

The recommended fouling factor for kerosene is $0.001-0.003 \mathrm{~h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ (Table 3.3), indicating a significant fouling potential. Therefore, a floating-head exchanger is selected to permit mechanical cleaning of the exterior tube surfaces. Also, the floating tubesheet will allow for differential thermal expansion due to the large temperature difference between the two streams. Hence, a type AES exchanger is specified.
(iii) Tubing

Following the design guidelines for a fouling oil service, 1 in ., 14 BWG tubes are selected with a length of 20 ft .
(iv) Tube layout

Since cleaning of the tube exterior surfaces will be required, square pitch is specified to provide cleaning lanes through the tube bundle. Following the design guidelines, for 1 in . tubes a tube pitch of 1.25 in . is specified.
(v) Baffles

Segmental baffles with a $20 \%$ cut are required by the Simplified Delaware method, but this is a reasonable starting point in any case. In consideration of Figure 5.4, a baffle spacing of 0.3 shell diameters is chosen, i.e., $B / d_{s}=0.3$.
(vi) Sealing strips

One pair of sealing strips per 10 tube rows is specified in accordance with the requirements of the Simplified Delaware method and the design guidelines.
(vii) Construction materials

Since neither fluid is corrosive, plain carbon steel is specified for tubes, shell, and other components.
(b) Energy balances.

$$
\begin{aligned}
& q=\left(\dot{m} C_{P} \Delta T\right)_{\text {ker }}=45,000 \times 0.59 \times 140=3,717,000 \mathrm{Btu} / \mathrm{h} \\
& 3,717,000=\left(\dot{m} C_{P} \Delta T\right)_{\text {oil }}=150,000 \times 0.49 \times \Delta T_{\text {oil }} \\
& \Delta T_{\text {oil }}=50.6^{\circ} \mathrm{F} \\
& \text { outlet oil temperature }=150.6^{\circ} \mathrm{F} \\
& \text { (c) LMTD. }
\end{aligned}
$$

$$
\left(\Delta T_{\ln }\right)_{c f}=\frac{239.4-150}{\ln (239.4 / 150)}=191.2^{\circ} \mathrm{F}
$$

(d) LMTD correction factor.

$$
\begin{aligned}
& R=\frac{T_{a}-T_{b}}{t_{b}-t_{a}}=\frac{390-250}{150.6-100}=2.77 \\
& P=\frac{t_{b}-t_{a}}{T_{a}-t_{a}}=\frac{150.6-100}{390-100}=0.174
\end{aligned}
$$

From Figure 3.9 or Equation (3.15), for a 1-2 exchanger $F \cong 0.97$. Therefore, one shell pass is required.
(e) Estimate $U_{D}$.

In order to obtain an initial estimate for the size of the exchanger, an approximate value for the overall heat-transfer coefficient is used. From Table 3.5, for a kerosene/oil exchanger, it is found that $20 \leq U_{D} \leq 35 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. A value near the middle of the range is selected: $U_{D}=25 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(f) Calculate heat-transfer area and number of tubes.

$$
\begin{aligned}
A & =\frac{q}{U_{D} F\left(\Delta T_{\mathrm{ln}}\right)_{c f}}=\frac{3,717,000}{25 \times 0.97 \times 191.2} \\
A & =801.7 \mathrm{ft}^{2} \\
n_{t} & =\frac{A}{\pi D_{o} L}=\frac{801.7}{\pi \times(1 / 12) \times 20} \\
n_{t} & =153
\end{aligned}
$$

(g) Number of tube passes.

The number of tube passes is chosen to give fully developed turbulent flow in the tubes and a reasonable fluid velocity.

$$
\begin{aligned}
R e & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu} \\
D_{i} & =0.834 \mathrm{in} .=0.0695 \mathrm{ft} \quad(\text { Table B.1) } \\
R e & =\frac{4 \times 150,000\left(n_{p} / 153\right)}{\pi \times 0.0695 \times 8.7}=2064.5 n_{p}
\end{aligned}
$$

We want $R e \geq 10^{4}$ and an even number of passes. Therefore, take $n_{p}=6$.
Checking the fluid velocity,

$$
V=\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\rho \pi D_{i}^{2} / 4}=\frac{(150,000 / 3600)(6 / 153)}{0.85 \times 62.43 \pi(0.0695)^{2} / 4}=8.1 \mathrm{ft} / \mathrm{s}
$$

The velocity is at the high end of the recommended range, but still acceptable. Therefore, six tube passes will be used.
(h) Determine shell size and actual tube count.

From the tube-count table for 1 in. tubes on $11 / 4-\mathrm{in}$. square pitch (Table C.5), with six tube passes and a type $S$ head, the listing closest to 153 is 156 tubes in a $21 \frac{1}{4}-\mathrm{in}$. shell. Hence, the number of tubes is adjusted to $n_{t}=156$ and the shell ID is taken as $d_{s}=21.25 \mathrm{in}$.

This completes the initial design of the heat exchanger. The initial design must now be rated to determine whether it is adequate for the service. Since the temperature dependence of the
fluid properties is not available, they will be assumed constant; the viscosity correction factors will be set to unity and the tube wall temperature will not be calculated.
(i) Calculate the required overall coefficient.

$$
\begin{aligned}
U_{\text {req }} & =\frac{q}{n_{t} \pi D_{o} L F\left(\Delta T_{\ln }\right)_{c f}}=\frac{3,717,000}{156 \times \pi \times(1.0 / 12) \times 20 \times 0.97 \times 191.2} \\
U_{\text {req }} & =24.5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(j) Calculate $h_{i}$.

$$
\begin{aligned}
\operatorname{Re} & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 150,000(6 / 156)}{\pi \times 0.0695 \times 8.7}=12,149 \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =(0.077 / 0.0695) \times 0.023(12,149)^{0.8}(55.36)^{1 / 3}(1.0) \\
h_{i} & =180 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(k) Calculate $h_{o}$.

$$
\begin{aligned}
B & =0.3 d_{s}=0.3 \times 21.25=6.375 \mathrm{in} \\
a_{s} & =\frac{d_{s} C^{\prime} B}{144 P_{T}}=\frac{21.25 \times 0.25 \times 6.375}{144 \times 1.25}=0.188 \mathrm{ft}^{2} \\
G & =\dot{m} / a_{s}=45,000 / 0.188=239,362 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
D_{e} & =0.99 / 12=0.0825 \mathrm{ft}(\text { from Figure } 3.12) \\
R e & =D_{e} G / \mu=0.0825 \times 239,362 / 0.97=20,358
\end{aligned}
$$

Equation (3.21) is used to calculate the Colburn factor, $j_{H}$.

$$
\begin{aligned}
j_{H} & =0.5\left(1+B / d_{s}\right)\left(0.08 R e^{0.6821}+0.7 R e^{0.1772}\right) \\
& =0.5(1+0.3)\left[0.08(20,538)^{0.6821}+0.7(20,358)^{0.1772}\right] \\
j_{H} & =47.8 \\
h_{o} & =j_{H}\left(k / D_{e}\right) \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =47.8(0.079 / 0.0825)(7.24)^{1 / 3}(1.0) \\
h_{o} & =88.5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(l) Calculate the clean overall coefficient.

$$
\begin{aligned}
U_{C} & =\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k_{\text {tube }}}+\frac{1}{h_{o}}\right]^{-1} \\
& =\left[\frac{1.0}{180 \times 0.834}+\frac{(1.0 / 12) \ln (1.0 / .834)}{2 \times 26}+\frac{1}{88.5}\right]^{-1} \\
U_{C} & =54.8 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Since $U_{C}>U_{r e q}$, continue.
(m) Fouling factors

The fouling factor for the crude oil is specified as $0.003 h \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$, and from Table 3.3, a value of $0.002 h \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is taken for kerosene. Hence, the total fouling allowance is:

$$
R_{D}=\frac{R_{D i} D_{o}}{D_{i}}+R_{D o}=\frac{0.003 \times 1.0}{0.834}+0.002=0.0056 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
$$

(n) Calculate the design overall coefficient.

$$
U_{D}=\left(1 / U_{C}+R_{D}\right)^{-1}=(1 / 54.8+0.0056)^{-1}=41.9 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}
$$

Since $U_{D}$ is much greater than $U_{r e q}$, the exchanger is thermally workable, but over-sized.
(o) Over-surface and over-design

It is convenient to perform the calculations using overall coefficients rather than surface areas. The appropriate relationships are as follows:

$$
\begin{aligned}
\text { over-surface } & =U_{C} / U_{r e q}-1=54.8 / 24.5-1=124 \% \\
\text { over-design } & =U_{D} / U_{\text {req }}-1=41.9 / 24.5-1=71 \%
\end{aligned}
$$

Clearly, the exchanger is much larger than necessary.
(p) Tube-side pressure drop

The friction factor is computed using Equation (5.2).

$$
\begin{aligned}
& f=0.4137 R e^{-0.2585}=0.4137(12,149)^{-0.2585}=0.03638 \\
& G=\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i}^{2} / 4}=\frac{150,000(6 / 156)}{\left[\pi(0.0695)^{2} / 4\right]}=1,520,752 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The friction loss is given by Equation (5.1):

$$
\Delta P_{f}=\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.03638 \times 6 \times 20(1,520,752)^{2}}{7.50 \times 10^{12} \times 0.0695 \times 0.85 \times 1.0}=22.8 \mathrm{psi}
$$

The tube entrance, exit, and return losses are estimated using Equation (5.3) with $\alpha_{r}$ equal to ( $2 n_{P}-1.5$ ) from Table 5.1.

$$
\begin{aligned}
& \Delta P_{r}=1.334 \times 10^{-13}\left(2 n_{p}-1.5\right) G^{2} / s=1.334 \times 10^{-13}(10.5)(1,520,752)^{2} / 0.85 \\
& \Delta P_{r}=3.81 \mathrm{psi}
\end{aligned}
$$

The sum of the two pressure drops is much greater than the allowed pressure drop. Therefore, the nozzle losses will not be calculated.
(q) Shell-side pressure drop

The friction factor is calculated using Equations (5.7)-(5.9).

$$
\begin{aligned}
& f_{1}=\left(0.0076+0.000166 d_{s}\right) R e^{-0.125}=(0.0076+0.000166 \times 21.25)(20,358)^{-0.125} \\
& f_{1}=0.00322 \mathrm{ft}^{2} / \mathrm{in}^{2} \\
& f_{2}=\left(0.0016+5.8 \times 10^{-5} d_{s}\right) R e^{-0.157}=\left(0.0016+5.8 \times 10^{-5} \times 21.25\right)(20,358)^{-0.157} \\
& f_{2}=0.000597 \mathrm{ft}^{2} / \mathrm{in}^{2}
\end{aligned}
$$

$$
\begin{aligned}
f & =144\left\{f_{1}-1.25\left(1-B / d_{s}\right)\left(f_{1}-f_{2}\right)\right\} \\
& =144\{0.00322-1.25(1-0.3)(0.00322-0.000597)\} \\
f & =0.1332
\end{aligned}
$$

The number of baffle spaces, $n_{b}+1$, is estimated by neglecting the thickness of the tubesheets. The baffle spacing is commonly interpreted as the center-to-center distance between baffles, which is technically the baffle pitch. In effect, the baffle thickness is accounted for in the baffle spacing. (This interpretation is inconsistent with the equation for the flow area, $a_{s}$, where the face-to-face baffle spacing should be used rather than the center-to-center spacing. However, the difference is usually of little practical consequence and is neglected herein.) The result is:

$$
n_{b}+1 \cong L / B=(20 \times 12) / 6.375=37.65 \Rightarrow 38
$$

The friction loss is given by Equation (5.6):

$$
\begin{aligned}
\Delta P_{f} & =\frac{f G^{2} d_{s}\left(n_{b}+1\right)}{7.50 \times 10^{12} d_{e} s \phi}=\frac{0.1332(239,362)^{2} \times 21.25 \times 38}{7.50 \times 10^{12} \times 0.99 \times 0.785 \times 1.0} \\
\Delta P_{f} & =1.06 \mathrm{psi}
\end{aligned}
$$

The nozzle losses will not be calculated because the initial design requires significant modification. This completes the rating of the initial design.

In summary, there are two problems with the initial configuration of the heat exchanger:
(1) The tube-side pressure drop is too large.
(2) The exchanger is over-sized.

In addition, the pressure drop on the shell-side is quite low, suggesting a poor trade-off between pressure drop and heat transfer.

To remedy these problems, both the number of tubes and the number of tube passes can be reduced. We first calculate the number of tubes required, assuming the overall heat-transfer coefficient remains constant.

$$
\begin{aligned}
A_{r e q} & =\frac{q}{U_{D} F\left(\Delta T_{\mathrm{ln}}\right)_{c f}}=\frac{3,717,000}{41.9 \times 0.97 \times 191.2}=478 \mathrm{ft}^{2} \\
\left(n_{t}\right)_{r e q} & =\frac{A_{r e q}}{\pi D_{o} L}=\frac{478}{\pi(1.0 / 12) \times 20}=91.3 \Rightarrow 92
\end{aligned}
$$

Taking four tube passes, the tube-count table shows that the closest count is 104 tubes in a 17.25 -in. shell. The effect of these changes on the tube-side flow and pressure drop are estimated as follows.

$$
R e \rightarrow 12,149(4 / 6)(156 / 104)=12,149
$$

From Equation (5.19),

$$
\begin{aligned}
& \Delta P_{f} \sim n_{p}^{2.74} n_{t}^{-1.74} \\
& \Delta P_{f} \rightarrow 22.8(4 / 6)^{2.74}(104 / 156)^{-1.74}=15.2 \mathrm{psi}
\end{aligned}
$$

Since these changes leave $R e$ (and hence G) unchanged, the minor losses are easily calculated using Equation (5.3).

$$
\Delta P_{r}=1.334 \times 10^{-13}(6.5)(1,520,752)^{2} / 0.85=2.36 \mathrm{psi}
$$

Thus, in order to meet the pressure-drop constraint, the tube length will have to be reduced significantly, to about 15 ft when allowance for nozzle losses is included. The resulting undersurfacing will have to be compensated by a corresponding increase in $h_{o}$, which is problematic. (Since $R e_{i}$ remains unchanged, so does $h_{i}$.) It is left as an exercise for the reader to check the viability of this configuration.

In order to further reduce the tube-side pressure drop, we next consider an exchanger with more tubes. Referring again to the tube-count table, the next largest unit is a $19.25-\mathrm{in}$. shell containing a maximum of 130 tubes (for four passes). The tube-side Reynolds number for this configuration is:

$$
R e \rightarrow 12,149(4 / 6)(156 / 130)=9719
$$

Reducing the number of tubes to 124 (31 per pass) gives $R e_{i}=10,189$. The friction loss then becomes:

$$
\Delta P_{f} \rightarrow 22.8(4 / 6)^{2.74}(124 / 156)^{-1.74}=11.2 \mathrm{psi}
$$

The minor losses will also be lower, and shorter tubes can be used in this unit, further assuring that the pressure-drop constraint will be met. (The final tube length will be determined after the overall heat-transfer coefficient has been recalculated.)

Thus, for the second trial a 19.25 -in. shell containing 124 tubes arranged for four passes is specified. Due to the low shell-side pressure drop, the baffle spacing is also reduced to the minimum of $0.2 d_{s}$. (Using a baffle spacing at or near the minimum can cause excessive leakage and bypass flows on the shell-side, resulting in reduced performance of the unit [9]. The low shell-side pressure drop in the present application should mitigate this problem.)

## Second trial

Based on the foregoing analysis, we anticipate that the exchanger will have sufficient heat-transfer area to satisfy the duty. Therefore, we will calculate the overall coefficient, $U_{D}$, and use it to determine the tube length that is needed. The pressure drops will then be checked.
(a) Calculate $h_{i}$

$$
\begin{aligned}
R e & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 150,000(4 / 124)}{\pi \times 0.0695 \times 8.7}=10,189 \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =(0.077 / 0.0695) \times 0.023(10,189)^{0.8}(55.36)^{1 / 3}(1.0) \\
h_{i} & =156 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(b) Calculate $h_{o}$

$$
\begin{aligned}
B & =0.2 d_{s}=0.2 \times 19.25=3.85 \mathrm{in} . \\
a_{s} & =\frac{d_{s} C^{\prime} B}{144 P_{T}}=\frac{19.25 \times 0.25 \times 3.85}{144 \times 1.25}=0.103 \mathrm{ft}^{2} \\
G & =\dot{m} / a_{s}=45,000 / 0.103=436,893 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =D_{e} G / \mu=0.0825 \times 436,893 / 0.97=37,158 \\
j_{H} & =0.5\left(1+B / d_{s}\right)\left(0.08 R e^{0.6821}+0.7 R e^{0.1772}\right) \\
& =0.5(1+0.2)\left[0.08(37,158)^{0.6821}+0.7(37,158)^{0.1772}\right]
\end{aligned}
$$

$$
\begin{aligned}
j_{H} & =65.6 \\
h_{o} & =j_{H}\left(k / D_{e}\right) P r^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =65.6(0.079 / 0.0825)(7.24)^{1 / 3}(1.0) \\
h_{o} & =122 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(c) Calculate $U_{D}$

$$
\begin{aligned}
U_{D} & =\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k_{\text {tube }}}+\frac{1}{h_{o}}+R_{D}\right]^{-1} \\
& =\left[\frac{1.0}{156 \times 0.834}+\frac{(1.0 / 12) \ln (1.0 / 0.839)}{2 \times 26}+\frac{1}{122}+0.0056\right]^{-1} \\
U_{D} & =46 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(d) Calculate tube length.

$$
\begin{aligned}
q & =U_{D} n_{t} \pi D_{o} L F\left(\Delta T_{\ln }\right)_{c f} \\
L & =\frac{q}{U_{D} n_{t} \pi D_{o} F\left(\Delta T_{\ln }\right)_{c f}}=\frac{3,717,000}{46 \times 124 \pi(1.0 / 12) \times 0.97 \times 191.2}=13.4 \mathrm{ft}
\end{aligned}
$$

Therefore, take $L=14 \mathrm{ft}$
(e) Tube-side pressure drop.

$$
\begin{aligned}
f & =0.4137 R e^{-0.2585}=0.4137(10,189)^{-0.2585}=0.03807 \\
G & =\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\left(\pi D_{i}^{2} / 4\right)}=\frac{150,000(4 / 124)}{\left[\pi(0.0695)^{2} / 4\right]}=1,275,469 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.03807 \times 4 \times 14(1,275,469)^{2}}{7.50 \times 10^{12} \times 0.0695 \times 0.85 \times 1.0} \\
\Delta P_{f} & =7.83 \mathrm{psi} \\
\Delta P_{r} & =1.334 \times 10^{-13}\left(2 n_{p}-1.5\right) G^{2} / s=1.334 \times 10^{-13}(6.5)(1,275,469)^{2} / 0.85 \\
\Delta P_{r} & =1.66 \mathrm{psi}
\end{aligned}
$$

Table 5.3 indicates that 4-in. nozzles are appropriate for a 19.25 -in. shell. Assuming schedule 40 pipe is used for the nozzles,

$$
\begin{aligned}
R e_{n} & =\frac{4 \dot{m}}{\pi D_{n} \mu}=\frac{4 \times 150,000}{\pi(4.026 / 12) \times 8.7}=65,432 \\
G_{n} & =\dot{m} /\left(\pi D_{n}^{2} / 4\right)=150,000 /\left[\pi(4.026 / 12)^{2} / 4\right]=1,696,744 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

Since the flow in the nozzles is turbulent, Equation (5.4) is applicable.

$$
\begin{aligned}
& \Delta P_{n}=2.0 \times 10^{-13} N_{s} G_{n}^{2} / s=2.0 \times 10^{-13} \times 1(1,696,744)^{2} / 0.85 \\
& \Delta P_{n}=0.68 \mathrm{psi}
\end{aligned}
$$

The total tube-side pressure drop is:

$$
\Delta P_{i}=\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=7.83+1.66+0.68=10.17 \cong 10.2 \mathrm{psi}
$$

(f) Shell-side pressure drop.

Since $B / d_{s}=0.2$, the friction factor is given by:

$$
\begin{aligned}
f & =144 f_{2}=144\left(0.0016+5.8 \times 10^{-5} d_{s}\right) R e^{-0.157} \\
& =144\left(0.0016+5.8 \times 10^{-5} \times 19.25\right)(37,158)^{-0.157} \\
f & =0.07497
\end{aligned}
$$

$n_{B}+1=L / B=(14 \times 12) / 3.85=43.6 \Rightarrow 43$ (Rounded downward to keep $B \geq B_{\min }$ )

$$
\begin{aligned}
& \Delta P_{f}=\frac{f G^{2} d_{s}\left(n_{b}+1\right)}{7.50 \times 10^{12} d_{e} s \phi}=\frac{0.07497(436,893)^{2} \times 19.25 \times 43}{7.50 \times 10^{12} \times 0.99 \times 0.785 \times 1.0} \\
& \Delta P_{f}=2.03 \mathrm{psi}
\end{aligned}
$$

Since the flow rate of kerosene is much less than that of the crude oil, 3 -in. nozzles should be adequate for the shell. Assuming schedule 40 pipe is used,

$$
\begin{aligned}
R e_{n} & =\frac{4 \dot{m}}{\pi D_{n} \mu}=\frac{4 \times 45,000}{\pi(3.068 / 12) \times 0.97}=231,034 \text { (turbulent) } \\
G_{n} & =\frac{\dot{m}}{\left(\pi D_{n}^{2} / 4\right)}=\frac{45,000}{\left[\pi(3.068 / 12)^{2} / 4\right]}=876,545 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{n} & =2.0 \times 10^{-13} N_{s} G_{n}^{2} / s=2.0 \times 10^{-13} \times 1(876,545)^{2} / 0.785 \\
\Delta P_{n} & =0.20 \mathrm{psi}
\end{aligned}
$$

Note: $\rho V_{n}^{2}=1210\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)(\mathrm{ft} / \mathrm{s})^{2}$, so impingement protection for the tube bundle will not be required to prevent erosion.
The total shell-side pressure drop is:

$$
\Delta P_{o}=\Delta P_{f}+\Delta P_{n}=2.03+0.20=2.23 \cong 2.2 \mathrm{psi}
$$

(g) Over-surface and over-design.

$$
\begin{aligned}
U_{C} & =\left[1 / U_{D}-R_{D}\right]^{-1}=[1 / 46-0.0056]^{-1}=62 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
A & =n_{t} \pi D_{0} L=124 \pi \times(1.0 / 12) \times 14=454 \mathrm{ft}^{2} \\
U_{\text {req }} & =\frac{q}{A F\left(\Delta T_{\mathrm{ln}}\right)_{c f}}=\frac{3,717,000}{454 \times 0.97 \times 191.2}=44 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\text { over-surface } & =U_{C} / U_{\text {req }}-1=62 / 44-1=41 \% \\
\text { over-design } & =U_{D} / U_{\text {req }}-1=46 / 44-1=4.5 \%
\end{aligned}
$$

All design criteria are satisfied. The shell-side pressure drop is still quite low, but the shellside heat-transfer coefficient ( $122 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ ) does not differ greatly from the tube-side coefficient ( $156 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ ). The reader can also verify that the tube-side fluid velocity is $6.7 \mathrm{ft} / \mathrm{s}$, which is within the recommended range. Therefore, the design is acceptable.

## Final design summary

Tube-side fluid: crude oil.
Shell-side fluid: kerosene.
Shell: Type AES, $19.25-$ in. ID
Tube bundle: 124 tubes, 1 -in. OD, 14 BWG, $14-\mathrm{ft}$ long, on $1.25-\mathrm{in}$. square pitch, arranged for four passes.
Heat-transfer area: $454 \mathrm{ft}^{2}$
Baffles: $20 \%$ cut segmental type with spacing approximately 3.85 in.
Sealing strips: one pair per ten tube rows.
Nozzles: 4 -in. schedule 40 on tube side; 3 -in. schedule 40 on shell side.
Materials: plain carbon steel throughout.

## Example 5.2

$350,000 \mathrm{lbm} / \mathrm{h}$ of a light oil are to be cooled from $240^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ using cooling water with a range of $85^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$. A maximum pressure drop of 7 psi has been specified for each stream, and fouling factors of $0.003 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ for the oil and $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{B} t u$ for the water are required. Fluid properties are given in the table below. Design a shell-and-tube heat exchanger for this service.

| Fluid property | Oil at $195^{\circ} \mathrm{F}$ | Water at $102.5^{\circ} \mathrm{F}$ |
| :--- | :---: | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.55 | 1.0 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.08 | 0.37 |
| $\mu(c p)$ | $0.68^{*}$ | 0.72 |
| Specific gravity | 0.80 | 0.99 |
| $P r$ | 11.31 | 4.707 |

${ }^{*} \mu_{o i l}(c p)=0.03388 \exp \left[1965.6 / T\left({ }^{\circ} R\right)\right]$.

## Solution

(a) Make initial specifications.
(i) Fluid placement

According to Table 3.4, cooling water should be placed in the tubes even though the required fouling factors indicate that the oil has a greater fouling tendency. Also, this service (organic fluid versus water) is a good application for a finned-tube exchanger, which requires that the oil be placed in the shell.
(ii) Shell and head types

With oil in the shell, the exterior tube surfaces will require cleaning. Therefore, a floating-head type AES exchanger is selected. This configuration will also accommodate differential thermal expansion resulting from the large temperature difference between the two streams.
(iii) Tubing

Finned tubes having 19 fins per inch will be used. For water service, the design guidelines indicate $3 / 4$-in., 16 BWG tubes. A tube length of 16 ft is chosen.

The tubing dimensions in Table B. 4 will be assumed for the purpose of this example. The last three digits of the catalog number (or part number) indicate the average wall thickness of the finned section in thousandths of an inch. Since a 16 BWG tube has a wall thickness of 0.065 in ., the specified tubing corresponds to catalog number 60-195065.
(iv) Tube layout

Square pitch is specified to allow mechanical cleaning of the tube exterior surfaces. Following the design guidelines, for $3 / 4-\mathrm{in}$. tubes a pitch of 1.0 in . is specified.
(v) Baffles

Segmental baffles with a $20 \%$ cut are specified, and the baffle spacing is set at 0.3 shell diameters.
(vi) Sealing strips

One pair of sealing strips per 10 tube rows is specified as required for the Simplified Delaware method.
(vii) Construction materials

Admiralty brass ( $k=64 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) will be used for the tubes and navel brass for the tubesheets. Plain carbon steel will be used for all other components, including the shell, heads, baffles, and tube-pass partitions. Although the heads and pass partitions will be exposed to the water, the corrosion potential is not considered sufficient to use alloys for these components. Brass tubesheets are specified for compatibility with the tubes in order to preclude electrolytic attack.
(b) Energy balances.

$$
\begin{aligned}
q & =\left(\dot{m} C_{P} \Delta T\right)_{\text {oil }}=350,000 \times 0.55 \times 90=17,325,000 \mathrm{Btu} / \mathrm{h} \\
17,325,000 & =\left(\dot{m} C_{P} \Delta T\right)_{\text {water }}=\dot{m}_{\text {water }} \times 1.0 \times 35 \\
\dot{m}_{\text {water }} & =495,000 \mathrm{lbm} / \mathrm{h}
\end{aligned}
$$

(c) LMTD.

$$
\left(\Delta T_{\ln }\right)_{c f}=\frac{120-65}{\ln (120 / 65)}=89.7^{\circ} \mathrm{F}
$$

(d) LMTD correction factor.

$$
\begin{aligned}
& R=\frac{T_{a}-T_{b}}{t_{b}-t_{a}}=\frac{240-150}{120-85}=2.57 \\
& P=\frac{t_{b}-t_{a}}{T_{a}-t_{a}}=\frac{120-85}{240-85}=0.226
\end{aligned}
$$

From Figure 3.9 or Equation (3.15), for a 1-2 exchanger $F \cong 0.93$.
(e) Estimate $U_{D}$.

Perusal of Table 3.5 indicates that the best matches are a kerosene-or-gas-oil/water exchanger and a low-viscosity-lube-oil/water exchanger, both with $U_{D}$ between 25 and $50 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Therefore, assume $U_{D}=40 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(f) Calculate heat-transfer area and number of tubes.

$$
A=\frac{q}{U_{D} F\left(\Delta T_{\ln }\right)_{c f}}=\frac{17,325,000}{40 \times 0.93 \times 89.7}=5192 \mathrm{ft}^{2}
$$

From Table B.4, the external surface area of a $3 / 4$-in. tube with 19 fins per inch is $0.507 \mathrm{ft}^{2}$ per foot of tube length. Therefore,

$$
n_{t}=\frac{5192}{0.507 \times 16}=640
$$

(g) Number of tube passes.

$$
\begin{aligned}
R e & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu} \\
D_{i} & =0.495 \mathrm{in}=0.04125 \mathrm{ft} \quad(\text { Table B.4) } \\
R e & =\frac{4 \times 495,000\left(n_{p} / 640\right)}{\pi \times 0.04125 \times 0.72 \times 2.419}=13,707 n_{p}
\end{aligned}
$$

Thus, one or two passes will suffice. For two passes, the fluid velocity is:

$$
V=\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\rho \pi D_{i}^{2} / 4}=\frac{(495,000 / 3600)(2 / 640)}{0.99 \times 62.43 \pi(0.04125)^{2} / 4}=5.2 \mathrm{ft} / \mathrm{s}
$$

For one pass, $V=2.6 \mathrm{ft} / \mathrm{s}$ (too low) and for four passes, $V=10.4 \mathrm{ft} / \mathrm{s}$ (too high). Therefore, two passes will be used.
(h) Determine shell size and actual tube count.

From the tube-count table for $3 / 4$-in. tubes on 1 -in. square pitch (Table C.3), the closest count is 624 tubes in a $31-\mathrm{in}$. shell.
This completes the initial design of the unit. The rating calculations follow.
(i) Calculate the required overall coefficient.

$$
U_{\text {req }}=\frac{q}{n_{t} A_{T o t} F\left(\Delta T_{\ln }\right)_{c f}}=\frac{17,325,000}{624(0.507 \times 16) \times 0.93 \times 89.7}=41 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(j) Calculate $h_{i}$ assuming $\phi_{i}=1.0$.

$$
\begin{aligned}
R e & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 495,000(2 / 624)}{\pi \times 0.04125 \times 0.72 \times 2.419}=28,117 \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =(0.37 / 0.04125) \times 0.023(28,117)^{0.8}(4.707)^{1 / 3}(1.0) \\
h_{i} & =1253 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(k) Calculate $h_{o}$ assuming $\phi_{o}=1.0$

$$
\begin{aligned}
B & =0.3 d_{s}=0.3 \times 31=9.3 \mathrm{in} . \\
C^{\prime} & =0.34 \mathrm{in} . \quad(\text { from Figure } 3.12) \\
a_{s} & =\frac{d_{s} C^{\prime} B}{144 P_{T}}=\frac{31 \times 0.34 \times 9.3}{144 \times 1.0}=0.681 \mathrm{ft}^{2} \\
G & =\dot{m} / a_{s}=350,000 / 0.681=513,950 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
d_{e} & =1.27 \mathrm{in} . \quad(\text { from Figure } 3.12) \\
D_{e} & =1.27 / 12=0.1058 \mathrm{ft} \\
R e & =D_{e} G / \mu=0.1058 \times 513,950 /(0.68 \times 2.419)=33,057
\end{aligned}
$$

$$
\begin{aligned}
j_{H} & =0.5\left(1+B / d_{S}\right)\left(0.08 R e^{0.6821}+0.7 R e^{0.1772}\right) \\
& =0.5(1+0.3)\left[0.08(33,057)^{6821}+0.7(33,057)^{0.1772}\right] \\
j_{H} & =65.77 \\
h_{o} & =j_{H}\left(k / D_{e}\right) \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =65.77(0.08 / 0.1058)(11.31)^{1 / 3}(1.0) \\
h_{o} & =112 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(l) Calculate fin efficiency.

The fin efficiency is calculated from Equations (2.27) and (5.12) with $k=64 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ for Admiralty brass. Fin dimensions are obtained from Table B.4.
$\tau=$ fin thickness $=0.011 \mathrm{in} .=0.0009167 \mathrm{ft}$
$r_{1}=$ root tube radius $=0.625 / 2=0.3125 \mathrm{in}$.
$r_{2}=r_{1}+$ fin height $=0.3125+0.05=0.3625 \mathrm{in}$.
$r_{2 c}=r_{2}+\tau / 2=0.3625+0.011 / 2=0.3680 \mathrm{in}$.
$\psi=\left(r_{2 c}-r_{1}\right)\left[1+0.35 \ln \left(r_{2 c} / r_{1}\right)\right]=(0.3680-0.3125)[1+0.35 \ln (0.3680 / 0.3125)]$
$\psi=0.058676 \mathrm{in} .=0.0048897 \mathrm{ft}$
$m=(2 h / k \tau)^{0.5}=(2 \times 112 / 64 \times 0.0009167)^{0.5}=61.7903 \mathrm{ft}^{-1}$
$m \psi=61.7903 \times 0.0048897=0.302136$
$\eta_{f}=\frac{\tanh (0.302136)}{0.302136}=0.971$
The weighted efficiency of the finned surface is given by Equation (2.31). The fin and prime surface areas per inch of tube length are first calculated to determine the area ratios:

$$
\begin{aligned}
A_{\text {fins }} & =2 N_{f} \pi\left(r_{2 c}^{2}-r_{1}^{2}\right)=19 \times 2 \pi\left[(0.3680)^{2}-(0.3125)^{2}\right]=4.5087 \mathrm{in}^{2} . \\
A_{\text {prime }} & =2 \pi r_{1}\left(L-N_{f} \tau\right)=2 \pi \times 0.3125(1.0-19 \times 0.011)=1.5531 \mathrm{in}^{2} . \\
A_{\text {fins }} / A_{\text {Tot }} & =4.5087 /(4.5087+1.5531)=0.744 \\
A_{\text {prime }} / A_{\text {Tot }} & =1-0.744=0.256 \\
\eta_{w} & =\left(A_{\text {prime }} / A_{\text {Tot }}\right)+\eta_{f}\left(A_{\text {fins }} / A_{\text {Tot }}\right)=0.256+0.971 \times 0.744 \\
\eta_{w} & =0.978
\end{aligned}
$$

(m) Calculate wall temperatures.

The wall temperatures used to obtain viscosity correction factors are given by Equations (4.38) and (4.39). From Table B.4, the ratio of external to internal tube surface area is $A_{T o t} / A_{i}=3.91$. Hence,

$$
\begin{aligned}
T_{p} & =\frac{h_{i} t_{\text {ave }}+h_{o} \eta_{w}\left(A_{\text {Tot }} / A_{i}\right) T_{\text {ave }}}{h_{i}+h_{o} \eta_{w}\left(A_{\text {Tot }} / A_{i}\right)} \\
& =\frac{1253 \times 102.5+112 \times 0.978 \times 3.91 \times 195}{1253+112 \times 0.978 \times 3.91} \\
T_{p} & =126^{\circ} \mathrm{F}
\end{aligned}
$$

$$
\begin{aligned}
T_{w t d} & =\frac{h_{i} \eta_{w} t_{\text {ave }}+\left[h_{i}\left(1-\eta_{w}\right)+h_{o} \eta_{w}\left(A_{\text {Tot }} / A_{i}\right)\right] T_{\text {ave }}}{h_{i}+h_{o} \eta_{w}\left(A_{T o t} / A_{i}\right)} \\
& =\frac{1253 \times 0.978 \times 102.5+[1253 \times 0.022+112 \times 0.978 \times 3.91] \times 195}{1253+112 \times 0.978 \times 3.91} \\
T_{w t d} & =128^{\circ} \mathrm{F}
\end{aligned}
$$

(n) Calculate viscosity correction factors and corrected heat-transfer coefficients. From Figure A.1, the viscosity of water at $126^{\circ} \mathrm{F}$ is approximately 0.58 cp . Hence,

$$
\phi_{i}=(0.72 / 0.58)^{-0.14}=1.031
$$

The oil viscosity at $128^{\circ} \mathrm{F}=588^{\circ} \mathrm{R}$ is:

$$
\mu_{o i l}=0.03388 \exp (1965.6 / 588)=0.96 \mathrm{cp}
$$

Therefore,

$$
\phi_{o}=(0.68 / 0.96)^{0.14}=0.953
$$

The corrected heat-transfer coefficients are:

$$
\begin{aligned}
& h_{i}=1253 \times 1.031=1292 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
& h_{o}=112 \times 0.953=107 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(o) Calculate the clean overall coefficient.

The clean overall coefficient for an exchanger with finned tubes is given by Equation (4.27):

$$
\begin{aligned}
U_{C} & =\left[\frac{A_{T o t}}{h_{i} A_{i}}+\frac{A_{\text {Tot }} \ln \left(D_{o} / D_{i}\right)}{2 \pi k_{\text {tube }} L}+\frac{1}{h_{o} \eta_{w}}\right]^{-1} \\
& =\left[\frac{3.91}{1292}+\frac{8.112 \ln (0.625 / 0.495)}{2 \pi \times 64 \times 16}+\frac{1}{107 \times 0.978}\right]^{-1} \\
U_{C} & =77.7 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Since $U_{C}>U_{r e q}$, continue.
(p) Fouling allowance

$$
\begin{aligned}
& R_{D}=R_{D i}\left(A_{T o t} / A_{i}\right)+R_{D o} / \eta_{w}=0.001 \times 3.91+0.003 / 0.978 \\
& R_{D}=0.00698 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
\end{aligned}
$$

(q) Calculate the design overall coefficient

$$
U_{D}=\left(1 / U_{C}+R_{D}\right)^{-1}=(1 / 77.7+0.00698)^{-1}=50.4 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

Since $U_{D}>U_{\text {req }}$, the exchanger is thermally workable, but somewhat over-sized (overdesign $=23 \%$.
(r) Tube-side pressure drop

$$
\begin{aligned}
f & =0.4137 R e^{-0.2585}=0.4137(28,117)^{-0.2585}=0.02928 \\
G & =\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\left(\pi D_{i}^{2} / 4\right)}=\frac{495,000(2 / 624)}{\left[\pi(0.04125)^{2} / 4\right]}=1,187,170 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.02928 \times 2 \times 16(1,187,170)^{2}}{7.50 \times 10^{12} \times 0.04125 \times 0.99 \times 1.031} \\
\Delta P_{f} & =4.18 \mathrm{psi} \\
\Delta P_{r} & =1.334 \times 10^{-13}\left(2 n_{p}-1.5\right) G^{2} / s=1.334 \times 10^{-13}(2.5)(1,187,170)^{2} / 0.99 \\
\Delta P_{r} & =0.475 \mathrm{psi}
\end{aligned}
$$

For a 31-in. shell, Table 5.3 indicates that 8 -in. nozzles are appropriate. For schedule 40 nozzles,

$$
\begin{aligned}
R e_{n} & =\frac{4 \dot{m}}{\pi D_{n} \mu}=\frac{4 \times 495,000}{\pi(7.981 / 12) \times 0.72 \times 2.419}=544,090 \\
G_{n} & =\dot{m} /\left(\pi D_{n}^{2} / 4\right)=495,000 /\left[\pi(7.98 / 12)^{2} / 4\right]=1,424,830 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

Since the nozzle flow is highly turbulent, Equation (5.4) is applicable:

$$
\begin{aligned}
& \Delta P_{n}=2.0 \times 10^{-13} N_{s} G_{n}^{2} / s=2.0 \times 10^{-13} \times 1(1,424,830)^{2} / 0.99 \\
& \Delta P_{n}=0.41 \mathrm{psi}
\end{aligned}
$$

The total tube-side pressure drop is:

$$
\Delta P_{i}=\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=4.18+0.475+0.41 \cong 5.1 \mathrm{psi}
$$

(s) Shell-side pressure drop

$$
\begin{aligned}
f_{1} & =\left(0.0076+0.000166 d_{s}\right) R e^{-0.125} \\
& =(0.0076+0.000166 \times 31)(33,057)^{-0.125} \\
f_{1} & =0.00347 \mathrm{ft}^{2} / \mathrm{in}^{2} \\
f_{2} & =\left(0.0016+5.8 \times 10^{-5} d_{s}\right) R e^{-0.157} \\
& =\left(0.0016+5.8 \times 10^{-5} \times 23.25\right)(33,057)^{-0.157} \\
f_{2} & =0.000576 \mathrm{ft}^{2} / \mathrm{in.}^{2} \\
f & =144\left\{f_{1}-1.25\left(1-B / d_{s}\right)\left(f_{1}-f_{2}\right)\right\} \\
& =144\{0.00347-1.25(1-0.3)(0.00347-0.000576)\} \\
f & =0.135 \\
n_{b}+1 & =L / B=(16 \times 12) / 9.3=20.6 \Rightarrow 21 \\
\Delta P_{f} & =\frac{f G^{2} d_{s}\left(n_{b}+1\right)}{7.50 \times 10^{12} d_{e} s \phi}=\frac{0.135(513,950)^{2} \times 31 \times 21}{7.50 \times 10^{12} \times 1.27 \times 0.8 \times 0.953} \\
\Delta P_{f} & =3.20 \mathrm{psi}
\end{aligned}
$$

Assuming 8-in. schedule 40 nozzles are also used for the shell, we first check the Reynolds number at the outlet conditions ( $T=150^{\circ} \mathrm{F}$ ) where the oil viscosity is highest.

$$
\begin{aligned}
& \mu_{o i l}=0.03388 \exp (1965.6 / 610)=0.85 \mathrm{cp} \\
& R e_{n}=4 \dot{m} / \pi D_{n} \mu=\frac{4 \times 350,000}{\pi(7.981 / 12) \times 0.85 \times 2.419}=325,872
\end{aligned}
$$

Since the flow is turbulent, Equation (5.4) can be used to estimate the nozzle losses.

$$
\begin{aligned}
G_{n} & =\dot{m} /\left(\pi D_{n}^{2} / 4\right)=350,000 /\left[\pi(7.981 / 12)^{2} / 4\right]=1,007,456 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{n} & =2.0 \times 10^{-13} N_{s} G_{n}^{2} / s=2.0 \times 10^{-13} \times 1(1,007,456)^{2} / 0.8 \\
\Delta P_{n} & =0.25 \mathrm{psi}
\end{aligned}
$$

Note: $\rho V_{n}^{2}=1,569\left(\mathrm{lbm} / \mathrm{ft}^{2}\right)(\mathrm{ft} / \mathrm{s})^{2}$, so impingement protection will be required, which will increase the pressure drop slightly. This could be avoided by using a larger diameter for the inlet nozzle.

The total shell-side pressure drop is:

$$
\Delta P_{o}=\Delta P_{f}+\Delta P_{n}=3.20+0.25 \cong 3.5 \mathrm{psi}
$$

This completes the rating of the initial configuration of the exchanger. To summarize, all design criteria are satisfied, but the exchanger is larger than necessary.

The size of the unit can be reduced by decreasing the number of tubes and/or the tube length. In order to determine the extent of the modifications required, we first calculate the required area assuming that the overall coefficient remains unchanged.

$$
A_{\text {req }}=\frac{q}{U_{D} F\left(\Delta T_{\ln }\right)_{c f}}=\frac{17,325,000}{50.4 \times 0.93 \times 89.7}=4121 \mathrm{ft}^{2}
$$

Next, we consider reducing the tube length while keeping the number of tubes fixed at 624 . The required tube length is:

$$
L=\frac{4121 \mathrm{ft}^{2}}{624 \times 0.507 \mathrm{ft}^{2} / \mathrm{ft}}=13.0 \mathrm{ft}
$$

Since this change will not affect the heat-transfer coefficients and will reduce the pressure drops, it is not necessary to repeat the rating calculations. The new pressure drops can be obtained by using the length ratio $(13 / 16)$ as a scale factor for the friction losses. The minor losses will not change. For the tube side,

$$
\begin{aligned}
\Delta P_{f} & =4.18(13 / 16)=3.40 \mathrm{psi} \\
\Delta P_{i} & =\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=3.40+0.475+0.41 \cong 4.3 \mathrm{psi}
\end{aligned}
$$

The calculation for the shell side is approximate because the requirement for an integral number of baffles is ignored:

$$
\begin{aligned}
& \Delta P_{f} \cong 3.20(13 / 16)=2.60 \mathrm{psi} \\
& \Delta P_{o}=\Delta P_{f}+\Delta P_{n} \cong 2.60+0.25 \cong 2.9 \mathrm{psi}
\end{aligned}
$$

The over-surface for the modified design is next computed.

$$
\begin{aligned}
A & =n_{t} \pi D_{o} L=624 \times 0.507 \times 13=4113 \mathrm{ft}^{2} \\
U_{\text {req }} & =\frac{q}{A F\left(\Delta T_{\mathrm{ln}}\right)_{c f}}=\frac{17,325,000}{4113 \times 0.93 \times 89.7}=50.5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\text { over-surface } & =U_{C} / U_{\text {req }}-1=77.7 / 50.5-1 \cong 54 \%
\end{aligned}
$$

The over-surface is fairly high, but as was the case with the finned-pipe exchanger of Example 5.2, this is simply a reflection of the high total fouling factor of $0.00698 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ that was required for this exchanger.

The over-design for this unit is effectively zero since the actual tube length is equal to the required tube length. If an additional safety margin is desired, the tube length can be increased. A length of 14 ft , for example, provides an over-design of $7.7 \%$, while both pressure drops remain well below the specified maximum.

Finally, the reader can verify that the tube-side fluid velocity is $5.3 \mathrm{ft} / \mathrm{s}$, which is within the recommended range. The final design parameters are summarized below.

## Design summary

Tube-side fluid: cooling water.
Shell-side fluid: oil.
Shell: Type AES, 31-in. ID
Tube bundle: 624 tubes, $3 / 4$-in. OD, 16 BWG, radial low-fin tubes, 19 fins per inch, 13 -ft long, on $1-\mathrm{in}$. square pitch, arranged for two passes.
Heat-transfer area: $4113 \mathrm{ft}^{2}$
Baffles: $20 \%$ cut segmental type with spacing approximately 9.3 in.
Sealing strips: one pair per 10 tube rows.
Nozzles: $8-\mathrm{in}$. schedule 40 on both tube side and shell side.
Materials: Admiralty brass tubes, naval brass tubesheets, all other components of plain carbon steel.
Now we consider modifying the initial design by reducing the number of tubes. If the tube length and overall heat-transfer coefficient remain constant, the number of tubes required is:

$$
n_{t}=\frac{4121 \mathrm{ft}^{2}}{0.507 \times 16 \mathrm{ft}^{2} \text { per tube }}=508
$$

From the tube-count table, the closest match with two tube passes is 532 tubes in a $29-\mathrm{in}$. shell. Reducing the number of tubes and the shell ID will cause both $h_{i}$ and $h_{o}$ to increase, so it may be possible to reduce the tube length as well. It will also cause the pressure drops to increase. To estimate the effect on tube-side pressure drop, note that from Equation (5.19), $\Delta P_{f} \sim n_{t}^{-1.74}$. Therefore, assuming no change in the tube length,

$$
\Delta P_{f} \rightarrow 4.18(532 / 624)^{-1.74}=5.52 \mathrm{psi}
$$

Also, since $G \sim n_{t}^{-1}$,

$$
\Delta P_{r} \rightarrow 0.475(532 / 624)^{-2}=0.65 \mathrm{psi}
$$

Hence,

$$
\Delta P_{i} \rightarrow 5.52+0.65+0.41=6.6 \mathrm{psi}
$$

For the shell side, if we neglect the effect of the changes on the friction factor, then Equation (5.28) shows that:

$$
\Delta P_{f} \sim B^{-3} d_{s}^{-2}
$$

Since $B=0.3 d_{s}$, the pressure drop is proportional to the -5 power of shell ID. Hence,
Thus,

$$
\begin{gathered}
\Delta P_{f} \rightarrow 3.20(29 / 31)^{-5}=4.47 \mathrm{psi} \\
\Delta P_{o} \rightarrow 4.47+0.25 \cong 4.7 \mathrm{psi}
\end{gathered}
$$

This configuration may provide a less expensive alternative to the one obtained above. To finalize the design, the overall heat-transfer coefficient must be recalculated, the required tube length determined, and the pressure drops checked, as was done for the second trial in Example 5.1. The calculations are left as an exercise for the reader.

### 5.9 Computer Software

Commercial software packages for designing shell-and-tube exchangers include HTFS/Aspen (www.aspentech.com), B-JAC (www.aspentech.com), ProMax (www.bre.com), HTRI Xchanger Suite (www.htri-net.com), and HEXTRAN (www.simsci-esscor.com). HEXTRAN is discussed in this section; the HTFS/Aspen and HTRI packages are considered in Chapter 7.

The shell-and-tube heat-exchanger module (STE) in HEXTRAN is very flexible. It can handle all of the TEMA shell types with either plain or radial low-fin tubes. Both single-phase and twophase flows are accommodated on either side of the exchanger. Therefore, this module is used for condensers, vaporizers, and reboilers as well as single-phase exchangers. Both un-baffled and baffled exchangers are accepted, including the no-tubes-in window configuration.

The STE module can operate in either rating mode (TYPE=Old) or design mode (TYPE=New). In design mode, certain design parameters are automatically varied to meet a given performance specification (such as the heat duty or a stream outlet temperature) and pressure drop constraints. The following parameters can be varied automatically:

- Number of tubes
- Number of tube passes
- Tube length
- Shell ID
- Number of shells in series and parallel
- Baffle spacing
- Baffle cut

Baffle spacing and baffle cut cannot be varied independently; they must be varied as a pair. As previously noted, these two parameters are highly correlated in practice, and HEXTRAN takes this correlation into account.

For applications in which the shell-side fluid does not undergo a phase change, the full Delaware method is used to calculate the shell-side heat-transfer coefficient and pressure drop. There is also an option (DPSMETHOD $=$ Stream) to calculate the pressure drop using a version of the stream analysis method. These methods will be discussed in more detail in subsequent chapters.

The STE module is not suitable for rod-baffle exchangers or for units, such as air-cooled exchangers, that employ radial high-fin tubes. HEXTRAN provides separate modules for these types of exchangers.

It is important to understand that the results generated by the STE module in design mode are not necessarily optimal. Therefore, it is incumbent on the user to scrutinize the results carefully and to make design modifications as necessary. The software does not eliminate the necessity of iteration in the design process; it just makes the process much faster, easier and less error prone.

Use of the STE module in HEXTRAN version 9.1 is illustrated by the following examples.

## Example 5.3

Use HEXTRAN to rate the final configuration obtained for the kerosene/crude-oil exchanger in Example 5.1, and compare the results with those obtained previously by hand.

## Solution

The procedure for problem setup and data entry is similar to that discussed in Example 4.3. Under Units of Measure, the viscosity unit is changed from cp to $\mathrm{lb} / \mathrm{ft} \cdot \mathrm{h}$ for convenience, and the flow sheet is then constructed in the usual manner. The two feed streams are defined as bulk property streams, and the physical properties are entered on the appropriate forms. Note that fluid density ( $49.008 \mathrm{lbm} / \mathrm{ft}^{3}$ for kerosene and $53.066 \mathrm{lbm} / \mathrm{ft}^{3}$ for crude oil), not specific gravity, must be entered. Since stream pressures were not given in Example 5.1 (they are not needed for the calculations, but must be specified in HEXTRAN), a value of 50 psia is arbitrarily assigned for each stream. Flow rates and temperatures of the feed streams are entered as given in Example 5.1.

The physical parameters of the heat exchanger are entered on the appropriate forms exactly as obtained from Example 5.1. In addition, on the Baffles form the baffle thickness is specified as 0.1875 in. (the default value) and the total tubesheet thickness as 4.0 in . ( 2.0 in . for each tubesheet), in accordance with the design guidelines given in Section 5.7. Note that the total thickness of both tubesheets must be entered, not the individual tubesheet thickness. Only the central baffle spacing ( 3.85 in .) is specified; no value is entered for the inlet or outlet spacing. One pair of sealing strips is also specified on this form. Finally, under Pressure Drop Options, the Two-Phase Film/DP Method is set to HEXTRAN 5.0x Method, and the Shell-side DP Method is set to Bell. (These settings are translated to TWOPHASE $=$ Old and DPSMETHOD $=$ Bell in the input file under UNIT OPERATIONS/STE/CALC.) With these settings, the program uses the Delaware method for both shell-side heat transfer and pressure drop calculations.

The input file generated by the HEXTRAN GUI is given below, followed by the Exchanger Data Sheet and Extended Data Sheet, which were extracted from the output file. Information obtained from the data sheets was used to prepare the following comparison between computer and hand calculations.

| Item | Hand calculation | HEXTRAN |
| :--- | :--- | :--- |
| $R e_{i}$ | 10,189 | 10,189 |
| $R e_{o}$ | 37,158 | 45,148 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 156 | 156.2 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 122 | 191.2 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 46 | 53.3 |
| $\Delta P_{i}(\mathrm{psi})$ | 10.2 | 10.06 |
| $\Delta P_{o}(\mathrm{psi})$ | 2.2 | 2.10 |

The tube-side Reynolds number, heat-transfer coefficient, and pressure drop computed by HEXTRAN agree almost exactly with the hand calculations. There is also excellent agreement between the shell-side pressure drops. However, there are significant differences in the shell-side Reynolds numbers and heat-transfer coefficients calculated by the two methods. The difference in Reynolds numbers is due to differences in the way $R e$ is defined in the two methods. As expected, the Simplified Delaware method gives a smaller value for the heat-transfer coefficient than does the full Delaware method. However, the difference is somewhat greater than expected, amounting to about $36 \%$ of the HEXTRAN value. This difference is reflected in the kerosene outlet temperature computed by HEXTRAN, $236^{\circ} \mathrm{F}$ versus the target temperature of $250^{\circ} \mathrm{F}$. Thus, according to HEXTRAN, the exchanger is over-sized. Also, notice that HEXTRAN adjusts the number of baffles and the end spacing to account for the thickness of the tubesheets. The baffle spacing is interpreted as baffle pitch since the tube length satisfies:

$$
L=\left(n_{b}-1\right) B+B_{\text {in }}+B_{\text {out }}+\text { total tubesheet thickness }
$$

## HEXTRAN Input File for Example 5.3

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=EX5-3, PROBLEM=KEROIL, SITE=
$
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
    ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
    PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
    UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=LBFH, WT=LB, *
    XDENSITY=API, STDVAPOR=379.490
$
PRINT ALL, *
    RATE=M
$
CALC PGEN=New, WATER=Saturated
$
$ Component Data Section
$
$ Thermodynamic Data Section
$
$Stream Data Section
$
STREAM DATA
$
PROP STRM=KEROSENE, NAME=KEROSENE, TEMP=390.00, PRES=50.000, *
    LIQUID (W)=45000.000, LCP (AVG) =0.59, Lcond (AVG) =0.079, *
    Lvis(AVG)=0.97, Lden (AVG) =49.008
$
    PROP STRM=4, NAME=4
$
    PROP STRM=OIL, NAME=OIL, TEMP=100.00, PRES=50.000, *
                LIQUID (W)=150000.000, LCP (AVG)=0.49, Lcond (AVG) =0.077, *
                Lvis (AVG) =8.7, Lden (AVG) =53.066
$
    PROP STRM=3, NAME=3
$
$ Calculation Type Section
$
SIMULATION
$
    TOLERANCE TTRIAL=0.01
$
    LIMITS AREA=200.00, 6000.00, SERIES=1, 10, PDAMP=0.00, *
            TTRIAL=30
$
    CALC TWOPHASE=Old, DPSMETHOD=Bell, MINFT=0.80
$
    PRINT UNITS, ECONOMICS, STREAM, STANDARD, *
        EXTENDED, ZONES
```


## HEXTRAN Input File for Example 5.3 (continued)

```
$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR
$
    UTCOST OIL=3.50, GAS=3.50, ELECTRICITY=0.10, *
        WATER=0.03, HPSTEAM=4.10, MPSTEAM=3.90, *
        LPSTEAM=3.60, REFRIGERANT=0.00, HEATINGMEDIUM=0.00
$
    HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        EXPONENT=0.60, CONSTANT=0.00, UNIT
$
$ Unit Operations Data
$
UNIT OPERATIONS
$
STE UID=STE1
    TYPE Old, TEMA=AES, HOTSIDE=Shellside, ORIENTATION=Horizontal, *
    FLOW=Countercurrent, *
    UESTIMATE=50.00, USCALER=1.00
TUBE FEED=OIL, PRODUCT=3, *
    LENGTH=14.00, OD=1.000, *
    BWG=14, NUMBER=124, PASS=4, PATTERN=90, *
    PITCH=1.2500, MATERIAL=1, *
    FOUL=0.003, LAYER=0, *
    DPSCALER=1.00
$
SHELL FEED=KEROSENE, PRODUCT=4, *
    ID=19.25, SERIES=1, PARALLEL=1, *
    SEALS=1, MATERIAL=1, *
    FOUL=0.002, LAYER=0, *
        DPSCALER=1.00
$
BAFF Segmental=Single, *
    CUT=0.20, *
    SPACING=3.850, *
    THICKNESS=0.1875, SHEETS=4.000
$
    TNOZZ TYPE=Conventional, ID=4.026, 4.026, NUMB=1, 1
$
    SNOZZ TYPE=Conventional, ID=3.068, 3.068, NUMB=1, 1
$
    CALC TWOPHASE=Old, *
        DPSMETHOD=Bell, *
        MINFT=0.80
$
    PRINT STANDARD, *
        EXTENDED, *
        ZONES
$
    COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        CONSTANT=0.00, EXPONENT=0.60, Unit
$
$ End of keyword file...
```


## HEXTRAN Output Data for Example 5.3



## HEXTRAN Output Data for Example 5-3 (continued)



## Example 5.4

Use HEXTRAN to design a shell-and-tube heat exchanger for the kerosene/crude-oil service of Example 5-1, and compare the resulting unit with the one designed previously by hand.

## Solution

The STE module in HEXTRAN is configured in design mode by right clicking on the unit and selecting Change Configuration from the pop-up menu. Exchanger parameters are set as in Example 5.3 , except for the following items that are left unspecified to be calculated by the program: number of tubes, tubesheet thickness, baffle spacing, number of sealing strips, and nozzle sizes. Design constraints are set as shown below, and the kerosene outlet temperature $\left(250^{\circ} \mathrm{F}\right)$ is given as the design specification on the Specifications form.


The HEXTRAN input file and Exchanger Data Sheets for this run (Run 1) are given below, and the results are compared with the hand calculations in the following table. In all cases, the tubes are $1-\mathrm{in}$. O.D., 14 BWG , on $1.25-\mathrm{in}$. square pitch. Notice that the nozzle diameters are rounded to one decimal place in the HEXTRAN output. The exact nozzle sizes determined by the program are the same as used in the hand calculations, namely, $4-\mathrm{in}$. schedule 40 on the tube side and $3-\mathrm{in}$. schedule 40 on the shell side.

| Item | Hand | Run 1 | Run 2 | Run 3 |
| :--- | :--- | :--- | :--- | :--- |
| Shell ID (in.) | 19.25 | 13.25 | 17.0 | 19.0 |
| Number of tubes | 124 | 47 | 79 | 99 |
| Tube length (ft) | 14 | 26 | 20 | 14 |
| Number of tube passes | 4 | 2 | 2 | 4 |
| Baffle cut (\%) | 20 | 24.9 | 22.9 | 22.3 |
| (Central) baffle spacing (in.) | 3.85 | 6.14 | 6.00 | 6.18 |
| Tube-side nozzle ID (in.) | 4.026 | 4.0 | 4.0 | 4.0 |
| Shell-side nozzle ID (in.) | 3.068 | 3.1 | 3.1 | 3.1 |
| $R e_{i}$ | 10,189 | 13,441 | 7997 | 12,762 |
| $\Delta P_{i}$ (psi) | 10.2 | 13.75 | 4.86 | 14.66 |
| $\Delta P_{o}$ (psi) | 2.2 | 3.55 | 1.74 | 1.04 |
| Surface area (ft ${ }^{2}$ ) | 454 | 322 | 419 | 366 |

All design criteria are met, but with a length of 26 ft and a diameter of only 13.25 in ., the configuration is awkward. In an attempt to obtain a more compact design, the maximum tube length was changed from 30 to 20 ft . The results for this run (Run 2) are given in the above table. As can be seen, the tube-side Reynolds number is in the transition region, which is undesirable.

A third run was made with the minimum number of tube passes set at four and the maximum tube length set at 20 ft . The Exchanger Data Sheet for this run is given below and the results are compared with those from the other runs in the table above. It can be seen that this run produced a configuration very similar to the one obtained by hand, albeit with less heat-transfer area due to the higher shell-side coefficient computed by HEXTRAN. Although the tube-side velocity is on the high side at $8.36 \mathrm{ft} / \mathrm{s}$, it is acceptable with carbon steel tubes. Checking the appropriate tube-count table (Table C.5) shows that a 17.25 in. shell should be adequate for a bundle containing 99 tubes. Since HEXTRAN specifies a 19 in . shell for this bundle, it is apparent that it uses a different set of tube-count data.

## HEXTRAN Input File for Example 5.4, Run 1

```
$
GENERATED FROM HEXTRAN KEYWORD EXPORTER $
$
$ General Data Section
$
TITLE PROJECT=Ex5-4, PROBLEM=KEROIL, SITE=
$
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
    ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
    PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
    UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=LBFH, WT=LB, *
    XDENSITY=API, STDVAPOR=379.490
$
PRINT ALL, *
    RATE=M
$
CALC PGEN=New, WATER=Saturated
$
```


## HEXTRAN Input File for Example 5.4, Run 1 (continued)

\$ Component Data Section
$\$$
\$ Thermodynamic Data Section
$\$$
\$
\$Stream Data Section
\$
STREAM DATA

## $\$$

PROP $S T R M=P S 2, \quad N A M E=P S 2$
\$
PROP STRM=OIL, NAME=OIL, TEMP=100.00, PRES=50.000, *
$\operatorname{LIQUID}(W)=150000.000, \operatorname{LCP}(A V G)=0.49, \operatorname{Lcond}(A V G)=0.077, *$ Lvis $(A V G)=8.7, \quad$ Lden $(A V G)=53.066$
\$
PROP $S T R M=P S 4, ~ N A M E=P S 4$
\$
PROP STRM=KEROSENE, NAME=KEROSENE, TEMP=390.00, PRES=50.000, * LIQUID $(W)=45000.000, ~ L C P(A V G)=0.59, ~ L C o n d(A V G)=0.079, ~ *$ Lvis $(A V G)=0.97, \quad \operatorname{Lden}(A V G)=49.008$
$\$$
\$ Calculation Type Section
\$
SIMULATION
\$
TOLERANCE TTRIAL=0.01
$\$$
LIMITS AREA $=200.00,6000.00, ~ S E R I E S=1,10, ~ P D A M P=0.00, *$ TTRIAL $=30$
$\$$
CALC TWOPHASE=New, DPSMETHOD=Stream, MINFT=0.80
$\$$
PRINT UNITS, ECONOMICS, STREAM, STANDARD, * EXTENDED, ZONES
$\$$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR \$

UTCOST OIL=3.50, GAS $=3.50, \mathrm{ELECTRICITY}=0.10$, * $W A T E R=0.03, ~ H P S T E A M=4.10, ~ M P S T E A M=3.90, *$ $\operatorname{LPSTEAM}=3.60, \operatorname{REFRIGERANT}=0.00, \mathrm{HEATINGMEDIUM}=0.00$
$\$$
HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, * EXPONENT $=0.60$, CONSTANT $=0.00, ~ U N I T$
\$
\$ Unit Operations Data
\$
UNIT OPERATIONS
$\$$

## HEXTRAN Input File for Example 5.4, Run 1 (continued)

```
STE UID=STE1
    TYPE New, TEMA=AES, HOTSIDE=Shellside, ORIENTATION=Horizontal, *
        FLOW=Countercurrent, AREA=200.00, 6000.00, *
        UESTIMATE=50.00, USCALER=1.00
    TUBE FEED=OIL, PRODUCT=PS4, *
        LENGTH=8.00, 30.00, 1.00, OD=1.000, *
        BWG=14, PASS=2, 16, 2, PATTERN=90, *
        PITCH=1.2500, MATERIAL=1, *
        FOUL=0.003, LAYER=0, *
        DPSCALER=1.00, DPSHELL=1.000, 15.000, VELOCITY=3.0, 10.0
$
SHELL FEED=KEROSENE, PRODUCT=PS2, *
        ID=8.00, 60.00, SERIES=1, 10, *
        MATERIAL=1, *
        FOUL=0.002, LAYER=0, *
        DPSCALER=1.00, DPSHELL=1.000, 15.000, VELOCITY=0.0, 1000.0
$
BAFF Segmental=Single, *
        CUT=0.20, 0.35, *
        THICKNESS=0.1875
$
    TNOZZ NUMB=1, 1
$
    SNOZZ NUMB=1, 1
$
    CALC TWOPHASE=Old, *
        DPSMETHOD=Bell, *
        MINFT=0.80
$
    SPEC Shell, Temp=250.000000
$
    PRINT STANDARD, *
        EXTENDED, *
        ZONES
$
COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
    CONSTANT=0.00, EXPONENT=0.60, Unit
$
$ End of keyword file...
```

HEXTRAN Output Data for Example 5.4, Run 1


## HEXTRAN Output Data for Example 5.4, Run 1 (continued)



## HEXTRAN Output Data for Example 5.4, Run 3



## HEXTRAN Output Data for Example 5.4, Run 3 (continued)



## References

1. Kern, D. Q. and A. D. Kraus, Extended Surface Heat Transfer, McGraw-Hill, New York, 1972.
2. Henry, J. A. R., Headers, nozzles and turnarounds, in Heat Exchanger Design Handbook, vol. 2, Hemisphere Publishing Corp., New York, 1988.
3. Bell, K. J. and A. C. Mueller, Wolverine Engineering Data Book II, Wolverine Tube, Inc., www.wlv.com, 2001.
4. Kern, D. Q., Process Heat Transfer, McGraw-Hill, New York, 1950.
5. Kakac, S. and H. Liu, Heat Exchangers: Selection, Rating and Thermal Design, CRC Press, Boca Raton, FL, 1998.
6. HEXTRAN Keyword Manual, Invensys Systems, Inc., Lake Forest, CA, 2002.
7. R. H. Perry and C. H. Chilton, eds, Chemical Engineers' Handbook, 5th edn, McGraw-Hill, New York, 1973.
8. Shah, R. K. and D. P. Sekulic, Fundamentals of heat exchanger design, Wiley, Hoboken, NJ, 2003.
9. Mukherjee, R., Effectively design shell-and-tube heat exchangers, Chem. Eng. Prog., 94, No. 2, 2137, 1998.
10. R. H. Perry and D. W. Green, eds, Perry's Chemical Engineers' Handbook, 7th edn, McGraw-Hill, New York, 1997.
11. Taborek, J., Shell-and-tube heat exchangers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
12. Standards of the Tubular Exchanger Manufacturers Association, 8th ed.,Tubular Exchanger Manufacturers Association, Inc., Tarrytown, NY, 1999.

## Appendix 5.A Hydraulic Equations in SI Units

The working equations for hydraulic calculations given in Section 5.3 are reformulated here in terms of SI units.
The pressure drop due to fluid friction in the tubes is calculated by the following equation:

$$
\begin{equation*}
\Delta P_{f}=\frac{f n_{p} L G^{2}}{2000 D_{i} s \phi} \tag{5.A.1}
\end{equation*}
$$

```
where
\(\Delta P_{f}=\) pressure drop ( \(P a\) )
    \(f=\) Darcy friction factor (dimensionless)
    \(n_{p}=\) number of tube passes
    \(L=\) tube length (m)
    \(G=\) mass flux \(\left(\mathrm{kg} / \mathrm{s} \cdot \mathrm{m}^{2}\right)\)
    \(D_{i}=\) tube ID (m)
    \(s=\) fluid specific gravity (dimensionless)
    \(\phi=\) viscosity correction factor (dimensionless)
        \(=\left(\mu / \mu_{w}\right)^{0.14}\) for turbulent flow
        \(=\left(\mu / \mu_{w}\right)^{0.25}\) for laminar flow
```

The above units for pressure drop and mass flux apply in the equations that follow as well. The minor losses on the tube side are estimated using the following equation:

$$
\begin{equation*}
\Delta P_{r}=5.0 \times 10^{-4} \alpha_{r} G^{2} / s \tag{5.A.2}
\end{equation*}
$$

where $\alpha_{r}$ is the number of velocity heads allocated for minor losses (Table 5.1). The pressure drop in the nozzles is estimated as follows:

$$
\begin{equation*}
\Delta P_{n}=7.5 \times 10^{-4} N_{s} G_{n}^{2} / s \quad \text { (turbulent flow) } \tag{5.A.3}
\end{equation*}
$$

$$
\begin{equation*}
\Delta P_{n}=1.5 \times 10^{-3} N_{s} G_{n}^{2} / s \quad \text { (laminar flow, } R e_{n} \geq 100 \text { ) } \tag{5.A.4}
\end{equation*}
$$

In these equations, $N_{s}$ is the number of shells connected in series.
The shell-side pressure drop, excluding nozzle losses, is computed using the following equation:

$$
\begin{equation*}
\Delta P_{f}=\frac{f G^{2} d_{s}\left(n_{b}+1\right)}{2000 D_{e} s \phi} \tag{5.А.5}
\end{equation*}
$$

where
$\Delta P_{f}=$ pressure drop $(P a)$
$f=$ shell-side friction factor (dimensionless)
$G=$ mass flux $=\dot{m} / a_{s}\left(\mathrm{~kg} / \mathrm{s} \cdot \mathrm{m}^{2}\right)$
$a_{s}=$ flow area across tube bundle ( $\mathrm{m}^{2}$ )
$=d_{S} C^{\prime} B / P_{T}$
$d_{s}=$ shell ID (m)
$C^{\prime}=$ clearance (m)
$B=$ baffle spacing (m)
$P_{T}=$ tube pitch (m); replaced by $P_{T} / \sqrt{2}$ for $45^{\circ}$ tube layouts
$n_{b}=$ number of baffles
$D_{e}=$ equivalent diameter from Fig. 3.12 (m)
$s=$ fluid specific gravity (dimensionless)
$\phi=$ viscosity correction factor $=\left(\mu / \mu_{w}\right)^{0.14}$ (dimensionless)

## Appendix 5.B Maximum Tube-Side Fluid Velocities

The data presented here are from Bell and Mueller [3]. The maximum velocities are based on prevention of tube wall erosion and are material specific. They are intended to serve as a supplement to the general guideline of $V_{\max }=8 \mathrm{ft} / \mathrm{s}$ for liquids given in Section 5.7.4.

Maximum velocities for water are given in Table 5.B.1. For liquids other than water, multiply the values from the table by the factor $\left(\rho_{\text {water }} / \rho_{\text {fluid }}\right)^{0.5}$.

Table 5.B.1 Maximum Recommended Velocities for Water in Heat-Exchanger Tubes

| Tube material | $V_{\max }(\mathrm{ft} / \mathrm{s})$ |
| :--- | :---: |
| Plain carbon steel | 10 |
| Stainless steel | 15 |
| Aluminum | 6 |
| Copper | 6 |
| $90-10$ cupronickel | 10 |
| $70-30$ cupronickel | 15 |
| Titanium | $>50$ |

For gases flowing in plain carbon steel tubing, the following equation can be used to estimate the maximum velocity:

$$
\begin{equation*}
V_{\max }=\frac{1800}{(P M)^{0.5}} \tag{5.B.1}
\end{equation*}
$$

where
$V_{\max }=$ maximum velocity ( $\mathrm{ft} / \mathrm{s}$ )
$P=$ gas pressure (psia)
$M=$ molecular weight of gas
For tubing materials other than plain carbon steel, assume the maximum velocities are in the same ratio as given in Table 5.B. 1 for water.

For example, to estimate the maximum velocity for air at 50 psia flowing in aluminum tubes, first calculate the velocity for plain carbon steel tubing using Equation 5.B.1:

$$
\left(V_{\max }\right)_{c s}=\frac{1800}{(50 \times 29)^{0.5}}=43.7 \mathrm{ft} / \mathrm{s}
$$

Then multiply by the ratio $(6 / 10)$ from Table 5.B.1 to obtain the velocity for aluminum tubing:

$$
V_{\max }=0.6 \times 47.3=28.4 \cong 28 \mathrm{ft} / \mathrm{s}
$$

## Appendix 5.C Maximum Unsupported Tube Lengths

In order to prevent tube vibration and sagging, TEMA standards specify maximum unsupported tube lengths for two groups of materials. Material group A consists of steel, steel alloys, nickel, nickel-copper alloys and nickel-chromium-steel alloys. Material group B consists of aluminum and its alloys, copper and its alloys, and titanium alloys at their upper temperature limit. For tube diameters between 19 mm and 51 mm , the standards are well-approximated by the following equations [11]:

Group A: maximum unsupported length $(\mathrm{mm})=52 D_{o}(\mathrm{~mm})+532$
Group B: maximum unsupported length $(\mathrm{mm})=46 D_{o}(\mathrm{~mm})+436$
These equations apply to un-finned tubes. The standards for finned tubes are more complicated, but can be estimated by using the above equations with the tube OD replaced by the root-tube diameter. The standards also include temperature limits above which the unsupported length must be reduced [12]. For convenience, values computed from Equations (5.C.1) and (5.C.2) are tabulated below.

Table 5.C. 1 Maximum Unsupported Straight Tube Lengths in Inches (mm)

| Tube OD | Material group A | Material group B |
| :--- | :---: | :---: |
| $0.75(19.1)$ | $60(1525)$ | $52(1315)$ |
| $0.875(22.2)$ | $66(1686)$ | $57(1457)$ |
| $1.0(25.4)$ | $73(1853)$ | $63(1604)$ |
| $1.25(31.8)$ | $86(2186)$ | $75(1899)$ |
| $1.5(38.1)$ | $99(2513)$ | $86(2189)$ |
| $2.0(50.8)$ | $125(3174)$ | $109(2773)$ |

The baffle spacing is generally restricted to be no greater than half the tabled values because tubes in the baffle windows are supported by every other baffle. However, the inlet and outlet baffle spacings are often larger than the central baffle spacing. In this case, the central spacing must satisfy the following relation:

$$
\begin{equation*}
B \leq \text { tabled value }-\max \left(B_{\text {in }}, B_{o u t}\right) \tag{5.C.3}
\end{equation*}
$$

In practice, the actual unsupported tube length should be kept safely below ( $80 \%$ or less) the TEMA limit.

## Appendix 5.D Comparison of Head Types for Shell-and-Tube Exchangers

Table 5.D. 1 Comparison of Stationary Head Types

| Head type | Advantages | Disadvantages |
| :---: | :---: | :---: |
| A, L | (1) Tubesheet easily accessible by removing channel cover <br> (2) Head can be removed if unrestricted access to tubesheet is required | (1) Most expensive type except for D <br> (2) Not well suited for high tube-side pressures; tube-side fluid can leak to environment through gasket at tubesheet <br> (3) Type L rear head used only with fixed tubesheets |
| B, M | (1) Low cost <br> (2) Removal of head provides unrestricted access to tubesheet <br> (3) Absence of channel cover eliminates one external gasket where leakage to environment can occur | (1) Head must be disconnected from process piping and removed to access tubesheet <br> (2) Not well suited for high tube-side pressures; tube-side fluid can leak to environment through gasket at tubesheet <br> (3) Type M rear head used only with fixed tubesheets |
| C | (1) Low cost <br> (2) Tubesheet easily accessed by removing channel cover <br> (3) Suitable for high pressures; channel cover seal is the only external gasket | (1) Head and tubesheet materials must be compatible for welding <br> (2) All tube-side maintenance must be done with channel in place <br> (3) Used only with removable tube bundles |
| D | (1) Least prone to leakage <br> (2) Best option when product of channel diameter and tube-side pressure exceeds about $86,000 \mathrm{in}$. psia | (1) Not cost effective unless tube-side pressure is high |
| N | (1) Least expensive <br> (2) Tubesheet easily accessed by removing channel cover <br> (3) Suitable for high pressures; channel cover seal is the only external gasket | (1) Head, tubesheet and shell materials must be compatible for welding <br> (2) Used only with fixed tubesheets <br> (3) All tube-side maintenance must be done with channel in place |

Table 5.D. 2 Comparison of Floating-Head Types

| Head type | Advantages | Disadvantages |
| :---: | :---: | :---: |
| P | (1) No internal gaskets where leakage and fluid mixing can occur | (1) Shell-side fluid can leak through packing to environment <br> (2) Shell-side $T\left(<600^{\circ} \mathrm{F}\right)$ and $P(<300 \mathrm{psia})$ are limited by packing |
| S | (1) Largest heat-transfer area per shell for an internal floating-head design <br> (2) Leakage is contained within shell | (1) Floating head must be disassembled to remove tube bundle <br> (2) Single tube pass requires special construction <br> (3) Leakage at internal gasket can result in mixing of fluids |
| T | (1) Bundle can be removed without removing rear shell cover or disassembling floating head <br> (2) Leakage is contained within shell <br> (3) Good option for kettle reboilers | (1) Smallest heat-transfer area per shell <br> (2) Most expensive design <br> (3) Single tube pass requires special construction <br> (4) Leakage at internal gasket can result in mixing of fluids |
| W | (1) Least expensive floating head design <br> (2) No internal gaskets where leakage and fluid mixing can occur | (1) Both fluids can leak through packing to environment <br> (2) Both tube-side and shell-side $T\left(<375^{\circ} \mathrm{F}\right)$ and $P(<150-300$ psia depending on shell size) are limited by packing <br> (3) Maximum of 2 tube passes |

U-tubes provide a less expensive alternative to a floating head. In common with type P and W floating heads (and all stationary heads), U-tube bundles have no internal gaskets where leakage and fluid mixing can occur. The main disadvantages are:
(1) Cleaning interior tube surfaces is more difficult due to U-bends.
(2) Except for outermost tubes in bundle, individual tube replacement is not practical.
(3) Cannot be used if a single tube pass is required.

## Notations

$A \quad$ Heat-transfer surface area
$A_{\text {fins }} \quad$ Surface area of fins
$A_{i} \quad \pi D_{i} L=$ Internal surface area of tube
$A_{\text {prime }}$ Prime surface area
$A_{\text {req }} \quad$ Required heat-transfer surface area
$A_{\text {Tot }} \quad A_{\text {prime }}+A_{\text {fins }}=$ Total external surface area of a finned tube
$a_{s} \quad$ Flow area across tube bundle
$B \quad$ Baffle spacing
$B_{c} \quad$ Baffle cut
$B_{\text {in }} \quad$ Inlet baffle spacing

| $B_{o u t}$ | Outlet baffle spacing |
| :--- | :--- |
| $B W G$ | Birmingham wire gage |
| $b$ | Fin height |
| $C_{P}$ | Heat capacity at constant pressure |
| $C^{\prime}$ | Clearance between tubes in bundle |
| $D$ | Diameter |
| $D_{e}$ | Equivalent diameter |
| $D_{i}$ | Internal diameter of tube |
| $D_{n}$ | Internal diameter of nozzle |
| $D_{o}$ | External diameter of tube |
| $D_{r}$ | External diameter of root tube |
| $\hat{D}_{r}$ | Effective root tube diameter |
| $d_{e}$ | Equivalent diameter expressed in inches |
| $d_{s}$ | Internal diameter of shell |
| $F$ | LMTD correction factor |
| $f$ | Darcy friction factor |
| $f_{1}$ | Friction factor from Figure 5.1 for $B / d_{s}=1.0$ |
| $f_{2}$ | Friction factor from Figure 5.1 for $B / d_{s}=0.2$ |
| $G$ | Mass flux |
| $G_{n}$ | Mass flux in nozzle |
| $h$ | Heat-transfer coefficient |
| $h_{i}$ | Tube-side heat-transfer coefficient |
| $h_{o}$ | Shell-side heat-transfer coefficient |
| $j_{H}$ | (hod $/ k) P r 1 / 3$ ( $\left.\mu / \mu_{w}\right)^{-0.14}=$ Modified Colburn factor for shell-side heat-transfer |
| $k$ | Thermal conductivity |
| $L$ | Tube length |
| $M$ | Molecular weight |
| $\dot{m}$ | Mass flow rate |
| $\dot{m}_{t}$ | Total mass flow rate of tube-side fluid |
| $N_{s}$ | Number of shells connected in series |
| $N_{u}$ | Nusselt number |
| $n_{b}$ | Number of baffles |
| $n_{f}$ | Number of fins per unit length of tube |
| $n_{p}$ | Number of tube passes |
| $n_{t}$ | Number of tubes in tube bundle |
| $\left(n_{t}\right)_{r e q}$ | Required number of tubes |
| $P$ | Pressure; parameter used to calculate LMTD correction factor |
| $P r$ | Prandtl number |
| $P_{T}$ | Tube pitch |
| $q$ | Rate of heat-transfer |
| $R$ | Parameter used to calculate LMTD correction factor |
| $R_{D}$ | Total fouling factor |
| $R_{D i}$ | Fouling factor for tube-side fluid |
| $R_{D o}$ | Fouling factor for shell-side fluid |
| $R e$ | Reynolds number |
| $r_{1}$ | External radius of root tube |
| $r_{2}$ | Outer radius of annular fin |
| $r_{2 c}$ | $r_{2}+\tau / 2=$ Corrected fin radius |
| $s$ | Specific gravity |
| $T$ | Temperature |
| $T_{a v e}$ | Average temperature of shell-side fluid |
| $T_{p}$ | Average temperature of prime surface in a finned-tube heat exchanger |
|  |  |

$T_{w t d}$ Weighted average temperature of finned surface in a finned-tube heat exchanger
$t_{\text {ave }} \quad$ Average temperature of tube-side fluid
$U \quad$ Overall heat-transfer coefficient
$U_{C} \quad$ Clean overall heat-transfer coefficient
$U_{D} \quad$ Design overall heat-transfer coefficient
$U_{\text {req }}$ Required overall heat-transfer coefficient
$V \quad$ Fluid velocity
$V_{\max }$ Maximum fluid velocity based on erosion prevention
$V_{n} \quad$ Fluid velocity in nozzle

## Greek Letters

| $\alpha_{r}$ | Number of velocity heads allocated for tube-side minor pressure losses |
| :--- | :--- |
| $\beta$ | Parameter in Equation (5.15) |
| $\Delta P$ | Pressure drop |
| $\Delta P_{f}$ | Pressure drop due to fluid friction in straight sections of tubes or in shell |
| $\Delta P_{i}$ | Total pressure drop for tube-side fluid |
| $\Delta P_{n}$ | Pressure drop in nozzles |
| $\Delta P_{o}$ | Total pressure drop for shell-side fluid |
| $\Delta P_{r}$ | Tube-side pressure drop due to tube entrance, exit and return losses |
| $\Delta T$ | Temperature difference |
| $\Delta T_{\text {ln }}$ | Logarithmic mean temperature difference |
| $\left(\Delta T_{\text {ln }}\right)_{c f}$ | Logarithmic mean temperature difference for counter-current flow |
| $\eta_{f}$ | Fin efficiency |
| $\eta_{w}$ | Weighted efficiency of finned surface |
| $\mu$ | Viscosity |
| $\mu_{w}$ | Fluid viscosity evaluated at average temperature of tube wall |
| $\rho$ | Fluid density |
| $\tau$ | Fin thickness |
| $\phi$ | Viscosity correction factor |
| $\phi_{i}$ | Viscosity correction factor for tube-side fluid |
| $\phi_{o}$ | Viscosity correction factor for shell-side fluid |
| $\psi$ | Parameter in equation for efficiency of annular fins |

## Problems

(5.1) Consider the following modified configuration for the kerosene/oil exchanger of Example 5.1:

$$
\begin{array}{ll}
d_{s}=17.25 \text { in. } & \text { tubes: } 1 \text {-in., } 14 \text { BWG on } 1.25 \text {-in. square pitch } \\
n_{t}=104 & \text { tube-side nozzles: } 4 \text {-in. schedule } 40 \\
n_{p}=4 & \text { shell-side nozzles: } 3 \text {-in. schedule } 40 \\
B / d_{s}=0.2 &
\end{array}
$$

As discussed in Example 5.1, the values of $R e_{i}$ and $h_{i}$ are the same for this configuration as for the initial configuration. Complete the design calculations for the modified configuration by calculating the following:
(a) $h_{o}$
(b) $U_{D}$
(c) The required tube length, rounded upward to the nearest foot.
(d) $\Delta P_{i}$
(e) $\Delta P_{o}$
(f) Over-surface and over-design
(g) Tube-side velocity

Ans. (a) $141 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (b) $51 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (c) 15 ft (d) 14.4 psi . (e) 3.4 psi (f) $45 \%$ and $4.1 \%$. (g) $7.96 \mathrm{ft} / \mathrm{s}$
(5.2) A fixed-tubesheet heat exchanger will use $3 / 4$ in. tubes, 20 ft long on 1 in . triangular pitch. It will require two shell-side passes and a total of four tube-side passes. A minimum of 1100 tubes will be required to handle the heat duty. If standard type E shells are used:
(a) What size shells will be required?
(b) What will be the approximate tube count for the exchanger?

Ans. (a) $d_{s}=27$ in. (b) $n_{t}=1148$
(5.3) A shell-and-tube heat exchanger on the used equipment lot at a chemical plant has the following configuration.

| Shell | Tube bundle |
| :--- | :--- |
| Type $=$ AES | Number of tubes $=84$ |
| ID $=13.25 \mathrm{in}$. | Tube OD $=0.75 \mathrm{in}$. |
| Baffle type $=$ segmental | BWG $=16$ |
| Baffle cut $=20 \%$ | Length $=20 \mathrm{ft}$ |
| Baffle spacing $=5.3$ in. (central) | Number of passes $=6$ |
| $\quad=8.7 \mathrm{in}$. (inlet/outlet) | Pitch $=1 \mathrm{in}$. (square) |
| Number of baffles $=43$ | Sealing strips: 1 pair |
| Nozzles: 3 -in. schedule 40 | Nozzles: 3-in. schedule 40 |

It is contemplated to use this unit in a new service for which the shell-side fluid will have the following properties:

| Shell-side fluid property | Value |
| :--- | :--- |
| $\dot{m}(\mathrm{lb} / \mathrm{h})$ | 50,000 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.5 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.25 |
| $\mu(\mathrm{cp})$ | 1.1 |
| $s$ | 0.86 |

The tube-side fluid will be water with a flow rate of $30,000 \mathrm{lb} / \mathrm{h}$ and a range of $80^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$. A maximum pressure drop of 12 psi has been specified for each stream. Determine if the exchanger will be hydraulically suitable for the service by calculating:
(a) The tube-side pressure drop
(b) The shell-side pressure drop
(c) The tube-side velocity

Ans. (a) 11 psi . (b) 2.9 psi . (c) $4.6 \mathrm{ft} / \mathrm{s}$.
(5.4) A shell-and-tube heat exchanger in a chemical process was designed to cool the shell-side fluid to a specified temperature. When clean, the heat exchanger performs adequately, but after two months of operation, the outlet temperature begins to rise above the design temperature, which causes inefficient operation of down-stream equipment. A process engineer has suggested that the problem can be solved by increasing the flow rate of the cold (tube-side) fluid, which is available in excess. She has stated that this will improve the performance of the exchanger by:

- Reducing fouling
- Increasing the heat-transfer coefficient
- Increasing the mean temperature difference in the unit

Comment on the engineer's proposed solution by addressing each of her three points as follows:

- Is the argument reasonable? Why or why not?
- Are there possible fallacies in her reasoning?

Finally, discuss any potential adverse consequences that might be associated with the proposed solution.
(5.5) The second design modification considered for the finned-tube heat exchanger of Example 5.2 was to use a $29-\mathrm{in}$. shell containing 532 tubes. Complete the design of this unit by following the procedure outlined at the end of Example 5.2.
(5.6) $60,000 \mathrm{lb} / \mathrm{h}$ of a petroleum fraction will be cooled from $250^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ using water with a range of $85^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$. For each stream, the inlet pressure will be 50 psia and a maximum pressure drop of 10 psi is specified. A fouling factor of $0.002 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for each stream. The petroleum fraction is not corrosive and its properties may be assumed constant at the values given below.

| Petroleum fraction property | Value |
| :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.52 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.074 |
| $\mu(\mathrm{cp})$ | 2.75 |
| $s$ | 0.82 |
| $P r$ | 46.7 |

(a) Develop an initial configuration for a shell-and-tube heat exchanger with plain (unfinned) tubes to meet this service.
(b) Perform the rating calculations for the initial configuration developed in part (a).
(c) Based on the results of the rating calculations in part (b), specify what changes, if any, should be made to the configuration of the heat exchanger for the next trial.
(d) Use HEXTRAN or other available software to rate the initial configuration developed in part (a).
(5.7) Work problem 5.6 for a shell-and-tube exchanger with finned tubes.
(5.8) $90,000 \mathrm{lb} / \mathrm{h}$ of benzene will be heated from $75^{\circ} \mathrm{F}$ to $145^{\circ} \mathrm{F}$ by cooling a stream of orthotoluidine from $230^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$. Inlet pressures are 45 psia for ortho-toluidine and 50 psia for benzene. A maximum pressure drop of 10 psi is specified for each stream. Properties of ortho-toluidine at $190^{\circ} \mathrm{F}$ are given below.

| o-Toluidine property | Value at $190^{\circ} \mathrm{F}$ |
| :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.51 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.0765 |
| $\mu(\mathrm{cp})$ | $0.91^{*}$ |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 58.6 |
| $P r$ | 14.7 |
| ${ }^{*} \log _{10} \mu(\mathrm{cp})=1085.1\left\{\frac{1}{T(K)}-\frac{1}{356.46}\right\}$. |  |

(a) Develop an initial configuration for a shell-and-tube heat exchanger to meet this service.
(b) Perform the rating calculations for the initial configuration developed in part (a).
(c) Based on the results of the rating calculations in part (b), specify what changes, if any, should be made to the configuration of the heat exchanger for the next trial.
(d) Use HEXTRAN or other available software to rate the initial configuration developed in part (a).
(5.9) $85,000 \mathrm{lb} / \mathrm{h}$ of amyl acetate ( n -pentyl acetate, $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ ) will be cooled from $175^{\circ} \mathrm{F}$ to $125^{\circ} \mathrm{F}$ by heating a stream of amyl alcohol (l-pentanol) from $75^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$. Inlet pressures are 45 psia for the acetate and 50 psia for the alcohol. A maximum pressure drop of 7 psi is specified for each stream. Specific gravities are 0.81 for the alcohol and 0.83 for the acetate.
(a) Develop an initial configuration for a shell-and-tube heat exchanger to meet this service.
(b) Perform the rating calculations for the initial configuration developed in part (a).
(c) Based on the results of the rating calculations in part (b), specify what changes, if any, should be made to the configuration of the heat exchanger for the next trial.
(d) Obtain a final design for the heat exchanger.
(5.10) Develop an initial configuration for a shell-and-tube heat exchanger to meet the service of problem 5.9 if the temperature ranges are $175^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$ for amyl acetate and $80^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ for amyl alcohol.
(5.11) $320,000 \mathrm{lb} / \mathrm{h}$ of oil $\left(32^{\circ} \mathrm{API}, K_{w}=12.0\right)$ will be cooled from $260^{\circ} \mathrm{F}$ to $130^{\circ} \mathrm{F}$ using treated water from a cooling tower with a range of $80^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$. For each stream, the inlet pressure will be 50 psia and a maximum pressure drop of 12 psi is specified. A fouling factor of $0.002 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for the oil stream, which is not corrosive. Properties of the oil are given below.

| Oil property | Value at $195^{\circ} \mathrm{F}$ |
| :--- | :---: |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.53 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.068 |
| $\mu(\mathrm{cp})$ | $3.12^{*}$ |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 50.5 |
| $P r$ | 58.8 |
| ${ }^{\mu} \mu(\mathrm{cp})=0.00488 \exp \left[4230.8 / T\left({ }^{\circ} R\right)\right]$. |  |

(a) Develop an initial configuration for a shell-and-tube heat exchanger to meet this service. Use plain (un-finned) tubes.
(b) Perform the rating calculations for the initial configuration obtained in part (a).
(c) Based on the results of the rating calculations in part (b), specify what changes, if any, should be made to the configuration of the heat exchanger for the next trial.
(d) Obtain a final design for the heat exchanger.
(5.12) Work problem 5.11 for a shell-and-tube exchanger with finned tubes. Use $90-10$ coppernickel alloy tubes with 26 fins per inch.
(5.13) $150,000 \mathrm{lb} / \mathrm{h}$ of kerosene will be heated from $75^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$ by cooling a gasoline stream from $160^{\circ} \mathrm{F}$ to $120^{\circ} \mathrm{F}$. Inlet pressure will be 50 psia for each stream and maximum pressure drops of 7 psi for gasoline and 10 psi for kerosene are specified. Published fouling factors for oil refinery streams should be used for this application. Stream properties may be assumed constant at the values given below. Design a shell-and-tube heat exchanger for this service.

| Property | Gasoline | Kerosene |
| :--- | :--- | :---: |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.55 | 0.48 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.087 | 0.081 |
| $\mu(\mathrm{cp})$ | 0.45 | 1.5 |
| $s$ | 0.74 | 0.82 |
| $P r$ | 6.88 | 21.5 |

(5.14) Rate the initial configuration obtained for the acetate-alcohol heat exchanger in Problem 5.10.
(5.15) $60,000 \mathrm{lb} / \mathrm{h}$ of acetone will be cooled from $250^{\circ} \mathrm{F}$ to $100^{\circ} \mathrm{F}$ using $185,000 \mathrm{lb} / \mathrm{h}$ of $100 \%$ acetic acid which is available at $90^{\circ} \mathrm{F}$. Inlet pressures will be 100 psia for acetone and 50 psia for acetic acid. A maximum pressure drop of 10 psi is specified for each stream.
(a) Develop an initial configuration for a shell-and-tube heat exchanger to meet this service.
(b) Rate the initial configuration obtained in part (a).
(c) Use HEXTRAN or other available software to rate the configuration obtained in part (a).

Note: Particular care is required in selecting materials of construction for this application. Corrosion rate data, such as the charts and tables presented in Chapter 23 of the 5th edition of Chemical Engineers'Handbook, should be carefully analyzed as part of the decision-making process.
(5.16) For the service of Problem 5.6, use HEXTRAN or other available software to design a shell-and-tube heat exchanger using:
(a) Plain tubes
(b) Finned tubes.
(5.17) Use HEXTRAN or other available software to design a shell-and-tube heat exchanger for the service of Problem 5.8.
(5.18) Use HEXTRAN or other available software to design a shell-and-tube heat exchanger for the service of Problem 5.9.
(5.19) Use HEXTRAN or other available software to design a shell-and-tube heat exchanger for the service of Problem 5.10.
(5.20) Use HEXTRAN or other available software to design a shell-and-tube heat exchanger for the service of Problem 5.11 using:
(a) Plain tubes
(b) 90-10 copper-nickel alloy tubes with 26 fins per inch.
(5.21) Use HEXTRAN or other available software to design a shell-and-tube heat exchanger for the service of Problem 5.13.
(5.22) Use HEXTRAN or other available software to design a shell-and-tube heat exchanger for the service of Problem 5.15.
(5.23) $250,000 \mathrm{lb} / \mathrm{h}$ of a hydrocarbon liquid $\left(30^{\circ} \mathrm{API}, K_{w}=11.5\right)$ are to be cooled from $225^{\circ} \mathrm{F}$ to $135^{\circ} \mathrm{F}$ using treated water from a cooling tower that is available at $80^{\circ} \mathrm{F}$. The hydrocarbon is not corrosive, but a fouling factor of $0.0025 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for this stream. Inlet pressure will be 50 psia for each stream with a maximum pressure drop of 10 psi . Use HEXTRAN or other suitable software to design a shell-and-tube heat exchanger for this service using:
(a) Plain tubes
(b) Finned tubes.
(5.24) $200,000 \mathrm{lb} / \mathrm{h}$ of lube oil $\left(26^{\circ} \mathrm{API}, K_{\mathrm{w}}=12.2\right)$ will be cooled from $440^{\circ} \mathrm{F}$ to $350^{\circ} \mathrm{F}$ by heating a light gas oil $\left(33^{\circ} \mathrm{API}, K_{\mathrm{w}}=11.8\right)$ from $310^{\circ} \mathrm{F}$ to $370^{\circ} \mathrm{F}$. The inlet pressure of each stream will be 50 psia and maximum pressure drops of 15 psi for the lube oil and 10 psi for the gas oil are specified. Design a shell-and-tube heat exchanger for this service using HEXTRAN or other suitable software.
(5.25) A tube bundle consists of low-fin tubes containing 26 fins per inch laid out on a 1-in. triangular pitch. The fins have an average height of 0.049 in . and an average thickness of 0.013 in . The diameter of the root tube is 0.652 in . Calculate the clearance and equivalent diameter to be used in the Simplified Delaware Method.
Ans. 0.313 and 0.908 in.
(5.26) A tube bundle consists of 1-in., $14 \mathrm{BWG}, 26 \mathrm{fpi}$ low-fin tubes on a 1.25 -in. square pitch. Tube and fin dimensions are as given in Table B.5. Calculate the clearance and equivalent diameter to be used in the Simplified Delaware Method.

Ans. 0.314 and 1.19 in.
(5.27) In Examples 5.1 and 5.2 over-surface and over-design were calculated using the equations:

$$
\begin{aligned}
& \text { over-surface }=\frac{U_{C}}{U_{r e q}}-1 \\
& \text { over-design }=\frac{U_{D}}{U_{r e q}}-1
\end{aligned}
$$

Show that these equations follow from the definitions of over-surface and over-design given in Chapter 4.
(5.28) Use HEXTRAN or other available software to rate the final design obtained for the finnedtube heat exchanger of Example 5.2. Compare the results of the computer calculations with those of the hand calculations in Example 5.2.

This page intentionally left blank

## THE DELAWARE METHOD

## Contents

6.1 Introduction 246
6.2 Ideal Tube Bank Correlations 246
6.3 Shell-Side Heat-Transfer Coefficient 248
6.4 Shell-Side Pressure Drop 250
6.5 The Flow Areas 254
6.6 Correlations for the Correction Factors 259
6.7 Estimation of Clearances 260

### 6.1 Introduction

The Delaware method for calculating the shell-side heat-transfer coefficient and pressure drop derives its name from a large industry sponsored study of shell-and-tube heat exchangers conducted at the University of Delaware, the final report of which was published in 1963 [1]. The method is often referred to as the Bell-Delaware method, after one of the principal investigators on the project, Kenneth J. Bell.

The Delaware method utilizes empirical correlations for the heat-transfer coefficient and friction factor in flow perpendicular to banks of tubes; these are referred to as ideal tube bank correlations. In baffled heat exchangers, this type of flow is approximated in the regions between the baffle tips. In the baffle windows, however, the flow is partly parallel to the tubes. Furthermore, only part of the shell-side fluid follows the main flow path through the exchanger due to the presence of leakage and bypass streams in the shell. These deviations from ideal tube bank conditions are accounted for by a set of empirical correction factors for heat transfer and pressure drop. The correction factors for leakage and bypass flows are correlated in terms of the flow areas for the leakage, bypass, and main cross-flow streams.

Slightly different versions of the Delaware method have been published in various handbooks and textbooks, e.g., [2-6]. The presentation in this chapter is based on the version given by Taborek [2]. Consideration is restricted to exchangers with standard type E shells, single-cut segmental baffles, and un-finned tubes. The extension of the method to other configurations is discussed in Refs. [2,5,6].

### 6.2 Ideal Tube Bank Correlations

The flow perpendicular to banks of tubes has been widely studied and a number of different correlations for heat transfer and pressure drop are available in the literature. Any of these correlations can, in principle, be used with the Delaware method. The correlation originally used in the development of the Delaware method has been recommended by Taborek [2], and is used herein. The correlation is in the form of three graphs (Figures 6.1-6.3), one for each of the commonly used tube bundle configurations.

The nomenclature for Figures 6.1-6.3 is as follows:

```
    \(f=\) Fanning friction factor, dimensionless
    \(j=\frac{h P r^{2 / 3}}{C_{P} G \phi}\), dimensionless
    \(h=\) heat-transfer coefficient, Btu/h \(\cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\left(\mathrm{W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)\)
\(C_{P}=\) heat capacity of shell-side fluid, \(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}(\mathrm{J} / \mathrm{kg} \cdot \mathrm{K})\)
    \(G=\dot{m}_{o} / S_{m}=\) mass flux of shell-side fluid, \(1 \mathrm{bm} / \mathrm{h} \cdot \mathrm{ft}^{2}\left(\mathrm{~kg} / \mathrm{s} \cdot \mathrm{m}^{2}\right)\)
\(\dot{m}_{o}=\) total mass flow rate of shell-side fluid, \(1 \mathrm{bm} / \mathrm{h}(\mathrm{kg} / \mathrm{s})\)
\(S_{m}=\) cross-flow area at shell centerline, \(\mathrm{ft}^{2}\left(\mathrm{~m}^{2}\right)\)
\(\operatorname{Pr}=\) Prandtl number, dimensionless
    \(\phi=\) viscosity correction factor, dimensionless
\(P_{T}=\) tube pitch, \(\mathrm{ft}(\mathrm{m})\)
\(D_{o}=\) tube OD, ft (m)
\(R e=D_{o} G / \mu\), dimensionless
    \(\mu=\) viscosity of shell-side fluid, \(\mathrm{lbm} / \mathrm{ft} \cdot \mathrm{h}(\mathrm{kg} / \mathrm{m} \cdot \mathrm{s})\)
```

Note that the Reynolds number is based on the tube OD rather than the equivalent diameter used in the Simplified Delaware method. The cross-flow area, $S_{m}$, used to calculate the mass flux is approximated by the area, $a_{s}$, used in the Simplified Delaware method. More precise equations for calculating $S_{m}$ are given in Section 6.5 below.


Figure 6.1 Ideal tube bank correlation for square pitch (Source: Ref. [2]).


Figure 6.2 Ideal tube bank correlation for triangular pitch (Source: Ref. [2]).


Figure 6.3 Ideal tube bank correlation for rotated square pitch (Source: Ref. [2]).

Approximate curve fits for Figures 6.1-6.3 are as follows [2]:

$$
\begin{align*}
& j=a_{1}\left(\frac{1.33}{P_{T} / D_{o}}\right)^{a}(R e)^{a_{2}}  \tag{6.1}\\
& f=b_{1}\left(\frac{1.33}{P_{T} / D_{o}}\right)^{b}(R e)^{b_{2}} \tag{6.2}
\end{align*}
$$

where

$$
\begin{align*}
a & =\frac{a_{3}}{1+0.14(R e)^{a_{4}}}  \tag{6.3}\\
b & =\frac{b_{3}}{1+0.14(R e)^{b_{4}}} \tag{6.4}
\end{align*}
$$

The constants to be used in these equations are given in Table 6.1.

### 6.3 Shell-Side Heat-Transfer Coefficient

The heat-transfer coefficient for an ideal tube bank is designated $h_{\text {ideal }}$. This value is obtained from the appropriate graph, Figures 6.1-6.3, or from Equations (6.1)-(6.4). The shell-side heat-transfer

Table 6.1 Constants for use with Equations 6.1-6.4

| Layout <br> angle | Reynolds <br> number | $a_{1}$ | $a_{2}$ | $a_{3}$ | $a_{4}$ | $b_{1}$ | $b_{2}$ | $b_{3}$ | $b_{4}$ |
| :--- | :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $30^{\circ}$ | $10^{5}-10^{4}$ | 0.321 | -0.388 | 1.450 | 0.519 | 0.372 | -0.123 | 7.00 | 0.500 |
|  | $10^{4}-10^{3}$ | 0.321 | -0.388 |  |  | 0.486 | -0.152 |  |  |
|  | $10^{3}-10^{2}$ | 0.593 | -0.477 |  |  | 4.570 | -0.476 |  |  |
|  | $10^{2}-10$ | 1.360 | -0.657 |  |  | 45.100 | -0.973 |  |  |
|  | $<10$ | 1.400 | -0.667 |  |  | 48.000 | -1.000 |  |  |
| $45^{\circ}$ | $10^{5}-10^{4}$ | 0.370 | -0.396 | 1.930 | 0.500 | 0.303 | -0.126 | 6.59 | 0.520 |
|  | $10^{4}-10^{3}$ | 0.370 | -0.396 |  |  | 0.333 | -0.136 |  |  |
|  | $10^{3}-10^{2}$ | 0.730 | -0.500 |  |  | 3.500 | -0.476 |  |  |
|  | $10^{2}-10$ | 0.498 | -0.656 |  |  | 26.200 | -0.913 |  |  |
|  | $<10$ | 1.550 | -0.667 |  |  | 32.000 | -1.000 |  |  |
|  | $10^{5}-10^{4}$ | 0.370 | -0.395 | 1.187 | 0.370 | 0.391 | -0.148 | 6.30 | 0.378 |
|  | $10^{4}-10^{3}$ | 0.107 | -0.266 |  |  | 0.0815 | +0.022 |  |  |
|  | $10^{3}-10^{2}$ | 0.408 | -0.460 |  |  | 6.0900 | -0.602 |  |  |
|  | $10^{2}-10$ | 0.900 | -0.631 |  |  | 32.1000 | -0.963 |  |  |
|  | 10 | 0.970 | -0.667 |  |  | 35.0000 | -1.000 |  |  |

Source: Ref. [2].
coefficient, $h_{o}$, is obtained by multiplying $h_{\text {ideal }}$ by a set of correction factors that account for the non-idealities in a baffled heat exchanger:

$$
\begin{equation*}
h_{o}=h_{\text {ideal }}\left(J_{C} J_{L} J_{B} J_{R} J_{S}\right) \tag{6.5}
\end{equation*}
$$

where
$J_{C}=$ correction factor for baffle window flow
$J_{L}=$ correction factor for baffle leakage effects
$J_{B}=$ correction factor for bundle bypass effects
$J_{R}=$ laminar flow correction factor
$J_{S}=$ correction factor for unequal baffle spacing
The factor $J_{C}$ accounts for heat transfer in the baffle windows. It has a value of 1.0 for exchangers with no tubes in the windows. For other exchangers, it ranges from about 0.65 for very large baffle cuts to about 1.15 for small baffle cuts. For well-designed exchangers, the value of $J_{C}$ is usually close to 1.0 [2].
The $J_{L}$ correction factor accounts for both the tube-to-baffle and shell-to-baffle leakage streams. These streams flow from one baffle space to the next through the gaps between the tubes and the baffle and the gap between the shell and the baffle. The shell-to-baffle leakage stream is the more detrimental to heat transfer because it flows outside the tube bundle near the shell wall and does not contact any of the tubes. Hence, $J_{L}$ decreases as the shell-to-baffle leakage fraction increases. The practical range of $J_{L}$ is from about 0.2 to 1.0 , with values of $0.7-0.8$ being typical. For a well-designed exchanger, $J_{L}$ should not be less than about 0.6 [2]. Smaller values indicate the need for design changes to decrease the size of the leakage streams, e.g., increasing the baffle spacing.

The bundle bypass stream flows around the periphery of the tube bundle from one baffle window to the next in the gap between the outermost tubes and the shell. It is accounted for by the factor $J_{B}$, which typically has values in the range of $0.7-0.9$. Lower values indicate the need to add sealing
strips, which force the bypass stream back into the tube bundle. The resulting improvement in heat transfer is reflected in an increase in the value of $J_{B}$ with the number of pairs of sealing strips.

The baffle spacing in the inlet and outlet sections is often larger than in the remainder of the exchanger in order to accommodate the nozzles and, in the case of U-tube exchangers, the return bends. The resulting decrease in heat transfer rate is accounted for by the factor $J_{S}$, which is usually in the range of $0.85-1.0$ [2]. If the baffle spacing is the same throughout the exchanger, $J_{S}$ has a value of 1.0.

The factor $J_{R}$ accounts for the decrease in the heat-transfer coefficient with downstream distance in laminar flow. The effect is analogous to the $(L)^{-1 / 3}$ dependence of the tube-side coefficient as expressed in the Seider-Tate equation for laminar flow. The range of $J_{R}$ is from about 0.4 to 1.0 , and it is equal to 1.0 for $R e \geq 100$.

For well-designed heat exchangers, the product of all the correction factors should not be less than about 0.5 [2]. A smaller value obtained during the design process indicates the need for appropriate design modifications. Correlations for calculating the correction factors are given in Section 6.6 below.

### 6.4 Shell-Side Pressure Drop

The nozzle-to-nozzle pressure drop in a type E shell is composed of three parts:

$$
\begin{equation*}
\Delta P_{f}=\Delta P_{c}+\Delta P_{w}+\Delta P_{e} \tag{6.6}
\end{equation*}
$$

where
$\Delta P_{c}=$ pressure drop in all central baffle spaces
$\Delta P_{w}=$ pressure drop in all baffle windows
$\Delta P_{e}=$ pressure drop in the entrance and exit baffle spaces
The three regions of the shell corresponding to $\Delta P_{c}, \Delta P_{w}$, and $\Delta P_{e}$ are shown schematically in Figure 6.4.

### 6.4.1 Calculation of $\Delta P_{c}$

Between the baffle tips the flow pattern is considered to be pure cross flow. Therefore, the pressure drop in one central baffle space is equal to the ideal tube bank pressure drop corrected for leakage


Figure 6.4 Flow regions considered for shell-side pressure drop. (a) Cross-flow region between baffle tips in the central baffle spaces, (b) window-flow region and (c) cross-flow region for inlet and outlet baffle spaces (Source: Ref. [2]).
and bypass effects. The ideal tube bank pressure drop is given by:

$$
\begin{equation*}
\Delta P_{\text {ideal }}=\frac{2 f_{\text {ideal }} N_{c} G^{2}}{g_{c} \rho \phi} \tag{6.7}
\end{equation*}
$$

```
where
    \(f_{\text {ideal }}=\) ideal tube bank friction factor, dimensionless
    \(N_{c}=\) number of tube rows crossed between baffle tips, dimensionless
            \(G=\dot{m}_{o} / S_{m}=\) mass flux, \(\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}\left(\mathrm{~kg} / \mathrm{s} \cdot \mathrm{m}^{2}\right)\)
            \(g_{c}=4.17 \times 10^{8}\left(\mathrm{lbm} \cdot \mathrm{ft} / \mathrm{h}^{2}\right) / \mathrm{lbf}=1.0\left(\mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}\right) / \mathrm{N}\)
            \(\rho=\) fluid density, \(\mathrm{lbm} / \mathrm{ft}^{3}\left(\mathrm{~kg} / \mathrm{m}^{3}\right)\)
\(\Delta P_{\text {ideal }} \propto \mathrm{lbf} / \mathrm{ft}^{2}(\mathrm{~Pa})\)
```

The number of tube rows crossed by the fluid between baffle tips is calculated as:

$$
\begin{equation*}
N_{c}=\frac{D_{s}\left(1-2 B_{c}\right)}{P_{T}^{\prime}} \tag{6.8}
\end{equation*}
$$

where
$D_{s}=$ shell ID, ft (m)
$B_{c}=$ (fractional) baffle cut, dimensionless
$P_{T}^{\prime}=P_{T}$ for square tube layout
$=P_{T} \cos \theta_{t p}$ for triangular $\left(\theta_{t p}=30^{\circ}\right)$ and rotated square $\left(\theta_{t p}=45^{\circ}\right)$ tube layouts
The numerator in Equation (6.8) is the length of the baffle over which cross flow occurs (refer to Figure 6.4(a)), while the denominator is the center-to-center distance between tube rows in the flow direction, i.e., the tube pitch projected onto the flow direction.

The pressure drop in all central baffle spaces is obtained by multiplying the ideal tube bank pressure drop by correction factors to account for the leakage and bypass streams, and then multiplying by the number of central baffle spaces. Thus,

$$
\begin{equation*}
\Delta P_{c}=\left(n_{b}-1\right) \Delta P_{\text {ideal }} R_{L} R_{B} \tag{6.9}
\end{equation*}
$$

where
$n_{b}=$ number of baffles
$R_{L}=$ leakage correction factor
$R_{B}=$ bypass correction factor
The correction factors $R_{L}$ and $R_{B}$ are analogous to the factors $J_{L}$ and $J_{B}$ for heat transfer. The practical range of $R_{L}$ is from about 0.1 to 1.0 , with values of $0.4-0.6$ being typical. For $R_{B}$ the practical range is from about 0.3 to 1.0 , with values of $0.4-0.7$ being typical. As is the case for $J_{B}$, values of $R_{B}$ increase with the number of pairs of sealing strips.

### 6.4.2 Calculation of $\Delta P_{w}$

In the baffle windows the fluid undergoes a $180^{\circ}$ change of direction (Figure 6.4(b)). The Delaware method allows 2 velocity heads for the associated pressure loss. There is an additional pressure loss in the windows due to fluid friction. The latter is handled by empirical correlations, one each for laminar $(R e<100)$ and turbulent $(R e \geq 100)$ flow. (The Reynolds number here is the same one used in the ideal tube bank correlation.)

The ideal (uncorrected) pressure drop in one baffle window for turbulent flow is given by:

$$
\begin{equation*}
\Delta P_{w, i d e a l}=\frac{\left(2+0.6 N_{c w}\right) \dot{m}_{o}^{2}}{2 g_{c} \rho S_{m} S_{w}} \tag{6.10}
\end{equation*}
$$

where
$N_{c w}=$ effective number of tube rows crossed in one baffle window
$S_{w}=$ window flow area, $\mathrm{ft}^{2}\left(\mathrm{~m}^{2}\right)$
$\Delta P_{w, i \text { ideal }} \propto \mathrm{lbf} / \mathrm{ft}^{2}(\mathrm{~Pa})$
Note that the total mass flow of shell-side fluid is used here, even though the leakage streams do not flow through the windows. Also, the flow area used in Equation (6.10) is the geometric mean of the cross flow and window flow areas, i.e., $\left(S_{m} S_{w}\right)^{1 / 2}$. The effective number of tube rows crossed in the window is given by:

$$
\begin{equation*}
N_{c w}=\frac{0.8 B_{c} D_{s}}{P_{T}^{\prime}} \tag{6.11}
\end{equation*}
$$

In this equation, $B_{c} D_{s}$ is the length of the baffle cut, while the denominator gives the center-to-center distance between tube rows in the cross-flow direction. Hence, without the factor of 0.8 , Equation (6.11) would give the number of tube rows in the cross-flow direction in one baffle window. The empirical factor of 0.8 accounts for the fact that the flow in the baffle windows is partly across the tubes and partly parallel to the tubes.

For laminar flow,

$$
\begin{equation*}
\Delta P_{w, \text { ideal }}=\frac{26 v \dot{m}_{o}}{g_{c} \sqrt{S_{m} S_{w}}}\left[\frac{N_{c w}}{P_{T}-D_{o}}+\frac{B_{c} D_{s}}{D_{w}^{2}}\right]+\frac{\dot{m}_{o}^{2}}{g_{c} \rho S_{m} S_{w}} \tag{6.12}
\end{equation*}
$$

where
$\nu=$ kinematic viscosity of shell-side fluid, $\mathrm{ft}^{2} / \mathrm{h}\left(\mathrm{m}^{2} / \mathrm{s}\right)$
$D_{w}=$ equivalent diameter for window flow, $\mathrm{ft}(\mathrm{m})$
The equivalent diameter for a baffle window is defined in the usual manner as 4 times the flow area divided by the wetted perimeter, except that the baffle edge is omitted from the wetted perimeter term:

$$
\begin{equation*}
D_{w}=\frac{4 S_{w}}{\pi D_{o} n_{t} \times 0.5\left(1-F_{c}\right)+D_{s} \theta_{d s}} \tag{6.13}
\end{equation*}
$$

where
$n_{t}=$ number of tubes in bundle
$F_{c}=$ fraction of tubes in cross flow between baffle tips
$\theta_{d s}=$ baffle window angle (rad) defined in Figure 6.5
Note that $0.5\left(1-F_{c}\right)$ is the fraction of tubes in one baffle window, so that the first term in the denominator of Equation (6.13) represents the total wetted perimeter of all the tubes in the baffle window. See Section 6.5.2 below for calculation of $F_{c}$.

The pressure drop in all the baffle windows is obtained by multiplying $\Delta P_{w \text {,ideal }}$ by the number or baffle windows (equal to the number of baffles, $n_{b}$ ) and by the leakage correction factor, $R_{L}$. No correction is made for the bundle bypass flow because the bypass stream is considered to flow through the windows along with the main cross-flow stream. Thus,

$$
\begin{equation*}
\Delta P_{w}=n_{b} \Delta P_{w, \text { ideal }} R_{L} \tag{6.14}
\end{equation*}
$$



Figure 6.5 Segmental baffle geometry. $B_{c}=$ baffle cut (\%) (Source: Ref. [2]).

### 6.4.3 Calculation of $\Delta P_{e}$

The inlet and outlet baffle spaces differ in several respects from the central baffle spaces. As previously mentioned, the baffle spacing in one or both of the end zones may differ from the central baffle spacing in order to accommodate the shell-side nozzles or the return bends in U-tube exchangers. Also, the number of tube rows crossed in the end baffle spaces includes the rows in one baffle window, in addition to the tube rows between the baffle tips (refer to Figure 6.4(c)). Finally, the correction for leakage is not applicable to the inlet and outlet spaces because the leakage streams have not yet developed at the inlet and have already rejoined the main flow at the outlet.

The pressure drop in the entrance and exit baffle spaces is obtained by correcting the ideal pressure drop given by Equation (6.7) for the additional number of tube rows crossed, for the altered baffle spacing, and for the effects of the bundle bypass stream. The result is:

$$
\begin{equation*}
\Delta P_{e}=2 \Delta P_{\text {ideal }}\left(1+\frac{N_{c w}}{N_{c}}\right) R_{B} R_{S} \tag{6.15}
\end{equation*}
$$

where $R_{S}=$ correction factor for unequal baffle spacing.
The practical range of $R_{S}$ is from about 0.3 to 1.0. When the baffle spacing is uniform throughout the shell, the value of $R_{S}$ is 1.0 .

### 6.4.4 Summary

Equations (6.6), (6.9), (6.14), and (6.15) can be combined to give the following equation for shell-side pressure drop (excluding nozzle losses):

$$
\begin{equation*}
\Delta P_{f}=\left[\left(n_{b}-1\right) \Delta P_{\text {ideal }} R_{B}+n_{b} \Delta P_{w, \text { ideal }}\right] R_{L}+2 \Delta P_{\text {ideal }}\left(1+N_{c w} / N_{c}\right) R_{B} R_{S} \tag{6.16}
\end{equation*}
$$

The ideal tube bank pressure drop, $\Delta P_{\text {ideal }}$, is obtained from Equation (6.7). The uncorrected window pressure drop, $\Delta P_{w, \text { ideal }}$, is calculated using Equation (6.10) for turbulent flow ( $R e \geq 100$ ) or Equation (6.13) for laminar flow ( $R e<100$ ).
Correlations for calculating the correction factors $R_{L}, R_{B}$, and $R_{S}$ are given in Section 6.6 below.

### 6.5 The Flow Areas

### 6.5.1 The cross-flow area

The cross-flow area, $S_{m}$, is the minimum flow area in one central baffle space at the center of the tube bundle. It is calculated by the following equation:

$$
\begin{equation*}
S_{m}=B\left[\left(D_{s}-D_{o t l}\right)+\frac{\left(D_{o t l}-D_{o}\right)}{\left(P_{T}\right)_{e f f}}\left(P_{T}-D_{o}\right)\right] \tag{6.17}
\end{equation*}
$$

where

$$
B=\text { central baffle spacing }
$$

$D_{\text {otl }}=$ outer tube limit diameter
$\left(P_{T}\right)_{\text {eff }}=P_{T}$ for square and triangular layouts
$=P_{T} / \sqrt{2}$ for rotated square layout
The outer tube limit diameter is the diameter of the circle that circumscribes the tube bundle (see Figure 6.5). It is also referred to as the tube bundle diameter.

From Figure 6.5, it can be seen that the term $\left(D_{s}-D_{o t l}\right)$ in Equation (6.17) is equal to twice the clearance between the tube bundle and the shell. The corresponding flow area on each side of the bundle is a rectangle of width $0.5\left(D_{s}-D_{o t t}\right)$ and length equal to the baffle spacing, $B$. The sum of these two areas is $B\left(D_{s}-D_{o t l}\right)$, which is the first term in Equation (6.17).

The second term in Equation (6.17) represents the minimum flow area between tubes within the bundle. For square $\left(90^{\circ}\right)$ layouts the tubes are aligned in the flow direction (Figure 6.6), and the width, $L_{1}$, of the openings through which the fluid flows is the tube clearance, $C^{\prime}=P_{T}-D_{0}$. The length of the openings is the baffle spacing, $B$, and the number of openings across the center of the bundle is $D_{c t l} / P_{T}=\left(D_{o t l}-D_{o}\right) / P_{T}$, where $D_{c t l}$ is the central tube limit diameter defined in Figure 6.5. Thus, the total area of these openings is given by the second term in Equation (6.17), with $\left(P_{T}\right)_{e f f}=P_{T}$.

For triangular and rotated-square tube layouts, the tubes are staggered in the flow direction (Figure 6.6). The fluid first flows through an opening of width $L_{1}$, and then through two openings, each of width $L_{2}$. The minimum flow area through the bundle is determined by the smaller of $L_{1}$ and $2 L_{2}$. For triangular layouts, $L_{1}=L_{2}=P_{T}-D_{o}$, and hence, $L_{1}<2 L_{2}$. The minimum opening is therefore a rectangle of width $\left(P_{T}-D_{o}\right)$ and length $B$. The number of openings across the center of the bundle is again $\left(D_{o t l}-D_{o}\right) / P_{T}$, which results in the same expression for the total area as for square layouts.


Figure 6.6 Aligned and staggered tube layouts. (a) Staggered and (b) inline square layout.

For rotated-square layouts, $L_{1}=\sqrt{2} P_{T}-D_{o}$ and $L_{2}=P_{T}-D_{o}$. With the dimensions used in standard tube layouts, $2 L_{2}<L_{1}$ in this case. Therefore, the minimum flow area per opening is $2 B\left(P_{T}-D_{o}\right)$, and the number of openings across the center of the bundle is $\left(D_{o t l}-D_{o}\right) /\left(\sqrt{2} P_{T}\right)$. Hence, the total flow area within the bundle is given by the second term in Equation (6.17) with the factor of $\sqrt{2}$ included in $\left(P_{T}\right)_{\text {eff }}$.

### 6.5.2 Tube-to-baffle leakage area

The holes in the baffles through which the tubes pass are slightly larger in diameter than the tubes, allowing leakage of fluid through the gaps from one baffle space to the next. The tube-to-baffle leakage area is the total area of the gaps in one baffle. Denoting the tube-to-baffle clearance by $\delta_{t b}$, the area of one gap is:

$$
\begin{equation*}
\left(S_{t b}\right)_{1}=\frac{\pi}{4}\left[\left(D_{o}+2 \delta_{t b}\right)^{2}-D_{o}^{2}\right] \cong \pi D_{o} \delta_{t b} \tag{6.18}
\end{equation*}
$$

The approximation in Equation (6.18) is valid because $\delta_{t b} \ll D_{o}$.
Now the fraction of tubes that pass through one baffle is equal to the fraction, $F_{c}$, between the baffle tips plus the fraction, $F_{w}$, in one baffle window. These quantities are related by:

$$
\begin{equation*}
F_{c}+2 F_{w}=1.0 \tag{6.19}
\end{equation*}
$$

Therefore,

$$
\begin{equation*}
F_{w}=\left(1-F_{c}\right) / 2 \tag{6.20}
\end{equation*}
$$

It follows that:

$$
\begin{equation*}
F_{c}+F_{w}=F_{c}+0.5\left(1-F_{c}\right)=0.5\left(1+F_{c}\right) \tag{6.21}
\end{equation*}
$$

Hence, the total leakage area for one baffle is given by:

$$
\begin{equation*}
S_{t b}=0.5 \pi D_{o} \delta_{t b} n_{t}\left(1+F_{c}\right) \tag{6.22}
\end{equation*}
$$

The fraction of tubes in one baffle window is estimated as the fractional area of the circle of radius $D_{c t l}$ that lies in the window (refer to Figure 6.5). The central tube limit diameter, $D_{c t l}$, is the diameter of the circle that passes through the centers of the outermost tubes in the bundle. It is obvious from Figure 6.5 that:

$$
\begin{equation*}
D_{c t l}=D_{o t l}-D_{o} \tag{6.23}
\end{equation*}
$$

The fractional area in the window depends on the angle $\theta_{c t l}$ shown in Figure 6.5. The triangle formed by the baffle edge and two radii of length $\frac{1}{2} D_{c t l}$ is shown in Figure 6.7. Also shown is the right triangle formed by cutting the large triangle in half. The height of this triangle is half the length of the central portion of the baffle, i.e., $\frac{1}{2} D_{s}\left(1-2 B_{c}\right)$. It can be seen from Figure 6.7 that:

$$
\begin{equation*}
\cos \left(\frac{1}{2} \theta_{c t l}\right)=\frac{\frac{1}{2} D_{s}\left(1-2 B_{c}\right)}{\frac{1}{2} D_{c t l}}=\frac{D_{s}\left(1-2 B_{c}\right)}{D_{c t l}} \tag{6.24}
\end{equation*}
$$

Solving for $\theta_{c t l}$ gives:

$$
\begin{equation*}
\theta_{c t l}=2 \cos ^{-1}\left[\frac{D_{s}\left(1-2 B_{c}\right)}{D_{c t l}}\right] \tag{6.25}
\end{equation*}
$$



Figure 6.7 Baffle geometry used for calculating the fraction, $F_{w}$, of tubes in one baffle window; $B_{c}=$ fractional baffle cut.

Now the length of the baffle edge in the small triangle of Figure 6.7 is $\frac{1}{2} D_{c t l} \sin \left(\frac{1}{2} \theta_{c t l}\right)$, and this is equal to one-half the base of the large triangle. Thus, the area of the large triangle is:

$$
\begin{aligned}
& A_{\text {triangle }}=\frac{1}{2} \text { base } \times \text { height } \\
& A_{\text {triangle }}=\frac{1}{2} D_{\text {ctl }} \sin \left(\frac{1}{2} \theta_{c t l}\right)\left[\frac{1}{2} D_{s}\left(1-2 B_{c}\right)\right]
\end{aligned}
$$

Multiplying and dividing by $D_{c t l}$ on the right side of this equation gives:

$$
\begin{equation*}
A_{\text {triangle }}=\frac{1}{4} D_{c t l}^{2} \sin \left(\frac{1}{2} \theta_{c t l}\right)\left[\frac{D_{s}\left(1-2 B_{c}\right)}{D_{c t l}}\right] \tag{6.26}
\end{equation*}
$$

Using Equation (6.24), Equation (6.26) can be written as:

$$
\begin{equation*}
A_{\text {triangle }}=\frac{1}{4} D_{c t l}^{2} \sin \left(\frac{1}{2} \theta_{c t l}\right) \cos \left(\frac{1}{2} \theta_{c t l}\right) \tag{6.27}
\end{equation*}
$$

Using the double-angle formula,

$$
\begin{equation*}
\sin \theta_{c t l}=2 \sin \left(\frac{1}{2} \theta_{c t l}\right) \cos \left(\frac{1}{2} \theta_{c t l}\right) \tag{6.28}
\end{equation*}
$$

Combining Equations (6.27) and (6.28) yields:

$$
\begin{equation*}
A_{\text {triangle }}=\frac{1}{8} D_{c t l}^{2} \sin \theta_{c t l} \tag{6.29}
\end{equation*}
$$

The area of the circular sector subtended by angle $\theta_{\text {ctl }}$ is:

$$
\begin{equation*}
A_{\text {sector }}=\frac{\pi}{4} D_{c t l}^{2} \frac{\theta_{c t l}}{2 \pi}=\frac{1}{8} D_{c t l}^{2} \theta_{c t l} \tag{6.30}
\end{equation*}
$$

where $\theta_{c t l}$ is in radians. Now the area of the circle lying in the baffle window is:

$$
\begin{equation*}
A_{\text {sector }}-A_{\text {triangle }}=\frac{1}{8} D_{c t l}^{2}\left(\theta_{c t l}-\sin \theta_{c t l}\right) \tag{6.31}
\end{equation*}
$$

Finally, the fractional area lying in the window is equated with $F_{w}$ :

$$
\begin{equation*}
F_{w}=\frac{A_{\text {sector }}-A_{\text {triangle }}}{A_{\text {circle }}} \tag{6.32}
\end{equation*}
$$

Substituting for the areas gives:

$$
F_{w}=\frac{\frac{1}{8} D_{c t l}^{2}\left(\theta_{c t l}-\sin \theta_{c t l}\right)}{(\pi / 4) D_{c t l}^{2}}
$$

or

$$
\begin{equation*}
F_{w}=\frac{1}{2 \pi}\left(\theta_{c t l}-\sin \theta_{c t l}\right) \tag{6.33}
\end{equation*}
$$

From Equation (6.19),

$$
\begin{equation*}
F_{c}=1-2 F_{w} \tag{6.34}
\end{equation*}
$$

Combining Equations (6.33) and (6.34) yields:

$$
\begin{equation*}
F_{c}=1+\frac{1}{\pi}\left(\sin \theta_{c t l}-\theta_{c t l}\right) \tag{6.35}
\end{equation*}
$$

In summary, the calculation of the tube-to-baffle leakage area involves the following steps:

- Calculate $\theta_{c t l}$ using Equation (6.25).
- Calculate $F_{c}$ using Equation (6.35).
- Calculate $S_{t b}$ using Equation (6.22).


### 6.5.3 Shell-to-baffle leakage area

The shell-to-baffle leakage area, $S_{s b}$, is shown in Figure 6.8. Denoting the clearance between the baffle and shell by $\delta_{s b}$ and noting that $\delta_{s b} \ll D_{s}$, the leakage area can be written as follows:

$$
\begin{equation*}
S_{s b}=\pi D_{s} \delta_{s b}\left(\frac{2 \pi-\theta_{d s}}{2 \pi}\right) \tag{6.36}
\end{equation*}
$$

or

$$
\begin{equation*}
S_{s b}=D_{s} \delta_{s b}\left(\pi-0.5 \theta_{d s}\right) \tag{6.37}
\end{equation*}
$$

where the baffle window angle, $\theta_{d s}$ (Figure 6.5), is expressed in radians.


Figure 6.8 Shell-to-baffle leakage area. The shaded region between the baffle and shell is the leakage area, $S_{s b}$.

The baffle geometry in Figure 6.7 remains valid if $D_{c t l}$ and $\theta_{c t l}$ are replaced by $D_{s}$ and $\theta_{d s}$, respectively. It follows that:

$$
\begin{equation*}
\cos \left(\frac{1}{2} \theta_{d s}\right)=\frac{\frac{1}{2} D_{s}\left(1-2 B_{c}\right)}{\frac{1}{2} D_{s}}=1-2 B_{c} \tag{6.38}
\end{equation*}
$$

and

$$
\begin{equation*}
\theta_{d s}=2 \cos ^{-1}\left(1-2 B_{c}\right) \tag{6.39}
\end{equation*}
$$

### 6.5.4 The bundle bypass flow area

The bundle bypass flow area, $S_{b}$, is the area between the outermost tubes and the shell at the shell centerline in one central baffle space. It is part of the cross-flow area, $S_{m}$, and in fact is represented by the first term in Equation (6.17). Thus,

$$
\begin{equation*}
S_{b}=B\left(D_{s}-D_{o t l}\right) \tag{6.40}
\end{equation*}
$$

### 6.5.5 The window flow area

The flow area in one baffle window, $S_{w}$, is the gross window area, $S_{w g}$, minus the area occupied by the tubes in the window. The gross window area is the open area between the shell and the baffle edge formed by the baffle cuts (Figure 6.9). It is equal to the area of the circular sector subtended by angle $\theta_{d s}$ minus the area of the triangle formed by the baffle edge and two radii of length $0.5 D_{s}$. The derivation is the same as that for Equation (6.31) with $D_{c t l}$ and $\theta_{c t l}$ replaced by $D_{s}$ and $\theta_{d s}$, respectively. Thus,

$$
\begin{equation*}
S_{w g}=\frac{1}{8} D_{s}^{2}\left(\theta_{d s}-\sin \theta_{d s}\right) \tag{6.41}
\end{equation*}
$$

The area occupied by the tubes in the window is simply the cross-sectional area per tube times the number of tubes in the window:

$$
\begin{equation*}
A_{t u b e s}=n_{t} F_{w}\left(\pi D_{o}^{2} / 4\right) \tag{6.42}
\end{equation*}
$$

The window flow area is given by:

$$
\begin{equation*}
S_{w}=S_{w g}-A_{t u b e s} \tag{6.43}
\end{equation*}
$$



Figure 6.9 Gross window area; $B_{c}=$ fractional baffle cut.

Substituting from Equations (6.41) and (6.42) gives:

$$
\begin{equation*}
S_{w}=\frac{1}{8} D_{s}^{2}\left(\theta_{d s}-\sin \theta_{d s}\right)-\frac{1}{4} n_{t} F_{w} \pi D_{o}^{2} \tag{6.44}
\end{equation*}
$$

### 6.6 Correlations for the Correction Factors

### 6.6.1 Correction factor for baffle window flow

The correction factor, $J_{c}$, expresses the effect on heat transfer of flow in the baffle windows. It depends on the number of tubes in the windows versus the number in cross flow between the baffle tips, which is determined by the baffle cut, $B_{c}$, and the diametral ratio $D_{s} / D_{c t l}$. The correction factor is correlated in terms of a single parameter, $F_{c}$, the fraction of tubes in cross flow between the baffle tips. For the practical range of baffle cuts ( $15-45 \%$ ), the correlation is well represented by a linear relationship [2]:

$$
\begin{equation*}
J_{c}=0.55+0.72 F_{c} \tag{6.45}
\end{equation*}
$$

### 6.6.2 Correction factors for baffle leakage

The correction factors, $J_{L}$ and $R_{L}$, express the effects of the tube-to-baffle and shell-to-baffle leakage streams on heat transfer and pressure drop, respectively. Both factors are correlated in terms of the following area ratios:

$$
\begin{align*}
& r_{s}=\frac{S_{s b}}{S_{s b}+S_{t b}}  \tag{6.46}\\
& r_{l}=\frac{S_{s b}+S_{t b}}{S_{m}} \tag{6.47}
\end{align*}
$$

The correlations are well approximated by the following equations [2]:

$$
\begin{gather*}
J_{L}=0.44\left(1-r_{s}\right)+\left[1-0.44\left(1-r_{s}\right)\right] \exp \left(-2.2 r_{l}\right)  \tag{6.48}\\
R_{L}=\exp \left[-1.33\left(1+r_{s}\right)\left(r_{l}\right)^{P}\right] \tag{6.49}
\end{gather*}
$$

where

$$
\begin{equation*}
p=0.8-0.15\left(1+r_{s}\right) \tag{6.50}
\end{equation*}
$$

### 6.6.3 Correction factors for bundle bypass flow

The correction factors, $J_{B}$ and $R_{B}$, express the effects of the bundle bypass flow on heat transfer and pressure drop, respectively. Both factors depend on the ratio, $S_{b} / S_{m}$, of bypass flow area to cross-flow area, and the number of pairs of sealing strips. The latter enters the correlation as the ratio, $r_{s s}$ :

$$
\begin{equation*}
r_{s s}=N_{s s} / N_{c} \tag{6.51}
\end{equation*}
$$

where
$N_{s s}=$ number of pairs of sealing strips
$N_{c}=$ number of tube rows crossed between baffle tips
The correlations can be expressed in terms of the following equations [2]:

$$
\begin{array}{ll}
J_{B}=\exp \left[-C_{J}\left(S_{b} / S_{m}\right)\left(1-\sqrt[3]{2 r_{s s}}\right)\right] & \text { for } r_{s s}<0.5 \\
J_{B}=1.0 & \text { for } r_{s s} \geq 0.5 \tag{6.52}
\end{array}
$$

where
$C_{J}=1.35$ for $R e<100$
$=1.25$ for $R e \geq 100$

$$
\begin{array}{ll}
R_{B}=\exp \left[-C_{R}\left(S_{b} / S_{m}\right)\left(1-\sqrt[3]{2 r_{s s}}\right)\right] & \text { for } r_{s s}<0.5 \\
R_{B}=1.0 & \text { for } r_{s s} \geq 0.5 \tag{6.53}
\end{array}
$$

where
$C_{R}=4.5$ for $R e<100$
$=3.7$ for $R e \geq 100$

### 6.6.4 Correction factors for unequal baffle spacing

The correction factors, $J_{S}$ and $R_{S}$, depend on the inlet baffle spacing, $B_{i n}$, the outlet baffle spacing, $B_{\text {out }}$, the central baffle spacing, $B$, and the number of baffles, $n_{b}$. They are calculated from the following equations [2]:

$$
\begin{equation*}
J_{S}=\frac{\left(n_{b}-1\right)+\left(B_{\text {in }} / B\right)^{\left(1-n_{1}\right)}+\left(B_{\text {out }} / B\right)^{\left(1-n_{1}\right)}}{\left(n_{b}-1\right)+\left(B_{\text {in }} / B\right)+\left(B_{\text {out }} / B\right)} \tag{6.54}
\end{equation*}
$$

where
$n_{1}=0.6$ for $R e \geq 100$
$n_{1}=\frac{1}{3} \quad$ for $R e<100$

$$
\begin{equation*}
R_{S}=0.5\left[\left(B / B_{\text {in }}\right)^{\left(2-n_{2}\right)}+\left(B / B_{\text {out }}\right)^{\left(2-n_{2}\right)}\right] \tag{6.55}
\end{equation*}
$$

where
$n_{2}=0.2$ for $R e \geq 100$
$n_{2}=1.0$ for $R e<100$
Note that for $B_{\text {in }}=B_{\text {out }}=B$, Equations (6.54) and (6.55) give $J_{S}=R_{S}=1.0$.

### 6.6.5 Laminar flow correction factor

The correction factor, $J_{R}$, accounts for the fact that in laminar flow the heat-transfer coefficient decreases with downstream distance, which in the present context is interpreted as the number of tube rows crossed. The correlating parameter is the total number, $N_{c t}$, of tube rows crossed in the entire exchanger, i.e., in the inlet, outlet, and central baffle spaces, and in the baffle windows. Thus,

$$
\begin{equation*}
N_{c t}=\left(n_{b}+1\right)\left(N_{c}+N_{c w}\right) \tag{6.56}
\end{equation*}
$$

where $N_{c}$ and $N_{c w}$ are given by Equations (6.8) and (6.11), respectively.
The correlation for $J_{R}$ is as follows [2]:

$$
\begin{array}{ll}
J_{R}=\left(10 / N_{c t}\right)^{0.18} & \text { for } R e \leq 20 \\
J_{R}=1.0 & \text { for } R e \geq 100 \tag{6.57}
\end{array}
$$

For $20<R e<100, J_{R}$ is calculated by linear interpolation between the above values.

### 6.7 Estimation of Clearances

Determination of the flow areas (Section 6.5) requires the values of three clearances, namely, the tube-to-baffle clearance, $\delta_{t b}$, the shell-to-baffle clearance, $\delta_{s b}$, and the bundle-to-shell diametral clearance, $D_{s}-D_{\text {otl }}$. When rating an existing exchanger, these values may be available from the
manufacturer's drawings and specifications. When the latter are unavailable, and for all design calculations, the clearances must be estimated. The estimation procedures given here are based on the recommendations of Taborek [2], which incorporate Tubular Exchanger Manufacturers Association (TEMA) standards and prevailing practice.
The TEMA specifications [7] for tube-to-baffle clearance are based on tube bundle assembly and tube vibration considerations, and depend on the tube size. For tube OD greater than 1.25 in ., $\delta_{t b}$ is specified as 0.4 mm . For tubes with OD of 1.25 in . or less, the specified clearance depends on the longest unsupported tube length in the exchanger. If this length is less than 3.0 ft , then $\delta_{t b}=0.4 \mathrm{~mm}$; otherwise, $\delta_{t b}=0.2 \mathrm{~mm}$.

The longest unsupported length occurs for tubes that pass through the baffle windows, and is equal to twice the baffle spacing for exchangers with evenly spaced baffles. If the inlet and/or outlet baffle spaces are larger than the central baffle spaces, as is often the case, the longest unsupported length is the larger of the inlet and outlet spacings plus the central baffle spacing.

The shell-to-baffle clearance reflects manufacturing tolerances for both the shell and the baffles. The average clearance specified by TEMA [7] can be represented by the following linear function of shell diameter [2]:

$$
\begin{equation*}
\delta_{s b}(\mathrm{~mm})=0.8+0.002 D_{s}(\mathrm{~mm}) \tag{6.58}
\end{equation*}
$$

To account for out-of-roundness tolerances in both the shell and the baffles, a safety factor of 0.75 mm is often added to the value of $\delta_{s b}$ calculated from Equation (6.58). Although this practice provides a conservative estimate for the heat-transfer coefficient, the larger clearance results in a smaller (non-conservative) value for the calculated pressure drop.

The shell-to-bundle clearance depends on shell diameter, head type, and in some cases, the design operating pressure. In order to accommodate the rear head, floating-head units require larger clearances than fixed-tubesheet and U-tube exchangers. Pull-through floating-head units require the largest clearances to provide room for the rear-head bolts, the size of which increases with the design operating pressure. Recommended values for the diametral shell-to-bundle clearance are given in Figure 6.10.
Application of the Delaware method is illustrated in the following example.

## Example 6.1

Use the Delaware method to calculate the shell-side heat-transfer coefficient and pressure drop for the final configuration of the kerosene/crude oil exchanger of Example 5.1. Compare the results with those obtained previously using the Simplified Delaware method and HEXTRAN.

## Solution

(a) The following data are obtained from Example 5.1.

Exchanger type = AES
Shell-side fluid = kerosene
Mass flow rate of kerosene $=45,000 \mathrm{lb} / \mathrm{h}$
$D_{s}=19.25 \mathrm{in}$.
$n_{t}=124$
$D_{o}=1.0 \mathrm{in}$.
$L=14 \mathrm{ft}$
$P_{T}=1.25$ in. (square)
$B=B_{\text {in }}=B_{\text {out }}=3.85 \mathrm{in}$.
$B_{c}=0.2=$ fractional baffle cut
$n_{b}=42$
$N_{s s} / N_{c}=0.1$
(b) Estimate leakage and bypass clearances.


Figure 6.10 Diametral shell-to-bundle clearance, $D_{s}-D_{\text {ott. }}$ (Source: Ref. [2]).

Since the tube OD is less than 1.25 in., the tube-to-baffle clearance depends on the longest unsupported tube length, which is twice the baffle spacing, or 7.7 in . As this length is less than 3.0 ft , the tube-to-baffle clearance is taken as:

$$
\delta_{t b}=0.4 \mathrm{~mm}=0.015748 \mathrm{in}
$$

Equation (6.58) is used to estimate the shell-to-baffle clearance:

$$
\begin{aligned}
& \delta_{s b}=0.8+0.002 D_{s}=0.8+0.002 \times 19.25 \times 25.4 \\
& \delta_{s b}=1.7779 \mathrm{~mm}
\end{aligned}
$$

Adding the safety factor (for heat transfer) of 0.75 mm gives:

$$
\delta_{s b}=2.5279 \mathrm{~mm}=0.09952 \mathrm{in}
$$

The shell-to-bundle diametral clearance is obtained from Figure 6.10 with $D_{s}=489 \mathrm{~mm}$. Reading the graph for split ring and packed floating heads gives:

$$
D_{s}-D_{o t l} \cong 34 \mathrm{~mm}=1.34 \mathrm{in}
$$

The outer tube limit and central tube limit diameters follow from this value:

$$
\begin{gathered}
D_{o t l}=D_{s}-1.34=19.25-1.34=17.91 \mathrm{in} \\
D_{c t l}=D_{o t l}-D_{o}=17.91-1.0=16.91 \mathrm{in}
\end{gathered}
$$

(c) Calculate the flow areas.
(i) Cross-flow area

The cross-flow area is calculated from Equation (6.17):

$$
\begin{aligned}
S_{m} & =B\left[\left(D_{s}-D_{o t l}\right)+\frac{\left(D_{o t l}-D_{o}\right)}{\left(P_{T}\right)_{e f f}}\left(P_{T}-D_{o}\right)\right] \\
& =3.85\left[1.34+\frac{(17.91-1.0)}{1.25}(1.25-1.0)\right] \\
S_{m} & =18.18 \mathrm{in} .^{2}=0.1262 \mathrm{ft}^{2}
\end{aligned}
$$

(ii) Tube-to-baffle leakage area

Equation (6.25) is first used to calculate the value of angle $\theta_{c t t}$ :

$$
\begin{aligned}
& \theta_{c t l}=2 \cos ^{-1}\left[\frac{D_{s}\left(1-2 B_{c}\right)}{D_{c t l}}\right]=2 \cos ^{-1}\left[\frac{19.25(1-2 \times 0.2)}{16.91}\right] \\
& \theta_{c t l}=1.6378 \mathrm{rad}
\end{aligned}
$$

Next, the fraction of tubes in cross flow is calculated from Equation (6.35):

$$
\begin{aligned}
& F_{c}=1+\frac{1}{\pi}\left(\sin \theta_{c t l}-\theta_{c t l}\right)=1+\frac{1}{\pi}(\sin 1.6378-1.6378) \\
& F_{c} \cong 0.7963
\end{aligned}
$$

The tube-to-baffle leakage area is given by Equation (6.22):

$$
\begin{aligned}
S_{t b} & =0.5 \pi D_{o} \delta_{t b} n_{t}\left(1+F_{c}\right) \\
& =0.5 \pi \times 1.0 \times 0.015748 \times 124(1+0.7963) \\
S_{t b} & =5.5099 \mathrm{in}^{2}=0.03826 \mathrm{ft}^{2}
\end{aligned}
$$

(iii) Shell-to-baffle leakage area

Equation (6.38) is first used to calculate the value of angle $\theta_{d s}$ :

$$
\begin{aligned}
& \theta_{d s}=2 \cos ^{-1}\left(1-2 B_{c}\right)=2 \cos ^{-1}(1-2 \times 0.2) \\
& \theta_{d s}=1.8546 \mathrm{rad}
\end{aligned}
$$

The shell-to-baffle leakage area is given by Equation (6.37):

$$
\begin{aligned}
& S_{s b}=D_{s} \delta_{s b}\left(\pi-0.5 \theta_{d s}\right)=19.25 \times 0.09952(\pi-0.5 \times 1.8546) \\
& S_{s b}=4.24205 \mathrm{in}^{2}=0.02946 \mathrm{ft}^{2}
\end{aligned}
$$

(iv) Shell-to-bundle bypass flow area

The bypass flow area is given by Equation (6.40):

$$
S_{b}=B\left(D_{s}-D_{o t l}\right)=3.85 \times 1.34=5.1590 \mathrm{in}^{2} \cong 0.03583 \mathrm{ft}^{2}
$$

(v) Window flow area

The fraction of tubes in one baffle window is calculated from Equation (6.19):

$$
F_{w}=0.5\left(1-F_{c}\right)=0.5(1-0.7963)=0.10185
$$

The window flow area is calculated using Equation (6.44):

$$
\begin{aligned}
S_{w} & =\frac{1}{8} D_{s}^{2}\left(\theta_{d s}-\sin \theta_{d s}\right)-\frac{1}{4} n_{t} F_{w} \pi D_{o}^{2} \\
& =\frac{1}{8}(19.25)^{2}(1.8546-\sin 1.8546)-\frac{1}{4} \times 124 \times 0.10185 \times \pi(1.0)^{2} \\
S_{w} & =31.5192 \mathrm{in.}^{2}=0.2189 \mathrm{ft}^{2}
\end{aligned}
$$

(d) Ideal tube bank correlations.

$$
G=\frac{\dot{m}_{o}}{S_{m}}=\frac{45,000}{0.1262}=356,577 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

From Example 5.1, the viscosity of kerosene is $0.97 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{h}$. Thus,

$$
R e=D_{o} G / \mu=\frac{(1.0 / 12) \times 356,577}{0.97}=30,634
$$

Also,

$$
P_{T} / D_{o}=1.25 / 1.0=1.25
$$

From Figure 6.1, $j \cong 0.0060$ and $f \cong 0.09$. (Equations (6.1) and (6.2) give $j=0.0063$ and $f=0.089$.) The ideal tube bank heat-transfer coefficient is given by:

$$
h_{\text {ideal }}=j C_{P} G \phi P r^{-2 / 3}
$$

From Example 5.1, for kerosene:

$$
\begin{aligned}
C_{P} & =0.59 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} \\
\operatorname{Pr} & =7.24 \\
\phi & =1.0(\text { constant fluid properties assumed) }
\end{aligned}
$$

Therefore, using the $j$-value read from Figure 6.1:

$$
\begin{aligned}
& h_{\text {ideal }}=0.0060 \times 0.59 \times 356,577 \times 1.0(7.24)^{-2 / 3} \\
& h_{\text {ideal }}=337 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(e) Calculate the correction factors.
(i) Correction factor for baffle window flow

From Equation (6.45),

$$
\begin{aligned}
J_{c} & =0.55+0.72 F_{c}=0.55+0.72 \times 0.7963 \\
J_{c} & =1.1233
\end{aligned}
$$

(ii) Baffle leakage correction factors

The area ratios $r_{s}$ and $r_{l}$ are calculated from Equations (6.46) and 6.47):

$$
\begin{aligned}
& r_{s}=\frac{S_{s b}}{S_{s b}+S_{t b}}=\frac{0.02946}{0.02946+0.03826}=0.43503 \\
& r_{l}=\frac{S_{s b}+S_{t b}}{S_{m}}=\frac{0.02946+0.03826}{0.1262}=0.53661
\end{aligned}
$$

From Equation (6.50),

$$
\begin{aligned}
& p=0.8-0.15\left(1+r_{s}\right)=0.8-0.15(1+0.43503) \\
& p=0.58475
\end{aligned}
$$

The leakage correction factors for heat transfer and pressure drop are calculated from Equations (6.48) and (6.49):

$$
\begin{aligned}
J_{L} & =0.44\left(1-r_{s}\right)+\left[1-0.44\left(1-r_{s}\right)\right] \exp \left(-2.2 r_{l}\right) \\
& =0.44(1-0.43503)+[1-0.44(1-0.43503)] \exp (-2.2 \times 0.53661) \\
J_{L} & =0.4794 \\
R_{L} & =\exp \left[-1.33\left(1+r_{s}\right)\left(r_{l}\right)^{p}\right] \\
& =\exp \left[-1.33(1+0.43503)(0.53661)^{0.58475}\right] \\
R_{L} & =0.2655
\end{aligned}
$$

Note: The value of $J_{L}$ is well below 0.6 , indicating that the baffle spacing may be too small. In Example 5.1, the baffle spacing was set to the minimum because the shell-side pressure drop was very low. (Omitting the safety factor of 0.75 mm in $\delta_{s b}$ gives $J_{L}=0.5410$.)
(iii) Bundle bypass correction factors

The correction factors for the bundle bypass flow are given by Equations (6.52) and (6.53) with $r_{s s}=N_{s s} / N_{c}=0.1$ :

$$
\begin{aligned}
J_{B} & =\exp \left[-C_{J}\left(S_{b} / S_{m}\right)\left(1-\sqrt[3]{2 r_{s s}}\right)\right] \\
& =\exp [-1.25(0.03583 / 0.1262)(1-\sqrt[3]{0.2})] \\
J_{B} & =0.8630 \\
R_{B} & =\exp \left[-C_{R}\left(S_{b} / S_{m}\right)\left(1-\sqrt[3]{2 r_{s s}}\right)\right] \\
& =\exp [-3.7(0.03583 / 0.1262)(1-\sqrt[3]{0.2})] \\
R_{B} & =0.6465
\end{aligned}
$$

(iv) Correction factors for unequal baffle spacing

Since $B_{\text {in }}=B_{\text {out }}=B$, both $J_{S}$ and $R_{S}$ are equal to 1.0.
(v) Laminar flow correction factor

Since $R e>100, J_{R}=1.0$.
(f) Calculate the shell-side heat-transfer coefficient.

The shell-side coefficient is given by Equation (6.5):

$$
\begin{aligned}
h_{o} & =h_{\text {ideal }}\left(J_{c} J_{L} J_{B} J_{R} J_{S}\right) \\
& =337(1.1233 \times 0.4794 \times 0.8630 \times 1.0 \times 1.0) \\
& =337(0.4647) \\
h_{o} & =156.6 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Note: The overall correction factor is outside the acceptable range (greater than 0.5). The leakage correction factor, $J_{L}$, is by far the most significant. (Omitting the safety factor in $\delta_{s b}$ gives an overall correction factor of 0.5244 . The corresponding value of $h_{o}$ is $169.9 \mathrm{Btu} /$ $\mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ )
(g) Calculate the shell-side pressure drop.
(i) Number of tube rows crossed

The number of tube rows crossed between baffle tips is calculated using Equation (6.8):

$$
\begin{aligned}
& N_{c}=\frac{D_{s}\left(1-2 B_{c}\right)}{P_{T}^{\prime}}=\frac{19.25(1-2 \times 0.2)}{1.25} \\
& N_{c}=9.24
\end{aligned}
$$

The effective number of tube rows crossed in one baffle window is given by Equation (6.11):

$$
\begin{aligned}
& N_{c w}=\frac{0.8 B_{c} D_{s}}{P_{T}^{\prime}}=\frac{0.8 \times 0.2 \times 19.25}{1.25} \\
& N_{c w}=2.464
\end{aligned}
$$

Neither $N_{c}$ nor $N_{c w}$ is rounded to the nearest integer.
(ii) Ideal tube bank pressure drop

From Example 5.1, the density of kerosene is $49 \mathrm{lbm} / \mathrm{ft}^{3}$. The ideal tube bank pressure drop for one baffle space is given by Equation (6.7):

$$
\begin{aligned}
& \Delta P_{\text {ideal }}=\frac{2 f_{\text {ideal }} N_{c} G^{2}}{g_{c} \rho \phi}=\frac{2 \times 0.09 \times 9.24 \times(356,577)^{2}}{4.17 \times 10^{8} \times 49 \times 1.0} \\
& \Delta P_{\text {ideal }}=10.35 \mathrm{lbf} / \mathrm{ft}^{2}
\end{aligned}
$$

(iii) Ideal window pressure drop

Since the flow is turbulent, the ideal pressure drop in one baffle window is calculated from Equation (6.10):

$$
\begin{aligned}
& \Delta P_{w, \text { deal }}=\frac{\left(2+0.6 N_{c w}\right) \dot{m}_{o}^{2}}{2 g_{c} \rho S_{m} S_{w}}=\frac{(2+0.6 \times 2.464)(45,000)^{2}}{2 \times 4.17 \times 10^{8} \times 49 \times 0.1262 \times 0.2189} \\
& \Delta P_{w, \text { ideal }}=6.24 \mathrm{lbf} / \mathrm{ft}^{2}
\end{aligned}
$$

(iv) Nozzle-to-nozzle pressure drop.

Equation (6.16) gives the shell-side pressure drop between nozzles:

$$
\begin{aligned}
\Delta P_{f}= & {\left[\left(n_{b}-1\right) \Delta P_{\text {ideal }} R_{B}+n_{b} \Delta P_{w, \text { ideal }}\right] R_{L}+2 \Delta P_{\text {ideal }}\left(1+N_{c w} / N_{c}\right) R_{B} R_{S} } \\
= & {[41 \times 10.35 \times 0.6465+42 \times 6.24] \times 0.2655+2 \times 10.35(1+2.464 / 9.24) } \\
& \times 0.6465 \times 1.0 \\
\Delta P_{f}= & 159.4 \mathrm{lbf} / \mathrm{ft}^{2}=1.11 \mathrm{psi}
\end{aligned}
$$

(v) Pressure drop in nozzles.

The pressure-drop calculation for the nozzles is the same as in the Simplified Delaware method. Hence, from Example 5.1 we obtain:

$$
\Delta P_{n}=0.20 \mathrm{psi}
$$

(vi) Total shell-side pressure drop

$$
\Delta P_{o}=\Delta P_{f}+\Delta P_{n}=1.11+0.20=1.31 \mathrm{psi}
$$

The results of the calculations are summarized in the following table, along with results obtained previously using the Simplified Delaware method and HEXTRAN.

| Item | Simplified <br> Delaware method | Delaware <br> method | HEXTRAN |
| :--- | :--- | :--- | :--- |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 122 | 156.6 | 191.2 |
| $\Delta P_{o}(\mathrm{psi})$ | 2.2 | 1.31 | 2.10 |
| $R e_{o}$ | 31,158 | 30,634 | 45,148 |
| $S_{m}\left(\mathrm{ft}^{2}\right)$ | - | 0.1262 | 0.086 |
| $S_{t b}\left(\mathrm{ft}^{2}\right)$ | - | 0.03826 | 0.033 |
| $S_{s b}\left(\mathrm{ft}^{2}\right)$ | - | 0.02946 | 0.022 |
| $S_{w}\left(\mathrm{ft}^{2}\right)$ | - | 0.2189 | 0.142 |
| $D_{o t t}($ inches $)$ | - | 17.91 | 17.0 |
| $F_{c}$ | - | 0.7963 | 0.565 |
| Tubes in cross flow | - | 99 | 70 |

Comparing the Delaware method with the Simplified Delaware method, the difference in heattransfer coefficients is about $22 \%$, which is close to the expected value of $25 \%$ due to the safety factor built into the simplified method. Both methods are in agreement that the shell-side pressure drop is quite low, although the difference between the two methods is large on a percentage basis. The Simplified Delaware method gives a conservative value of pressure drop compared with the full method. The Reynolds numbers do not agree exactly because $R e$ is defined differently in the two methods.

Comparing the Delaware and HEXTRAN results, there are significant differences despite the fact that HEXTRAN uses a version of the Delaware method. The two heat-transfer coefficients differ by about $20 \%$. The discrepancy is in large part due to different ideal tube bank correlations. HEXTRAN uses the correlation presented by Gnielinski et al. [8] for the ideal tube bank heattransfer coefficient. The difference in pressure drops is large on a percentage basis and may
be partly due to the correlation used by HEXTRAN for the ideal tube bank friction factor. The correlation is not identified in the HEXTRAN documentation.

The difference in Reynolds numbers calculated by HEXTRAN and the Delaware method is due to the difference in cross-flow areas. HEXTRAN adjusts the cross-flow area for the presence of sealing strips by not including the bundle bypass flow area, which amounts to about $0.06 \mathrm{ft}^{2}$ with the clearance used by HEXTRAN. Without sealing strips it gives a crossflow area of $0.145 \mathrm{ft}^{2}$ and a Reynolds number of 26,586 , which differ from the values obtained by hand mainly due to the difference in clearances. HEXTRAN does not use this Reynolds number in calculating the heat-transfer coefficient because the correlation given by Gnielinski et al. is based on an entirely different definition of Reynolds number.

The difference in tube-to-baffle leakage areas is due to the different values of $F_{c}$. Back calculation using $S_{t b}=0.033 \mathrm{ft}^{2}$ and $F_{c}=0.565$ gives $\delta_{t b}=0.396 \cong 0.4 \mathrm{~mm}$, demonstrating that HEXTRAN uses the TEMA specification for tube-to-baffle clearance.

The difference in shell-to-baffle leakage areas is primarily due to the $0.75-\mathrm{mm}$ safety factor for shell-to-baffle clearance used in the hand calculation. Without the safety factor, the hand calculation would have given a leakage area of $0.0207 \mathrm{ft}^{2}$, which is close to the HEXTRAN value. The difference in window areas is due to the different values of $F_{c}$. With fewer tubes in cross flow between baffle tips, HEXTRAN calculates more tubes in the window with correspondingly less free area. The window area of $0.142 \mathrm{ft}^{2}$ is consistent with $F_{c}=0.565$.

The small fraction of tubes in cross flow is the most puzzling aspect of the HEXTRAN results. With only 70 tubes in cross flow, there are 54 tubes in the windows, i.e., 27 tubes in each window. However, for the specified exchanger with $1.0-\mathrm{in}$. tubes on $1.25-\mathrm{in}$. square pitch and $20 \%$ baffle cut, a single baffle window can accommodate only about 15 tubes. Therefore, the number ( $12-13$ tubes) estimated in the hand calculation is reasonable, whereas the number ( 27 tubes) found by HEXTRAN is physically impossible. This observation casts doubt on the validity of the entire HEXTRAN calculation.

There are other inconsistencies in the results produced by HEXTRAN, one of which is shown in the table below. Significantly different values of the heat-transfer coefficient are obtained for the three possible combinations of TWOPHASE and DPSMETHOD. (For TWOPHASE = New, HEXTRAN automatically takes DPSMETHOD = Stream, regardless of the user-specified pressure-drop method.) Since this problem involves single-phase flow, neither the method used for two-phase flow calculations nor the method used to calculate pressure drop should have any effect on the calculated value of the heat-transfer coefficient.

| TWOPHASE | DPSMETHOD | $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :--- | :--- | :--- |
| Old | Bell | 191.2 |
| Old | Stream | 394.1 |
| New | Stream | 223.4 |

These observations emphasize the need to scrutinize results obtained from even wellestablished commercial software, and the importance of using standardized test problems for validation purposes. It is not unusual for errors to be introduced when a new version of a software product is developed. For this reason, testing and validation should be performed whenever a new version of an existing code is obtained.

## References

1. Bell, K. J., Final report of the cooperative research program on shell-and-tube heat exchangers, University of Delaware Engineering Experiment Station Bulletin No. 5, 1963.
2. Taborek, J., Shell-and-tube heat exchangers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
3. R. H. Perry and D. W. Green, eds, Perry's Chemical Engineers' Handbook, 7th edn, McGraw-Hill, New York, 1997.
4. Hewitt, G. F., G. L. Shires and T. R. Bott, Process Heat Transfer, CRC Press, Boca Raton, FL, 1994.
5. Bell, K. J. and A. C. Mueller, Wolverine Engineering Data Book II, Wolverine Tube, Inc., www.wlv.com, 2001.
6. Shah, R. K. and D. P. Sekulic, Fundamentals of Heat Exchanger Design, Wiley, Hoboken, NJ, 2003.
7. Standards of the Tubular Exchanger Manufacturers Association, 8th edn, Tubular Exchanger Manufacturers Association, Inc., Tarrytown, NY, 1999.
8. Gnielinski, A., A. Zukauskas and A. Skrinska, Banks of plain and finned tubes, in Heat Exchanger Design Handbook, Vol. 2, Hemisphere Publishing Corp., New York, 1988.

## Notations

| A | Area |
| :---: | :---: |
| $a, a_{1}, a_{2}$, | Curve-fit parameters for Figures 6.1-6.3 |
| $a_{3}, a_{4}$ |  |
| $B$ | Baffle spacing |
| $B_{c}$ | Baffle cut |
| $B_{\text {in }}$ | Inlet baffle spacing |
| $B_{\text {out }}$ | Outlet baffle spacing |
| $b, b_{1}, b_{2}$, | Curve-fit parameters for Figures 6.1-6.3. |
| $b_{3}, b_{4}$ |  |
| $C_{J}$ | Parameter in correlation for $J_{B}$, Equation (6.52) |
| $C_{P}$ | Heat capacity at constant pressure |
| $C_{R}$ | Parameter in correlation for $R_{B}$, Equation (6.53) |
| $D_{c t l}$ | Central tube limit diameter |
| $D_{0}$ | Outside diameter of tube |
| $D_{\text {otl }}$ | Outer tube limit diameter |
| $D_{s}$ | Inside diameter of shell |
| $D_{w}$ | Equivalent diameter for window flow |
| $F_{c}$ | Fraction of tubes in cross flow between baffle tips |
| $F_{w}$ | Fraction of tubes in one baffle window |
| $f$ | Fanning friction factor |
| $f_{\text {ideal }}$ | Fanning friction factor for ideal tube bank flow |
| G | $\dot{m}_{o} / S_{m}=$ Mass flux of shell-side fluid based on cross-flow area |
| $g_{c}$ | Unit conversion factor $=4.17 \times 10^{8} \mathrm{lbm} \cdot \mathrm{ft} / \mathrm{h}^{2} \cdot \mathrm{lbf}=1.0 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2} \cdot \mathrm{~N}$ |
| $h$ | Heat-transfer coefficient |
| $h_{0}$ | Shell-side heat-transfer coefficient |
| $h_{\text {ideal }}$ | Ideal tube bank heat-transfer coefficient |
| $J_{B}$ | Heat-transfer correction factor for bundle bypass effects |
| $J_{C}$ | Heat-transfer correction factor for effect of baffle window flow |
| $J_{L}$ | Heat-transfer correction factor for baffle leakage effects |
| $J_{R}$ | Heat-transfer correction factor for laminar flow |
| $J_{S}$ | Heat-transfer correction factor for unequal baffle spacing $h \mathrm{Pr}^{2 / 3}$ |
| $j$ | $\frac{h P r^{L / D}}{C_{P} G \phi}=\text { Colburn factor for heat transfer }$ |
| $L_{1}, L_{2}$ | Clearances between tubes in aligned and staggered tube layouts, Figure 6.6 |
| $\dot{m}_{0}$ | Mass flow rate of shell-side fluid |
| $N_{c}$ | Number of tube rows crossed in flow between two baffle tips |
| $N_{c t}$ | Total number of tube rows crossed in flow through shell |
| $N_{c w}$ | Effective number of tube rows crossed in flow through one baffle window |
| $N_{s s}$ | Number of pairs of sealing strips |
| $n_{b}$ | Number of baffles |
| $n_{t}$ | Number of tubes in bundle |


| $n_{1}$ | Parameter in correlation for $J_{S}$, Equation (6.54) |
| :--- | :--- |
| $n_{2}$ | Parameter in correlation for $R_{S}$, Equation (6.55) |
| $P$ | Pressure |
| $P r$ | Prandtl number |
| $P_{T}$ | Tube pitch |
| $P_{T}^{\prime}$ | Tube pitch parallel to flow direction |
| $\left(P_{T}\right)_{e f f}$ | $P_{T}$ (for square and triangular layouts) or $P_{T} / \sqrt{2}$ (for rotated square layout) |
| $p$ | $0.8-0.15\left(1+r_{s}\right)=$ Parameter in correlation for $R_{L}$, Equation (6.49) |
| $R_{B}$ | Pressure-drop correction factor for bundle bypass effects |
| $R e$ | $D_{o} G / \mu=$ Shell-side Reynolds number |
| $R_{L}$ | Pressure-drop correction factor for baffle leakage effects |
| $R_{S}$ | Pressure-drop correction factor for unequal baffle spacing |
| $r_{l}$ | Parameter in correlations for $J_{L}$ and $R_{L}$, defined by Equation (6.47) |
| $r_{s}$ | Parameter in correlations for $J_{L}$ and $R_{L}$, defined by Equation $(6.46)$ |
| $r_{s s}$ | $N_{s s} / N_{c}$ |
| $S_{b}$ | Bundle bypass flow area |
| $S_{m}$ | Cross-flow area |
| $S_{s b}$ | Shell-to-baffle leakage area |
| $S_{t b}$ | Tube-to-baffle leakage area |
| $\left(S_{t b}\right)_{1}$ | Tube-to-baffle leakage area for one tube |
| $S_{w}$ | Window flow area |
| $S_{w g}$ | Gross window area |

## Greek Letters

| $\Delta P_{c}$ | Total pressure drop in all central baffle spaces |
| :--- | :--- |
| $\Delta P_{e}$ | Sum of pressure drops in the entrance and exit baffle spaces |
| $\Delta P_{f}$ | Nozzle-to-nozzle shell-side pressure drop |
| $\Delta P_{\text {ideal }}$ | Ideal tube bank pressure drop |
| $\Delta P_{n}$ | Pressure drop in nozzles |
| $\Delta P_{o}$ | Total shell-side pressure drop |
| $\Delta P_{w}$ | Total pressure drop in all baffle windows |
| $\Delta P_{w, \text { ideal }}$ | Pressure drop in one baffle window, uncorrected for baffle leakage effects |
| $\delta_{s b}$ | Shell-to-baffle clearance |
| $\delta_{t b}$ | Tube-to-baffle clearance |
| $\theta_{c t l}$ | Angle defined in Figure 6.5 and given by Equation (6.25) |
| $\theta_{d s}$ | Baffle window angle defined in Figure 6.5 and given by Equation (6.39) |
| $\theta_{t p}$ | Tube layout angle |
| $\mu$ | Viscosity |
| $\nu$ | Kinematic viscosity |
| $\rho$ | Fluid density |
| $\phi$ | Viscosity correction factor |

## Problems

(6.1) Use the data given below to calculate the shell-side heat-transfer coefficient and nozzle-tonozzle pressure drop by the Delaware method. Neglect the corrections for unequal baffle spacing.
Shell-side fluid properties

$$
\begin{array}{rlrl}
\dot{m} & =1.382 \mathrm{~kg} / \mathrm{s} & \rho & =1200 \mathrm{~kg} / \mathrm{m}^{3} \\
C_{P} & =2800 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{~K} & P r & =3.5 \\
\mu & =5 \times 10^{-4} \mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2} & &
\end{array}
$$

## Shell-side geometry

Cross-flow area: $0.035096 \mathrm{~m}^{2}$
Tube-to-baffle leakage area: $0.006893 \mathrm{~m}^{2}$
Shell-to-baffle leakage area: $0.003442 \mathrm{~m}^{2}$
Bundle bypass flow area: $0.004088 \mathrm{~m}^{2}$
Flow area in one baffle window: $0.0255 \mathrm{~m}^{2}$
Fraction of tubes in cross flow: 0.66
Number of tube rows crossed between baffle tips: 12
Effective number of tube rows crossed in one window: 3.2
Number of baffles: 15
Tube OD: 0.0254 m
Tube pitch: 0.033782 m (square)
Sealing strips: none
Ans. $h_{o}=450 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}, \Delta P_{f}=40 \mathrm{~Pa}$
(6.2) Use the data given below to calculate the shell-side heat-transfer coefficient by the Delaware method. Neglect the correction for unequal baffle spacing.

## Data

Shell-side Reynolds number: 20,695
Ideal tube bank heat-transfer coefficient: $376 \mathrm{Bth} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$
Tube-to-baffle leakage area: $0.074194 \mathrm{ft}^{2}$
Shell-to-baffle leakage area: $0.037048 \mathrm{ft}^{2}$
Bundle bypass flow area: $0.044002 \mathrm{ft}^{2}$
Fraction of tubes in cross flow: 0.657
Sealing strips: None
Ans. $220 \mathrm{Bth} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$
(6.3) Use the following data to calculate the shell-side heat-transfer coefficient and nozzle-to-nozzle pressure drop by the Delaware method. Neglect the corrections for unequal baffle spacing.

## Shell-side fluid properties

$$
\begin{aligned}
\dot{m} & =6.3 \mathrm{~kg} / \mathrm{s} & \rho & =850 \mathrm{~kg} / \mathrm{m}^{3} \\
C_{P} & =2500 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{~K} & \operatorname{Pr} & =23.7 \\
\mu & =0.0015 \mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2} & &
\end{aligned}
$$

Shell-side geometry
Shell ID: 0.7874 m
Bundle diameter: 0.7239 m
Number of tubes: 368
Number of tubes between baffle tips: 232
Tube OD: 0.0254 m
Tube pitch: 0.0318 m
Tube layout: rotated square ( $45^{\circ}$ )
Number of baffles: 29
Baffle cut: 20\%
Central baffle spacing: 0.1575 m
Sealing strips: none
Tube-to-baffle leakage area: $0.0095 \mathrm{~m}^{2}$
Shell-to-baffle leakage area: $0.0039 \mathrm{~m}^{2}$
Ans. $\Delta P_{f}=1900 \mathrm{~Pa}$
(6.4) Consider again the heat-transfer service of Problem 5.3. In addition to the data given in that problem the following information has been obtained from blueprints and manufacturer's specifications.

Number of tubes between baffle tips: 60
Tube-to-baffle clearance: $\delta_{t b}=0.007874$ in.
Shell-to-baffle clearance: $\delta_{s b}=0.07874$ in.
Shell-to-bundle diametral clearance: 0.6 in .
(a) What is the value of the outer tube limit diameter?
(b) Calculate the cross-flow area for the shell-side fluid.
(c) Calculate the tube-to-baffle leakage area.
(d) Calculate the shell-to-baffle leakage area.
(e) Calculate the bundle bypass flow area.
(f) Use the Delaware method to calculate the shell-side heat-transfer coefficient.
(g) What is the value of the correction factor, $J_{s}$, for unequal baffle spacing?
(h) Use the Delaware method to calculate the shell-side pressure drop.

Ans. (a) 12.65 in. (b) $0.13158 \mathrm{ft}^{2}$. (c) $0.00902 \mathrm{ft}^{2}$. (d) $0.01604 \mathrm{ft}^{2}$. (e) $0.02208 \mathrm{ft}^{2}$.
(f) $435 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (g) 0.98135 .
(6.5) Use the following data to calculate the shell-side heat-transfer coefficient and pressure drop by the Delaware method. Neglect the corrections for unequal baffle spacing.

Shell-side fluid Properties

$$
\begin{array}{rlrl}
\dot{m} & =15 \mathrm{~kg} / \mathrm{s} & \rho & =900 \mathrm{~kg} / \mathrm{m}^{3} \\
C_{P} & =2500 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{~K} & \operatorname{Pr} & =4.0 \\
\mu & =5 \times 10^{-4} \mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{3} &
\end{array}
$$

## Shell-side geometry

Cross-flow area: $0.05 \mathrm{~m}^{2}$
Tube-to-baffle leakage area: $0.01 \mathrm{~m}^{2}$
Shell-to-baffle leakage area: $0.005 \mathrm{~m}^{2}$
Bundle bypass flow area: $0.005 \mathrm{~m}^{2}$
Flow area in one baffle window: $0.03 \mathrm{~m}^{2}$
Fraction of tubes in cross flow: 0.5
Number of tube rows crossed between baffle tips: 10
Effective number of tube rows crossed in one window: 5
Number of baffles: 90
Tube OD: 0.0254 m
Tube pitch: 0.0381 m (triangular)
Sealing strips: one pair
Nozzle ID: 0.1282 m
(6.6) A shell-and-tube heat exchanger has the following specifications:

Shell ID $=0.635 \mathrm{~m}$
Number of tubes $=454$
Tube OD $=0.0191 \mathrm{~m}$
Tube pitch $=0.0254 \mathrm{~m}$
Tube layout $=$ Triangular $\left(30^{\circ}\right)$
Number of baffles $=29$
Baffle spacing $=0.254 \mathrm{~m}$
Baffle cut $=25 \%$

Tube-baffle clearance: $\delta_{t b}=0.2 \mathrm{~mm}$ Shell-baffle clearance: $\delta_{s b}=2.75 \mathrm{~mm}$
Shell-bundle diametral clearance $=25 \mathrm{~mm}$ Sealing strips: none Shell-side nozzles: $\mathrm{ID}=0.0779 \mathrm{~m}$

The shell-side fluid properties are:

$$
\begin{array}{rlrl}
\dot{m} & =7 \mathrm{~kg} / \mathrm{s} & \rho & =800 \mathrm{~kg} / \mathrm{m}^{3} \\
C_{P} & =2200 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{~K} & P r & =22.0 \\
\mu & =0.001 \mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2} & &
\end{array}
$$

Calculate the following:
(a) The outer tube limit and central tube limit diameters.
(b) The cross-flow area and bundle bypass flow area.
(c) The heat-transfer and pressure-drop correction factors for the bypass flow.
(d) The number of tube rows crossed between baffle tips and the effective number of tube rows crossed in one baffle window.
(e) The ideal cross-flow pressure drop in one baffle space.
(f) The actual (non-ideal) pressure drop in one baffle space.
(g) The shell-side heat-transfer coefficient.
(h) The total shell-side pressure drop.

Ans. (a) 0.610 and 0.5909 m . (b) 0.043577 and $0.00635 \mathrm{~m}^{2}$. (c) 0.83 and 0.58
(d) $N_{c}=14.4, \mathrm{~N}_{c w}=5.77$. (e) 130 Pa . (f) 37 Pa .
(g) $425 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. (h) 4640 Pa .
(6.7) A computer program was used to rate a shell-and-tube heat exchanger having the following configuration:

| Shell ID $=31 \mathrm{in}$. | Number of baffles $=29$ |
| :--- | :--- |
| Number of tubes $=368$ | Baffle spacing $=6.2 \mathrm{in}$. |
| Tube OD $=1.0$ in. | Baffle cut $=20 \%$ |
| Tube pitch $=1.25$ in. (square) | Sealing strips: none |

The shell-side fluid properties are as follows:

$$
\begin{aligned}
\dot{m} & =50,000 \mathrm{lb} / \mathrm{h} & \rho & =53 \mathrm{lbm} / \mathrm{ft}^{3} \\
C_{P} & =0.545 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} & \operatorname{Pr} & =19.78 \\
\mu & =1.5 \mathrm{cp} & &
\end{aligned}
$$

The output file generated by the computer program contained the following data:

Bundle diameter $=28.5$ in.
Cross-flow area $=0.346 \mathrm{ft}^{2}$
Tube-baffle leakage area $=0.102 \mathrm{ft}^{2}$

Shell-baffle leakage area $=0.042 \mathrm{ft}^{2}$
Window area $=0.377 \mathrm{ft}^{2}$
Tubes in cross flow $=232$

Based on the data in the output file:
(a) What value did the program calculate for the fraction of tubes in cross flow?
(b) What value did the program use for the diametral shell-to-bundle clearance?
(c) What value did the program use for the shell-to-baffle clearance, $\delta_{s b}$ ?
(d) What flow area did the program use for the bundle bypass stream?
(e) Use the data from the program's output file to calculate the shell-side heat-transfer coefficient by the Delaware method. Neglect the correction for unequal baffle spacing.
(f) Use the data from the program's output file to calculate the shell-side pressure drop by the Delaware method. Neglect the correction for unequal baffle spacing.
(g) If the inlet/outlet baffle spacing is 12 in., calculate the correction factors for unequal baffle spacing.

Ans. (a) 0.63. (b) 2.5 in. (c) 0.1762 in. (d) $0.1076 \mathrm{ft}^{2}$. (e) $66 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(g) $J_{S}=0.960, R_{S}=0.305$.
(6.8) Consider the modified design for the kerosene/oil exchanger of Problem 5.1. For this configuration:
(a) Estimate values for the tube-to-baffle clearance, shell-to-baffle clearance and shell-tobundle diametral clearance.
(b) Use the values obtained in part (a) to calculate the shell-side heat-transfer coefficient by the Delaware method.
(6.9) For a shell-and-tube heat exchanger employing radial low-fin tubes, the following modifications are made in the Delaware method [2]:
(1) The shell-side Reynolds number is calculated as follows:

$$
R e=D_{r e} G / \mu
$$

where
$D_{r e}=D_{r}+2 n_{f} b \tau=$ equivalent root-tube diameter
$D_{r}=$ root-tube diameter
$n_{f}=$ number of fins per unit length
$b=$ average fin height
$\tau=$ average fin thickness
(2) The cross-flow area is calculated as follows:

$$
S_{m}=B\left\{D_{s}-D_{o t l}+\frac{\left(D_{o t l}-D_{o}\right)\left(P_{T}-D_{r e}\right)}{\left(P_{T}\right)_{e f f}}\right\}
$$

where $D_{o}=D_{r}+2 b=$ fin OD.
(3) In all other calculations, $D_{o}$ is interpreted as the fin OD.
(4) The ideal tube bank friction factor obtained from Figures $6.1-6.3$ is multiplied by a correction factor of 1.4.
(5) If the shell-side Reynolds number is less than 1000, the Colburn $j$-factor obtained from Figures 6.1-6.3 is multiplied by a correction factor, $j_{c f}$, given by the following equation:

$$
j_{c f}=0.566+0.00114 R e-1.01 \times 10^{-6} R e^{2}+2.99 \times 10^{-10} R e^{3}
$$

Consider the final configuration of the oil/water heat exchanger obtained in Example 5.2. For this configuration:
(a) Estimate values for the tube-to-baffle clearance, shell-to-baffle clearance, and shell-tobundle diametral clearance.
(b) Calculate the shell-side heat-transfer coefficient by the Delaware method.
(c) Calculate the shell-side pressure drop by the Delaware method.
(d) Compare the results obtained in parts (b) and (c) with the corresponding values calculated using the Simplified Delaware method in Example 5.2.
(6.10) Consider the modified design for the oil/water heat exchanger of Problem 5.5. For this configuration:
(a) Estimate values for the tube-to-baffle clearance, shell-to-baffle clearance, and shell-tobundle diametral clearance.
(b) Use the Delaware method as modified for finned-tube exchangers (see Problem 6.9) to calculate the shell-side heat-transfer coefficient.
(6.11) A shell-and-tube heat exchanger has the following configuration:

Type: AEU
Shell ID $=39$ in.
Number of tubes $=1336$
Tube $\mathrm{OD}=0.75 \mathrm{in}$.
Tube pitch $=15 / 16$ in. (triangular)

Number of baffles $=11$
Baffle spacing $=15.6$ in.
Baffle cut = 35\%
Sealing strips: none

The shell-side fluid is a gas with the following properties:

$$
\begin{aligned}
\dot{m} & =180,000 \mathrm{lb} / \mathrm{h} & \rho & =0.845 \mathrm{lbm} / \mathrm{ft}^{3} \\
C_{P} & =0.486 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} & \operatorname{Pr} & =0.84 \\
\mu & =0.0085 \mathrm{cp} & &
\end{aligned}
$$

(a) Estimate values for the tube-to-baffle clearance, shell-to-baffle clearance, and shell-tobundle diametral clearance.
(b) Use the Delaware method to calculate the shell-side heat-transfer coefficient.
(c) Use the Delaware method to calculate the nozzle-to-nozzle pressure drop for the shellside fluid.

This page intentionally left blank

## THE STREAM ANALYSIS METHOD

## Contents

7.1 Introduction ..... 278
7.2 The Equivalent Hydraulic Network ..... 278
7.3 The Hydraulic Equations ..... 279
7.4 Shell-Side Pressure Drop ..... 281
7.5 Shell-Side Heat-Transfer Coefficient ..... 281
7.6 Temperature Profile Distortion ..... 282
7.7 The Wills-Johnston Method ..... 284
7.8 Computer Software ..... 295

### 7.1 Introduction

In the Stream Analysis method a hydraulic model is used to calculate the pressure drop and flow rates of the cross flow, leakage and bypass streams in the shell of a shell-and-tube exchanger. These flow rates are then used to calculate the shell-side heat-transfer coefficient. This approach, although still highly empirical, is considered more fundamental than that of the Delaware method because it is based on sound hydraulic principles that properly account for interactions among the shell-side streams. The method was conceived by Tinker [1-3] and further developed by others, notably Palen and Taborek [4] at Heat Transfer Research, Inc. (HTRI). By computerizing the model and fitting it to HTRI's extensive experimental database on industrial-size exchangers, the latter workers produced a powerful tool for design and analysis of shell-and-tube exchangers.
Although the basic ideas and equations involved in the Stream Analysis method have been published, values of the many empirical parameters required for its implementation remain proprietary. Therefore, commercial software is required in order to use the method, with one exception. Wills and Johnston [5] published a simplified, but complete, version that can be used to calculate shell-side pressure drop. The HTRI version is presented below, followed by the Wills-Johnston version.

### 7.2 The Equivalent Hydraulic Network

The shell-side flow is represented by an equivalent hydraulic network as shown in Figure 7.1. The streams are defined as follows:
$A=$ tube-to-baffle leakage
$B=$ Cross flow
$C=$ bundle-to-shell bypass
$E=$ shell-to-baffle leakage
$F=$ tube pass partition bypass
These streams are the same as in the Delaware method with the exception of stream $F$, which was neglected in Chapter 6. Tube holes cannot be drilled in the tubesheets where they are intersected by the tube pass partition plates. When the resulting gaps in the tube bundle are aligned with the


Figure 7.1 Equivalent hydraulic network for shell-side flow (Source: Ref. [4]).
cross-flow direction, fluid can flow across each baffle compartment through the gaps, bypassing most of the heat-transfer surface. It is possible to fill the gaps using dummy tubes, seal rods or sealing strips to eliminate or partially block stream $F$.

The valve symbols in Figure 7.1 represent flow resistances. Note in particular that there is no resistance between the inlet node and central node in each baffle compartment. The essential features of this rather confusing model representation are as follows. Streams $B, C$, and $F$ flow in parallel across each baffle compartment and then recombine to flow through the baffle windows. Leakage streams $A$ and $E$, by contrast, flow in parallel from one baffle compartment to the next and do not flow through the windows. (Note that the depiction in Figure 7.1 is strictly valid only for a single baffle and window; otherwise, the total flow out, which includes streams $A$ and $E$, would flow through the next window.)

### 7.3 The Hydraulic Equations

The equations that describe the hydraulic network of Figure 7.1 are presented in this section.

### 7.3.1 Stream pressure drops

The pressure drop of each stream in one baffle space is expressed in terms of a flow resistance (pressure loss) coefficient as follows:

$$
\begin{equation*}
\Delta P_{j}=\frac{K_{j}\left(\dot{m}_{j} / S_{j}\right)^{2}}{2 \rho g_{c} \phi} \quad j=A, B, C, E, F \tag{7.1}
\end{equation*}
$$

where
$\dot{m}_{j}=$ mass flow rate of stream $j$
$S_{j}=$ flow area for stream $j$
$K_{j}=$ flow resistance coefficient for stream $j$
$\rho=$ fluid density
$g_{c}=$ unit conversion factor
$\phi=\left(\mu / \mu_{w}\right)^{0.14}=$ viscosity correction factor
The flow areas for streams $A, B, C$, and $E$ are the same as in the Delaware method (Chapter 6). For stream $F$, the flow area is the baffle spacing multiplied by the width of the gap in the tube bundle created by the missing tubes.

### 7.3.2 Balanced pressure drop requirements

The pressure difference between any two points in a hydraulic network must be the same for all paths connecting the points. This requirement leads to the following equations:

$$
\begin{align*}
& \Delta P_{B}=\Delta P_{C}=\Delta P_{F} \equiv \Delta P_{x}  \tag{7.2}\\
& \Delta P_{A}=\Delta P_{E}=\Delta P_{x}+\Delta P_{w} \tag{7.3}
\end{align*}
$$

In these equations $\Delta P_{x}$ denotes the common value of the pressure drop experienced by streams $B, C$, and $F$ in one baffle space, and $\Delta P_{w}$ is the window pressure drop. Since the last equality in Equation (7.2) is just a definition of $\Delta P_{x}$, Equations (7.2) and (7.3) constitute four independent relationships among the pressure drops.

### 7.3.3 Mass conservation

Conservation of mass requires that the mass flow rates of the individual streams sum to the total mass flow rate of the shell-side fluid, which is fixed. Thus,

$$
\begin{equation*}
\dot{m}_{o}=\dot{m}_{A}+\dot{m}_{B}+\dot{m}_{C}+\dot{m}_{E}+\dot{m}_{F} \tag{7.4}
\end{equation*}
$$

### 7.3.4 Correlations for flow resistance coefficients

Each flow resistance coefficient, $K_{j}$, is a function of the Reynolds number for stream $j$ and the flow geometry, i.e.,

$$
\begin{equation*}
K_{j}=K_{j}\left(\text { Re }_{j}, \text { geometry }\right) \quad j=A, B, C, E, F \tag{7.5}
\end{equation*}
$$

The empirical correlations used to represent these relationships are discussed in some detail by Palen and Taborek [4]. However, complete details are publicly available only for the cross-flow stream, for which the ideal tube bank correlation is used. Equating $\Delta P_{B}$ with the ideal tube bank pressure drop, $\Delta P_{\text {ideal }}$, from Equation (6.7) gives:

$$
\begin{equation*}
\frac{K_{B}\left(\dot{m}_{B} / S_{m}\right)^{2}}{2 \rho g_{c} \phi}=\frac{2 f_{\text {ideal }} N_{c} G^{2}}{g_{c} \rho \phi} \tag{7.6}
\end{equation*}
$$

Since in this context $G=G_{B}=\dot{m}_{B} / S_{m}$, where $S_{m}$ is the cross-flow area given by Equation (6.17), it follows that

$$
\begin{equation*}
K_{B}=4 N_{c} f_{\text {ideal }} \tag{7.7}
\end{equation*}
$$

where $N_{c}$ is the number of tube rows crossed between baffle tips, and $f_{\text {ideal }}$ is the ideal tube bank friction factor based on $R e_{B}=D_{o} G_{B} / \mu$.

### 7.3.5 Window pressure drop

The pressure drop in one baffle window is calculated from the following equation [4]:

$$
\begin{equation*}
\Delta P_{w}=2 \alpha\left(\frac{G_{w}^{2}}{2 \rho g_{c}}\right)+\frac{4 f_{w} N_{c w} G_{w}^{2} \beta}{2 \rho g_{C}} \tag{7.8}
\end{equation*}
$$

where

$$
\begin{aligned}
G_{w} & =\frac{\dot{m}_{B}+\dot{m}_{C}+\dot{m}_{F}}{S_{w}} \\
S_{w} & =\text { flow area in window }
\end{aligned}
$$

$N_{c w}=$ effective number of tube rows crossed in window
$f_{w}=$ ideal tube bank friction factor based on $R e_{w}=D_{o} G_{w} / \mu$
$\alpha, \beta=$ empirical correction factors
The first term in Equation (7.8) is the pressure drop due to the $180^{\circ}$ change of direction in the window. The correction factor, $\alpha$, varies from 1.0 for small baffle spacings to zero at very large baffle spacings. Thus, the pressure drop due to the change of direction is equal to two velocity heads for small baffle spacing and approaches zero for very large baffle spacing.

The second term in Equation (7.8) represents the friction loss in the window, and is equal to the pressure drop in an ideal tube bank multiplied by the correction factor, $\beta$, that accounts for non-ideal flow conditions in the window. For laminar flow, $\beta$ is close to unity, but in turbulent flow it is a function of the baffle-cut-to-baffle-spacing ratio, $\left(B_{c} / B\right)$ [4].

### 7.3.6 Window friction factor

The friction factor for window flow is obtained from an empirical correlation of the form

$$
\begin{equation*}
f_{w}=f_{w}\left(R e_{w}, \text { geometry }\right) \tag{7.9}
\end{equation*}
$$

This correlation is, again, the ideal tube bank correlation.

### 7.3.7 Summary

The equivalent hydraulic network is described by a set of 17 equations, consisting of:

- five stream pressure drop equations, Equation (7.1)
- four balanced pressure drop equations, Equations (7.2) and (7.3)
- one mass conservation equation, Equation (7.4)
- five correlations for the flow resistance coefficients, Equation (7.5)
- one equation for window pressure drop, Equation (7.8)
- one correlation for the window friction factor, Equation (7.9)

The equations are to be solved for the following 17 variables:

- five flow rates, $\dot{m}_{j}(j=A, B, C, E, F)$
- six pressure drops, $\Delta P_{w}$ and $\Delta P_{j}(j=A, B, C, E, F)$
- five flow resistance coefficients, $K_{j}(j=A, B, C, E, F)$
- the window friction factor, $f_{w}$

The stream flow rates and the pressure drops are the desired quantities, while the resistance coefficients and friction factor are obtained as a necessary part of the solution procedure. Since Equations (7.1), (7.5), (7.8), and (7.9) are nonlinear, an iterative procedure (described in Ref. [4]) is required to obtain the solution. However, the number of equations is small and the solution is easily obtained on a computer.

### 7.4 Shell-Side Pressure Drop

The total shell-side pressure drop is the sum of the pressure drops, $\Delta P_{x}$ and $\Delta P_{w}$, for each central baffle space and baffle window, plus the pressure drops, $\Delta P_{\text {in }}$ and $\Delta P_{\text {out }}$, for the inlet and outlet baffle spaces, plus the pressure drop, $\Delta P_{n}$, in the nozzles. Thus,

$$
\begin{equation*}
\Delta P_{o}=\left(n_{b}-1\right) \Delta P_{x}+n_{b} \Delta P_{w}+\Delta P_{\text {in }}+\Delta P_{o u t}+\Delta P_{n} \tag{7.10}
\end{equation*}
$$

The values of $\Delta P_{x}$ and $\Delta P_{w}$ are obtained from the solution of the hydraulic equations as discussed above. Separate hydraulic calculations are required to obtain the values of $\Delta P_{\text {in }}$ and $\Delta P_{\text {out }}$ due to differences in baffle spacing and number of tube rows crossed in the end baffle spaces. In addition, the leakage streams join the cross-flow stream in the end baffle compartments, resulting in a higher pressure drop across these compartments. The pressure drop in the nozzles is calculated in the same manner as in the Delaware and Simplified Delaware methods.

### 7.5 Shell-Side Heat-Transfer Coefficient

The shell-side heat-transfer coefficient is calculated as a weighted average of the coefficients, $h_{x}$ and $h_{w}$, for cross flow and window flow, respectively.

$$
\begin{equation*}
h_{o}=\gamma\left(F_{c} h_{x}+2 F_{w} h_{w}\right) \tag{7.11}
\end{equation*}
$$

where
$F_{c}=$ fraction of tubes in cross flow
$F_{w}=$ fraction of tubes in one baffle window
$\gamma=$ empirical correction factor
Calculation of $F_{c}$ and $F_{w}$ is discussed in Chapter 6. Both $h_{x}$ and $h_{w}$ are obtained from the ideal tube bank correlation using appropriate Reynolds numbers given below. The factor $\gamma$ accounts for departures from ideal tube bank conditions. An additional correction factor, not shown in Equation (7.11), is used to account for differences between the central baffle spaces and the end spaces [4].

Each of the shell-side streams has a different degree of effectiveness for heat transfer, with the cross-flow stream $(B)$ being the most effective and the shell-to-baffle leakage stream $(E)$ being the least effective. The effectiveness of each stream for heat transfer in cross flow and in the windows is accounted for by means of empirically determined effectiveness factors, $\varepsilon_{x j}$ and $\varepsilon_{w j}$. These factors are incorporated in the Reynolds numbers used to calculate $h_{x}$ and $h_{w}$. The Reynolds numbers, designated $R e_{\varepsilon x}$ and $R e_{\varepsilon w}$, respectively, are computed as follows [4]:

$$
\begin{gather*}
R e_{\varepsilon x}=\frac{D_{o}}{S_{m} \mu}\left(\varepsilon_{x A} F_{c} \dot{m}_{A}+\varepsilon_{x B} \dot{m}_{B}+\varepsilon_{x C} \dot{m}_{C}+\varepsilon_{x E} \dot{m}_{E}+\varepsilon_{x F} \dot{m}_{F}\right)  \tag{7.12}\\
R e_{\varepsilon w}=\frac{D_{o}}{S_{w} \mu}\left(2 \varepsilon_{w A} F_{w} \dot{m}_{A}+\varepsilon_{w B} \dot{m}_{B}+\varepsilon_{w C} \dot{m}_{C}+\varepsilon_{w E} \dot{m}_{E}+\varepsilon_{w F} \dot{m}_{F}\right) \tag{7.13}
\end{gather*}
$$

Equations (7.11)-(7.13) contain a total of eleven empirical parameters, and Equation (7.8) contains two additional parameters, $\alpha$ and $\beta$. Furthermore, the correlations for the flow resistance coefficients contain a number of constants that were back-calculated from the HTRI data bank. With this many adjustable parameters, it is not surprising that the HTRI model provides a good representation of the experimental data for shell-side heat transfer and pressure drop. Comparison of model predictions with experimental data and with predictions of other methods is given in Ref. [4].

### 7.6 Temperature Profile Distortion

Since each of the shell-side streams has a different effectiveness for heat transfer, and since mixing of these streams in the shell is incomplete, each stream exhibits a different temperature profile along the exchanger. The cross-flow stream is the most effective for heat transfer, and therefore its temperature profile lies closest to that of the tube-side fluid, resulting in the lowest driving force for heat transfer. The least effective stream for heat transfer is the shell-to-baffle leakage stream, which also experiences the least amount of mixing with the other streams. Hence, it experiences the largest driving force for heat transfer. The net result of these different temperature profiles is that the mean temperature difference in the exchanger can be less than that calculated using the logarithmic mean temperature difference (LMTD) correction factor, which does not take account of these effects. This phenomenon is referred to as temperature profile distortion.

In order to account for temperature profile distortion, Palen and Taborek [4] introduced another correction factor, $\delta$, into the calculation of the mean temperature difference:

$$
\begin{equation*}
\Delta T_{\text {mean }}=\delta F\left(\Delta T_{\ln }\right)_{c f} \tag{7.14}
\end{equation*}
$$

where $F$ is the LMTD correction factor and the value of $\delta$ ranges from 0 to 1.0 . The overall rate of heat transfer in the exchanger is then calculated as:

$$
\begin{equation*}
q=U A \delta F\left(\Delta T_{\ln }\right)_{c f} \tag{7.15}
\end{equation*}
$$

An empirical correlation was developed for $\delta$ of the form [4]:

$$
\begin{equation*}
\delta=\delta\left(\frac{T_{b}-t_{a}}{T_{b}-T_{a}}, \frac{\dot{m}_{E}}{\dot{m}_{o}}, R e_{B}\right) \tag{7.16}
\end{equation*}
$$

where
$T_{a}=$ inlet temperature of shell-side fluid
$T_{b}=$ outlet temperature of shell-side fluid
$t_{a}=$ inlet temperature of tube-side fluid
For the reasons indicated above, the shell-to-baffle leakage stream $(E)$ is the most important for temperature profile distortion effects, and the value of $\delta$ decreases as the flow fraction of this stream
increases. The extent of mixing increases as the Reynolds number increases, and $\delta$ approaches 1.0 for large values of $R e_{B}$. The least amount of mixing occurs in laminar flow. At low Reynolds numbers, $\delta$ also decreases as the temperature difference ratio in Equation (7.16) decreases [4].

Fortunately, for properly designed exchangers with recommended shell-to-baffle clearances, $\delta$ should be close to 1.0 for turbulent flow and greater than 0.85 for laminar flow [4]. Nevertheless, values of $\delta$ ranged from about 0.4 to 1.0 for the HTRI test units, "none of which was of extreme design" [4]. A value of $\delta$ in the lower end of this range, if not accounted for in the design procedure, could result in severe under-design of the exchanger. Conditions favoring high leakage flow rates and low Reynolds numbers (hence, low $\delta$ ) are high shell-side fluid viscosity and small baffle spacing. Thus, care must be taken in the design of viscous liquid coolers such as vacuum residue coolers in oil refineries [6]. The same is true for exchangers operating in laminar flow with a close temperature approach between streams. The effect of temperature profile distortion can be mitigated by using multiple shells in series because the shell-side fluid becomes well mixed as it exits one shell and enters the next.

The following example, due to Mukherjee [6], illustrates the effect of temperature profile distortion.

## Example 7.1

In the design of a naphtha cooler for an oil refinery, the initial configuration of the exchanger was under surfaced by about $21 \%$. The tube bundle consisted of 188 tubes, $3 / 4-\mathrm{in}$. OD, 20 ft long on $1.25-$ in. square pitch. Single segmental baffles were used with a cut of $21 \%$ and a spacing of 140 mm , corresponding to $B / D_{s}=0.28$. The initial configuration was subsequently modified by progressively increasing the baffle spacing to a maximum of 210 mm while keeping all other design parameters fixed. Results of the calculations are shown in the table below [6]. Analyze and explain these results.

| Parameter | Case 1 | Case 2 | Case 3 | Case 4 | Case 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Baffle spacing (mm) | 140 | 150 | 175 | 190 | 210 |
| $B / D_{s}$ | 0.28 | 0.30 | 0.35 | 0.38 | 0.42 |
| Stream flow fraction |  |  |  |  |  |
| $\quad A$ | 0.189 | 0.173 | 0.163 | 0.154 | 0.143 |
| $B$ | 0.463 | 0.489 | 0.506 | 0.521 | 0.539 |
| $C$ | 0.109 | 0.113 | 0.116 | 0.118 | 0.121 |
| $E$ | 0.239 | 0.225 | 0.215 | 0.207 | 0.196 |
| $F$ | 0 | 0 | 0 | 0 | 0 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 126 | 117 | 115 | 113 | 105 |
| $\Delta P_{o}(\mathrm{psi})$ | 0.48 | 0.41 | 0.38 | 0.37 | 0.33 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 77.8 | 74.2 | 73.5 | 72.5 | 69.2 |
| $\Delta T_{\text {mean }}\left({ }^{\circ} \mathrm{F}\right)$ | 24.7 | 28.6 | 30.4 | 31.6 | 32.8 |
| Under-design $(\%)$ | 21.1 | 12.8 | 8.26 | 5.73 | 6.61 |

## Solution

As expected, increasing the baffle spacing reduces both the shell-side pressure drop and heattransfer coefficient. Nevertheless, the performance of the exchanger improves significantly up to a baffle spacing of 190 mm , beyond which it begins to deteriorate. Therefore, a baffle spacing of about 190 mm , corresponding to $B / D_{s}=0.38$, is optimal for this configuration.

But how can the rate of heat transfer increase when the heat-transfer coefficient decreases? The answer is that the mean driving force for heat transfer, $\Delta T_{\text {mean }}$, increases from $24.7^{\circ} F$ to $31.6^{\circ} \mathrm{F}$, an increase of nearly $28 \%$, as the baffle spacing is increased from 140 mm to 190 mm . This effect can be explained in terms of temperature profile distortion. Note that as the baffle spacing is increased, the
flow rates of the leakage streams (Streams $A$ and $E$ ) decrease, while the flow rate of the cross-flow stream (Stream $B$ ) increases. As a result, there is less temperature profile distortion at the larger baffle spacings. Consequently, the temperature profile distortion factor, $\delta$, and hence, $\Delta T_{\text {mean }}$, increases as the baffle spacing is increased. For the conditions of this example, the increase in $\Delta T_{\text {mean }}$ outweighs the decrease in $h_{o}$ for baffle spacing up to 190 mm .

Note that these results could not be predicted by the Delaware or Simplified Delaware methods. Only a version of the Stream Analysis method that accounts for temperature profile distortion is capable of generating such results. In fact, the HTRI software package was used to perform the calculations for this example [6].

### 7.7 The Wills-Johnston Method

Wills and Johnston [5], who were affiliated with HTFS, published a simplified set of correlations for the flow resistance coefficients that permit a relatively simple solution of the hydraulic equations. Iteration is required only for triangular tube layouts, and even then the computational requirements are minimal. The method is available as an option (DPSMETHOD $=$ Stream) for calculating shellside pressure drop in the HEXTRAN software package. Furthermore, the Stream Analysis algorithm used in the HTFS Suite is (presumably) an enhanced version of this procedure. The basic method described here is applicable to exchangers with type E or J shells, single segmental baffles, and single-phase flow in the shell.

### 7.7.1 Streams and flow areas

The streams are the same as in the HTRI method except that the $C$ and $F$ streams are combined to form a single bypass stream. Denoting this stream as $C F$, the streams are:

$$
\begin{aligned}
A & =\text { tube-to-baffle leakage } \\
B & =\text { cross flow } \\
C F & =\text { combined bypass flow } \\
E & =\text { shell-to-baffle leakage }
\end{aligned}
$$

The cross flow and window flow areas are the same as in the Delaware method, namely, $S_{m}$ and $S_{w}$, respectively. The bypass flow area is the sum of the flow areas for the $C$ and $F$ streams. Denoting this area as $S_{b p}$, we have:

$$
\begin{equation*}
S_{b p}=B\left(D_{s}-D_{o t l}+N_{p} \delta_{p}\right) \tag{7.17}
\end{equation*}
$$

where
$B=$ central baffle spacing
$D_{o t l}=$ outer tube limit diameter
$N_{p}=$ number of tube pass partitions aligned with the cross-flow direction
$\delta_{p}=$ pass partition clearance
The flow areas for the two leakage streams are intentionally over estimated by neglecting the effect of the baffle cut. This is done to improve the agreement between calculated and measured pressure drop. Denoting these modified flow areas by $S_{t}$ (tube-to-baffle leakage) and $S_{s}$ (shell-tobaffle leakage), the equations are:

$$
\begin{align*}
& S_{t}=n_{t} \pi D_{o} \delta_{t b}  \tag{7.18}\\
& S_{s}=\pi D_{s} \delta_{s b} \tag{7.19}
\end{align*}
$$

where
$n_{t}=$ number of tubes in bundle
$\delta_{t b}=$ tube-to-baffle clearance
$\delta_{s b}=$ shell-to-baffle clearance

The ideal tube bank correlation used by Wills and Johnston involves an additional area that will be denoted as $S_{B W}$. It is calculated as follows:

$$
\begin{equation*}
S_{B W}=\frac{B D_{o t l}^{2}\left(\pi-\theta_{o t l}+\sin \theta_{o t l}\right)}{4 D_{s}\left(1-2 B_{c}\right)}-B N_{p} \delta_{p} \tag{7.20}
\end{equation*}
$$

where

$$
\begin{equation*}
\theta_{o t l}=2 \cos ^{-1}\left[\frac{D_{s}\left(1-2 B_{c}\right)}{D_{o t l}}\right] \tag{7.21}
\end{equation*}
$$

Here, $B_{c}$ is the fractional baffle cut and $\theta_{o t l}$ is expressed in radians.

### 7.7.2 Pressure drops and stream flow rates

The pressure drop for each stream is written as:

$$
\begin{equation*}
\Delta P_{j}=\xi_{j} \dot{m}_{j}^{2} \quad j=A, B, C F, E \tag{7.22}
\end{equation*}
$$

Comparison with Equation (7.1) shows that:

$$
\begin{equation*}
\xi_{j}=\frac{K_{j}}{2 \rho g_{c} S_{j}^{2} \phi} \tag{7.23}
\end{equation*}
$$

The viscosity correction factor, $\phi$, is taken to be 1.0 in this method. The window pressure drop is written in the same format:

$$
\begin{equation*}
\Delta P_{w}=\xi_{w} \dot{m}_{w}^{2} \tag{7.24}
\end{equation*}
$$

Now the flow rate in the window is the sum of the flow rates of the cross flow and bypass streams, i.e.,

$$
\begin{equation*}
\dot{m}_{w}=\dot{m}_{B}+\dot{m}_{C F} \tag{7.25}
\end{equation*}
$$

From Equation (7.22), the flow rates on the right-hand side can be expressed as:

$$
\begin{gather*}
\dot{m}_{B}=\left(\Delta P_{B} / \xi_{B}\right)^{1 / 2}  \tag{7.26}\\
\dot{m}_{C F}=\left(\Delta P_{C F} / \xi_{C F}\right)^{1 / 2} \tag{7.27}
\end{gather*}
$$

Referring to Figure 7.1, it is seen that:

$$
\begin{equation*}
\Delta P_{B}=\Delta P_{C F}=\Delta P_{x} \tag{7.28}
\end{equation*}
$$

Upon substitution, Equation (7.25) becomes:

$$
\begin{equation*}
\dot{m}_{w}=\Delta P_{x}^{1 / 2}\left(\xi_{B}^{-1 / 2}+\xi_{C F}^{-1 / 2}\right) \tag{7.29}
\end{equation*}
$$

Solving for $\Delta P_{x}$ gives:

$$
\begin{equation*}
\Delta P_{x}=\left(\xi_{B}^{-1 / 2}+\xi_{C F}^{-1 / 2}\right)^{-2} \dot{m}_{w}^{2}=\xi_{x} \dot{m}_{w}^{2} \tag{7.30}
\end{equation*}
$$

where

$$
\begin{equation*}
\xi_{x} \equiv\left(\xi_{B}^{-1 / 2}+\xi_{C F}^{-1 / 2}\right)^{-2} \tag{7.31}
\end{equation*}
$$

From the balanced pressure drop conditions we have:

$$
\begin{equation*}
\Delta P_{A}=\Delta P_{E}=\Delta P_{x}+\Delta P_{w} \tag{7.3}
\end{equation*}
$$

Denote this common pressure drop by $\Delta P_{y}$ and substitute for $\Delta P_{w}$, and $\Delta P_{x}$ from Equations (7.24) and (7.30) to obtain:

$$
\begin{equation*}
\Delta P_{y}=\left(\xi_{w}+\xi_{x}\right) \dot{m}_{w}^{2}=\xi_{y} \dot{m}_{w}^{2} \tag{7.32}
\end{equation*}
$$

where

$$
\begin{equation*}
\xi_{y} \equiv \xi_{w}+\xi_{x} \tag{7.33}
\end{equation*}
$$

Now the total mass flow rate, $\dot{m}_{o}$, is given by:

$$
\begin{equation*}
\dot{m}_{o}=\dot{m}_{A}+\dot{m}_{E}+\dot{m}_{w} \tag{7.34}
\end{equation*}
$$

Each flow rate on the right-hand side of this equation can be expressed in terms of $\Delta P_{y}$ to obtain:

$$
\begin{equation*}
\dot{m}_{o}=\Delta P_{y}^{1 / 2}\left(\xi_{A}^{-1 / 2}+\xi_{E}^{-1 / 2}+\xi_{y}^{-1 / 2}\right) \tag{7.35}
\end{equation*}
$$

Solving for $\Delta P_{y}$ gives:

$$
\begin{equation*}
\Delta P_{y}=\left(\xi_{A}^{-1 / 2}+\xi_{E}^{-1 / 2}+\xi_{y}^{-1 / 2}\right)^{-2} \dot{m}_{o}^{2}=\xi_{o} \dot{m}_{o}^{2} \tag{7.36}
\end{equation*}
$$

where

$$
\begin{equation*}
\xi_{o} \equiv\left(\xi_{A}^{-1 / 2}+\xi_{E}^{-1 / 2}+\xi_{y}^{-1 / 2}\right)^{-2} \tag{7.37}
\end{equation*}
$$

Notice that Equation (7.36) gives the total pressure drop for one baffle space and one baffle window in terms of the flow resistances.
Next, Equations (7.36) and (7.22) are used to obtain the flow fractions of the two leakage streams. We have:

$$
\begin{aligned}
\Delta P_{A} & =\Delta P_{y} \\
\xi_{A} \dot{m}_{A}^{2} & =\xi_{0} \dot{m}_{o}^{2}
\end{aligned}
$$

Therefore,

$$
\begin{equation*}
\dot{m}_{A} / \dot{m}_{o}=\left(\xi_{o} / \xi_{A}\right)^{1 / 2} \tag{7.38}
\end{equation*}
$$

Similarly,

$$
\begin{equation*}
\dot{m}_{E} / \dot{m}_{o}=\left(\xi_{0} / \xi_{E}\right)^{1 / 2} \tag{7.39}
\end{equation*}
$$

In the same manner, the window flow fraction is obtained from Equations (7.32) and (7.36):

$$
\begin{gather*}
\Delta P_{y}=\xi_{y} \dot{m}_{w}^{2}=\xi_{o} \dot{m}_{o}^{2} \\
\dot{m}_{w} / \dot{m}_{o}=\left(\xi_{o} / \xi_{y}\right)^{1 / 2} \tag{7.40}
\end{gather*}
$$

Finally, Equations (7.30) and (7.40) are used to obtain the flow fractions of the cross-flow and bypass streams. For the cross-flow stream we have:

$$
\begin{aligned}
\Delta P_{B} & =\Delta P_{x} \\
\xi_{B} \dot{m}_{B}^{2} & =\xi_{x} \dot{m}_{w}^{2}
\end{aligned}
$$

Substituting for $\dot{m}_{w}$ from Equation (7.40) gives:

$$
\begin{equation*}
\xi_{B} \dot{m}_{B}^{2}=\xi_{x}\left(\xi_{o} / \xi_{y}\right) \dot{m}_{o}^{2} \tag{7.41}
\end{equation*}
$$

Therefore,

$$
\begin{equation*}
\frac{\dot{m}_{B}}{\dot{m}_{o}}=\left(\frac{\xi_{x} \xi_{o}}{\xi_{B} \xi_{y}}\right)^{1 / 2} \tag{7.42}
\end{equation*}
$$

Similarly, for the bypass stream we have:

$$
\begin{gather*}
\Delta P_{C F}=\Delta P_{x} \\
\xi_{C F} \dot{m}_{C F}^{2}=\xi_{x} \dot{m}_{w}^{2}=\xi_{x}\left(\xi_{o} / \xi_{y}\right) \dot{m}_{o}^{2} \\
\frac{\dot{m}_{C F}}{\dot{m}_{o}}=\left(\frac{\xi_{x} \xi_{o}}{\xi_{C F} \xi_{y}}\right)^{1 / 2} \tag{7.43}
\end{gather*}
$$

All the stream flow rates have now been expressed explicitly as simple functions of the flow resistances alone. Therefore, once the resistances are known, the stream flow rates and pressure drops can be easily computed.

### 7.7.3 Flow resistances

The resistances of the two leakage streams, the bypass stream and the window flow are assumed to be independent of the stream flow rates. Therefore, these resistances can be treated as constants for a given rating problem. Justification for these assumptions is given in Ref. [5]. Only the cross-flow resistance need be treated as a variable in the calculations. It is obtained from an ideal tube bank friction factor correlation and is a function of the cross-flow Reynolds number.

## The cross-flow resistance

The cross-flow resistance is given by the following equation [5]:

$$
\begin{equation*}
\xi_{B}=\frac{4 a D_{o} D_{s} D_{v}\left(1-2 B_{c}\right)\left(P_{T}-D_{o}\right)^{-3}\left(\frac{\dot{m}_{B} D_{o}}{\mu S_{B W}}\right)^{-b}}{2 \rho g_{c} S_{B W}^{2}} \tag{7.44}
\end{equation*}
$$

where
$a=0.061, b=0.088$ for square and rotated-square pitch
$a=0.450, b=0.267$ for triangular pitch

$$
\begin{equation*}
D_{V}=\left(\Omega_{1} P_{T}^{2}-D_{o}^{2}\right) / D_{o} \tag{7.45}
\end{equation*}
$$

$$
\begin{aligned}
\Omega_{1} & =1.273 \text { for square and rotated-square pitch } \\
& =1.103 \text { for triangular pitch }
\end{aligned}
$$

Note that the Reynolds number in Equation (7.44) is based on $S_{B W}$ rather than the cross-flow area, $S_{m}$, that is used in most ideal tube bank correlations. Also, notice that the Reynolds number dependence is very weak for square and rotated-square tube layouts. For this reason, iteration is not required to determine the value of $\xi_{B}$ for these layouts. For these cases, $\dot{m}_{B}$ can be set to $0.5 \dot{m}_{o}$ in Equation (7.44). For triangular pitch, iteration is required to determine the values of $\dot{m}_{B}$ and $\xi_{B}$ using Equations (7.42) and (7.44). A starting value of $\dot{m}_{B}=0.5 \dot{m}_{o}$ is used in Equation (7.44) to calculate $\xi_{B}$, which is then used in equation (7.42) to calculate a new value of $\dot{m}_{B}$. Iteration is continued until successive values of $\dot{m}_{B}$ agree to within the desired accuracy. Convergence is usually rapid [5]; therefore, the use of a convergence acceleration method is not required.

The bypass flow resistance
The bypass flow resistance is computed as follows [5]:

$$
\begin{equation*}
\xi_{C F}=\frac{0.3164 D_{s}\left(\frac{1-2 B_{C}}{\Omega_{2} P_{T}}\right)\left(\frac{\dot{m}_{o} D_{e}}{\mu S_{b p}}\right)^{-0.025}+2 N_{s s}}{2 \rho g_{c} S_{b p}^{2}} \tag{7.46}
\end{equation*}
$$

where
$N_{s s}=$ number of pairs of sealing strips
$\Omega_{2}=1.0$ for square pitch
$=1.414$ for rotated-square pitch
$=1.732$ for triangular pitch
$D_{e}=$ equivalent diameter for the bypass flow
The equivalent diameter is given by the following equation:

$$
\begin{equation*}
D_{e}=\frac{2 S_{b p}}{D_{s}-D_{o t l}+2 B+N_{p}\left(B+\delta_{p}\right)} \tag{7.47}
\end{equation*}
$$

Due to the small exponent on the Reynolds number in Equation (7.46), little error is introduced in most cases by treating this term as a constant. The resulting simplified form of the equation is $[7,8]$ :

$$
\begin{equation*}
\xi_{C F}=\frac{0.266 D_{s}\left(\frac{1-2 B_{c}}{\Omega_{2} P_{T}}\right)+2 N_{s s}}{2 \rho g_{c} S_{b p}^{2}} \tag{7.48}
\end{equation*}
$$

## The tube-to-baffle leakage flow resistance

The flow resistance for the tube-to-baffle leakage stream is given by the following equation [5], which is based on data for flow through eccentric orifices:

$$
\begin{equation*}
\xi_{A}=\frac{\left(2 B_{t} / \delta_{t b}\right)\left[0.0035+\frac{0.528 \dot{m}_{o} \delta_{t b}}{\mu S_{t}}\right]^{-0.42}+2.3\left(B_{t} / \delta_{t b}\right)^{-0.177}}{2 \rho g_{c} S_{t}^{2}} \tag{7.49}
\end{equation*}
$$

where $B_{t}$ is the baffle thickness. A simplified form of this equation can also be used $[7,8]$ :

$$
\begin{equation*}
\xi_{A}=\frac{0.036 B_{t} / \delta_{t b}+2.3\left(B_{t} / \delta_{t b}\right)^{-0.177}}{2 \rho g_{c} S_{t}^{2}} \tag{7.50}
\end{equation*}
$$

The shell-to-baffle leakage flow resistance
The flow resistance for the shell-to-baffle leakage stream is given by an equation analogous to (7.49) [5]:

$$
\begin{equation*}
\xi_{E}=\frac{\left(2 B_{t} / \delta_{s b}\right)\left[0.0035+\frac{0.528 \dot{m}_{o} \delta_{s b}}{\mu S_{s}}\right]^{-0.42}+2.3\left(B_{t} / \delta_{s b}\right)^{-0.177}}{2 \rho g_{c} S_{s}^{2}} \tag{7.51}
\end{equation*}
$$

The simplified form analogous to Equation (7.50) is [7, 8]:

$$
\begin{equation*}
\xi_{E}=\frac{0.036 B_{t} / \delta_{s b}+2.3\left(B_{t} / \delta_{s b}\right)^{-0.177}}{2 \rho g_{c} S_{s}^{2}} \tag{7.52}
\end{equation*}
$$

## The window flow resistance

The window flow resistance is given by the following simple expression that is independent of the flow rate [5]:

$$
\begin{equation*}
\xi_{w}=\frac{1.9 \exp \left(0.6856 S_{w} / S_{m}\right)}{2 \rho g_{c} S_{w}^{2}} \tag{7.53}
\end{equation*}
$$

### 7.7.4 Inlet and outlet baffle spaces

The pressure-drop calculation in the end baffle spaces is modified to account for differences in baffle spacing, number of tube rows crossed and flow distribution. The flow rate in the end spaces is taken as the arithmetic mean of the window and total flow rates, i.e.,

$$
\begin{equation*}
\dot{m}_{e}=0.5\left(\dot{m}_{o}+\dot{m}_{w}\right) \tag{7.5}
\end{equation*}
$$

where the subscript "e" denotes end baffle space, either inlet or outlet. The cross-flow resistance, $\xi_{e}$, in the end spaces is estimated by the following equation [5]:

$$
\begin{equation*}
\xi_{e}=0.5 \xi_{x}\left(B / B_{e}\right)^{2}\left\{1+D_{\text {ott }} /\left[D_{s}\left(1-2 B_{c}\right)\right]\right\} \tag{7.55}
\end{equation*}
$$

where $B_{e}$ represents either the inlet or outlet baffle spacing.
Half the pressure drop in the end baffle windows is allocated to the end baffle spaces. The flow resistance, $\xi_{w e}$, in the end windows is calculated as follows [5]:

$$
\begin{equation*}
\xi_{w e}=\frac{1.9 \exp \left[0.6856 S_{w} B /\left(S_{m} B_{e}\right)\right]}{2 \rho g_{c} S_{w}^{2}} \tag{7.5}
\end{equation*}
$$

The pressure drop in the inlet or outlet baffle space is then given by:

$$
\begin{equation*}
\Delta P_{e}=\xi_{e} \dot{m}_{e}^{2}+0.5 \xi_{w e} \dot{m}_{w}^{2} \tag{7.5}
\end{equation*}
$$

### 7.7.5 Total shell-side pressure drop

The total shell-side pressure drop is obtained by summing the pressure drops in all the central baffle spaces and windows, the pressure drops in the inlet and outlet baffle spaces, and the pressure drops in the nozzles. Thus,

$$
\begin{equation*}
\Delta P_{o}=\left(n_{b}-1\right) \Delta P_{y}+\Delta P_{\text {in }}+\Delta P_{\text {out }}+\Delta P_{n} \tag{7.58}
\end{equation*}
$$

Here, $n_{b}$ is the number of baffles, and $\Delta P_{\text {in }}$ and $\Delta P_{\text {out }}$ are computed from Equation (7.57).
In order to improve the agreement between calculated and measured pressure drop at low Reynolds numbers, Wills and Johnston [5] modified Equation (7.58) by introducing an empirical correction factor. The cross-flow Reynolds number based on the cross-flow area, $S_{m}$, is first calculated:

$$
\begin{equation*}
R e_{B}=\frac{D_{o} \dot{m}_{B}}{\mu S_{m}} \tag{7.59}
\end{equation*}
$$

For $R e_{B}<1000$, the flow in some or all of the streams may not be fully turbulent, thus necessitating use of a correction factor. The correction factor, $\psi$, is computed as follows:

$$
\begin{align*}
\psi & =3.646 R e_{B}^{-0.1934} & & R e_{B}<1000 \\
& =1.0 & & R e_{B} \geq 1000 \tag{7.60}
\end{align*}
$$

Equation (7.58) is then modified by multiplying the nozzle-to-nozzle pressure drop by $\psi$ to obtain:

$$
\begin{equation*}
\Delta P_{o}=\psi\left[\left(n_{b}-1\right) \Delta P_{y}+\Delta P_{\text {in }}+\Delta P_{\text {out }}\right]+\Delta P_{n} \tag{7.61}
\end{equation*}
$$

Wills and Johnston do not recommend using their method for $R e_{B}<300$. However, their data indicate that for $100 \leq R e_{B}<300$, the worst errors are on the high (safe) side. Therefore, a reasonable lower limit for use of the method is $R e_{B}=100$.

## Example 7.2

Use the Wills-Johnston method to calculate the shell-side pressure drop for the final configuration of the kerosene/crude-oil exchanger of Example 5.1. Compare the results with those obtained previously using the Delaware and Simplified Delaware methods.

## Solution

(a) The following data are obtained from Examples 5.1 and 6.1:

| Exchanger type $=A E S$ | $B_{c}=0.2$ |
| :--- | :--- |
| Shell-side fluid $=$ kerosene | $n_{b}=42$ |
| Kerosene viscosity $=0.97 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{h}$ | $N_{s s} / N_{c}=0.1$ |
| Kerosene density $=49 \mathrm{lbm} / \mathrm{ft}^{3}$ | $\delta_{t b}=0.015748 \mathrm{in}$. |
| $\dot{m}_{o}=45,000 \mathrm{lb} / \mathrm{h}$ | $\delta_{s b}=0.09952 \mathrm{in}$. |
| $D_{s}=19.25 \mathrm{in}$. | $D_{o t l}=17.91 \mathrm{in}$. |
| $n_{t}=124$ | $D_{c t l}=16.91 \mathrm{in}$. |
| $n_{p}=4$ | $S_{m}=0.1262 \mathrm{ft}^{2}$ |
| $D_{o}=1.0 \mathrm{in}$. | $S_{w}=0.2189 \mathrm{ft}^{2}$ |
| $P_{T}=1.25 \mathrm{in} .($ square $)$ | $S_{b}=0.03583 \mathrm{ft}^{2}$ |
| $B=B_{\text {in }}=B_{\text {out }}=3.85 \mathrm{in}$. | $N_{c}=9.24$ |

It is assumed that all tube-pass partitions are aligned normal to the cross-flow direction so that the flow rate of the $F$ stream is zero.
(b) Calculate the flow areas.

The bypass flow area is given by Equation (7.17) with $N_{p}=0$ (since the tube pass partitions are normal to the cross-flow direction). Thus,

$$
S_{b p}=B\left(D_{s}-D_{o t l}\right)=S_{b}=0.03583 \mathrm{ft}^{2}
$$

The modified leakage flow areas are calculated from Equations (7.18) and (7.19):

$$
\begin{aligned}
& S_{t}=n_{t} \pi D_{o} \delta_{t b}=124 \pi \times 1.0 \times 0.015748 \\
& S_{t}=6.13475 \mathrm{in} . .^{2}=0.04260 \mathrm{ft}^{2} \\
& S_{s}=\pi D_{s} \delta_{s b}=\pi \times 19.25 \times 0.09952 \\
& S_{s}=6.01854 \mathrm{in}^{2}=0.04180 \mathrm{ft}^{2}
\end{aligned}
$$

To find the area $S_{B W}$, angle $\theta_{o t l}$ is first calculated using Equation (7.21):

$$
\begin{aligned}
\theta_{\text {otl }} & =2 \cos ^{-1}\left[\frac{D_{s}\left(1-2 B_{c}\right)}{D_{\text {otl }}}\right] \\
& =2 \cos ^{-1}\left[\frac{19.25(1-2 \times 0.2)}{17.91}\right] \\
\theta_{\text {otl }} & =1.73983 \text { radians }
\end{aligned}
$$

Equation (7.20) is then used to compute $S_{B W}$.

$$
\begin{aligned}
S_{B W} & =\frac{B D_{o t l}^{2}\left(\pi-\theta_{o t l}+\sin \theta_{o t l}\right)}{4 D_{s}\left(1-2 B_{c}\right)}-B N_{p} \delta_{p} \\
& =\frac{3.85(17.91)^{2}(\pi-1.73983+\sin 1.73983)}{4 \times 19.25(1-2 \times 0.2)}-0 \\
S_{B W} & =63.8198 \mathrm{in}^{2}=0.44319 \mathrm{ft}^{2}
\end{aligned}
$$

The cross-flow area, $S_{m}$, and window flow area, $S_{W}$, were obtained from Example 6.1, and therefore are not calculated here.
(c) Calculate the flow resistances.
(i) The cross-flow resistance is given by Equation (7.44) with $a=0.061$ and $b=0.088$ for square pitch. The value of $D_{V}$ is first calculated from Equation (7.45):

$$
\begin{aligned}
& D_{V}=\left(\Omega_{1} P_{T}^{2}-D_{o}^{2}\right) / D_{o}=\left[1.273(1.25)^{2}-(1.0)^{2}\right] / 1.0 \\
& D_{V}=0.98906 \text { in. }
\end{aligned}
$$

Setting $\dot{m}_{B}$ to $0.5 \dot{m}_{o}=22,500 \mathrm{lb} / \mathrm{h}$ in Equation (7.44), we have:

$$
\begin{aligned}
\xi_{B} & =\frac{4 a D_{o} D_{s} D_{V}\left(1-2 B_{c}\right)\left(P_{T}-D_{o}\right)^{-3}\left(\frac{\dot{m}_{B} D_{o}}{\mu S_{B W}}\right)^{-b}}{2 \rho g_{c} S_{B W}^{2}} \\
& =\frac{4 \times 0.061 \times 1.0 \times 19.25 \times 0.98906(1-2 \times 0.2)(0.25)^{-3}\left(\frac{22,500 \times 1.0 / 12}{0.97 \times 0.44319}\right)^{-0.088}}{2 \times 49 \times 32.174(0.44319)^{2}} \\
\xi_{B} & =0.13778 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(ii) The bypass flow resistance is calculated using the simplified expression given by Equation (7.48). The number of pairs of sealing strips is first determined as follows:

$$
N_{s s}=\left(N_{s s} / N_{c}\right) N_{c}=0.1 \times 9.24=0.924 \rightarrow 1
$$

Equation (7.48) is then used with $\Omega_{2}=1.0$ for square pitch:

$$
\begin{aligned}
\xi_{C F} & =\frac{0.266 D_{s}\left(\frac{1-2 B_{c}}{\Omega_{2} P_{T}}\right)+2 N_{s s}}{2 \rho g_{c} S_{b p}^{2}} \\
& =\frac{0.266 \times 19.25\left(\frac{1-2 \times 0.2}{1.0 \times 1.25}\right)+2 \times 1}{2 \times 49 \times 32.174(0.03583)^{2}} \\
\xi_{C F} & =1.10129 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(iii) The tube-to-baffle leakage flow resistance is obtained from Equation (7.50). The baffle thickness, $B_{t}$, is 0.1875 in. from Table 5.2:

$$
\begin{aligned}
\xi_{A} & =\frac{0.036 B_{t} / \delta_{t b}+2.3\left(B_{t} / \delta_{t b}\right)^{-0.177}}{2 \rho g_{c} S_{t}^{2}} \\
& =\frac{0.036 \times 0.1875 / 0.015748+2.3(0.1875 / 0.015748)^{-0.177}}{2 \times 49 \times 32.174(0.04260)^{2}} \\
\xi_{A} & =0.33419 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(iv) Equation (7.52) is used to calculate the shell-to-baffle leakage flow resistance:

$$
\begin{aligned}
\xi_{E} & =\frac{0.036 B_{t} / \delta_{s b}+2.3\left(B_{t} / \delta_{s b}\right)^{-0.177}}{2 \rho g_{c} S_{s}^{2}} \\
& =\frac{0.036 \times 0.1875 / 0.09952+2.3(0.1875 / 0.09952)^{-0.177}}{2 \times 49 \times 32.174(0.04180)^{2}} \\
\xi_{E} & =0.38552 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(v) The window flow resistance is computed from Equation (7.53):

$$
\begin{aligned}
\xi_{w} & =\frac{1.9 \exp \left(0.6856 S_{w} / S_{m}\right)}{2 \rho g_{c} S_{w}^{2}} \\
& =\frac{1.9 \exp (0.6856 \times 0.2189 / 0.1262)}{2 \times 49 \times 32.174(0.2189)^{2}} \\
\xi_{w} & =0.041304 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(vi) Equation (7.31) is used to calculate $\xi_{x}$ :

$$
\begin{aligned}
& \xi_{x}=\left(\xi_{B}^{-1 / 2}+\xi_{C F}^{-1 / 2}\right)^{-2}=\left[(0.13778)^{-1 / 2}+(1.10129)^{-1 / 2}\right]^{-2} \\
& \xi_{x}=0.075186 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(vii) Equation (7.33) is used to calculate $\xi_{y}$ :

$$
\begin{aligned}
& \xi_{y}=\xi_{w}+\xi_{X}=0.041304+0.075186 \\
& \xi_{y}=0.116490 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(viii) Finally, Equation (7.37) is used to calculate $\xi_{0}$ :

$$
\begin{aligned}
\xi_{o} & =\left(\xi_{A}^{-1 / 2}+\xi_{E}^{-1 / 2}+\xi_{y}^{-1 / 2}\right)^{-2} \\
& =\left[(0.33419)^{-1 / 2}+(0.38552)^{-1 / 2}+(0.116490)^{-1 / 2}\right]^{-2} \\
\xi_{0} & =0.025434 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(d) Calculate the flow fractions.

The flow resistances are now used to calculate the flow fractions, starting with the cross-flow stream. From Equation (7.42),

$$
\begin{aligned}
& \dot{m}_{B} / \dot{m}_{o}=\left(\frac{\xi_{x} \xi_{o}}{\xi_{B} \xi_{y}}\right)^{1 / 2}=\left(\frac{0.075186 \times 0.025434}{0.13778 \times 0.116490}\right)^{1 / 2} \\
& \dot{m}_{B} / \dot{m}_{o}=0.345
\end{aligned}
$$

Since the tube layout is square, iteration is not required, and this value is accepted as final.
In a similar manner, Equation (7.43) is used to calculate the bypass flow fraction:

$$
\begin{aligned}
& \dot{m}_{C F} / \dot{m}_{o}=\left(\frac{\xi_{x} \xi_{o}}{\xi_{C F} \xi_{y}}\right)^{1 / 2}=\left(\frac{0.075186 \times 0.025434}{1.10129 \times 0.116490}\right)^{1 / 2} \\
& \dot{m}_{C F} / \dot{m}_{o}=0.122
\end{aligned}
$$

The leakage flow fractions are obtained from Equations (7.38) and (7.39):

$$
\begin{aligned}
& \dot{m}_{A} / \dot{m}_{o}=\left(\xi_{o} / \xi_{A}\right)^{1 / 2}=(0.025434 / 0.33419)^{1 / 2}=0.276 \\
& \dot{m}_{E} / \dot{m}_{o}=\left(\xi_{o} / \xi_{E}\right)^{1 / 2}=(0.025434 / 0.38552)^{1 / 2}=0.257
\end{aligned}
$$

Note that the sum of the flow fractions is 1.000 .
Finally, the window flow fraction is given by Equation (7.40):

$$
\dot{m}_{w} / \dot{m}_{o}=\left(\xi_{o} / \xi_{y}\right)^{1 / 2}=(0.025434 / 0.116490)^{1 / 2}=0.467
$$

Notice that the window flow fraction equals the sum of the cross-flow and bypass flow fractions.
(e) Calculate $\Delta P_{y}$.

The total pressure drop in one baffle space and one baffle window is given by Equation (7.36):

$$
\begin{aligned}
& \Delta P_{y}=\xi_{o} \dot{m}_{o}^{2}=0.025434(45,000 / 3600)^{2} \\
& \Delta P_{y}=3.974 \mathrm{lbf} / \mathrm{ft}^{2}
\end{aligned}
$$

Note: The factor of 3600 converts the flow rate to $\mathrm{lbm} / \mathrm{s}$.
(f) Calculations for the end baffle spaces.

The window flow rate is obtained from the window flow fraction:

$$
\dot{m}_{w}=0.467 \dot{m}_{o}=0.467(45,000 / 3600)=5.8375 \mathrm{lbm} / \mathrm{s}
$$

The flow rate in the end baffle spaces is given by Equation (7.54):

$$
\begin{aligned}
& \dot{m}_{e}=0.5\left(\dot{m}_{o}+\dot{m}_{w}\right)=0.5(45,000 / 3600+5.8375) \\
& \dot{m}_{e}=9.16875 \mathrm{lbm} / \mathrm{s}
\end{aligned}
$$

The flow resistance in the end spaces is calculated from Equation (7.55) with $B_{e}=B$ :

$$
\begin{aligned}
\xi_{e} & =0.5 \xi_{x}\left(B / B_{e}\right)^{2}\left\{1+D_{o t l} /\left[D_{s}\left(1-2 B_{c}\right)\right]\right\} \\
& =0.5 \times 0.075186(1.0)^{2}\{1+17.91 /[19.25(1-2 \times 0.2)]\} \\
\xi_{e} & =0.095887 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The flow resistance, $\xi_{w e}$, in the end baffle windows is given by Equation (7.56). However, since $B_{e}=B$, this equation reduces to Equation (7.53) for $\xi_{w}$. Hence,

$$
\xi_{w e}=\xi_{w}=0.041304 \mathrm{lbf} \cdot \mathrm{~s}^{2} / \mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}
$$

Now the pressure drop in each end space is calculated from Equation (7.57):

$$
\begin{aligned}
\Delta P_{e} & =\xi_{e} \dot{m}_{e}^{2}+0.5 \xi_{w e} \dot{m}_{w}^{2} \\
& =0.095887(9.16875)^{2}+0.5 \times 0.041304(5.8375)^{2} \\
\Delta P_{e} & =8.765 \mathrm{lbf} / \mathrm{ft}^{2}
\end{aligned}
$$

(g) Calculate shell-side pressure drop.

First, the cross-flow Reynolds number is calculated according to Equation (7.59):

$$
R e_{B}=\frac{D_{o} \dot{m}_{B}}{\mu S_{m}}=\frac{(1.0 / 12)(0.345 \times 45,000)}{0.97 \times 0.1262}=10,569
$$

Since the Reynolds number is greater than 1000 , the correction factor, $\psi$, is equal to 1.0 from Equation (7.60). The total shell-side pressure drop is then obtained from Equation (7.61).

$$
\begin{aligned}
\Delta P_{o} & =\psi\left[\left(n_{b}-1\right) \Delta P_{y}+\Delta P_{\text {in }}+\Delta P_{\text {out }}\right]+\Delta P_{n} \\
& =1.0[(42-1) \times 3.974+8.765+8.765]+\Delta P_{n} \\
\Delta P_{o} & =180.5+\Delta P_{n} \mathrm{lbf} / \mathrm{ft}^{2}=1.25+\Delta P_{n} \mathrm{psi}
\end{aligned}
$$

From Example 5.1, the nozzle pressure drop is 0.20 psi. Hence,

$$
\Delta P_{o}=1.25+0.20=1.45 \mathrm{psi}
$$

The following table compares this result with those obtained previously by other methods:

| Method | $\Delta P_{o}(\mathrm{psi})$ |
| :--- | :--- |
| Wills-Johnston | 1.45 |
| Delaware | 1.31 |
| Simplified Delaware | 2.2 |
| HEXTRAN (DPSMETHOD = Bell) | 2.10 |
| HEXTRAN (DPSMETHOD $=$ Stream) | 2.11 |

All methods are consistent in predicting a small pressure drop for the exchanger. The WillsJohnston value is within about $10 \%$ of the value found by the Delaware method. However, it differs by a large percentage from the value given by HEXTRAN (DPSMETHOD = Stream), even though the latter uses the Wills-Johnston method. The anomalies discussed in Example 6.1 may be partly responsible for the discrepancy.

The Wills-Johnston method predicts that the two leakage streams account for more than $50 \%$ of the total shell-side flow. The large amount of leakage is consistent with the result obtained by the Delaware method in Example 6.1. Recall that the leakage correction factor, $J_{L}$, was found to be less that 0.6 , indicating abnormally high flow fractions for the leakage streams. Note in particular that the $E$ stream, which is the least effective for heat transfer, accounts for approximately $25 \%$ of the total flow.

### 7.8 Computer Software

### 7.8.1 HTRI

As previously noted, the HTRI software package, Xchanger Suite, is available only to member companies, which include most major chemical, petroleum and engineering firms. The package consists of eight major components, six of which perform design and rating calculations for the following types of heat-transfer equipment: air-cooled heat exchangers and economizers (Xace), fired heaters (Xfh), hairpin heat exchangers (Xhpe), shell-and-tube heat exchangers (Xist), jacketedpipe heat exchangers (Xjpe), and plate-and-frame heat exchangers (Xphe). The other two modules develop detailed tube layouts (Xtlo) and perform flow-induced tube vibration analyses (Xvib) for shell-and-tube exchangers. The software contains pure-component physical property data for a large number of compounds, and includes a third-party thermodynamics package (VMG Thermo). Hence, Xchanger Suite can be used on a stand-alone basis. It also interfaces with flowsheet simulator software such as Aspen Plus, HYSYS, PRO II and HEXTRAN, so that the extensive physical property data banks, property estimation methods, and thermodynamic routines available in these simulators can be utilized as well. Handling exchangers with multiple shells of different sizes is also greatly facilitated by utilizing the interface with a flowsheet simulator.

An educational version of Xchanger Suite is available to universities for a nominal fee. This version includes only three of the eight modules, Xace, Xist and Xphe. However, Xtlo is a part of Xist in addition to being a separate program, and Xist also performs tube vibration analyses at strategic points in the tube bundle. Thus, tube layouts and vibration analyses are still available, even though Xtlo and Xvib cannot be used as stand-alone programs in the educational version.

Xist is a fully incremental program, utilizing three-dimensional incrementation for all TEMA shell types. The heat exchanger is first divided into increments along the tube length. For baffled exchangers, one increment is used for each baffle space unless a larger number is specified by the user. For non-baffled exchangers, 20 increments are used, with the exception of X-shells ( 10 increments) and K-shells ( 5 increments). Next, the exchanger is divided into rows (top to bottom) and sections (side to side). The program uses enough rows and sections so that each three-dimensional subdivision of the exchanger involves only one type of flow (window flow or cross flow) and one tube pass. Thermal and hydraulic calculations are performed for each subdivision using local values of temperatures, pressures and physical properties, and the individual results are integrated to obtain overall results that are displayed in the output report files.

Xist can be run in any one of three modes as specified on the Input Summary form shown in Figure 7.2. In rating mode, the user specifies inlet stream conditions, the exchanger geometry, and either the duty or the outlet temperature of one stream. The program then uses energy balances to calculate missing outlet temperatures and, if not given, the duty. Based on these temperatures and the given geometry, the pressure drops and the achievable duty are computed along with the percentage over-design. The latter is based on the computed achievable duty versus the specified (required) duty; it is calculated as $\left(U_{D} / U_{r e q}-1\right) \times 100$. The program is most frequently used in this mode.

Simulation mode is similar to rating mode except that neither the duty nor the outlet temperatures are specified. The program calculates the actual outlet temperatures, pressure drops and duty based on the given exchanger geometry. This mode is equivalent to the HEXTRAN rating mode (TYPE = Old).
In design mode, Xist finds the smallest exchanger that meets a given performance specification and pressure drop constraints. Parameters that can be automatically varied are:

- Shell type and diameter
- Number of shells in series and parallel
- Number, diameter and length of tubes
- Number of tube passes
- Baffle type, cut and spacing
- Tube pitch

The range over which each parameter is allowed to vary is user specified.


Figure 7.2 Input Summary screen in Xist, version 4.0.

There are seven major categories of input data for Xist as shown in the tree at the left of Figure 7.2. Key geometrical parameters and process conditions can be entered and/or modified on the Input Summary form. They can also be entered on the more detailed individual forms by expanding the tree at the left of the screen. Exchanger geometry can be specified in great detail using individual forms for the shell, tubes, baffles, nozzles, etc. However, many of the input parameters either have a default value or can be calculated by the program. Text boxes for required input items are outlined in red until a suitable value is entered.

In addition to geometry and process data, physical properties of the hot and cold fluids must be supplied. As in TASC, this can be accomplished by entering bulk property data for the stream or by specifying the composition of the stream and selecting a thermodynamic method to be used for calculating mixture properties.

The Piping input category is used to specify the configuration of inlet and outlet piping for reboilers. It is not used for other applications.

The Design input category is used to specify which parameters are to be automatically varied in design mode, and the allowed ranges of these parameters. It is not used when the program is run in rating or simulation mode.

Under the Control input category, alternate computational methods can be chosen for certain calculations performed by the program, the number of increments per baffle can be specified, and default convergence tolerances can be over-ridden. For most applications, no input is required in this category.
The use of Xist is illustrated in the following examples.

## Example 7.3

Use the Xist module of the HTRI Xchanger Suite to rate the final configuration of the kerosene/crude-oil exchanger of Example 5.1, and compare the results with those obtained previously using other methods.

## Solution

Since stream pressures were not given in Example 5.1, the inlet pressure is arbitrarily set at 50 psia for each stream as in previous examples. Other input data are obtained from Example 5.1 and entered on the appropriate forms, starting with the Geometry/Shell form shown below. Rating mode is selected for this problem and the shell ID is entered. Other items on this form, including exchanger type (AES) and hot fluid location (shell side) are default settings.


Next, tube-side data are entered on the Geometry/Tubes form as shown below. Notice that the box for rigorous tube count is checked. This is the default setting and instructs the program to generate a detailed tube layout. The specified tube count of 124 is used in the calculations irregardless of whether or not this box is checked.


The baffle cut, central spacing and thickness are entered on the Geometry/Baffles form as shown. The number of baffles (42) is specified by setting the number of cross passes to 43 . The latter is the number of passes that the shell-side fluid makes across the tube bundle, which is equal to the number of baffle spaces.


The Geometry/Clearances form is used to specify the number of pairs of sealing strips, which is one in this case. For this problem, no other entries are required on this form.


Nozzle data are entered next. The first entry on the Geometry/Nozzles form is the piping standard to be used. With this entry and the schedule number, the program brings up a table of pipe sizes from which the nozzle ID can be selected. The piping standard is used solely to provide this convenience
to the user. The default standard (number 01 on the list) corresponds to the most commonly used piping.


The total thickness of both tubesheets is entered on the Geometry/Optional form shown below. If this value is not supplied, the program uses one-fifth of the shell ID for this item.


Stream data and fouling factors are entered on the Process form as shown below. Notice that only one outlet temperature (or the exchanger duty) need be given.


Physical properties of the hot fluid (kerosene) are entered next. Several forms are needed to accomplish this task, the first of which is used to specify the input option for the data. For bulk property data, as we have in this case, the mixture properties via grid option is chosen. The component by component option provides an alternate data entry method for bulk property streams, pure components and ideal mixtures. (See Note below.) The third option, component and grid properties, allows the user to override some stream properties generated from pure-component properties. For a stream with defined composition, clicking on the Property Generator button accesses the thermodynamics interface. If the HYSYS or PRO II process simulators are installed on the computer running Xist, then the thermodynamic routines and physical property data banks of these programs can be used directly in Xist. Alternatively, the VMG thermodynamic package can be selected.


Temperature and pressure ranges for the bulk stream properties are specified on the T\&P form. At least one pressure and three temperatures must be entered. Since constant fluid properties are used in this case, a single pressure level is sufficient. The temperatures must be entered in either ascending or descending order. It is also important for the temperature range to include the tube wall temperature at all points in the exchanger. Otherwise, the program will extrapolate the data to obtain fluid properties at the wall temperature, and a warning message will be issued. With constant fluid properties, the extrapolation would have no effect in the present case. In general, however, extrapolation to the wall temperature should be avoided. The T\&P form for the hot fluid follows.

| Input Summary <br> + Geometry <br> 氖 Piping <br> † 己 Process <br> $\square$ Hot Fluid Properties <br> $+\square$ Cold Fluid Properties <br> + 0 Design <br> + I Control | Pressure | psia | 50 |  |  |  |  | $\wedge$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Profile 1 | Profile 2 | Profile 3 | Profile 4 | Profile 5 |  |
|  | Temperature 1 | F | 390 |  |  |  |  |  |
|  | Temperature 2 | F | 250 |  |  |  |  |  |
|  | Temperature 3 | F | 150 |  |  |  |  |  |
|  | Temperature 4 | F |  |  |  |  |  |  |
|  | Temperature 5 | F |  |  |  |  |  |  |
|  | Temperature 6 | F |  |  |  |  |  |  |
|  | Temperature 7 | F |  |  |  |  |  |  |
|  | Temperature 8 | F |  |  |  |  |  |  |
|  | Temperature 9 | F |  |  |  |  |  |  |
|  | Temperature 10 | F |  |  |  |  |  |  |
|  | Temperature 11 | F |  |  |  |  |  |  |
|  | Temperature 12 | F |  |  |  |  |  |  |
|  | Temperature 13 | F |  |  |  |  |  |  |
|  | Temperature 14 | F |  |  |  |  |  |  |
|  | Temperature 15 | F |  |  |  |  |  |  |
|  | Temperature 16 | F |  |  |  |  |  |  |
|  | Temperature 17 | F |  |  |  |  |  |  |
|  | Temperature 18 | F |  |  |  |  |  |  |
|  | Temperature 19 | F |  |  |  |  |  | $\checkmark$ |
|  | 4] |  |  |  |  |  | $\bullet$ |  |
| <<Previous Next>> | Clear All Temperature Data |  |  |  |  |  |  |  |

Values of thermal conductivity ( $0.079 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ), density $\left(49.008 \mathrm{lbm} / \mathrm{ft}^{3}\right)$, heat capacity ( $0.59 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ ) and viscosity ( 0.4008 cp ) are entered on the Property Grid form as shown below.

The above procedure is repeated using identical forms for the cold fluid (crude oil). A single pressure of 50 psia and temperatures of $100^{\circ} \mathrm{F}, 150^{\circ} \mathrm{F}$ and $350^{\circ} \mathrm{F}$ are specified on the $\mathrm{T} \& \mathrm{P}$ form. Values of thermal conductivity ( $0.077 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ), density ( $53.066 \mathrm{lbm} / \mathrm{ft}^{3}$ ), heat capacity ( $0.49 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ ) and viscosity $(3.595 \mathrm{cp})$ are then entered on the Property Grid form. This completes the data entry for the present case.

Note: An alternate method for entering bulk property data is to select the component by component option, proceed to the Components form, select <USER DEFINED> from the list and click the $\operatorname{Add}$ button. This opens a form where the properties can be entered at one or two temperatures; no pressure dependence can be specified. An option is included to generate hydrocarbon properties based on user-supplied values of API gravity and the Watson characterization factor (see Appendix E).

When all necessary data have been entered, the traffic signal icon on the tool bar shows a green light, and clicking on the icon then executes the program. Upon completion, the Output Summary is displayed on the screen. More detailed results are contained in a number of additional report files. Warning messages, if any, are contained in the Runtime Messages report file.


The Output Summary and warning messages for the present case are shown below. Three of the messages involve violation of the TEMA specification for minimum baffle spacing. The warning for the central baffle spacing is clearly incorrect since the value of 3.85 in . is exactly equal to the TEMA minimum of 0.2 times the shell ID. This message is apparently due to a minor error in the computer code; it can be eliminated by entering a slightly larger value of 3.85001 in .

The values calculated by Xist for the inlet and outlet baffle spacings are given in the detailed output file as 3.6515 in . and 2.4985 in ., respectively, both of which are below the TEMA minimum. These values satisfy the following equation for the tube length:

$$
\begin{equation*}
L=\left(n_{b}-1\right) B+B_{\text {in }}+B_{\text {out }}+\text { total tubesheet thickness } \tag{7.62}
\end{equation*}
$$

Xist Output Summary and Runtime Messages for Example 7.3

| Xist E Ver. 4.00 SP2 9/20/2005 18:18 SN: 1600201024 <br> Rating - Horizontal Multipass Flow TEMA AES Shell With Single-Segmental Baffles |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No Data Check Messages. See Runtime Message Report for Warning Messages. |  |  |  |  |  |
| Proces <br> Fluid name | nditions | Hot Shel kerosene | side | Cold Tu |  |
| Flow rate | (1000-lb/hr) |  | 45.0000 |  | 150.000 |
| Inlet/Outlet Y | (Wt. frac vap.) | 0.000 | 0.000 | 0.000 | 0.000 |
| Inlet/Outlet T | (Deg F) | 390.00 | 250.00 | 100.00 | 150.57 |
| Inlet P/Avg | (psia) | 50.000 | 49.009 | 50.000 | 44.827 |
| dP/Allow. | (psi) | 1.983 | 15.000 | 10.346 | 5.000 |
| Fouling | (ft2-hr-F/Btu) |  | 0.00200 |  | 0.00300 |
| Exchanger Performance |  |  |  |  |  |
| Shell h | (Btu/ft2-hr-F) | 253.56 | Actual U | (Btu/ft2-hr-F) | 65.57 |
| Tube h | (Btu/ft2-hr-F) | 219.33 | Required U | (Btu/ft2-hr-F) | 46.25 |
| Hot regime | $(-)$ | Sens. Liquid | Duty | (MM Btu/hr) | 3.7166 |
| Cold regime | (-) | Sens. Liquid | Area | (ft2) | 443.662 |
| EMTD | (Deg F) | 181.1 | Overdesign | (\%) | 41.75 |

## Xist Output Summary and Runtime Messages for Example 7.3 (continued)

| Shell Geometry |  |  | Baffle Geometry |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| TEMA type | (-) | AES | Baffle type | (-) | Single-Seg. |
| Shell ID | (inch) | 19.2500 | Baffle cut | (Pct Dia.) | 20.00 |
| Series | (-) | 1 | Baffle orientation | (-) | PERPEND. |
| Parallel | (-) | 1 | Central spacing | (inch) | 3.8500 |
| Orientation | (deg) | 0.00 | Crosspasses | (-) | 43 |
| Tube Geometry |  |  | Nozzles |  |  |
| Tube type | (-) | Plain | Shell intel | (inch) | 3.0680 |
| Tube OD | (inch) | 1.0000 | Shell outlet | (inch) | 3.0680 |
| Length | (ft) | 14.000 | Inlet height | (inch) | 1.6875 |
| Pitch ratio | (-) | 1.2500 | Outlet height | (inch) | 1.6875 |
| Layout | (deg) | 90 | Tube inlet | (inch) | 4.0260 |
| Tubecount | $(-)$ | 124 | Tube outlet | (inch) | 4.0260 |
| Tube Pass | (-) | 4 |  |  |  |
| Thermal Resistance, \% |  | Velocities, ft/sec |  | Flow Fractions |  |
| Shell | 25.84 | Shellside | 1.22 | A | 0.224 |
| Tube | 35.86 | Tubeside | 6.68 | B | 0.371 |
| Fouling | 36.71 | Crossflow | 2.04 | C | 0.135 |
| Metal | 1.599 | Window | 1.15 | E | 0.270 |
|  |  |  |  | F | 0.000 |


| Unit ID $\mathbf{1 0 0}$ - WARNING MESSAGES (CALCULATIONS CONTINUE) |
| :--- |
| The B-stream flow fraction is very low. check the design. |
| The inlet spacing is less than the TEMA minimum. |
| The central spacing is less than the TEMA minimum. |
| The outlet spacing is less than the TEMA minimum. |

In Example 5.1, the tubesheet thickness was neglected in calculating the number of baffles, and hence the discrepancy. [Notice that the baffle thickness is not included in Equation (7.62), indicating that the program interprets baffle spacing as center-to-center distance, i.e., as the baffle pitch.]

By decreasing the number of cross passes from 43 to 42 , the inlet and outlet spacings increase to 5.9374 in. and 4.0626 in., respectively, which are above the minimum. However, two new warning messages appear to the effect that the inlet and outlet spacings are below the recommended minimum spacings. These messages persist until the number of cross passes is reduced to 37 , giving inlet and outlet spacings of 17.3668 in . and 11.8832 in ., respectively. These values include allowances for nozzles, flanges and bolts, plus adequate work spaces for welding the nozzles to the shell and bolting the front and rear heads to the shell.

The results obtained with the HTRI method are compared with those from other methods in the two tables below. The greatest differences are in the heat-transfer coefficients; the HTRI method gives significantly higher (less conservative) values for both $h_{i}$ and $h_{o}$. As a result, the exchanger is over designed by about $42 \%$ according to the HTRI results.

| Item | Simplified Delaware | Delaware | HEXTRAN | HTRI |
| :--- | :--- | :--- | :--- | :--- |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 156 | - | 156.2 | 219.3 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 122 | 156.6 | 191.2 | 253.6 |
| $\Delta P_{i}(\mathrm{psi})$ | 10.2 | - | 10.06 | 10.35 |
| $\Delta P_{o}(\mathrm{psi})$ | 2.2 | 1.31 | 2.11 | 1.98 |


| Item | Wills-Johnston | HTRI |
| :--- | :---: | :--- |
| $\Delta P_{o}(\mathrm{psi})$ | 1.45 | 1.98 |
| Stream flow fraction |  |  |
| $A$ | 0.276 | 0.224 |
| $B$ | 0.345 | 0.371 |
| $C$ | 0.122 | 0.135 |
| $E$ | 0.257 | 0.270 |
| $F$ | 0 | 0 |

The flow fractions predicted by the Wills-Johnston method are in reasonably good agreement with the HTRI values. For the $A$ stream, the difference is about $23 \%$; the differences are $10 \%$ or less for the other streams. The two methods differ by about $27 \%$ in the shell-side pressure drop, however.

Results from both the Delaware and Stream Analysis methods indicate that the baffle spacing may be too small, leading to large leakage flows and a very low cross-flow fraction. To investigate this situation, several additional runs were made with Xist for central baffle spacings ranging from 0.2 to 0.3 shell diameters. The results are summarized in the following table.

| Parameter | Case 1 | Case 2 | Case 3 | Case 4 | Case 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $B / D_{s}$ | 0.20 | 0.21 | 0.22 | 0.25 | 0.30 |
| Stream flow fraction |  |  |  |  |  |
| A | 0.228 | 0.218 | 0.213 | 0.198 | 0.179 |
| $B$ | 0.371 | 0.380 | 0.388 | 0.409 | 0.439 |
| C | 0.135 | 0.138 | 0.141 | 0.148 | 0.157 |
| E | 0.270 | 0.264 | 0.259 | 0.244 | 0.224 |
| $F$ | 0 | 0 | 0 | 0 | 0 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 253.6 | 250.9 | 248.0 | 241.8 | 230.1 |
| $\Delta P_{o}$ (psi) | 1.98 | 1.84 | 1.70 | 1.48 | 1.10 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 65.57 | 65.39 | 65.19 | 64.75 | 63.88 |
| $\Delta T_{\text {mean }}\left({ }^{\circ} \mathrm{F}\right)$ | 181.1 | 181.3 | 181.4 | 181.7 | 182.2 |
| Over-design (\%) | 41.75 | 41.48 | 41.15 | 40.47 | 38.91 |

It can be seen that exchanger performance decreases continuously as the baffle spacing increases. The mean driving force increases with baffle spacing as expected, but the percentage increase is small and insufficient to compensate for the decrease in the shell-side heat-transfer coefficient. Factors contributing to this behavior are the very large mean driving force of approximately $180^{\circ} \mathrm{F}$, the large temperature approach (approximately $100^{\circ} \mathrm{F}$ ) and the high shell-side Reynolds number (about 30,000 ). Thus, despite the large leakage flows and the very low cross-flow fraction, the minimum baffle spacing is optimal for this unit.

## Example 7.4

Use the Xist module of the HTRI Xchanger Suite to obtain a final design for the kerosene/crude-oil exchanger of Example 5.1.

## Solution

Xist is run in design mode for this case. Data entry is similar to that for the rating case in the previous example:
(a) Geometry/Shell

The Case Mode is set to Design and the shell ID is left unspecified as it will be calculated by the program. Other settings are the same as for the rating case.
(b) Geometry/Tubes

The tube OD ( 1 in. ), pitch ( 1.25 in. ), wall thickness ( 0.083 in .), and layout angle ( $90^{\circ}$ ) are entered as before. The number of tube passes and the tube length specified here are irrelevant because they will be varied during the calculations as specified on the Design form. Hence, the default values can be used here. The number of tubes is left unspecified; it is to be calculated by the program.
(c) Geometry/Baffles

No entries are made on this form. The number of baffles, the cut, spacing, and thickness are to be calculated by the program.
(d) Geometry/Clearances

No entries are made on this form. The number of sealing strips is to be determined by the program.
(e) Geometry/Nozzles

No entries are made on this form. The nozzle sizes are to be determined by the program.
(f) Geometry/Optional

The tubesheet thickness is left unspecified; it will be set by the program based on the calculated shell size. The floating head support plate option is set to Yes. The purpose of this plate is to support the weight of an internal floating head (type S or T ). It was omitted in the rating calculation for consistency with the hand calculations and HEXTRAN. Since the support plate is a full circle baffle, the tube length between the plate and the rear tubesheet ( 4 in . in Xist) is ineffective for heat transfer. Hence, Xist reduces the effective tube length by 4 in . when this option is selected.
(g) Process

The entries on this form are the same as for the rating case. The kerosene outlet temperature and the allowable pressure drops constitute the design specifications.
(h) Fluid Properties

Hot and cold fluid properties are entered exactly as in the rating case.
(i) Design/Geometry

The parameters to be varied in the design calculations and their allowable ranges are specified on this form as shown below. No restrictions are placed on the ranges of shell diameter and

baffle spacing. Based on the results of previous examples, the minimum number of tube passes is set to 4 and the range for tube length is specified as $8-20 \mathrm{ft}$ with an increment of 1 ft .

The shortcut method is normally used for design calculations because it is much faster than the rigorous method. This is the default setting. The program automatically performs a rigorous rating calculation on the best exchanger configuration obtained in the design run to ensure its validity.
(j) Design/Constraints

The allowable range for tube-side velocity is set at $3-8 \mathrm{ft} / \mathrm{s}$ on this form as shown below.


The Output Summary for the design run is given below. The exchanger consists of a $19.25-\mathrm{in}$. shell containing 126 tubes with a length of 12 ft . This configuration is similar to the designs obtained previously by hand and using HEXTRAN.

Xist Output Summary for Example 7.4: Design Run

| Xist E Ver. 4.00 SP2 9/21/2005 15:24 SN: 1600201024 |  |  |  |  | US Units |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Design - Horizontal Multipass Flow TEMA AES Shell With Single-Segmental Baffles |  |  |  |  |  |
| No Data Check Messages. See Runtime Message Report for Warning Messages. |  |  |  |  |  |
|  |  |  |  |  |  |  |
| Process Conditions |  | Hot Shellside |  | Cold Tubeside |  |
| Fluid name |  | kerosene | oil |  |  |
| Flow rate | (1000-lb/hr) |  | 45.0000 |  | 150.000 |
| Inlet/Outlet Y | (Wt. frac vap) | 0.000 | 0.000 | 0.000 | 0.000 |
| Inlet/Outlet T | (Deg F) | 390.00 | 250.00 | 100.00 | 150.57 |
| Inlet P/Avg | (psia) | 50.000 | 49.313 | 50.000 | 45.094 |
| dP/Allow. | (psi) | 1.373 | 15.000 | 9.812 | 15.000 |
| Fouling | (ft2-hr-F/Btu) |  | 0.00200 |  | 0.00300 |
|  |  | Exchanger P | erformance |  |  |
| Shell h | (Btu/ft2-hr-F) | 231.49 | Actual U | (Btu/t2-hr-F) | 62.30 |
| Tube h | (Btu/ft2-hr-F) | 203.60 | Required U | (Btu/t2-hr-F) | 54.81 |
| Hot regime | (-) | Sens. Liquid | Duty | (MM Btu/hr) | 3.7166 |
| Cold regime | (-) | Sens. Liquid | Area | (ft2) | 374.262 |
| EMTD | ( Deg F) | 181.2 | Overdesign | (\%) | 13.67 |

## Xist Output Summary for Example 7.4: Design Run (continued)

| Shell Geometry |  |  | Baffle Geometry |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| TEMA type | (-) | AES | Baffle type | (-) | Single-Seg. |
| Shell ID | (inch) | 19.2500 | Baffle cut | (Pct Dia.) | 16.97 |
| Series | (-) | 1 | Baffle orientation | (-) | PERPEND. |
| Parallel | (-) | 1 | Central spacing | (inch) | 4.0548 |
| Orientation | (deg) | 0.00 | Crosspasses | (-) | 29 |
| Tube Geometry |  |  | Nozzles |  |  |
| Tube type | (-) | Plain | Shell inlet | (inch) | 3.0680 |
| Tube OD | (inch) | 1.0000 | Shell outlet | (inch) | 3.0680 |
| Length | (ft) | 12.000 | Inlet height | (inch) | 1.6875 |
| Pitch ratio | (-) | 1.2500 | Outlet height | (inch) | 1.6875 |
| Layout | (deg) | 90 | Tube inlet | (inch) | 4.0260 |
| Tubecount | $(-)$ | 126 | Tube outlet | (inch) | 4.0260 |
| Tube Pass | (-) | 4 |  |  |  |
| Thermal Resistance, \% |  | Velocities, ft/sec |  | Flow Fractions |  |
| Shell | 26.92 | Shellside | 1.15 | A | 0.234 |
| Tube | 36.69 | Tubeside | 5.59 | B | 0.363 |
| Fouling | 34.88 | Crossflow | 1.93 | C | 0.135 |
| Metal | 1.519 | Window | 1.41 | E | 0.268 |
|  |  |  |  | F | 0.000 |

The baffle cut of approximately $17 \%$ is within the acceptable range ( $15-45 \%$ ), but below the preferred range for single-phase fluids ( $20-35 \%$ ). Based on the tube layout generated by Xist, the cut was increased to $21 \%$ and the configuration was checked by running Xist in rating mode. For this run, the actual tube layout generated by Xist was used. The layout contains 132 tubes, in contrast to the tube count of 126 calculated by the program. The difference of six tubes is equal to the number of tie rods calculated by Xist. The program does not place tie rods (or sealing strips) on the tube-layout diagram. In order to use the actual tube layout in a rating calculation, the user must place these items on the diagram by specifying which tubes are to be replaced by tie rods. This is done on the Geometry/Tube Layout form shown below. Right-clicking on an item in the tube field brings up a menu for modifying the item. Sealing strips can be added by right-clicking in the desired location between the baffle and shell. The shaded circles on the tube-layout diagram represent tie rods.


Note: The purpose of tie rods is to hold the tube bundle assembly together. They are metal rods that are screwed into the tubesheet at the stationary (front) end, pass through holes in the baffles, and are fastened to the last baffle with lock nuts. Between the baffles, the rods are fitted with sleeves that act as spacers to hold the baffles securely in place. The minimum number of tie rods required by TEMA standards varies from 4 to 12 and the rod diameter varies from $3 / 8$ to $5 / 8$ in., depending on the shell diameter. Tie rods and spacers also help block the bundle bypass flow area, and extra sets may be installed for this purpose. However, they are not as effective as sealing strips in reducing the bypass flow.

The results of the rating run show that the change in baffle cut has a very small effect on exchanger performance, decreasing the over-design from $13.7 \%$ to $13.1 \%$. Therefore, this configuration is accepted as final.

The ribbon-banded tube layout generated by Xist has all of the pass partition lanes oriented normal to the cross-flow direction, thereby eliminating the pass partition bypass stream. However, the tubes are not allocated equally among the passes; passes one and four each contain 26 tubes, while passes two and three each contain 37 . As a result, the Reynolds number in passes 2 and 3 is about 8500, which is in the transition region. This situation is not a major concern since the Reynolds number is near the upper end of the transition region. Furthermore, the HTRI correlations are based on a large amount of experimental data in the transition region and are considered reliable in this regime.

Two other tube layout patterns are available for this unit, H-banded and quadrant. The H-banded layout has nearly the same allocation of tubes among passes as the ribbon-banded layout. The quadrant pattern (shown below) has nearly the same number of tubes in each pass, but with 134 tubes (plus 6 tie rods), the tube-side Reynolds number is still below 10,000 .

## Quadrant Tube Layout Generated by Xist: Baffle Cut of 23\%



The Reynolds number can be increased by eliminating some of the tubes. Although this is not necessary in the present context, it is done here to illustrate how the tube layout can be modified in Xist. Six tubes are converted to tie rods and another ten tubes are removed to obtain a bundle having a total of 124 tubes with 31 tubes in each pass. One pair of sealing strips and four pass partition seal rods (1-in. diameter) are also added in accordance with the values calculated by Xist for this tube pattern. (The modified tube layout is shown at the end of this section.) In addition, the baffle cut is increased to $23 \%$ to better conform with the tube layout. The program is then run in rating mode using the modified tube layout as input. The Output Summary given below shows that the exchanger performance is satisfactory with an over-design of $12 \%$.

## Xist Output Summary for Example 7.4: Rating Run with Modified Quadrant Layout

| Xist E Ver. 4.00 SP2 10/3/2005 16:56 SN: 1600201024 |  |  |  |  | US Units |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Rating - Horizontal Multipass Flow TEMA AES Shell With Single-Segmental Baffles |  |  |  |  |  |
| No Data Check Messages. See Runtime Message Report for Warning Messages. |  |  |  |  |  |
|  |  |  |  |  |  |  |
| Process Conditions Fluid name |  | Hot Shellside |  | Cold Tubeside |  |
|  |  | kerosene | - oil | 150.000 |  |
| Flow rate | (1000-lb/hr) |  | 45.0000 |  |  |  |
| Inlet/Outlet Y | (Wt. frac vap.) | ) 0.000 | 0.000 | 0.000 | 0.000 |
| Inlet/Outlet T | (Deg F) | ) 390.00 | 250.00 | 100.00 | 150.57 |
| Inlet P/Avg | (psia) | ) 50.000 | 49.325 | 50.000 | 45.355 |
| dP/Allow. | (psi) | ) 1.351 | 15.000 | 9.290 | 15.000 |
| Fouling | (ft2-hr-F/Btu) |  | 0.00200 |  | 0.00300 |
| Exchanger Performance |  |  |  |  |  |
| Shell h | (Btu/tt2-hr-F) | 211.66 | 6 Actual U | (Btu/ft2-hr-F) | 62.37 |
| Tube h | (Btu/ft2-hr-F) | 219.33 | 3 Required U | (Btu/ft2-hr-F) | 55.71 |
| Hot regime | $(-)$ | Sens. Liquid | d Duty | (MM Btu/hr) | 3.7166 |
| Cold regime | $(-)$ | Sens. Liquid | d Area | (ft2) | 368.321 |
| EMTD | (Deg F) | 181.1 | 1 Overdesign | (\%) | 11.97 |
| Shell Geometry |  |  | Baffle Geometry |  |  |
| TEMA type | (-) | AES | Baffle type | (-) | Single-Seg. |
| Shell ID | (inch) | 19.2500 | Baffle cut | (Pct Dia.) | 23.00 |
| Series | (-) | 1 | Baffle orientation | (-) | PERPEND. |
| Parallel | (-) | 1 | Central spacing | (inch) | 4.0548 |
| Orientation | (deg) | 0.00 | Crosspasses | (-) | 29 |
| Tube Geometry |  |  | Nozzles |  |  |
| Tube type | (-) | Plain | Shell inlet | (inch) | 3.0680 |
| Tube OD | (inch) | 1.0000 | Shell outlet | (inch) | 3.0680 |
| Length | (ft) | 12.000 | Inlet height | (inch) | 2.0625 |
| Pitch ratio | (-) | 1.2500 | Outlet height | (inch) | 2.0625 |
| Layout | (deg) | 90 | Tube inlet | (inch) | 4.0260 |
| Tubecount | (-) | 124 | Tube outlet | (inch) | 4.0260 |
| Tube Pass | (-) | 4 |  |  |  |
| Thermal Resistance, \% |  | Velocities, ft/sec |  | Flow Fractions |  |
| Shell | 29.45 | Shellside | 1.17 | A | 0.207 |
| Tube | 34.11 | Tubeside | 6.68 | B | 0.348 |
| Fouling | 34.92 | Crossflow | 1.96 | C | 0.136 |
| Metal | 1.521 | Window | 0.96 | E | 0.262 |
|  |  |  |  | F | 0.047 |

Values of the final design parameters using both tube layouts are summarized in the following table. The exchanger setting plan and tube layout diagrams generated by Xist are also shown below.

| Item | Ribbon-banded <br> tube layout | Modified quadrant <br> tube layout |
| :--- | :--- | :--- |
| Exchanger type | AES | AES |
| Shell size (in.) | 19.25 | 19.25 |
| Surface Area $\left(\mathrm{ft}^{2}\right.$ ) | 374 | 368 |
| Number of tubes | 126 | 124 |
| Tube OD (in.) | 1.0 | 1.0 |
| Tube length (ft) | 12 | 12 |
| Tube BWG | 14 | 14 |
| Tube passes | 4 | 4 |


| Item | Ribbon-banded <br> tube layout | Modified quadrant <br> tube layout |
| :--- | :--- | :--- |
| Tube pitch (in.) | 1.25 | 1.25 |
| Tube layout | Square | Square |
| Tubesheet thickness (in.) | $1.925^{*}$ | $1.925^{*}$ |
| Number of baffles | 28 | 28 |
| Baffle cut (\%) | 21 | 23 |
| Baffle thickness (in.) | 0.1875 | 0.1875 |
| Central baffle spacing (in.) | 4.05 | 4.05 |
| Inlet baffle spacing (in.) | 15.84 | 15.84 |
| Outlet baffle spacing (in.) | 10.84 | 10.84 |
| Length beyond | 4 | 4 |
| support baffle (in.) |  |  |
| Sealing strip pairs | 1 | 1 |
| Seal rods | 0 | 4 |
| Tube-side nozzles | 4 -in. schedule 40 | 4 -in. schedule 40 |
| Shell-side nozzles | 3 -in. schedule 40 | 3 -in. schedule 40 |
| Tube-side velocity (ft/s) | 8.0 (passes 1,4) | 6.7 |
| $\Delta P_{i}$ (psi) | 5.6 (passes 2,3) |  |
| $\Delta P_{o}$ (psi) | 9.8 | 9.3 |
| $R e_{i}$ | 1.3 | 1.4 |
| Over-design (\%) | 12,150 (passes 1,4) | 10,190 |

* Thickness of individual tubesheets.


## Setting Plan and Tube Layouts for Example 7.4



### 7.8.2 HTFS/Aspen

The software package developed by HTFS and currently available from Aspen Technology contains six major programs for design and rating of the following types of heat-transfer equipment: air-cooled heat exchangers (ACOL), plate-and-frame heat exchangers (APLE), fired heaters and furnaces (FRAN), plate-fin brazed heat exchangers (MUSE), and shell-and-tube/hairpin heat exchangers (TASC). As mentioned in Chapter 4, the TASC module consists of two interconnected programs, TASC Thermal for thermal/hydraulic design/rating and TASC Mechanical for mechanical design/rating. The former handles all thermal and hydraulic calculations; it also performs tube vibration analyses and generates tube layouts. TASC Mechanical performs stress analyses on the individual components of shell-and-tube exchangers; it also generates a complete list of parts and material specifications for a new shell-and-tube heat exchanger. The HTFS software can be run on a stand-alone basis or it can be accessed through the HYSYS or Aspen Plus process simulators.
As previously noted, TASC uses a version of the Stream Analysis method for shell-side calculations. It performs an incremental analysis and calculates the flow fractions of the shell-side streams in each increment, or zone, along the length of the shell. All TEMA shell types are supported, as are bundles with no-tubes-in-windows and rod-baffle arrangements.

TASC Thermal can be run in three different modes, called checking, simulation, and design. The checking mode is similar to rating mode in Xist. Either checking or simulation mode can be used to rate a heat exchanger. In either of these two modes, TASC generates a complete tube layout that can be modified by the user, if necessary, to fit an existing tube layout. In design mode TASC finds the optimal heat-exchanger configuration within a given set of constraints based on either minimum cost or minimum heat-transfer area, as specified by the user.

Design and analysis of shell-and-tube heat exchangers using TASC is illustrated in the following examples. Data entry is similar to that for double-pipe exchangers, as described in Examples 4.5 and 4.6.

## Example 7.5

Use TASC to rate the final configuration of the kerosene/crude-oil exchanger of Example 5.1 and compare the results with those obtained previously using other software.

## Solution

The inlet pressures of both streams were (arbitrarily) set to 50 psia . Two runs were made, one with an H -banded tube layout and the other with a ribbon-banded layout. The data that were entered on each input form are listed below. Parameters not listed were either left at their default settings or were left unspecified to be calculated by the software.
(a) Start up

Calculation Mode: Simulation
Basic Input Mode: Not checked
(b) Exchanger Geometry
(i) Exchanger General

Type: AES
No. Exchangers in Series: 1
No. Exchangers in Parallel: 1
Shell Inside Diameter: 19.25 in.
Side for Hot Stream: Shell side Hot
(ii) Exchanger Details

Tubesheet Thickness: 2 in.
Note: The thickness of one tubesheet is entered here, not the total thickness of both tubesheets as in Xist and HEXTRAN.
(c) Bundle Geometry
(i) Tube Details

Tube Outside Diameter: 1 in. Tube Pattern: Square
Tube Wall Thickness: 0.083 in. Tube Length: 168 in.
Tube Pitch: 1.25 in.
(ii) Bundle Layout

Number of Tube-side Passes: 4
Number of Sealing Strip Pairs: 1
Tube Layout Data: Revise from input
Pass partitions, Band Layout: H Banded (1st run); Ribbon Banded (2nd run)
(iii) Bundle Size

Tube Count (effective): 124
(iv) Transverse Baffles

Baffle Pitch: 3.85 in. Baffle Cut: 20\%
Baffle Thickness: 0.1875 in. Number of Baffles: 42
Note: TASC distinguishes between baffle pitch and baffle spacing; the spacing is defined as the face-to-face distance between baffles.
(v) Special Baffles/Supports

Support/Blanking Baffle: No
Note: The support baffle is omitted for consistency with previous calculations.
(d) Nozzles.

Inlet and outlet nozzles are specified for both the tube side and the shell side. For the tube side, nozzle ID is 4.026 in.; for the shell side, it is 3.068 in .
(e) Process.

|  | Hot stream | Cold stream |
| :--- | :--- | :--- |
| Total mass flow rate $(\mathrm{lb} / \mathrm{h})$ | 45,000 | 150,000 |
| Inlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 390 | 100 |
| Inlet pressure (psia) | 50 | 50 |
| Inlet mass quality | 0 | 0 |
| Outlet mass quality | 0 | 0 |
| Fouling resistance <br> $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ | 0.002 | 0.003 |
| Heat load $(\mathrm{Btu} / \mathrm{h})$ | $3,717,000$ | $3,717,000$ |

(f) Physical properties.

The physical property data were entered as in Example 4.5. For each stream, the Stream Data Source was set to <Direct Input> and the data were entered on the spreadsheet at a single pressure level ( 50 psia ) and a single temperature (stream inlet temperature).

The results summaries for the two runs are given below along with the tube layout drawings generated by TASC, which always include tie rods and, if present, sealing strips. The H-banded layout contains 120 tubes divided equally into 30 tubes per pass. Note that the vertical pass partition lane is aligned with the cross-flow direction, so this arrangement produces an $F$ leakage stream. TASC automatically includes a seal on the in-line pass partition lane with each pair of sealing strips used. The ribbon-banded layout contains 124 tubes and all pass partitions lanes are normal to the crossflow direction. However, two passes each contain 36 tubes while the other two passes each contain 26 tubes. As a result, the flow in the passes with 36 tubes is in the transition region. (It should be noted that TASC ignores the unequal tube apportionment in performing the rating calculations.) Notice that the H-banded layout yields a higher shell-side heat-transfer coefficient despite the presence of the $F$ stream, perhaps because the baffle cut is adjusted to $18 \%$ for compatibility with this layout.

## TASC Tube Layouts for Example 7.5



## TASC Results Summary for Example 7.5: H-Banded Layout

| Geometric details |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shell type/series/parallel | AES |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 19.3 | in | 168.0 | in | 454.5 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 4 |  | 124 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 1.25(90) | in |
| No of baffles/pitch/cut | 42 |  | 3.85 | in | 18 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 45000.0 | lb/h | 150000.0 | lb/h |  |  |
| Inlet temperature shell/tube | 390.0 | ${ }^{\circ} \mathrm{F}$ | 100.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 228.76 | ${ }^{\circ} \mathrm{F}$ | 158.24 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 0.0/0.0 |  | 0.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 1.413 | psi | 9.545 | psi |  |  |
| Velocity highest shell xflow/tube | 1.8 | $\mathrm{ft} / \mathrm{s}$ | 6.8 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 198 | Btu/h ft ${ }^{2}{ }^{\circ} \mathrm{F}$ | 162 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 3930 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 500 | Btu/h ft ${ }^{\circ} \mathrm{F}$ | 278 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 87.0 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 58.5 | Btu/h ft ${ }^{\circ} \mathrm{F}$ | 58.5 | Btu/ $\mathrm{fft}^{2}$ © F |
| Heat load/eff wtd mtd | 4281 | kBtu/h | 165.11 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.000 |  | 1.152 |  |  |  |

## TASC Results Summary for Example 7.5: Ribbon-Banded Layout

TASC Version 5.01 - SIMULATION

| Geometric details |  |  |  |  | 1 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Shell type/series/parallel | AES |  | 1 | 454.5 | $\mathrm{ft}^{2}$ |  |
| Shell diam/tube length/total area | 19.3 | in | 168.0 | in |  |  |
| No of passes/no of plain tubes | 4 |  | 124 |  | $1.25(90)$ | in |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 20 | $\%$ |

## TASC Results Summary for Example 7.5: Ribbon-Banded Layout (continued)

| Process details |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Total mass flowrates shell/tube | 45000.0 | $\mathrm{lb} / \mathrm{h}$ | 150000.0 | $\mathrm{lb} / \mathrm{h}$ |  |  |
| Inlet temperature shell/tube | 390.0 | ${ }^{\circ} \mathrm{F}$ | 100.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 230.66 | ${ }^{\circ} \mathrm{F}$ | 157.56 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | $0.0 / 0.0$ |  | $0.0 / 0.0$ |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 1.697 | psi | 9.545 | psi |  |  |
| Velocity highest shell xflow/tube | 2.17 | $\mathrm{ft} / \mathrm{s}$ | 6.8 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 184 | $\mathrm{Btu} / \mathrm{hft}{ }^{\circ}{ }^{\circ} \mathrm{F}$ | 162 | $\mathrm{Btu} / \mathrm{hft}^{\circ}{ }^{\circ} \mathrm{F}$ | 3930 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 500 | $\mathrm{Btu} / \mathrm{hft}^{\circ}{ }^{\circ} \mathrm{F}$ | 278 | $\mathrm{Btu} / \mathrm{hft}^{\circ}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 84.2 | $\mathrm{Btu} / \mathrm{hft}^{\circ} \mathrm{F}$ | 57.2 | $\mathrm{Btu} / \mathrm{hft}^{\circ} \mathrm{F}$ | 57.2 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 4231 | $\mathrm{kBtu} / \mathrm{h}$ | 166.87 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.000 |  | 1.138 |  |  |  |

TASC generates warning messages regarding the inlet and outlet baffle spacings similar to the Xist warnings, although the minimum spacings recommended by TASC are different: 8.7 in . for the inlet and 12.7 in . for the outlet. The TASC results are compared with those obtained in previous examples in the following tables, which were prepared using the full output file. Results obtained with Xist using an H -banded tube layout are also included for comparison.

| Item | HEXTRAN | Xist <br> H-Banded | Xist <br> Ribbon <br> banded | TASC <br> H-Banded | TASC Ribbon banded |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 156.2 | 219.3 | 219.3 | 194 | 194 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 191.2 | 260.1 | 253.6 | 198 | 184 |
| $\Delta P_{i}(\mathrm{psi})$ | 10.06 | 10.35 | 10.35 | 9.55 | 9.55 |
| $\Delta P_{o}(\mathrm{psi})$ | 2.11 | 2.06 | 1.98 | 1.41 | 1.70 |
|  |  | Xist | Xist | TASC | TASC |
| Item | Wills-Johnston | H-Banded | Ribbon banded | H-Banded | Ribbon banded |
| $\Delta P_{o}$ (psi) | 1.45 | 2.06 | 1.98 | 1.41 | 1.70 |
| Stream flow fraction |  |  |  |  |  |
| A | 0.276 | 0.225 | 0.224 | 0.252 | 0.326 |
| B | 0.345 | 0.319 | 0.371 | 0.221 | 0.298 |
| C | 0.122 | 0.141 | 0.135 | 0.135 | 0.052 |
| E | 0.257 | 0.270 | 0.270 | 0.257 | 0.324 |
| F | 0 | 0.044 | 0 | 0.135 | 0 |


|  | Hand <br> Example 6.1 | Xist | TASC |
| :--- | :--- | :--- | :--- |
| Clearance (in.) | 0.01575 | 0.01565 | 0.01565 |
| Tube-baffle (radial) | 0.09952 | 0.09375 | 0.095 |
| Shell-baffle (radial) | 1.34 | 1.59 | 1.61 |
| Shell-bundle $\left(D_{s}-D_{\text {ott }}\right)$ | - | 0.625 | 0.75 |
| Pass partition (horizontal) | - | 0.625 | 1.5 |
| Pass partition (vertical) | - |  |  |

The shell-side heat-transfer coefficient calculated by TASC is close to the HEXTRAN value and considerably lower than that calculated by the HTRI method. The tube-side coefficient is within
$13 \%$ of the HTRI value and is about $25 \%$ greater than the HEXTRAN value. (Note that the tubeside coefficient of 162 given in the TASC output is actually $h_{i} D_{i} / D_{0}$.) The shell-side pressure drop computed by TASC is within the range of values found by other methods, and for the H -banded layout agrees almost exactly with the Wills-Johnston value. However, the flow fractions of the shellside streams computed by TASC differ greatly from the Wills-Johnston and HTRI values. As shown in the third table above, the clearances used by TASC are similar to those used in the other methods, with the exception of the vertical pass partition clearance in the H-banded layout. (The clearances used in the Wills-Johnston method are those estimated in Example 6.1.) Therefore, the differences in results must be attributed to differences in the correlations for the flow resistances used in the three methods. Indeed, there is a systematic difference in the flow fractions calculated by Xist and TASC; the warning message concerning abnormally low cross-flow fraction is issued by Xist when the $B$-stream fraction is below 0.4 , whereas the threshold is 0.3 for the same warning in TASC.

## Example 7.6

Use TASC to obtain a final design for the kerosene/crude-oil exchanger of Example 5.1.

## Solution

The design procedure consists of the following steps:

- Run TASC in design mode to generate an approximate design.
- Rate the initial design by running TASC in checking or simulation mode using the initial design parameters.
- Modify the design as needed and re-rate until a configuration is obtained that is consistent with the tube layout and that meets all design specifications.
- Run TASC Mechanical to perform the mechanical design calculations and generate a setting plan for the exchanger.
- If no problems are identified in the mechanical design, the unit is acceptable; otherwise, further modification and re-rating is required.
- Consider alternate designs.

Note: Items that require particular attention in TASC Mechanical include tubesheet thickness, nozzle size and schedule number, and nozzle-baffle juxtaposition (as shown on the setting plan).
Input data used for the design run are as follows.
(a) Start up

Calculation Mode: Design
Basic Input Mode: Not checked
(b) Exchanger Geometry
(i) Exchanger General

Type: AES
Side for Hot Stream: Shell side Hot
(c) Bundle Geometry
(i) Tube Details

Tube Outside Diameter: 1 in.
Tube Wall Thickness: 0.083 in.
Tube Pitch: 1.25 in.
Tube Pattern: Square
Maximum Tube Length: 240 in .
Incremental Tube Length: 12 in .
Note: The maximum tube length of 240 in . is the default setting in TASC. Designing for minimum cost generally leads to units with large tube lengths and small shell diameters. Based
on plot space considerations, a maximum length of $20-25 \mathrm{ft}$ is often imposed, especially with floating-head and U-tube exchangers, for which space must be provided to pull the tube bundle. In the present problem, we know from previous examples that with four tube passes, the length of the exchanger will be less than 20 ft .
(ii) Bundle Layout

Minimum Number of Tube-side Passes: 4
Number of Sealing Strip Pairs: 1
(iii) Special Baffles/Supports

Support/Blanking Baffle: Yes
(d) Process.
(i) Process Data

|  | Hot stream | Cold stream |
| :--- | :--- | :--- |
| Total mass flow rate $(\mathrm{lb} / \mathrm{h})$ | 45,000 | 150,000 |
| Inlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 390 | 100 |
| Outlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 250 | 150.6 |
| Inlet pressure $(\mathrm{psia})$ | 50 | 50 |
| Allowable pressure drop (psi) | 15 | 15 |
| Inlet mass quality | 0 | 0 |
| Outlet mass quality | 0 | 0 |
| Fouling resistance $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ | 0.002 | 0.003 |

(ii) Process Constraints

Maximum Tube-side Velocity: $8 \mathrm{ft} / \mathrm{s}$
(e) Physical properties.

Same as example 7.5.
The TASC results summary for the design run is given below. Additional design data obtained from the full output file are:

- Tubesheet thickness: 1.22 in.
- Baffle thickness: 0.1875 in.
- Length beyond support baffle: 6.38 in.
- Shell-side nozzles: 2.5-in. schedule 40 ( 2.469 in . ID)
- Tube-side inlet nozzle: $3.5-\mathrm{in}$. schedule 40 (3.548 in. ID)
- Tube-side outlet nozzle: 3-in. schedule 40 (3.068 in. ID)


## TASC Results Summary for Example 7.6: Design Run

## TASC Version 5.01 - DESIGN

| Geometric details |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Shell type/series/parallel | AES |  | 1 |  |  |  |
| Shell diam/tube length/total area | 17.3 | in | 156.0 | in | 354.0 | $\mathrm{ft}^{2}$ |
| No.of passes/no.of plain tubes | 4 |  | 104 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | $1.25(90)$ | in |
| No.of baffles/pitch/cut | 40 |  | 3.51 | in | 15 | $\%$ |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 45000.0 | $\mathrm{lb} / \mathrm{h}$ | 150000.0 | $\mathrm{lb} / \mathrm{h}$ |  |  |
| Inlet temperature shell/tube | 390.0 | ${ }^{\circ} \mathrm{F}$ | 100.0 | ${ }^{\circ} \mathrm{F}$ |  |  |

## TASC Results Summary for Example 7.6: Design Run (continued)

| Outlet temperature shell/tube | 250.0 | ${ }^{\circ} \mathrm{F}$ | 150.6 | ${ }^{\circ} \mathrm{F}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Inlet/outlet quality shell/tube | 0.0/0.0 |  | 0.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 3.416 | psi | 12.583 | psi |  |  |
| Velocity highest shell xflow/tube | 2.66 | $\mathrm{ft} / \mathrm{s}$ | 7.96 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 216 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 186 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 3930 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 500 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 278 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/ dirty/service | 97.5 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 63.1 | Btu/ $\mathrm{fft}^{2} \mathrm{~F}$ | 59.8 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 3719 | kBtu/h | 184.88 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req) | 1.054 |  |  |  |  |  |

When the initial design configuration is rated by running it in simulation (or checking) mode, the following problems are found:

- The actual tube count (H-banded layout) is 92, compared with the design value of 104.
- The tube-side nozzles are too small; the value of $\rho V_{n}^{2}$ exceeds the TEMA recommended limit.
- The end baffle spacings are too small.
- For the shell-side inlet nozzle, $\rho V_{n}^{2}=2886$. Either a larger nozzle or impingement protection is required.
- The baffle cut is too small, having been adjusted by TASC to $14 \%$ for compatibility with the tube layout.

To rectify these problems, the following changes are made for the next simulation run:

- The number of tubes is changed to 92 .
- The tube-side nozzles are changed to 4 -in. schedule 40.
- The shell-side nozzles are changed to 3 -in. schedule 40.
- The number of baffles is reduced from 40 to 38 .
- The baffle cut is changed to $20 \%$.

With these settings, the problems with the nozzles and end baffle spacings are resolved, and TASC adjusts the baffle cut to $22 \%$ (thereby placing one additional tube row in each window). However, the kerosene outlet temperature is now $253^{\circ} \mathrm{F}$, so the exchanger is slightly under-surfaced. Also, the tube-side velocity is $9.0 \mathrm{ft} / \mathrm{s}$.

Additional surface area can be obtained by increasing the tube length, but this will increase the tube-side pressure drop, which is already near the maximum. Therefore, an additional pair of sealing strips is included for the next trial in an attempt to increase the shell-side heat-transfer coefficient. The results, given below, show that the kerosene outlet temperature is now about $248^{\circ} \mathrm{F}$, which is satisfactory.

## TASC Results Summary for Example 7.6: Final Simulation Run

TASC Version 5.01 - SIMULATION

| Geometric details |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shell type/series/parallel | AES |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 17.3 | in | 156.0 | in | 313.1 | $\mathrm{ft}^{2}$ |
| No.of passes/no.of plain tubes | 4 |  | 92 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 1.25(90) | in |
| No of baffles/pitch/cut | 38 |  | 3.51 | in | 22 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 45000.0 | $\mathrm{lb} / \mathrm{h}$ | 150000.0 | lb/h |  |  |
| Inlet temperature shell/tube | 390.0 | ${ }^{\circ} \mathrm{F}$ | 100.0 | ${ }^{\circ} \mathrm{F}$ |  |  |

## TASC Results Summary for Example 7.6: Final Simulation Run (continued)

| Outlet temperature shell/tube | 247.96 | ${ }^{\circ} \mathrm{F}$ | 151.31 | ${ }^{\circ} \mathrm{F}$ |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Inlet/outlet quality shell/tube | $0.0 / 0.0$ |  | $0.0 / 0.0$ |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 1.72 | psi | 14.611 | psi |  |  |
| Velocity highest shell xflow/tube | 2.1 | $\mathrm{ft} / \mathrm{s}$ | 9.0 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 260 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ | 205 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ | 3910 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 500 | $\mathrm{Btu} / \mathrm{hft}^{\circ}{ }^{\circ} \mathrm{F}$ | 278 | $\mathrm{Btu} / \mathrm{h} \mathrm{ft}^{2} \mathrm{~F}$ |  |  |
| Overall coefficient clean/dirty/service | 111.3 | $\mathrm{Btu} / \mathrm{hft}^{\circ}{ }^{\circ} \mathrm{F}$ | 68.6 | $\mathrm{Btu} / \mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ | 68.6 | $\mathrm{Btu} / \mathrm{hft}{ }^{\circ}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 3771 | $\mathrm{kBtu} / \mathrm{h}$ | 183.15 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 0.991 |  | 0.544 |  |  |  |

Running TASC Mechanical for this configuration reveals no additional problems, and therefore, it is accepted as final. The only potential drawback is the high tube-side velocity in passes 1 and 4. Although with steel tubes this unit is considered acceptable, a second design was developed having a $19.25-\mathrm{in}$. shell. The same procedure was followed, starting with an initial process constraint of $7.5 \mathrm{ft} / \mathrm{s}$ for the tube-side velocity. Both designs are summarized in the following table. Tube layouts and setting plans (from TASC Mechanical) are also shown. Cost estimates generated by TASC indicate that the $19.25-\mathrm{in}$. exchanger is about $15 \%$ more expensive than the smaller unit.

The over-design is approximately $1 \%$ for each of these units. The tube length in the $19.25-\mathrm{in}$. exchanger can be increased to provide a greater safety margin, if desired. A tube length of 13 ft , for example, gives an over-design of about $10 \%$. The same cannot be done with the $17.25-\mathrm{in}$. exchanger without exceeding the maximum allowable tube-side pressure drop.

The overall configuration of the $19.25-\mathrm{in}$. exchanger obtained using TASC is very similar to that of the exchanger designed using Xist. However, there are significant differences in some parameters, including tube layout, inlet baffle spacing and tubesheet thickness. It will be noticed that the surface area reported by TASC is slightly larger than the value given by Xist, despite the fact that the TASC exchanger has fewer tubes. The reason is that the area given by TASC is based on the total tube length ( 12 ft in this case), whereas Xist uses the effective tube length to calculate the heat-transfer area. The effective tube length used by Xist in this case is 11.346 ft , obtained by subtracting the total tubesheet thickness ( 3.85 in ) and the length beyond the support baffle ( 4 in ) from the total tube length. This is the length of the tubes that is effective in transferring heat.

| Item | Design 1 | Design 2 |
| :--- | :--- | :--- |
| Exchanger type | AES | AES |
| Shell size (in.) | 17.25 | 19.25 |
| Surface area (ft ${ }^{2}$ ) | 313 | 377 |
| Number of tubes | 92 | 120 |
| Tube OD (in.) | 1.0 | 1.0 |
| Tube length (ft) | 13 | 12 |
| Tube BWG | 14 | 14 |
| Tube passes | 4 | 4 |
| Tube pitch (in.) | 1.25 | 1.25 |
| Tube layout | Square | Square |
| Tubesheet thickness (in.) | 1.22 | 1.34 |
| Number of baffles | 38 | 31 |
| Baffle cut (\%) | 22 | 25 |
| Baffle thickness (in.) | 0.1875 | 0.1875 |
| Central baffle spacing (in.) | 3.51 | 3.87 |
| End baffle spacing (in.) | 9.20 | 9.91 |
| Length beyond support baffle (in.) | $6.38^{\star}$ | $6.61^{*}$ |

Sealing strip pairs
Tube-side nozzles
Shell-side nozzles
Tube-side velocity ( $\mathrm{ft} / \mathrm{s}$ )
$\Delta P_{i}(\mathrm{psi})$
$\Delta P_{o}(\mathrm{psi})$
Kerosene outlet temp. ( ${ }^{\circ} \mathrm{F}$ )
$R e_{i}$

2
4 in. schedule 40
3 in. schedule 40
8.3 (passes 2,3)
9.9 (passes 1,4)
14.6
1.7

248
12,634 (passes 2,3)
15,041 (passes 1,4)

1
4 in . schedule 40
3 in. schedule 40
6.9
8.8
1.0

248
10,529

* Includes the rear tubesheet thickness and length of tube projection beyond tubesheet.

Setting Plan and Tube Layout for Design 1


## Setting Plan and Tube Layout for Design 2



Note: In TASC the tube length satisfies the following relationship:

$$
\begin{equation*}
L=\left(n_{b}-1\right) B+B_{\text {in }}+B_{\text {out }}+\text { total tubesheet thickness }+ \text { total tube outstand } \tag{7.63}
\end{equation*}
$$

where $B$ is the central baffle spacing (the baffle pitch in TASC), $B_{\text {in }}$ and $B_{\text {out }}$ are the face-to-face distances between the tubesheets and end baffles (the "endspaces" in TASC) plus half a baffle
thickness, and the tube outstand (or tube projection) is the extension of the tube beyond the tubesheet. If a support baffle is present, the distance between this baffle and the inside face of the rear tubesheet is added to the right side of Equation (7.63). (In this case, the corresponding end baffle spacing, $B_{\text {in }}$ or $B_{\text {out }}$, is measured from the support plate rather than the rear tubesheet.) TASC uses a default value of 3 mm ( 0.12 in .) for the front outstand. The default for the rear outstand is either 3 mm or zero, depending on exchanger configuration. The baffle spacings given in the design summary table above and elsewhere in the text correspond to $B, B_{\text {in }}$, and $B_{\text {out }}$. In the present case, $B_{\text {in }}=B_{\text {out }}$ for both designs.

Note: The configuration of the tube-pass partitions in the four-pass H-banded layout is shown in the following diagram.


Front header


Rear header

## References

1. Tinker, T., Shell-side Heat Transfer Characteristics of Segmentally Baffled Shell-and-tube Exchangers, ASME Paper No. 47-A-130, American Society of Mechanical Engineers, 1947.
2. Tinker, T., Shell-Side Characteristics of Shell-and-tube Heat Exchangers, Parts I, II and III, Proc. General Discussion on Heat Transfer, Institute of Mechanical Engineers, London, pp. 89-116, 1951.
3. Tinker, T., Shell-side characteristics of shell-and-tube heat exchangers-a simplified rating system for commercial heat exchangers, Trans. Am. Soc. Mech. Engrs., 80, 36-52, 1958.
4. Palen, J. W. and J. Taborek, Solution of shell side flow pressure drop and heat transfer by stream analysis method, Chem. Eng. Prog. Symp. Series, 65, No. 92, 53-63, 1969.
5. Wills, M. J. N. and D. Johnston, A New and Accurate Hand Calculation Method for Shell-side Pressure Drop and Flow Distribution, Proc. 22nd National Heat Transfer Conference, HTD Vol. 36, American Society of Mechanical Engineers, pp. 67-79, 1984.
6. Mukherjee, R., Effectively design shell-and-tube heat exchangers, Chem. Eng. Prog., 94, No. 2, 21-37, 1998.
7. Wills, M. J. N., A hand Calculation Method for Shellside Pressure Drop and Flow Distribution in a Shell-And-Tube Heat Exchanger, Report AERE-R11136, Atomic Energy Research Establishment, Harwell, U.K, 1984.
8. Hewitt, G. F., G. L. Shires and T. R. Bott, Process Heat Transfer, CRC Press, Boca Raton, FL, 1994.

## Notation

A Label for tube-to-baffle leakage stream
$a \quad$ Parameter in Equation (7.44)
$B$ Label for cross-flow stream; (central) baffle spacing
$B_{c} \quad$ Baffle cut
$B_{e} \quad$ End (inlet or outlet) baffle spacing
$B_{t} \quad$ Baffle thickness
$b \quad$ Parameter in Equation (7.44)
C Label for bundle-to-shell bypass stream
CF Label for combined (bundle-to-shell and pass partition) bypass stream
$D_{c t l} \quad$ Central tube limit diameter
$D_{e} \quad$ Equivalent diameter for bypass flow
$D_{i} \quad$ Internal diameter of tube
$D_{o}$ External diameter of tube
$D_{\text {otl }} \quad$ Outer tube limit diameter
$D_{s} \quad$ Internal diameter of shell
$D_{V} \quad\left(\Omega_{1} P_{T}^{2}-D_{o}^{2}\right) / D_{o}$
$E \quad$ Label for shell-to-baffle leakage stream
$F \quad$ Label for tube pass partition bypass stream; LMTD correction factor
$F_{c} \quad$ Fraction of tubes in cross flow between baffle tips
$F_{w} \quad$ Fraction of tubes in one baffle window
$f_{\text {ideal }}$ Ideal tube bank friction factor for cross flow
$f_{w} \quad$ Ideal tube bank friction factor for window flow
$G$ Mass flux
$G_{B} \quad$ Mass flux for cross flow
$G_{w} \quad$ Mass flux for window flow
$g_{c} \quad$ Unit conversion factor $=32.174 \frac{\mathrm{lbm} \cdot \mathrm{ft} / \mathrm{s}^{2}}{\mathrm{lbf}}=1.0 \frac{\mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}}{N}$
$h \quad$ Heat-transfer coefficient
$h_{i} \quad$ Tube-side heat-transfer coefficient
$h_{o} \quad$ Shell-side heat-transfer coefficient
$h_{x} \quad$ Heat-transfer coefficient for cross flow
$h_{w} \quad$ Heat-transfer coefficient for window flow
$K_{j} \quad$ Flow resistance coefficient for stream $j(j=A, B, C, C F, E, F)$
$L$ Tube length
$\dot{m} \quad$ Mass flow rate
$\dot{m}_{e} \quad 0.5\left(\dot{m}_{o}+\dot{m}_{w}\right)=$ Effective mass flow rate in end baffle spaces
$\dot{m}_{j} \quad$ Mass flow rate of stream $j(j=A, B, C, C F, E, F)$
$\dot{m}_{o} \quad$ Total mass flow rate of shell-side fluid
$N_{c} \quad$ Number of tube rows crossed between baffle tips
$N_{c w} \quad$ Effective number of tube rows crossed in one baffle window
$N_{p} \quad$ Number of tube pass partitions aligned in cross-flow direction
$N_{s s} \quad$ Number of pairs of sealing strips
$n_{b} \quad$ Number of baffles
$n_{p} \quad$ Number of tube-side passes
$n_{t} \quad$ Number of tubes in bundle
$P \quad$ Pressure
$P_{T} \quad$ Tube pitch
$R e \quad$ Reynolds number
$R e_{i} \quad$ Tube-side Reynolds number
$R e_{j} \quad$ Reynolds number for stream $j(j=A, B, C, E, F)$
$R e_{w} \quad$ Reynolds number for window flow
$R e_{\varepsilon w} \quad$ Effective Reynolds number for heat transfer in window flow
$R e_{\varepsilon x} \quad$ Effective Reynolds number for heat transfer in cross flow
$S_{B W} \quad$ Flow area defined by Equation (7.20)
$S_{b p} \quad$ Flow area for combined bypass stream
$S_{j} \quad$ Flow area for stream $j(j=A, B, C, C F, E, F)$
$S_{m} \quad$ Cross-flow area
$S_{s} \quad$ Approximate flow area for shell-to-baffle leakage stream, defined by Equation (7.19)
$S_{t} \quad$ Approximate flow area for tube-to-baffle leakage stream, defined by Equation (7.18)
$S_{w} \quad$ Window flow area
$T$ Temperature
$T_{a} \quad$ Inlet temperature of shell-side fluid
$T_{b} \quad$ Outlet temperature of shell-side fluid
$t_{a} \quad$ Inlet temperature of tube-side fluid
$U_{D} \quad$ Design overall heat-transfer coefficient
$V_{n} \quad$ Fluid velocity in nozzle

## Greek Letters

| $\alpha$ | Empirical correction factor for window pressure drop, Equation (7.8) |
| :--- | :--- |
| $\beta$ | Empirical correction factor for window pressure drop, Equation (7.8) |
| $\gamma$ | Empirical correction factor for shell-side heat-transfer coefficient, Equation (7.11) |
| $\Delta P_{e}$ | Pressure drop in end (inlet or outlet) baffle space |
| $\Delta P_{i}$ | Tube-side pressure drop |
| $\Delta P_{i n}$ | Pressure drop in inlet baffle space |
| $\Delta P_{j}$ | Pressure drop for stream $j(j=A, B, C, C F, E, F)$ |
| $\Delta P_{o}$ | Total shell-side pressure drop |
| $\Delta P_{o u t}$ | Pressure drop in outlet baffle space |
| $\Delta P_{w}$ | Pressure drop in one baffle window |
| $\Delta P_{x}$ | Pressure drop in one central baffle space |
| $\Delta P_{y}$ | $\Delta P_{x}+\Delta P_{w}=$ Pressure drop across one baffle space and one baffle window |
| $\left(\Delta T_{\text {lin }}\right)_{c f}$ | Logarithmic mean temperature difference for counter-current flow |
| $\Delta T_{m e a n}$ | Mean temperature difference in a heat exchanger |
| $\delta$ | Temperature profile distortion factor |
| $\delta_{p}$ | Tube-pass-partition clearance |
| $\delta_{s b}$ | Shell-to-baffle clearance |
| $\delta_{t b}$ | Tube-to-baffle clearance |
| $\varepsilon_{w j}$ | Effectiveness of stream $j(j=A, B, C, E, F)$ for heat transfer in baffle window |
| $\varepsilon_{x j}$ | Effectiveness of stream $j(j=A, B, C, E, F)$ for heat transfer in cross flow |
| $\theta_{o t l}$ | Angle defined by Equation (7.21) |
| $\mu$ | Viscosity |
| $\mu_{w}$ | Viscosity of fluid at average tube wall temperature |
| $\xi_{e}$ | Cross-flow resistance in end (inlet or outlet) baffle space |
| $\xi_{j}$ | Flow resistance for stream $j(j=A, B, C F, E)$ |
| $\xi_{o}$ | Flow resistance defined by Equation $(7.37)$ |
| $\xi_{w}$ | Flow resistance for baffle window |
| $\xi_{w_{e}}$ | Flow resistance in end (inlet or outlet) baffle window |
| $\xi_{x}$ | Flow resistance defined by Equation $(7.31)$ |
| $\xi_{y}$ | $\xi_{w}+\xi_{x}$ |
| $\rho$ | Fluid density |
| $\phi$ | Viscosity correction factor |
| $\psi$ | Correction factor for shell-side pressure drop, defined in Equation (7.60) |
| $\Omega_{1}$ | Parameter in correlation for cross-flow resistance, Equation (7.44) |
| $\Omega_{2}$ | Parameter in correlation for bypass flow resistance, Equation (7.46) |

## Problems

(7.1) The data given below pertain to the shell-side flow in a shell-and-tube heat exchanger. The tube bundle consists of $1-\mathrm{in}$. OD tubes laid out on $1.25-\mathrm{in}$. square pitch. The shell-side fluid has a flow rate of $1.38 \mathrm{~kg} / \mathrm{s}$ and a density of $1,200 \mathrm{~kg} / \mathrm{m}^{3}$.

| Stream | Flow Area $\left(\mathrm{m}^{2}\right)$ | Flow resistance $\left(\mathrm{kg}^{-1} \mathrm{~m}^{-1}\right)$ |
| :--- | :--- | :--- |
| Cross flow | 0.035096 | 3.1 |
| Bypass | 0.007400 | 23.6 |
| Tube-baffle leakage | 0.006893 | 12.0 |
| Shell-baffle leakage | 0.003942 | 48.0 |
| Window flow | 0.025500 | - |

Use the Wills-Johnston method to calculate the following:
(a) The flow fraction of the cross-flow stream.
(b) The pressure drop across one baffle compartment. (This does not include the baffle window.)
(c) The pressure drop in one baffle window.
(d) The pressure drop in one end (inlet or outlet) baffle space if $B / B_{e}=0.6$ and $\xi_{e}=0.90 \mathrm{~kg}^{-1} \mathrm{~m}^{-1}$.
(e) The nozzle-to-nozzle shell side pressure drop if the exchanger contains 20 baffles and the flow regime for all shell-side streams is fully turbulent.

Ans. (a) 0.40 . (b) 0.94 Pa . (c) 1.14 Pa . (d) 1.49 Pa . (e) 42.5 Pa .
(7.2) Rework Example 7.2 for the case in which one of the tube-pass partitions is aligned with the cross-flow direction, as in an H-banded tube layout. Assume that the pass partition clearance is equal to the tube OD.
(7.3) The data given below pertain to the shell-side flow in a shell-and-tube heat exchanger. The tube bundle consists of $3 / 4-\mathrm{in}$. OD tubes laid out on $1.0-\mathrm{in}$. square pitch. The flow rate of the shell-side fluid is $50,000 \mathrm{lb} / \mathrm{h}$ and its density is $55 \mathrm{lbm} / \mathrm{ft}^{3}$.

| Stream | Flow Area $\left(\mathrm{ft}^{2}\right)$ | Flow resistance $\left(\frac{\mathrm{lbf} \cdot \mathrm{s}^{2}}{\mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}}\right)$ |
| :--- | :--- | :---: |
| Cross flow | 0.180 | 0.30 |
| Bypass | 0.050 | 11.10 |
| Tube-baffle leakage | 0.055 | 4.20 |
| Shell-baffle leakage | 0.040 | - |
| Window flow | 0.275 |  |

Use the Wills-Johnston method to calculate the following:
(a) The flow fractions of the cross flow, leakage and bypass streams.
(b) The pressure drop across one baffle compartment.
(c) The pressure drop in one baffle window.
(d) The pressure drop in one end (inlet or outlet) baffle space if $B / B_{e}=0.5$ and $\xi_{e}=0.1 \frac{\mathrm{lbf} \cdot \mathrm{s}^{2}}{\mathrm{lbm}^{2} \cdot \mathrm{ft}^{2}}$.
(e) The nozzle-to-nozzle shell-side pressure drop if the exchanger contains 37 baffles and the flow regime for all shell-side streams is fully turbulent.

Ans. (a) cross flow $=0.587, \quad$ bypass $=0.096, \quad$ tube-baffle leakage $=0.164, \quad$ shell-baffle leakage $=0.153$. (b) $19.4 \mathrm{lbf} / \mathrm{ft}^{2}$. (c) $1.8 \mathrm{lbf} / \mathrm{ft}^{2}$. (d) $14.2 \mathrm{lbf} / \mathrm{ft}^{2}$. (e) 5.6 psi .
(7.4) Use the Wills-Johnston method to calculate the shell-side pressure drop for the heat exchanger of problems 5.3 and 6.4. Assume that all tube pass partitions are oriented normal to the cross-flow direction, so that $N_{p}=0$.
(7.5) Use the Wills-Johnston method to calculate the shell-side pressure drop for the heat exchanger of problem 6.6. Assume that all tube pass partitions are oriented normal to the cross-flow direction, so that $N_{p}=0$.
(7.6) Use the Wills-Johnston method to calculate the shell-side pressure drop for the modified configuration of the kerosene/oil exchanger considered previously in problems 5.1 and 6.8. Assume that all tube pass partitions are oriented normal to the cross-flow direction, so that $N_{p}=0$.
(7.7) Use the Wills-Johnston method to calculate the nozzle-to-nozzle shell-side pressure drop for the heat exchanger of problem 6.11. Assume that the tube pass partition is oriented normal to the cross-flow direction.
(7.8) Use the Xist module of the HTRI Xchanger Suite to design a heat exchanger with two tube passes for the kerosene/oil service of Example 5.1.
(7.9) Use the Xist module of the HTRI Xchanger Suite to design a heat exchanger for the service of problem 5.6 with:
(a) Plain tubes.
(b) Finned tubes.
(7.10) Design a heat exchanger for the service of problem 5.8 using:
(a) Xist.
(b) TASC.
(7.11) Design a heat exchanger for the service of problem 5.9 using:
(a) Xist.
(b) TASC.
(7.12) Use the Xist module of the HTRI Xchanger Suite to design a heat exchanger for the service of problem 5.11 with:
(a) Plain tubes.
(b) Finned tubes.
(7.13) Design a heat exchanger for the service of problem 5.13 using:
(a) Xist.
(b) TASC.
(7.14) Use the Xist module of the HTRI Xchanger Suite to design a heat exchanger for the service of problem 5.23 with:
(a) Plain tubes.
(b) Finned tubes.
(7.15) Solve problem 5.5 using:
(a) Xist.
(b) TASC.
(7.16) Use TASC to design a heat exchanger for the service of problem 5.6 with:
(a) Plain tubes.
(b) Finned tubes.
(7.17) Design a heat exchanger for the service of problem 5.10 using:
(a) Xist.
(b) TASC.
(7.18) Use TASC to design a heat exchanger for the service of problem 5.11 with:
(a) Plain tubes.
(b) Finned tubes.
(7.19) Design a heat exchanger for the service of problem 5.15 using:
(a) Xist.
(b) TASC.
(7.20) Use TASC to design a heat exchanger for the service of problem 5.23. The hydrocarbon properties at $180^{\circ} \mathrm{F}$ are as follows:

| Hydrocarbon property | Value at $180^{\circ} \mathrm{F}$ |
| :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.50 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.070 |
| $\mu(\mathrm{cp})$ | 1.56 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 51.5 |

(7.21) Design a heat exchanger for the service of problem 5.24 using:
(a) Xist.
(b) TASC.

Average stream properties are given in the table below.

| Property | Lube oil at $395^{\circ} \mathrm{F}$ | Gas oil at $340^{\circ} \mathrm{F}$ |
| :--- | :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.63 | 0.60 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.056 | 0.058 |
| $\mu(\mathrm{cp})$ | 2.75 | 0.63 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 47.5 | 46.3 |

(7.22) (a) Use Xist to rate the 17.25 -in. kerosene/oil heat exchanger designed in Example 7.6. Is the unit thermally acceptable? Is it hydraulically acceptable?
(b) Use Xist to rate the 19.25 -in. kerosene/oil exchanger designed in Example 7.6. What is the over-design for this unit according to Xist?
(7.23) (a) Consider again the kerosene/oil heat exchanger designed in Example 7.4. This unit has one pair of sealing strips. Use Xist to rate this design using the actual ribbon-banded tube layout with 0,2 , and 3 pairs of sealing strips. Based on these calculations, what is the optimal number of pairs of sealing strips for this exchanger?
(b) Repeat part (a) using TASC. Use a ribbon-banded tube layout with the tube count determined by TASC. Based on these calculations, what is the optimal number of sealing strips for this exchanger? Is this result consistent with the results obtained in part (a)?
(7.24) Consider again the 19.25-in. heat exchanger designed in Example 7.6. This unit has an H -banded tube layout with one pair of sealing strips. Use TASC to rate this design with 0 , 2 , and 3 pairs of sealing strips. Based on these calculations, what is the optimal number of pairs of sealing strips for this exchanger?
(7.25) For the final configuration of the kerosene/oil exchanger of Example 5.1, use Equation (2.38) to calculate the tube-side heat-transfer coefficient. Compare your result with the values computed by Xist and TASC in Examples 7.3 and 7.5, respectively.
(7.26) A shell-and-tube heat exchanger has an LMTD of $50^{\circ} \mathrm{F}$ and an LMTD correction factor of 0.9. When the exchanger is rated using Xist, the program output shows an effective mean temperature difference of $40.4^{\circ} \mathrm{F}$. What is the explanation for the apparent discrepancy in mean temperature difference?

## HEATEXCHANGER NETWORKS

Contents
8.1 Introduction ..... 328
8.2 An Example: TC3 ..... 328
8.3 Design Targets ..... 329
8.4 The Problem Table ..... 329
8.5 Composite Curves ..... 331
8.6 The Grand Composite Curve ..... 334
8.7 Significance of the Pinch ..... 335
8.8 Threshold Problems and Utility Pinches ..... 337
8.9 Feasibility Criteria at the Pinch ..... 337
8.10 Design Strategy ..... 339
8.11 Minimum-Utility Design for TC3 ..... 340
8.12 Network Simplification ..... 344
8.13 Number of Shells ..... 347
8.14 Targeting for Number of Shells ..... 348
8.15 Area Targets ..... 353
8.16 The Driving Force Plot ..... 356
8.17 Super Targeting ..... 358
8.18 Targeting by Linear Programming ..... 359
8.19 Computer Software ..... 361

### 8.1 Introduction

The transport of energy in chemical plants and petroleum refineries is accomplished by means of heat-exchanger networks (HENs). Hence, the design of such networks is an important aspect of chemical process design. Each individual heat exchanger in the network can be designed by the methods discussed in previous chapters. But before this can be done, the overall configuration of the HEN must be determined. Decisions must be made as to how the process streams will be paired for heat exchange and the extent of the heat exchange between each pair.

The Pinch Design method provides a systematic approach for configuring HENs based on fundamental thermodynamic principles and simple heuristic rules. This chapter provides an introduction to the Pinch Design method.

### 8.2 An Example: TC3

Test Case Number 3, or TC3 for short, is a simple HEN problem devised by Linnhoff and Hindmarsh [1] to illustrate the concepts involved in the Pinch Design method. The problem has four process streams as shown in Table 8.1. The nomenclature used in this table is as follows:

$$
\begin{aligned}
C P & \equiv \dot{m} C_{P}=\text { heat capacity flow rate } \\
T S & =\text { supply temperature } \\
T T & =\text { target temperature }
\end{aligned}
$$

In addition to the four process streams, there is a single hot utility available at a temperature above $150^{\circ} \mathrm{C}$ and a single cold utility available at a temperature below $20^{\circ} \mathrm{C}$. The minimum approach, $\Delta T_{\text {min }}$, for all heat exchangers is specified as $20^{\circ} \mathrm{C}$. This is the smallest allowable temperature difference between hot and cold streams (including utilities) at either end of a co-current or counter-current exchanger. For purposes of this example, all exchangers are assumed to operate counter-currently.

The problem is to design a HEN to bring each process stream from its supply temperature to its target temperature. A trivial solution is obtained by supplying all heating and cooling requirements from utilities. The resulting network consists of four units (two heaters and two coolers) and consumes a total of 487.5 kW of hot utility and 420 kW of cold utility. This represents the limiting case of zero heat recovery.

A non-trivial solution can be obtained with a little more effort, e.g., by pairing each hot stream with the cold stream that most closely matches its duty. The resulting network is shown on a grid diagram in Figure 8.1. It consists of two process exchangers, two heaters and one cooler. The total hot utility consumption is 182.5 kW , cold utility consumption is 115 kW , and the heat recovery amounts to 305 kW (the total rate of heat exchange between process streams). Notice that in this network the heat exchange between streams 2 and 3 is limited to 125 kW by the temperature difference at the hot end of the exchanger. A larger duty would result in a violation of $\Delta T_{\min }=20^{\circ} \mathrm{C}$.

Other solutions to TC3 are clearly possible. The optimal solution is the one that minimizes the total cost, i.e., the capital cost of the heat exchange equipment and the operating cost of the system, including the cost of the utilities consumed.

Table 8.1 Stream Data for TC3

| Stream | Type | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | Duty $(\mathrm{kW})$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | Hot | 150 | 60 | 2.0 | 180 |
| 2 | Hot | 90 | 60 | 8.0 | 240 |
| 3 | Cold | 20 | 125 | 2.5 | 262.5 |
| 4 | Cold | 25 | 100 | 3.0 | 225 |



Figure 8.1 A non-trivial solution for TC3.

### 8.3 Design Targets

Capital and operating costs are inconvenient to calculate, especially in the early stages of process design. Therefore, HEN design methods have traditionally used surrogates for these costs, namely, the number of units (process exchangers, heaters, and coolers) in the HEN and the amounts of hot and cold utilities consumed. Optimal networks are expected to have close to the minimum number of units because extra units require additional foundations, piping, fittings, and instrumentation that greatly increase the capital cost. Likewise, using more utilities than necessary increases the operating cost. Therefore, networks for which the number of units and the utility usage are both close to their respective minimum values should be close to optimal.

Design targets for minimum number of units and minimum-utility usage are easy to calculate and are independent of any specific network design. Hence, they can be computed at the outset and used as standards of comparison for all HEN designs that are subsequently developed. In a similar manner, the design targets can be used to assess the potential improvement that could be obtained by retrofitting an existing HEN.

The minimum number of units, $U_{\text {min }}$, for a given HEN problem can be estimated as follows [1]:

$$
\begin{equation*}
U_{\min }=N-1 \tag{8.1}
\end{equation*}
$$

where $N$ is the number of process streams and utilities. For example, in problem TC3 there are four process streams and two utilities, giving $N=6$ and $U_{\min }=5$. Notice that this is not the absolute minimum because the trivial solution with no heat recovery requires only four units. Equation (8.1) also does not account for the situation in which hot and cold stream duties exactly match, so that a single exchanger brings both streams to their target temperatures. These cases are of little practical interest, however, and with these exceptions, Equation (8.1) usually gives the correct result.

Minimum-utility requirements for a given HEN problem can be calculated in two ways, using the problem table algorithm of Linnhoff and Flower [2] or using composite curves. These methods are described in the following sections.

### 8.4 The Problem Table

In problem TC3, the total duty of the hot streams is 420 kW while that of the cold streams is 487.5 kW . Thus, if all the heat available from the hot streams were transferred to the cold streams, the hot utility would have to supply the remaining 67.5 kW of heating and no cold utility would be needed.

Thus, based on an energy balance (first law of thermodynamics), it appears that the minimum hot utility required for this problem is 67.5 kW and the minimum cold utility is zero. However, this result is incorrect because it ignores the constraint imposed by the second law of thermodynamics, i.e., heat exchange between hot and cold streams can occur only when the temperature of the hot stream exceeds that of the cold stream. In fact, since $\Delta T_{\min }=20^{\circ} \mathrm{C}$ for this problem, the temperature of the hot stream must exceed that of the cold stream by at least $20^{\circ} \mathrm{C}$. (It is shown in the following section that it is possible to utilize all the heat available in the hot streams of TC3 if $\Delta T_{\min }$ is reduced by a sufficient amount. This result does not hold in general, however.)

The problem table algorithm accounts for second law constraints and the effect of $\Delta T_{\text {min }}$ by dividing the temperature range into intervals, referred to as subnetworks (SNs), that are determined by the supply and target temperatures of each hot and cold stream. The heating and cooling requirements are then calculated for each SN, and any excess heat is transferred to the next lowest temperature interval. This procedure enforces the requirement that heat available at a given temperature level can be used only at lower levels. The problem table for TC3 is given below as Table 8.2.
The steps in constructing the problem table are as follows:
Step 1. Construct the temperature scales: Separate temperature scales differing by $\Delta T_{\min }=20^{\circ} \mathrm{C}$ are constructed for the hot and cold streams using the supply and target temperatures of the streams. For the cold streams, these temperatures are $20^{\circ} \mathrm{C}, 25^{\circ} \mathrm{C}, 100^{\circ} \mathrm{C}$, and $125^{\circ} \mathrm{C}$. To this list are added the values obtained by subtracting $\Delta T_{\text {min }}$ from each hot stream terminal temperature, giving $130^{\circ} \mathrm{C}, 70^{\circ} \mathrm{C}$, and $40^{\circ} \mathrm{C}$. The resulting seven temperatures are placed in ascending order on the cold stream temperature grid. Adding $\Delta T_{\text {min }}$ to each of the seven temperatures then gives the hot stream temperature scale.
Step 2. Add SNs and streams: Each interval on the temperature scales corresponds to a SN. Thus, there are six SNs for TC3. For each stream, arrows are drawn from the supply temperature level to the target temperature level to indicate which streams occur in each SN.
Step 3. Calculate deficits: The energy deficit in each SN is the difference between the energy required to heat the cold streams and the energy available from cooling the hot streams. It is calculated as follows:

$$
\begin{equation*}
\text { deficit }=\left[\sum_{i}(C P)_{c o l d, i}-\sum_{i}(C P)_{h o t, i}\right] \Delta T \tag{8.2}
\end{equation*}
$$

where $\Delta T$ is the magnitude of the temperature difference across the SN and the summations are over only those streams that exist in the SN. Thus, for SN1, only stream 1 occurs and Equation (8.2) becomes:

$$
\text { deficit }=-C P_{1} \Delta T=-2.0 \times 5=-10 \mathrm{~kW}
$$

Table 8.2 The Problem Table for TC3

| Subnetwork | Cold | ams | T ( ${ }^{\circ} \mathrm{C}$ ) |  | Hot streams |  | Deficit | Heat flow |  | Adj. heat flow |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (4) |  |  | (1) | (2) |  | In | Out | In | Out |
|  |  |  | 130 | 150 |  |  |  |  |  |  |  |
| SN1 |  |  | 125 | 145 | 1 |  | -10 | 0 | 10 | 107.5 | 117.5 |
| SN2 | $\uparrow$ |  | 100 | 120 | 1 |  | 12.5 | 10 | -2.5 | 117.5 | 105 |
| SN3 | , | 个 | 70 | 90 | I |  | 105 | -2.5 | -107.5 | 105 | 0 |
| SN4 | 1 | 1 | 40 | 60 | $\begin{aligned} & 1 \\ & \downarrow \end{aligned}$ | $\begin{aligned} & 1 \\ & \downarrow \\ & \hline \end{aligned}$ | -135 | -107.5 | 27.5 | 0 | 135 |
| SN5 | 1 | 」 | 25 | 45 |  |  | 82.5 | 27.5 | -55 | 135 | 52.5 |
| SN6 | 1 |  | 20 | 40 |  |  | 12.5 | -55 | -67.5 | 52.5 | 40 |

Note that a negative deficit represents a surplus of energy that can be used at lower temperature levels in the network. In SN2, streams 1 and 3 occur. Therefore,

$$
\text { deficit }=\left[C P_{3}-C P_{1}\right] \Delta T=[2.5-2.0] \times 25=12.5 \mathrm{~kW}
$$

The remaining deficits are similarly computed.
Step 4. Calculate heat flows: For each SN, the output is the input minus the deficit. The energy output is transferred to the next lower temperature level and becomes the input for the next SN. To start the calculation, the input to SN1 is assumed to be zero. Thus, for SN1 the output is 10 kW , which becomes the input for SN2. Subtracting the deficit of 12.5 kW for SN2 gives an output of -2.5 kW , and so on.
Step 5. Calculate adjusted heat flows: Negative heat flows must be eliminated by addition of heat from the hot utility. Since there is only one hot utility in the problem and it is available above $150^{\circ} \mathrm{C}$, the heat is added at the top of the energy cascade at SN1. The amount of energy that must be supplied corresponds to the largest negative heat flow, namely, 107.5 kW . Taking this value as the input to SN1, the remaining heat flows are computed as before to give the adjusted heat flows.

Now the minimum hot utility requirement for the network is the energy supplied as input to SN1, i.e., 107.5 kW . Likewise, the minimum cold utility requirement is the energy removed from SN6 at the bottom of the cascade, i.e., 40 kW .
The point of zero energy flow in the cascade is called the pinch. The problem table shows that the pinch occurs at a hot stream temperature of $90^{\circ} \mathrm{C}$ and a cold stream temperature of $70^{\circ} \mathrm{C}$. The significance of the pinch is discussed in subsequent sections.

### 8.5 Composite Curves

Composite curves are essentially temperature-enthalpy diagrams for the combined hot streams and combined cold streams, respectively. Their construction is illustrated by reference to problem TC3.
To construct the composite curve for the hot streams, we start at the lowest temperature level, $60^{\circ} \mathrm{C}$, and calculate the change in enthalpy (actually enthalpy per unit time) for each temperature subinterval determined from the hot stream terminal temperatures. The calculations are shown in Table 8.3.
Now the reference temperature for enthalpy is taken to be the lowest temperature level, $60^{\circ} \mathrm{C}$, for the hot streams, and the enthalpy at this temperature is set to zero. The $\Delta H$ values from Table 8.3 are then used to obtain the data points shown in Table 8.4. The points are plotted in Figure 8.2.
Exactly the same procedure is followed to construct the cold composite curve. The calculations are summarized in Table 8.5 and the data points to be plotted are given in Table 8.6. The cold composite curve is plotted in Figure 8.2 along with the hot composite curve.
It can be seen from Figure 8.2 that the point of closest approach between the hot and cold curves occurs at an enthalpy of 300 kW . The hot stream temperature at this point is $90^{\circ} \mathrm{C}$ and the cold stream temperature is between 70 and $80^{\circ} \mathrm{C}$. The exact cold stream temperature can be found from the equation for the line segment between $25^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$, which is easily determined using the

Table 8.3 Enthalpy Calculation for Hot Composite Curve of TC3

| Temperature $\left({ }^{\circ} \mathrm{C}\right)$ interval | $\Delta H(\mathrm{~kW})=\left(\sum C P_{\text {hot }, i}\right) \Delta T$ |
| :--- | :--- |
| $60-90$ | $(2+8) \times 30=300$ |
| $90-150$ | $2 \times 60=120$ |

Table 8.4 Data Points for Hot Composite
Curve of TC3

| $T\left({ }^{\circ} \mathrm{C}\right)$ | $H(\mathrm{~kW})$ |
| :---: | :---: |
| 60 | 0 |
| 90 | 300 |
| 150 | 420 |



Figure 8.2 Composite curves for TC3.

Table 8.5 Enthalpy Calculation for Cold Composite
Curve of TC3

| Temperature $\left({ }^{\circ} \mathrm{C}\right)$ interval | $\Delta H(\mathrm{~kW})=\left(\sum C P_{\text {cold }, i}\right) \Delta T$ |
| :--- | :--- |
| $20-25$ | $2.5 \times 5=12.5$ |
| $25-100$ | $(2.5+3) \times 75=412.5$ |
| $100-125$ | $2.5 \times 25=62.5$ |

Table 8.6 Data Points for Cold Composite Curve of TC3

| $T\left({ }^{\circ} \mathrm{C}\right)$ | $H(\mathrm{~kW})$ |
| :--- | :---: |
| 20 | 0 |
| 25 | 12.5 |
| 100 | 425 |
| 125 | 487.5 |



Figure 8.3 Shifted composite curves for TC3.
data points in Table 8.5:

$$
\begin{equation*}
T=22.727+0.18182 H \tag{8.3}
\end{equation*}
$$

Setting $H=300$ in this equation gives $T=77.273^{\circ} \mathrm{C}$. Thus, the minimum temperature difference between the hot and cold curves is:

$$
\Delta T_{\min }=90-77.273=12.727^{\circ} \mathrm{C}
$$

This is less than the minimum approach of $20^{\circ} \mathrm{C}$ for TC 3 . Since the reference point for enthalpy was set arbitrarily for each curve, either (or both) curve(s) can be shifted parallel to the $H$-axis. From Figure 8.2, it can be seen that shifting the cold curve to the right will increase $\Delta T_{\min }$. In order to determine the minimum heating and cooling requirements, the value of $\Delta T_{\text {min }}$ must be increased to $20^{\circ} \mathrm{C}$. This will occur when the cold curve is shifted so that its temperature at $H=300 \mathrm{~kW}$ is $70^{\circ} \mathrm{C}$. From Equation (8.3) we find that $H=260 \mathrm{~kW}$ when $T=70^{\circ} \mathrm{C}$. Therefore, a shift of 40 kW will bring the two curves into proper alignment, as shown in Figure 8.3.

The region where the hot and cold curves overlap represents (potential) heat exchange between hot and cold process streams. In Figure 8.3 this region extends from $H=40 \mathrm{~kW}$ to $H=420 \mathrm{~kW}$. The difference, 380 kW , represents the maximum possible heat exchange for the network (with $\Delta T_{\min }=20^{\circ} \mathrm{C}$ ). In the region from $H=0$ to $H=40 \mathrm{~kW}$, where only the hot curve exists, cold utility must be used to cool the hot streams. The duty of 40 kW represents the minimum cold utility requirement for the network. Similarly, in the region from $H=420 \mathrm{~kW}$ to $H=527.5 \mathrm{~kW}$, hot utility must be used. The duty of 107.5 kW represents the minimum hot utility requirement for the network. The point of closest approach between the hot and cold curves is the pinch. Thus, Figure 8.3 gives the hot and cold stream temperatures at the pinch, $90^{\circ} \mathrm{C}$ and $70^{\circ} \mathrm{C}$, respectively.

In Figure 8.2 it can be seen that the maximum possible amount of overlap between the hot and cold curves is attained, and as previously determined, $\Delta T_{\min }=12.727^{\circ} \mathrm{C}$. The maximum possible

| Table 8.7 <br> Curve of TC3 |  |
| :--- | :---: |
| $T\left({ }^{\circ} \mathrm{C}\right)$ | $H(\mathrm{~kW})$ |
| 140 | 107.5 |
| 135 | 117.5 |
| 110 | 105 |
| 80 | 0 |
| 50 | 135 |
| 35 | 52.5 |
| 30 | 40 |

heat recovery ( 420 kW ) occurs in this situation. Any further reduction in $\Delta T_{\min }$ does not increase the amount of heat that is recoverable. At the other extreme, by shifting the cold curve to the right by 420 kW , the point of zero overlap between the hot and cold curves is reached. Here there is no heat recovery and all heating and cooling is provided by utilities. The value of $\Delta T_{\min }$ at this point is $150^{\circ} \mathrm{C}-20^{\circ} \mathrm{C}=130^{\circ} \mathrm{C}$. Thus, the practical range for $\Delta T_{\text {min }}$ is $12.727-130^{\circ} \mathrm{C}$. For any value in this range, the maximum heat exchange and minimum-utility requirements can be determined from the composite curves.

As $\Delta T_{\text {min }}$ is decreased from its maximum value, the extent of heat recovery increases while the amount and cost of utility usage decreases. At the same time, the surface area required for process heat exchangers increases, due to greater total heat duty and smaller average driving force for heat transfer. Thus, for any HEN problem there is an optimal value of $\Delta T_{\min }$ that minimizes the total cost. The procedure for estimating this optimum is referred to as super targeting [3,4].

It should be noted that the method of composite curves is applicable to systems in which the stream enthalpies are nonlinear functions of temperature, including those involving condensation and boiling. Although the calculations are more complicated in these cases, there is no fundamental problem in applying the method. The problem table algorithm presented in the previous section can also be applied in these cases by using piecewise linear functions to approximate the nonlinear temperature-enthalpy relationships.

### 8.6 The Grand Composite Curve

The grand composite curve is a plot of adjusted heat flow versus the average of the hot and cold stream temperatures. The points to be plotted are obtained directly from the problem table, and for TC3 are listed in Table 8.7. The data are plotted in Figure 8.4.

The grand composite curve embodies the same basic information as the problem table. The intercept at $80^{\circ} \mathrm{C}$ on the temperature axis represents the pinch. The two end points of the curve give the minimum hot and cold utility requirements. The various line segments that constitute the graph display the magnitudes of heat sources and sinks and the temperature intervals over which they occur. Net heat is produced by the system over temperature intervals where the line segments slope downward and to the right. Conversely, net heat is consumed over intervals where the line segments slope downward and to the left.

When utilities are available at different temperature levels, as is normally the case in chemical and petroleum processing, these levels are indicated on the diagram to show their positions relative to heat sources and sinks in the process. The grand composite curve thus serves as an aid in properly matching utilities with process requirements. Another use is in process integration work, where it is used to determine the appropriate placement of unit operations within the overall network for effective energy utilization. Unit operations involving heat pumps, heat engines, distillation columns, evaporators, furnaces, etc. that can be represented in terms of heat sources and sinks, can be analyzed in this manner [3,4].


Figure 8.4 Grand composite curve for TC3.

As an example, suppose there is a second hot utility in TC3 that is available at a temperature of $110^{\circ} \mathrm{C}$. For simplicity, we will assume that the temperature change for this utility is negligible, so that it can be used to supply heat to cold streams at temperatures of $90^{\circ} \mathrm{C}$ or less. This temperature corresponds to $100^{\circ} \mathrm{C}$ on the graph because the temperatures used for the grand composite curve are averages of hot and cold stream temperatures. Using the procedure shown in Figure 8.5, it is found that 70 kW of hot utility could be supplied by the second utility (HU2), leaving 37.5 kW to be supplied by the hotter (and presumably more expensive) utility (HU1). The remaining cold stream duty of 10 kW above the pinch is supplied by heat exchange with the hot streams. This heat exchange is represented by the uppermost triangle in Figure 8.5.

### 8.7 Significance of the Pinch

The pinch is the point of closest approach between the hot and cold composite curves. It is also the point of zero energy flow in a network with minimum-utility usage. The latter representation has some important consequences for HEN design.

Referring to the problem table for TC3 (Table 8.2), suppose we transfer some energy across the pinch, say 10 kW . To do this, we simply increase all the adjusted heat flows in the last two columns of the table by 10 kW . The hot utility requirement is now 117.5 kW and the cold utility requirement is 50 kW . Thus, we see that transferring energy across the pinch increases both hot and cold utility requirements. It therefore tends to be inefficient and expensive, and should generally be avoided to the extent that is practical.

One way to transfer energy across the pinch is to put a heater below the pinch. In such a unit heat is transferred directly from the hot utility, which is hotter than the pinch temperature, to a cold stream that is colder than the pinch temperature. Thus, the heat flows from the hot utility temperature, across the pinch to the cold stream temperature. Similarly, placing a cooler above the pinch results in heat flow directly from the hot stream temperature above the pinch to the cold


Figure 8.5 Using the grand composite curve to determine utility requirements when two hot utilities are available.

Table 8.8 The Hot End Problem for TC3

| Stream | Type | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | Duty $(\mathrm{kW})$ |
| :--- | :--- | :--- | :---: | :--- | :--- |
| 1 | Hot | 150 | 90 | 2.0 | 120 |
| 3 | Cold | 70 | 125 | 2.5 | 137.5 |
| 4 | Cold | 70 | 100 | 3.0 | 90 |

Table 8.9 The Cold End Problem for TC3

| Stream | Type | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | Duty $(\mathrm{kW})$ |
| :--- | :--- | :--- | :--- | :--- | :---: |
| 1 | Hot | 90 | 60 | 2.0 | 60 |
| 2 | Hot | 90 | 60 | 8.0 | 240 |
| 3 | Cold | 20 | 70 | 2.5 | 125 |
| 4 | Cold | 25 | 70 | 3.0 | 135 |

utility temperature below the pinch. It follows that heaters should be used only above the pinch, while coolers should be used only below the pinch.

Since any energy transfer across the pinch increases utility requirements, it is clear that for a minimum-utility design, there can be no energy flow across the pinch. This allows the HEN design problem to be decomposed into two separate problems, the hot end problem above the pinch and the cold end problem below the pinch. The two problems can be solved separately and then combined to obtain a solution for the entire network. The hot and cold end problems for TC3 are summarized in Tables 8.8 and 8.9, respectively. Note that stream 2 does not appear in the hot end problem because

Table 8.10 The Problem Table for TC3 with $\Delta T_{\min }=10^{\circ} \mathrm{C}$.

| Subnetwork |  |  | T ( ${ }^{\circ} \mathrm{C}$ ) |  | Hot streams |  | Deficit | Heat flow |  | Adj. heat flow |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (3) | (4) |  |  | (1) | (2) |  | In | Out | In | Out |
|  |  |  | 140 | 150 |  |  |  |  |  |  |  |
| SN1 |  |  | 125 | 135 | 1 |  | -30 | 0 | 30 | 67.5 | 97.5 |
| SN2 | $\uparrow$ |  | 100 | 110 | 1 |  | 12.5 | 30 | 17.5 | 97.5 | 85 |
| SN3 | 1 | $\uparrow$ | 80 | 90 | 1 |  | 70 | 17.5 | -52.5 | 85 | 15 |
| SN4 | 1 | 1 | 50 | 60 | $\begin{aligned} & 1 \\ & \downarrow \end{aligned}$ | $\begin{aligned} & 1 \\ & \downarrow \\ & \hline \end{aligned}$ | -135 | -52.5 | 82.5 | 15 | 150 |
| SN5 | 1 | 1 | 25 | 35 |  |  | 137.5 | 82.5 | -55 | 150 | 12.5 |
| SN6 | 1 |  | 20 | 30 |  |  | 12.5 | -55 | -67.5 | 12.5 | 0 |

its temperature range, from $90^{\circ} \mathrm{C}$ to $60^{\circ} \mathrm{C}$, falls below the pinch temperature of $90^{\circ} \mathrm{C}$ for the hot streams.

### 8.8 Threshold Problems and Utility Pinches

Virtually all industrial HEN problems contain a pinch. However, it is possible to construct problems that do not exhibit a pinch. This can be done by setting $\Delta T_{\text {min }}$ below the value at which the maximum possible amount of heat recovery is attained. For TC3, this value is approximately $12.727^{\circ} \mathrm{C}$, as previously shown. The problem table for TC 3 with $\Delta T_{\min }$ set at $10^{\circ} \mathrm{C}$ is given as Table 8.10. Although the composite curves still exhibit a point of closest approach, at $90^{\circ} \mathrm{C}$ on the hot side and $80^{\circ} \mathrm{C}$ on the cold side in this case, the energy flow is not equal to zero at this point. The energy flow becomes zero at the very bottom of the energy cascade, indicating that no cold utility is required. In effect, the entire HEN problem consists of a hot end problem; there is no cold end problem.

As long as $\Delta T_{\min }$ for TC 3 is less than $12.727^{\circ} \mathrm{C}$, it places no restriction on the amount of heat that can be transferred between the hot and cold streams. Only when this threshold value is exceeded does the heat transfer become restricted. For this reason, problems for which $\Delta T_{\text {min }}$ is below the threshold value are referred to as threshold problems [1]. For a pinch to occur, it is necessary to have $\Delta T_{\text {min }} \geq \Delta T_{\text {threshold }}$.

It is also possible for HEN problems to contain more than a single pinch. This situation occurs when utilities are available at different temperature levels; e.g., high-, intermediate-, and low-pressure steam. Since there is usually an excess of low-pressure steam in chemical plants and petroleum refineries, it is economical to utilize this utility whenever possible. Higher-pressure steam is normally used only when the required steam temperature exceeds that of the lower pressure steam. This situation can result in additional pinches at the temperature levels of the available utilities, thereby allowing further decomposition of the HEN problem. For obvious reasons, these additional pinches are referred to as utility pinches.

### 8.9 Feasibility Criteria at the Pinch

The pinch represents the most temperature-constrained region of a HEN, and as such, it is the most critical region for HEN design. Due to the low driving force, exchangers operating near the pinch tend to be relatively large and expensive units. Identification of appropriate stream matches for exchangers operating at the pinch is a key aspect of the Pinch Design method. Exchangers that operate at the pinch have a temperature difference equal to $\Delta T_{\min }$ on at least one end. Three feasibility criteria applied to the stream data at the pinch are used in determining appropriate matches. These criteria are discussed in the following subsections.


Figure 8.6 A pinch match that violates the CP inequality for the cold end of TC3.

### 8.9.1 Number of process streams and branches

For a minimum-utility design, coolers are not permitted above the pinch. Therefore, in the hot end problem, each hot stream that intersects the pinch must be brought to the pinch temperature by heat exchange with a cold process stream. For this to occur, the following inequality must be satisfied in the hot end problem:

$$
\begin{equation*}
N H \leq N C \quad \text { (hot end) } \tag{8.4}
\end{equation*}
$$

where
$N H=$ number of hot streams or branches at the pinch
$N C=$ number of cold streams or branches at the pinch
A similar argument shows that for the cold end problem, the inequality is reversed:

$$
\begin{equation*}
N H \geq N C \quad(\text { cold end }) \tag{8.5}
\end{equation*}
$$

Stream splitting, i.e., dividing a stream into two or more branches, may be required in order to satisfy these inequalities.

### 8.9.2 The $C P$ inequality

For an exchanger operating at the pinch, $\Delta T=\Delta T_{\min }$ at the pinch end of the exchanger. Therefore, the temperature difference between the two streams cannot decrease from the pinch end to the other end of the exchanger. This requirement leads to the following inequalities that must be satisfied for every stream match at the pinch:

$$
\begin{align*}
& C P H \leq C P C \quad(\text { hot end })  \tag{8.6}\\
& C P H \geq C P C \quad \text { (cold end) } \tag{8.7}
\end{align*}
$$

where $C P H$ and $C P C$ are the heat capacity flow rates of the hot and cold streams, respectively. Violation of these inequalities will result in $\Delta T<\Delta T_{\min }$ in the heat exchanger. Figure 8.6 shows a pinch match between streams 1 and 4 in the cold end problem for TC3. Note that inequality (8.7) is violated and as a result, the driving force in the exchanger decreases from $\Delta T_{\min }=20^{\circ} \mathrm{C}$ at the pinch end to $10^{\circ} \mathrm{C}$ at the opposite end.

Note that the $C P$ inequalities hold only for exchangers operating at the pinch. Away from the pinch, temperature differences between hot and cold streams may be large enough to permit matches that violate these inequalities.

### 8.9.3 The CP difference

For an individual exchanger operating at the pinch, the $C P$ difference is defined as follows:

$$
\begin{align*}
C P \text { difference } & =C P C-C P H \quad \text { (hot end) }  \tag{8.8}\\
& =C P H-C P C \quad \text { (cold end) }
\end{align*}
$$

Table 8.11 The CP Table for the Hot End Problem of TC3

| $C P H \leq C P C$ |  | $N H \leq N C$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Stream number | Hot | Cold | Stream number |  |
| 1 | 2.0 | 3.0 | 4 |  |
|  |  | 2.5 | 3 |  |
| Total | 2.0 | 5.5 |  |  |

Note that the $C P$ difference must be non-negative according to the $C P$ inequality criterion.
The overall $C P$ difference is defined as follows:

$$
\begin{array}{rlr}
\text { overall } C P \text { difference } & =\sum C P C-\sum C P H & \text { (hot end) }  \tag{8.9}\\
& =\sum C P H-\sum C P C & (\text { cold end })
\end{array}
$$

The summations in Equation (8.9) are taken over only those streams that intersect the pinch.
The third feasibility condition states that the $C P$ difference for any exchanger operating at the pinch must not exceed the overall $C P$ difference. The reason is that if one exchanger has a $C P$ difference greater than the total, then another must have a negative $C P$ difference that violates the $C P$ inequality.

### 8.9.4 The CP table

The $C P$ table is a convenient means of identifying feasible pinch matches. The $C P$ table for the hot end problem of TC3 is given as Table 8.11. The $C P$ values for the hot and cold streams are listed separately in descending order, and the sums of these values are entered below each column. As a reminder, the feasibility criteria are given at the top of the table. Note that only those streams that intersect the pinch are included in the $C P$ table.
It can be seen by inspection that the number of hot streams is less than the number of cold streams, and that the $C P$ inequality is satisfied for each of the possible matches. In addition, the overall $C P$ difference is immediately obtained from the $C P$ totals as 3.5 . Now the individual $C P$ differences for the two possible matches are as follows:

> stream 1 and stream 4: $C P$ difference $=3-2=1$
> stream 1 and stream 3: $C P$ difference $=2.5-2=0.5$

Since both of these values are less than the overall $C P$ difference, both satisfy all of the feasibility criteria.

### 8.10 Design Strategy

The pinch method attempts to develop HENs that meet the design targets, i.e., that have the minimum number of units and that consume the minimum amounts of utilities. Toward this end, the problem is decomposed at the pinch (es) into two or more subproblems that are solved independently. In each subproblem (e.g., the hot end and cold end problems), the design is begun at the pinch where the restrictions on stream matches are greatest. The feasibility criteria at the pinch are used to identify appropriate matches and the need for stream splitting.

When an appropriate stream match has been identified, the next step is to determine the duty that should be assigned to the corresponding exchanger. A simple rule called the tick-off heuristic [1] can be used for this purpose. It can be stated as follows:

Tick-off heuristic: In order to minimize the number of units, each exchanger should bring one stream to its target temperature (or exhaust a utility).

For process exchangers operating at the pinch, the duty can be taken as the lower of the two stream duties since the $C P$ inequality will ensure an adequate driving force in the unit.

The tick-off heuristic can sometimes result in excess utility usage that is incompatible with a minimum-utility design. This situation occurs when excessive temperature driving force is utilized in pinch exchangers, leaving too little driving force available for exchangers elsewhere in the network. In these cases, the duty on the offending exchanger(s) can be reduced (which may lead to more than the minimum number of units) or a different set of pinch matches can be tried [1]. Methods for analyzing these situations are given by Linnhoff and Ahmad [5,6] and in Section 8.16.

Once the pinch matches have been made, the remaining problem can be solved with much greater flexibility. The feasibility criteria that apply at the pinch need not be satisfied away from the pinch, leaving other factors, such as process constraints, plant layout, controllability, and engineering judgment, as paramount in determining stream matches. (Safety is an overriding consideration in all stream matches, including those at the pinch.)
A complete network design is obtained by joining the subproblem solutions at the pinches. The resulting network is usually too complex to be practical, however. Therefore, further analysis is required to simplify the network. Some energy flow across the pinch is generally necessary in order to obtain a practical network design.

The basic pinch design strategy is applied to obtain a minimum-utility design for TC3 in the following section. Network simplification is considered in subsequent sections.

### 8.11 Minimum-Utility Design for TC3

### 8.11.1 Hot end design

The hot end problem for TC3 is summarized in Table 8.8. Before starting the design, consider the design targets for this problem. Since stream 2 does not appear in the hot end, there are only three process streams. Also, there is only one utility (hot) because no cooling is permitted in the hot end. Therefore, according to Equation (8.1), the minimum number of units is:

$$
U_{\min }=(3+1)-1=3
$$

All the heating for the entire network must be done in the hot end because no heaters are allowed in the cold end. Therefore, the minimum hot utility requirement for the hot end is 107.5 kW , the minimum for the entire network. The minimum cold utility requirement is obviously zero, since no coolers are allowed in the hot end.

The $C P$ table for the hot end problem is given as Table 8.11. As previously shown, there are two feasible pinch matches, stream 1 with stream 3 , and stream 1 with stream 4 . We consider each of these in turn.

## Case A: Match stream 1 with stream 3

From Table 8.8, the stream duties are 120 kW for stream 1 and 137.5 kW for stream 3 . The lower value, 120 kW , is the duty assigned to the exchanger, bringing stream 1 to its target temperature. The remaining duty on stream 3 is 17.5 kW , which must be supplied by a heater since no hot streams remain to exchange heat with the cold streams. Likewise, a heater must be used to supply the entire duty of 90 kW for stream 4. The resulting network is shown in Figure 8.7. Note that there are three units (a process exchanger and two heaters), the total hot utility consumption is 107.5 kW , and no


Figure 8.7 Hot end design for TC3: Case A.


Figure 8.8 Hot end design for TC3: Case B.
cold utility is used. Comparing these values with the design targets for the hot end problem, it is seen that this is a minimum-utility, minimum-number-of-units design.

## Case B: Match stream 1 with stream 4

The stream duties in this case are 120 kW for stream 1 and 90 kW for stream 4. Assigning the lower value of 90 kW to the exchanger brings stream 4 to its target temperature, while leaving a residual duty of 30 kW for stream 1 . This residual duty can be handled with a second exchanger matching stream 1 with stream 3 . The remaining duty of 107.5 kW for stream 3 must be supplied by a heater. The network is shown in Figure 8.8. Note that it, too, is a minimum-utility, minimum-number-of-units design.

### 8.11.2 Cold end design

The cold end problem for TC3 is summarized in Table 8.9. Considering first the design targets for this problem, there are four process streams and one (cold) utility. Therefore, Equation (8.1) gives:

$$
U_{\min }=(4+1)-1=4
$$

Table 8.12 The CP Table for the Cold End Problem of TC3

| $C P H \geq C P C$ |  |  |  |
| :---: | ---: | :---: | :---: |
| Stream number | Hot | Cold | Stream number |
| 2 | 8.0 | 3.0 | 4 |
| 1 | 2.0 | 2.5 | 3 |
| Total | 10.0 | 5.5 |  |

The minimum hot utility requirement is zero (no heaters allowed in cold end) and the minimum cold utility requirement is equal to the minimum for the entire network, namely, 40 kW .

The $C P$ table for the cold end problem is given as Table 8.12. It is seen that hot stream 1 cannot be matched with either cold stream due to violation of the $C P$ inequality. Hot stream 2 can be matched with either cold stream without violating the $C P$ inequality, but the $C P$ differences are 5 and 5.5 , respectively, for these matches, while the overall $C P$ difference is 4.5 . Therefore, neither of these matches is feasible.

Since there are no feasible pinch matches, stream splitting is required. For instance, one of the cold streams can be split to allow a match with stream 1 . However, this will result in $N C>N H$, thereby requiring a hot stream split as well. Alternatively, stream 2 can be split to allow a match with either cold stream. For example, an equal split giving $C P=4$ in each branch permits matches with both cold streams. The exact split ratio need not be specified at this point; it will be determined when duties and stream temperatures are specified for the matches. In order to minimize the number of stream splits and the associated complexity of the HEN, it is clearly preferable to split stream 2 rather than one of the cold streams.

From Table 8.9, the cold end duties are 240 kW for stream $2,135 \mathrm{~kW}$ for stream 4 and 125 kW for stream 3. Therefore, in matching the two branches of stream 2 with the cold streams, one cold stream can be brought to its target temperature along with stream 2 . There are two cases, depending on which cold stream is "ticked-off."

## Case A: Tick-off stream 3

The match between streams 2 and 3 is assigned a duty of 125 kW to satisfy the duty on stream 3 . The remaining duty on stream 2 is 115 kW , which is less than the duty for stream 4 . Therefore, the match between streams 2 and 4 is assigned a duty of 115 kW , leaving a duty of 20 kW on stream 4 . A match is now possible between streams 1 and 4 . Since the exchanger will not be operating at the pinch, the feasibility criteria are not applicable to this unit. The duty for stream 1 is 60 kW , so the lower value of 20 kW is assigned, bringing stream 4 to its target temperature and leaving a duty of $40-\mathrm{kW}$ on stream 1 . Since both cold streams have now been ticked-off, a $40-\mathrm{kW}$ cooler must be used to satisfy the remaining duty on stream 1. The resulting network is shown in Figure 8.9. Comparison with the cold end design targets shows that it is a minimum-utility, minimum-number-of-units design. If the outlet temperature of stream 2 from each exchanger is set at $60^{\circ} \mathrm{C}$ as in Figure 8.9, then the $C P$ values are $3.83 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$ for the branch matched with stream 4 and $4.17 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$ for the branch matched with stream 3.

## Case B: Tick-off stream 4

In this case, the match between streams 2 and 4 is assigned a duty of 135 kW to satisfy the duty on stream 4. The remaining duty on stream 2 is 105 kW , which is less than the duty of 125 kW on stream 3. Therefore, the match between streams 2 and 3 is assigned a duty of 105 kW , thereby ticking off stream 2 and leaving a duty of 20 kW on stream 3 . A 20 kW match between streams 1 and 3 brings stream 3 to its target temperature, and a $40-\mathrm{kW}$ cooler on stream 1 completes the design.


Figure 8.9 Cold end design for TC3: Case A.


Figure 8.10 Cold end design for TC3: Case B.

The resulting network is shown in Figure 8.10. Note that it, too, is a minimum-utility, minimum-number-of-units design. With the outlet temperature of stream 2 set at $60^{\circ} \mathrm{C}$ for each exchanger, the $C P$ values are $4.5 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$ for the branch matched with stream 4 and $3.5 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$ for the branch matched with stream 3 .

### 8.11.3 Complete network design

To obtain a complete network design, a hot end design and a cold end design are spliced together at the pinch. Each hot end design can be combined with either cold end design, leading to four possible


Figure 8.11 Network obtained by combining the hot $A$ and cold $B$ cases for TC3.
networks for TC3. Figure 8.11 shows the network obtained by combining the hot A and cold B cases. It contains seven units and uses the minimum amounts of hot and cold utilities. Recall that the target for minimum number of units in the entire network was previously determined to be five. We now see that the actual minimum number of units consistent with minimum-utility usage is seven. The difference is due to the presence of the pinch. Equation (8.1) must be applied separately on either side of the pinch and the results summed to obtain a value consistent with a minimum-utility design.

The effect of the pinch on the number of units can be clearly seen in Figure 8.11. An unusual feature of this HEN is that streams 1 and 3 are matched twice, with one exchanger operating above the pinch and one below the pinch. One of these units can obviously be eliminated, but doing so will result in energy flow across the pinch and increased utility usage.

### 8.12 Network Simplification

The basic pinch design strategy illustrated in the previous section generally results in networks that are too complex, i.e., have too many units, to be considered practical. The two exchangers involving streams 1 and 3 in Figure 8.11 are an example of this complexity. Therefore, further analysis is required to simplify the design. An obvious way to simplify the HEN of Figure 8.11, for example, is to simply remove the small $20-\mathrm{kW}$ exchanger operating between streams 1 and 3 . To satisfy the stream duties, the duty on the stream 1 cooler can be increased to 60 kW and the duty on the stream 3 heater can be increased to 37.5 kW . However, the simplification can be done in a more energy-efficient manner by using the concepts of heat load loop and heat load path.

### 8.12.1 Heat load loops

A heat load loop is a loop in the HEN around which duties can be shifted from one exchanger to another without affecting stream duties. Changing the duty on an exchanger may result in a violation of $\Delta T_{\text {min }}$, however. The number of heat load loops is the difference between the actual number of units in the network and the minimum number of units calculated by applying Equation (8.1) to the network as a whole, i.e., ignoring the pinch. For the HEN of Figure 8.11, there are seven units compared with the minimum number of five. Hence, there are two loops as shown in Figures 8.12 and 8.13. The loop shown in Figure 8.12 is obvious and is formed by the two exchangers operating


Figure 8.12 HEN for TC3 showing the heat load loop formed by the $20-\mathrm{kW}$ and $120-\mathrm{kW}$ exchangers.


Figure 8.13 HEN for TC3 showing the second heat load loop.
between streams 1 and 3. The loop shown in Figure 8.13 is less obvious, passing through the heaters on streams 3 and 4, which are not physically connected. Notice that both loops cross the pinch.

Now we can use the heat load loop in Figure 8.12 to simplify the network by eliminating the 20 kW exchanger. To do this, simply shift the 20 kW duty around the loop to the $120-\mathrm{kW}$ exchanger, bringing its duty to 140 kW . The resulting network is shown in Figure 8.14. Notice that the temperature difference on the cold end of the $140-\mathrm{kW}$ exchanger is now $18^{\circ} \mathrm{C}$, a violation of $\Delta T_{\text {min }}$. However,


Figure 8.14 Modified HEN for TC3 after using heat load loop to eliminate the 20-kW exchanger.
the utility consumption has not increased. Thus, by using the heat load loop to transfer the 20 kW across the pinch, a violation of $\Delta T_{\text {min }}$ has been incurred rather than increased utility usage.

In a similar manner, the loop shown in Figure 8.12 can be used to further simplify the network by eliminating the small $17.5-\mathrm{kW}$ heater on stream 3 . The reader can verify that this results in a temperature difference of $11^{\circ} \mathrm{C}$ on the cold side of the $140-\mathrm{kW}$ exchanger. This is a large violation of $\Delta T_{\min }$, and although it might nevertheless be acceptable in practice, it will not be considered further here. Instead, the $17.5-\mathrm{kW}$ heater on stream 3 will be used to illustrate the concept of a heat load path.

### 8.12.2 Heat load paths

A heat load path is a continuous connection in the network between a heater, one or more heat exchangers, and a cooler. Heat load can be shifted along a path by alternately adding and subtracting a duty from each successive unit. This procedure will not affect stream duties, but intermediate stream temperatures will change due to the change in exchanger duties. Therefore, a heat load path can be used to eliminate a $\Delta T_{\min }$ violation incurred during network simplification.

Consider again the $140-\mathrm{kW}$ exchanger in Figure 8.14. Although the $18^{\circ} \mathrm{C}$ driving force on the cold end would normally be considered entirely adequate in practice, suppose for the sake of argument that it is desired to restore this value to $20^{\circ} \mathrm{C}$. This can be done by increasing the exit temperature of stream 1 from $80^{\circ} \mathrm{C}$ to $82^{\circ} \mathrm{C}$. Since the $C P$ of stream 1 is $2 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$, the exchanger duty must be reduced by 4 kW . The exchanger forms part of a heat load path from the heater on stream 3 to the cooler on stream 1. Therefore, the desired result can be obtained by adding 4 kW to the heater duty, subtracting the same amount from the exchanger (bringing its duty to 136 kW ), and adding 4 kW to the cooler. The resulting network is shown in Figure 8.15.

The net result of the above modifications is that the $20-\mathrm{kW}$ exchanger has been eliminated from the network without violating the $\Delta T_{\min }$ on any remaining exchanger, and the hot and cold utility consumption have each increased by only 4 kW . By comparison, simply removing the $20-\mathrm{kW}$ exchanger increases both utility loads by 20 kW . Furthermore, the network of Figure 8.15 compares favorably with the original design targets: 6 units versus $5,111.5 \mathrm{~kW}$ hot utility versus 107.5 kW , and 44 kW cold utility versus 40 kW .


Figure 8.15 HEN for TC3 after using heat load path to restore $\Delta T_{\min }$ to $20^{\circ} \mathrm{C}$.
Table 8.13 Shells Required for the HEN of Figure 8.15

| Exchanger <br> $(\mathrm{kW})$ | Temperature <br> cross $\left({ }^{\circ} \mathrm{C}\right)$ | LMTD correction <br> factor for 1-2 exchanger | Shells required |
| :--- | :--- | :--- | :--- |
| 105 | 2 | 0.77 | $1-2$ |
| 135 | 10 | $<0.5$ | 2 |
| 136 | 34.4 | $<0.5$ | 3 |

### 8.13 Number of Shells

Up to this point we have assumed that all exchangers in the network operate counter-currently. Most exchangers in the chemical process industries, however, are multi-pass shell-and-tube exchangers. Although the network of Figure 8.15 is valid regardless of the type of exchangers employed, two of the three process exchangers have large temperature crosses. A temperature cross exists in an exchanger whenever the cold fluid outlet temperature exceeds the hot fluid outlet temperature, and the magnitude of the cross is the difference between these two temperatures. Due to the limitation imposed by the parallel pass in a 1-2 exchanger, only a small temperature cross can be supported. As the magnitude of the cross increases, the logarithmic mean temperature difference (LMTD) correction factor rapidly decreases, indicating the need for multiple shell passes. The most common way of achieving multiple shell passes is by connecting E shells in series, making these units relatively expensive compared with 1-2 or counter-flow exchangers that comprise a single shell.

Table 8.13 gives the number of shells required for each of the process exchangers in the HEN of Figure 8.15 in order to achieve a satisfactory LMTD correction factor. Although $F<0.8$ for the $105-\mathrm{kW}$ exchanger with one shell pass, the operating point is not on the steeply sloping portion of the $F$-curve, so a single shell pass could in fact be used. Alternatively, the small temperature cross on this exchanger can be eliminated by increasing the $C P$ value of the stream 2 branch allocated to this unit to $3.75 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$. The outlet temperature of stream 2 is then $62^{\circ} \mathrm{C}$ and the LMTD correction factor is 0.80 for one shell pass, which is definitely acceptable. The $C P$ value for the stream 2 branch allocated to the $135-\mathrm{kW}$ exchanger becomes $4.25 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$, resulting in an outlet temperature of $58.2^{\circ} \mathrm{C}$, and a temperature cross of $11.8^{\circ} \mathrm{C}$. Two shell passes are still adequate for this unit. Therefore, assuming


Figure 8.16 HEN for TC3 after modification to eliminate temperature crosses on two exchangers.
that each of the utility exchangers in the HEN requires a single shell pass, a total of nine shells is required if the exchangers are multi-tube-pass shell-and-tube units. Although this appears to be a rather complicated solution to a very simple problem, large temperature crosses are the inevitable result of attempting to maximize heat exchange using a minimal number of exchangers.

The HEN of Figure 8.15 can be simplified by eliminating the temperature cross on the $136-\mathrm{kW}$ exchanger. This is accomplished by shifting 38 kW of duty along the heat load path used previously. The resulting HEN, shown in Figure 8.16, has only seven shells, but uses 149.5 kW of hot utility and 82 kW of cold utility. It is not close to a minimum-utility design, but the trade-off of added utility consumption for capital cost reduction might be economically justifiable.

### 8.14 Targeting for Number of Shells

The composite curves can be used to estimate the minimum number of shells required for a HEN composed of shell-and-tube exchangers. Two methods are considered here, a very simple graphical procedure and a somewhat more accurate, albeit more computationally intensive, analytical procedure.

### 8.14.1 Graphical method

In this method the hot and cold composite curves are used to step off shells in the same manner that ideal stages are stepped off between the equilibrium curve and operating line for a distillation column on a McCabe-Thiele diagram. The number of shells is determined for each individual stream in the system, including the utilities. For this reason, the utilities are usually included in the composite curves as shown in Figure 8.17 for TC3. In this form, the composite curves are referred to as balanced. Since utility temperatures were not specified for TC 3 , values of $200^{\circ} \mathrm{C}$ and $10^{\circ} \mathrm{C}$ were assumed for the hot and cold utilities, respectively. For convenience, the temperature changes of the utility streams were assumed to be negligible.

Figure 8.17 shows the construction to estimate the number of shells for stream 4 of TC3. Starting from the stream's target temperature $\left(100^{\circ} \mathrm{C}\right)$ on the appropriate (cold) curve, triangles are stepped off between the hot and cold curves until the supply temperature $\left(25^{\circ} \mathrm{C}\right)$ of the stream is reached. Trivedi et al. [7] have shown that each horizontal line segment between the two composite curves


Figure 8.17 Estimating the minimum number of shells for cold stream 4 of TC3.

Table 8.14 Estimated Number of Shells
Required for the Streams of TC3

| Stream | Entire network | Hot end | Cold end |
| :--- | :--- | :--- | :--- |
| 1 | 3 | 2 | 2 |
| 2 | 2 | 0 | 2 |
| 3 | 3 | 2 | 2 |
| 4 | 3 | 2 | 2 |
| HU | 1 | 1 | 0 |
| CU | 1 | 0 | 1 |

represents a single shell with no temperature cross. Thus, it is seen that three shells are required to cover the entire temperature interval for stream 4.

Repeating the graphical procedure for each of the hot and cold process streams of TC3 yields the results shown in the first column of Table 8.14. The same procedure can by applied separately to the hot end problem (above the pinch) and the cold end problem (below the pinch) to obtain a result that is consistent with minimum energy usage. The values so obtained are also shown in Table 8.14.

The total number of shells required is the larger of the sums for the hot and cold streams, respectively, including utilities. Thus, for the entire network neglecting the pinch, seven shells are required. Four shells are required in the hot end and five in the cold end treated separately, giving a total of nine for the entire network when the pinch is accounted for. Trivedi et al. [7] point out that the graphical method can sometimes give values that are less than the minimum number of units calculated by Equation (8.1). In these cases, the estimated number of shells should be equated with $U_{\min }$. For TC3, the minimum number of units is five for the entire network neglecting the pinch, three for the hot end and four for the cold end. Therefore, no adjustments are needed for the number-of-shells estimates.

The actual number of shells required in the hot end of TC3 is four (Figures 8.7 and 8.8), which agrees with the estimated value. In the cold end, however, six shells are required (Figures 8.9 and 8.10) compared with the estimated value of five. For the entire network, ten shells are required for a strict minimum-utility design (Figure 8.11) and nine shells are needed for the simplified network of Figure 8.15 , compared with the predicted number of nine shells for a minimum-utility design. Neglecting the pinch, the estimate of seven shells can be compared with the network of Figure 8.16, which has seven shells. It is seen that the graphical method gives reasonable estimates for the minimum number of shells, but it is not as accurate as Equation (8.1), the minimum-number-of-units estimator.

### 8.14.2 Analytical method

The analytical method is based on a procedure developed by Ahmad et al. [8] for calculating the required number of shell passes in a shell-and-tube heat exchanger. The basic idea is that when a multi-pass exchanger is comprised of TEMA E shells connected in series, an acceptable value of the LMTD correction factor should be attained in each individual shell. Inspection of Figure 3.9 shows that for any value of the parameter $R$, there is a maximum value of the parameter $P$ that is, in fact, attained asymptotically as $F \rightarrow-\infty$. This maximum value, $P_{\max }$, is given by [9]:

$$
\begin{equation*}
P_{\max }=\frac{2}{R+1+\sqrt{R^{2}+1}} \tag{8.10}
\end{equation*}
$$

Any exchanger must operate at some fraction, $X_{P}$, of $P_{\max }$ to achieve an acceptable value of $F$. The number of $E$ shells in series required to attain $P=X_{P} P_{\max }$ in each shell is given by the following equations [8]:

$$
\begin{align*}
& N_{s}=\ln [(1-R P) /(1-P)] / \ln W \quad(R \neq 1)  \tag{8.11}\\
& N_{s}=[P /(1-P)]\left(1-X_{P}+1 / \sqrt{2}\right) / X_{P} \quad(R=1)  \tag{8.12}\\
& W=\left(R+1+\sqrt{R^{2}+1}-2 R X_{P}\right) /\left(R+1+\sqrt{R^{2}+1}-2 X_{P}\right) \tag{8.13}
\end{align*}
$$

Ahmad et al. [8] show that a reasonable value for $X_{P}$ is 0.9 . However, the somewhat more conservative value of 0.85 is recommended here. With $X_{P}=0.9$, the smallest value of $F$ for a 1-2 exchanger is approximately 0.75 at an $R$-value of about 1.0. Higher values of $F$ are obtained at larger and smaller values of $R$ where the slopes of the $F$-curves are steeper. With $X_{P}=0.85$, the minimum value of $F$ is approximately 0.8 , again at an $R$-value of about 1.0. Thus, $X_{P}=0.85$ is more in line with the standard procedure of designing for $F \geq 0.8$.

Equations (8.11)-(8.13) can be applied to any individual heat exchanger, e.g., the $136-\mathrm{kW}$ exchanger of Figure 8.15. The hot fluid enters at $150^{\circ} \mathrm{C}$ and leaves at $82^{\circ} \mathrm{C}$, while the cold fluid enters at $62^{\circ} \mathrm{C}$ and leaves at $116.4^{\circ} \mathrm{C}$. Either fluid may be assumed to flow in the shell due to the symmetry of $F$ with respect to fluid placement. Assuming the hot fluid is in the shell, Equations (3.11) and (3.12) give:

$$
\begin{aligned}
& R=\frac{150-82}{116.4-62}=1.25 \\
& P=\frac{116.4-62}{150-62}=0.6182
\end{aligned}
$$

From Equation (8.13) with $X_{P}=0.85$, we obtain:

$$
W=\frac{1.25+1+\sqrt{(1.25)^{2}+1}-2 \times 1.25 \times 0.85}{1.25+1+\sqrt{(1.25)^{2}+1}-2 \times 0.85}=0.8024
$$



Figure 8.18 Enthalpy intervals for TC3.

Table 8.15 Enthalpy Interval Data for TC3

| Interval | Streams | Hot <br> temperature $\left({ }^{\circ} \mathrm{C}\right)$ | Cold <br> temperature $\left({ }^{\circ} \mathrm{C}\right)$ | Number <br> of shells |
| :--- | :--- | :--- | :--- | :--- |
| 1 | $\mathrm{HU}, 3$ | 200 | $100-125$ | 0.1516 |
| 2 | $\mathrm{HU}, 3,4$ | 200 | $91.82-100$ | 0.0414 |
| 3 | $1,3,4$ | $150-90$ | $70-91.82$ | 1.1729 |
| 4 | $1,2,3,4$ | $90-65.25$ | $25-70$ | 1.2227 |
| 5 | $1,2,3$ | $65.25-64$ | $20-25$ | 0.0767 |
| 6 | $1,2, \mathrm{CU}$ | $64-60$ | 10 | 0.0406 |

The required number of shells is obtained from Equation (8.11):

$$
N_{s}=\frac{\ln [(1-1.25 \times 0.6182) /(1-0.6182)]}{\ln [0.8024]}=2.3568 \rightarrow 3
$$

The result is rounded to the next largest integer, giving three shells, in agreement with the value given previously in Table 8.13, which was based on the criterion $F \geq 0.8$.

In order to use Equations (8.11)-(8.13) to predict the number of shells required in a HEN, the composite curves for the HEN are divided into enthalpy intervals as shown in Figure 8.18 for TC3. For each interval, the terminal temperatures of the hot and cold curves are used as stream temperatures to calculate the number of shells required in that interval. The data for TC3 are shown in Table 8.15. Notice that the number of shells in each interval is not rounded to an integral value.

Table 8.16 Shells Required for the Streams of TC3: Analytical Method

| Stream | Number of Shells |  |
| :--- | :--- | :--- |
|  | Above pinch | Below pinch |
| HU | $0.1930 \rightarrow 1.0$ | 0 |
| 1 | 1.1729 | 1.3400 |
| 2 | 0 | 1.3400 |
| 3 | 1.3659 | 1.2994 |
| 4 | 1.2140 | 1.2227 |
| CU | 0 | $0.0406 \rightarrow 1.0$ |
| Total | 4.7531 | 6.2021 |

The number of shells required for each stream, including the utilities, is now obtained by adding the number of shells for each interval in which the stream occurs. This is done separately for intervals above and below the pinch. If the number of shells for any stream turns out to be greater than zero but less than one, it is reset to unity. The results for TC3 are given in Table 8.16.

Ahmad and Smith [10] have shown that the number of shells required for the network is given by the following equation:

$$
\begin{equation*}
\left(N_{s}\right)_{\text {Network }}=\sum_{\text {Streams }}\left(N_{s}\right)_{\text {Stream } j}-\sum_{\text {Intervals }}\left(N_{s}\right)_{\text {Interval } i} \tag{8.14}
\end{equation*}
$$

The first three intervals for TC3 are above the pinch, and the sum of the shells for these intervals is 1.3659. From Table 8.16, the sum of the shells required for the streams above the pinch is 4.7531 . Thus, the number of shells required for the network above the pinch is:

$$
\left(N_{s}\right)_{a b o v e ~ p i n c h}=4.7531-1.3659=3.3872 \Rightarrow 4
$$

At this point, the number of shells is rounded to the next largest integer, giving a total of four shells above the pinch. Below the pinch, the sum of the shells for intervals 4,5 , and 6 is 1.3400 and the sum of the shells required for the streams is 6.2021 . Therefore,

$$
\left(N_{s}\right)_{\text {below pinch }}=6.2021-1.3400=4.8621 \Rightarrow 5
$$

The number of shells required for the entire network is the sum of the values required above and below the pinch, or nine in this case. The analytical method can also be applied to the entire network disregarding the pinch, but due to the additivity of shells over the intervals, the same result is obtained except for rounding to integral values and (possibly) resetting of values to unity for individual streams. For TC3, the sum of shells for the streams above and below the pinch is 10.9552 and the sum of shells for all six intervals is 2.7059, giving:

$$
\left(N_{s}\right)_{n e t w o r k}=10.9552-2.7059=8.2493 \Rightarrow 9
$$

In this case, exactly the same result is obtained when the pinch is ignored. Comparison with results obtained previously shows that both the graphical and analytical methods give the same number of shells when the pinch is accounted for. This is not always the case, however, and in general, the analytical method is considered to be the more reliable of the two [10].

### 8.15 Area Targets

In order to determine the heat-transfer area in a HEN, it is necessary to perform a detailed design of each unit in the network and then sum the areas of all the individual units. It is rather remarkable, therefore, that it is possible to estimate the minimum area required for a HEN before even starting the design process. The estimation procedure relies on estimates of heat-transfer coefficients for individual streams such as the compilation presented by Bell [11].

Suppose we have estimates, $h_{1}$ and $h_{2}$, for the film coefficients, including fouling allowances, of two streams. We can estimate the overall heat-transfer coefficient for a match between the two streams by neglecting the tube wall resistance and setting the area ratio, $A_{o} / A_{i}$, equal to unity. With these approximations, the equation for the design coefficient becomes:

$$
\begin{equation*}
U_{D} \cong\left(1 / h_{1}+1 / h_{2}\right)^{-1} \tag{8.15}
\end{equation*}
$$

(Note that assuming $A_{o} / A_{i} \cong 1.0$ is reasonable for plain tubes, but not for finned tubes.)
Now suppose that in a particular enthalpy interval on the composite curves for the HEN, these two streams are the only streams. Assuming the streams are matched in a counter-current exchanger, the heat-transfer area required for the interval is given by:

$$
\begin{equation*}
A_{\text {interval }}=\frac{q}{U_{D} \Delta T_{\ln }}=\frac{\Delta H}{\Delta T_{\ln }}\left(\frac{1}{h_{1}}+\frac{1}{h_{2}}\right) \tag{8.16}
\end{equation*}
$$

where $\Delta H$ is the width of the enthalpy interval and $\Delta T_{\text {ln }}$ is computed from the terminal temperatures of the hot and cold composite curves on the interval. When the interval contains more than two streams, Linnhoff and Ahmad [5] have shown that the area is given by:

$$
\begin{equation*}
A_{\text {interval } i}=\frac{1}{\left(\Delta T_{\ln }\right)_{i}} \sum_{j}\left(q_{j} / h_{j}\right)_{i} \tag{8.17}
\end{equation*}
$$

where $q_{j}$ is the duty for stream $j$ in the $i$ th interval and the summation extends over all streams that exist in the $i$ th interval. The minimum area required for the network is obtained by summing the areas for all intervals.

When multi-pass shell-and-tube exchangers are used, Equation (8.17) is modified by introducing the LMTD correction factor:

$$
\begin{equation*}
A_{\text {interval } i}=\frac{1}{F_{i}\left(\Delta T_{\ln }\right)_{i}} \sum_{j}\left(q_{j} / h_{j}\right)_{i} \tag{8.18}
\end{equation*}
$$

The LMTD correction factor should be computed based on the number of shells required for the interval. For example, Table 8.15 shows that 1.2227 shells are required for interval 4 of TC3. Rounding to the next largest integer gives two shells, so $F$ for this interval would be computed for an exchanger with two $E$ shells in series, i.e., for a 2-4 exchanger.

To illustrate the procedure, heat-transfer coefficients were (arbitrarily) assigned to the streams of TC3 as shown in Table 8.17. The stream duties in each of the six intervals are given in Table 8.18.

The calculations were performed both for counter-flow exchangers and multi-pass shell-and-tube exchangers, and are summarized in Table 8.19. The predicted minimum network area for counterflow exchangers is $33.74 \mathrm{~m}^{2}$ and the value for multi-pass exchangers is $35.46 \mathrm{~m}^{2}$. These areas are rather small because the stream duties specified for TC3 are small. Note that $F=1.0$ for intervals 1,2 , and 6 because the utility streams were assumed to be isothermal.

Table 8.17 Heat-transfer Coefficients
Assigned to Streams of TC3

| Stream | $h\left(\mathrm{~kW} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |
| :--- | :--- |
| 1 | 1.1 |
| 2 | 0.6 |
| 3 | 0.8 |
| 4 | 1.0 |
| HU | 2.0 |
| CU | 1.5 |

Table 8.18 Stream Duties (kW) in Enthalpy Intervals of TC3

| Stream | Interval |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 |  |
| HU | 62.5 | 45 | - | - | - | - |  |
| 1 | - | - | 120 | 49.5 | 2.5 | 8 |  |
| 2 | - | - | - | 198 | 10 | 32 |  |
| 3 | 62.5 | 20.45 | 54.55 | 112.5 | 12.5 | - |  |
| 4 | - | 24.55 | 65.45 | 135 | - | - |  |
| CU | - | - | - | - | - | 40 |  |

Table 8.19 Area Targeting Calculations for TC3

| Interval | Streams | $\Delta T_{\text {ln }}\left({ }^{\circ} \mathrm{C}\right)$ | Shells | F | Counter-flow <br> area $\left(\mathrm{m}^{2}\right)$ | Multi-pass <br> area $\left(\mathrm{m}^{2}\right)$ |
| :--- | :--- | ---: | :--- | :--- | :---: | :---: |
| 1 | $\mathrm{HU}, 3$ | 86.90 | 1 | 1.0 | 1.26 | 1.26 |
| 2 | $\mathrm{HU}, 3,4$ | 104.04 | 1 | 1.0 | 0.70 | 0.70 |
| 3 | $1,3,4$ | 35.76 | 2 | 0.9550 | 6.79 | 7.11 |
| 4 | $1,2,3,4$ | 28.95 | 2 | 0.9416 | 22.47 | 23.87 |
| 5 | $1,2,3$ | 42.10 | 1 | 0.9994 | 0.82 | 0.82 |
| 6 | $1,2, \mathrm{CU}$ | 51.97 | 1 | 1.0 | 1.70 | 1.7 |
| Total |  |  |  |  | 33.74 | 35.46 |

Details of the calculations for interval 4 are given here. From Table 8.15, the hot temperature range is $90-65.25^{\circ} \mathrm{C}$ and the cold temperature range is $25-70^{\circ} \mathrm{C}$. Therefore,

$$
\left(\Delta T_{\ln }\right)_{c f}=\frac{(65.25-25)-(90-70)}{\ln \left(\frac{65.25-25}{90-70}\right)}=28.95^{\circ} \mathrm{C}
$$

Assuming that the hot stream is in the shell, Equations (3.11) and (3.12) give

$$
\begin{aligned}
& R=\frac{90-65.25}{70-25}=0.55 \\
& P=\frac{70-25}{90-25}=0.6923
\end{aligned}
$$

Since two shells are required in this interval, $F$ is calculated for an exchanger with two shell passes. From Equations (3.13) and (3.14),

$$
\begin{aligned}
& \alpha=\left(\frac{1-R P}{1-P}\right)^{1 / 2}=\left(\frac{1-0.55 \times 0.6923}{1-0.6923}\right)^{1 / 2}=1.41861 \\
& S=\frac{\alpha-1}{\alpha-R}=\frac{1.41861-1}{1.41861-.055}=0.481933
\end{aligned}
$$

Also,

$$
\sqrt{R^{2}+1}=\sqrt{(0.55)^{2}+1}=1.14127
$$

Substitution into Equation (3.15) gives the LMTD correction factor:

$$
\begin{aligned}
F & =\frac{\sqrt{R^{2}+1} \ln \left(\frac{1-S}{1-R S}\right)}{(R-1) \ln \left[\frac{2-S\left(R+1-\sqrt{R^{2}+1}\right)}{2-S\left(R+1+\sqrt{R^{2}+1}\right)}\right]} \\
& =\frac{1.14127\left(\frac{1-0.481933}{1-0.6923 \times 0.481933}\right)}{(0.55-1) \ln \left[\frac{2-0.481933(0.55+1-1.14127}{2-0.481933(0.55+1+1.14127)}\right]} \\
F & =0.9416
\end{aligned}
$$

For interval 4, Equation (8.18) becomes:

$$
A_{\text {interval } 4}=\frac{1}{F_{4}\left(\Delta T_{\ln }\right)_{4}}\left(\frac{q_{1}}{h_{1}}+\frac{q_{2}}{h_{2}}+\frac{q_{3}}{h_{3}}+\frac{q_{4}}{h_{4}}\right)_{4}
$$

The stream heat duties for interval 4 are obtained from Table 8.18, and the heat-transfer coefficients from Table 8.17. Substituting gives:

$$
\begin{aligned}
& A_{\text {interval } 4}=\frac{1}{0.9416 \times 28.95}\left(\frac{49.5}{1.1}+\frac{19.8}{0.6}+\frac{112.5}{0.8}+\frac{135}{1.0}\right) \\
& A_{\text {interval } 4}=23.87 \mathrm{~m}^{2}
\end{aligned}
$$

This is the area for multi-pass exchangers. Setting $F_{4}=1.0$ in the above calculation gives the area for counter-flow exchangers.

The target area can be compared with the area for the network of Figure 8.15, which was obtained by the Pinch Design method. The area of each unit in the network can be calculated using the film coefficients from Table 8.17 and Equation (8.15) for the overall coefficient. The calculations are summarized in Table 8.20. For counter-flow exchangers, the total network area of $36.53 \mathrm{~m}^{2}$ is about $8 \%$ above the target value of $33.74 \mathrm{~m}^{2}$. For multi-pass shell-and-tube exchangers, the estimated network area of $41.84 \mathrm{~m}^{2}$ is about $18 \%$ above the target area of $35.46 \mathrm{~m}^{2}$.

Table 8.20 Heat-transfer Area for the HEN of Figure 8.15

| Unit | Streams | $\Delta T_{\ln }\left({ }^{\circ} \mathrm{C}\right)$ | $U_{D}\left(\mathrm{~kW} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ | $F$ | Counter-flow <br> Area $\left(\mathrm{m}^{2}\right)$ | Multi-pass <br> Area $\left(\mathrm{m}^{2}\right)$ |
| :--- | :--- | ---: | :--- | :--- | :---: | :---: |
| 44-kW cooler | $1, \mathrm{CU}$ | 60.33 | 0.6346 | 1.0 | 1.15 | 1.15 |
| 21.5-kW heater | $\mathrm{HU}, 3$ | 79.22 | 0.5714 | 1.0 | 0.47 | 0.47 |
| 90-kW heater | $\mathrm{HU}, 4$ | 14.34 | 0.6667 | 1.0 | 1.18 | 1.18 |
| 136-kW exchanger | 1,3 | 26.21 | 0.4632 | 0.8906 | 11.20 | 12.58 |
| 135-kW exchanger | 2,4 | 26.80 | 0.3750 | 0.9157 | 13.43 | 14.67 |
| 105-kW exchanger | 2,3 | 33.64 | 0.3429 | 0.7718 | 9.10 | 11.79 |
| Total |  |  |  |  | 36.53 | 41.84 |

### 8.16 The Driving Force Plot

The minimum area target described in the preceding section is based on temperature differences for heat transfer that are obtained from the composite curves. Therefore, in order for a HEN design to approach the target area, the temperature differences in individual exchangers should mimic those of the composite curves. For exchangers operating at the pinch, the $C P$ inequalities (8.6) and (8.7) ensure that the temperature difference increases with distance from the pinch end of the exchanger. This same general trend is exhibited by the composite curves, i.e., the difference between the hot and cold curves increases as one moves away from the pinch in either direction along the curves. In fact, the trends would be identical if the $C P$ ratio of the two streams in a pinch exchanger exactly matched the $C P$ ratio of the composite curves at the pinch. Thus, to approach minimum area in a HEN design, exchangers operating at the pinch should satisfy the following condition [5]:

$$
\begin{equation*}
\left(\frac{C P H}{C P C}\right)_{\text {pinch exchanger }} \cong\left(\frac{C P_{\text {hot composite }}}{C P_{\text {cold composite }}}\right)_{\text {pinch }} \tag{8.19}
\end{equation*}
$$

For example, consider the hot end problem for TC3, where stream 1 can be matched with either stream 3 or stream 4 . The $C P$ ratios for these matches are as follows:

$$
\begin{aligned}
& C P_{1} / C P_{3}=2 / 2.5=0.8 \\
& C P_{1} / C P_{4}=2 / 3=0.67
\end{aligned}
$$

Above the pinch, stream 1 is the only hot stream, so the $C P$ for the hot composite curve is $2 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$. The $C P$ of the cold composite curve is the sum of the $C P$ values for streams 3 and 4 , or $5.5 \mathrm{~kW} /{ }^{\circ} \mathrm{C}$. Therefore, the $C P$ ratio for the composite curves at the pinch is:

$$
C P_{\text {hot composite }} / C P_{\text {cold composite }}=2 / 5.5 \cong 0.36
$$

Although neither stream match closely approximates this value, the match between streams 1 and 4 is the better of the two.

The driving force plot provides a convenient means of examining the driving forces in individual exchangers $v i s-a ̀-v i s$ the composite curves for both pinch and non-pinch exchangers. It is a plot of the temperature difference between the hot and cold composite curves versus the temperature of either the hot or cold streams. For TC3, the data needed to construct the plot are extracted from Table 8.15 and shown in Table 8.21. The temperature differences are plotted against the cold stream temperatures in Figure 8.19.

The driving forces for the two hot end pinch matches are also plotted in Figure 8.19, from which it can be seen that the match between streams 1 and 4 conforms more closely to the driving force

Table 8.21 Data for Constructing the Driving
Force Plot for TC3

| $T_{\text {cold }}\left({ }^{\circ} \mathrm{C}\right)$ | $T_{\text {hot }}\left({ }^{\circ} \mathrm{C}\right)$ | $\Delta T\left({ }^{\circ} \mathrm{C}\right)$ |
| :--- | :---: | :---: |
| 10 | 60 | 50 |
| 10 | 64 | 54 |
| 20 | 64 | 44 |
| 25 | 65.25 | 40.25 |
| 70 | 90 | 20 |
| 91.82 | 150 | 58.18 |
| 91.82 | 200 | 108.18 |
| 100 | 200 | 100 |
| 125 | 200 | 75 |



Figure 8.19 The driving force plot for TC3.
obtained from the composite curves. It is also clear from the graph that both matches significantly under-utilize the available driving force. Due to the simplicity of the problem, however, this underutilization does not cause a problem in completing the hot end design for TC3.
Two exchangers from the cold end design for Case B (Figure 8.10) are also shown in Figure 8.19. The $135-\mathrm{kW}$ pinch exchanger agrees closely with the driving force plot, but the $20-\mathrm{kW}$ non-pinch exchanger significantly over-utilizes the available driving force. Since the $20-\mathrm{kW}$ exchanger was the last process exchanger needed to complete the cold end design, the over-utilization does no harm in this case.

The driving force plot can be used to guide the design process toward the minimum area target and to analyze designs that are grossly over target. One reason for failure to achieve the desired heat-transfer area is over-utilization of driving force due to use of the tick-off heuristic. In such
cases it may be necessary to reduce the duty on one or more exchangers to obtain a better fit to the driving force plot. This procedure will generally result in more than the minimum number of units in the HEN. However, designs that achieve a good fit to the driving force plot while maintaining the number of units within $10 \%$ of the minimum are usually within $10 \%$ of the area target [5].

Although the driving force plot is intuitive and easy to use, the information that it provides is qualitative in nature. A quantitative assessment of the area penalty incurred by the improper use of driving force in a given match can be obtained by recalculating the area target after each successive exchanger is added to the evolving network design. While such a procedure is inconvenient for hand calculations, it is easily implemented in computer software.

### 8.17 Super Targeting

It has been shown in the preceding sections that for a given value of $\Delta T_{\text {min }}$, it is possible to estimate the minimum number of units, minimum-utility usage, minimum number of shells, and minimum heat-transfer area for a HEN. These values can be used to also estimate the minimum capital and operating costs of the HEN. All these estimates can be made prior to starting the actual design of the HEN.

Correlations for estimating the capital cost of heat exchangers are typically of the form:

$$
\begin{equation*}
\operatorname{cost}=a+b(\text { area })^{c} \tag{8.20}
\end{equation*}
$$

where $a, b$, and $c$ are constants for a given type of heat exchanger, and the area to be used is the heat-transfer surface area of the exchanger. Ahmad et al. [6] have shown that the minimum capital cost of the HEN can be estimated by using the average area per shell in Equation (8.20) as follows:

$$
\begin{equation*}
\text { network cost }=a U_{\min }+b N_{s}\left(A_{\min } / N_{s}\right)^{c} \tag{8.21}
\end{equation*}
$$

where $U_{\min }, N_{s}$, and $A_{\min }$ are the target values for minimum number of units, minimum number of shells, and minimum heat-transfer area, respectively. Note that the fixed cost, $a$, is included only once per unit, regardless of the number of shells that comprise the unit. Ahmad et al. [6] and Hall et al. [12] also show how other factors such as materials of construction, pressure ratings, and different exchanger types can be included in the capital cost estimate. If counter-flow heat exchangers are assumed, the number of shells equals the number of units and $N_{s}$ is replaced by $U_{\min }$ in Equation (8.21).

The minimum annual operating cost for the HEN can be estimated as the annual utility cost for a minimum-utility design. The other major factor involved in the operating cost is pumping cost, which depends on the pressure drop experienced by the streams in each heat exchanger. Methods for estimating these pressure drops are discussed in Refs. [13-15]. The heat exchanger design equations are used to relate stream pressure drop to heat-transfer area and stream heat-transfer coefficient. This is possible because both pressure drop and heat-transfer coefficient depend on the stream velocity. In this way, the estimated heat-transfer coefficients for the streams are used to estimate pressure drops for a given heat-transfer area. Although the accuracy of such estimates is questionable, neglecting pressure-drop effects can lead to serious errors in HEN design [3,4]. Hence, it is preferable to use both utility and pumping costs in estimating the annual operating cost for a HEN. With estimates of stream pressure drops, the capital cost for pumps and compressors can also be estimated and included in the total cost estimate for the HEN [15].

By using a capital cost recovery factor to annualize the capital cost, the operating and capital costs can be combined to obtain an estimate of the total annual cost of the HEN. These calculations can be performed for different values of $\Delta T_{\min }$ within the range of feasible values determined from the composite curves. The optimum value of $\Delta T_{\text {min }}$ to use in designing the HEN is the one that


Figure 8.20 Determination of the optimal value of $\Delta T_{\min }$ for $H E N$ design. $P / C$ system cost is the annualized capital and operating cost of pumps and compressors. Area cost is the annualized capital cost of heat exchangers (Source: Ref. [15]).
minimizes the total annual cost. Figure 8.20 depicts the situation schematically and illustrates the effect of neglecting pumping costs on the optimum value of $\Delta T_{\text {min }}$ that is calculated.

### 8.18 Targeting by Linear Programming

The targeting procedures presented in preceding sections cannot be used when there are forbidden stream matches. Forbidden matches may arise from considerations such as safety, process operability, or plant layout. These additional constraints may result in higher utility requirements for the HEN. An alternative targeting procedure that can handle these constraints uses linear programming (LP).

A linear program is an optimization problem in which a linear function is to be maximized or minimized subject to a set of linear equality and/or inequality constraints. Here we will show that the problem table algorithm presented in Section 8.4 can be formulated as a linear program. To this end, let $Q_{j}$ be the heat flow leaving the $j$ th SN and let $Q_{o}$ be the amount of hot utility supplied to SN1. Then the energy balance for $\mathrm{SN} j$ can be written as:

$$
\begin{equation*}
Q_{j}=Q_{j-1}+\left\{\sum(C P)_{h o t, i}-\sum(C P)_{c o l d, i}\right\} \Delta T_{j} \tag{8.22}
\end{equation*}
$$

where the summations extend over the streams that exist in $\mathrm{SN} j$. Using Equation (8.2), Equation (8.22) can be written as:

$$
\begin{equation*}
Q_{j}=Q_{j-1}-(\text { deficit })_{j} \tag{8.23}
\end{equation*}
$$

or

$$
\begin{equation*}
Q_{j}-Q_{j-1}+(\text { deficit })_{j}=0 \tag{8.24}
\end{equation*}
$$

Table 8.22 Solution to Linear
Program (8.26)

| $j$ | $Q_{j}(\mathrm{~kW})$ |
| :--- | :---: |
| 0 | 107.5 |
| 1 | 117.5 |
| 2 | 105 |
| 3 | 0 |
| 4 | 135 |
| 5 | 52.5 |
| 6 | 40 |

Now for a problem with one hot and one cold utility and $N \mathrm{SNs}, Q_{N}$ is the heat flow to the cold utility, i.e., the cold utility requirement. Therefore, to find the minimum-utility requirements for the problem we need to minimize $Q_{o}$ and $Q_{N}$ while satisfying the energy balance equation for each SN. In addition, all the heat flows must be non-negative. These conditions can be stated mathematically as follows:

$$
\begin{array}{ll} 
& \min f=Q_{0}+Q_{N}  \tag{8.25}\\
\text { subject to: } & Q_{j}-Q_{j-1}+\left({\text { deficit })_{j}=0 \quad(j=1,2, \ldots, N)} Q_{j} \geq 0 \quad(j=0,1,2, \ldots, N)\right.
\end{array}
$$

Notice that both the objective function, $f$, and the constraints are linear in the variables, $Q_{j}$. Therefore, this is a linear program.

The deficits for TC3 are given in Table 8.2. Substituting these values into (8.25) and setting $N=6$ gives:

$$
\begin{array}{ll} 
& \min f=Q_{0}+Q_{6}  \tag{8.26}\\
\text { subject to: } & Q_{1}-Q_{0}-10=0 \\
& Q_{2}-Q_{1}+12.5=0 \\
& Q_{3}-Q_{2}+105=0 \\
& Q_{4}-Q_{3}-135=0 \\
& Q_{5}-Q_{4}+82.5=0 \\
& Q_{6}-Q_{5}+12.5=0 \\
& Q_{0}, Q_{1}, Q_{2}, Q_{3}, Q_{4}, Q_{5}, Q_{6} \geq 0
\end{array}
$$

This linear program can be solved using any of the widely available LP software packages, such as EXCEL Solver. The solution, given in Table 8.22, shows that the minimum hot and cold utility requirements are 107.5 and 40 kW , respectively, in agreement with the results obtained previously. Notice that the heat flow leaving SN3 is zero, indicating that the pinch occurs between SN3 and SN4, i.e., at $70^{\circ} \mathrm{C}$ for the cold streams and $90^{\circ} \mathrm{C}$ for the hot streams.

When the problem contains more that a single hot or cold utility, the total utility cost is minimized rather than the total utility usage. The energy balance equations are also modified to allow introduction of utilities at the appropriate SNs. More substantive modifications are required to accommodate forbidden matches. In this case the problem is formulated as a mixed integer linear program (MILP), i.e., a linear program in which some variables take on only integer values. The MILP arises from the introduction of binary variables used to track the stream matches in the SNs. Each of these variables is equal to one if the two streams that it tracks are matched; otherwise, it is equal to zero. A good presentation of this topic can be found in the textbook by Biegler et al. [16]; the use of mathematical programming for the automatic synthesis of HENs is also covered in some detail. Further information can be found in Refs. [15,17-20].

### 8.19 Computer Software

Commercial software packages for HEN design include SuperTarget by Linnhoff-March, a division of KBC Process Technology, Ltd. (www.linhoffmarch.com), Aspen Pinch and HX-Net from Aspen Technology, Inc. (www.aspentech.com), and HEXTRAN by SimSci-Esscor (www.simsciesscor.com). With the exception of HEXTRAN, these packages are interactive programs that allow the user to develop HEN designs on a grid diagram. They all have the capability to generate HEN designs automatically as well. HEXTRAN and HX-Net are considered in the following subsections.

### 8.19.1 HEXTRAN

Commercialized in 1980, HEXTRAN is the oldest of the HEN design packages and by far the most primitive. In Targeting mode it calculates minimum-utility targets and pinch temperatures, and constructs composite and grand composite curves. A variety of other targeting plots can also be generated. Although the program's graphing capability is minimal, all plots can be exported to EXCEL for manipulation by the user.
In Synthesis mode, HEXTRAN automatically generates HEN designs using a dual temperature approach method. The Heat Recovery Approach Temperature (HRAT) is the $\Delta T_{\text {min }}$ used for calculating utility and heat recovery targets. The Exchanger Minimum Approach Temperature (EMAT) is the $\Delta T_{\text {min }}$ imposed on individual heat exchangers. Setting EMAT $<$ HRAT allows some heat transfer across the pinch, which is required for practical HEN configurations. The algorithm identifies feasible stream matches in each SN and then combines the SNs to obtain an initial network configuration. Network simplification is accomplished by identifying and breaking heat load loops until a configuration is obtained that approaches the minimum-number-of-units target [21]. Use of the program for retrofit applications is discussed in Ref. [22].
The use of HEXTRAN for targeting and HEN design is considered in the following examples.

## Example 8.1

Use HEXTRAN to perform targeting calculations for TC3 by proceeding as follows:
(a) Determine the range of $\Delta T_{\text {min }}$ for heat recovery, i.e., HRAT.
(b) Find the minimum-utility requirements, maximum amount of heat recovery, and the hot and cold stream temperatures at the pinch for a set of HRAT values covering the range found in part (a).

## Solution

(a) When HEXTRAN is run in targeting mode with HRAT set to zero, it calculates the feasible range for HRAT. To begin, SI units are selected, the temperature unit is changed from Kelvin to Celsius and the unit of time is changed from hour to second. Next, the Calculation Type is set to Targeting, and under Calculation Options HRAT is set to zero (the default value).

The flowsheet for this problem consists simply of six unconnected streams (four process streams and two utility streams) as shown below:


The stream type is changed to Bulk Property for each of the four process streams and to Utility for the two utility streams. The following data are entered for each process stream:

- Flow rate $=5 \mathrm{~kg} / \mathrm{s}$ (arbitrary)
- Pressure $=500 \mathrm{kPa}$ (arbitrary)
- Temperature = Supply temperature
- Outlet (exit) temperature = Target temperature
- Stream duty as an average value
- Heat-transfer coefficient $\left(\mathrm{W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ as an average value

The stream flow rate and pressure are required by HEXTRAN but are not needed for this problem, so the values were chosen arbitrarily. The unit for duty ( $\mathrm{MMkJ} / \mathrm{s}$ ) is very large and only one or two decimal places are typically printed in the output file. Therefore, to avoid loss of significant figures, the stream duties are scaled by a factor of $10^{5}$ (a factor of $10^{6}$ causes the program to hang up during execution). For example, the duty for stream 1 is entered as $18 \mathrm{MMkJ} / \mathrm{s}$. This scaling does not affect the targeting calculations. The same results are obtained when different scale factors and/or units are used. The default value ( $100 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ ) for heat-transfer coefficients can be used if estimated values are not available or if area estimates are not required.

Required data for the utility streams are inlet and outlet temperatures and available duty. HEXTRAN does not accept an isothermal utility stream, so for the hot utility, inlet and outlet
temperatures of $200^{\circ} \mathrm{C}$ and $199^{\circ} \mathrm{C}$ are specified. For the cold utility, $10^{\circ} \mathrm{C}$ and $10.1^{\circ} \mathrm{C}$ are used. The duty for each utility is set at $50 \mathrm{MMkJ} / \mathrm{s}$ (equivalent to 500 kW in the original problem).

The input file generated by the HEXTRAN GUI is given below, followed by the relevant data extracted from the output file. Under heat recovery limits, the range for HRAT is seen to be from $12.5^{\circ} \mathrm{C}$ to $130^{\circ} \mathrm{C}$, corresponding to a threshold value of $12.5^{\circ} \mathrm{C}$. In fact, the correct threshold value was found by hand calculation to be $12.727^{\circ} \mathrm{C}$. The output data for the composite curves shows a minimum temperature difference of $12.7^{\circ} \mathrm{C}$, which is correct to the given number of significant figures.

## HEXTRAN Input File for Example 8.1, Part (a)

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
```

$\$$
\$ General Data Section
\$
TITLE PROJECT=EX8-1, PROBLEM=TARGETING, SITE=
$\$$
DIME SI, AREA=M2, CONDUCTIVITY=WMK, DENSITY=KG/M3, *
ENERGY=KJ, FILM=WMK, LIQVOLUME=M3, POWER=KW, *
PRESSURE=KPA, SURFACE=NM, TIME=SEC, TEMPERATURE=C, *
UVALUE=WMK, VAPVOLUME=M3, VISCOSITY=PAS, WT=KG, *
XDENSITY=DENS, STDVAPOR=22.414
\$
OUTD SI, AREA=M2, CONDUCTIVITY=WMK, DENSITY=KG/M3, *
ENERGY=KJ, FILM=WMK, LIQVOLUME=M3, POWER=KW, *
PRESSURE=KPA, SURFACE=NM, TIME=SEC, TEMPERATURE=C, *
UVALUE=WMK, VAPVOLUME=M3, VISCOSITY=PAS, WT=KG, *
XDENSITY=DENS, STDVAPOR=22.414, ADD
$\$$
PRINT ALL, *
RATE=M
\$
CALC PGEN=New, WATER=Saturated
\$
$\$ \quad$ Component Data Section
$\$$
\$ Thermodynamic Data Section
$\$$
\$Stream Data Section
$\$$
STREAM DATA
$\$$
PROP $S T R M=1, ~ N A M E=1, ~ T E M P=150.00, ~ P R E S=500.000$, *
TOUT $=60.00, \operatorname{LIQUID}(W)=5.000, \operatorname{Duty}(A V G)=18, ~ *$
Film $($ AVG $)=1100$
$\$$
PROP STRM=2, NAME=2, TEMP=90.00, PRES=500.000, *
TOUT $=60.00, \operatorname{LIQUID}(W)=5.000, \operatorname{Duty}(A V G)=24, *$
Film (AVG) $=600$

## HEXTRAN Input File for Example 8.1, Part (a) (continued)

```
    PROP STRM=3, NAME=3, TEMP=20.00, PRES=500.000, *
        TOUT=125.00, LIQUID (W)=5.000, Duty(AVG)=26.25, *
        Film(AVG)=800
$
    PROP STRM=4, NAME=4, TEMP=25.00, PRES=500.000, *
        TOUT=100.00, LIQUID (W)=5.000, Duty(AVG)=22.5, *
        Film(AVG) =1000
$
    UTILITY STRM=HU, TEMP=200.00, TOUT=199.00, FILM=2000.00, *
    DUTY=50.00, BSIZE=92.90, BCOST=0.00, LINEAR=538.20, *
    CONSTANT=0.00, EXPONENT=0.60
$
    UTILITY STRM=CU, TEMP=10.00, TOUT=10.10, FILM=1500.00, *
    DUTY=50.00, BSIZE=92.90, BCOST=0.00, LINEAR=538.20, *
    CONSTANT=0.00, EXPONENT=0.60
$
$ Calculation Type Section
$
TARGETING
$
    SPEC HRAT=0.00
$
    PARAMETER FILM=100.00, ALPHA=1.00, EXPONENT=1.00, *
                        DELTA=0.00
$
    PRINT DUTY, COMPOSITE, GRAND, SUMMARY
$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR, RATE=10.0, *
            LIFE=30
$
    HXCOST BSIZE=92.90, BCOST=0.00, LINEAR=538.20, *
        EXPONENT=0.60, CONSTANT=0.00
$
$ End of keyword file...
```


## HEXTRAN Results for Example 8.1, Part (a)

HEAT RECOVERY LIMITS
MAXIMUM MINIMUM

| HRAT | - DEG C | 12.5 | 130.0 |
| :--- | :--- | ---: | ---: |
| QPROCESS DUTY | - MMKJ /SEC | 42.0 | 0.0 |
| QHEATING DUTY | - MMKJ /SEC | 6.8 | 48.8 |
| QCOOLING DUTY | - MMKJ /SEC | 0.0 | 42.0 |
| THEATING TEMPERATURE | - DEG C | 99.1 | 20.0 |
| TCOOLING TEMPERATURE | - DEG C | 60.0 | 150.0 |
| MTD | - DEG C | 24.0 | 130.0 |

## HEXTRAN Results for Example 8.1, Part (a) (continued)

RUN NO. 1 HRAT $=0.0$ DEG C PROCESS EXCHANGE DUTY $=42.0000 \mathrm{MMKJ} / \mathrm{SEC}$

| HOT | COLD | APPROACH | ENTE |
| :---: | :---: | :---: | :---: |
| COMPOSITE | COMPOSITE | TEMPERATURE |  |
| 150.0 | 99.1 | 50.9 | 1 |
| 146.0 | 97.6 | 48.4 |  |
| 142.0 | 96.2 | 45.8 |  |
| 138.0 | 94.7 | 43.3 |  |
| 134.0 | 93.3 | 40.7 |  |
| 130.0 | 91.8 | 38.2 |  |
| 126.0 | 90.4 | 35.6 |  |
| 122.0 | 88.9 | 33.1 |  |
| 118.0 | 87.5 | 30.5 |  |
| 114.0 | 86.0 | 28.0 |  |
| 110.0 | 84.5 | 25.5 |  |
| 106.0 | 83.1 | 22.9 |  |
| 102.0 | 81.6 | 20.4 |  |
| 98.0 | 80.2 | 17.8 |  |
| 94.0 | 78.7 | 15.3 |  |
| 90.0 | 77.3 | 12.7 MIN | 2 |
| 87.8 | 73.3 | 14.5 |  |
| 85.6 | 69.3 | 16.3 |  |
| 83.4 | 65.3 | 18.1 |  |
| 81.2 | 61.3 | 19.9 |  |
| 79.0 | 57.3 | 21.7 |  |
| 76.8 | 53.3 | 23.5 |  |
| 74.6 | 49.3 | 25.3 |  |
| 72.4 | 45.3 | 27.1 |  |
| 70.2 | 41.3 | 28.9 |  |
| 68.0 | 37.3 | 30.7 |  |
| 65.8 | 33.3 | 32.5 |  |
| 63.6 | 29.3 | 34.3 |  |
| 61.4 | 25.3 | 36.1 |  |
| 61.2 | 25.0 | 36.2 | 4 |
| 60.2 | 21.0 | 39.2 |  |
| 60.0 | 20.0 | 40.0 | 1 |

50.9
48.4
146.0
97.6
45.8
138.0
134.0
130.0
126.0
118.0
114.0
110.0
106.0
102.0
98.0
90.0
77.3
12.7 MIN 2
87.8
83.4
81.2
79.0
74.6
49.3
25.3
72.4
45.3
28.9
30.7
32.5
34.3
$61.4 \quad 25.3 \quad 36.1$
$\begin{array}{llll}61.2 & 25.0 & 36.2 & 4 \\ 60.2 & 21.0 & 39.2 & \end{array}$
$\begin{array}{llll}60.0 & 20.0 & 40.0 & 1\end{array}$
$\begin{array}{lll}1 & 2 & 3\end{array}$

## SUMMARY OF CASES

TEMPERATURE SUMMARY TABLE

| HRAT | QPROCESS | THEATING | TCOOLING | HOT APPROACH | CLD APPROACH | LMTD |
| :--- | :---: | :--- | :---: | :---: | :---: | :---: |
| DEG C | MMKJ /SEC <br> DEG C | DEG C | DEG C | DEG C |  |  |

DUTY SUMMARY TABLE
HRAT QPROCESS QHEATING QCOOLING QUTILITY AREA U-VALUE DEG C MMKJ /SEC MMKJ /SEC MMKJ /SEC MMKJ /SEC M2 WATTS / M2-K
0.0
42.00
6.75
0.00
6.75
4267042 .
409.6
(b) A second run is made with the following set of HRAT values:

| 12.73 | 50.0 |
| :--- | ---: |
| 12.80 | 100.0 |
| 15.0 | 120.0 |
| 20.0 | 125.0 |
| 30.0 | 130.0 |

The summary of cases shown below was extracted from the output file and contains all the required information for this problem. Note that the areas and duties must be divided by the scale factor of $10^{5}$ to obtain the correct values.

## HEXTRAN Results for Example 8.1, Part (b)



```
SUMMARY OF CASES
```

TEMPERATURE SUMMARY TABLE

| HRAT | QPROCESS | THEATING | TCOOLING | HOT APPROACH | CLD APPROACH | LMTD |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DEG C | MMKJ / SEC | DEG C | DEG C | DEG C | DEG C | DEG C |
| 130.0 | 0.00 | 0.0 | 150.0 | 0.0 | 0.0 | 0.0 |
| 125.0 | 1.00 | 0.0 | 145.0 | 145.0 | 20.0 | 125.5 |
| 120.0 | 1.80 | 0.0 | 141.0 | 141.0 | 20.0 | 122.1 |
| 100.0 | 5.80 | 33.3 | 121.0 | 121.0 | 20.0 | 107.6 |
| 50.0 | 21.50 | 61.8 | 80.5 | 90.0 | 40.0 | 60.7 |
| 30.0 | 32.50 | 81.8 | 69.5 | 90.0 | 60.0 | 40.6 |
| 20.0 | 38.00 | 91.8 | 64.0 | 90.0 | 70.0 | 31.1 |
| 15.0 | 40.55 | 96.5 | 61.5 | 90.0 | 74.6 | 26.7 |
| 12.8 | 41.65 | 98.5 | 60.4 | 90.0 | 76.6 | 24.7 |
| 12.7 | 41.65 | 98.5 | 60.4 | 90.0 | 76.6 | 24.7 |

DUTY SUMMARY TABLE

| HRAT | QPROCESS | QHEATING | QCOOLING | QUTILITY | AREA | U-VALUE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DEG C | MMKJ / SEC | MMKJ / SEC | MMKJ / SEC | MMKJ / SEC | M2 | ATTS / M2-K |
| 130.0 | 0.00 | 48.75 | 42.00 | 90.75 | 0 | . 0.0 |
| 125.0 | 1.00 | 47.75 | 41.00 | 88.75 | 17714 | 449.9 |
| 120.0 | 1.80 | 46.95 | 40.20 | 87.15 | 35069 | 420.5 |
| 100.0 | 5.80 | 42.95 | 36.20 | 79.15 | 109324 | 493.2 |
| 50.0 | 21.50 | 27.25 | 20.50 | 47.75 | 804602 | 440.5 |
| 30.0 | 32.50 | 16.25 | 9.50 | 25.75 | 1913414 | . 418.2 |
| 20.0 | 38.00 | 10.75 | 4.00 | 14.75 | 2959870 | . 412.2 |
| 15.0 | 40.55 | 8.20 | 1.45 | 9.65 | 3713650 | . 409.6 |
| 12.8 | 41.65 | 7.10 | 0.35 | 7.45 | 4129781 | 408.8 |
| 12.7 | 41.65 | 7.10 | 0.35 | 7.45 | 4129781 | . 408.8 |

Here again it can be seen that some of the results are surprisingly inaccurate. Two of the hot stream pinch temperatures are off by one degree (141 versus 140 and 121 versus 120). Likewise,
the cold stream pinch temperatures are inaccurate for HRAT values of $15,12.8$, and 12.73. The hot and cold utility requirements for $\mathrm{HRAT}=12.73$ are 71 and 3.5 kW , respectively, whereas the correct values are approximately 67.5 kW and zero. Although these minor discrepancies may be of little practical significance, they nevertheless seem inexcusable considering that accurate results are easily obtained by hand for this problem. The error in the area estimates is more substantial. For HRAT $=20^{\circ} \mathrm{C}$, the value of $29.6 \mathrm{~m}^{2}$ is about $10 \%$ below the counter-flow area of $33.74 \mathrm{~m}^{2}$ obtained by hand in Table 8.19.

## Example 8.2

Use HEXTRAN to design a HEN for TC3.

## Solution

For this problem, HEXTRAN is run in synthesis mode with HRAT $=20^{\circ} \mathrm{C}$. To obtain a practical design, a value of EMAT must be selected that is less than HRAT. Two values of EMAT are tried, $17^{\circ} \mathrm{C}$ and $18^{\circ} \mathrm{C}$. The HEXTRAN data from Example 8.1 are modified for this problem by changing the Calculation Type to Synthesis and entering the desired values of HRAT and EMAT under Calculation Options/Specifications. Note that both cases can be executed in a single HEXTRAN run. In addition, under Calculation Options/Limits, the maximum area per shell is set to $5 \times 10^{6} \mathrm{~m}^{2}$, an absurdly large value, in order to accommodate the scale factor of $10^{5}$ applied to the stream duties. The resulting input file generated by the GUI is shown below.

Data for the network generated with EMAT $=17^{\circ} \mathrm{C}$ were extracted from the output file and are shown below following the input file. These data and the corresponding results for EMAT $=18^{\circ} \mathrm{C}$ were used to construct the grid diagrams for the networks shown below following the output data. Notice that both networks meet the minimum-utility targets for $\Delta T_{\text {min }}=\mathrm{HRAT}=20^{\circ} \mathrm{C}$, but have small $\Delta T_{\min }$ violations as allowed by the specified values of EMAT.

## HEXTRAN Input File for Example 8.2

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=EX8-2, PROBLEM=SYNTHESIS, SITE=
$
DIME SI, AREA=M2, CONDUCTIVITY=WMK, DENSITY=KG/M3, *
    ENERGY=KJ, FILM=WMK, LIQVOLUME=M3, POWER=KW, *
    PRESSURE=KPA, SURFACE=NM, TIME=SEC, TEMPERATURE=C, *
    UVALUE=WMK, VAPVOLUME=M3, VISCOSITY=PAS, WT=KG, *
    XDENSITY=DENS, STDVAPOR=22.414
$
OUTD SI, AREA=M2, CONDUCTIVITY=WMK, DENSITY=KG/M3, *
    ENERGY=KJ, FILM=WMK, LIQVOLUME=M3, POWER=KW, *
    PRESSURE=KPA, SURFACE=NM, TIME=SEC, TEMPERATURE=C, *
    UVALUE=WMK, VAPVOLUME=M3, VISCOSITY=PAS, WT=KG, *
    XDENSITY=DENS, STDVAPOR=22.414, ADD
$
PRINT ALL, *
    RATE=M
$
CALC PGEN=New, WATER=Saturated
$
$ Component Data Section
```

\$

## HEXTRAN Input File for Example 8.2 (continued)

```
$ Thermodynamic Data Section
$
$Stream Data Section
$
STREAM DATA
```

\$
PROP $S T R M=1, ~ N A M E=1, ~ T E M P=150.00, ~ P R E S=500.000$, *
TOUT $=60.00$, LIQUID $(W)=5.000, ~ D u t y(A V G)=18, ~ *$
Film $($ AVG $)=1100$
$\$$
PROP STRM=2, NAME=2, TEMP=90.00, PRES=500.000, *
TOUT=60.00, LIQUID $(W)=5.000, \operatorname{Duty}(A V G)=24, ~ *$
Film (AVG) $=600$
\$
PROP STRM=3, NAME=3, TEMP=20.00, PRES=500.000, *
TOUT=125.00, LIQUID $(W)=5.000$, Duty (AVG) $=26.25$, *
Film (AVG) $=800$
\$
PROP STRM=4, $\mathrm{NAME}=4, \mathrm{TEMP}=25.00, ~ \mathrm{PRES}=500.000$, *
TOUT=100.00, LIQUID $(W)=5.000, ~ D u t y(A V G)=22.5, ~ *$
Film(AVG) $=1000$
$\$$
UTILITY STRM=HU, TEMP=200.00, TOUT=199.00, FILM=2000.00, *
DUTY=50.00, $\operatorname{BSIZE}=92.90, \quad B C O S T=0.00, ~ L I N E A R=538.20$, *
CONSTANT=0.00, EXPONENT=0.60
\$
UTILITY STRM=CU, TEMP=10.00, TOUT=10.10, FILM=1500.00, *
DUTY=50.00, $\operatorname{BSIZE}=92.90, \quad B C O S T=0.00, ~ L I N E A R=538.20, ~ *$
CONSTANT=0.00, EXPONENT=0.60
\$
\$ Calculation Type Section
$\$$
SYNTHESIS
\$
SPEC HRAT=20.00, 20.00, EMAT=17.00, 18.00
\$
PARAMETER FILM=100.00
\$
PRINT SPLIT=Short, UNSPLIT=Last
$\$$
PLOT ALL
\$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR, RATE=10.0, *
LIFE=30
\$
HXCOST BSIZE=92.90, BCOST=0.00, LINEAR=538.20, *
EXPONENT=0.60, CONSTANT=0.00
\$
LIMITS MAXP=10, MAXS=10, MAXAREA=5000000.000000, *
MINFT=0.800000
\$
\$ End of keyword file...

## HEXTRAN Results for Example 8.2 with EMAT $=17^{\circ} \mathrm{C}$

NETWORK WITHOUT STREAM SPLITTING FOR RUN NO. 1


HEAT EXCHANGER SUMMARY - TEMPERATURE DATA

| UNIT | STRM | TEMP (DEG C) |  | FLOW | STRM | TEMP (DEG C) |  | FLOW |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | ID | IN | OUT | RATIO | ID | IN | OUT | RATIO |
| 1 | 1 | 150.0 | / 109.5 | 1.000 | 4 | 73.0 | / 100.0 | 1.000 |
| 2 | 2 | 90.0 | / 72.0 | 1.000 | 4 | 25.0 | / 73.0 | 1.000 |
| 3 | 1 | 109.5 | / 60.0 | 1.000 | 3 | 42.4 | / 82.0 | 1.000 |
| 4 | 2 | 72.0 | / 65.0 | 1.000 | 3 | 20.0 | / 42.4 | 1.000 |
| 500 | 2 | 65.0 | / 60.0 | 1.000 | CU | 10.0 | / 10.1 |  |
| 501 | HU | 200.0 | / 199.0 |  | 3 | 82.0 | / 125.0 | 1.000 |

## HEAT EXCHANGER SUMMARY - GENERAL DATA

| UNIT | DUTY | AREA | U-VALUE | FT | NUMBER OF SHELLS |
| :---: | :---: | :--- | :---: | :---: | :---: | :---: |
| NUMBER | MMKJ /SEC | M2 | WATTS / M2-K |  | SERIES PARALLEL |


| 1 | 8.1000 | 404645.3 | 523.810 | 0.891 | 1 | 1 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 2 | 14.4000 | 1360883.7 | 375.000 | 0.957 | 2 | 1 |
| 3 | 9.9000 | 1200684.0 | 463.158 | 0.803 | 2 | 1 |
| 4 | 5.6000 | 453297.4 | 342.857 | 0.980 | 1 | 1 |
| 500 | 4.0000 | 178097.0 | 428.571 | 1.000 | 1 | 1 |
| 501 | 10.7500 | 199360.6 | 571.429 | 0.999 | 1 | 1 |

## HEN for TC3 Generated By HEXTRAN with EMAT $=17^{\circ} \mathrm{C}$



## HEN for TC3 Generated By HEXTRAN with EMAT $=18^{\circ} \mathrm{C}$



With EMAT $=17^{\circ} \mathrm{C}$, the network contains six units and no stream splits. The $99-\mathrm{kW}$ and $144-\mathrm{kW}$ exchangers operate across the pinch and thus have $\Delta T_{\text {min }}$ violations. Only the $99-\mathrm{kW}$ exchanger has a significant temperature cross, and it requires two shells. The counter-flow area estimate for this network is $34.46 \mathrm{~m}^{2}$, which is about $1.4 \%$ over target. For multi-pass exchangers, the estimated area (calculated by hand) is $40.85 \mathrm{~m}^{2}$, which is approximately $15 \%$ over target. With six units, seven shells, no stream splits, on-target utility usage, near minimum heat-transfer area, and only small $\Delta T_{\min }$ violations, this network is clearly superior to any of those obtained by hand.

Notice that HEXTRAN uses two shells in series for the $144-\mathrm{kW}$ exchanger. The reason is that the minimum value for the LMTD correction factor was set at the default value of 0.8 , whereas the actual $F$-value for this unit is 0.789 with one shell pass. In fact, a single shell pass is adequate; checking the operating point on Figure 3.9 shows that it does not lie on the steeply sloping part of the graph. The higher $F$-value for this unit used by HEXTRAN results in a smaller network area. Re-running with the minimum $F$-value set at 0.78 results in a network area of $40.86 \mathrm{~m}^{2}$, in agreement with the value given above.

With EMAT $=18^{\circ} \mathrm{C}$, a network without stream splitting was obtained comprising eight units and nine shells. This network is not shown since it is clearly inferior to the one obtained with EMAT $=17^{\circ} \mathrm{C}$. A second network was obtained with stream 2 split into two branches as shown above. It contains seven units and ten shells. The network obtained by hand and shown in Figure 8.14 also meets the minimum-utility targets with $\Delta T_{\min }=18^{\circ} \mathrm{C}$ and stream 2 split into two branches. However, the latter network contains only six units and nine shells, and is therefore simpler than the configuration generated by HEXTRAN.

### 8.19.2 HX-Net

HX-Net was developed by Hyprotech, Ltd. and is now marketed by Aspen Technology, Inc. As noted above, HX-Net is an interactive program that provides a grid diagram on which the user can develop a HEN design. The software calculates targets for utility consumption, heat-transfer area, and number of shells. It contains an MILP routine that is used for targeting when forbidden stream matches are specified by the user. Super targeting is done based on the trade-off between the capital cost of heat exchangers and utility costs; pressure-drop effects are neglected. The software also generates composite curves, the grand composite curve, and driving force plots.

HX-Net can generate HEN designs automatically, starting either from scratch or from a partially completed network developed by the user. The algorithm employs a two-stage procedure. In the first stage, an MILP is solved to minimize an annualized cost function comprised of exchanger capital cost and utility cost. The solution gives the optimal utility loads, stream matches and duties. Details of the model are given by Shethna et al. [23]. In the second stage, another MILP is solved to obtain a network configuration that conforms to the optimal stream matches and duties obtained in the first stage. Unfortunately, the automatic design feature is not available with an academic license.

HX-Net interfaces with the HYSYS process simulator. It can, for example, automatically extract data from a HYSYS flowsheet and set up the corresponding HEN on an interactive grid diagram. Modifications made to the HEN can subsequently be implemented in the HYSYS flowsheet so that their effect on the overall process can be evaluated. The HYSYS flowsheet must be modified manually, however.

## Example 8.3

Use HX-Net to perform targeting calculations for TC3. Use the following economic data:

$$
\begin{array}{ll}\text { Hot utility cost: } & \begin{array}{l}\$ 150 / \mathrm{kW} \cdot \text { year } \\ \text { Cold utility cost: }\end{array} \\ \text { Rate of return: } & \$ 200 / \mathrm{kW} \cdot \text { year } \\ \text { Plant life: } & 50 \% \\ \text { Heat exchanger capital cost }(\$)=4000+7500 \text { (area) })^{0.8}\end{array}
$$

## Solution

After starting HX-Net, select Tools on the toolbar, then Preferences, and under Variables set the units to Energy Integration - SI. Then add new units as follows:

| Energy: | kW |
| :--- | :--- |
| $M C_{P}:$ | $\mathrm{kW} /{ }^{\circ} \mathrm{C}$ |
| Heat-transfer coefficient: | $\mathrm{kW} / \mathrm{m}^{2} \cdot{ }^{\circ} \mathrm{C}$ |

Next, open a new Heat Integration Case and enter the data for the four process streams. In the column labeled Clean HTC, enter the heat-transfer coefficients from Table 8.17, and enter zero for the fouling factors. This will give the correct values for the stream coefficients, which are automatically entered in the column labeled Film HTC. The columns labeled Flowrate and Effective $C_{P}$ are left blank.

Now enter the data for the two utility streams, including unit costs. No flow rate, load, or heat capacity data are required.

Next, select the Economics tab and set the default parameters for capital cost as follows:

$$
\begin{aligned}
a & =4000 \\
b & =7500 \\
c & =0.8
\end{aligned}
$$

Notice that the rate of return and plant life specified for this problem are the default values in HX-Net.
Clicking on the targeting icon opens the targets window shown below. The user can change the value of $\Delta T_{\min }$ and new target values are automatically calculated. Notice that the target values for utility usage, number of units (MER stands for Maximum Energy Recovery), number of shells, and counter-flow area are in agreement with the hand calculations. However, the shell-and-tube target area of $43.5 \mathrm{~m}^{2}$ is significantly higher than the value of $35.46 \mathrm{~m}^{2}$ calculated by hand. HX-Net clearly overestimates this target because the optimal network generated by HEXTRAN in Example 8.2 has an area of $40.85 \mathrm{~m}^{2}$, which is $6 \%$ below the HX-Net value. The "sufficient" designation for heating and cooling at the bottom of the targets form indicates that the temperature driving force between the utility streams and process streams is greater than or equal to the specified value of $\Delta T_{\text {min }}$.

## Example 8.3: Targets Window in HX-Net



Super targeting is performed by clicking the Range Targets tab and entering the range of $\Delta T_{\min }$ values desired and the increment to be used. The results shown in the graph below were obtained with an increment of $1.0^{\circ} \mathrm{C}$. From the graph, the optimum value of $\Delta T_{\min }$ for this problem is approximately $24.5^{\circ} \mathrm{C}$.

Various types of composite curve and driving force plots are available under the Plots/Tables tab; several of these are shown below. By right-clicking on the plot area, the user can change the title, axis labels, and format of each graph as desired. Graphs can be printed on a stand-alone basis or included in a report generated by HX-Net, the contents of which are selected by the user.

## Example 8.3: Super Targeting Results from HX-Net

## Super Targeting



Example 8.3: Targeting Graphs Generated by HX-Net

## Balanced Composite Curves



## Example 8.3: Targeting Graphs Generated by HX-Net (continued)

## Grand Composite Curve



Driving Force Plot - Cold


## References

1. Linnhoff, B. and E. Hindmarsh, The pinch design method for heat exchanger networks, Chem. Eng. Sci., 38, 745-763, 1983.
2. Linnhoff, B. and J. R. Flower, Synthesis of heat exchanger networks, AIChE J., 24, 633-654, 1978.
3. Linnhoff, B., Use pinch analysis to knock down capital costs and emissions, Chem. Eng. Prog., 18, No. 8, 32-57, 1994.
4. Linnhoff, B., Pinch analysis - a state-of-the-art overview, Trans. IChemE, 71 (Part A), 503-522, 1993.
5. Linnhoff, B. and S. Ahmad, Cost optimum heat exchanger networks. 1. Minimum energy and capital using simple models for capital cost, Comp. Chem. Eng., 14, 729-750, 1990.
6. Ahmad, S., B. Linnhoff and R. Smith, Cost optimum heat exchanger networks. 2. Targets and design for detailed capital cost models, Comp. Chem. Eng., 14, 751-767, 1990.
7. Trivedi, K. K., J. R. Roach and B. K. O'Neill, Shell targeting in heat exchanger networks, AIChE J., 33, 2087-2090, 1987.
8. Ahmad, S., B. Linnhoff and R. Smith, Design of multipass heat exchangers: an alternative approach, J. Heat Transfer, 110, 304-309, 1988.
9. Taborek, J., Mean temperature difference, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
10. Ahmad, S. and R. Smith, Targets and design for minimum number of shells in heat exchanger networks, Chem. Eng. Res. Des., 67, 481-494, 1989.
11. Bell, K. J., Approximate sizing of shell-and-tube heat exchangers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
12. Hall, S. G., S. Ahmad and R. Smith, Capital cost targets for heat exchanger networks comprising mixed materials of construction, pressure ratings and exchanger types, Comp. Chem. Eng., 14, 319-335, 1990.
13. Polley, G. T., M. H. Panjeh Shaki and F. O. Jegede, Pressure drop considerations in the retrofit of heat exchanger networks, Trans. IChemE, 68 (Part A), 211-220, 1990.
14. Jegede, F. O. and G. T. Polley, Optimum heat exchanger design, Trans. IChemE, 70 (Part A), 133-141, 1992.
15. Zhu, X. X. and X. R. Nie, Pressure drop considerations for heat exchanger network grassroots design, Comp. Chem. Eng., 26, 1661-1676, 2002.
16. Biegler, L. T., I. E. Grossman and A. W. Westerberg, Systematic Methods of Chemical Process Design, Prentice Hall, Upper Saddle River, NJ, 1997.
17. Cerda, J., A. W. Westerberg, D. Mason and B. Linnhoff, Minimum utility usage in heat exchanger network synthesis - a transportation problem, Chem. Eng. Sci., 38, 373-387, 1983.
18. Floudas, C. A., A. R. Ciric and I. E. Grossman, Automatic synthesis of optimum heat exchanger network configurations, AIChE J., 32, 276-290, 1986.
19. Yee, T. F., I. E. Grossman and Z. Kravanja, Simultaneous optimization models for heat integration. I. Area and energy targeting and modeling of multistream exchangers, Comp. Chem. Eng., 14, 1151-1164, 1990.
20. Yee, T. F. and I. E. Grossman, Simultaneous optimization models for heat integration. II. Heat exchanger network synthesis, Comp. Chem. Eng., 14, 1165-1184, 1990.
21. Challand, T. B., R. W. Colbert and C. K. Venkatesh, Computerized heat exchanger networks, Chem. Eng. Prog., 5, No. 7, 65-71, 1981.
22. Jones, D. A., N. Y. Asuman and B. E. Tilton, Synthesis techniques for retrofitting heat recovery systems, Chem. Eng. Prog., 10, No. 7, 28-33, 1986.
23. Shethna, H.A., J. M. Jezowski and F.J.L. Castillo, A new methodology for simultaneous optimization of capital and operating cost targets in heat exchanger network design, App. Thermal Eng., 20, 1577-1587, 2000.

## Notations

| $A$ | Heat-transfer surface area |
| :--- | :--- |
| $A_{\text {min }}$ | Target for minimum heat-transfer area in a heat exchanger network <br> $a$ |
| $b$ | Constant in capital cost equation for heat exchangers, Equation (8.20) |
| $b$ | Constant in capital cost equation for heat exchangers, Equation (8.20) |
| $C_{P}$ | Heat capacity at constant pressure |
| $C P$ | $\dot{m} C_{P}=$ Heat capacity flow rate |
| $C P_{j}$ | $C P$ for stream $j$ |
| $C P C$ | $C P$ for cold stream |
| $C P H$ | $C P$ for hot stream |
| $c$ | Constant in capital cost equation for heat exchangers, Equation (8.20) |
| $E M A T$ | Minimum temperature approach for an individual heat exchanger in a network |
| $F$ | LMTD correction factor |
| $F_{i}$ | LMTD correction factor for enthalpy interval $i$ |
| $f$ | Objective function for linear program |
| $H$ | Stream enthalpy per unit time |


| $H R A T$ | Temperature approach for heat recovery |
| :--- | :--- |
| $h$ | Heat-transfer coefficient with fouling allowance included |
| $h_{j}$ | Heat-transfer coefficient, including fouling allowance, for stream $j$ |
| $\dot{m}$ | Mass flow rate |
| $N$ | Number of process streams and utilities in a network |
| $N_{s}$ | Number of E shells connected in series |
| $N C$ | Number of cold streams or branches at the pinch |
| $N H$ | Number of hot streams or branches at the pinch |
| $P$ | Parameter used to calculate LMTD correction factor |
| $P_{\text {max }}$ | Maximum value of $P$ for a given value of $R$ |
| $q_{j}$ | Heat flow leaving $j$ th subnetwork |
| $Q_{o}$ | Amount of hot utility supplied to first subnetwork |
| $q$ | Rate of heat transfer |
| $q_{j}$ | Rate of heat transfer in enthalpy interval $j$ |
| $R$ | Parameter used to calculate LMTD correction factor |
| $S$ | Parameter used in calculating LMTD correction factor |
| $T$ | Temperature |
| $T S$ | Supply temperature |
| $T T$ | Target temperature |
| $U_{D}$ | Design overall heat-transfer coefficient |
| $U_{\text {min }}$ | Minimum number of units required in a heat exchanger network |
| $W$ | Parameter defined by Equation (8.13) |
| $X_{P}$ | $P / P_{\text {max }}$ |

## Greek Letters

$\alpha \quad$ Parameter used in calculating LMTD correction factor
$\Delta H \quad$ Enthalpy difference (per unit time)
$\Delta T \quad$ Temperature difference
$\Delta T_{\ln } \quad$ Logarithmic mean temperature difference
$\left(\Delta T_{\text {ln }}\right)_{c f}$ LMTD for counter-current flow
$\Delta T_{\text {min }} \quad$ Minimum temperature approach

## Problems

| Stream | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | $h\left(\mathrm{~kW} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |
| :--- | :---: | :--- | :--- | :--- |
| 1 | 220 | 150 | 2.0 | 1.1 |
| 2 | 240 | 60 | 3.0 | 0.6 |
| 3 | 50 | 190 | 2.5 | 0.8 |
| 4 | 100 | 210 | 4.0 | 1.0 |
| HU | 250 | 250 | - | 2.0 |
| CU | 20 | 25 | - | 1.5 |

A HEN will involve the four process streams and two utilities shown above. A minimum approach of $10^{\circ} \mathrm{C}$ will be used for design purposes. Set up the problem table for the network and use it to determine:
(a) The minimum hot and cold utility requirements.
(b) The hot and cold stream temperatures at the pinch.

Ans. (a) 135 kW (hot), 25 kW (cold). (b) $110^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$.
(8.2) For the system of Problem 8.1:
(a) Construct the hot and cold composite curves.
(b) From the graph, determine the value of $\Delta T_{\min }$ that results in the maximum possible heat recovery, and the value (in kW ) of the maximum possible heat recovery.
(c) What is the largest value of $\Delta T_{\min }$ that can be specified for this system? (Remember to account for the utility temperatures.)

Ans. (b) $1.67^{\circ} \mathrm{C}, 680 \mathrm{~kW}$. (c) $40^{\circ} \mathrm{C}$.
(8.3) For the system of Problem 8.1, use the Pinch Design method to develop a minimum-utility design for:
(a) The hot end problem.
(b) The cold end problem.
(c) The complete network.
(8.4) (a) For the HEN designed in Problem 8.3, what is the largest temperature cross in the network?
(b) If the exchanger having the largest temperature cross is a shell-and-tube unit, how many shells will it require?

Ans. (a) $87.5^{\circ} \mathrm{C}$. (b) 6 .
(8.5) For the system of Problem 8.1, the given heat-transfer coefficients include fouling allowances. Use the given data to solve the following problems.
(a) For the enthalpy interval from 680 to 735 kW , the temperature ranges for the hot and cold composite curves are:
Hot: $250^{\circ} \mathrm{C}$
Cold: $181.54-190^{\circ} \mathrm{C}$
Calculate the counter-flow area target for this interval.
(b) Repeat the calculation of part (a) for each of the remaining enthalpy intervals and determine the counter-flow area target for the entire network.

Ans. (a) $1.37 \mathrm{~m}^{2}$.
(8.6) Use the analytical method to calculate the number-of-shells target for the system of Problem 8.1.
(8.7) Use HX-Net or other available software to perform targeting calculations for the system of Problem 8.1. Since the software will not accept an isothermal utility stream, use a value of $249^{\circ} \mathrm{C}$ for the target temperature of the hot utility. Compare the results with those obtained by hand in Problems 8.1, 8.2, 8.5, and 8.6.
(8.8) Use HEXTRAN or other suitable software to synthesize one or more HENs for the system of Problem 8.1. Since the software will not accept an isothermal utility stream, use a value of $249^{\circ} \mathrm{C}$ for the target temperature of the hot utility. Display each network that you obtain on a grid diagram and compare each of the following parameters with the corresponding target value found in Problem 8.7:

- Number of units
- Number of shells
- Hot and cold utility usage
- Counter-flow area for the network
- Multi-pass area for the network

| Stream | $T S\left({ }^{\circ} \mathrm{F}\right)$ | $T T\left({ }^{\circ} \mathrm{F}\right)$ | $C P\left(\mathrm{Btu} / \mathrm{h} \cdot{ }^{\circ} \mathrm{F}\right)$ | $h\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :--- | ---: | :--- | :--- | :--- |
| 1 | 250 | 120 | 10,000 | 120 |
| 2 | 200 | 100 | 40,000 | 150 |
| 3 | 90 | 150 | 30,000 | 100 |
| 4 | 130 | 190 | 60,000 | 125 |
| HU | 300 | 299 | - | 750 |
| CU | 70 | 85 | - | 200 |

A HEN will involve the four process streams and two utilities shown above. A minimum approach of $10^{\circ} \mathrm{F}$ will be used for design purposes. Set up the problem table for the network and use it to determine:
(a) The minimum hot and cold utility requirements.
(b) The hot and cold stream temperatures at the pinch.

Ans. (a) $700,000 \mathrm{Btu} / \mathrm{h}$ (hot); $600,000 \mathrm{Btu} / \mathrm{h}$ (cold). (b) $140^{\circ} \mathrm{F}$ and $130^{\circ} \mathrm{F}$.
(8.10) For the system of Problem 8.9:
(a) Construct the hot and cold composite curves.
(b) From the graph determine the value of $\Delta T_{\min }$ that results in the maximum possible heat recovery, and the value of the maximum possible heat recovery.
(c) What is the largest value of $\Delta T_{\text {min }}$ that can be specified for this system? What are the minimum hot and cold utility requirements and maximum energy recovery corresponding to this value of $\Delta T_{\text {min }}$ ? (Remember to account for the utility temperatures.)
Ans. (b) $0^{\circ} \mathrm{F}, 5.2 \times 10^{6} \mathrm{Btu} / \mathrm{h}$.
(c) $30^{\circ} \mathrm{F}, 1.7 \times 10^{6} \mathrm{Btu} / \mathrm{h}(\mathrm{hot}), 1.6 \times 10^{6} \mathrm{Btu} / \mathrm{h}$ (cold), $3.7 \times 10^{6} \mathrm{Btu} / \mathrm{h}$ (MER).
(8.11) For the system of Problem 8.9, do the following:
(a) Set up the $C P$ table for the hot end problem and use it to identify the feasible pinch matches. Then develop a minimum-utility design for the hot end problem.
(b) Repeat part (a) for the cold end problem.
(c) Combine the hot and cold end designs from parts (a) and (b) to obtain a minimum-utility design for the complete network.
(d) Determine the number of heat load loops that exist in the network. Then identify the loops on your grid diagram.
(e) Simplify the network of part (c) by eliminating the unit with the smallest duty using heat load loops and paths. For consistency, any unit whose duty falls below that of the unit eliminated should also be eliminated.
(8.12) For the final network obtained in Problem 8.11(e), assume that all units are multi-pass shell-and-tube exchangers. How many type E shells will be required to realize this network?
(8.13) For the system of Problem 8.9, the given heat-transfer coefficients include fouling allowances. Use the given data to calculate the minimum counter-flow area target for the network.
Ans. $4,000 \mathrm{ft}^{2}$.
(8.14) Use the analytical method to calculate the number-of-shells target for the system of Problem 8.9.

Ans. 13.
(8.15) Use HX-Net or other available software to perform targeting calculations for the system of Problem 8.9. Compare the results with those obtained by hand in Problems 8.9, 8.10, 8.13, and 8.14.
(8.16) Use HEXTRAN or other suitable software to synthesize one or more HENs for the system of Problem 8.9. Display each network that you obtain on a grid diagram and compare each of the following parameters with the corresponding target value found in Problem 8.15.

- Number of units
- Number of shells
- Hot and cold utility usage
- Counter-flow area for the network
- Multi-pass area for the network

| Stream | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | Duty $(\mathrm{kW})$ |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 280 | 60 | 3.0 | 660 |
| 2 | 180 | 20 | 4.5 | 720 |
| 3 | 20 | 160 | 4.0 | 560 |
| 4 | 120 | 260 | 6.0 | 840 |
| HU | 300 | 299 | - | - |
| CU | -20 | -15 | - | - |

A HEN will involve the four process streams and two utilities shown above. A minimum approach of $30^{\circ} \mathrm{C}$ will be used for design purposes. Set up the problem table for the network and use it to determine the hot and cold stream temperatures at the pinch and the minimumutility targets for the system.

Ans. $150^{\circ} \mathrm{C}, 120^{\circ} \mathrm{C}, 475 \mathrm{~kW}$ (hot), 455 kW (cold).
(8.18) Construct the hot and cold composite curves for the system of Problem 8.17. Then use the composite curves to determine the following to within graphical accuracy.
(a) The range of values that can be specified for $\Delta T_{\min }$ in this system.
(b) The maximum amount of heat exchange ( kW ) between hot and cold streams that is theoretically possible.
(c) The minimum cold utility $(\mathrm{kW})$ required for $\Delta T_{\min }=20^{\circ} \mathrm{C}$.
(d) The maximum amount of heat exchange ( kW ) that is possible for $\Delta T_{\min }=20^{\circ} \mathrm{C}$.
(e) The hot stream pinch temperature corresponding to a minimum hot utility requirement of 620 kW .
Ans. (a) $0-260^{\circ} \mathrm{C}$.
(b) 1150 kW .
(c) 380 kW .
(d) 1000 kW .
(e) $169^{\circ} \mathrm{C}$.
(8.19) (a) Use the Pinch Design method to find a minimum-utility design for the system of Problem 8.17.
(b) Modify the network obtained in part (a) by using a heat load path to eliminate the temperature cross on one of the heat exchangers.

| Stream | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | $h\left(\mathrm{~kW} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |
| :--- | :---: | :---: | :--- | :--- |
| 1 | 180 | 40 | 2.0 | 0.9 |
| 2 | 150 | 40 | 4.0 | 1.2 |
| 3 | 60 | 180 | 3.0 | 1.0 |
| 4 | 30 | 105 | 2.6 | 0.7 |
| HU | 220 | 219 | - | 2.5 |
| CU | 0 | 15 | - | 1.6 |

A HEN will involve the four process streams and two utilities shown above. A minimum approach of $20^{\circ} \mathrm{C}$ will be used for design purposes. Set up the problem table for the network and use it to determine the pinch temperatures and minimum-utility targets.

Ans. $150^{\circ} \mathrm{C}, 130^{\circ} \mathrm{C}, 90 \mathrm{~kW}$ (hot), 255 kW (cold).
(8.21) For the system of Problem 8.20, construct the hot and cold composite curves. Then use the composite curves to determine the following:
(a) The smallest value of $\Delta T_{\text {min }}$ that can be specified and the maximum amount of heat recovery corresponding to this value of $\Delta T_{\text {min }}$.
(b) The largest value of $\Delta T_{\min }$ that can be specified and the maximum amount of heat recovery corresponding to this value of $\Delta T_{\min }$. (Remember to account for the utility temperatures.)
(c) The minimum-utility requirements for $\Delta T_{\min }=10^{\circ} \mathrm{C}$.

Ans. (a) $0^{\circ} \mathrm{C}, 525 \mathrm{~kW}$. (b) $40^{\circ} \mathrm{C}, 405 \mathrm{~kW}$.
(8.22) (a) Use the Pinch Design method to develop a minimum-utility design for the system of Problem 8.20.
(b) Simplify the network obtained in part (a) as appropriate using heat load loops and paths.
(8.23) For the final network obtained in Problem 8.22(b):
(a) Assuming all units are counter-flow exchangers, use the heat-transfer coefficients given in Problem 8.20 to calculate the total heat-transfer area in the network.
(b) If all units are multi-pass shell-and-tube exchangers, how many type E shells will be required to realize the network?
(8.24) (a) For the system of Problem 8.20, construct the balanced composite curves for $\Delta T_{\text {min }}=20^{\circ}$.
(b) Delineate the enthalpy intervals for the system.
(c) Use the heat-transfer coefficients given in Problem 8.20 to calculate the counter-flow area target for the network.
(d) Use the graphical method to calculate the minimum-number-of-shells target for the network.
(8.25) Use HX-Net or other available software to perform targeting calculations for the system of Problem 8.20. Compare the results with those obtained by hand in Problems 8.20, 8.21, and 8.24.
(8.26) Use HEXTRAN or other suitable software to synthesize one or more HENs for the system of Problem 8.20. Display each network obtained on a grid diagram and compare the network parameters with the targets calculated in Problem 8.25.

| Stream | $T S\left({ }^{\circ} \mathrm{F}\right)$ | $T T\left({ }^{\circ} \mathrm{F}\right)$ | $C P\left(\mathrm{Btu} / \mathrm{h} \cdot{ }^{\circ} \mathrm{F}\right)$ | $h\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :--- | :---: | :--- | :--- | :--- |
| 1 | 260 | 160 | 30,000 | 350 |
| 2 | 250 | 130 | 15,000 | 250 |
| 3 | 180 | 240 | 40,000 | 300 |
| 4 | 120 | 235 | 20,000 | 320 |
| HU | 290 | 289 | - | 800 |
| CU | 60 | 75 | - | 400 |

A HEN will involve the four process streams and two utilities shown above. A minimum approach of $10^{\circ} \mathrm{F}$ will be used for design purposes. Set up the problem table and use it to determine the pinch temperatures and minimum-utility targets for the network.
Ans. $190^{\circ} \mathrm{F}, 180^{\circ} \mathrm{F} ; 500,000 \mathrm{Btu} / \mathrm{h}$ (hot); $600,000 \mathrm{Btu} / \mathrm{h}$ (cold).
(8.28) Construct the hot and cold composite curves for the system of Problem 8.27. Use the composite curves to determine:
(a) The smallest value of $\Delta T_{\min }$ that can be specified and the maximum amount of heat recovery corresponding to this value of $\Delta T_{\text {min }}$.
(b) The largest value of $\Delta T_{\text {min }}$ that can be specified and the maximum amount of heat recovery corresponding to this value of $\Delta T_{\text {min }}$. (Remember to consider utility temperatures.)
(c) The minimum-utility requirements for $\Delta T_{\min }=20^{\circ} \mathrm{F}$.
Ans. (a) $0^{\circ} \mathrm{F}, 4.64 \times 10^{6} \mathrm{Btu} / \mathrm{h}$.
(b) $50^{\circ} \mathrm{F}, 3.04 \times 10^{6} \mathrm{Btu} / \mathrm{h}$.
(c) $950,000 \mathrm{Btu} / \mathrm{h}$ (hot), $1.05 \times 10^{6} \mathrm{Btu} / \mathrm{h}$ (cold).
(8.29) (a) Use the Pinch Design method to develop a minimum-utility design for the system of Problem 8.27.
(b) Simplify the network obtained in part (a) as appropriate using heat load loops and paths.
(8.30) For the final network obtained in Problem 8.29 (b):
(a) Assuming all units are counter-flow exchangers, use the heat-transfer coefficients given in Problem 8.27 to calculate the total heat-transfer area in the network.
(b) If all units are multi-pass shell-and-tube exchangers, how many type E shells will be required to realize the network?
(8.31) (a) For the system of Problem 8.27, construct the balanced composite curves for $\Delta T_{\min }=10^{\circ} \mathrm{F}$.
(b) Delineate the enthalpy intervals for the system.
(c) Use the heat-transfer coefficients given in Problem 8.27 to calculate the counter-flow area target for the network.
(d) Use the graphical method to calculate the minimum-number-of-shells target for the network.
(8.32) Use HX-Net or other available software to perform targeting calculations for the system of Problem 8.27. Compare the results with those obtained by hand in Problems 8.27, 8.28, and 8.31.
(8.33) Use HEXTRAN or other suitable software to synthesize one or more HENs for the system of Problem 8.27. Display each network obtained on a grid diagram and compare the network parameters with the targets calculated in Problem 8.32.

(8.34) |  | Stream | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | $h\left(\mathrm{~kW} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |
| :--- | :--- | ---: | :--- | :--- | :--- |
|  | 1 | 250 | 120 | 16.5 | 0.8 |
| 2 | 205 | 65 | 13.5 | 0.6 |  |
| 3 | 40 | 205 | 11.5 | 1.1 |  |
| 4 | 65 | 180 | 13.0 | 0.9 |  |
|  | 5205 | 13.0 | 0.7 |  |  |
|  | 95 | 2059 | - | 3.0 |  |
|  | HU | 280 | 279 | - | 1.2 |
|  | CU | 25 | 30 | - |  |

A HEN will involve the five process streams and two utilities shown above.
(a) Set up the problem table for $\Delta T_{\text {min }}=10^{\circ} \mathrm{C}$ and use it to determine the minimum-utility targets for the network.
(b) Calculate the minimum-number-of-units target for the network.
(c) Construct the hot and cold composite curves for the system and use them to determine the smallest value of $\Delta T_{\min }$ for which a pinch exists, i.e., find $\Delta T_{\text {threshold }}$.
(d) Set up the problem table for $\Delta T_{\min }=30^{\circ} \mathrm{C}$ and use it to find the pinch temperatures and minimum-utility targets.
Ans. (a) 787.5 kW (hot), 0 kW (cold).
(b) 6 .
(c) $21.3^{\circ} \mathrm{C}$
(d) $95^{\circ} \mathrm{C}, 65^{\circ} \mathrm{C}, 905 \mathrm{~kW}$ (hot), 117.5 kW (cold).
(8.35) Use HX-Net or other available software to perform targeting calculations for the system of Problem 8.34 and verify the results obtained by hand in the latter.
(8.36) For the system of Problem 8.34 with $\Delta T_{\min }=30^{\circ} \mathrm{C}$, use HEXTRAN or other suitable software to synthesize one or more HENs. Display the results on a grid diagram and compare the network parameters with the targets calculated in Problem 8.32.
(8.37) Repeat Example 8.3 for the case in which there is a second hot utility having the following properties:

$$
\begin{aligned}
T S & =110^{\circ} \mathrm{C} \\
T T & =109.5^{\circ} \mathrm{C} \\
\text { Cost } & =\$ 50 / \mathrm{kW} \cdot \text { year } \\
h & =2.0 \mathrm{~kW} / \mathrm{m}^{2} \cdot \mathrm{~K} \text { (fouling included) }
\end{aligned}
$$

All other data are the same as in Example 8.3. Use HX-Net to determine the following:

- Pinch temperatures.
- Minimum requirements for each of the three utilities.
- Minimum number of units.
- Minimum number of shells.
- Counter-flow area target.
- Multi-pass area target.
- Optimum value of $\Delta T_{\text {min }}$ (super targeting).
- A graph of the balanced composite curves.
(8.38) For example problem TC3 discussed in the text, do the following:
(a) Combine the hot B and cold A designs given in the text to obtain a minimum-utility design for the network. Identify the heat load loops on the grid diagram.
(b) Simplify the network from part (a) using heat load loops and paths.
(c) Compare the parameters for the final network from part (b) with those for TC3 calculated in the text.
(d) Consider the case in which there is a second hot utility available at $110^{\circ} \mathrm{C}$. Assume that the temperature change for this utility is negligible and that it is the less expensive of the two hot utilities. Set up the problem table for this case and use it to determine pinch temperatures and minimum requirements for each of the three utilities.

| Stream | $T S\left({ }^{\circ} \mathrm{F}\right)$ | $T T\left({ }^{\circ} \mathrm{F}\right)$ | $C P\left(\mathrm{Btu} / \mathrm{h} \cdot{ }^{\circ} \mathrm{F}\right)$ | $h\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 590 | 400 | 23,760 | 320 |
| 2 | 471 | 200 | 15,770 | 260 |
| 3 | 533 | 150 | 13,200 | 190 |
| 4 | 200 | 400 | 16,000 | 230 |
| 5 | 100 | 430 | 16,000 | 150 |
| 6 | 300 | 400 | 41,280 | 280 |
| 7 | 150 | 280 | 26,240 | 250 |
| HU | 500 | 499 | - | 1000 |
| CU | 75 | 115 | - | 450 |

A HEN will involve the seven process streams and two utilities shown above. The given heat-transfer coefficients include appropriate fouling allowances. A minimum approach of $20^{\circ} \mathrm{F}$ will be used for design purposes. Use HX-Net or other available software to perform targeting calculations for this system.
(8.40) Use HEXTRAN or other suitable software to synthesize a HEN for the system of Problem 8.39. Display the resulting network on a grid diagram and compare the network parameters with the target values found in Problem 8.39.

| Stream | $T S\left({ }^{\circ} \mathrm{C}\right)$ | $T T\left({ }^{\circ} \mathrm{C}\right)$ | $C P\left(\mathrm{~kW} /{ }^{\circ} \mathrm{C}\right)$ | $h\left(\mathrm{~kW} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |
| :--- | :--- | ---: | :--- | :--- |
| 1 | 327 | 40 | 100 | 1.6 |
| 2 | 220 | 160 | 160 | 0.7 |
| 3 | 220 | 60 | 60 | 1.2 |
| 4 | 160 | 45 | 400 | 1.0 |
| 5 | 100 | 300 | 100 | 0.8 |
| 6 | 35 | 164 | 70 | 0.6 |
| 7 | 85 | 138 | 350 | 1.5 |
| 8 | 60 | 170 | 60 | 1.0 |
| 9 | 140 | 300 | 200 | 0.9 |
| HU1 | 350 | 349 | - | 4.3 |
| HU2 | 210 | 209 | - | 4.3 |
| CU1 | -5 | 10 | - | 2.2 |
| CU2 | 25 | 40 | - | 2.2 |

A HEN will involve the nine process streams and four utilities shown above. The given heattransfer coefficients include appropriate fouling allowances. A minimum approach of $20^{\circ} \mathrm{C}$ will be used for design purposes. Use HX-Net or other available software to perform targeting calculations for this system.

This page intentionally left blank

## BOILING HEAT TRANSFER

Contents
9.1 Introduction ..... 386
9.2 Pool Boiling ..... 386
9.3 Correlations for Nucleate Boiling on Horizontal Tubes ..... 387
9.4 Two-Phase Flow ..... 402
9.5 Convective Boiling in Tubes ..... 416
9.6 Film Boiling ..... 428

### 9.1 Introduction

In reboilers and vaporizers, boiling usually takes place either on the exterior surface of submerged tubes or on the interior surface as the fluid flows through the tubes. In the former case the tubes are oriented horizontally, while in the latter they may be either horizontal or vertical, but the most common configuration is vertical with the fluid flowing upward through the tubes. In both situations, the rate of heat transfer is normally much higher than in ordinary forced convection, and different correlations are required to predict heat-transfer coefficients in boiling systems.

A boiling fluid consists of a two-phase mixture of vapor and liquid. When such a fluid flows through a tube, a number of distinct flow regimes can occur depending on the flow rate and the relative amounts of vapor and liquid present. Two-phase flow is thus more complex than singlephase flow, and special methods are needed to calculate the pressure drop in equipment handling boiling fluids.

Correlations used in the thermal and hydraulic analysis of reboilers and vaporizers are presented in this chapter. Equipment design is covered in Chapter 10.

### 9.2 Pool Boiling

Pool boiling refers to vaporization that takes place at a solid surface submerged in a quiescent liquid. When the temperature, $T_{s}$, of the solid surface exceeds the saturation temperature, $T_{s a t}$, of the liquid, vapor bubbles form at nucleation sites on the surface, grow and subsequently detach from the surface. The driving force for heat transfer is $\Delta T_{e}=T_{s}-T_{\text {sat }}$, called the excess temperature. Liquid circulation in pool boiling occurs by natural convection and by the agitation resulting from bubble growth and detachment.

The boiling curve is a plot of surface heat flux versus excess temperature, and has the general features illustrated in Figure 9.1. Point A on the curve marks the onset of nucleate boiling (ONB). At lower excess temperatures, heat transfer occurs by natural convection alone. Nucleate boiling exists between points A and C on the curve. Two different boiling regimes can be distinguished in this region. Between points $A$ and $B$, the boiling is characterized by the formation of isolated vapor bubbles at nucleation sites dispersed on the solid surface. Bubble growth and detachment result in significant fluid mixing near the solid surface that greatly increases the rate of heat transfer. In this regime, heat is transferred primarily from the solid surface directly to the liquid flowing across the surface.

As the heat flux increases beyond point B , the number of active nucleation sites and the rate of vapor formation become so great that bubble interference and coalescence occur. The vapor leaves the solid surface in jets or columns that subsequently merge and form large slugs of vapor. The high rate of vapor formation begins to inhibit the flow of liquid across the solid surface, causing the slope of the boiling curve to decrease. An inflection point occurs at point P; here, the heat-transfer coefficient reaches a maximum. The heat flux continues to increase between points P and C since the increase in temperature driving force more than compensates for the decreasing heat-transfer coefficient.

The heat flux attains a maximum, called the critical heat flux, at point C. At this point, the rate of vapor formation is so great that some parts of the surface are covered by a continuous vapor film. Since heat-transfer rates for gases are generally much lower than for liquids, the overall rate of heat transfer begins to decrease. Although the vapor film tends to be unstable, breaking up and reforming at any given point, the fraction of the solid surface covered by vapor continues to increase from point C to point D . This region, in which the heat flux decreases as $\Delta T_{e}$ increases, is referred to as the transition region.

The heat flux reaches a minimum at point D , the so-called Liedenfrost point, where the entire solid surface is covered by a vapor blanket. Beyond this point, heat is transferred from the solid surface across the vapor film to the liquid. Hence, this regime is called film boiling. As indicated


Figure 9.1 Pool boiling curve for water at one atmosphere pressure. (Source: Ref. [1].)
in Figure 9.1, very high surface temperatures may be reached in film boiling, and consequently radiative heat transfer can be significant in this regime.

Most reboilers and vaporizers are designed to operate in the nucleate boiling regime. Although film boiling is sometimes employed, the much higher temperature driving force (corresponding to a much lower heat-transfer coefficient) in this regime generally makes it unattractive compared with nucleate boiling. The transition region, with its unusual characteristic of decreasing heat flux with increasing driving force, is always avoided in equipment design.

### 9.3 Correlations for Nucleate Boiling on Horizontal Tubes

Kettle, internal and horizontal thermosyphon reboilers (see Section 10.2) all involve boiling on the external surfaces of tubes configured in horizontal bundles. Correlations for the heat-transfer coefficient and critical heat flux in this geometry are presented in the following subsections.

### 9.3.1 Heat-transfer coefficients for pure component nucleate boiling on a single tube

Nucleate pool boiling has been widely studied and many heat-transfer correlations have been proposed for this regime. The presentation here is limited to several methods that have been among the most widely used.

## The Forster-Zuber correlation

Published in 1955, the Forster-Zuber correlation is the oldest of the methods presented here. It is usually stated in the following form [2,3]:

$$
\begin{equation*}
h_{n b}=0.00122 \frac{k_{L}^{0.79} C_{P, L}^{0.45} \rho_{L}^{0.49} g_{c}^{0.25} \Delta T_{e}^{0.24} \Delta P_{s a t}^{0.75}}{\sigma^{0.5} \mu_{L}^{0.29} \lambda^{0.24} \rho_{V}^{0.24}} \tag{9.1}
\end{equation*}
$$

where
$h_{n b}=$ nucleate boiling heat-transfer coefficient, $\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\left(\mathrm{W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$
$k_{L}=$ liquid thermal conductivity, $\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}(\mathrm{W} / \mathrm{m} \cdot K)$
$C_{P, L}=$ liquid heat capacity, Btu/lbm $\cdot{ }^{\circ} \mathrm{F}(\mathrm{J} / \mathrm{kg} \cdot \mathrm{K})$
$\rho_{L}=$ liquid density, $\mathrm{lbm} / \mathrm{ft}^{3}\left(\mathrm{~kg} / \mathrm{m}^{3}\right)$
$\mu_{L}=$ liquid viscosity, $\mathrm{lbm} / \mathrm{ft} \cdot \mathrm{h}(\mathrm{kg} / \mathrm{m} \cdot \mathrm{s})$
$\sigma=$ surface tension, $\mathrm{lbf} / \mathrm{ft}(\mathrm{N} / \mathrm{m})$
$\rho_{V}=$ vapor density, $\mathrm{lbm} / \mathrm{ft}^{3}\left(\mathrm{~kg} / \mathrm{m}^{3}\right)$
$\lambda=$ latent heat of vaporization, Btu/lbm (J/kg)
$g_{c}=$ unit conversion factor $=4.17 \times 10^{8} \mathrm{lbm} \cdot \mathrm{ft} / \mathrm{lbf} \cdot \mathrm{h}^{2}\left(1.0 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{N} \cdot \mathrm{s}^{2}\right)$
$\Delta T_{e}=T_{w}-T_{\text {sat }},{ }^{\circ} \mathrm{F}(\mathrm{K})$
$T_{w}=$ tube-wall temperature, ${ }^{\circ} \mathrm{F}(\mathrm{K})$
$T_{s a t}=$ saturation temperature at system pressure, ${ }^{\circ} \mathrm{F}(\mathrm{K})$
$\Delta P_{s a t}=P_{s a t}\left(T_{w}\right)-P_{s a t}\left(T_{s a t}\right), 1 \mathrm{bf} / \mathrm{ft}^{2}(\mathrm{~Pa})$
$P_{s a t}(T)=$ vapor pressure of fluid at temperature $T, 1 \mathrm{bf} / \mathrm{ft}^{2}(\mathrm{~Pa})$
Any consistent set of units can be used with Equation (9.1), including the English and SI units shown above.

## The Mostinski correlation

The Mostinski correlation is based on the principle of corresponding states and can be expressed as follows:

$$
\begin{equation*}
h_{n b}=0.00622 P_{c}^{0.69} \hat{q}^{0.7} F_{P} \tag{9.2a}
\end{equation*}
$$

where
$h_{n b} \propto \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$
$P_{c}=$ fluid critical pressure, psia
$\hat{q}=$ heat flux, Btu $/ \mathrm{h} \cdot \mathrm{ft}^{2}$
$F_{P}=$ pressure correction factor, dimensionless
In terms of SI units, the above equation becomes [4]:

$$
\begin{equation*}
h_{n b}=0.00417 P_{c}^{0.69} \hat{q}^{0.7} F_{P} \tag{9.2b}
\end{equation*}
$$

where

$$
\begin{aligned}
h_{n b} & \propto \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} \\
P_{c} & \propto \mathrm{kPa} \\
\hat{q} & \propto \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

An alternative form of the Mostinski correlation that is explicit in the temperature difference can be obtained by making the substitution $\hat{q}=h_{n b} \Delta T_{e}$. The result corresponding to Equation (9.2a) is:

$$
\begin{equation*}
h_{n b}=4.33 \times 10^{-8} P_{c}^{2.3} \Delta T_{e}^{2.333} F_{P}^{3.333} \tag{9.3a}
\end{equation*}
$$

where

$$
\begin{aligned}
h_{n b} & \propto \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
P_{c} & \propto \mathrm{psia} \\
\Delta T_{e} & \propto{ }^{\circ} \mathrm{F}
\end{aligned}
$$

In terms of SI units, the result is:

$$
\begin{equation*}
h_{n b}=1.167 \times 10^{-8} P_{c}^{2.3} \Delta T_{e}^{2.333} F_{P}^{3.333} \tag{9.3b}
\end{equation*}
$$

where

$$
\begin{aligned}
h_{n b} & \propto \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} \\
P_{c} & \propto \mathrm{kPa} \\
\Delta T_{e} & \propto \mathrm{~K}
\end{aligned}
$$

The pressure correction factor given by Mostinski is:

$$
\begin{equation*}
F_{P}=1.8 P_{r}^{0.17}+4 P_{r}^{1.2}+10 P_{r}^{10} \tag{9.4}
\end{equation*}
$$

where
$P_{r}=P / P_{c}=$ reduced pressure
Various modifications of this relationship have been suggested by other workers, and Palen [4] recommends the following alternative expression for design purposes:

$$
\begin{equation*}
F_{P}=2.1 P_{r}^{0.27}+\left[9+\left(1-P_{r}^{2}\right)^{-1}\right] P_{r}^{2} \tag{9.5}
\end{equation*}
$$

## The Cooper correlation

Cooper [5] developed the following correlation, which is of the same general type as the Mostinski correlation:

$$
\begin{equation*}
h_{n b}=21 \hat{q}^{0.67} P_{r}^{0.12}\left(-\log _{10} P_{r}\right)^{-0.55} M^{-0.5} \tag{9.6a}
\end{equation*}
$$

where $M$ is the molecular weight of the fluid and the other terms and units are the same as in Equation (9.2a). In terms of SI units, as in Equation (9.2b), the corresponding equation is:

$$
\begin{equation*}
h_{n b}=55 \hat{q}^{0.67} P_{r}^{0.12}\left(-\log _{10} P_{r}\right)^{-0.55} M^{-0.5} \tag{9.6b}
\end{equation*}
$$

A surface roughness term in the exponent on $P_{r}$ has been omitted in Equation (9.6) because it is usually dropped in practice.

The Stephan-Abdelsalam correlation
Stephan and Abdelsalam [6] used regression analysis to correlate a large set of experimental data in terms of the following dimensionless groups of physical properties:

$$
\begin{align*}
& Z_{1}=\frac{\hat{q} d_{B}}{k_{L} T_{s a t}}  \tag{9.7}\\
& Z_{2}=\frac{\alpha_{L}^{2} \rho_{L}}{g_{c} \sigma d_{B}} \tag{9.8}
\end{align*}
$$

$$
\begin{align*}
Z_{3} & =\frac{g_{c} \lambda d_{B}^{2}}{\alpha_{L}^{2}}  \tag{9.9}\\
Z_{4} & =\rho_{V} / \rho_{L}  \tag{9.10}\\
Z_{5} & =\frac{\rho_{L}-\rho_{V}}{\rho_{L}} \tag{9.11}
\end{align*}
$$

where

$$
\begin{equation*}
d_{B}=0.0146 \theta_{c}\left[\frac{2 g_{c} \sigma}{g\left(\rho_{L}-\rho_{V}\right)}\right]^{0.5} \tag{9.12}
\end{equation*}
$$

$d_{B}=$ theoretical diameter of bubbles leaving surface, $\mathrm{ft}(\mathrm{m})$
$\theta_{c}=$ contact angle in degrees
$g=$ gravitational acceleration, $\mathrm{ft} / \mathrm{h}^{2}\left(\mathrm{~m} / \mathrm{s}^{2}\right)$
$g_{c}=4.17 \times 10^{8} \mathrm{lbm} \cdot \mathrm{ft} / \mathrm{lbf} \cdot \mathrm{h}^{2}=1.0 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{N} \cdot \mathrm{s}^{2}$
$\alpha_{L}=$ liquid thermal diffusivity, $\mathrm{ft}^{2} / \mathrm{s}\left(\mathrm{m}^{2} / \mathrm{s}\right)$
$\hat{q} \propto \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}\left(\mathrm{~W} / \mathrm{m}^{2}\right)$
$k_{L} \propto \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}(\mathrm{W} / \mathrm{m} \cdot \mathrm{K})$
$T_{s a t} \propto{ }^{\circ} \mathrm{R}(\mathrm{K})$
$\sigma \propto \mathrm{lbf} / \mathrm{ft}(\mathrm{N} / \mathrm{m})$
$\rho_{L}, \rho_{V} \propto \mathrm{lbm} / \mathrm{ft}^{3}\left(\mathrm{~kg} / \mathrm{m}^{3}\right)$
$\lambda \propto \mathrm{ft} \cdot \mathrm{lbf} / \mathrm{lbm}(\mathrm{J} / \mathrm{kg})$
Note that in this correlation the latent heat has units of $\mathrm{ft} \cdot \mathrm{lbf} / \mathrm{lbm}$ in the English system $(1 \mathrm{Btu}=778 \mathrm{ft} \cdot \mathrm{lbf})$. The heat-transfer coefficient is given by the following equation:

$$
\begin{equation*}
\frac{h_{n b} d_{B}}{k_{L}}=0.23 Z_{1}^{0.674} Z_{2}^{0.35} Z_{3}^{0.371} Z_{4}^{0.297} Z_{5}^{-1.73} \tag{9.13}
\end{equation*}
$$

Fluids in the database were classified in four groups, each with a characteristic contact angle, as shown in Table 9.1. Note that the group labels are somewhat misleading, as alcohols are included in the hydrocarbon group and some of the light hydrocarbons are in the refrigerant and cryogenic groups. A contact angle of $35^{\circ}$ can be assumed for organic compounds that do not fit in any of the listed groups.

Stephan and Abdelsalam [6] also gave separate correlations for each of the four fluid groups. These group-specific correlations provide somewhat better fits to the data within each group than does the general correlation, Equation (9.13).

The following example due to Hewitt et al. [2] illustrates the use of the above correlations.

Table 9.1 Fluid Groups and Contact Angles for Stephan-Abdelsalam Correlation

| Fluid group | Contact angle $\left(\theta_{c}\right)$ |
| :--- | :--- |
| Water | $45^{\circ}$ |
| Hydrocarbons (including alcohols) | $35^{\circ}$ |
| Refrigerants (including $\mathrm{CO}_{2}$, propane, $n$-butane) | $35^{\circ}$ |
| Cryogenic fluids (including methane, ethane) | $1^{\circ}$ |

## Example 9.1

Pure component nucleate boiling takes place on the surface of a 1-in. OD horizontal tube immersed in a saturated liquid organic compound. The tube-wall temperature is 453.7 K and the system pressure is 310.3 kPa . Fluid properties are given in the table below. Calculate the heat-transfer coefficient and wall heat flux using:
(a) The Forster-Zuber correlation.
(b) The Mostinski correlation.
(c) The Mostinski correlation with Palen's recommendation for $F_{P}$.
(d) The Cooper correlation.
(e) The Stephan-Abdelsalam correlation.

| Fluid property | Value |
| :--- | :--- |
| Vapor density $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$ | 18.09 |
| Liquid density $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$ | 567 |
| Liquid heat capacity $(\mathrm{J} / \mathrm{kg} \cdot \mathrm{K})$ | 2730 |
| Liquid viscosity $(\mathrm{kg} / \mathrm{m} \cdot \mathrm{s})$ | $156 \times 10^{-6}$ |
| Vapor viscosity $(\mathrm{kg} / \mathrm{m} \cdot \mathrm{s})$ | $7.11 \times 10^{-6}$ |
| Liquid thermal conductivity $(\mathrm{W} / \mathrm{m} \cdot \mathrm{K})$ | 0.086 |
| Surface tension $($ dyne $/ \mathrm{cm})$ | 8.2 |
| Latent heat of vaporization $(\mathrm{J} / \mathrm{kg})$ | 272,000 |
| Critical pressure $(\mathrm{kPa})$ | 2550 |
| Saturation temperature $(\mathrm{K})$ at 310.3 kPa | 437.5 |
| Vapor pressure $(\mathrm{kPa})$ at 453.7 K | 416.6 |
| Molecular weight | 110.37 |

## Solution

(a) For the Forster-Zuber correlation, first calculate $\Delta T_{e}$ and $\Delta P_{s a t}$.

$$
\begin{aligned}
\Delta T_{e} & =T_{w}-T_{\text {sat }}=453.7-437.5=16.2 \mathrm{~K} \\
\Delta P_{\text {sat }} & =P_{\text {sat }}\left(T_{w}\right)-P_{\text {sat }}\left(T_{\text {sat }}\right) \\
& =416.6-310.3 \\
\Delta P_{\text {sat }} & =106.3 \mathrm{kPa}=106,300 \mathrm{~Pa}
\end{aligned}
$$

All the physical properties appearing in the correlation are given in proper SI units except the surface tension, which is:

$$
\sigma=8.2 \text { dyne } / \mathrm{cm}=8.2 \times 10^{-3} \mathrm{~N} / \mathrm{m}
$$

Substituting the appropriate values into Equation (9.1) yields:

$$
\begin{aligned}
h_{n b} & =0.00122 \frac{k_{L}^{0.79} C_{P, L}^{0.45} \rho_{L}^{0.49} g_{c}^{0.25} \Delta T_{e}^{0.24} \Delta P_{s a t}^{0.75}}{\sigma^{0.5} \mu_{L}^{0.29} \lambda^{0.24} \rho_{V}^{0.24}} \\
& =\frac{0.00122(0.086)^{0.79}(2730)^{0.45}(567)^{0.49}(1.0)^{0.25}(16.2)^{0.24}(106,300)^{0.75}}{\left(8.2 \times 10^{-3}\right)^{0.5}\left(156 \times 10^{-6}\right)^{0.29}(272,000)^{0.24}(18.09)^{0.24}} \\
h_{n b} & =5512 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

The heat flux at the pipe wall is given by:

$$
\hat{q}=h_{n b} \Delta T_{e}=5512 \times 16.2=89,294 \cong 89,300 \mathrm{~W} / \mathrm{m}^{2}
$$

(b) For the Mostinski correlation, first calculate the pressure correction factor using Equation (9.4).

$$
\begin{aligned}
& P_{r}=P / P_{c}=\frac{310.3}{2550}=0.1217 \\
& F_{P}=1.8 P_{r}^{0.17}+4 P_{r}^{1.2}+10 P_{r}^{10} \\
& F_{P}=1.8(0.1217)^{0.17}+4(0.1217)^{1.2}+10(0.1217)^{10}=1.5777
\end{aligned}
$$

Since $\Delta T_{e}=16.2 \mathrm{~K}$ is known, use Equation (9.3b) to calculate the heat-transfer coefficient.

$$
\begin{aligned}
h_{n b} & =1.167 \times 10^{-8} P_{c}^{2.3} \Delta T_{e}^{2.333} F_{P}^{3.333} \\
& =1.167 \times 10^{-8}(2550)^{2.3}(16.2)^{2.333}(1.5777)^{3.333} \\
h_{n b} & =2421 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

The heat flux is calculated as before:

$$
\hat{q}=h_{n b} \Delta T_{e}=2421 \times 16.2=39,220 \mathrm{~W} / \mathrm{m}^{2}
$$

(c) The calculation is the same as in part (b) except that Equation (9.5) is used to calculate the pressure correction factor.

$$
\begin{aligned}
F_{P} & =2.1 P_{r}^{0.27}+\left[9+\left(1-P_{r}^{2}\right)^{-1}\right] P_{r}^{2} \\
& =2.1(0.1217)^{0.27}+\left\{9+\left[1-(0.1217)^{2}\right]^{-1}\right\}(0.1217)^{2} \\
F_{P} & =1.3375 \\
h_{n b} & =1.167 \times 10^{-8}(2550)^{2.3}(16.2)^{2.333}(1.3375)^{3.333} \\
h_{n b} & =1396 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} \\
\hat{q} & =h_{n b} \Delta T_{e}=1396 \times 16.2=22,615 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

(d) To use the Cooper correlation, substitute $\hat{q}=h_{n b} \Delta T_{e}$ in Equation (9.6b) to obtain:

$$
h_{n b}=55\left(h_{n b} \Delta T_{e}\right)^{0.67} P_{r}^{0.12}\left(-\log _{10} P_{r}\right)^{-0.55} M^{-0.15}
$$

Solving for $h_{n b}$ gives:

$$
\begin{aligned}
h_{n b} & =\left\{55 \Delta T_{e}^{0.67} P_{r}^{0.12}\left(-\log _{10} P_{r}\right)^{-0.55} M^{-0.15}\right\}^{3.03} \\
& =\left\{55(16.2)^{0.67}(0.1217)^{0.12}\left(-\log _{10} 0.1217\right)^{-0.55}(110.37)^{-0.5}\right\}^{3.03} \\
h_{n b} & =23,214 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

The heat flux is then:

$$
\hat{q}=h_{n b} \Delta T_{e}=23,214 \times 16.2 \cong 376,070 \mathrm{~W} / \mathrm{m}^{2}
$$

(e) For the Stephan-Abdelsalam correlation, the theoretical bubble diameter is calculated using Equation (9.12). A contact angle of $35^{\circ}$ is assumed for a non-cryogenic organic compound.

$$
\begin{aligned}
& d_{B}=0.0146 \theta_{c}\left[\frac{2 g_{c} \sigma}{g\left(\rho_{L}-\rho_{V}\right)}\right]^{0.5}=0.0146 \times 35\left[\frac{2 \times 1.0 \times 8.2 \times 10^{-3}}{9.81(567-18.09)}\right]^{0.5} \\
& d_{B}=8.918 \times 10^{-4} \mathrm{~m}
\end{aligned}
$$

The five dimensionless parameters are calculated using Equations (9.7)-(9.11). Since the heat flux is unknown, it is retained in $Z_{1}$.

$$
\begin{aligned}
& Z_{1}=\frac{\hat{q} d_{B}}{k_{L} T_{\text {sat }}}=\frac{\hat{q} \times 8.918 \times 10^{-4}}{0.086 \times 437.5}=2.370 \times 10^{-5} \hat{q} \\
& Z_{2}=\frac{\alpha_{L}^{2} \rho_{L}}{g_{c} \sigma d_{B}}=\frac{\left(5.556 \times 10^{-8}\right)^{2} \times 567}{1.0 \times 8.2 \times 10^{-3} \times 8.918 \times 10^{-4}}=2.393 \times 10^{-7} \\
& Z_{3}=\frac{g_{c} \lambda d_{B}^{2}}{\alpha_{L}^{2}}=\frac{1.0 \times 272,000\left(8.918 \times 10^{-4}\right)^{2}}{\left(5.556 \times 10^{-8}\right)^{2}}=7.008 \times 10^{13} \\
& Z_{4}=\rho_{V} / \rho_{L}=18.09 / 567=0.031905 \\
& Z_{5}=\left(\rho_{L}-\rho_{V}\right) / \rho_{L}=(567-18.09) / 567=0.9681
\end{aligned}
$$

Substituting these values into Equation (9.13) yields:

$$
\begin{aligned}
& \frac{h_{n b} d_{B}}{k_{L}}=0.23 Z_{1}^{0.674} Z_{2}^{0.35} Z_{3}^{0.371} Z_{4}^{0.297} Z_{5}^{-1.73} \\
& \quad=0.23\left(2.370 \times 10^{-5} \hat{q}\right)^{0.674}\left(2.393 \times 10^{-7}\right)^{0.35}\left(7.008 \times 10^{13}\right)^{0.371}(0.031905)^{0.297}(0.9681)^{-1.73} \\
& \frac{h_{n b} d_{B}}{k_{L}}=0.04402 \hat{q}^{0.674}
\end{aligned}
$$

Substituting $\hat{q}=h_{n b} \Delta T_{e}=h_{n b} \times 16.2$ gives:

$$
\begin{aligned}
h_{n b} & =\left(k_{L} / d_{B}\right) \times 0.04402\left(16.2 h_{n b}\right)^{0.674} \\
& =\left(0.086 / 8.918 \times 10^{-4}\right) \times 0.04402(16.2)^{0.674} h_{n b}^{0.674} \\
h_{n b} & =27.739 h_{n b}^{0.674} \\
h_{n b} & =26,709 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

Finally, the heat flux is given by:

$$
\hat{q}=h_{n b} \Delta T_{e}=26,709 \times 16.2=432,686 \mathrm{~W} / \mathrm{m}^{2}
$$

The calculated values of the heat-transfer coefficient are summarized in the following table:

| Correlation | $h_{n b}\left(\mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ |
| :--- | :--- |
| Forster-Zuber | 5512 |
| Mostinski | 2421 |
| Modified Mostinski | 1396 |
| Cooper | 23,214 |
| Stephan-Abdelsalam | 26,709 |

The predictions of the various correlations differ by a huge amount, the ratio of largest to smallest value being nearly 20 . One reason for the wide variation is that nucleate boiling is very sensitive to the precise condition of the surface on which boiling occurs. Although the factors that govern the nucleation process are reasonably well understood (7-10), it is not practical to specify the detailed surface characteristics required to rigorously model the phenomenon. Even if this could be done, it would be of dubious utility in equipment design because the surface characteristics change in an uncontrollable manner over time due to aging, corrosion, fouling, cleaning procedures, etc. As a result, the variability exhibited by the calculated values actually reflects the variability observed among the sets of experimental data upon which the various correlations are based [2]. Fortunately, tests with commercial tube bundles indicate that the effect of surface condition is much less pronounced in the operation of industrial equipment [11]. Nevertheless, significant conservatism in equipment design is warranted by the level of uncertainty in the fundamental boiling correlations.

### 9.3.2 Mixture effects

It is a well-established fact, based on experimental results, that the rate of heat transfer for nucleate boiling of mixtures is lower than for pure substances. The reason is that the more volatile components accumulate preferentially in the vapor bubbles, leaving the surrounding liquid enriched in the less volatile (higher boiling) components. As a result, the temperature of the liquid in the immediate vicinity of the heating surface increases and the effective driving force for heat transfer is reduced. Furthermore, the concentration gradient generates a mass-transfer resistance in addition to the thermal resistance. In fact, the apparent heat-transfer coefficient for a mixture can be lower than for any of the pure components at equivalent conditions.

Schlünder [12] performed a fundamental analysis of the heat and mass transfer associated with mixture boiling and derived the following equation for the heat-transfer coefficient:

$$
\begin{equation*}
h_{n b}=h_{\text {ideal }}\left\{1+\left(h_{\text {ideal }} / \hat{q}\right)\left[1-\exp \left(\frac{-\hat{q}}{\rho_{L} \lambda \beta}\right)\right] \sum_{i=1}^{n-1}\left(T_{\text {sat }, n}-T_{\text {sat }, i}\right)\left(y_{i}-x_{i}\right)\right\}^{-1} \tag{9.14}
\end{equation*}
$$

where
$n=$ number of components and the index of the highest boiling component
$T_{\text {sat }, i}=$ boiling point of pure component $i$ at system pressure
$y_{i}=$ mole fraction of component $i$ in vapor
$x_{i}=$ mole fraction of component $i$ in liquid
$\beta=0.0002 \mathrm{~m} / \mathrm{s}$ (SI units) $=2.36 \mathrm{ft} / \mathrm{h}$ (English units)
$=$ approximate mass-transfer coefficient

The coefficient, $h_{\text {ideal }}$, is an average of the pure component values that is calculated as follows:

$$
\begin{equation*}
h_{\text {ideal }}=\left[\sum_{i=1}^{n} x_{i} / h_{n b, i}\right]^{-1} \tag{9.15}
\end{equation*}
$$

where $h_{n b, i}$ is the heat-transfer coefficient for pure component $i$.
Note that in Equation (9.14) " $n$ " represents both the number of components in the mixture and the index of the component with the highest boiling point. Also, the vapor and liquid phases are assumed to be in equilibrium. In general, thermodynamic calculations are required to determine the phase compositions. For complex mixtures such as petroleum fractions, these calculations are not feasible. Although it might be possible to use pseudo-components to represent these mixtures, the validity of this procedure in conjunction with Equation (9.14) has not been established.

Thome and Shakir [13] derived a modified version of Equation (9.14) in which the boiling range of the fluid replaces the term involving the phase compositions, making the method more convenient to use. Their result is as follows:

$$
\begin{equation*}
h_{n b}=h_{\text {ideal }}\left\{1+\left(B R \cdot h_{\text {ideal }} / \hat{q}\right)\left[1-\exp \left(\frac{-\hat{q}}{\rho_{L} \lambda \beta}\right)\right]\right\}^{-1} \tag{9.16}
\end{equation*}
$$

where
$B R=T_{D}-T_{B}=$ boiling range
$T_{D}=$ dew-point temperature
$T_{B}=$ bubble-point temperature
$\beta=0.0003 \mathrm{~m} / \mathrm{s}$ (SI units) $=3.54 \mathrm{ft} / \mathrm{h}$ (English units)
Notice that the value of the mass-transfer coefficient, $\beta$, is different from that in Schlünder's equation. Thome and Shakir [13] also showed that $h_{\text {ideal }}$ can be calculated with sufficient accuracy by using mixture properties in a pure component correlation for the heat-transfer coefficient, rather than using Equation (9.15). They used the Stephan-Abdelsalam correlation for this purpose. Since the boiling range of petroleum fractions can be readily determined, Equation (9.16) is directly applicable to these fluids.

Palen [4] presented a simple empirical method that involves a (multiplicative) mixture correction factor that is applied to the heat-transfer coefficient calculated from the Mostinski correlation. The correction factor, $F_{m}$, is given by the following equation:

$$
\begin{equation*}
F_{m}=\left(1+0.0176 \hat{q}^{0.15} B R^{0.75}\right)^{-1} \tag{9.17a}
\end{equation*}
$$

Here, $\hat{q} \propto \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$ and $B R \propto^{\circ} \mathrm{F}$. The corresponding equation in terms of SI units is:

$$
\begin{equation*}
F_{m}=\left(1+0.023 \hat{q}^{0.15} B R^{0.75}\right)^{-1} \tag{9.17b}
\end{equation*}
$$

where $\hat{q} \propto W / m^{2}$ and $B R \propto \mathrm{~K}$.
In conjunction with Equation (9.17), for $P_{r}>0.2$ the pressure correction factor given by Equation (9.5) is replaced by the following:

$$
\begin{equation*}
F_{P}=1.8 P_{r}^{0.17} \tag{9.18}
\end{equation*}
$$

According to Palen [4], this pressure correction is necessary to ensure a conservative estimate for the heat-transfer coefficient. For this reason, Equation (9.17) should not be used with any correlation other than the Mostinski correlation, Equation (9.3), for calculating the heat-transfer coefficient.

Equations (9.14) and (9.16), on the other hand, can be used with any method for calculating pure component heat-transfer coefficients.

The following example is based on data from Ref. [12].

## Example 9.2

Nucleate pool boiling takes place in a liquid consisting of $54.5 \mathrm{~mol} . \% \mathrm{SF}_{6}$ (1) and $45.5 \mathrm{~mol} . \% \mathrm{CCl}_{2} \mathrm{~F}_{2}$ (2) at a pressure of 23 bar with a heat flux of $10^{4} \mathrm{~W} / \mathrm{m}^{2}$. The vapor in equilibrium with the liquid contains $71.1 \mathrm{~mol} . \% \mathrm{SF}_{6}$. The liquid density of the mixture is $10 \mathrm{kmol} / \mathrm{m}^{3}$. At 23 bar, the boiling point of $\mathrm{SF}_{6}$ is $22^{\circ} \mathrm{C}$ and that of $\mathrm{CCl}_{2} \mathrm{~F}_{2}$ is $80^{\circ} \mathrm{C}$. Experimental values for the pure component heat-transfer coefficients at this pressure are $11,787 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ for $\mathrm{SF}_{6}$ and $6,105 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ for $\mathrm{CCl}_{2} \mathrm{~F}_{2}$. Additional data are given in the table below. Estimate the heat-transfer coefficient for the mixture using:
(a) Schlünder's method.
(b) The method of Thome and Shakir.
(c) Palen's method.

| Property | $\mathrm{SF}_{6}$ | $\mathrm{CCl}_{2} \mathrm{~F}_{2}$ |
| :--- | :--- | :--- |
| Critical temperature $\left({ }^{\circ} \mathrm{C}\right)$ | 45.5 | 111.5 |
| Critical pressure (bar) | 37.6 | 41.2 |
| Normal boiling point $\left({ }^{\circ} \mathrm{C}\right)$ | -63.5 | -29.8 |
| Latent heat of vaporization at normal <br> boiling point $(\mathrm{J} / \mathrm{mol})$ | 16,790 | 20,207 |

## Solution

(a) Since $\mathrm{CCl}_{2} \mathrm{~F}_{2}$ has the higher boiling point, it is designated as component number 2 and $\mathrm{SF}_{6}$ as component number 1. Values of all the parameters appearing in Equation (9.14) are given except for the latent heat of vaporization of the mixture. In order to estimate this value, the pure component latent heats must first be determined at the system pressure of 23 bar. The Watson correlation, which relates the latent heats at two different temperatures, is used for this purpose:

$$
\lambda\left(T_{2}\right)=\lambda\left(T_{1}\right)\left[\frac{T_{c}-T_{2}}{T_{c}-T_{1}}\right]^{0.38}
$$

In the present application, $T_{1}$ is taken as the normal boiling point and $T_{2}$ is taken as the boiling point at system pressure. Thus, for $\mathrm{SF}_{6}$ we have:

$$
\begin{aligned}
\lambda_{1}\left(22^{\circ} \mathrm{C}\right) & =16,790\left[\frac{45.5-22}{45.5-(-63.5)}\right]^{0.38} \\
\lambda_{1} & =9372 \mathrm{~J} / \mathrm{mol}
\end{aligned}
$$

Similarly, for $\mathrm{CCl}_{2} \mathrm{~F}_{2}$ we have:

$$
\begin{aligned}
\lambda_{2}\left(80^{\circ} \mathrm{C}\right) & =20,207\left[\frac{111.5-80}{111.5-(-29.8)}\right]^{0.38} \\
\lambda_{2} & =11,424 \mathrm{~J} / \mathrm{mol}
\end{aligned}
$$

For the mixture, the mole fraction weighted average of the pure component latent heats is used:

$$
\begin{aligned}
& \lambda=x_{1} \lambda_{1}+x_{2} \lambda_{2}=0.545 \times 9372+0.455 \times 11,424 \\
& \lambda \cong 10,300 \mathrm{~J} / \mathrm{mol}
\end{aligned}
$$

Next, $h_{\text {ideal }}$ is computed using Equation (9.15):

$$
\begin{aligned}
h_{\text {ideal }} & =\left(x_{1} / h_{n b, 1}+x_{2} / h_{n b, 2}\right)^{-1} \\
& =(0.545 / 11,787+0.455 / 6105)^{-1} \\
h_{\text {ideal }} & =8280 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

The heat-transfer coefficient for the mixture can now be obtained by substituting the data into Equation (9.14):

$$
\begin{aligned}
h_{n b}= & h_{\text {ideal }}\left\{1+\left(h_{\text {ideal }} / \hat{q}\right)\left[1-\exp \left(\frac{-\hat{q}}{\rho_{L} \lambda \beta}\right)\right] \sum_{i=1}^{n-1}\left(T_{\text {sat }, n}-T_{\text {sat }, i}\right)\left(y_{i}-x_{i}\right)\right\}^{-1} \\
= & 8280\left\{1+(8280 / 10,000)\left[1-\exp \left(\frac{-10,000}{10,000 \times 10,300 \times 0.0002}\right)\right]\right. \\
& \quad \times(80-22)(0.711-0.545)\}^{-1}
\end{aligned}
$$

The measured heat-transfer coefficient for this mixture is $2096 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}[12]$, which differs from the calculated value by about $3 \%$.
(b) Since the dew-point and bubble-point temperatures for the mixture were not given in Ref. [12], the PRO II (SimSci-Esscor) process simulator was used to obtain the following values at a pressure of 23 bars: $T_{D}=326.5 \mathrm{~K}$ and $T_{B}=316.9 \mathrm{~K}$. The boiling range for the mixture is, therefore:

$$
B R=T_{D}-T_{B}=326.5-316.9=9.6 \mathrm{~K}
$$

The heat-transfer coefficient for the mixture is obtained from Equation (9.16) using the values of $h_{\text {ideal }}$ and $\lambda$ from part (a):

$$
\begin{aligned}
h_{n b} & =h_{\text {ideal }}\left\{1+\left(B R \cdot h_{\text {ideal }} / \hat{q}\right)\left[1-\exp \left(\frac{-\hat{q}}{\rho_{L} \lambda \beta}\right)\right]\right\}^{-1} \\
& =8280\left\{1+\left(\frac{9.6 \times 8280}{10,000}\right)\left[1-\exp \left(\frac{-10,000}{10,000 \times 10,300 \times 0.0003}\right)\right]\right\} \\
h_{n b} & =2589 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

This value is about $24 \%$ higher than the experimental value of $2096 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$.
(c) For a mixture, the pseudo-critical pressure, $P_{p c}$, can be used in place of the critical pressure in the Mostinski correlation. The pseudo-critical pressure is the mole fraction weighted average
of the pure component critical pressures. Thus,

$$
\begin{aligned}
& P_{p c}=x_{1} P_{c 1}+x_{2} P_{c 2}=0.545 \times 37.6+0.435 \times 41.2 \\
& P_{p c} \cong 39.24 \mathrm{bar}=3924 \mathrm{kPa}
\end{aligned}
$$

The pseudo-reduced pressure is then:

$$
P_{p r}=P / P_{p c}=23 / 39.24=0.586
$$

Since this value is greater than 0.2 , Equation (9.18) is used to calculate the pressure correction factor with $P_{p r}$ in place of $P_{r}$.

$$
F_{P}=1.8 P_{p r}^{0.17}=1.8(0.587)^{0.17}=1.6437
$$

The mixture correction factor is obtained from Equation (9.17b).

$$
\begin{aligned}
F_{m} & =\left(1+0.023 \hat{q}^{0.15} B R^{0.75}\right)^{-1} \\
& =\left[1+0.023(10,000)^{0.15}(9.6)^{0.75}\right]^{-1} \\
F_{m} & =0.6669
\end{aligned}
$$

Including this factor in Equation (9.2b) gives:

$$
\begin{aligned}
h_{n b} & =0.00417 P_{c}^{0.69} \hat{q}^{0.7} F_{P} F_{m} \\
& =0.00417(3924)^{0.69}(10,000)^{0.7} \times 1.6437 \times 0.6669 \\
h_{n b} & =870 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

This value is very conservative compared with the measured value of $2096 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$ for this system. Note, however, that the mixture correction factor itself is not conservative, since $F_{m} \cdot h_{\text {ideal }}=5522 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$, which is much higher than the measured heat-transfer coefficient. This result emphasizes the point that Palen's mixture correction factor is intended for use only with the Mostinski correlation for calculating $h_{n b}$.

### 9.3.3 Convective effects in tube bundles

Heat-transfer coefficients for boiling on tube bundles are generally higher than for boiling on single tubes under the same conditions. The enhancement in heat-transfer rate is due to the convective circulation that is set up within and around the tube bundle. The circulation is driven by the density difference between the liquid surrounding the bundle and the two-phase mixture within the bundle. In this respect it is similar to the circulation in a thermosyphon reboiler. The circulation rate can be calculated with a computer model and used to determine the convective contribution to the heat transfer.
For hand calculations, Palen [4] presented an approximate method for calculating convective effects. The average boiling heat-transfer coefficient, $h_{b}$, is expressed as follows:

$$
\begin{equation*}
h_{b}=h_{n b} F_{b}+h_{n c} \tag{9.19}
\end{equation*}
$$

where $h_{n c}$ is a heat-transfer coefficient for liquid-phase natural convection and $F_{b}$ is a factor that accounts for the effect of the thermosyphon-type circulation in the tube bundle. The
bundle convection factor is correlated in terms of bundle geometry by the following empirical equation [4]:

$$
\begin{equation*}
F_{b}=1.0+0.1\left[\frac{0.785 D_{b}}{C_{1}\left(P_{T} / D_{o}\right)^{2} D_{o}}-1.0\right]^{0.75} \tag{9.20}
\end{equation*}
$$

where
$D_{b}=$ bundle diameter (outer tube-limit diameter)
$D_{o}=$ tube OD
$P_{T}=$ tube pitch
$C_{1}=1.0$ for square and rotated square layouts
$=0.866$ for triangular layouts
The coefficient, $h_{n c}$, can be estimated using Equation (2.57) for free convection from a horizontal cylinder. However, liquid-phase natural convection makes a relatively small contribution to the total heat transfer except when the temperature difference, $\Delta T_{e}$, is less than about $4^{\circ} \mathrm{C}$. For larger temperature differences, therefore, Palen [4] suggests using a rough approximation for $h_{n c}$ of $250 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}\left(44 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ for hydrocarbons and $1000 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}\left(176 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ for water and aqueous solutions.

### 9.3.4 Critical heat flux

At high heat fluxes, the vapor bubbles leave the heated surface in columns or jets. When the velocity of the vapor jets reaches a sufficiently large value, the jets become unstable and collapse. The resultant accumulation of vapor at the heated surface prevents an adequate supply of liquid from reaching the surface, and the heat flux begins to decrease. Zuber [14] performed a stability analysis to derive equations for the maximum vapor velocity and critical heat flux in nucleate pool boiling on a large flat upward-facing surface. The equation for critical heat flux is generally used in the following form:

$$
\begin{equation*}
\hat{q}_{c}=0.149 \lambda \rho_{V}^{0.5}\left[\sigma g g_{c}\left(\rho_{L}-\rho_{V}\right)\right]^{0.25} \tag{9.21}
\end{equation*}
$$

The coefficient of 0.149 is based on experimental data; the theoretical value is $\pi / 24 \cong 0.131$. Equation (9.21) is often used irrespective of the geometry of the heated surface.

Results for other geometries can be found in Ref. [9, 15]. For boiling on a horizontal cylinder, the result is:

$$
\begin{equation*}
\hat{q}_{c}=K \lambda \rho_{V}^{0.5}\left[\sigma g g_{c}\left(\rho_{L}-\rho_{V}\right)\right]^{0.25} \tag{9.22}
\end{equation*}
$$

where
$K=0.118 \quad$ for $R^{*} \geq 1.17$
$=0.123\left(R^{*}\right)^{-0.25}$ for $0.12<R^{*}<1.17$
$R^{*}=R\left[\frac{g\left(\rho_{L}-\rho_{V}\right)}{g_{c} \sigma}\right]^{0.5}=$ dimensionless radius
$R=$ radius of cylinder
Although Equations (9.21) and (9.22) do not contain an explicit pressure dependence, the critical heat flux is a strong function of pressure through its effect on $\lambda, \rho_{V}$, and $\sigma$.

A correlation for boiling on a single horizontal tube based on the principle of corresponding states and due to Mostinski is the following [4,7]:

$$
\begin{equation*}
\hat{q}_{c}=803 P_{c} P_{r}^{0.35}\left(1-P_{r}\right)^{0.9} \tag{9.23a}
\end{equation*}
$$

where $\hat{q}_{c} \propto \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$ and $P_{c} \propto \mathrm{psia}$.

The corresponding equation in terms of SI units is:

$$
\begin{equation*}
\hat{q}_{c}=367 P_{c} P_{r}^{0.35}\left(1-P_{r}\right)^{0.9} \tag{9.23b}
\end{equation*}
$$

where $\hat{q}_{c} \propto \mathrm{~W} / \mathrm{m}^{2}$ and $P_{c} \propto \mathrm{kPa}$.
For tube bundles, Palen [4] presented the following correlation:

$$
\begin{equation*}
\hat{q}_{c, \text { bundle }}=\hat{q}_{c, \text { tube }} \phi_{b} \tag{9.24}
\end{equation*}
$$

where
$\hat{q}_{c, \text { bundle }}=$ critical heat flux for tube bundle
$\hat{q}_{c, \text { tube }}=$ critical heat flux for a single tube
$\phi_{b}=$ bundle correction factor
$=3.1 \psi_{b}$ for $\psi_{b}<1.0 / 3.1 \cong 0.323$
$=1.0$ otherwise
$\psi_{b}=$ dimensionless bundle geometry parameter $=\frac{\pi D_{b} L}{A}$
$D_{b}=$ bundle diameter
$A=$ bundle surface area $=n_{t} \pi D_{0} L$ for plain tubes
$D_{o}=$ tube OD
$L=$ tube length
$n_{t}=$ number of tubes in bundle
It is recommended that vapor release lanes be provided to aid vapor flow out of the bundle if $\phi_{b}<0.1$ and the heat flux exceeds $50 \%$ of the critical heat flux for the bundle [4].

The above correlations apply to pure component nucleate boiling. The critical heat flux for a mixture may be higher or lower than for a pure component under similar conditions. Although a higher value is usually found, as would be expected from the effect of boiling point elevation and mass-transfer resistance in mixture boiling, the variation of surface tension with composition can cause the mixture critical heat flux to be lower than the pure component value in some cases. In any event, the mixture effect is generally neglected in design work since it cannot be reliably predicted. The above correlations are used with the mixture physical properties replacing the pure component properties. For the Mostinski correlation, the pseudo-critical and pseudo-reduced pressures can be used in place of the true mixture values.

## Example 9.3

Estimate the critical heat flux for the conditions of Example 9.1 using the following methods:
(a) The Zuber equation.
(b) The Zuber-type equation for a horizontal cylinder.
(c) The Mostinski correlation.

## Solution

(a) The following data are obtained from Example 9.1:

$$
\begin{array}{ll}
\lambda=272,000 \mathrm{~J} / \mathrm{kg} & \rho_{L}=567 \mathrm{~kg} / \mathrm{m}^{3} \\
\sigma=8.2 \times 10^{-3} \mathrm{~N} / \mathrm{m} & \rho_{V}=18.09 \mathrm{~kg} / \mathrm{m}^{3}
\end{array}
$$

Substituting these values into Equation (9.21) with $g=9.81 \mathrm{~m} / \mathrm{s}^{2}$ and $g_{c}=1.0 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{N} \cdot \mathrm{s}^{2}$ gives:

$$
\begin{aligned}
\hat{q}_{c} & =0.149 \lambda \rho_{V}^{0.5}\left[\sigma g g_{c}\left(\rho_{L}-\rho_{V}\right)\right]^{0.25} \\
& =0.149 \times 272,000(18.09)^{0.5}\left[8.2 \times 10^{-3} \times 9.81 \times 1.0(567-18.09)\right]^{0.25} \\
\hat{q}_{c} & =444,345 \cong 444,000 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

(b) The first step is to calculate the dimensionless radius, $R^{*}$. For a 1-in. tube, $R=0.0127 \mathrm{~m}$. Hence,

$$
\begin{aligned}
R^{*} & =R\left[\frac{g\left(\rho_{L}-\rho_{V}\right)}{g_{c} \sigma}\right]^{0.5} \\
& =0.0127\left[\frac{9.81(567-18.09)}{1.0 \times 8.2 \times 10^{-3}}\right]^{0.5} \\
R^{*} & =10.3
\end{aligned}
$$

Since $R^{*}>1.17$, set $K=0.118$ in Equation (9.22):

$$
\begin{aligned}
\hat{q}_{c} & =0.118 \lambda \rho_{V}^{0.5}\left[\sigma g g_{c}\left(\rho_{L}-\rho_{V}\right)\right]^{0.25} \\
& =0.118 \times 272,000(18.09)^{0.5}\left[8.2 \times 10^{-3} \times 9.81 \times 1.0(567-18.09)\right]^{0.25} \\
\hat{q}_{c} & =351,898 \cong 352,000 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

(c) From Example 9.1, $P=310.3 \mathrm{kPa}$ and $P_{c}=2550 \mathrm{kPa}$. Therefore,

$$
P_{r}=P / P_{c}=0.1217
$$

Using Equation (9.23b) gives:

$$
\begin{aligned}
\hat{q}_{c} & =367 P_{c} P_{r}^{0.35}\left(1-P_{r}\right)^{0.9} \\
& =367 \times 2550(0.1217)^{0.35}(1-0.1217)^{0.9} \\
\hat{q}_{c} & =398,416 \cong 398,000 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

The Zuber and Mostinski values differ by about 11\%. The results from Equations (9.21) and (9.22) differ by about $23 \%$, of which $10 \%$ is due to the effect of surface geometry. The other $13 \%$ is due to the empirical coefficient of 0.149 in Equation (9.21) as opposed to the theoretical coefficient in Equation (9.22).

## Example 9.4

The nucleate boiling of Example 9.1 takes place on a tube bundle consisting of 520 one-in. OD tubes on a $1.25-\mathrm{in}$. square pitch. The bundle diameter is approximately 34 in . Estimate the critical heat flux and heat-transfer coefficient for this situation.

## Solution

The critical heat flux for the tube bundle is given by Equation (9.24):

$$
\hat{q}_{c, \text { bundle }}=\hat{q}_{c, \text { tube }} \phi_{b}
$$

The critical heat flux for a single tube was calculated in Example 9.3, and any of the three results obtained there can be used here. Choosing the result calculated by the Mostinski correlation, we have:

$$
\hat{q}_{c, t u b e}=398,000 \mathrm{~W} / \mathrm{m}^{2}
$$

To determine the bundle correction factor, first calculate the bundle geometry parameter, $\psi_{b}$, which for plain tubes is:

$$
\psi_{b}=\frac{D_{b}}{n_{t} D_{o}}=\frac{34}{520 \times 1.0}=0.0654
$$

Since this value is less than 0.323 , the bundle correction factor is:

$$
\phi_{b}=3.1 \psi_{b}=3.1 \times 0.0654 \cong 0.203
$$

Therefore,

$$
\hat{q}_{c, \text { bundle }}=398,000 \times 0.203 \cong 81,000 \mathrm{~W} / \mathrm{m}^{2}
$$

The heat-transfer coefficient for a tube bundle is given by Equation (9.19):

$$
h_{b}=h_{n b} F_{b}+h_{n c}
$$

We will use the value of $h_{n b}$ calculated in Example 9.1 by the modified Mostinski correlation, i.e., $h_{n b}=1396 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. Also, from Example 9.1, $\Delta T_{e}=16.2 \mathrm{~K}$. Since this value is much greater than 4 K , a rough estimate is sufficient for the natural convection coefficient, $h_{n c}$. For an organic compound, Palen's recommendation for hydrocarbons is adequate, so we take $h_{n c} \cong 250 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$. The value of $F_{b}$ is calculated using Equation (9.20):

$$
\begin{aligned}
F_{b} & =1.0+0.1\left[\frac{0.785 D_{b}}{C_{1}\left(P_{T} / D_{o}\right)^{2} D_{o}}-1.0\right]^{0.75} \\
& =1.0+0.1\left[\frac{0.785 \times 34}{1.0(1.25 / 1.0)^{2} \times 1.0}-1.0\right]^{0.75} \\
F_{b} & \cong 1.803
\end{aligned}
$$

Therefore,

$$
h_{b}=1396 \times 1.803+250=2767 \cong 2770 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
$$

### 9.4 Two-Phase Flow

### 9.4.1 Two-phase flow regimes

When a vapor-liquid mixture flows through a circular tube, a number of different flow regimes can occur, depending on the vapor fraction, flow rate, and orientation of the tube. For vertical tubes, the following flow regimes are distinguished (Figure 9.2(a)):

- Bubbly flow: At low vapor fractions, vapor bubbles are dispersed in a continuous liquid phase.
- Slug flow: At moderate vapor fractions and relatively low flow rates, large bullet-shaped vapor bubbles flow through the tube separated by slugs of liquid in which smaller bubbles may be dispersed. A percolating coffee pot exemplifies this type of flow.
- Churn flow: At higher flow rates, the large vapor bubbles present in slug flow become unstable and break apart, resulting in an oscillatory, or churning, motion of the liquid upward and downward in the tube.
- Annular flow: At high vapor fractions and high flow rates, the liquid flows as a film along the tube wall while the vapor flows at a higher velocity in the central region of the tube. Small liquid droplets are usually entrained in the vapor phase, and vapor bubbles may be dispersed in the liquid film as well. At sufficiently high liquid flow rates, the droplets coalesce to form large streaks or wisps of liquid entrained in the vapor phase. This condition, which is characteristic of flows with a high mass flux, is referred to as wispy annular flow.
- Mist Flow: At very high vapor fractions, the liquid phase exists entirely as droplets entrained in a continuous vapor phase.


Figure 9.2 Two-phase flow regimes in circular tubes: (a) vertical tube and (b) horizontal tube (Source:
Ref. [8])

In horizontal tubes the situation is somewhat different due to stratification of the flow resulting from the gravitational force. The following flow regimes are observed (Figure 9.2(b)):

- Bubbly flow: The flow pattern is similar to that in vertical tubes except the bubbles tend to concentrate in the upper part of the tube.
- Plug flow: The flow pattern is similar to slug flow in vertical tubes, but the bullet-shaped bubbles tend to flow closer to the top of the tube and occupy less of the tube cross-section.
- Stratified flow: The two phases are completely stratified, with the liquid flowing along the bottom of the tube and the vapor flowing along the top.
- Wavy flow: In stratified flow at higher vapor velocities, waves are formed on the surface of the liquid that characterize this flow regime.
- Slug flow: In this regime, intermittent slugs of liquid pass through the tube. The slugs occupy the entire tube cross-section and contain a large number of entrained vapor bubbles that impart a frothy character to the liquid.
- Annular flow: The flow pattern is similar to annular flow in vertical tubes except that the liquid film thickness is non-uniform, being greater on the bottom than the top of the tube.
- Mist flow: The flow pattern is the same as in a vertical tube and, hence, is not illustrated for the horizontal tube in Figure 9.2.

Flow pattern maps, which show the operating regions over which the various flow regimes exist, can be found in Refs. [2,8], among others. The latter also discusses modeling and empirical correlations for predicting the frictional pressure drop in each flow regime. However, most process equipment design is based on generalized pressure drop correlations that do not explicitly account for the two-phase flow regime. These correlations are presented in the following subsection.

### 9.4.2 Pressure drop correlations

Two general models of two-phase flow are used, the homogeneous flow model and the separated flow model. In the former, the two phases are assumed to have the same velocity. In the separated flow model, it is assumed that the two phases flow in separate zones, as in the annular and stratified regimes. In this case the two phases generally have different velocities, but can interact with each other. Under most conditions, the separated flow model provides a better representation of the pressure drop in pipe flow. Several widely used pressure drop correlations based on this model are presented below.

## The Lockhart-Martinelli correlation

In this method the two-phase pressure gradient is expressed as a multiple of the pressure gradient that would occur if the liquid phase flowed alone in the conduit. Thus,

$$
\begin{equation*}
\left(\frac{\Delta P_{f}}{L}\right)_{t p}=\phi_{L}^{2}\left(\frac{\Delta P_{f}}{L}\right)_{L} \tag{9.25}
\end{equation*}
$$

where
$\phi_{L}^{2}=$ two-phase multiplier
$\left(\Delta P_{f} / L\right)_{L}=$ negative pressure gradient for liquid alone
$\left(\Delta P_{f} / L\right)_{t p}=$ negative two-phase pressure gradient
The negative pressure gradient is the pressure drop per unit length or, more precisely, the rate of decrease of pressure with distance in the flow direction. Equation (9.25) is formulated in terms of pressure gradients rather than pressure drops because the vapor fraction and other flow parameters may vary in the flow direction. In this case the pressure drop is obtained by integrating the
two-phase pressure gradient along the flow path. When the vapor fraction and other flow parameters are essentially constant, either pressure gradients or pressure drops can be used in Equation (9.25).

The two-phase multiplier is a function of the parameter, $X$, which is defined as follows:

$$
\begin{equation*}
X=\left[\frac{\left(\Delta P_{f} / L\right)_{L}}{\left(\Delta P_{f} / L\right)_{V}}\right]^{0.5} \tag{9.26}
\end{equation*}
$$

where $\left(\Delta P_{f} / L\right)_{V}$ is the pressure gradient that would occur if the vapor phase flowed alone in the conduit. The relationship between $\phi_{L}^{2}$ and $X$ was given in graphical form by Lockhart and Martinelli [16], and subsequently expressed analytically by Chisholm [17] as follows:

$$
\begin{equation*}
\phi_{L}^{2}=1+\frac{C}{X}+\frac{1}{X^{2}} \tag{9.27}
\end{equation*}
$$

The constant, $C$, depends on whether the flow in each phase is laminar or turbulent, as shown in Table 9.2. Approximate critical Reynolds numbers for determining the flow condition of each phase, as suggested by Lockhart and Martinelli [16], are also listed. These Reynolds numbers are calculated as if each phase flowed alone in the conduit.

In practice, if the liquid phase is turbulent, the vapor phase will usually be turbulent as well, and this is by far the most important case. Therefore, Equation (9.27) is restated for the turbulent-turbulent case as follows:

$$
\begin{equation*}
\phi_{L}^{2}=1+\frac{20}{X_{t t}}+\frac{1}{X_{t t}^{2}} \tag{9.28}
\end{equation*}
$$

The calculation of $X$ can also be simplified if the friction factor has the same functional form for each phase, namely:

$$
\begin{equation*}
f=\text { const. } / R e^{n} \tag{9.29}
\end{equation*}
$$

From Equation (4.5) or (5.1), the negative pressure gradient has the following functionality:

$$
\begin{equation*}
\Delta P_{f} / L \propto \frac{f G^{2}}{s} \tag{9.30}
\end{equation*}
$$

Combining Equations (9.29) and (9.30) yields:

$$
\begin{equation*}
\Delta P_{f} / L \propto G^{2-n} \mu^{n} s^{-1} \propto \dot{m}^{2-n} \mu^{n} s^{-1} \tag{9.31}
\end{equation*}
$$

Taking square roots gives:

$$
\begin{equation*}
\left(\Delta P_{f} / L\right)^{0.5} \propto \dot{m}^{(2-n) / 2} \mu^{n / 2} s^{-0.5} \tag{9.32}
\end{equation*}
$$

Table 9.2 Values of the Constant in Equation (9.27)

| Liquid | Vapor | Notation | $R e_{L}$ | $R e_{V}$ | $C$ |
| :--- | :--- | :--- | :--- | :--- | ---: |
| Turbulent | Turbulent | $t t$ | $>2000$ | $>2000$ | 20 |
| Viscous (laminar) | Turbulent | $v t$ | $<1000$ | $>2000$ | 12 |
| Turbulent | Viscous (laminar) | $t v$ | $>2000$ | $<1000$ | 10 |
| Viscous (laminar) | Viscous (laminar) | $v v$ | $<1000$ | $<1000$ | 5 |

From the definition of $X$ given by Equation (9.26), it then follows that:

$$
\begin{equation*}
X=\left(\dot{m}_{L} / \dot{m}_{V}\right)^{(2-n) / 2}\left(\mu_{L} / \mu_{V}\right)^{n / 2}\left(s_{V} / s_{L}\right)^{0.5} \tag{9.33}
\end{equation*}
$$

Now the mass flow rates of the two phases are related to the vapor mass fraction, $x$, by:

$$
\begin{align*}
\dot{m}_{L} & =\dot{m}(1-x)  \tag{9.34}\\
\dot{m}_{V} & =\dot{m} x \tag{9.35}
\end{align*}
$$

Using these relations and replacing the specific gravity ratio by the density ratio, Equation (9.33) becomes:

$$
\begin{equation*}
X=\left(\frac{1-x}{x}\right)^{(2-n) / 2}\left(\mu_{L} / \mu_{V}\right)^{n / 2}\left(\rho_{V} / \rho_{L}\right)^{0.5} \tag{9.36}
\end{equation*}
$$

For the turbulent-turbulent case, Lockhart and Martinelli [16] assumed the value $n=0.2$ to obtain:

$$
\begin{equation*}
X_{t t}=\left(\frac{1-x}{x}\right)^{0.9}\left(\rho_{V} / \rho_{L}\right)^{0.5}\left(\mu_{L} / \mu_{V}\right)^{0.1} \tag{9.37}
\end{equation*}
$$

Equation (9.37) is generally used in practice. Although the exponent, $n$, is closer to 0.25 for commercial pipe and tubing (cf. Equations (4.8) and (5.2)), the difference is insignificant compared with the inherent uncertainty associated with the Lockhart-Martinelli correlation. It will be noted from Equation (9.37) that $X_{t t}$ is zero when the vapor fraction, $x$, equals 1.0. In this case, Equation (9.28) shows that the two-phase multiplier, $\phi_{L}^{2}$, becomes infinite. For high vapor fractions, an alternate formulation in terms of the (negative) vapor-phase pressure gradient, $\left(\Delta P_{f} / L\right)_{V}$, can be used (see Problem 9.1). For process engineering work, however, the formulation in terms of the liquid-phase pressure gradient is used almost exclusively.

## The Chisholm correlation

Chisholm [18] expressed the two-phase pressure gradient as a multiple of the pressure gradient that would occur if the entire flow (vapor and liquid) had the properties of the liquid phase. The result is analogous to Equation (9.25):

$$
\begin{equation*}
\left(\frac{\Delta P_{f}}{L}\right)_{t p}=\phi_{L O}^{2}\left(\frac{\Delta P_{f}}{L}\right)_{L O} \tag{9.38}
\end{equation*}
$$

where

$$
\phi_{L O}^{2}=\text { two-phase multiplier }
$$

$\left(\frac{\Delta P_{f}}{L}\right)_{L O}=$ negative pressure gradient for total flow as liquid
The two-phase multiplier is a function of the parameter, $Y$, defined as:

$$
\begin{equation*}
Y=\left[\frac{\left(\Delta P_{f} / L\right)_{V O}}{\left(\Delta P_{f} / L\right)_{L O}}\right]^{0.5} \tag{9.39}
\end{equation*}
$$

where $\left(\Delta P_{f} / L\right)_{V O}$ is the negative pressure gradient that would occur if the entire flow had the properties of the vapor phase. Comparison with Equation (9.26) shows that $Y$ is analogous to
the reciprocal of the Lockhart-Martinelli parameter. Since the mass flux, $G$, is the same for the numerator and denominator, it follows from Equation (9.30) that Equation (9.39) can be written in the alternate form:

$$
\begin{equation*}
Y=\left[\left(f_{V O} / f_{L O}\right)\left(s_{L} / s_{V}\right)\right]^{0.5}=\left[\left(f_{V O} / f_{L O}\right)\left(\rho_{L} / \rho_{V}\right)\right]^{0.5} \tag{9.40}
\end{equation*}
$$

where $f_{V O}$ and $f_{L O}$ are friction factors calculated with vapor and liquid properties, respectively. Assuming that the friction factor is the same function of Reynolds number in both phases as given by Equation (9.29), it follows that:

$$
\begin{equation*}
f_{V O} / f_{L O}=\left(\mu_{v} / \mu_{L}\right)^{n} \tag{9.41}
\end{equation*}
$$

Substituting this relationship in Equation (9.40) yields:

$$
\begin{equation*}
Y=\left(\rho_{L} / \rho_{V}\right)^{0.5}\left(\mu_{V} / \mu_{L}\right)^{n / 2} \tag{9.42}
\end{equation*}
$$

The correlation for the two-phase multiplier is the following [18]:

$$
\begin{equation*}
\phi_{L O}^{2}=1+\left(Y^{2}-1\right)\left\{B[x(1-x)]^{(2-n) / 2}+x^{2-n}\right\} \tag{9.43}
\end{equation*}
$$

where $x$ is the vapor fraction. The parameter, $B$, depends on both $Y$ and $G$. Chisholm [18] determined this relationship empirically using results from the literature. He then adjusted the correlation to obtain a conservative estimate of pressure drop for design purposes. As a result, his final correlation for $B$ is an awkward discontinuous function that tends to over-predict the pressure drop in certain ranges of $G$ and $Y$. Therefore, we will follow Hewitt's [2,19] recommendation and use Chisholm's unadjusted correlation for $B$, which is represented by the following piecewise continuous function (with $G$ in units of $\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$ ):

$$
\begin{align*}
B & =1500 / G^{0.5} & & (0<Y \leq 9.5) \\
& =14,250 /\left(Y G^{0.5}\right) & & (9.5<Y \leq 28)  \tag{9.44}\\
& =399,000 /\left(Y^{2} G^{0.5}\right) & & (Y>28)
\end{align*}
$$

For calculations in SI units, the following conversion can be used:

$$
G\left(\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}\right)=737.35 G\left(\mathrm{~kg} / \mathrm{s} \cdot \mathrm{~m}^{2}\right)
$$

## The Friedel correlation

The two-phase pressure gradient is expressed in the same manner as the Chisholm method, Equation (9.38), with the following correlation for the two-phase multiplier [20]:

$$
\begin{equation*}
\phi_{L O}^{2}=E+\frac{3.24 F H}{F r^{0.045} W e^{0.035}} \tag{9.45}
\end{equation*}
$$

where

$$
\begin{align*}
E & =(1-x)^{2}+x^{2}\left(f_{V O} / f_{L O}\right)\left(\rho_{L} / \rho_{V}\right)  \tag{9.46}\\
F & =x^{0.78}(1-x)^{0.24}  \tag{9.47}\\
H & =\left(\rho_{L} / \rho_{V}\right)^{0.91}\left(\mu_{V} / \mu_{L}\right)^{0.19}\left(1-\mu_{V} / \mu_{L}\right)^{0.7}  \tag{9.48}\\
F r & =\frac{G^{2}}{g D_{i} \rho_{t p}^{2}}=\text { Froude number }  \tag{9.49}\\
W e & =\frac{G^{2} D_{i}}{g_{c} \rho_{t p} \sigma}=\text { Weber number }  \tag{9.50}\\
D_{i} & =\text { internal diameter of conduit } \\
\rho_{t p} & =\text { two-phase density }
\end{align*}
$$

For the purpose of this correlation, the two-phase density is calculated as follows:

$$
\begin{equation*}
\rho_{t p}=\left[x / \rho_{V}+(1-x) / \rho_{L}\right]^{-1} \tag{9.51}
\end{equation*}
$$

Equation (9.46) can be restated in a more convenient form by using Equation (9.41) to eliminate the friction factors:

$$
\begin{equation*}
E=(1-x)^{2}+x^{2}\left(\mu_{V} / \mu_{L}\right)^{n}\left(\rho_{L} / \rho_{V}\right) \tag{9.52}
\end{equation*}
$$

The correlation as given here is valid for horizontal and vertical upward flow.

## The Müller-Steinhagen and Heck correlation

The correlation is given in Ref. [21], and can be reformulated in the Chisholm format of Equation (9.38) with the two-phase multiplier given by the following equation:

$$
\begin{equation*}
\phi_{L O}^{2}=Y^{2} x^{3}+\left[1+2 x\left(Y^{2}-1\right)\right](1-x)^{1 / 3} \tag{9.53}
\end{equation*}
$$

where $x$ is the vapor mass fraction and $Y$ is the Chisholm parameter. Equation (9.53) is an interpolation formula between all liquid flow $(x=0)$ and all vapor flow $(x=1)$. For $x=0, \phi_{L O}^{2}=1$ and the negative two-phase pressure gradient reduces to $\left(\Delta P_{f} / L\right)_{L O}$. For $x=1, \phi_{L O}^{2}=Y$ and the negative two-phase pressure gradient reduces to $\left(\Delta P_{f} / L\right)_{V O}$.
The Friedel correlation is widely regarded as the most reliable general method for computing two-phase pressure losses. However, in two recent studies [22, 23] the performance of the simpler Müller-Steinhagen and Heck (MSH) method was found to be superior to that of the Friedel method. It should be recognized that the uncertainty associated with all of these methods is much greater than for single-phase pressure drop calculations, and relatively large errors are possible in any given application.

## Example 9.5

The return line from a thermosyphon reboiler consists of $10-\mathrm{in}$. schedule 40 pipe with an ID of 10.02 in . ( 0.835 ft ). The total mass flow rate in the line is $300,000 \mathrm{lbm} / \mathrm{h}$, of which $60,000 \mathrm{lbm} / \mathrm{h}$
(20\%) is vapor and $240,000 \mathrm{lbm} / \mathrm{h}$ is liquid. Physical properties of the vapor and liquid fractions are given in the following table:

| Property | Liquid | Vapor |
| :--- | :---: | :---: |
| $\mu(\mathrm{cp})$ | 0.177 | 0.00885 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 38.94 | 0.4787 |
| $\sigma(\mathrm{dyne} / \mathrm{cm})$ | 11.4 | - |

Calculate the friction loss per unit length in the line using:
(a) The Lockhart-Martinelli correlation.
(b) The Chisholm correlation.
(c) The Friedel correlation.
(d) The MSH correlation.

## Solution

(a) The friction loss for the liquid fraction flowing alone in the pipe is calculated first.

$$
\begin{aligned}
G_{L} & =\frac{\dot{m}_{L}}{(\pi / 4) D_{i}^{2}}=\frac{240,000}{(\pi / 4)(0.835)^{2}}=438,277 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e_{L} & =\frac{D_{i} G_{L}}{\mu_{L}}=\frac{0.835 \times 438,277}{0.177 \times 2.419}=854,724 \\
s_{L} & =\rho_{L} / \rho_{\text {water }}=38.94 / 62.43=0.6237
\end{aligned}
$$

Equation (4.8) is used to calculate the friction factor:

$$
f_{L}=0.3673 R e_{L}^{-0.2314}=0.3673(854,724)^{-0.2314}=0.01557
$$

The friction loss per unit length is given by:

$$
\begin{aligned}
& \left(\frac{\Delta P_{f}}{L}\right)_{L}=\frac{f_{L} G_{L}^{2}}{7.50 \times 10^{12} D_{i} s_{L} \phi_{L}}=\frac{0.01557(438,277)^{2}}{7.5 \times 10^{12} \times 0.835 \times 0.6237 \times 1.0} \\
& \left(\frac{\Delta P_{f}}{L}\right)_{L}=0.000766 \mathrm{psi} / \mathrm{ft}
\end{aligned}
$$

Since the flow is turbulent, the Lockhart-Martinelli parameter is calculated using Equation (9.37).

$$
\begin{aligned}
X_{t t} & \cong\left(\frac{1-x}{x}\right)^{0.9}\left(\frac{\rho_{V}}{\rho_{L}}\right)^{0.5}\left(\frac{\mu_{L}}{\mu_{V}}\right)^{0.1} \\
& =(0.8 / 0.2)^{0.9}(0.4787 / 38.94)^{0.5}(0.177 / 0.00885)^{0.1} \\
X_{t t} & \cong 0.521
\end{aligned}
$$

For comparison, the reader can verify that using Equation (9.36) with $n=0.2314$ to calculate $X_{t t}$ gives a value of 0.534 , which differs from the value calculated above by less than $3 \%$.

For turbulent flow, the two-phase multiplier is given by Equation (9.28):

$$
\phi_{L}^{2}=1+\frac{20}{X_{t t}}+\frac{1}{X_{t t}^{2}}=1+\frac{20}{0.521}+\frac{1}{(0.521)^{2}}=43.07
$$

The two-phase friction loss is then:

$$
\left(\frac{\Delta P_{f}}{L}\right)_{t p}=\phi_{L}^{2}\left(\frac{\Delta P_{f}}{L}\right)_{L}=43.07 \times 0.000766=0.033 \mathrm{psi} / \mathrm{ft}
$$

(b) For the Chisholm method, the friction loss is calculated assuming the total flow has the properties of the liquid. Thus,

$$
\begin{aligned}
G & =\frac{\dot{m}}{(\pi / 4) D_{i}^{2}}=\frac{300,000}{(\pi / 4)(0.835)^{2}}=547,846 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e_{L O} & =\frac{D_{i} G}{\mu_{L}}=\frac{0.835(547,846)}{0.177 \times 2.419}=1,068,405 \\
f_{L O} & =0.3673 R e_{L O}^{-0.2314}=0.3673(1,068,405)^{-0.2314}=0.01479 \\
\left(\frac{\Delta P_{f}}{L}\right)_{L O} & =\frac{f_{L O} G^{2}}{7.50 \times 10^{12} D_{i} s_{L} \phi_{L}}=\frac{0.01479(547,846)^{2}}{7.5 \times 10^{12} \times 0.835 \times 0.6237 \times 1.0} \\
\left(\frac{\Delta P_{f}}{L}\right)_{L O} & =0.001136 \mathrm{psi} / \mathrm{ft}
\end{aligned}
$$

Since the flow is turbulent, the Chisholm parameter is calculated using Equation (9.42) with $n=0.2314$.

$$
\begin{aligned}
& Y=\left(\rho_{L} / \rho_{V}\right)^{0.5}\left(\mu_{V} / \mu_{L}\right)^{n / 2}=(38.94 / 0.4787)^{0.5}(0.00885 / 0.177)^{0.1157} \\
& Y \cong 6.38
\end{aligned}
$$

Since $Y<9.5$, Equation (9.44) gives:

$$
B=1500 / G^{0.5}=1500 /(547,846)^{0.5} \cong 2.027
$$

The two-phase multiplier is calculated using Equation (9.43):

$$
\begin{aligned}
\phi_{L O}^{2} & =1+\left(Y^{2}-1\right)\left\{B[x(1-x)]^{(2-n) / 2}+x^{2-n}\right\} \\
& =1+\left[(6.38)^{2}-1\right]\left\{2.027[0.2(1-0.2)]^{0.8843}+(0.2)^{1.7686}\right\} \\
\phi_{L O}^{2} & \cong 19.22
\end{aligned}
$$

Finally, the two-phase friction loss is given by Equation (9.38):

$$
\left(\frac{\Delta P_{f}}{L}\right)_{t p}=\phi_{L O}^{2}\left(\frac{\Delta P_{f}}{L}\right)_{L O}=19.22 \times 0.001136 \cong 0.022 \mathrm{psi} / \mathrm{ft}
$$

(c) For the Friedel method, we need only recalculate $\phi_{L O}^{2}$ according to Equation (9.45). The parameters $E, F, H, F r$, and $W e$ are first calculated using Equations (9.47)-(9.52).

$$
\begin{aligned}
E & =(1-x)^{2}+x^{2}\left(\mu_{V} / \mu_{L}\right)^{n}\left(\rho_{L} / \rho_{V}\right) \\
& =(0.8)^{2}+(0.2)^{2}(0.00885 / 0.177)^{0.2314}(38.94 / 0.4787) \\
E & =2.2668 \\
F & =x^{0.78}(1-x)^{0.24}=(0.2)^{0.78}(0.8)^{0.24}=0.2701 \\
H & =\left(\rho_{L} / \rho_{V}\right)^{0.91}\left(\mu_{V} / \mu_{L}\right)^{0.19}\left(1-\mu_{V} / \mu_{L}\right)^{0.7} \\
& =(38.94 / 0.4787)^{0.91}(0.00885 / 0.177)^{0.19}(1-0.00885 / 0.177)^{0.7} \\
H & =29.896 \\
\rho_{t p} & =\left[x / \rho_{V}+(1-x) / \rho_{L}\right]^{-1}=[0.2 / 0.4787+0.8 / 38.94]^{-1} \\
\rho_{t p} & =2.2813 \mathrm{lbm} / \mathrm{ft}^{3} \\
F r & =\frac{G^{2}}{g D_{i} \rho_{t p}^{2}}=\frac{(547,846)^{2}}{4.17 \times 10^{8} \times 0.835(2.2813)^{2}}=165.63
\end{aligned}
$$

The surface tension must be converted to English units for consistency.

$$
\begin{aligned}
\sigma & =11.4 \text { dyne } / \mathrm{cm} \times 6.8523 \times 10^{-5}\left(\frac{\mathrm{lbf} / \mathrm{ft}}{\text { dyne } / \mathrm{cm}}\right)=7.812 \times 10^{-4} \mathrm{lbf} / \mathrm{ft} \\
W e & =\frac{G^{2} D_{i}}{g_{c} \rho_{t p} \sigma}=\frac{(547,846)^{2} \times 0.835}{4.17 \times 10^{8} \times 2.2813 \times 7.812 \times 10^{-4}} \\
W e & =337,227 \\
\phi_{L O}^{2} & =E+\frac{3.24 F H}{F r^{0.045} W e^{0.035}} \\
& =2.2668+\frac{3.24 \times 0.2701 \times 29.896}{(165.63)^{0.045}(337,227)^{0.035}} \\
\phi_{L O}^{2} & =15.58
\end{aligned}
$$

The two-phase friction loss is calculated using the value of $\left(\Delta P_{f} / L\right)_{L O}$ found in part (b):

$$
\left(\frac{\Delta P_{f}}{L}\right)_{t p}=\phi_{L O}^{2}\left(\frac{\Delta P_{f}}{L}\right)_{L O}=15.58 \times 0.001136 \cong 0.018 \mathrm{psi} / \mathrm{ft}
$$

(d) For the MSH method, the two-phase multiplier is calculated using Equation (9.53).

$$
\begin{aligned}
\phi_{L O}^{2} & =Y^{2} x^{3}+\left[1+2 x\left(Y^{2}-1\right)\right](1-x)^{1 / 3} \\
& =(6.38)^{2}(0.2)^{3}+\left[1+2 \times 0.2\left((6.38)^{2}-1\right)\right](1-0.2)^{1 / 3} \\
\phi_{L O}^{2} & \cong 16.00
\end{aligned}
$$

The two-phase friction loss is again given by Equation (9.38):

$$
\left(\frac{\Delta P_{f}}{L}\right)_{t p}=\phi_{L O}^{2}\left(\frac{\Delta P_{f}}{L}\right)_{L O}=16.00 \times 0.001136 \cong 0.018 \mathrm{psi} / \mathrm{ft}
$$

The predictions of the Friedel and MSH correlations are in very close agreement, while the Chisholm method predicts a value about $20 \%$ higher and the Lockhart-Martinelli prediction is about $80 \%$ higher.

### 9.4.3 Void fraction and two-phase density

## Void fraction

The void fraction, $\varepsilon_{V}$, is the fraction of the total volume that is occupied by the vapor phase. Since the two-phase density is the total mass (vapor and liquid) of fluid divided by the total volume of fluid, it follows that:

$$
\begin{equation*}
\rho_{t p}=\varepsilon_{V} \rho_{V}+\left(1-\varepsilon_{V}\right) \rho_{L} \tag{9.54}
\end{equation*}
$$

The void fraction is also equal to the fractional area of the conduit cross-section occupied by the vapor. This alternate interpretation is helpful in relating the void fraction to the vapor weight fraction, or quality, $x$. If we denote the average vapor velocity by $U_{V}$, then the mass flux of vapor is:

$$
\begin{equation*}
\rho_{V} U_{V}=\dot{m}_{V} / A_{V} \tag{9.55}
\end{equation*}
$$

where $A_{V}$ is the cross-sectional area occupied by the vapor phase. Since $x=\dot{m}_{V} / \dot{m}$, it follows that:

$$
\begin{equation*}
x / \rho_{V} U_{V}=\left(\dot{m}_{V} / \dot{m}\right)\left(A_{V} / \dot{m}_{V}\right)=A_{V} / \dot{m} \tag{9.56}
\end{equation*}
$$

Similarly, for the liquid phase:

$$
\begin{equation*}
(1-x) / \rho_{L} U_{L}=A_{L} / \dot{m} \tag{9.57}
\end{equation*}
$$

where $A_{L}$ is the cross-sectional area occupied by the liquid. Using Equations (9.56) and (9.57) we obtain the void fraction as follows:

$$
\begin{equation*}
\frac{x / \rho_{V} U_{V}}{x / \rho_{V} U_{V}+(1-x) / \rho_{L} U_{L}}=\frac{A_{V} / \dot{m}}{A_{V} / \dot{m}+A_{L} / \dot{m}}=\frac{A_{V}}{A_{V}+A_{L}}=\varepsilon_{V} \tag{9.58}
\end{equation*}
$$

Rearranging this equation yields:

$$
\begin{equation*}
\varepsilon_{V}=\frac{x}{x+S R(1-x) \rho_{V} / \rho_{L}} \tag{9.59}
\end{equation*}
$$

where $S R \equiv U_{V} / U_{L}$ is the slip ratio. A flow model or empirical correlation is required to evaluate $S R$.

## Homogeneous flow model

If homogeneous flow is assumed, both phases have the same velocity and $S R=1$. Therefore,

$$
\begin{equation*}
\varepsilon_{V}=\frac{x}{x+(1-x) \rho_{V} / \rho_{L}} \tag{9.60}
\end{equation*}
$$

Substituting this result in Equation (9.54) and rearranging leads to the following expression for the two-phase density:

$$
\rho_{t p}=\left[x / \rho_{V}+(1-x) / \rho_{L}\right]^{-1}
$$

This equation was given previously in connection with the Friedel correlation as Equation (9.51).
The homogeneous model generally gives reliable results for the mist flow and bubbly flow regimes where the velocities of the two phases do not differ greatly. For other flow regimes, it tends to overestimate the void fraction, which causes the two-phase density to be underestimated. One of the following methods should be used in these cases.

## Lockhart-Martinelli correlation

In their classic paper, Lockhart and Martinelli [16] presented a single correlation for void fraction covering all four laminar-turbulent combinations. Their graphical correlation can be represented analytically by the following equation:

$$
\begin{equation*}
\varepsilon_{V}=\frac{\phi_{L}-1}{\phi_{L}} \tag{9.61}
\end{equation*}
$$

where $\phi_{L}$ is calculated for the turbulent-turbulent case using Equation (9.28). Substituting the above expression for $\varepsilon_{V}$ in Equation (9.54) yields the following equation for the two-phase density:

$$
\begin{equation*}
\rho_{t p}=\frac{\rho_{L}+\left(\phi_{L}-1\right) \rho_{V}}{\phi_{L}} \tag{9.62}
\end{equation*}
$$

## The Chisholm correlation

Chisholm [24] presented the following simple correlation for the slip ratio:

$$
\begin{align*}
S R & =\left(\rho_{L} / \rho_{h o m}\right)^{0.5} & & \text { for } X>1 \\
& =\left(\rho_{L} / \rho_{V}\right)^{0.25} & & \text { for } X \leq 1 \tag{9.63}
\end{align*}
$$

where $X$ is the Lockhart-Martinelli parameter and $\rho_{h o m}$ is the homogeneous two-phase density given by Equation (9.51). This correlation is valid for flow in both vertical and horizontal tubes over a wide range of conditions, including void fractions from zero to unity. Chisholm states that in a test of 14 methods it proved to be the best for density prediction.

## The CISE correlation

The CISE correlation was devised by Premoli et al. [25] so as to provide the correct asymptotic behavior for the slip ratio as various fluid properties and flow parameters approach their theoretical limits. The correlation is based on experimental data for upward flow in vertical channels. The equation for the slip ratio is:

$$
\begin{equation*}
S R=1+E_{1}\left[\left(\frac{y}{1+y E_{2}}\right)+y E_{2}\right]^{0.5} \tag{9.64}
\end{equation*}
$$

where

$$
\begin{equation*}
y=\frac{\left(\varepsilon_{V}\right)_{h o m}}{1-\left(\varepsilon_{V}\right)_{h o m}} \tag{9.65}
\end{equation*}
$$

$\left(\varepsilon_{V}\right)_{\text {hom }}=$ homogeneous void fraction from Equation (9.60)

$$
\begin{align*}
& E_{1}=1.578 R e_{L O}^{-0.19}\left(\rho_{L} / \rho_{V}\right)^{0.22}  \tag{9.66}\\
& E_{2}=0.0273 W e_{L O} R e_{L O}^{-0.51}\left(\rho_{L} / \rho_{V}\right)^{-0.08} \tag{9.67}
\end{align*}
$$

As the subscripts indicate, both the Reynolds and Weber numbers in this correlation are computed using the total mass flux, $G$, and physical properties of the liquid phase.

In the article by Premoli et al. [25], the last term in square brackets in Equation (9.64) was incorrectly printed with a minus sign in place of the plus sign, and this typographical error has been repeated many times in the subsequent literature. The plus sign is required on theoretical grounds in order for the slip ratio to exhibit the correct asymptotic behavior, and to prevent the square root of negative numbers from occurring at low Reynolds numbers or high Weber numbers. It is also needed to reproduce the graphical results presented in Ref. [25].

## Example 9.6

Calculate the void fraction and two-phase density for the reboiler return line of Example 9.5 using:
(a) The homogeneous flow model.
(b) The Lockhart-Martinelli correlation.
(c) The Chisholm correlation.
(d) The CISE correlation.

## Solution

(a) For the homogeneous flow model, the void fraction is given by Equation (9.60):

$$
\begin{aligned}
& \varepsilon_{V}=\frac{x}{x+(1-x) \rho_{V} / \rho_{L}}=\frac{0.2}{0.2+0.8(0.4787 / 38.94)} \\
& \varepsilon_{V}=0.9531
\end{aligned}
$$

The two-phase density can be calculated using either Equation (9.54) or (9.51). The latter was used in Example 9.5 to obtain $\rho_{t p}=2.2813 \mathrm{lbm} / \mathrm{ft}^{3}$. Using Equation (9.54) we obtain:

$$
\begin{aligned}
\rho_{t p} & =\varepsilon_{V} \rho_{V}+\left(1-\varepsilon_{V}\right) \rho_{L}=0.9531 \times 0.4787+(1-0.9531) \times 38.94 \\
\rho_{t p} & =2.2825 \cong 2.28 \mathrm{lbm} / \mathrm{ft}^{3}
\end{aligned}
$$

The difference between the two values of $\rho_{t p}$ is due to round-off error in the value of $\varepsilon_{V}$, and is negligible.
(b) A value of $\phi_{L}^{2}=43.07$ was calculated in Example 9.5, giving $\phi_{L}=6.5628$. The void fraction is computed from Equation (9.61):

$$
\varepsilon_{V}=\left(\phi_{L}-1\right) / \phi_{L}=(6.5628-1) / 6.5628=0.8476
$$

The two-phase density is calculated using Equation (9.62):

$$
\begin{aligned}
& \rho_{t p}=\frac{\rho_{L}+\left(\phi_{L}-1\right) \rho_{V}}{\phi_{L}}=\frac{38.94+(6.5628-1) \times 0.4787}{6.5628} \\
& \rho_{t p}=6.3392 \cong 6.34 \mathrm{lbm} / \mathrm{ft}^{3}
\end{aligned}
$$

(c) From Example 9.5, the Lockhart-Martinelli parameter is $X_{t t}=0.521<1$. Therefore, Equation (9.63) gives:

$$
S R=\left(\rho_{L} / \rho_{V}\right)^{0.25}=(38.94 / 0.4787)^{0.25}=3.0032
$$

Substitution into Equation (9.59) gives the void fraction:

$$
\begin{aligned}
& \varepsilon_{V}=\frac{x}{x+S R(1-x) \rho_{V} / \rho_{L}}=\frac{0.2}{0.2+3.0032 \times 0.8 \times 0.4787 / 38.94} \\
& \varepsilon_{V}=0.8713
\end{aligned}
$$

The two-phase density is obtained from Equation (9.54).

$$
\begin{aligned}
& \rho_{t p}=\varepsilon_{V} \rho_{V}+\left(1-\varepsilon_{V}\right) \rho_{L}=0.8713 \times 0.4787+(1-0.8713) \times 38.94 \\
& \rho_{t p}=5.4287 \cong 5.43 \mathrm{lbm} / \mathrm{ft}^{3}
\end{aligned}
$$

(d) The following values are obtained from Example 9.5:

$$
\begin{aligned}
D_{i} & =0.835 \mathrm{ft} \\
\sigma & =7.812 \times 10^{-4} \mathrm{lbf} / \mathrm{ft} \\
G & =547,846 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\operatorname{Re}_{L O} & =1,068,405
\end{aligned}
$$

The Weber number is calculated as follows:

$$
W e_{L O}=\frac{G^{2} D_{i}}{g_{c} \rho_{L} \sigma}=\frac{(547,846)^{2} \times 0.835}{4.17 \times 10^{8} \times 38.94 \times 7.812 \times 10^{-4}}=19,756
$$

The parameters in the CISE correlation are calculated using Equations (9.65) to (9.67). From part (a), the homogeneous void fraction is $\left(\varepsilon_{V}\right)_{\text {hom }}=0.9531$.

$$
\begin{aligned}
y & =\frac{\left(\varepsilon_{V}\right)_{h o m}}{1-\left(\varepsilon_{V}\right)_{h o m}}=\frac{0.9531}{1-0.9531}=20.322 \\
E_{1} & =1.578 R e_{L O}^{-0.19}\left(\rho_{L} / \rho_{V}\right)^{0.22}=1.578(1,068,405)^{-0.19}(38.94 / 0.4787)^{0.22} \\
E_{1} & =0.2973 \\
E_{2} & =0.0273 W e_{L O} R e_{L O}^{-0.51}\left(\rho_{L} / \rho_{V}\right)^{-0.08} \\
& =0.0273 \times 19,756(1,068,405)^{-0.51}(38.94 / 0.4787)^{-0.08} \\
E_{2} & =0.3194
\end{aligned}
$$

The slip ratio is calculated from Equation (9.64):

$$
\begin{aligned}
S R & =1+E_{1}\left[\left(\frac{y}{1+y E_{2}}\right)+y E_{2}\right]^{0.5} \\
& =1+0.2973\left[\frac{20.322}{1+20.322 \times 0.3194}+20.322 \times 0.3194\right]^{0.5} \\
S R & =1.9013
\end{aligned}
$$

The void fraction is calculated using Equation (9.59):

$$
\begin{aligned}
& \varepsilon_{V}=\frac{x}{x+S R(1-x) \rho_{V} / \rho_{L}}=\frac{0.2}{0.2+1.9013 \times 0.8 \times 0.4787 / 38.94} \\
& \varepsilon_{V}=0.9145
\end{aligned}
$$

Finally, the two-phase density is calculated using Equation (9.54).

$$
\begin{aligned}
\rho_{t p} & =\varepsilon_{V} \rho_{V}+\left(1-\varepsilon_{V}\right) \rho_{L}=0.9145 \times 0.4787+(1-0.9145) \times 38.94 \\
\rho_{t p} & =3.7671 \cong 3.77 \mathrm{lbm} / \mathrm{ft}^{3}
\end{aligned}
$$

Notice that while the void fractions predicted by the four methods are within about $12 \%$ of one another, the two-phase densities differ by large percentages.

### 9.4.4 Other losses

Pressure losses due to valves, fittings, expansions, and contractions can be calculated using flow resistance coefficients that specify the number of velocity heads corresponding to the loss in each element of a pipeline. Methods for estimating these coefficients for two-phase flow can be found in Refs. [2,8,24,26].

A more expedient approach is commonly used in design work, namely, the equivalent length concept. The equivalent length of a piping element is the length of straight pipe that generates the same pressure loss as the given valve, fitting, etc. Tables of equivalent lengths used for single-phase flow are assumed to be valid for two-phase flow as well, and are used to determine the effective length of a pipeline in the usual manner by summing the equivalent lengths of all fittings, etc. and the lengths of all straight sections of pipe. The effective pipe length is then multiplied by the two-phase pressure gradient to obtain the total pressure loss. Although equivalent lengths for two-phase flow tend to be somewhat higher than for single-phase flow [26], the longstanding use of this method for industrial design work indicates that it is generally reliable, at least in the context of two-phase flow calculations, which, as previously noted, involve a significant level of uncertainty. Computational details are given in Chapter 10.

### 9.4.5 Recommendations

The MSH correlation is recommended for calculating two-phase pressure drop, while the Chisholm method is recommended for calculating two-phase density. These methods are easy to use, applicable over a wide range of conditions, and are among the more reliable of their respective genres.

### 9.5 Convective Boiling in Tubes

### 9.5.1 Boiling regimes in a vertical tube

Figure 9.3 depicts the variation in flow regime and heat-transfer coefficient for convective boiling in a vertical tube. The fluid enters the tube as a subcooled liquid, and initially heat is transferred by convection alone. With the onset of boiling and the establishment of the bubbly flow regime, the heat-transfer coefficient starts to rise sharply as the nucleate boiling mechanism contributes to the heat transfer. As the vapor fraction increases, the flow regime changes from bubbly to slug flow, and then to annular flow (the churn flow regime is omitted here) while the heat-transfer coefficient continues to increase. Eventually, the amount of liquid is reduced to the point where dry spots begin to appear on the tube wall, and the heat-transfer coefficient begins to decrease. It continues to decrease until the tube wall is completely dry and all remaining liquid is in the form of droplets entrained in the vapor phase (mist flow regime). The heat-transfer coefficient remains relatively constant as the droplets are gradually vaporized and the vapor becomes superheated. In the final stages, heat is transferred solely by gas-phase convection.

In vertical thermosyphon reboilers, which employ the configuration shown in Figure 9.3, the vapor fraction is kept sufficiently low that the mist flow regime does not occur and the sharp drop in heat-transfer coefficient is avoided. Nevertheless, the rate of heat transfer can vary greatly over the length of the reboiler, and an incremental analysis is therefore required to accurately predict performance.


Figure 9.3 Convective boiling in a vertical tube (Source: Ref. [1]).

### 9.5.2 The Chen correlation

The correlation developed by Chen [27] has been the most widely used method for calculating heat-transfer coefficients in convective boiling. Chen assumed that the convective and nucleate boiling contributions to heat transfer were additive. However, it is known that convection tends to suppress nucleate boiling. Chen attributed this effect to the steepening of the temperature gradient near the wall with increasing flow rate, which reduces the effective temperature difference between the tube wall and bubbles growing outward from the wall. He therefore introduced a suppression factor, $S_{C H}$, that is the ratio of the effective temperature difference for bubble growth to the overall temperature difference, $T_{w}-T_{\text {sat }}$.

Chen also expressed the convective heat-transfer coefficient in terms of the coefficient, $h_{L}$, for the liquid flowing alone in the tube. Thus,

$$
\begin{equation*}
h_{f c}=F\left(X_{t t}\right) h_{L} \tag{9.68}
\end{equation*}
$$

where
$h_{f c}=$ two-phase convective heat-transfer coefficient
$h_{L}=$ convective heat-transfer coefficient for liquid phase flowing alone
$F\left(X_{t t}\right)=$ function of Lockhart-Martinelli parameter

Chen's graphs for $S_{C H}$ and $F\left(X_{t t}\right)$, which were based on experimental data, have been replaced by curve-fit equations to obtain the following form of the Chen correlation (2):

$$
\begin{equation*}
h_{b}=S_{C H} h_{n b}+F\left(X_{t t}\right) h_{L} \tag{9.69}
\end{equation*}
$$

where

$$
\begin{array}{rlr}
h_{b} & =\text { convective boiling heat-transfer coefficient } \\
h_{n b} & =\text { nucleate boiling heat-transfer coefficient } \\
S_{C H} & =\left(1+2.53 \times 10^{-6} R e^{1.17}\right)^{-1} \\
F\left(X_{t t}\right) & =2.35\left(X_{t t}^{-1}+0.213\right)^{0.736} & \left(X_{t t}<10\right) \\
& =1.0 & \left(X_{t t} \geq 10\right)  \tag{9.72}\\
R e & =\operatorname{Re}_{L}\left[F\left(X_{t t}\right)\right]^{1.25} &
\end{array}
$$

The heat flux is given by:

$$
\begin{equation*}
\hat{q}=h_{b}\left(T_{w}-T_{s a t}\right) \tag{9.73}
\end{equation*}
$$

Although Chen developed his correlation for saturated boiling, it has been applied to subcooled boiling as well. The latter occurs when the bulk liquid temperature is below the saturation temperature, but the tube-wall temperature is high enough for vapor bubbles to form and grow. In this case, the suppression factor is computed by setting $R e=R e_{L}$ in Equation (9.70), and the heat flux is calculated as follows [2]:

$$
\begin{equation*}
\hat{q}=S_{C H} h_{n b}\left(T_{w}-T_{s a t}\right)+h_{L}\left(T_{w}-T_{b}\right) \tag{9.74}
\end{equation*}
$$

where $T_{b}$ is the bulk liquid temperature.
The convective coefficient, $h_{L}$, can be calculated using any appropriate correlation for forced convection in pipes and ducts, such as the Seider-Tate equation (Chapter 2). However, Chen [27] used the Dittus-Boelter equation, a predecessor of the Seider-Tate equation for turbulent flow, as follows:

$$
\begin{equation*}
h_{L}=0.023\left(k_{L} / D_{i}\right) R e_{L}^{0.8} \operatorname{Pr}_{L}^{0.4} \tag{9.75}
\end{equation*}
$$

Note that the Reynolds number in this equation is calculated using the flow rate of the liquid phase alone.

Chen used the Forster-Zuber correlation for the nucleate boiling heat-transfer coefficient. In order to obtain a conservative estimate for mixtures, however, Palen [4] suggested using the Mostinski correlation together with the mixture correction factor given by Equation (9.17).

Although the Chen correlation was developed using a limited amount of experimental data (for water, methanol, benzene, cyclohexane, pentane, and heptane, all in vertical tubes), it has a sound physical basis and reduces correctly in the limiting cases of zero flow rate ( $S_{C H}=1$ ), infinite flow rate $\left(S_{C H} \rightarrow 0\right)$, and zero vapor fraction $\left[F\left(X_{t t}\right)=1.0\right]$, characteristics not always found in later correlations. It has also been widely used for many years, and is still the standard of comparison for new correlations.

### 9.5.3 The Gungor-Winterton correlation

The correlation of Gungor and Winterton [28] is similar in form to the Chen correlation in that the nucleate boiling and convection terms are additive. A nucleate boiling suppression factor is included, along with a convective enhancement factor, $E_{G W}$, to account for the effect of boiling on the convective heat transfer. The correlation is as follows:

$$
\begin{equation*}
h_{b}=S_{G W} h_{n b}+E_{G W} h_{L} \tag{9.76}
\end{equation*}
$$

$$
\begin{align*}
S_{G W} & =\left(1+1.15 \times 10^{-6} E_{G W}^{2} R e_{L}^{1.17}\right)^{-1}  \tag{9.77}\\
E_{G W} & =1+24,000 B o^{1.16}+1.37 X_{t t}^{-0.86} \tag{9.78}
\end{align*}
$$

The boiling number, Bo, is defined by the following equation:

$$
\begin{equation*}
B o=\frac{\hat{q}}{\lambda G} \tag{9.79}
\end{equation*}
$$

For horizontal tubes and $F r_{L O}<0.05, S_{G W}$ is to be multiplied by $F r_{L O}^{0.5}$, and $E_{G W}$ is to be multiplied by $F r_{L O}^{\left(0.1-2 F r_{L O}\right)}$. The nucleate boiling heat-transfer coefficient is calculated using the Cooper correlation, and the Dittus-Boelter equation is used for the forced convection coefficient.

For subcooled boiling, Equation (9.74) is used with $S_{C H}$ replaced by $S_{G W}$. Liquid properties are evaluated at $T_{s a t}$ for saturated boiling and at $T_{b}$ for subcooled boiling. The correlation was developed using a database consisting of approximately 3700 data points for water, ethylene glycol, and five refrigerants.

Due to the boiling number term in Equation (9.79), the enhancement factor does not reduce to unity when the vapor fraction is zero. Nevertheless, the correlation provides a relatively good representation of the data upon which it is based, particularly for refrigerants in the saturated boiling regime. The constants in Equations (9.77) and (9.78) were determined by a complex iterative regression procedure, and the nucleate and convective terms are strongly coupled through Equation (9.77). Therefore, it is not advisable to substitute another nucleate boiling correlation for the Cooper correlation in this method.

### 9.5.4 The Liu-Winterton correlation

The correlation developed by Liu and Winterton [29] is described by the following equations:

$$
\begin{align*}
h_{b} & =\left[\left(S_{L W} h_{n b}\right)^{2}+\left(E_{L W} h_{L}\right)^{2}\right]^{1 / 2}  \tag{9.80}\\
S_{L W} & =\left[1+0.055 E_{L W}^{0.1} R e_{L}^{0.16}\right]^{-1}  \tag{9.81}\\
E_{L W} & =\left[1+x \operatorname{Pr}_{L}\left(\rho_{L}-\rho_{V} / \rho_{V}\right]^{0.35}\right. \tag{9.82}
\end{align*}
$$

For horizontal tubes, the low Froude number corrections are applied to $S_{L W}$ and $E_{L W}$ as in the Gungor-Winterton method. The Cooper and Dittus-Boelter correlations are used to calculate $h_{n b}$ and $h_{L}$. Notice that the enhancement factor, $E_{L W}$, correctly reduces to unity when the vapor fraction, $x$, is zero.
Equation (9.80) is a special case of the general formula:

$$
\begin{equation*}
h_{b}=\left[\left(a h_{n b}\right)^{m}+\left(b h_{f c}\right)^{m}\right]^{1 / m} \tag{9.83}
\end{equation*}
$$

where $1 \leq m<\infty$. Formulas of this type provide a smooth transition between two limiting cases, in this instance between forced convection and nucleate boiling. The abruptness of the transition is governed by the size of the exponent, with larger values of $m$ resulting in more abrupt transitions. This approach has been used to develop many very successful correlations for heat, mass, and momentum transport, as exemplified by the Churchill correlations presented in Chapter 2.

The Liu-Winterton correlation was developed using the same database as used for the GungorWinterton correlation. It provides a significantly better fit to the data than the latter correlation in both the saturated and subcooled boiling regimes.

### 9.5.5 Other correlations

More complex correlations have been developed by Shah [30], Kandlikar [31], Steiner and Taborek [32], and Kattan et al. [33]. The Shah correlation appears to be no more reliable than the simpler methods given above. The Kandlikar correlation provides a good representation of test data, but it contains a fluid-specific parameter, values of which are given only for a small number of fluids. The Steiner-Taborek correlation takes the form of Equation (9.83) with $a=b=1$ and $m=3$. It was developed using a database containing over 13,000 data points for water, three alcohols, four hydrocarbons, four refrigerants, ammonia, nitrogen, and helium. All data are for convective boiling in vertical tubes. Although this method is among the best currently available in the open literature, the overall computational procedure is rather complicated and to some extent fluid specific. The correlation of Kattan et al. is based on data for five refrigerants flowing in horizontal tubes, and is restricted to vapor fractions above 0.15 . Equation (9.83) is used with $a=b=1$ and $m=3$, and the Cooper correlation is used to calculate the nucleate boiling coefficient. Different models are used to calculate the heat-transfer coefficient in each of four flow regimes: annular, stratified, stratified-wavy, and annular flow with partial dryout at high vapor fractions.

All convective boiling correlations are developed and tested with experimental data for pure components, or in some cases, binary mixtures. Even for pure component boiling, they are not highly reliable when applied beyond the range of data used in their development. For the complex, often very non-ideal mixtures encountered in chemical and petroleum processing, their performance is still more problematic. Therefore, a relatively conservative approach to design, such as the use of Palen's method for nucleate boiling of mixtures in conjunction with Chen's method, seems warranted. Note, however, that while this procedure will provide a conservative estimate for the nucleate boiling coefficient, the end result may not be conservative if the convective contribution or the suppression factor is overestimated by Chen's method. For pure components, and refrigerants in particular, the Liu-Winterton correlation is likely to be more reliable than the Chen correlation.

## Example 9.7

The fluid of Example 9.1 boils while flowing vertically upward through a 1-in., 14 BWG tube (ID $=2.12 \mathrm{~cm}$ ) with a mass flux of $300 \mathrm{~kg} / \mathrm{m}^{2} \cdot \mathrm{~s}$. At a point in the tube where the wall temperature is 453.7 K , the pressure is 310.3 kPa and the quality is 0.2 , calculate the heat-transfer coefficient using:
(a) Chen's method.
(b) Chen's method with the Mostinski correlation for nucleate boiling.
(c) The Gungor-Winterton correlation.
(d) The Liu-Winterton correlation.

## Solution

(a) The first step is to calculate the heat-transfer coefficient for forced convection using Equation (9.75). The Reynolds number is based on the flow rate of the liquid phase alone, and fluid properties are obtained from Example 9.1.

$$
\begin{aligned}
R e_{L} & =\frac{D_{i} G_{L}}{\mu_{L}}=\frac{0.0212 \times 0.8 \times 300}{156 \times 10^{-6}}=32,615 \\
\operatorname{Pr}_{L} & =\frac{C_{P, L} \mu_{L}}{k_{L}}=\frac{2730 \times 156 \times 10^{-6}}{0.086}=4.9521 \\
h_{L} & =0.023\left(k_{L} / D_{i}\right) \operatorname{Re}_{L}^{0.8} P_{r}^{0.4} \\
& =0.023(0.086 / 0.0212)(32,615)^{0.8}(4.9521)^{0.4} \\
h_{L} & =722 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

Next, the Lockhart-Martinelli parameter is calculated using Equation (9.37).

$$
\begin{aligned}
X_{t t} & =\left(\frac{1-x}{x}\right)^{0.9}\left(\rho_{V} / \rho_{L}\right)^{0.5}\left(\mu_{L} / \mu_{L}\right)^{0.1} \\
& =(0.8 / 0.2)^{0.9}(18.09 / 567)^{0.5}\left(156 \times 10^{-6} / 7.11 \times 10^{-6}\right)^{0.1} \\
X_{t t} & =0.847
\end{aligned}
$$

Equation (9.71) is used to calculate $F\left(X_{t t}\right)$. Since $X_{t t}<10$, we have:

$$
\begin{aligned}
& F\left(X_{t t}\right)=2.35\left(X_{t t}^{-1}+0.213\right)^{0.736}=2.35\left[(0.847)^{-1}+0.213\right]^{0.736} \\
& F\left(X_{t t}\right)=3.00
\end{aligned}
$$

Equations (9.72) and (9.70) are used to calculate the suppression factor.

$$
\begin{aligned}
R e & =\operatorname{Re}_{L}\left[F\left(X_{t t}\right)\right]^{1.25}=32,615(3.00)^{1.25}=128,771 \\
S_{C H} & =\left(1+2.53 \times 10^{-6} R e^{1.17}\right)^{-1}=\left[1+2.53 \times 10^{-6}(128,771)^{1.17}\right]^{-1} \\
S_{C H} & =0.2935
\end{aligned}
$$

In Example 9.1, the Forster-Zuber correlation was used to obtain $h_{n b}=5,512 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$, and this value is still valid here. Therefore, $h_{b}$ can be found by substituting in Equation (9.69):

$$
\begin{aligned}
& h_{b}=S_{C H} h_{n b}+F\left(X_{t t}\right) h_{L}=0.2935 \times 5512+3.00 \times 722 \\
& h_{b}=3784 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

(b) The values of $h_{L}, F\left(X_{t t}\right)$, and $S_{C H}$ are the same as in part (a). The Mostinski correlation in the form of Equation (9.3) was used in Example 9.1 to calculate the nucleate boiling heattransfer coefficient. However, Equation (9.3) was derived from Equation (9.2) by substituting $\hat{q}=h_{n b} \Delta T_{e}$, which for convective boiling is replaced by $\hat{q}=h_{b} \Delta T_{e}$. Therefore, the calculation must be repeated using Equation (9.2b).

$$
h_{n b}=0.00417 P_{c}^{0.69} \hat{q}^{0.7} F_{P}
$$

Using Palen's recommendation for the pressure correction factor, we obtain $F_{P}=1.3375$ from Example 9.1, part (c). Also, $P_{c}=2500 \mathrm{kP}_{\mathrm{a}}$ as given in Example 9.1. Thus,

$$
\begin{aligned}
& h_{n b}=0.00417(2500)^{0.69} \hat{q}^{0.7} \times 1.3375 \\
& h_{n b}=1.2331 \hat{q}^{0.7}
\end{aligned}
$$

Substituting in Equation (9.69) gives:

$$
\begin{aligned}
h_{b} & =S_{C H} h_{n b}+F\left(X_{t t}\right) h_{L} \\
& =0.2935 \times 1.2331 \hat{q}^{0.7}+3.00 \times 722 \\
h_{b} & =0.3619 \hat{q}^{0.7}+2166
\end{aligned}
$$

Since $\Delta T_{e}=16.2 \mathrm{~K}$ from Example 9.1,

$$
\begin{aligned}
& \hat{q}=h_{b} \Delta T_{e}=\left(0.3619 \hat{q}^{0.7}+2166\right) \times 16.2 \\
& \hat{q}=5.8628 \hat{q}^{0.7}+35,089.2 \\
& \hat{q}-5.8628 \hat{q}^{0.7}-35,089.2=0
\end{aligned}
$$

Using the nonlinear equation solver on a TI-80 series calculator, the solution to this equation is found to be $\hat{q}=45,826 \mathrm{~W} / \mathrm{m}^{2}$. The heat-transfer coefficient is obtained from this value as follows:

$$
h_{b}=\hat{q} / \Delta T_{e}=45,826 / 16.2=2829 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
$$

(c) The following results from part (a) apply here as well:

$$
\begin{aligned}
R e_{L} & =32,615 \\
h_{L} & =722 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} \\
X_{t t} & =0.847
\end{aligned}
$$

Also, from Example 9.1, the latent heat of vaporization is $272,000 \mathrm{~J} / \mathrm{kg}$.
The boiling number is given by Equation (9.79):

$$
B_{o}=\frac{\hat{q}}{\lambda G}=\frac{\hat{q}}{272,000 \times 300}=1.2255 \times 10^{-8} \hat{q}
$$

The convective enhancement factor is computed by substituting in Equation (9.78).

$$
\begin{align*}
E_{G W} & =1+24,000 B o^{1.16}+1.37 X_{t t}^{-0.86} \\
& =1+24,000\left(1.2255 \times 10^{-8} \hat{q}\right)^{1.16}+1.37(0.847)^{-0.86} \\
& =1+1.5946 \times 10^{-5} \hat{q}^{1.16}+1.5803 \\
E_{G W} & =2.5803+1.5946 \times 10^{-5} \hat{q}^{1.16} \tag{i}
\end{align*}
$$

The suppression factor is computed using Equation (9.77).

$$
\begin{align*}
S_{G W} & =\left(1+1.15 \times 10^{-6} E_{G W}^{2} R e_{L}^{1.17}\right)^{-1} \\
& =\left(1+1.15 \times 10^{-6} E_{G W}^{2}(32,615)^{1.17}\right)^{-1} \\
S_{G W} & =\left(1+0.2195 E_{G W}^{2}\right)^{-1} \tag{ii}
\end{align*}
$$

The Cooper nucleate boiling correlation in SI units is given by Equation (9.6b):

$$
h_{n b}=55 \hat{q}^{0.67} P_{r}^{0.12}\left(-\log _{10} P_{r}\right)^{-0.55} M^{-0.5}
$$

From Example 9.1, $P_{r}=0.1217$ and the molecular weight is 110.37 . Substitution gives:

$$
\begin{aligned}
& h_{n b}=55 \hat{q}^{0.67}(0.1217)^{0.12}\left(-\log _{10} 0.1217\right)^{-0.55}(110.37)^{-0.5} \\
& h_{n b}=4.2704 \hat{q}^{0.67}
\end{aligned}
$$

Substituting in Equation (9.76) gives the following result for $h_{b}$ :

$$
\begin{aligned}
& h_{b}=S_{G W} h_{n b}+E_{G W} h_{L} \\
& h_{b}=4.2704 S_{G W} \hat{q}^{0.67}+722 E_{G W}
\end{aligned}
$$

The equation for the heat flux is obtained as follows:

$$
\begin{align*}
& \hat{q}=h_{b} \Delta T_{e}=h_{b} \times 16.2 \\
& \hat{q}=69.1805 S_{G W} \hat{q}^{0.67}+11,696.4 E_{G W} \\
& \hat{q}-69.1805 S_{G W} \hat{q}^{0.67}-11,696.4 E_{G W}=0 \tag{iii}
\end{align*}
$$

Equation (iii) is to be solved in conjunction with Equations (i) and (ii) for the heat flux. However, these equations have no real solution, as the reader can verify using the nonlinear equation solver on a TI calculator or by graphing the left side of Equation (iii). The crux of the problem is the term involving the boiling number in the enhancement factor, which, as previously noted, is not physically realistic. Therefore, the Gungor-Winterton correlation cannot be used to solve this problem.
(d) The following results from part (a) are applicable:

$$
\begin{aligned}
R e_{L} & =32,615 \quad h_{L}=722 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K} \\
P r_{L} & =4.9521
\end{aligned}
$$

The enhancement and suppression factors are calculated from Equations (9.82) and (9.81).

$$
\begin{aligned}
E_{L W} & =\left[1+x \operatorname{Pr}_{L}\left(\rho_{L}-\rho_{V}\right) / \rho_{V}\right]^{0.35} \\
& =[1+0.2 \times 4.9521(567-18.09) / 18.09]^{0.35} \\
E_{L W} & =3.3284 \\
S_{L W} & =\left[1+0.055 E_{L W}^{0.1} R e_{L}^{0.16}\right]^{-1} \\
& =\left[1+0.055(3.3284)^{0.1}(32,615)^{0.16}\right]^{-1} \\
S_{L W} & =0.7535
\end{aligned}
$$

From part (c), the Cooper correlation gives:

$$
h_{n b}=4.2704 \hat{q}^{0.67}
$$

Substituting in Equation (9.80) for the convective boiling coefficient gives:

$$
\begin{aligned}
h_{b} & =\left\{\left(S_{L W} h_{n b}\right)^{2}+\left(E_{L W} h_{L}\right)^{2}\right\}^{1 / 2} \\
& =\left\{\left(0.7535 \times 4.2704 \hat{q}^{0.67}\right)^{2}+(3.3284 \times 722)^{2}\right\}^{1 / 2} \\
h_{b} & =\left\{10.3539 \hat{q}^{1.34}+5,774,913\right\}^{1 / 2}
\end{aligned}
$$

Setting $h_{b}=\hat{q} / \Delta T_{e}$ gives the following nonlinear equation for the heat flux:

$$
\frac{\hat{q}}{16.2}-\left(10.3539 \hat{q}^{1.34}+5,774,913\right)^{0.5}=0
$$

Using the nonlinear equation solver on a TI calculator, the solution is found to be $\hat{q}=172,788 \mathrm{~W} / \mathrm{m}^{2}$. Thus, the heat-transfer coefficient is:

$$
h_{b}=\hat{q} / \Delta T_{e}=172,788 / 16.2=10,666 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
$$

This value is much higher than the one obtained with the Chen correlation, primarily due to the difference in the nucleate boiling terms. Recall that in Example 9.1 the Cooper correlation predicted a much higher value for the nucleate boiling heat-transfer coefficient than either the Forster-Zuber or Mostinski correlation.

### 9.5.6 Critical heat flux

At low vapor fractions, the mechanism responsible for critical heat flux in convective boiling is essentially the same as in pool boiling. At high vapor fractions, the phenomenon is caused by dryout of the tube wall due to depletion of the liquid phase. The transition between the two mechanisms is gradual, however, and there is no clear demarcation between them. In horizontal tubes, dryout occurs at lower heat fluxes than in vertical tubes under the same conditions because the liquid preferentially accumulates on the bottom of the tube, allowing the upper portion of the tube wall to dry more readily.

## Vertical tubes

The majority of the work on critical heat flux in convective boiling has been done with water due to the importance of the problem in relation to nuclear reactor cooling systems. Two methods that have been tested on a variety of fluids for flow in vertical tubes are presented here. The following simple correlation for vertical thermosyphon reboilers was given by Palen [4]:

$$
\begin{equation*}
\hat{q}_{c}=16,070\left(D^{2} / L\right)^{0.35} P_{c}^{0.61} P_{r}^{0.25}\left(1-P_{r}\right) \tag{9.84a}
\end{equation*}
$$

where
$\hat{q}_{c}=$ critical heat flux, $\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$
$D=$ tube ID, ft
$L=$ tube length, ft
$P_{r}=$ reduced pressure in tube
$P_{c}=$ critical pressure of fluid, psia
The corresponding relationship in SI units is:

$$
\begin{equation*}
\hat{q}_{c}=23,660\left(D^{2} / L\right)^{0.35} P_{c}^{0.61} P_{r}^{0.25}\left(1-P_{r}\right) \tag{9.84b}
\end{equation*}
$$

where
$\hat{q}_{c} \propto \mathrm{~W} / \mathrm{m}^{2}$
$D, L \propto \mathrm{~m}$
$P_{c} \propto \mathrm{kPa}$
The correlation of Katto and Ohno [34] is considerably more complicated and rather cumbersome to state. The critical heat flux is given by the following equation:

$$
\begin{equation*}
\hat{q}_{c}=\hat{q}_{o}\left(1+\Gamma \Delta H_{i n} / \lambda\right) \tag{9.85}
\end{equation*}
$$

where
$\hat{q}_{o}=$ basic critical heat flux
$\Gamma=$ inlet subcooling parameter
$\Delta H_{\text {in }}=$ inlet enthalpy of subcooling
$\lambda=$ latent heat of vaporization
The following five equations are used in determining the value of $\hat{q}_{0}$ :

$$
\begin{align*}
& \frac{\hat{q}_{o A}}{G \lambda}=C_{2}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{0.043}(L / D)^{-1}  \tag{9.86}\\
& \frac{\hat{q}_{o B}}{G \lambda}=0.10\left(\rho_{V} / \rho_{L}\right)^{0.133}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{1 / 3}(1+0.0031 L / D)^{-1}  \tag{9.87}\\
& \frac{\hat{q}_{o C}}{G \lambda}=0.098\left(\rho_{V} / \rho_{L}\right)^{0.133}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{0.433}(L / D)^{0.27}(1+0.0031 L / D)^{-1}  \tag{9.88}\\
& \frac{\hat{q}_{o D}}{G \lambda}=0.0384\left(\rho_{V} / \rho_{L}\right)^{0.6}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{0.173}\left\{1+0.28\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{0.233}(L / D)\right\}^{-1}  \tag{9.89}\\
& \frac{\hat{q}_{o E}}{G \lambda}=0.234\left(\rho_{V} / \rho_{L}\right)^{0.513}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{0.433}(L / D)^{0.27}(1+0.0031 L / D)^{-1} \tag{9.90}
\end{align*}
$$

In the above equations, $L$ is the heated length of the tube and $D$ is the inside diameter. The constant, $C_{2}$, in Equation (9.86) is given by:

$$
\begin{align*}
C_{2} & =0.25 & & (L / D<50) \\
& =0.25+0.0009(L / D-50) & & (50 \leq L / D \leq 150)  \tag{9.91}\\
& =0.34 & & (L / D>150)
\end{align*}
$$

The following three equations are used in determining the value of $\Gamma$ :

$$
\begin{align*}
\Gamma_{A} & =\frac{1.043}{4 C_{2}\left(g_{c} \sigma \rho_{L} / G^{2} L\right)^{0.043}}  \tag{9.92}\\
\Gamma_{B} & =\frac{(5 / 6)(0.0124+D / L)}{\left(\rho_{V} / \rho_{L}\right)^{0.133}\left(g_{c} \sigma \rho_{L} / G^{2} L\right)^{1 / 3}}  \tag{9.93}\\
\Gamma_{C} & =\frac{1.12\left\{1.52\left(g_{c} \sigma \rho_{L} / G^{2} L\right)^{0.233}+D / L\right\}}{\left(\rho_{V} / \rho_{L}\right)^{0.6}\left(g_{c} \sigma \rho_{L} / G^{2} L\right)^{0.173}} \tag{9.94}
\end{align*}
$$

The values of $\hat{q}_{o}$ and $\Gamma$ are determined as follows, depending on the value of $\rho_{V} / \rho_{L}$.
For $\rho_{V} / \rho_{L} \leq 0.15$ :

$$
\begin{array}{rlr}
\hat{q}_{o} & =\hat{q}_{o A} & \left(\hat{q}_{o A} \leq \hat{q}_{o B}\right) \\
& =\operatorname{Min}\left(\hat{q}_{o B}, \hat{q}_{o C}\right) & \left(\hat{q}_{o A}>\hat{q}_{o B}\right) \\
\Gamma & =\operatorname{Max}\left(\Gamma_{A}, \Gamma_{B}\right) & \tag{9.96}
\end{array}
$$

For $\rho_{V} / \rho_{L}>0.15$ :

$$
\begin{array}{rlr}
\hat{q}_{O} & =\hat{q}_{o A} &  \tag{9.97}\\
& =\operatorname{Max}\left(\hat{q}_{O D}, \hat{q}_{O E} \leq \hat{q}_{O E}\right) \\
& \left(\hat{q}_{O A}>\hat{q}_{O E}\right)
\end{array}
$$

$$
\begin{array}{rlrl}
\Gamma & =\Gamma_{A} & & \left(\Gamma_{A} \geq \Gamma_{B}\right)  \tag{9.98}\\
& =\operatorname{Min}\left(\Gamma_{B}, \Gamma_{C}\right) & \left(\Gamma_{A}<\Gamma_{B}\right)
\end{array}
$$

## Horizontal tubes

For flow in horizontal tubes, the dimensionless correlation of Merilo [35] is recommended by Hewitt et al. [2].

$$
\begin{equation*}
\frac{\hat{q}_{c}}{G \lambda}=575 \gamma_{H}^{-0.34}(L / D)^{-0.511}\left(\frac{\rho_{L}-\rho_{V}}{\rho_{V}}\right)^{1.27}\left(1+\Delta H_{\text {in }} / \lambda\right)^{1.64} \tag{9.99}
\end{equation*}
$$

where

$$
\begin{equation*}
\gamma_{H}=\left(\frac{G D}{\mu_{L}}\right)\left(\frac{\mu_{L}^{2}}{g_{c} \sigma D \rho_{L}}\right)^{-1.58}\left[\frac{\left(\rho_{L}-\rho_{V}\right) g D^{2}}{g_{c} \sigma}\right]^{-1.05}\left(\frac{\mu_{L}}{\mu_{V}}\right)^{6.41} \tag{9.100}
\end{equation*}
$$

The correlation is based on 605 data points for water and Freon-12 covering the ranges $5.3 \leq D \leq 19.1 \mathrm{~mm}, 700 \leq G \leq 8100 \mathrm{~kg} / \mathrm{s} \cdot \mathrm{m}^{2}, 13 \leq \rho_{L} / \rho_{V} \leq 21$.

## Example 9.8

The fluid of Example 9.1 boils while flowing through a vertical 1-in. 14 BWG tube (ID $=2.12 \mathrm{~cm}$ ) with a mass flux of $300 \mathrm{~kg} / \mathrm{m}^{2} \cdot \mathrm{~s}$. The tube length is $10 \mathrm{ft}(3.048 \mathrm{~m})$ and the inlet subcooling of the fluid is $23,260 \mathrm{~J} / \mathrm{kg}$. The tube is uniformly heated over its entire length, and the average internal pressure is 310 kPa . Estimate the critical heat flux using:
(a) The Palen correlation.
(b) The Katto-Ohno correlation.

## Solution

(a) From Example 9.1, the critical pressure is 2550 kPa . Hence, the reduced pressure is:

$$
P_{r}=P / P_{c}=310 / 2550 \cong 0.12157
$$

Equation (9.84b) is used to calculate the critical heat flux.

$$
\begin{aligned}
\hat{q}_{c} & =23,660\left(D^{2} / L\right)^{0.35} P_{c}^{0.61} P_{r}^{0.25}\left(1-P_{r}\right) \\
& =23,660\left[(0.0212)^{2} / 3.048\right]^{0.35}(2550)^{0.61}(0.12157)^{0.25}(1-0.12157) \\
\hat{q}_{c} & =66,980 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

Notice that this method does not take into account either the inlet subcooling or the flow rate of the fluid.
(b) From Example 9.1, the liquid and vapor densities are $567 \mathrm{~kg} / \mathrm{m}^{3}$ and $18.09 \mathrm{~kg} / \mathrm{m}^{3}$, respectively. Hence,

$$
\rho_{V} / \rho_{L}=18.09 / 567=0.031905
$$

Since this value is less than 0.15 , Equations (9.95) and (9.96) are used to evaluate $\hat{q}_{o}$ and $\Gamma$. We first calculate $\hat{q}_{o A}$ and $\hat{q}_{o B}$ using Equations (9.86) and (9.87). Since $L / D=3.048 / 0.0212=143.8$, Equation (9.91) gives the value of $C_{2}$ as:

$$
C_{2}=0.25+0.0009(143.8-50)=0.334
$$

From Example 9.1, $\sigma=8.2 \times 10^{-3} \mathrm{~N} / \mathrm{m}$. Hence,

$$
\begin{aligned}
\frac{g_{c} \sigma \rho_{L}}{G^{2} L} & =\frac{1.0 \times 8.2 \times 10^{-3} \times 567}{(300)^{2} \times 3.048}=1.6949 \times 10^{-5} \\
\hat{q}_{o A} / G \lambda & =C_{2}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{0.043}(L / D)^{-1} \\
= & 0.334\left(1.6949 \times 10^{-5}\right)^{0.043}(143.8)^{-1} \\
\hat{q}_{o A} / G \lambda= & 1.4482 \times 10^{-3} \\
\hat{q}_{o A}= & 1.4482 \times 10^{-3} \times 300 \times 272,000=118,176 \mathrm{~W} / \mathrm{m}^{2} \\
\hat{q}_{o B} / G \lambda= & 0.10\left(\rho_{V} / \rho_{L}\right)^{0.133}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{1 / 3}(1+0.0031 L / D)^{-1} \\
= & 0.10(0.031905)^{0.133}\left(1.6949 \times 10^{-5}\right)^{1 / 3}(1+0.0031 \times 143.8)^{-1} \\
\hat{q}_{o B} / G \lambda= & 1.1236 \times 10^{-3} \\
\hat{q}_{o B}= & 1.1236 \times 10^{-3} \times 300 \times 272,000=91,688 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

Since $\hat{q}_{o A}>\hat{q}_{o B}$, we need to calculate $\hat{q}_{o C}$ from Equation (9.88).

$$
\begin{aligned}
\hat{q}_{o C} / G \lambda & =0.098\left(\rho_{V} / \rho_{L}\right)^{0.133}\left(\frac{g_{c} \sigma \rho_{L}}{G^{2} L}\right)^{0.433}(L / D)^{0.27}(1+0.0031 L / D)^{-1} \\
& =0.098(0.031905)^{0.133}\left(1.6949 \times 10^{-5}\right)^{0.433}(143.8)^{0.27}(1+0.0031 \times 143.8)^{-1} \\
\hat{q}_{o C} / G \lambda & =1.4091 \times 10^{-3} \\
\hat{q}_{o C} & =1.4091 \times 10^{-3} \times 300 \times 272,000=114,985 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

From Equation (9.95), since $\hat{q}_{o A}>\hat{q}_{O B}$, we have:

$$
\hat{q}_{o}=\operatorname{Min}\left(\hat{q}_{o B}, \hat{q}_{o C}\right)=91,688 \mathrm{~W} / \mathrm{m}^{2}
$$

The next step is to calculate $\Gamma_{A}$ and $\Gamma_{B}$ from Equations (9.92) and (9.93).

$$
\begin{aligned}
& \Gamma_{A}=\frac{1.043}{4 C_{2}\left(g_{c} \sigma \rho_{L} / G^{2} L\right)^{0.043}}=\frac{1.043}{4 \times 0.334\left(1.6949 \times 10^{-5}\right)^{0.043}} \\
& \Gamma_{A}=1.2521
\end{aligned}
$$

$$
\begin{aligned}
\Gamma_{B} & =\frac{(5 / 6)(0.0124+D / L)}{\left(\rho_{V} / \rho_{L}\right)^{0.133}\left(g_{c} \sigma \rho_{L} / G^{2} L\right)^{1 / 3}} \\
& =\frac{(5 / 6)(0.0124+0.0212 / 3.048)}{(0.031905)^{0.133}\left(1.6949 \times 10^{-5}\right)^{1 / 3}} \\
\Gamma_{B} & =0.9929
\end{aligned}
$$

From Equation (9.96) we have:

$$
\Gamma=\operatorname{Max}\left(\Gamma_{A}, \Gamma_{B}\right)=1.2521
$$

The critical heat flux is given by Equation (9.85):

$$
\begin{aligned}
& \hat{q}_{c}=\hat{q}_{o}\left(1+\Gamma \Delta H_{\text {in }} / \lambda\right)=91,688(1+1.2521 \times 23,260 / 272,000) \\
& \hat{q}_{c} \cong 101,500 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

This value is about $50 \%$ higher than the result obtained using Palen's correlation.

## Example 9.9

Calculate the critical heat flux for the conditions of Example 9.8 assuming that the tube is horizontal rather than vertical.

## Solution

The factor $\gamma_{H}$ is calculated from Equation (9.100) using fluid properties from Example 9.1.

$$
\begin{aligned}
\gamma_{H}= & \left(\frac{G D}{\mu_{L}}\right)\left(\frac{\mu_{L}^{2}}{g_{c} \sigma D \rho_{L}}\right)^{-1.58}\left[\frac{\left(\rho_{L}-\rho_{V}\right) g D^{2}}{g_{c} \sigma}\right]^{-1.05}\left(\frac{\mu_{L}}{\mu_{V}}\right)^{6.41} \\
= & \left(\frac{300 \times 0.0212}{156 \times 10^{-6}}\right)\left[\frac{\left(156 \times 10^{-6}\right)^{2}}{1.0 \times 8.2 \times 10^{-3} \times 0.0212 \times 567}\right]^{-1.58} \\
& \times\left[\frac{(567-18.09) \times 9.81(0.0212)^{2}}{1.0 \times 8.2 \times 10^{-3}}\right]^{-1.05}\left(\frac{156 \times 10^{-6}}{7.11 \times 10^{-6}}\right)^{6.41} \\
\gamma_{H}= & 1.1326 \times 10^{21}
\end{aligned}
$$

Equation (9.99) is now used to calculate the critical heat flux:

$$
\begin{aligned}
\frac{\hat{q}_{c}}{G \lambda} & =575 \gamma_{H}^{-0.34}(L / D)^{-0.511}\left(\frac{\rho_{L}-\rho_{V}}{\rho_{V}}\right)^{1.27}\left(1+\Delta H_{\text {in }} / \lambda\right)^{1.64} \\
& =575\left(1.1326 \times 10^{21}\right)^{-0.34}(143.8)^{-0.511}\left(\frac{567-18.09}{18.09}\right)^{1.27}(1+23,260 / 272,000)^{1.64} \\
\frac{\hat{q}_{c}}{G \lambda} & =2.750 \times 10^{-4} \\
\hat{q}_{c} & =2.750 \times 10^{-4} \times 300 \times 272,000 \cong 22,440 \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

This result is much lower than the critical heat flux for vertical flow calculated in Example 9.8, demonstrating that the effect of tube orientation on critical heat flux can be very significant.

### 9.6 Film Boiling

As previously noted, most reboilers and vaporizers operate in the nucleate boiling regime. In some situations, however, process constraints or economics may make it impractical to match the temperature of the process stream and heating medium so as to obtain a temperature difference low enough for nucleate boiling. Film boiling may be a viable option for these situations provided that the higher tube-wall temperature required for film boiling will not result in fluid decomposition and/or heavy fouling. Methods for predicting heat-transfer coefficients in film boiling are presented in this section.

For saturated film boiling on the outside of a single horizontal tube, the semi-empirical equation of Bromley [36] has been widely used. It can be stated in dimensionless form as follows:

$$
\begin{equation*}
\frac{h_{f b} D_{o}}{k_{V}}=0.62\left[\frac{g \rho_{V}\left(\rho_{L}-\rho_{V}\right) D_{o}^{3}\left(\lambda+0.76 C_{P, V} \Delta T_{e}\right)}{k_{V} \mu_{V} \Delta T_{e}}\right]^{0.25} \tag{9.101}
\end{equation*}
$$

Here, $D_{o}$ is the tube OD and $h_{f b}$ is the heat-transfer coefficient for film boiling. The coefficient of 0.76 in the bracketed term of Equation (9.101) is based on the analysis of Sadasivan and Lienhard [37]. In Equation (9.101), vapor properties are evaluated at the film temperature, $T_{f}=0.5\left(T_{w}+T_{s a t}\right)$, and the liquid density is evaluated at $T_{\text {sat }}$.

Radiative heat transfer is often significant in film boiling. The convective and radiative effects are not simply additive, however, because the radiation acts to increase the thickness of the vapor film, which reduces the rate of convective heat transfer. A combined heat-transfer coefficient, $h_{t}$, for both convection and radiation can be calculated from the following equation [36]:

$$
\begin{equation*}
h_{t}^{4 / 3}=h_{f b}^{4 / 3}+h_{r} h_{t}^{1 / 3} \tag{9.102}
\end{equation*}
$$

Here, $h_{r}$ is the radiative heat-transfer coefficient calculated from the following equation:

$$
\begin{equation*}
h_{r}=\frac{\varepsilon \sigma_{S B}\left(T_{w}^{4}-T_{s a t}^{4}\right)}{T_{w}-T_{s a t}} \tag{9.103}
\end{equation*}
$$

where
$\varepsilon=$ emissivity of tube wall
$\sigma_{S B}=$ Stefan-Boltzmann constant
$=5.67 \times 10^{-8} \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}^{4}=1.714 \times 10^{-9} \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{R}^{4}$
If $h_{r}<h_{f b}$, Equation (9.102) can be approximated by the following explicit formula for $h_{t}$ [36]:

$$
\begin{equation*}
h_{t}=h_{f b}+0.75 h_{r} \tag{9.104}
\end{equation*}
$$

A more rigorous correlation for film boiling on a horizontal tube has been developed by Sakurai et al. [38, 39]. However, the method is rather complicated and will not be given here. The heattransfer coefficient for a single tube provides a somewhat conservative approximation for film boiling on horizontal tube bundles [4].

Two types of convective dry wall boiling occur in tubes. At low vapor quality, the vapor film blanketing the tube wall is in contact with a continuous liquid phase that flows in the central region of the tube. This regime is analogous to pool film boiling, and is sometimes referred to as inverted annular flow. At high vapor quality, boiling takes place in the mist flow regime wherein the vapor phase is continuous over the entire tube cross-section, with the liquid phase in the form of entrained droplets. For the latter situation, the empirical correlation developed by Groeneveld is applicable [26]:

$$
\begin{equation*}
\frac{h D}{k_{V}}=1.09 \times 10^{-3}\left\{R e_{V}\left[x+(1-x) \rho_{V} / \rho_{L}\right]\right\}^{0.989} \operatorname{Pr}_{V}^{1.41} Y_{G}^{-1.15} \tag{9.105}
\end{equation*}
$$

where
$\begin{aligned} R e_{V} & =D G x / \mu_{V} \\ \operatorname{Pr}_{V} & =C_{P, V} \mu_{V} / k_{V} \\ D & =\text { tube ID } \\ x & =\text { vapor weight fraction }\end{aligned}$

$$
\begin{equation*}
Y_{G}=1-0.1\left[\left(\rho_{L}-\rho_{V}\right) / \rho_{V}\right]^{0.4}(1-x)^{0.4} \tag{9.106}
\end{equation*}
$$

In this correlation, the Prandtl number is evaluated at the tube-wall temperature; other properties are evaluated at the fluid temperature.

For the inverted annular flow regime, Palen [4] presented the following equation that is intended to provide a conservative estimate for the heat-transfer coefficient:

$$
\begin{equation*}
h_{f b}=105 P_{c}^{0.5} \Delta T_{e}^{-0.33} P_{r}^{0.38}\left(1-P_{r}\right)^{0.22} \tag{9.107}
\end{equation*}
$$

where
$h_{f b} \propto \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\left(\mathrm{W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$
$\Delta T_{e} \propto{ }^{\circ} \mathrm{F}(\mathrm{K})$
$P_{c} \propto \mathrm{psia}(\mathrm{kPa})$
Either English or SI units may be used with this equation, as indicated above. Since this equation is based on a pool film boiling correlation, it should be more conservative at higher flow rates.

The following equation for film boiling on a flat vertical surface is given in Ref. [26]:

$$
\begin{equation*}
h_{f b}=0.056 R e_{V}^{0.2} \operatorname{Pr}_{V}^{1 / 3}\left[\frac{k_{V}^{3} g \rho_{V}\left(\rho_{L}-\rho_{V}\right)}{\mu_{V}^{2}}\right]^{1 / 3} \tag{9.108}
\end{equation*}
$$

This equation is based on turbulent flow in the vapor film and should be applicable to inverted annular flow in vertical tubes. However, no comparison with experimental data has been given in the literature.

## Example 9.10

The pool boiling of Example 9.1 takes place with a tube-wall temperature of 537.5 K , at which film boiling occurs. Estimate the heat-transfer coefficient for this situation. In addition to the data given in Example 9.1, the heat capacity and thermal conductivity of the vapor are $C_{P, V}=2360 \mathrm{~J} / \mathrm{kg} \cdot \mathrm{K}$ and $k_{V}=0.011 \mathrm{~W} / \mathrm{m} \cdot \mathrm{K}$.

## Solution

For pool film boiling on a horizontal tube, the Bromley equation is applicable. The following data are obtained from Example 9.1:

$$
\begin{aligned}
\rho_{L} & =567 \mathrm{~kg} / \mathrm{m}^{3} & & \mu_{V}
\end{aligned}=7.11 \times 10^{-6} \mathrm{~kg} / \mathrm{m} \cdot \mathrm{~s} .
$$

The temperature difference is:

$$
\Delta T_{e}=T_{w}-T_{s a t}=537.5-437.5=100 \mathrm{~K}
$$

The heat-transfer coefficient for film boiling is obtained by substituting into Equation (9.101).

$$
\begin{aligned}
\frac{h_{f b} D_{o}}{k_{V}} & =0.62\left[\frac{g \rho_{V}\left(\rho_{L}-\rho_{V}\right) D_{o}^{3}\left(\lambda+0.76 C_{P, V} \Delta T_{e}\right)}{k_{V} \mu_{V} \Delta T_{e}}\right]^{0.25} \\
& =0.62\left[\frac{9.81 \times 18.09(567-18.09)(0.0254)^{3}(272,000+0.76 \times 2360 \times 100)}{0.011 \times 7.11 \times 10^{-6} \times 100}\right]^{0.25} \\
\frac{h_{f b} D_{o}}{k_{V}} & =341.57 \\
h_{f b} & =341.57 \times k_{V} / D_{o}=341.57 \times 0.011 / 0.0254 \\
h_{f b} & =148 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

The radiative heat-transfer coefficient is estimated using Equation (9.103). Assuming an emissivity of 0.8 for the tube wall, we have:

$$
\begin{aligned}
& h_{r}=\frac{\varepsilon \sigma_{S B}\left(T_{w}^{4}-T_{\text {sat }}^{4}\right)}{T_{w}-T_{\text {sat }}}=\frac{0.8 \times 5.67 \times 10^{-8}\left[(537.5)^{4}-(437.5)^{4}\right]}{537.5-437.5} \\
& h_{r}=21 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
\end{aligned}
$$

Since $h_{r}<h_{f b}$, Equation (9.104) is used to obtain the effective heat-transfer coefficient:

$$
h_{t}=h_{f b}+0.75 h_{r}=148+0.75 \times 21 \cong 164 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
$$

This value is one to two orders of magnitude lower than the heat-transfer coefficient for nucleate boiling calculated in Example 9.1.

## References

1. Incropera, F. P. and D. P. DeWitt, Introduction to Heat Transfer, 4th edn, Wiley, New York, 2002.
2. Hewitt, G. F., G. L. Shires and T. R. Bott, Process Heat Transfer, CRC Press, Boca Raton, FL, 1994.
3. Forster, H. K. and N. Zuber, Dynamics of vapor bubbles and boiling heat transfer, AIChE J., 1, 531-535, 1955.
4. Palen, J. W., Shell-and-tube reboilers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
5. Cooper, M. G., Saturation nucleate pool boiling: a simple correlation, I. Chem. Eng. Symp. Ser., 86, No. 2, 785-793, 1984.
6. Stephan, K. and M. Abdelsalam, Heat-transfer correlations for natural convection boiling, Int. J. Heat Mass Trans., 23, 73-87, 1980.
7. Bell, K. J. and A. C. Mueller, Wolverine Engineering Data Book II, Wolverine Tube, Inc., www.wlv.com, 2001.
8. Tong, L. S. and Y. S. Tang, Boiling Heat Transfer and Two-Phase Flow, 2nd edn, Taylor \& Francis, Bristol, PA, 1997.
9. Heat Exchanger Design Handbook, Vol. 2, Hemisphere Publishing Corp., New York, 1988.
10. Kandlikar, S. G., M. Shoji and V. K. Dhir, eds, Handbook of Phase Change: Boiling and Condensation, Taylor and Francis, Philadelphia, 1999.
11. Palen, J. W., A. Yarden and J. Taborek, Characteristics of boiling outside large-scale horizontal multitube bundles, Chem. Eng. Prog. Symp. Ser, 68, No. 118, 50-61, 1972.
12. Schlünder, E. U., Heat transfer in nucleate boiling of mixtures, Int. Chem. Eng., 23, 589-599, 1983.
13. Thome, J. R. and S. Shakir, A new correlation for nucleate pool boiling of aqueous mixtures, AIChE Symp. Ser., 83, No. 257, 46-51, 1987.
14. Zuber, N., On the stability of boiling heat transfer, Trans. ASME, 80, 711-720, 1958.
15. Kreith, F. and M. S. Bohn, Principles of heat transfer, 6th edn, Brooks/Cole, Pacific Grove, CA, 2001.
16. Lockhart, R. W. and R. C. Martinelli, Proposed correlation of data for isothermal two-phase, twocomponent flow in pipes, Chem. Eng. Prog., 45, No. 1, 39-48, 1949.
17. Chisholm, D., A theoretical basis for the Lockhart-Martinelli correlation for two-phase flow, Int. J. Heat Mass Trans., 10, 1767-1778, 1967.
18. Chisholm, D., Pressure gradients due to friction during the flow of evaporating two-phase mixtures in smooth tubes and channels, Int. J. Heat Mass Trans., 16, 347-358, 1973.
19. Hewitt, G. F., Fluid mechanics aspects of two-phase flow, in Handbook of Phase Change: Boiling and Condensation, S. G. Kandlikar, M. Shoji and V. K. Dhir, eds, Taylor and Francis, Philadelphia, 1999.
20. Friedel, L., Improved friction pressure drop correlations for horizontal and vertical two-phase pipe flow, Paper E2, European Two-Phase Flow Group Meeting, Ispra, Italy, 1979.
21. Müller-Steinhagen, H. and K. Heck, A simple friction pressure drop correlation for two-phase flow in pipes, Chem. Eng. Process., 20, 297-308, 1986.
22. Tribbe, C. and H. Müller-Steinhagen, An evaluation of the performance of phenomenological models for predicting pressure gradient during gas-liquid flow in horizontal pipelines, Int. J. Multiphase Flow, 26, 1019-1036, 2000.
23. Ould Didi, M. B., N. Kattan and J. R. Thome, Prediction of two-phase pressure gradients of refrigerants in horizontal tubes, Int. J. Refrig., 25, 935-947, 2002.
24. Chisholm, D., Gas-liquid flow in pipeline systems, in Handbook of Fluids in Motion, N. P. Cheremisinoff and R. Gupta, eds, Butterworth, Boston, 1983.
25. Premoli, A., D. Francesco and A. Prina, Una Correlazione Adimensionale per la Determinazione della Densita di Miscele Bifasiche", La Termotecnica, 25, 17-26, 1971.
26. Collier, J. G. and J. R. Thome, Convective boiling and condensation, 3rd edn, Clarendon Press, Oxford, 1994.
27. Chen, J. C., Correlation for boiling heat transfer to saturated fluids in convective flow, $I$ \& EC Proc. Des. Dev., 5, No. 3, 322-329, 1966.
28. Gungor, K. E. and R. H. S. Winterton, A general correlation for flow boiling in tubes and annuli, Int. J. Heat Mass Trans., 29, No. 3, 351-358, 1986.
29. Liu, Z. and R. H. S. Winterton, A general correlation for saturated and subcooled boiling in tubes and annuli, based on a nucleate pool boiling equation, Int. J. Heat Mass Trans., 34, No. 11, 2759-2766, 1991.
30. Shah, M. M., Chart correlation for saturated boiling heat transfer equations and further study, ASHRAE Trans., 88, 185-196, 1982.
31. Kandlikar, S. G., A general correlation for two-phase flow boiling heat transfer coefficient inside horizontal and vertical tubes, J. Heat Transfer, 112, 219-228, 1990.
32. Steiner, D. and J. Taborek, Flow boiling heat transfer in vertical tubes correlated by an asymptotic model, Heat Transfer Eng., 13, No. 2, 43-69, 1992.
33. Kattan, N., J. R. Thome and D. Favrat, Flow boiling in horizontal tubes: Part 3. Development of a new heat transfer model based on flow pattern, J. Heat Transfer, 120, 156-165, 1998.
34. Katto, Y. and H. Ohno, An improved version of the generalized correlation of critical heat flux for the forced convective boiling in uniformly heated vertical tubes, Int. J. Heat Mass Trans., 27, No. 9, 1641-1648, 1984.
35. Merilo, M., Fluid-to-fluid modeling and correlation of flow boiling crisis in horizontal tubes, Int. J. Multiphase Flow, 5, 313-325, 1979.
36. Bromley, L. A., Heat transfer in stable film boiling, Chem. Eng. Prog., 46, No. 5, 221-227, 1950.
37. Sadasivan, P. and J. H. Lienhard, Sensible heat correction in laminar film boiling and condensation, $J$. Heat Transfer, 109, 545-547, 1987.
38. Sakurai, A., M. Shiotsu and K. Hata, A general correlation for pool film boiling heat transfer from a horizontal cylinder to subcooled liquid: Part 1. A theoretical pool film boiling heat transfer model including radiation contributions and its analytical solution, J. Heat Transfer, 109, 545-547, 1987.
39. Sakurai, A., M. Shiotsu and K. Hata, A general correlation for pool film boiling heat transfer from a horizontal cylinder to subcooled liquid: Part 2. Experimental data for various liquids and its correlation, J. Heat Transfer, 112, 441-450, 1990.

## Notations

A Total heat-transfer surface area in tube bundle
$A_{L} \quad$ Cross-sectional area of conduit occupied by liquid phase
$A_{V} \quad$ Cross-sectional area of conduit occupied by vapor phase
$a \quad$ Constant in Equation (9.83)
$B \quad$ Parameter in Chisholm correlation for two-phase pressure drop
Bo Boiling number
$B R \quad T_{D}-T_{B}=$ Boiling range
$b \quad$ Constant in Equation (9.83)
C Constant in Equation (9.27)
$C_{P, L} \quad$ Constant-pressure heat capacity of liquid
$C_{P, V} \quad$ Constant-pressure heat capacity of vapor
$C_{1} \quad$ Parameter in Equation (9.20)
$C_{2} \quad$ Parameter in Equation (9.86), defined in Equation (9.91)
$D \quad$ Diameter of tube
$D_{b} \quad$ Diameter of tube bundle
$D_{i} \quad$ Internal diameter of tube
$D_{o} \quad$ External diameter of tube
$d_{B} \quad$ Theoretical diameter of bubbles leaving solid surface in nucleate boiling
$E \quad$ Parameter in Friedel correlation for two-phase pressure drop
$E_{G W} \quad$ Convective enhancement factor in Gungor-Winterton correlation
$E_{L W} \quad$ Convective enhancement factor in Liu-Winterton correlation
$E_{1}, E_{2} \quad$ Parameters in CISE correlation for two-phase density
$F \quad$ Parameter in Friedel correlation for two-phase pressure drop
$F_{b} \quad$ Factor defined by Equation (9.20) that accounts for convective effects in boiling on tube bundles
$F_{m} \quad$ Mixture correction factor for Mostinski correlation, defined by Equation (9.17)
$F_{P} \quad$ Pressure correction factor in Mostinski correlation
$\mathrm{Fr} \quad$ Froude number
$F_{L O} \quad$ Froude number based on total flow as liquid
$F\left(X_{t t}\right) \quad$ Convective enhancement factor in Chen correlation
$f$ (Darcy) friction factor
$f_{L} \quad$ Friction factor for liquid phase
$f_{L O} \quad$ Friction factor for total flow as liquid
$f_{V O} \quad$ Friction factor for total flow as vapor
$G \quad$ Mass flux
$G_{L} \quad$ Mass flux for liquid phase
$g \quad$ Gravitational acceleration
$g_{c} \quad$ Unit conversion factor
$H \quad$ Parameter in Friedel correlation
$h \quad$ Heat-transfer coefficient
$h_{b} \quad$ Convective boiling heat-transfer coefficient
$h_{f b} \quad$ Heat-transfer coefficient for film boiling
$h_{f c} \quad$ Forced convection heat-transfer coefficient for two-phase flow
$h_{\text {ideal }} \quad$ Ideal mixture heat-transfer coefficient defined by Equation (9.15)
$h_{L} \quad$ Heat-transfer coefficient for liquid phase flowing alone
$h_{n b} \quad$ Nucleate boiling heat-transfer coefficient
$h_{n b, i} \quad$ Nucleate boiling heat-transfer coefficient for pure component $i$
$h_{n c} \quad$ Natural convection heat-transfer coefficient
$h_{r} \quad$ Radiative heat-transfer coefficient
$h_{t} \quad$ Combined heat-transfer coefficient for convection and radiation in film boiling
$K \quad$ Parameter in Equation (9.22)
$k_{L} \quad$ Thermal conductivity of liquid
$k_{V} \quad$ Thermal conductivity of vapor
$L \quad$ Length of conduit
$M \quad$ Molecular weight
$m \quad$ Exponent in Equation (9.83)
$\dot{m} \quad$ Mass flow rate
$\dot{m}_{L} \quad$ Mass flow rate of liquid phase
$\dot{m}_{V} \quad$ Mass flow rate of vapor phase
$n \quad$ Exponent in friction factor versus Reynolds number relationship
$n_{t} \quad$ Number of tubes in tube bundle
$P_{c} \quad$ Critical pressure
$P_{p c} \quad$ Pseudo-critical pressure

| $P_{p r}$ | Pseudo-reduced pressure |
| :---: | :---: |
| $P_{r}$ | Reduced pressure |
| $P_{L}$ | Prandtl number for liquid phase |
| $\mathrm{Pr}_{V}$ | Prandtl number for vapor phase |
| $P_{\text {sat }}$ | Vapor pressure |
| $P_{T}$ | Tube pitch |
| $\hat{q}$ | Heat flux |
| $\hat{q}_{c}$ | Critical heat flux |
| $\hat{q}_{c, \text { bundle }}$ | Critical heat flux for boiling on a tube bundle |
| $\hat{q}_{c, t u b e}$ | Critical heat flux for boiling on a single tube |
| $\hat{q}_{o}$ | Critical heat flux for convective boiling in vertical tubes with no inlet subcooling |
| $\begin{aligned} & \hat{q}_{O A}, \hat{q}_{O B}, \hat{q}_{O C}, \hat{q}_{O D}, \hat{q}_{O E} \\ & \hline \end{aligned}$ | Quantities used to determine the value of $\hat{q}_{o}$ in Katto-Ohno correlation Tube radius |
| $R^{*}$ | $R\left[\frac{g\left(\rho_{L}-\rho_{V}\right)}{g_{c} \sigma}\right]^{0.5}=\text { Dimensionless radius }$ |
| $R e$ | Reynolds number |
| $R_{L}$ | Reynolds number for liquid phase |
| $R e_{V}$ | Reynolds number for vapor phase |
| $R e_{L O}$ | Reynolds number calculated for total flow as liquid |
| $S_{\text {CH }}$ | Nucleate boiling suppression factor in Chen correlation |
| $S_{L W}$ | Nucleate boiling suppression factor in Liu-Winterton correlation |
| $S_{G W}$ | Nucleate boiling suppression factor in Gungor-Winterton correlation |
| SR | $U_{V} / U_{L}=$ Slip ratio in two-phase flow |
| $s$ | Specific gravity |
| $s_{L}$ | Specific gravity of liquid phase |
| $s_{V}$ | Specific gravity of vapor phase |
| T | Temperature |
| $T_{B}$ | Bubble-point temperature |
| $T_{b}$ | Temperature of bulk liquid phase |
| $T_{D}$ | Dew-point temperature |
| $T_{f}$ | Film temperature |
| $T_{s}$ | Temperature of solid surface |
| $T_{\text {sat }}$ | Saturation temperature at system pressure |
| $T_{\text {sat, } i}$ | Saturation temperature of component $i$ at system pressure |
| $T_{\text {sat, } n}$ | Saturation temperature of highest boiling component at system pressure |
| $T_{w}$ | Wall temperature |
| $T_{1}, T_{2}$ | Arbitrary temperatures in Watson correlation |
| $U_{L}$ | Velocity of liquid phase |
| $U_{V}$ | Velocity of vapor phase |
| We | Weber number |
| We ${ }_{L O}$ | Weber number calculated for total flow as liquid |
| $X$ | Lockhart-Martinelli parameter for two-phase flow |
| $X_{t t}$ | Lockhart-Martinelli parameter for the case in which the flow in both phases is turbulent |
| $x$ | Vapor mass fraction in a vapor-liquid mixture |
| $x_{i}$ | Mole fraction of component $i$ in liquid phase |
| $Y$ | Chisholm parameter for two-phase flow |
| $Y_{G}$ | Parameter in Groeneveld correlation, defined by Equation (9.106) |
| $y$ | Parameter in CISE correlation, defined by Equation (9.65) |
| $y_{i}$ | Mole fraction of component $i$ in vapor phase |
| $Z_{1}, Z_{2}, Z_{3}, Z_{4}, Z_{5}$ | Dimensionless groups used in the Stephan-Abdelsalam correlation |

## Greek Letters

| $\alpha_{L}$ | Thermal diffusivity of liquid |
| :---: | :---: |
| $\beta$ | Approximate mass-transfer coefficient used in nucleate boiling correlations for mixtures |
| $\Gamma$ | Inlet sub-cooling parameter in Katto-Ohno correlation |
| $\Gamma_{A}, \Gamma_{B}, \Gamma_{C}$ | Quantities used to determine the value of $\Gamma$ in Katto-Ohno correlation |
| $\gamma_{H}$ | Parameter in Merilo correlation, defined by Equation (9.100) |
| $\Delta H_{\text {in }}$ | Enthalpy of subcooling at inlet of tube |
| $\Delta P_{f}$ | Pressure loss due to fluid fraction |
| $\Delta P_{\text {sat }}$ | $P_{\text {sat }}\left(T_{w}\right)-P_{\text {sat }}\left(T_{\text {sat }}\right)$ |
| $\left(\Delta P_{f} / L\right)_{L}$ | Frictional negative pressure gradient for liquid phase flowing alone |
| $\left(\Delta P_{f} / L\right)_{L O}$ | Frictional negative pressure gradient for total flow as liquid |
| $\left(\Delta P_{f} / L\right)_{t p}$ | Frictional negative two-phase pressure gradient |
| $\left(\Delta P_{f} / L\right)_{V}$ | Frictional negative pressure gradient for vapor phase flowing alone |
| $\left(\Delta P_{f} / L\right)_{V O}$ | Frictional negative pressure gradient for total flow as vapor |
| $\Delta T_{e}$ | $T_{s}-T_{s a t}=$ Excess temperature |
| $\varepsilon$ | Emissivity of tube wall |
| $\varepsilon_{V}$ | Void fraction |
| $\left(\varepsilon_{V}\right)_{\text {hom }}$ | Void fraction for homogeneous two-phase flow |
| $\theta_{c}$ | Contact angle |
| , | Latent heat of vaporization |
| $\mu$ | Viscosity |
| $\mu_{L}$ | Viscosity of liquid |
| $\mu_{V}$ | Viscosity of vapor |
| $\rho_{\text {hom }}$ | Two-phase density for homogeneous flow |
| $\rho_{L}$ | Density of liquid |
| $\rho_{t p}$ | Two-phase density |
| $\rho_{V}$ | Density of vapor |
| $\sigma$ | Surface tension |
| $\sigma_{S B}$ | Stefan-Boltzmann constant |
| $\phi_{b}$ | Correction factor for critical heat flux in tube bundles |
| $\phi_{L}$ | Square root of two-phase multiplier applied to pressure gradient for liquid phase flowing alone |
| $\phi_{L O}$ | Square root of two-phase multiplier applied to pressure gradient for total flow as liquid |
| $\psi_{b}$ | Dimensionless bundle geometry parameter |

### 9.7 Problems

(9.1) (a) Show that the Chisholm, Friedel, and MSH correlations exhibit the correct behavior at low and high vapor fractions, i.e., $\phi_{L O}^{2}=1$ for $x=0$ and $\phi_{L O}^{2}=Y^{2}$ for $x=1$.
(b) Show that the two-phase multiplier, $\phi_{L}^{2}$, in the Lockhart-Martinelli correlation has the following properties:

$$
\begin{array}{ll}
\phi_{L}^{2}=1 & \text { for } x=0 \\
\phi_{L}^{2} \rightarrow \infty & \text { as } x \rightarrow 1
\end{array}
$$

(c) The Lockhart-Martinelli correlation can be formulated in terms of the vapor-phase pressure gradient as follows:

$$
\left(\frac{\Delta P_{f}}{L}\right)_{t p}=\phi_{V}^{2}\left(\frac{\Delta P_{f}}{L}\right)_{V}
$$

where

$$
\phi_{V}^{2}=1+C X+X^{2}
$$

The parameter, $X$, and constant, $C$, are the same as specified in Equation (9.18) and Table 9.1, respectively. Show that the two-phase multiplier, $\phi_{V}^{2}$, has the following properties:

$$
\begin{array}{ll}
\phi_{V}^{2}=1 & \text { for } x=1 \\
\phi_{V}^{2} \rightarrow \infty & \text { as } x \rightarrow 0
\end{array}
$$

(9.2) A stream with a flow rate of $500 \mathrm{lb} / \mathrm{h}$ and a quality of $50 \%$ flows through a $3 / 4$-in., 14 BWG heat exchanger tube. Physical properties of the fluid are as follows:

$$
\begin{array}{ll}
\rho_{L}=49 \mathrm{lbm} / \mathrm{ft}^{3} & \mu_{L}=0.73 \mathrm{cp} \\
\rho_{V}=0.123 \mathrm{lbm} / \mathrm{ft}^{3} & \mu_{V}=0.0095 \mathrm{cp}
\end{array}
$$

(a) Calculate the following Reynolds numbers: $R e_{L O}, R e_{L}, R e_{V O}, R e_{V}$.
(b) Calculate the negative pressure gradients $\left(\Delta P_{f} / L\right)_{L}$ and $\left(\Delta P_{f} / L\right)_{L O}$.
(c) Calculate the Lockhart-Martinelli parameter, $X$, and the Chisholm parameter, $Y$.
(d) Use the Lockhart-Martinelli correlation to calculate the two-phase multiplier, $\phi_{L}^{2}$, and the negative two-phase pressure gradient.
(e) Use the MSH correlation to calculate the two-phase multiplier, $\phi_{L O}^{2}$, and the negative two-phase pressure gradient.

Ans. (a) $R e_{L O}=7408 ; R e_{L}=3704 ; R e_{V O}=569,231 ; R e_{V}=284,616$.
(b) $\left(\Delta P_{f} / L\right)_{L}=0.00312 \mathrm{psi} / \mathrm{ft} ;\left(\Delta P_{f} / L\right)_{L O}=0.0104 \mathrm{psi} / \mathrm{ft}$.
(c) $X=0.07734 ; Y=11.39$.
(d) $\phi_{L}^{2}=426.8 ;\left(\Delta P_{f} / L\right)_{t p}=1.33 \mathrm{psi} / \mathrm{ft}$.
(e) $\phi_{L O}^{2}=119.2 ;\left(\Delta P_{f} / L\right)_{t p}=1.24 \mathrm{psi} / \mathrm{ft}$.
(9.3) For the conditions specified in Problem 9.2, calculate the two-phase pressure gradient using:
(a) The Chisholm correlation.
(b) The Friedel correlation.

The surface tension of the fluid is 20 dynes $/ \mathrm{cm}$.
Ans. (a) $\left(\Delta P_{f} / L\right)_{t p}=1.38 \mathrm{psi} / \mathrm{ft}$.
(9.4) For the conditions of Problems 9.2 and 9.3, calculate the void fraction and two-phase density using:
(a) The homogeneous flow model.
(b) The Lockhart-Martinelli correlation.
(c) The Chisholm correlation.
(d) The CISE correlation.

Ans.
(a) $\varepsilon_{V}=0.9975 ; \rho_{t p}=0.245 \mathrm{lbm} / \mathrm{ft}^{3}$.
(b) $\varepsilon_{V}=0.9516 ; \rho_{t p}=2.49 \mathrm{lbm} / \mathrm{ft}^{3}$.
(c) $\varepsilon_{V}=0.9889 ; \rho_{t p}=0.666 \mathrm{lbm} / \mathrm{ft}^{3}$.
(d) $\varepsilon_{V}=0.9789 ; \rho_{t p}=1.15 \mathrm{lbm} / \mathrm{ft}^{3}$.
(9.5) Repeat Problem 9.2 for a flow rate of $45.87 \mathrm{lb} / \mathrm{h}$.

Ans. (a) $R e_{L O}=680 ; R e_{L}=340 ; R e_{V O}=52,221 ; R e_{V}=26,111$.
(b) $\left(\Delta P_{f} / L\right)_{L}=9.99 \times 10^{-5} \mathrm{psi} / \mathrm{ft} ;\left(\Delta P_{f} / L\right)_{L O}=2.00 \times 10^{-4} \mathrm{psi} / \mathrm{ft}$.
(c) $X=0.1259 ; Y=10.29$
(d) $\phi_{L}^{2}=159.4 ;\left(\Delta P_{f} / L\right)_{t p}=0.0159 \mathrm{psi} / \mathrm{ft}$.
(e) $\phi_{L O}^{2}=97.28 ;\left(\Delta P_{f} / L\right)_{t p}=0.0195 \mathrm{psi} / \mathrm{ft}$.
(9.6) Repeat Problem 9.4 for a flow rate of $45.87 \mathrm{lb} / \mathrm{h}$.
Ans. (a) Same as Problem 9.4.
(b) $\varepsilon_{V}=0.9208 ; \rho_{t p}=3.99 \mathrm{lbm} / \mathrm{ft}^{3}$.
(c) Same as Problem 9.4.
(d) $\varepsilon_{V}=0.9269 ; \rho_{t p}=3.70 \mathrm{lbm} / \mathrm{ft}^{3}$.
(9.7) Nucleate boiling takes place on the surface of a $3 / 4-\mathrm{in}$. OD horizontal tube immersed in saturated liquid toluene. The tube-wall temperature is $300^{\circ} \mathrm{F}$ and the system pressure is 25 psia. Properties of toluene at these conditions are given in the table below. Calculate the heat-transfer coefficient and wall heat flux using:
(a) The Forster-Zuber correlation.
(b) The Mostinski correlation.
(c) The Cooper correlation.
(d) The Stephan-Abdelsalam correlation.

Ans. (a) $902 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} ; 29,950 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$. (b) $571 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} ; 18,950 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(c) $2431 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} ; 80,710 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$
(d) $1594 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} ; 52,920 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.

| Toluene property | Value |
| :--- | :--- |
| $\rho_{V}\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 0.310 |
| $\rho_{L}\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 47.3 |
| $C_{P, V}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.369 |
| $C_{P, L}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.491 |
| $\mu_{V}(\mathrm{cp})$ | 0.00932 |
| $\mu_{L}(\mathrm{cp})$ | 0.213 |
| $k_{V}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.010 |
| $k_{L}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.059 |
| $\sigma(\mathrm{dyne} / \mathrm{cm})^{\circ}$ | 16.2 |
| $\lambda(\mathrm{Btu} / \mathrm{lbm})$ | 151.5 |
| $P_{c}(\mathrm{psia})$ | 595.9 |
| $T_{\text {sat }}\left({ }^{\circ} \mathrm{F}\right)$ at 25 psia | 266.8 |
| Vapor pressure $(\mathrm{psia})$ at $300^{\circ} \mathrm{F}$ | 39.0 |
| Molecular weight | 92.14 |

$$
* 1 \text { dyne } / \mathrm{cm}=6.8523 \times 10^{-5} \mathrm{lbf} / \mathrm{ft} .
$$

(9.8) Nucleate boiling takes place on the surface of a $3 / 4-\mathrm{in}$. OD horizontal tube immersed in saturated liquid refrigerant 134a (1, 1, 1, 2-tetrafluoroethane). The tube-wall temperature is 300 K and the system pressure is 440 kPa . Properties of $\mathrm{R}-134 \mathrm{a}$ at these conditions are given in the table below. Calculate the heat-transfer coefficient and wall heat flux using:
(a) The Forster-Zuber correlation.
(b) The Mostinski correlation.
(c) The Cooper correlation.
(d) The Stephan-Abdelsalam correlation.

| $\mathrm{R}-134 \mathrm{a}$ property | Value |
| :--- | :--- |
| $\rho_{V}\left(\mathrm{~kg} / \mathrm{m}^{3}\right)$ | 20.97 |
| $\rho_{L}\left(\mathrm{~kg} / \mathrm{m}^{3}\right)$ | 1253 |
| $C_{P, V}(\mathrm{~J} / \mathrm{kg} \cdot \mathrm{K})$ | 865 |
| $C_{P, L}(\mathrm{~J} / \mathrm{kg} \cdot \mathrm{K})$ | 1375 |
| $\mu_{V}(\mathrm{~kg} / \mathrm{m} \cdot \mathrm{s})$ | $1.185 \times 10^{-5}$ |
| $\mu_{L}(\mathrm{~kg} / \mathrm{m} \cdot \mathrm{s})$ | $2.41 \times 10^{-4}$ |
| $k_{V}(\mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ | 0.0122 |
| $k_{L}(\mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ | 0.087 |
| $\sigma(\mathrm{~N} / \mathrm{m})$ | 0.00993 |
| $\lambda(\mathrm{~J} / \mathrm{kg})$ | 192,800 |
| $P_{c}(\mathrm{kPa})$ | 4064 |
| $T_{\text {sat }}(\mathrm{K})$ at 440 kPa | 285 |
| Vapor pressure $(\mathrm{kPa})$ at 300 K | 700 |
| Molecular weight | 102.03 |

(9.9) Calculate the critical heat flux for the conditions of Problem 9.7 using:
(a) The Zuber equation.
(b) The Zuber-type equation for a horizontal cylinder.
(c) The Mostinski correlation.
Ans.
(a) $122,640 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(b) $97,127 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(c) $151,740 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(9.10) Calculate the critical heat flux for the conditions of Problem 9.8 using:
(a) The Zuber equation.
(b) The Zuber-type equation for a horizontal cylinder.
(c) The Mostinski correlation.
(9.11) The nucleate boiling of Problem 9.7 takes place on a tube bundle consisting of 10,200 tubes having an OD of $3 / 4 \mathrm{in}$. and laid out on a $1.0-\mathrm{in}$. triangular pitch. The bundle diameter is 106.8 in . Calculate the critical heat flux and heat-transfer coefficient for this situation.

Ans. $6570 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$ and $2020 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ (based on Mostinski correlations).
(9.12) The nucleate boiling of Problem 9.8 takes place on a tube bundle consisting of 1270 tubes having an OD of 19 mm and laid out on a 23.8 mm triangular pitch. The bundle diameter is approximately 920 mm . Calculate the critical heat flux and heat-transfer coefficient for this situation.
(9.13) Nucleate boiling takes place on the surface of a $1.0-\mathrm{in}$. OD horizontal tube immersed in a saturated liquid consisting of $40 \mathrm{~mol} . \% n$-pentane and $60 \mathrm{~mol} . \%$ toluene. The system pressure is 35 psia and the heat flux is $25,000 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$. The vapor in equilibrium with the liquid contains $87.3 \mathrm{~mol} . \% n$-pentane. At system pressure, the boiling point of $n$-pentane is $147.4^{\circ} \mathrm{F}$ while that of toluene is $291.6^{\circ} \mathrm{F}$. The critical pressures are 488.6 psia for $n$-pentane and 595.9 psia for toluene. Mixture properties at system conditions are given in the table below.
(a) Use the mixture properties together with the Stephan-Abdelsalam correlation to calculate the ideal heat-transfer coefficient for the mixture.
(b) Use Schlünder's method with the ideal heat-transfer coefficient from part (a) to calculate the heat-transfer coefficient for the mixture.
(c) Repeat part (b) using the method of Thome and Shakir.
(d) Use Palen's method to calculate the mixture heat-transfer coefficient.

Ans. (a) $543 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (b) $248 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(c) $262 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(d) $198 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.

| Mixture property | Value |
| :--- | :--- |
| $\rho_{L}\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 43.7 |
| $\rho_{V}\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 0.404 |
| $k_{L}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.0607 |
| $C_{P, L}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.498 |
| $\mu_{L}(\mathrm{cp})$ | 0.231 |
| $\mu_{V}(\mathrm{cp})$ | 0.00833 |
| $\sigma(\text { dyne } / \mathrm{cm})^{*}$ | 16.5 |
| $\lambda(\mathrm{Btu} / \mathrm{lbm})$ | 149.5 |
| Bubble-point temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 183.5 |
| Dew-point temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 258.3 |

*1 dyne $/ \mathrm{cm}=6.8523 \times 10^{-5} \mathrm{lbf} / \mathrm{ft}$.
(9.14) Estimate the value of the critical heat flux for the conditions of Problem 9.13.

Ans. $159,350 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$ (from Mostinski correlation).
(9.15) The nucleate boiling of Problem 9.13 takes place on a horizontal tube bundle consisting of 390 tubes having an OD of 1.0 in . and laid out on a $1.25-\mathrm{in}$. square pitch. The bundle diameter is approximately 30 in . Calculate the heat-transfer coefficient and critical heat flux for this situation.

Ans. $472 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ (using Schlünder $h_{n b}$ ); $38,000 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(9.16) The Gorenflo correlation (Gorenflo, D., Pool boiling, VDI Heat Atlas, VDI Verlag, Düsseldorf, 1993) is a fluid-specific method for calculating nucleate boiling heat-transfer coefficients that, when applicable, is reputed to be very reliable. It utilizes experimental heat-transfer coefficients obtained at the following reference conditions:

$$
\begin{aligned}
\text { Reduced pressure } & =0.1 \\
\text { Heat flux } & =20,000 \mathrm{~W} / \mathrm{m}^{2} \\
\text { Surface roughness } & =0.4 \mu \mathrm{~m}
\end{aligned}
$$

The heat-transfer coefficient is calculated as follows:

$$
h_{n b}=h_{r e f} F_{P}\left(\hat{q} / \hat{q}_{r e f}\right)^{m}\left(\Xi / \Xi_{r e f}\right)^{0.133}
$$

where
$h_{\text {ref }}=$ nucleate boiling heat-transfer coefficient at reference conditions
$F_{P}=$ pressure correction factor
$\hat{q}_{r e f}=20,000 \mathrm{~W} / \mathrm{m}^{2}=6,342 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$
$\Xi=$ surface roughness
$\Xi_{\text {ref }}=0.4 \mu \mathrm{~m}=1.31 \times 10^{-6} \mathrm{ft}$
The pressure correction factor and exponent, $m$, are functions of reduced pressure that are calculated as follows:

$$
\begin{array}{ll}
F_{P}=1.73 P_{r}^{0.27}+\left(6.1+\frac{0.68}{1-P_{r}}\right) P_{r}^{2} & \text { (water) } \\
F_{P}=1.2 P_{r}^{0.27}+2.5 P_{r}+P_{r} /\left(1-P_{r}\right) & \text { (other fluids) } \\
m=0.9-0.3 P_{r}^{0.15} & \text { (water) } \\
m=0.9-0.3 P_{r}^{0.3} & \text { (other fluids) }
\end{array}
$$

If the surface roughness is unknown, it is set to $0.4 \mu \mathrm{~m}$. Reference heat-transfer coefficients for a few selected fluids are given in the table below. Values for a number of other fluids are available on the web (Thome, J. R., Engineering Data Book III, Wolverine Tube, Inc., www.wlv.com, 2004).

| Fluid | $h_{\text {ref }}\left(\mathrm{W} / \mathrm{m}^{2}\right)$ |
| :--- | :--- |
| $n$-pentane | 3400 |
| $n$-heptane | 3200 |
| Toluene | 2650 |
| $n$-propanol | 3800 |
| R-134a | 4500 |
| Water | 5600 |

Use the Gorenflo correlation to calculate:
(a) The heat-transfer coefficient and heat flux for the conditions of Problem 9.7.
(b) The heat-transfer coefficient and heat flux for the conditions of Problem 9.8.
(c) The ideal heat-transfer coefficient for the mixture of Problem 9.13.
(9.17) The Stephan-Abdelsalam correlation for the "hydrocarbon" group is as follows:

$$
\frac{h_{n b} d_{B}}{k_{L}}=0.0546\left(Z_{1} Z_{4}^{0.5}\right)^{0.67} Z_{3}^{0.248} Z_{5}^{-4.33}
$$

Use this correlation to calculate the nucleate boiling heat-transfer coefficient for the conditions of:
(a) Example 9.1.
(b) Problem 9.7.
(c) Problem 9.8.
(d) Problem 9.13.

Ans. (a) $21,000 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}$.
(9.18) Toluene boils while flowing vertically upward through a 1 -in. OD, 14 BWG tube with a mass flux of $250,000 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$. At a point in the tube where the wall temperature is $300^{\circ} \mathrm{F}$, the pressure is 25 psia and the quality is 0.1 , calculate the heat-transfer coefficient using:
(a) Chen's method.
(b) Chen's method with the Mostinski-Palen correlation for nucleate boiling.
(c) The Liu-Winterton correlation.

See Problem 9.7 for fluid property data.
Ans.
(a) $690 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(b) $554 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(c) $1377 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(9.19) Refrigerant 134a boils while flowing vertically upward through a $3 / 4-\mathrm{in}$. OD, 14 BWG tube with a mass flux of $400 \mathrm{~kg} / \mathrm{s} \cdot \mathrm{m}^{2}$. At a point in the tube where the wall temperature is 300 K , the pressure is 440 kPa and the quality is 0.25 , calculate the heat-transfer coefficient using:
(a) Chen's method.
(b) Chen's method with the Mostinski correlation for nucleate boiling.
(c) The Liu-Winterton correlation.

See Problem 9.8 for fluid property data.
(9.20) A mixture of $n$-pentane and toluene boils while flowing vertically upward through a $1-\mathrm{in}$. OD, 14 BWG tube with a mass flux of $300,000 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$. At a point in the tube where the
conditions specified in Problem 9.13 exist and the quality is 0.15 , calculate the heat-transfer coefficient using the Chen-Palen method.

Ans. $578 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(9.21) For the conditions specified in Problem 9.18, the tube length is 8 ft and the enthalpy of subcooling at the tube inlet is $10 \mathrm{Btu} / \mathrm{lbm}$. Calculate the critical heat flux using:
(a) Palen's method.
(b) The Katto-Ohno correlation.

Ans. (a) $25,660 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$. (b) $54,740 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(9.22) For the conditions specified in Problem 9.19, the tube length is 10 ft and the liquid entering the tube is subcooled by 2 K . Calculate the critical heat flux using:
(a) Palen's method.
(b) The Katto-Ohno correlation.
(9.23) For the conditions specified in Problem 9.20, the tube length is 12 ft and the enthalpy of subcooling at the tube inlet is $5 \mathrm{Btu} / \mathrm{lbm}$. Estimate the critical heat flux using:
(a) Palen's method.
(b) The Katto-Ohno correlation.
(9.24) Calculate the critical heat flux for the conditions of Problem 9.21 assuming that the tube is horizontal rather than vertical. Is the result consistent with the values calculated in Problem 9.21 for a vertical tube?

Ans. $65,050 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$.
(9.25) Calculate the critical heat flux for the conditions of Problem 9.22 assuming that the tube is horizontal rather than vertical. Is the result consistent with the values calculated for a vertical tube in Problem 9.22?
(9.26) Calculate the critical heat flux for the conditions of Problem 9.23 if the tube is horizontal rather than vertical. Is the result consistent with the values calculated for a vertical tube in Problem 9.23?
(9.27) The pool boiling of Problem 9.7 takes place with a tube-wall temperature of $400^{\circ} \mathrm{F}$, at which film boiling occurs. Assuming an emissivity of 0.8 for the tube wall, estimate the heat-transfer coefficient for this situation.
Ans. $40 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(9.28) The pool boiling of Problem 9.8 takes place with a tube-wall temperature of 380 K , at which film boiling occurs. Assuming an emissivity of 0.8 for the tube wall, calculate the heat-transfer coefficient for this situation.
(9.29) The convective boiling of Problem 9.18 takes place with a tube-wall temperature of $400^{\circ} \mathrm{F}$. Inverted annular flow exists under these conditions. Estimate the heat-transfer coefficient for this situation using:
(a) Equation (9.107).
(b) Equation (9.108).

Ans. (a) $151 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (b) $114 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(9.30) The convective boiling of Problem 9.19 takes place with a tube-wall temperature of 380 K . Inverted annular flow exists under these conditions. Estimate the heat-transfer coefficient for this situation using:
(a) Equation (9.107).
(b) Equation (9.108).

This page intentionally left blank

## 10

## REBOILERS

## Contents

10.1 Introduction 444
10.2 Types of Reboilers 444
10.3 Design of Kettle Reboilers 449
10.4 Design of Horizontal Thermosyphon Reboilers 467
10.5 Design of Vertical Thermosyphon Reboilers 473
10.6 Computer Software 488

### 10.1 Introduction

A reboiler is a heat exchanger that is used to generate the vapor supplied to the bottom tray of a distillation column. The liquid from the bottom of the column is partially vaporized in the exchanger, which is usually of the shell-and-tube type. The heating medium is most often condensing steam, but commercial heat-transfer fluids and other process streams are also used. Boiling takes place either in the tubes or in the shell, depending on the type of reboiler. Exchangers that supply vapor for other unit operations are referred to as vaporizers, but are similar in most respects to reboilers.

Thermal and hydraulic analyses of reboilers are generally more complex than for single-phase exchangers. Some of the complicating factors are the following:

- Distillation bottom liquids are often mixtures having substantial boiling ranges. Hence, the physical properties of the liquid and vapor fractions can exhibit large variations throughout the reboiler. Thermodynamic calculations are required to determine the phase compositions and other properties within the reboiler.
- A zone or incremental analysis is generally required for rigorous calculations.
- Two-phase flow occurs in the boiling section of the reboiler and, in the case of thermosyphon units, in the return line to the distillation column.
- For recirculating thermosyphon reboilers, the circulation rate is determined by the hydraulics in both the reboiler and the piping connecting the distillation column and reboiler. Hence, the reboiler and connecting piping must be considered as a unit. The hydraulic circuit adds another iterative loop to the design procedure.

Even with simplifying assumptions, the complete design of a reboiler system can be a formidable task without the aid of computer software. For rigorous calculations, commercial software is a practical necessity.

### 10.2 Types of Reboilers

Reboilers are classified according to their orientation and the type of circulation employed. The most commonly used types are described below.

### 10.2.1 Kettle reboilers

A kettle reboiler (Figure 10.1) consists of a horizontally mounted TEMA K-shell and a tube bundle comprised of either U-tubes or straight tubes (regular or finned) with a pull-through (type T) floating head. The tube bundle is unbaffled, so support plates are provided for tube support. Liquid is fed by gravity from the column sump and enters at the bottom of the shell through one or more nozzles. The liquid flows upward across the tube bundle, where boiling takes place on the exterior surface of the tubes. Vapor and liquid are separated in the space above the bundle, and the vapor flows overhead to the column, while the liquid flows over a weir and is drawn off as the bottom product.

Low circulation rates, horizontal configuration and all-vapor return flow make kettle reboilers relatively insensitive to system hydraulics. As a result, they tend to be reliable even at very low (vacuum) or high (near critical) pressures where thermosyphon reboilers are most prone to operational problems. Kettles can also operate efficiently with small temperature driving forces, as high heat fluxes can be obtained by increasing the tube pitch [1]. On the negative side, low circulation rates make kettles very susceptible to fouling, and the over-sized K-shell is relatively expensive.

### 10.2.2 Vertical thermosyphon reboilers

A vertical thermosyphon reboiler (Figure 10.2) consists of a TEMA E-shell with a single-pass tube bundle. The boiling liquid usually flows through the tubes as shown, but shell-side boiling may be used in special situations, e.g., with a corrosive heating medium. A mixture of vapor and liquid is returned to the distillation column, where phase separation occurs. The driving force for the flow is the density difference between the liquid in the feed circuit and the two-phase mixture in the


Figure 10.1 Typical configuration for a kettle reboiler (Source: Ref. [1]).


Figure 10.2 Typical configuration for a vertical thermosyphon reboiler (Source: Ref. [1]).
boiling region and return line. Except for vacuum services, the liquid in the column sump is usually maintained at a level close to that of the upper tubesheet in the reboiler to provide an adequate static head. For vacuum operations, the liquid level is typically maintained at $50-70 \%$ of the tube height to reduce the boiling point elevation of the liquid fed to the reboiler [3].

Vertical thermosyphon reboilers are usually attached directly to distillation columns, so the costs of support structures and piping are minimized, as is the required plot space. The TEMA E-shell is also relatively inexpensive. Another advantage is that the relatively high velocity attained in these units tends to minimize fouling. On the other hand, tube length is limited by the height of liquid in the column sump and the cost of raising the skirt height to increase the liquid level. This limitation tends to make these units relatively expensive for services with very large duties. The boiling point increase due to the large static head is another drawback for services with small temperature driving forces. Also, the vertical configuration makes maintenance more difficult, especially when the heating medium causes fouling on the outside of the tubes and/or the area near the unit is congested.

### 10.2.3 Horizontal thermosyphon reboilers

Horizontal thermosyphon reboilers (Figure 10.3) usually employ a TEMAG-, H-, or X-shell, although E - and J-shells are sometimes used. The tube bundle may be configured for a single pass as shown, or for multiple passes. In the latter case, either U-tubes or straight tubes (plain or finned) may be used. Liquid from the column is fed to the bottom of the shell and flows upward across the tube
bundle. Boiling takes place on the exterior tube surface, and a mixture of vapor and liquid is returned to the column. As with vertical thermosyphons, the circulation is driven by the density difference between the liquid in the column sump and the two-phase mixture in the reboiler and return line.

The flow pattern in horizontal thermosyphon reboilers is similar to that in kettle reboilers, but the higher circulation rates and lower vaporization fractions in horizontal thermosyphons make them less susceptible to fouling. Due to the horizontal configuration and separate support structures, these units are not subject to restrictions on weight or tube length. As a result, they are generally better suited than vertical thermosyphons for services with very large duties. The horizontal configuration is also advantageous for handling liquids of moderately high viscosity, because a relatively small static head is required to overcome fluid friction and drive the flow. Arule of thumb is that a horizontal rather than a vertical thermosyphon should be considered if the feed viscosity exceeds 0.5 cp .

### 10.2.4 Forced flow reboilers

In a forced flow reboiler system (Figure 10.4) the circulation is driven by a pump rather than by gravity. The boiling liquid usually flows in the tubes, and the reboiler may be oriented either horizontally or vertically. A TEMA E-shell is usually used with a tube bundle configured for a single pass. These units are characterized by high tube-side velocities and very low vaporization fractions (usually less than $1 \%$ [1]) in order to mitigate fouling. The main use of forced flow reboilers is in services with severe fouling problems and/or highly viscous (greater than 25 cp ) liquids for which kettle and thermosyphon reboilers are not well suited. Pumping costs render forced flow units uneconomical for routine services.


Figure 10.3 Typical configuration for a horizontal thermosyphon reboiler (Source: Ref. [1]).


Figure 10.4 Typical configuration for a forced flow reboiler (Source: Ref. [1]).

### 10.2.5 Internal reboilers

An internal reboiler (Figure 10.5) consists of a tube bundle (usually U-tubes) that is inserted directly into the sump of the distillation column. Since no shell or connecting piping is required, it is the least expensive type of reboiler. However, the amount of heat-transfer area that can be accommodated is severely limited. Also, formation of froth and foam in the column sump can cause operational problems. As a result, this type of reboiler is infrequently used.

### 10.2.6 Recirculating versus once-through operation

Thermosyphon reboiler systems can be of either the recirculating type, as in Figures 10.2 and 10.3, or the once-through type shown in Figure 10.6. In the latter case, the liquid from the bottom tray is collected in a trap-out, from which it flows to the reboiler. The liquid fraction of the return flow collects in the column sump, from which it is drawn as the bottom product. Thus, the liquid passes through the reboiler only once, as with a kettle reboiler.

Once-through operation requires smaller feed lines and generally provides a larger temperature driving force in the reboiler. For mixtures, the boiling point of the liquid fed to a recirculating reboiler is elevated due to the addition of the liquid returned from the reboiler, which is enriched in the higher boiling components. As a result, the mean temperature difference in the boiling zone of the exchanger is reduced. Recirculation can also result in increased fouling in some systems, e.g., when exposure to high temperatures results in chemical decomposition or polymerization.


Figure 10.5 Typical configuration for an internal reboiler (Source: Ref. [1]).


Figure 10.6 Typical configuration for a once-through thermosyphon reboiler system (Source: Ref. [2]).

For reliable design and operation, the vapor weight fraction in thermosyphon reboilers should be limited to about $25-30 \%$ for organic compounds and about $10 \%$ for water and aqueous solutions [1,2]. If these limits cannot be attained with once-through operation, then a recirculating system should be used.

### 10.2.7 Reboiler selection

In some applications the choice of reboiler type is clear-cut. For example, severely fouling or very viscous liquids dictate a forced flow reboiler. Similarly, a dirty or corrosive heating medium together with a moderately fouling process stream favors a horizontal thermosyphon reboiler. In most applications, however, more than one type of reboiler will be suitable. In these situations the selection is usually based on considerations of economics, reliability, controllability, and experience with similar services. The guidelines presented by Palen [1] and reproduced in Table 10.1 provide useful information in this regard. Kister [3] also gives a good concise comparison of reboiler types and the applications in which each is preferred.

Sloley [2] surveyed the use of vertical versus horizontal thermosyphon reboilers in the petroleum refining, petrochemical and chemical industries. Of the thermosyphons used in petroleum refining, 95\% are horizontal units; in the petrochemical industry, $70 \%$ are vertical units; and in the chemical industry, nearly $100 \%$ are vertical units. He attributes this distribution to two factors, size and fouling tendency. For the relatively small, clean services typical of the chemical industry, vertical thermosyphons are favored, whereas the large and relatively dirty services common in petroleum refining dictate horizontal thermosyphons. Services in the petrochemical industry also tend to be

## Table 10.1 Guidelines for Reboiler Selection

| Process conditions | Reboiler type |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Kettle or internal | Horizontal shell-side thermosyphon | Vertical tube-side thermosyphon | Forced flow |
| Operating pressure |  |  |  |  |
| Moderate | E | G | B | E |
| Near critical | B-E | R | Rd | E |
| Deep vacuum | B | R | Rd | E |
| Design $\Delta T$ |  |  |  |  |
| Moderate | E | G | B | E |
| Large | B | R | G-Rd | E |
| Small (mixture) | F | F | Rd | P |
| Very small (pure component) | B | F | P | P |
| Fouling |  |  |  |  |
| Clean | G | G | G | E |
| Moderate | Rd | G | B | E |
| Heavy | P | Rd | B | G |
| Very heavy | P | P | Rd | B |
| Mixture boiling range |  |  |  |  |
| Pure component | G | G | G | E |
| Narrow | G | G | B | E |
| Wide | F | G | B | E |
| Very wide, with viscous liquid | F-P | G-Rd | P | B |

Category abbreviations: B: best; G: good operation; F: fair operation, but better choice is possible; Rd: risky unless carefully designed, but could be best choice in some cases; R: risky because of insufficient data; P: poor operation; and E: operable but unnecessarily expensive.
Source: Ref. [1]
relatively large, but to a lesser extent than in petroleum refining, and they are generally cleaner as well. Hence, the use of horizontal thermosyphons in petrochemical applications is less extensive compared with petroleum refining, but greater than in the chemical industry. The above analysis is somewhat contradictory with Table 10.1 because size permitting, a vertical thermosyphon is indicated for moderate to heavy fouling on the boiling side. The reason is that in a vertical unit the boiling fluid is on the tube side, which is relatively easy to clean, the vertical configuration notwithstanding.

Overall, however, the vertical thermosyphon is the most frequently used type of reboiler [3]. Size permitting, it will generally be the reboiler type of choice unless the service is such that one of the other types offers distinct advantages, as discussed above.

### 10.3 Design of Kettle Reboilers

### 10.3.1 Design strategy

A schematic representation of the circulation in a kettle reboiler is shown in Figure 10.7. The circulation rate through the tube bundle is determined by a balance between the static head of liquid outside the bundle and the pressure drop across the bundle. A two-phase mixture exists in the bundle and the vapor fraction varies with position. Therefore, the bundle hydraulics are coupled with the heat transfer, and a computer model (such as that in the HTRI or HTFS software package) is required to perform these calculations.

Since the circulation rate in a kettle reboiler is relatively low, the pressure drop in the unit is usually quite small. Therefore, a reasonable approximation is to neglect the pressure drop in the unit and size the bundle using the heat-transfer correlations given in Section 9.3. Since kettles utilize once-through operation, the feed rate is equal to the liquid flow rate from the bottom tray of the distillation column. Hence, the feed and return lines can be sized to accommodate the required liquid and vapor flows based on the available static head of liquid in the column sump. Because the flow in each line is single phase (liquid feed and vapor return), the hydraulic calculations are


Figure 10.7 Schematic representation of the circulation in a kettle reboiler Source: Ref. [4].
straightforward. Furthermore, the heat-transfer and hydraulic calculations are independent of one another, making the entire approximate design procedure relatively simple and suitable for hand calculations.

### 10.3.2 Mean temperature difference

In exchangers with boiling or condensing mixtures, the true mean temperature difference is not generally equal to $F\left(\Delta T_{\ln }\right)_{c f}$ because the stream enthalpy varies nonlinearly with temperature over the boiling or condensing range, violating an underlying premise of the $F$-factor method. Computer algorithms handle this situation by performing a zone analysis (incremental calculations) in which each zone or section of the exchanger is such that the stream enthalpy is nearly linear within the zone. For the approximate design procedure outlined above, however, an effective mean temperature difference for the reboiler is required. For kettle reboilers, Palen [1] recommends using the logarithmic mean temperature difference (LMTD) based on the exit vapor temperature as a conservative approximation for the mean temperature difference. That is, the LMTD is calculated assuming that the shell-side fluid temperature is constant and equal to the temperature of the vapor leaving the reboiler.

### 10.3.3 Fouling factors

Since heat-transfer coefficients are generally high in reboilers, the specified fouling allowance can account for a substantial fraction of the total thermal resistance. Therefore, it is important to use realistic values for the fouling factors in order to avoid gross over-design that could result in operational problems as well as needless expense. The recommendations of Palen and Small [5] are given in Table 10.2. TEMA fouling factors or those given in Table 3.3 may also be useful for some applications. As always, however, the best source for fouling factors is prior experience with the same or similar application.

### 10.3.4 Number of nozzles

In order to obtain a reasonably uniform flow distribution along the length of the tube bundle, an adequate number of feed and vapor return nozzles should be used. For a tube bundle of length $L$ and diameter $D_{b}$, the number, $N_{n}$, of nozzle pairs (feed and return) is determined from the following empirical equation [1,6]:

$$
\begin{equation*}
N_{n}=\frac{L}{5 D_{b}} \tag{10.1}
\end{equation*}
$$

The calculated value is rounded upward to the next largest integer.

Table 10.2 Recommended Fouling Factors for Reboiler Design

| Boiling-side stream | Fouling factor $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ |
| :--- | :--- |
| $C_{1}-C_{8}$ normal hydrocarbons | $0-0.001$ |
| Heavier normal hydrocarbons | $0.001-0.003$ |
| Diolefins and polymerizing hydrocarbons | $0.003-0.005$ |
| Heating-side stream |  |
| Condensing steam | $0-0.0005$ |
| Condensing organic | $0.0005-0.001$ |
| Organic liquid | $0.0005-0.002$ |

### 10.3.5 Shell diameter

The diameter of the K-shell is chosen to provide adequate space above the surface of the boiling liquid for vapor-liquid disengagement. A rule of thumb is that the distance from the uppermost tube to the top of the shell should be at least $40 \%$ of the shell diameter. A somewhat more rigorous sizing procedure is based on the following empirical equation for the vapor loading $[5,6]$ :

$$
\begin{equation*}
V L=2290 \rho_{v}\left(\frac{\sigma}{\rho_{L}-\rho_{v}}\right)^{0.5} \tag{10.2}
\end{equation*}
$$

where

$$
V L=\text { vapor loading }\left(\mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{3}\right)
$$

$\rho_{V}, \rho_{L}=$ vapor and liquid densities $\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$
$\sigma=$ surface tension (dyne/cm)
The vapor loading is the mass flow rate of vapor divided by the volume of the vapor space. The value given by Equation (10.2) is intended to provide a sufficiently low vapor velocity to allow gravitational settling of entrained liquid droplets. The dome segment area, $S A$, is calculated from the vapor loading as follows:

$$
\begin{equation*}
S A=\frac{\dot{m}_{V}}{L \times V L} \tag{10.3}
\end{equation*}
$$

where
$\dot{m}_{V}=$ vapor mass flow rate ( $\mathrm{lbm} / \mathrm{h}$ )
$L=$ length of tube bundle (ft)
$V L \propto \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{3}$
$S A \propto \mathrm{ft}^{2}$
Considering the K-shell cross-section shown in Figure 10.7, the dome segment area is the area of the circular segment that lies above the liquid surface. For known bundle diameter and dome segment area, the shell diameter can be determined (by trial and error) from the table of circular segment areas in Appendix 10.A. Since the liquid level is usually maintained slightly above the top row of tubes, the height of liquid in the shell is approximately equal to the bundle diameter plus the clearance between the bundle and the bottom of the shell. However, to account for the effect of foaming and froth formation, this height may be incremented by $3-5 \mathrm{in}$. for the purpose of calculating the shell diameter [6]. Demister pads can also be installed in the vapor outlet nozzles to further reduce entrainment.

## Example 10.1

A kettle reboiler requires a dome segment area of $5.5 \mathrm{ft}^{2}$. The bundle diameter plus clearance is approximately 22.4 in . What shell diameter is required?

## Solution

Adding 4 in. to the liquid height to account for foaming gives an effective liquid height of $26.4 \mathrm{in} .=2.2 \mathrm{ft}$. For the first trial, assume the effective liquid height is approximately $60 \%$ of the shell diameter. Then,

$$
D_{s}=2.2 / 0.6=3.67 \mathrm{ft}
$$

Further, the ratio of sector height, $h$, to circle (shell) diameter is $40 \%$, i.e.,

$$
h / D=1-0.6=0.4
$$

From the table in Appendix 10.A with $h / D=0.4$, the sector area factor is $A=0.29337$. This value must be multiplied by the square of the shell diameter to obtain the actual segment area. Thus,

$$
S A=0.29337(3.67)^{2}=3.95 \mathrm{ft}^{2}
$$

Since this is less than the required dome segment area, a larger shell diameter is needed. For the second trial, assume the effective liquid height is $55 \%$ of the shell diameter. Then,

$$
\begin{aligned}
D_{s} & =\frac{2.2}{0.55}=4.0 \mathrm{ft} \\
h / D & =1-0.55=0.45 \\
A & =0.34278(\text { Appendix } 10 . \mathrm{A}) \\
S A & =0.34278(4.0)^{2}=5.48 \cong 5.5 \mathrm{ft}^{2}
\end{aligned}
$$

Therefore, a shell diameter of approximately 4 ft is required.

### 10.3.6 Liquid overflow reservoir

With a kettle reboiler, surge capacity is provided by the liquid overflow reservoir in the kettle, as opposed to the column sump when a thermosyphon reboiler is used. The liquid holdup time in the overflow reservoir is usually significantly less than in the column sump due to the cost of extending the length of the K-shell, of which only the bottom portion is useable. The small size and limited holdup time can make the liquid level in the reservoir difficult to control, and can lead to relatively large fluctuations in the bottom product flow rate. These fluctuations can adversely affect the operation of downstream units unless a separate surge vessel is provided downstream of the reboiler, or the bottom product flows to storage. These problems can be avoided by eliminating the overflow weir in the kettle [7]. However, a drawback of this strategy is that incomplete separation of reboiler feed and reboiled liquid results in the (partial) loss of one theoretical distillation stage.

### 10.3.7 Finned tubing

Radial low-fin tubes and tubes with surface enhancements designed to improve nucleate boiling characteristics can be used in reboilers and vaporizers. They are particularly effective when the temperature driving force is small, and hence they are widely used in refrigeration systems. In addition to providing a large heat-transfer surface per unit volume, finned tubes can result in significantly higher boiling heat-transfer coefficients compared with plain tubes due to the convective effect of two-phase flow between the fins [1]. As the temperature driving force increases, the boiling-side resistance tends to become small compared with the thermal resistances of the tube wall and heating medium, and the advantage of finned tubes is substantially diminished. A quantitative treatment of boiling on finned and enhanced surfaces is beyond the scope of this book.

### 10.3.8 Steam as heating medium

When condensing steam is used as a heating medium, it is common practice to use an approximate heat-transfer coefficient on the heating side for design purposes. Typically, a value of $1500 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\left(8500 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right)$ is used. This value is referred to the external tube surface and includes a fouling allowance. Thus, for steam condensing inside plain tubes we have:

$$
\left[\left(D_{o} / D_{i}\right)\left(1 / h_{i}+R_{D i}\right)\right]^{-1} \cong 1500 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \cong 8500 \mathrm{~W} / \mathrm{m}^{2} \cdot \mathrm{~K}
$$

Some guidelines for sizing steam and condensate nozzles are presented in Table 10.3. The data are taken from Ref. [8] and are for vertical thermosyphon reboilers. However, they can be used as general guidelines for all types of reboilers of similar size.

Table 10.3 Guidelines for Sizing Steam and Condensate Nozzles

| Shell OD (in.) | Heat-transfer <br> area $\left(\mathrm{ft}^{2}\right)$ | Nominal nozzle diameter (in.) |  |
| :--- | :--- | :--- | :--- |
|  |  | Steam | Condensate |
| 16 | 130 | 4 | 1.5 |
| 20 | 215 | 4 | 2 |
| 24 | $330-450$ | 6 | 3 |
| 30 | $525-1065$ | $6-8$ | $3-4$ |
| 36 | $735-1520$ | 8 | 4 |
| 42 | $1400-2180$ | 8 | 4 |

Source: Ref. [8]

### 10.3.9 Two-phase density calculation

In order to calculate the static head in the reboiler, the density of the two-phase mixture in the boiling region must be determined. For cross flow over tube bundles, this calculation is usually made using either the homogeneous model, Equation (9.51), or one of the methods for separated flow in tubes, such as the Chisholm correlation, Equation (9.63). Experimental data indicate that neither approach is particularly accurate [9], but there is no entirely satisfactory alternative. The homogeneous model is somewhat easier to use, but the Chisholm correlation will generally give a more conservative (larger) result for the static head.

The following example illustrates the design procedure for kettle reboilers.

## Example 10.2

$96,000 \mathrm{lb} / \mathrm{h}$ of a distillation bottoms having the following composition will be partially vaporized in a reboiler:

| Component | Mole \% | Critical pressure (psia) |
| :--- | :--- | :--- |
| Propane | 15 | 616.3 |
| $i$-butane | 25 | 529.0 |
| $n$-butane | 60 | 551.1 |

The stream will enter the reboiler as a (nearly) saturated liquid at 250 psia. The dew-point temperature of the stream at 250 psia is $205.6^{\circ} \mathrm{F}$. Saturated steam at a design pressure of 20 psia will be used as the heating medium. The reboiler is to supply $48,000 \mathrm{lb} / \mathrm{h}$ of vapor to the distillation column. The reboiler feed line will be approximately 23 ft long, while the vapor return line will have a total length of approximately 20 ft . The available elevation difference between the liquid level in the column sump and the reboiler inlet is 9 ft . Physical property data are given in the following table. Design a kettle reboiler for this service.

| Property | Reboiler feed | Liquid overflow | Vapor return |
| :--- | :---: | :---: | :---: |
| $T\left({ }^{\circ} \mathrm{F}\right)$ | 197.6 | 202.4 | 202.4 |
| $H(\mathrm{Btu} / \mathrm{lbm})$ | 106.7 | 109.9 | 216.4 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.805 | 0.811 | 0.576 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.046 | 0.046 | 0.014 |
| $\mu(\mathrm{cp})$ | 0.074 | 0.074 | 0.0095 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 28.4 | 28.4 | 2.76 |
| $\sigma($ dyne $/ \mathrm{cm})$ | 3.64 | 3.59 | - |
| Molecular weight | 56.02 | 56.57 | 55.48 |

## Solution

## (a) Make initial specifications.

(i) Fluid placement

There is no choice here; the boiling fluid must be placed in the shell and the heating medium in the tubes.
(ii) Tubing

One-inch, 14 BWG , U-tubes with a length of 16 ft are specified. A tubing diameter of $3 / 4 \mathrm{in}$. could also be used.
(iii) Shell and head types

A TEMA K-shell is chosen for a kettle reboiler, and a type B head is chosen since the tube-side fluid (steam) is clean. Thus, a BKU configuration is specified.
(iv) Tube layout

A square layout with a tube pitch of 1.25 in . is specified to permit mechanical cleaning of the external tube surfaces. Although this service should be quite clean, contaminants in distillation feed streams tend to concentrate in the bottoms, and kettle reboilers are very prone to fouling.
(v) Baffles and sealing strips

None are specified for a kettle reboiler. Support plates will be used to provide tube support and vibration suppression. Four plates are specified to give an unsupported tube length that is safely below the maximum of 74 in . listed in Table 5.C1.
(vi) Construction materials

Since neither stream is corrosive, plain carbon steel is specified for all components.
(b) Energy balance and steam flow rate.

The reboiler duty is obtained from an energy balance on the process stream (boiling fluid):

$$
q=\dot{m}_{V} H_{V}+\dot{m}_{L} H_{L}-\dot{m}_{F} H_{F}
$$

where the subscripts $F, L$, and $V$ refer to the reboiler feed, liquid overflow, and vapor return streams, respectively. Substituting the appropriate enthalpies and flow rates gives:

$$
\begin{aligned}
& q=48,000 \times 216.4+48,000 \times 109.9-96,000 \times 106.7 \\
& q \cong 5.42 \times 10^{6} \mathrm{Btu} / \mathrm{h}
\end{aligned}
$$

From Table A.8, the latent heat of condensation for steam at 20 psia is $960.1 \mathrm{Btu} / \mathrm{lbm}$. Therefore, the steam flow rate will be:

$$
\dot{m}_{\text {steam }}=q / \lambda_{\text {steam }}=5.42 \times 10^{6} / 960.1=5645 \mathrm{lbm} / \mathrm{h}
$$

(c) Mean temperature difference.

The effective mean temperature difference is computed as if the boiling-side temperature were constant at the vapor exit temperature, which in this case is $202.4^{\circ} \mathrm{F}$. The temperature of the condensing steam is also constant at the saturation temperature, which is $228.0^{\circ} \mathrm{F}$ at 20 psia from Table A.8. Therefore, the effective mean temperature difference is:

$$
\Delta T_{m}=228.0-202.4=25.6^{\circ} \mathrm{F}
$$

(d) Approximate overall coefficient.

Referring to Table 3.5, it is seen that for light hydrocarbons boiling on the shell side with condensing steam on the tube side, $200 \leq U_{D} \leq 300 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Taking the mid-range value gives $U_{D}=250 \mathrm{Btu} / \mathrm{h} . \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ for preliminary design purposes.
(e) Heat-transfer area and number of tubes.

$$
\begin{aligned}
& A=\frac{q}{U_{D} \Delta T_{m}}=\frac{5.42 \times 10^{6}}{250 \times 25.6} \cong 847 \mathrm{ft}^{2} \\
& n_{t}=\frac{A}{\pi D_{o} L}=\frac{847}{\pi(1 / 12) \times 16}=202
\end{aligned}
$$

Note that $n_{t}$ represents the number of straight sections of tubing in the bundle, i.e., the number of tube holes in the tubesheet. For U-tubes, this is twice the actual number of tubes. However, it corresponds to the value listed in the tube-count tables, and so will be referred to as the number of tubes.
(f) Number of tube passes.

For condensing steam, two passes are sufficient.
(g) Actual tube count and bundle diameter.

From Table C.5, the closest tube count is 212 tubes in a 23.25 in . shell. This shell size is the smaller diameter of the K-shell at the tubesheet. The bundle diameter will, of course, be somewhat smaller, but a value of 23 in . will be sufficiently accurate for design calculations.
(h) Required overall coefficient.

The required overall heat-transfer coefficient is calculated in the usual manner:

$$
U_{r e q}=\frac{q}{n_{t} \pi D_{o} L \Delta T_{m}}=\frac{5.42 \times 10^{6}}{212 \times \pi \times(1 / 12) \times 16 \times 25.6}=238 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(i) Inside coefficient, $h_{i}$.

For condensing steam we take:

$$
\left[\left(D_{o} / D_{i}\right)\left(1 / h_{i}+R_{D i}\right)\right]^{-1} \cong 1500 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(j) Outside coefficient, $h_{o}=h_{b}$.

Palen's [1] method, which was presented in Chapter 9, will be used in order to ensure a safe (i.e., conservative) design. It is based on the Mostinski correlation for the nucleate boiling heat-transfer coefficient, to which correction factors are applied to account for mixture effects and convection in the tube bundle.
(i) Nucleate boiling coefficient, $h_{n b}$

The first step is to compute the pseudo-critical and pseudo-reduced pressures for the mixture, which will be used in place of the true values in the Mostinski correlation:

$$
\begin{aligned}
& P_{p c}=\sum x_{i} P_{c, i}=0.15 \times 616.3+0.25 \times 529.0+0.60 \times 551.1=555.4 \mathrm{psi} \\
& P_{p r}=P / P_{p c}=250 / 555.4=0.45
\end{aligned}
$$

The Mostinski correlation is used as given in Equation (9.2a), along with the mixture correction factor as given by Equation (9.17a). Also, since $P_{p r}>0.2$, Equation (9.18) is used to calculate the pressure correction factor. Thus,

$$
\begin{aligned}
h_{n b} & =0.00622 P_{c}^{0.69} \hat{q}^{0.7} F_{p} F_{m} \\
F_{p} & =1.8 P_{r}^{0.17}=1.8(0.45)^{0.17}=1.5715 \\
F_{m} & =\left(1+0.0176 \hat{q}^{0.15} B R^{0.75}\right)^{-1} \\
B R & =T_{D}-T_{B}=205.6-197.6=8.0^{\circ} \mathrm{F}
\end{aligned}
$$

Since the actual heat flux is unknown, it is approximated using the required duty:

$$
\begin{aligned}
\hat{q} & =\frac{q}{n_{t} \pi D_{o} L}=\frac{5.42 \times 10^{6}}{212 \pi(1 / 12) \times 16}=6103 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
F_{m} & =\left[1+0.0176(6103)^{0.15}(8)^{0.75}\right]^{-1}=0.7636 \\
h_{n b} & =0.00622(555.4)^{0.69}(6103)^{0.7} \times 1.5715 \times 0.7636 \\
h_{n b} & =261 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(ii) Bundle boiling coefficient, $h_{b}$

The boiling heat-transfer coefficient for the tube bundle is given by Equation (9.19):

$$
h_{b}=h_{n b} F_{b}+h_{n c}
$$

Although the tube wall temperature is unknown, with an overall temperature difference of $25.6^{\circ} \mathrm{F}$, the heat transfer by natural convection should be small compared to the boiling component. Therefore, $h_{n c}$ is roughly estimated as $44 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.

The bundle convection factor is computed using Equation (9.20) with $D_{b} \cong 23$ in.:

$$
\begin{aligned}
F_{b} & =1.0+0.1\left[\frac{0.785 D_{b}}{C_{1}\left(P_{T} / D_{o}\right)^{2} D_{o}}-1.0\right]^{0.75} \\
& =1.0+0.1\left[\frac{0.785 \times 23}{1.0(1.25 / 1.0)^{2} \times 1.0}-1.0\right]^{0.75} \\
F_{b} & =1.5856
\end{aligned}
$$

The outside coefficient is then:

$$
h_{o}=h_{b}=261 \times 1.5856+44 \cong 458 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(k) Overall coefficient.

$$
U_{D}=\left[\left(1 / h_{i}+R_{D i}\right)\left(D_{o} / D_{i}\right)+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k_{\text {tube }}}+1 / h_{o}+R_{D o}\right]^{-1}
$$

Based on the values in Table 10.2, a boiling-side fouling allowance of $0.0005 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is deemed appropriate for this service. For $1-\mathrm{in} .14$ BWG tubes, $D_{i}=0.834 \mathrm{in}$. from Table B.1. Taking $k_{\text {tube }} \cong 26 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ for carbon steel, we obtain:

$$
\begin{aligned}
& U_{D}=\left[(1 / 1500)+\frac{(1.0 / 12) \ln (1.0 / 0.834)}{2 \times 26}+1.0 / 458+0.0005\right]^{-1} \\
& U_{D}=275 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(l) Check heat flux and iterate if necessary.

A new estimate of the heat flux can be obtained using the overall coefficient:

$$
\hat{q}=U_{D} \Delta T_{m}=275 \times 25.6=7040 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

Since this value differs significantly from the previous estimate used to calculate $h_{n b}$, steps (j) and (k) should be repeated until consistent values for $\hat{q}$ and $U_{D}$ are obtained. Due to the uncertainty in both the heat-transfer coefficient and the mean temperature difference, exact convergence is not required. The following values are obtained after several more iterations:

$$
\begin{aligned}
h_{b} & \cong 523 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
U_{D} & \cong 297 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\hat{q} & \cong 7600 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The overall coefficient exceeds the required coefficient of $238 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ by a significant amount (over-design $=25 \%$ ), indicating that the reboiler is over-sized.
(m) Critical heat flux.

The critical heat flux for nucleate boiling on a single tube is calculated using the Mostinski correlation, Equation (9.23a):

$$
\begin{aligned}
\hat{q}_{c} & =803 P_{c} P_{r}^{0.35}\left(1-P_{r}\right)^{0.9} \\
& =803 \times 555.4(0.45)^{0.35}(1-0.45)^{0.9} \\
\hat{q}_{c} & =196,912 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The critical heat flux for the bundle is obtained from Equation (9.24):

$$
\hat{q}_{c, \text { bundle }}=\hat{q}_{c, t u b e} \phi_{b}=196,912 \phi_{b}
$$

The bundle geometry parameter is given by:

$$
\psi_{b}=\frac{D_{b}}{n_{t} D_{o}}=\frac{23}{212 \times 1.0}=0.1085
$$

Since this value is less than 0.323 , the bundle correction factor is calculated as:

$$
\phi_{b}=3.1 \psi_{b}=3.1 \times 0.1085=0.3364
$$

Therefore, the critical heat flux for the bundle is:

$$
\hat{q}_{c, \text { bundle }}=196,912 \times 0.3364 \cong 66,240 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

Now the ratio of the actual heat flux to the critical heat flux is:

$$
\hat{q} / \hat{q}_{c, \text { bundle }}=7600 / 66,240 \cong 0.11
$$

This ratio should not exceed 0.7 in order to provide an adequate safety margin for reliable operation of the reboiler. In the present case, this criterion is easily met.
Note: In addition, the process-side temperature difference, $\Delta T_{e}$, must be in the nucleate boiling range. In operation, the value of $\Delta T_{e}$ may exceed the maximum value for nucleate boiling, particularly when the unit is clean. This situation can usually be rectified by adjusting the steam pressure. Maximum values of $\Delta T_{e}$ are tabulated for a number of substances in Ref. [10], and they provide guidance in specifying an appropriate design temperature for the heating
medium in these and similar cases. For a given substance, the critical $\Delta T_{e}$ decreases markedly with increasing pressure. It is sometimes stated that the overall $\Delta T$ should not exceed about $90-100^{\circ} \mathrm{F}$ in order to ensure nucleate boiling. However, this rule is not generally valid owing (in part) to the effect of pressure on the critical $\Delta T_{e}$.
(n) Design modification.

The simplest way to modify the initial design in order to reduce the amount of heat-transfer area is to shorten the tubes. The required tube length is calculated as follows:

$$
\begin{aligned}
L_{\text {req }} & =\frac{q}{n_{t} \pi D_{o} U_{D} \Delta T_{m}}=\frac{5.42 \times 10^{6}}{212 \pi(1 / 12) \times 297 \times 25.6} \\
L_{\text {req }} & =12.8 \mathrm{ft}
\end{aligned}
$$

Therefore, a tube length of 13 ft will be sufficient.
A second option is to reduce the number of tubes. From the tube-count table, the next smallest standard bundle ( 21.25 in .) contains 172 tubes. This modification will not be pursued here; it is left as an exercise for the reader to determine the suitability of this configuration.
(o) Number of nozzles.

Equation (10.1) gives the number of pairs of nozzles:

$$
N_{n}=\frac{L}{5 D_{b}}=\frac{13}{5(23 / 12)}=1.36
$$

Rounding upward to the next largest integer gives two pairs of inlet and outlet nozzles. They will be spaced approximately 4.4 ft apart.
(p) Shell diameter.

We first use Equation (10.2) to calculate the vapor loading:

$$
\begin{aligned}
& V L=2290 \rho_{v}\left(\frac{\sigma}{\rho_{L}-\rho_{v}}\right)^{0.5}=2290 \times 2.76\left(\frac{3.59}{28.4-2.76}\right)^{0.5} \\
& V L=2365 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{3}
\end{aligned}
$$

The required dome segment area is then found using Equation (10.3):

$$
S A=\frac{\dot{m}_{v}}{L \times V L}=\frac{48,000}{13 \times 2365} \cong 1.56 \mathrm{ft}^{2}
$$

Next, the effective liquid height in the reboiler is estimated by adding 4 in. to the approximate bundle diameter ( 23 in .) to account for foaming, giving a value of 27 in . Assuming as a first approximation that the liquid height is $60 \%$ of the shell diameter, we obtain:

$$
\begin{aligned}
D_{s} & =\frac{27}{0.6}=45.0 \mathrm{in} . \cong 3.75 \mathrm{ft} \\
h / D & =1-0.6=0.4
\end{aligned}
$$

The sector area factor is obtained from Appendix 10.A:

$$
A=0.29337
$$

Multiplying this factor by the square of the diameter gives the segment area:

$$
S A=0.29337(3.75)^{2}=4.13 \mathrm{ft}^{2}
$$

Since this is greater than the required area, a smaller diameter is needed. Assuming (after several more trials) that the effective liquid height is $73 \%$ of the shell diameter, the next trial gives:

$$
\begin{aligned}
D_{s} & =\frac{27}{0.73}=36.99 \mathrm{in} . \cong 3.08 \mathrm{ft} \\
h / D & =1-0.73=0.27 \\
A & =0.17109 \quad(\text { Appendix } 10 . \mathrm{A}) \\
S A & =0.17109(3.08)^{2}=1.62 \mathrm{ft}^{2}
\end{aligned}
$$

This value is slightly larger than the required dome segment area, which is acceptable. Therefore, a shell diameter of about 37 in . will suffice.
(q) Liquid overflow reservoir.

The reservoir is sized to provide adequate holdup time for control purposes. We first calculate the volumetric flow rate of liquid over the weir:

$$
\text { volumetric flow rate }=\frac{48,000 \mathrm{lbm} / \mathrm{h}}{\left(28.4 \mathrm{lbm} / \mathrm{ft}^{3}\right)(60 \mathrm{~min} / \mathrm{h})}=28.17 \mathrm{ft}^{3} / \mathrm{min}
$$

Next, the cross-sectional area of the shell sector below the weir is calculated. The sector height is equal to the weir height, which is about 23 in . Therefore,

$$
\begin{aligned}
h / D & =23 / 37=0.62 \\
1-h / D & =0.38
\end{aligned}
$$

The sector area factor corresponding to this value is 0.27386 from Appendix 10.A. Hence,

$$
\begin{aligned}
& \text { sector area above weir }=0.27386(37 / 12)^{2}=2.60 \mathrm{ft}^{2} \\
& \text { sector area below weir }=\pi(37 / 12)^{2} / 4-2.60=4.87 \mathrm{ft}^{2}
\end{aligned}
$$

Now the shell length required is:

$$
L_{s}=\frac{28.17 \mathrm{ft}^{3} / \mathrm{min}}{4.87 \mathrm{ft}^{2}} \cong 5.8 \mathrm{ft} / \mathrm{min} \text { of holdup }
$$

Therefore, a reservoir length of 3 ft will provide a holdup time of approximately 30 s , which is adequate to control the liquid level using a standard cascaded level-to-flow control loop. With allowances for U-tube return bends and clearances, the overall length of the shell will then be about 17 ft . It is assumed that relatively large fluctuations in the bottom product flow rate are acceptable in this application.
(r) Feed and return lines.

The available liquid head between the reboiler inlet and the surface of the liquid in the column sump is 9 ft . The corresponding pressure difference is:

$$
\begin{aligned}
\Delta P_{\text {available }} & =\rho_{L}\left(g / g_{c}\right) \Delta h_{L}=28.4(1.0) \times 9 \\
\Delta P_{\text {available }} & =255.6 \mathrm{lbf} / \mathrm{ft}^{2}=1.775 \mathrm{psi}
\end{aligned}
$$

This pressure difference must be sufficient to compensate for the friction losses in the feed line, vapor return line, and the reboiler itself; the static heads in the reboiler and return line; and the pressure loss due to acceleration of the fluid in the reboiler resulting from vapor formation. Of these losses, only the friction losses in the feed and return lines can be readily controlled, and these lines must be sized to meet the available pressure drop. We consider each of the pressure losses in turn.
(i) Static heads

The static head consists of two parts, namely, the two-phase region between the reboiler inlet and the surface of the boiling fluid, and the vapor region from the surface of the boiling fluid through the return line and back down to the liquid surface in the column sump. We estimate the two-phase head loss using the average vapor fraction in the boiling region, $x_{\text {ave }}=0.25$. The average density is calculated using the homogeneous model, which is sufficiently accurate for the present purpose:

$$
\rho_{\text {ave }}=\left[\frac{1-x_{\text {ave }}}{\rho_{L}}+\frac{x_{\text {ave }}}{\rho_{V}}\right]^{-1}=\left[\frac{0.75}{28.4}+\frac{0.25}{2.76}\right]^{-1} \cong 8.55 \mathrm{lbm} / \mathrm{ft}^{3}
$$

The vertical distance between the reboiler inlet and the surface of the boiling fluid is approximately 23 in . The corresponding static pressure difference is:

$$
\Delta P_{t p}=\frac{8.55 \times(23 / 12)}{144}=0.114 \mathrm{psi}
$$

The elevation difference between the boiling fluid surface in the reboiler and the liquid surface in the column sump is:

$$
\Delta h=9-23 / 12=7.08 \mathrm{ft}
$$

The pressure difference corresponding to this head of vapor is:

$$
\Delta P_{V}=\frac{2.76 \times 7.08}{144} \cong 0.136 \mathrm{psi}
$$

The total pressure difference due to static heads is the sum of the above values:

$$
\Delta P_{\text {static }}=0.114+0.136=0.250 \mathrm{psi}
$$

(ii) Friction and acceleration losses in reboiler

The friction loss is small due to the low circulation rate characteristic of kettle reboilers. The large vapor volume provided in the kettle results in a relatively low vapor velocity, and therefore the acceleration loss is also small. Hence, both these losses can be neglected. However, as a safety factor, an allowance of 0.2 psi will be made for the sum of these losses. (A range of $0.2-0.5 \mathrm{psi}$ is typical for thermosyphon reboilers, so an allowance of 0.2 psi should be more than adequate for a kettle.)
(iii) Friction loss in feed lines

We begin by assuming the configuration shown below for the feed lines. The total length of the primary line between the column sump and the tee is approximately 23 ft as given in the problem statement. Each branch of the secondary line between the tee and the reboiler has a horizontal segment of length 2.2 ft and a vertical segment of length 1.0 ft .


The pipe diameter is chosen to give a liquid velocity of about $5 \mathrm{ft} / \mathrm{s}$. Thus, for the primary line:

$$
\begin{aligned}
& D_{i}=\left(\frac{4 \dot{m}}{\pi \rho V}\right)^{1 / 2}=\left[\frac{4(96,000 / 3600)}{\pi \times 28.4 \times 5}\right]^{1 / 2} \\
& D_{i}=0.49 \mathrm{ft}=5.87 \mathrm{in}
\end{aligned}
$$

From Table B.2, a 6 -in. schedule 40 pipe with an inside diameter of 6.065 in. is appropriate.
For the secondary line, the flow rate is halved. Therefore,

$$
D_{i}=\left[\frac{4(48,000 / 3600)}{\pi \times 28.4 \times 5}\right]^{1 / 2}=0.0346 \mathrm{ft}=4.15 \mathrm{in}
$$

A 4-in. schedule 40 pipe with an inside diameter of 4.026 in. is the closest match. However, with 4 -in. inlet nozzles, the value of $\rho V^{2}$ will exceed the TEMA erosion prevention limit of $500 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{s}^{2}$ for bubble-point liquids. Therefore, in order to avoid the need for impingement protection, 5 -in. nozzles with matching piping will be used.

The pressure drop is computed using the equivalent pipe lengths for flow resistance of fittings given in Appendix D. The equivalent lengths for the two pipe sizes are tabulated below. Note that only one branch of the 5 -in. pipe is used because the pressure drop is the same for each parallel branch.

| Item | Equivalent length <br> of 6-in. pipe (ft) | Equivalent length <br> of 5-in. pipe (ft) |
| :--- | :--- | :---: |
| Straight pipe sections | 23 | 3.2 |
| $90^{\circ}$ elbows | 20 | 8.5 |
| Tee | 30 | - |
| $6^{\prime \prime} \times 5^{\prime \prime}$ reducer | - | 4 |
| Entrance loss | 18 | - |
| Exit loss | - | 28 |
| Total | 91 | 43.7 |

The Reynolds number for the 6 -in. pipe is:

$$
R e=\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 96,000}{\pi(6.065 / 12) \times 0.074 \times 2.419}=1.351 \times 10^{6}
$$

The friction factor is calculated using Equation (4.8):

$$
\begin{aligned}
& f=0.3673 R e^{-0.2314}=0.3673\left(1.351 \times 10^{6}\right)^{-0.2314} \\
& f=0.014
\end{aligned}
$$

The pressure drop is given by Equation (4.5) with the equivalent pipe length used in place of the actual length. The mass flux and specific gravity are computed first:

$$
\begin{aligned}
G & =\dot{m} / A_{\text {flow }}=\frac{96,000}{(\pi / 4)(6.065 / 12)^{2}}=478,500 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
s & =\rho / \rho_{\text {water }}=28.4 / 62.43=0.455 \\
\Delta P_{f} & =\frac{f L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.014 \times 91(478,500)^{2}}{7.50 \times 10^{12}(6.065 / 12) \times 0.455 \times 1.0} \\
\Delta P_{f} & \cong 0.169 \mathrm{psi}
\end{aligned}
$$

The calculations for the 5 -in. pipe are similar:

$$
\begin{aligned}
R e & =\frac{4 \times 48,000}{\pi(5.047 / 12) \times 0.074 \times 2.419}=811,768 \\
f & =0.3673(811,768)^{-0.2314} \cong 0.0158 \\
G & =\frac{48,000}{(\pi / 4)(5.047 / 12)^{2}}=345,499 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{0.0158 \times 43.7(345,499)^{2}}{7.50 \times 10^{12}(5.047 / 12) \times 0.455 \times 1.0} \\
\Delta P_{f} & \cong 0.0574 \mathrm{psi}
\end{aligned}
$$

The total friction loss in the feed lines is therefore:

$$
\Delta P_{\text {feed }}=0.169+0.0574 \cong 0.226 \mathrm{psi}
$$

(iv) Friction loss in return lines

A return line configuration similar to that of the feed line is assumed as shown below. The primary line has a total length of 20 ft as given in the problem statement. Each branch of the line connected to the reboiler has a vertical segment of length 1.0 ft and a horizontal segment of length 2.2 ft .


We begin by calculating the maximum recommended vapor velocity using Equation (5.B.1):

$$
V_{\max }=\frac{1800}{(P M)^{0.5}}=\frac{1800}{(250 \times 55.48)}=15.3 \mathrm{ft} / \mathrm{s}
$$

The lines will be sized for a somewhat lower velocity of about $12 \mathrm{ft} / \mathrm{s}$. For the main line, the required diameter is:

$$
\begin{aligned}
D_{i} & =\left(\frac{4 \dot{m}}{\pi \rho V}\right)^{1 / 2}=\left[\frac{4(48,000 / 3600)}{\pi \times 2.76 \times 12}\right]^{1 / 2} \\
D_{i} & =0.716 \mathrm{ft}=8.59 \mathrm{in} .
\end{aligned}
$$

From Table B.2, the closest match is an 8 -in. schedule 40 pipe with an internal diameter of 7.981 in.

For the split-flow section, we have:

$$
D_{i}=\left[\frac{4(29,000 / 3600)}{\pi \times 2.76 \times 12}\right]^{1 / 2}=0.506 \mathrm{ft}=6.07 \mathrm{in}
$$

Six-inch schedule 40 pipe ( $\mathrm{ID}=6.065 \mathrm{in}$.) is appropriate for this section. Equivalent pipe lengths are summarized in the following table:

| Item | Equivalent length <br> of 8-in. pipe $(\mathrm{ft})$ | Equivalent length <br> of 6-in. pipe $(\mathrm{ft})$ |
| :--- | :---: | :---: |
| Straight pipe sections | 20 | 3.2 |
| $90^{\circ}$ elbow | 14 | 10 |
| Tee | 40 | - |
| $6^{\prime \prime} \times 8^{\prime \prime}$ expander | - | 7 |
| Entrance loss | - | 18 |
| Exit loss | 48 | - |
| Total | 122 | 38.2 |

The calculations for the 8 -in. line are as follows:

$$
\begin{aligned}
R e & =\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 48,000}{\pi(7.891 / 12) \times 0.0095 \times 2.419}=4.044 \times 10^{6} \\
f & =0.3673 R e^{-0.2314}=0.3673\left(4.044 \times 10^{6}\right)^{-0.2314} \cong 0.0109 \\
G & =\dot{m} / A_{\text {flow }}=\frac{48,000}{(\pi / 4)(7.981 / 12)^{2}}=138,165 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
s & =\rho / \rho_{\text {water }}=2.76 / 62.43=0.0442 \\
\Delta P_{f} & =\frac{f L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.0109 \times 122(138,165)^{2}}{7.50 \times 10^{12}(7.981 / 12) \times 0.0442 \times 1.0} \\
\Delta P_{f} & \cong 0.115 \mathrm{psi}
\end{aligned}
$$

The calculations for the 6 -in. line are similar, but the flow rate is halved:

$$
\begin{aligned}
R e & =\frac{4 \times 24,000}{\pi(6.065 / 12) \times 0.0095 \times 2.419}=2.631 \times 10^{6} \\
f & =0.3673\left(2.631 \times 10^{6}\right)^{-0.2314}=0.012 \\
G & =\frac{24,000}{(\pi / 4)(6.065 / 12)^{2}}=119,625 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{0.012 \times 38.2(119,625)^{2}}{7.50 \times 10^{12}(6.065 / 12) \times 0.0442 \times 1.0} \\
\Delta P_{f} & \cong 0.0392 \mathrm{psi}
\end{aligned}
$$

The total friction loss in the return lines is thus:

$$
\Delta P_{\text {return }}=0.115+0.0392 \cong 0.154 \mathrm{psi}
$$

(v) Total pressure loss

The total pressure loss is the sum of the individual losses calculated above:

$$
\begin{aligned}
\Delta P_{\text {total }} & =\Delta P_{\text {static }}+\Delta P_{\text {reboiler }}+\Delta P_{\text {feed }}+\Delta P_{\text {return }} \\
& =0.191+0.2+0.226+0.154 \\
\Delta P_{\text {total }} & =0.770 \mathrm{psi}
\end{aligned}
$$

Since this value is less than the available pressure drop of 1.775 psi, the piping configuration is acceptable. In actual operation, the liquid level in the column sump will self-adjust to satisfy the pressure balance.
(s) Tube-side pressure drop.

The pressure drop for condensing steam is usually small due to the low flow rate compared with sensible heating media. For completeness, however, the pressure drop is estimated here. For a condensing vapor, the two-phase pressure drop in the straight sections of tubing can be approximated by half the pressure drop calculated at the inlet conditions (saturated steam
at 20 psia, vapor fraction $=1.0$ ). The requisite physical properties of steam are obtained from Tables A. 8 and A.9:

$$
\begin{aligned}
\rho & =1 / 20.087=0.0498 \mathrm{lbm} / \mathrm{ft}^{3} \\
s & =\rho / \rho_{\text {water }}=0.0498 / 62.43=0.000797 \\
\mu & =0.012 \mathrm{cp} \\
\dot{m} & =5645 \mathrm{lbm} / \mathrm{h} \quad(\text { from step }(\mathrm{b})) \\
\dot{m}_{\text {per tube }} & =\dot{m}\left(n_{p} / n_{t}\right)=5645(2 / 212)=53.25 \mathrm{lbm} / \mathrm{h} \\
G & =\frac{\dot{m}_{\text {per tube }}}{(\pi / 4) D_{i}^{2}}=\frac{53.25}{(\pi / 4)(0.834 / 12)^{2}}=14,037 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =\frac{D_{i} G}{\mu}=\frac{(0.834 / 12) \times 14,037}{0.012 \times 2.419}=33,608
\end{aligned}
$$

The friction factor is calculated using Equation (5.2):

$$
\begin{aligned}
& f=0.4137 R e^{-0.2585}=0.4137(33,608)^{-0.2585} \\
& f=0.0280
\end{aligned}
$$

The pressure drop is calculated by incorporating a factor of $1 / 2$ on the right side of Equation (5.1):

$$
\begin{aligned}
\Delta P_{f} & \cong \frac{1}{2}\left[\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}\right]=\frac{1}{2}\left[\frac{0.0280 \times 2 \times 13(14,037)^{2}}{7.50 \times 10^{12}(0.834 / 12) \times 0.000797 \times 1.0}\right] \\
\Delta P_{f} & \cong 0.173 \mathrm{psi}
\end{aligned}
$$

To this degree of approximation, the pressure drop in the return bends can be neglected. However, the pressure drop in the nozzles will be calculated to check the nozzle sizing. Based on Table 10.3, 6 and 3 -in. schedule 40 nozzles are selected for steam and condensate, respectively. For the steam nozzle we have:

$$
\begin{aligned}
G_{n} & =\frac{\dot{m}}{(\pi / 4) D_{i}^{2}}=\frac{5645}{(\pi / 4)(6.065 / 12)^{2}}=28,137 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e_{n} & =\frac{D_{i} G_{n}}{\mu}=\frac{(6.065 / 12) \times 28,137}{0.012 \times 2.419}=489,903
\end{aligned}
$$

Since the flow is turbulent, allow 1 velocity head for the inlet nozzle loss. From Equation (4.11), we obtain:

$$
\begin{aligned}
& \Delta P_{n, s t e a m}=1.334 \times 10^{-13} G_{n}^{2} / s=\frac{1.334 \times 10^{-13}(28,137)^{2}}{0.000797} \\
& \Delta P_{n, s \text { team }}=0.133 \mathrm{psi}
\end{aligned}
$$

For the condensate at 20 psia , the physical properties are obtained from Tables A. 8 and A.9.

$$
\begin{aligned}
\rho & =1 / 0.016834=59.40 \mathrm{lbm} / \mathrm{ft}^{3} \\
s & =\rho / \rho_{\text {water }}=59.40 / 62.43=0.9515 \\
\mu & =0.255 \mathrm{cp} \\
G_{n} & =\frac{\dot{m}}{(\pi / 4) D_{i}^{2}}=\frac{5645}{(\pi / 4)(3.068 / 12)^{2}}=109,958 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e_{n} & =\frac{D_{i} G_{n}}{\mu}=\frac{(3.068 / 12) \times 109,958}{0.255 \times 2.419}=45,575
\end{aligned}
$$

Since the flow is turbulent, allow 0.5 velocity head for the loss in the exit nozzle:

$$
\Delta P_{n, \text { condensate }}=\frac{0.5 \times 1.334 \times 10^{-13}(109,958)^{2}}{0.9515}=0.00085 \mathrm{psi}
$$

The total tube-side pressure drop is estimated as:

$$
\begin{aligned}
& \Delta P_{i} \cong \Delta P_{f}+\Delta P_{n, \text { steam }}+\Delta P_{n, \text { condensate }} \\
& \Delta P_{i}=0.173+0.133+0.00085 \cong 0.3 \mathrm{psi}
\end{aligned}
$$

The pressure drop is small, as it should be for condensing steam. Therefore, the tubing and nozzle configurations are acceptable.

The final design parameters are summarized below.

## Design summary

Shell type: BKU
Shell ID: 23.25 in./37 in.
Shell length: approximately 17 ft
Length beyond weir: 3 ft
Weir height: approximately 23 in.
Tube bundle: 212 tubes (106 U-tubes), 1 in . OD, $14 \mathrm{BWG}, 13 \mathrm{ft}$ long on 1.25 in . square pitch Baffles: none
Support plates: 3 (One less plate is used due to the reduced tube length.)
Shell-side nozzles: two 5 -in. schedule 40 inlet, two 6 -in. schedule 40 vapor outlet, one 4 -in. schedule 40 liquid outlet
Tube-side nozzles: 6 -in. schedule 40 inlet, 3 -in. schedule 40 outlet
Feed lines: 6 -in. schedule 40 from column to inlet tee, 5 -in. schedule 40 from tee to reboiler Return lines: 6 -in. schedule 40 from reboiler to outlet tee, 8 -in. schedule 40 from tee to column Materials: plain carbon steel throughout

Note: The wall thickness of shell-side nozzles is subject to revision pending results of mechanical design calculations. See Example 10.7 for the latter.

### 10.4 Design of Horizontal Thermosyphon Reboilers

### 10.4.1 Design strategy

The boiling-side circulation in a horizontal thermosyphon reboiler is similar to that in a kettle reboiler, particularly when a cross-flow shell (X-shell) is used. With G- and H-shells, the horizontal baffle(s) impart additional axial flow components, so the overall flow pattern is more a mixture of cross flow and axial flow. The higher circulation rate typical of thermosyphons also results in a higher shell-side heat-transfer coefficient and pressure drop relative to kettles, as well as a higher mean temperature difference due to better mixing in the shell.

The above differences notwithstanding, an approximate computational scheme similar to that used for kettle reboilers can be applied to horizontal thermosyphon units. Notice from Equation (9.20) that the bundle convection factor, $F_{b}$, depends only on the bundle geometry and is independent of the circulation rate. Therefore, to this degree of approximation, the heat-transfer coefficient is independent of circulation rate, and the heat transfer and hydraulics are decoupled. Clearly, this approximation is conservative for thermosyphon units.

Due to the difficulty of calculating the two-phase pressure drop in a horizontal tube bundle with a flow area that varies with vertical position, it is not practical to calculate the pressure drop in a horizontal thermosyphon reboiler within the framework of an approximate method suitable for hand calculations. As an expedient alternative, an average value of 0.35 psi can be used to estimate the sum of the friction and acceleration losses in the reboiler.
To account for the higher mean temperature difference in a horizontal thermosyphon relative to a kettle reboiler, Palen [1] recommends using a co-current LMTD as a conservative approximation for the mean driving force. That is, the LMTD is calculated as if the shell-side and tube-side fluids were flowing co-currently.

With the heat transfer and hydraulics decoupled, the hydraulic calculations can, in principle, be performed in a manner similar to that used for the kettle reboiler in Example 10.2. In the thermosyphon case, however, the calculations are considerably more difficult. The fluid in the return line from the reboiler is a vapor-liquid mixture, so two-phase flow calculations are required. Also, in a recirculating unit the circulation rate is determined by a balance between the available static head of liquid in the column sump and the losses in the feed lines, return lines, and reboiler. Therefore, closure of the pressure balance must be attained to within reasonable accuracy. Furthermore, the pressure drop in the return lines depends on the vapor fraction, which in turn depends on the circulation rate. The upshot is that an iterative procedure is required to size the connecting lines and determine the circulation rate and vapor fraction.

More rigorous computational methods, suitable for computer implementation, are discussed in Refs. [11,12].

### 10.4.2 Design guidelines

The recommendations for fouling factors and number of nozzles given in Section 10.3 for kettle reboilers are also applicable to horizontal thermosyphon reboilers, as are the guidelines given for steam as the heating medium. The clearance between the top of the tube bundle and the shell is much less than in kettle reboilers, since vapor-liquid disengagement is not required in a thermosyphon unit. One rule of thumb is to make the clearance cross-sectional area equal to approximately half the outlet nozzle flow area [13].

TEMA G- and H -shells are preferred for wide boiling mixtures because the horizontal baffles in these units help to reduce flashing of the lighter components. Flashing leaves the liquid enriched in the higher boiling components, which reduces the temperature driving force and, hence, the rate of heat transfer. The total length of the horizontal baffle(s) in these units is about two-thirds of the shell length.

In order to prevent unstable operation of the reboiler system, the velocity of the two-phase mixture in the return line should not exceed the following value [14]:

$$
\begin{equation*}
V_{\max }=\left(4000 / \rho_{t p}\right)^{0.5} \tag{10.4}
\end{equation*}
$$

where
$V_{\text {max }}=$ maximum velocity ( $\mathrm{ft} / \mathrm{s}$ )
$\rho_{t p}=$ density of two-phase mixture $\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$

A complete design problem will not be worked here due to the lengthiness of the calculations. However, the following example illustrates the thermal analysis of a horizontal thermosyphon reboiler.

## Example 10.3

A reboiler for a revamped distillation column in a refinery must supply $60,000 \mathrm{lb} / \mathrm{h}$ of vapor consisting of a petroleum fraction. The stream from the column sump will enter the reboiler as a (nearly) saturated liquid at 35 psia . The dew-point temperature of this stream is $321^{\circ} \mathrm{F}$ at 35 psia , and approximately $20 \%$ by weight will be vaporized in the reboiler. The properties of the reboiler feed and the vapor and liquid fractions of the return stream are given in the following table:

| Property | Reboiler <br> feed | Liquid <br> return | Vapor <br> return |
| :--- | :--- | :---: | :---: |
| $T\left({ }^{\circ} \mathrm{F}\right)$ | 289 | 298.6 | 298.6 |
| $H(\mathrm{Btu} / \mathrm{lbm})$ | 136.6 | 142.1 | 265.9 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.601 | 0.606 | 0.494 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.055 | 0.054 | 0.014 |
| $\mu(\mathrm{cp})$ | 0.179 | 0.177 | 0.00885 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 39.06 | 38.94 | 0.4787 |
| $\sigma(\mathrm{dyne} / \mathrm{cm})$ | 11.6 | 11.4 | - |
| $P_{p c}(\mathrm{psia})$ | 406.5 | - | - |

Heat will be supplied by a Therminol ${ }^{\circledR}$ synthetic liquid organic heat-transfer fluid with a temperature range of $420-380^{\circ} \mathrm{F}$. The allowable pressure drop is 10 psi . Average properties of the Therminol ${ }^{\circledR}$ are given in the table below:

| Property | Therminol $^{\circledR}$ at $T_{\text {ave }}=400^{\circ} \mathrm{F}$ |
| :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.534 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.0613 |
| $\mu(\mathrm{cp})$ | 0.84 |
| $s$ | 0.882 |
| $P r$ | 17.70 |

A used horizontal thermosyphon reboiler consisting of a 23.25 -in. ID TEMA X-shell with 145 U tubes (tube count of 290) is available at the plant site. The tubes are $3 / 4-\mathrm{in}$. OD, $14 \mathrm{BWG}, 16 \mathrm{ft}$ long on a $1.0-\mathrm{in}$. square pitch, and the bundle, which is configured for two passes, has a diameter of approximately 20 in . Tube-side nozzles consist of $6-\mathrm{in}$. schedule 40 pipe. Material of construction is plain carbon steel throughout. Will the reboiler be suitable for this service?

## Solution

(a) Energy balances.

The energy balance for the boiling fluid is:

$$
q=\dot{m}_{V} H_{V}+\dot{m}_{L} H_{L}-\dot{m}_{F} H_{F}
$$

The feed rate to the reboiler is $60,000 / 0.20=300,000 \mathrm{lbm} / \mathrm{h}$, and the liquid return rate is $300,000-60,000=240,000 \mathrm{lbm} / \mathrm{h}$. Therefore,

$$
\begin{aligned}
& q=60,000 \times 265.9+240,000 \times 142.1-300,000 \times 136.6 \\
& q=9,078,000 \mathrm{Btu} / \mathrm{h}
\end{aligned}
$$

The energy balance for the Therminol ${ }^{\circledR}$ is:

$$
\begin{aligned}
q & =\left(\dot{m} C_{P} \Delta T\right)_{T h} \\
9,078,000 & =\dot{m}_{T h} \times 0.534(420-380) \\
\dot{m}_{T h} & =425,000 \mathrm{lbm} / \mathrm{h}
\end{aligned}
$$

(b) Mean temperature difference.

The effective mean temperature difference is computed as if the flow were co-current:

$$
\begin{gathered}
\Delta T=131^{\circ} \mathrm{F}\left\{\begin{array}{ll}
289^{\circ} \mathrm{F} \longrightarrow & 298.6^{\circ} \mathrm{F} \\
420^{\circ} \mathrm{F} \longrightarrow 380^{\circ} \mathrm{F}
\end{array}\right\} \Delta T=81.4^{\circ} \mathrm{F} \\
\Delta T_{\text {mean }} \cong\left(\Delta T_{\ln }\right)_{\text {co-current }}=\frac{131-81.4}{\ln (131 / 81.4)}=104.2^{\circ} \mathrm{F}
\end{gathered}
$$

(c) Heat-transfer area.

$$
A=n_{t} \pi D_{o} L=290 \times \pi \times(0.75 / 12) \times 16=911 \mathrm{ft}^{2}
$$

(d) Required overall coefficient.

$$
U_{\text {req }}=\frac{q}{A \Delta T_{\text {mean }}}=\frac{9,078,000}{911 \times 104.2}=96 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(e) Inside coefficient, $h_{i}$.

$$
\begin{aligned}
D_{i} & =0.584 \mathrm{in} . \quad(\text { Table B.1) } \\
G & =\frac{\dot{m}\left(n_{p} / n_{t}\right)}{(\pi / 4) D_{i}^{2}}=\frac{425,000(2 / 290)}{(\pi / 4)(0.584 / 12)^{2}}=1,575,679 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =D_{i} G / \mu=\frac{(0.584 / 12) \times 1,575,679}{0.84 \times 2.419}=37,738
\end{aligned}
$$

Since the flow is turbulent, Equation (4.1) is used to calculate $h_{i}$ :

$$
\begin{aligned}
N u & =0.023 \operatorname{Re}^{0.8} \mathrm{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14}=0.023(37,738)^{0.8}(17.70)^{1 / 3}(1.0) \\
N u & =274.9 \\
h_{i} & =\left(k / D_{i}\right) N u=\frac{0.0613 \times 274.9}{(0.584 / 12)}=346 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(f) Outside coefficient, $h_{o}=h_{b}$.
(i) Nucleate boiling coefficient

The pseudo-reduced pressure is used in place of the reduced pressure:

$$
P_{p r}=P / P_{p c}=35 / 406.5=0.0861
$$

Since this value is less than 0.2 , Equation (9.5) is used to calculate the pressure correction factor in the Mostinski correlation:

$$
\begin{aligned}
F_{P} & =2.1 P_{r}^{0.27}+\left[9+\left(1-P_{r}^{2}\right)^{-1}\right] P_{r}^{2} \\
& =2.1(0.0861)^{0.27}+\left\{9+\left[1-(0.0861)^{2}\right]^{-1}\right\}(0.0861)^{2} \\
F_{P} & =1.1573
\end{aligned}
$$

The required duty is used to obtain an initial estimate of the heat flux:

$$
\hat{q}=q / A=9,078,000 / 911=9965 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

The boiling range is calculated from the given data and used to compute the mixture correction factor using Equation (9.17a):

$$
\begin{aligned}
B R & =T_{D}-T_{B}=321-289=32^{\circ} \mathrm{F} \\
F_{m} & =\left(1+0.0176 \hat{q}^{0.15} B R^{0.75}\right)^{-1} \\
& =\left[1+0.0176(9965)^{0.15}(32)^{0.75}\right]^{-1} \\
F_{m} & =0.5149
\end{aligned}
$$

The nucleate boiling coefficient is obtained by substituting the above values into the Mostinski correlation, Equation (9.2a):

$$
\begin{aligned}
h_{n b} & =0.00622 P_{c}^{0.69} \hat{q}^{0.7} F_{p} F_{m} \\
& =0.00622(406.5)^{0.69}(9965)^{0.7} \times 1.1573 \times 0.5149 \\
h_{n b} & =147 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(ii) Bundle boiling coefficient, $h_{b}$

The correction factor for bundle convective effects is calculated using Equation (9.20):

$$
\begin{aligned}
F_{b} & =1.0+0.1\left[\frac{0.785 D_{b}}{C_{1}\left(P_{T} / D_{o}\right)^{2} \times D_{o}}-1.0\right]^{0.75} \\
& =1.0+0.1\left[\frac{0.785 \times 20}{1.0(1.0 / 0.75)^{2} \times 0.75}-1.0\right]^{0.75} \\
F_{b} & =1.5947
\end{aligned}
$$

A rough approximation of $44 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ is adequate for the natural convection coefficient, $h_{n c}$, because the temperature difference is large. The boiling coefficient for the bundle is given by Equation (9.19):

$$
\begin{aligned}
& h_{b}=h_{n b} F_{b}+h_{n c}=147 \times 1.5947+44 \\
& h_{b}=278 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}=h_{o}
\end{aligned}
$$

(g) Fouling factors.

Based on the guidelines in Table 10.2, the fouling factors are chosen as follows:

$$
\begin{aligned}
& R_{D i}=0.0005 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu} \quad \text { (organic liquid heating medium) } \\
& R_{D o}=0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu} \quad \text { (heavier normal hydrocarbon) }
\end{aligned}
$$

(h) Overall coefficient.

$$
\begin{aligned}
U_{D} & =\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k_{\text {tube }}}+\frac{1}{h_{o}}+\frac{R_{D i} D_{o}}{D_{i}}+R_{D o}\right]^{-1} \\
& =\left[\frac{0.75}{346 \times 0.584}+\frac{(0.584 / 12) \ln (0.75 / 0.584)}{2 \times 26}+\frac{1}{278}+\frac{0.0005 \times 0.75}{0.584}+0.001\right]^{-1} \\
U_{D} & \cong 109 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(i) Check heat flux.

$$
\hat{q}=U_{D} \Delta T_{m}=109 \times 104.2=11,358 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

This value is about $14 \%$ higher than the initial estimate of the heat flux. Therefore, several more iterations were performed to obtain the following converged values:

$$
\begin{aligned}
h_{b} & \cong 304 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
U_{D} & \cong 113 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\hat{q} & \cong 11,730 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(j) Critical heat flux.

The critical heat flux for a single tube is calculated using Equation (9.23a):

$$
\begin{aligned}
\hat{q}_{c} & =803 P_{c} P_{r}^{0.35}\left(1-P_{r}\right)^{0.9} \\
& =803 \times 406.5(0.0861)^{0.35}(1-0.0861)^{0.9} \\
\hat{q}_{c} & =127,596 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The bundle geometry factor is given by:

$$
\psi_{b}=\frac{D_{b}}{n_{t} D_{o}}=\frac{20}{290 \times 0.75}=0.09195
$$

Since this value is less than 0.323 , the bundle correction factor is:

$$
\phi_{b}=3.1 \psi_{b}=3.1 \times 0.09195=0.285
$$

The critical heat flux for the bundle is given by Equation (9.24):

$$
\begin{aligned}
& \hat{q}_{c, \text { bundle }}=\hat{q}_{c, \text { tube }} \phi_{b}=127,596 \times 0.285 \\
& \hat{q}_{c, \text { bundle }}=36,365 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

The ratio of the actual heat flux to the critical heat flux is:

$$
\hat{q} / \hat{q}_{c, \text { bundle }}=11,730 / 36,365 \cong 0.32
$$

Since the ratio is less than 0.7 and $U_{D}>U_{r e q}$, the reboiler is thermally acceptable.
(k) Tube-side pressure drop.
(i) Friction loss

The calculation uses Equation (5.2) for the friction factor and Equation (5.1) for the pressure drop:

$$
\begin{aligned}
f & =0.4137 R e^{-0.2585}=0.4137(37,738)^{-0.2585}=0.0271 \\
\Delta P_{f} & =\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi_{i}}=\frac{0.0271 \times 2 \times 16(1,575,679)^{2}}{7.5 \times 10^{12}(0.584 / 12) \times 0.882 \times 1.0} \\
\Delta P_{f} & =6.69 \mathrm{psi}
\end{aligned}
$$

(ii) Minor losses

From Table 5.1, the number of velocity heads allocated for minor losses with turbulent flow in U-tubes is:

$$
\alpha_{r}=1.6 n_{p}-1.5=1.6 \times 2-1.5=1.7
$$

Substituting in Equation (5.3) yields:

$$
\begin{aligned}
& \Delta P_{r}=1.334 \times 10^{-13} \alpha_{r} G^{2} / s=1.334 \times 10^{-13} \times 1.7(1,575,679)^{2} / 0.882 \\
& \Delta P_{r}=0.64 \mathrm{psi}
\end{aligned}
$$

(iii) Nozzle losses

For 6 -in. schedule 40 nozzles we have:

$$
\begin{aligned}
G_{n} & =\frac{\dot{m}}{(\pi / 4) D_{i}^{2}}=\frac{425,000}{(\pi / 4)(6.065 / 12)^{2}}=2,118,361 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e_{n} & =\frac{D_{i} G_{n}}{\mu}=\frac{(6.065 / 12) \times 2,118,361}{0.84 \times 2.419}=526,907
\end{aligned}
$$

Since the flow is turbulent, Equation (5.4) is used to estimate the pressure drop:

$$
\begin{aligned}
& \Delta P_{n}=2.0 \times 10^{-13} N_{s} G_{n}^{2} / s=2.0 \times 10^{-13} \times 1(2,118,361)^{2} / 0.882 \\
& \Delta P_{n}=1.02 \mathrm{psi}
\end{aligned}
$$

(iv) Total pressure drop

$$
\begin{aligned}
\Delta P_{i} & =\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=6.69+0.64+1.02 \\
\Delta P_{i} & \cong 8.4 \mathrm{psi}
\end{aligned}
$$

Since the pressure drop is within the specified limit of 10 psi , the reboiler is hydraulically acceptable.

In summary, the reboiler is thermally and hydraulically suitable for this service.

### 10.5 Design of Vertical Thermosyphon Reboilers

### 10.5.1 Introduction

The procedure developed by Fair [10] for design of vertical thermosyphon reboilers is presented in this section. This method has been widely used for industrial reboiler design, and it incorporates some simplifications that help make the design problem more amenable to hand calculation. Newer correlations for two-phase flow and convective boiling are used in place of those given by Fair [10], but the basic design strategy is the same.

Figure 10.8 shows the configuration of the reboiler system. Point $A$ is at the surface of the liquid in the column sump. Points $B$ and $D$ are at the inlet and outlet tubesheets, respectively. Boiling begins at point $C$; between points $B$ and $C$, it is assumed that only sensible heat transfer occurs. The reason for the sensible heating zone is that the liquid generally enters the reboiler subcooled to some extent due to the static head in the column sump and heat losses in the inlet line.


Figure 10.8 Configuration of vertical thermosyphon reboiler system.

### 10.5.2 Pressure balance

With reference to Figure 10.8, the system pressure balance can be stated as follows:

$$
\begin{equation*}
\left(P_{B}-P_{A}\right)+\left(P_{C}-P_{B}\right)+\left(P_{D}-P_{C}\right)+\left(P_{A}-P_{D}\right)=0 \tag{10.5}
\end{equation*}
$$

The first pressure difference, $P_{B}-P_{A}$, consists of the static liquid head minus the friction loss in the inlet line. Expressing the pressure difference in units of psi and setting the viscosity correction factor to unity in Equation (4.5), we have:

$$
\begin{equation*}
P_{B}-P_{A}=\frac{\rho_{L}\left(g / g_{c}\right)\left(z_{A}-z_{B}\right)}{144}-\frac{f_{i n} L_{i n} G_{i n}^{2}}{7.50 \times 10^{12} D_{i n} s_{L}} \tag{10.6}
\end{equation*}
$$

Here, $z_{A}$ and $z_{B}$ are the elevations at points $A$ and $B$, respectively, and the subscript " $i n$ " refers to the inlet line to the reboiler. Also, $L_{i n}$ is an equivalent length that accounts for entrance, exit, and fitting losses.
A similar result holds for the second term, $P_{C}-P_{B}$, if the tube entrance loss is neglected:

$$
\begin{equation*}
P_{C}-P_{B}=-\frac{\rho_{L}\left(g / g_{c}\right) L_{B C}}{144}-\frac{f_{t} L_{B C} G_{t}^{2}}{7.50 \times 10^{12} D_{t} s_{L}} \tag{10.7}
\end{equation*}
$$

The subscript " $t$ " in this equation refers to the reboiler tubes.
The pressure difference, $P_{D}-P_{C}$, across the boiling zone includes an acceleration loss term in addition to the static head and friction loss terms:

$$
\begin{equation*}
P_{D}-P_{C}=-\Delta P_{\text {static }, C D}-\Delta P_{f, C D}-\Delta P_{a c c, C D} \tag{10.8}
\end{equation*}
$$

The pressure difference due to the static head of fluid is obtained by integrating the two-phase density over the boiling zone, but the integral can be approximated using an appropriate average density:

$$
\begin{equation*}
\Delta P_{\text {static }, C D}=\left(g / 144 g_{c}\right) \int_{z_{C}}^{z_{D}} \rho_{t p} d z \cong\left(g / 144 g_{c}\right) \bar{\rho}_{t p} L_{C D} \tag{10.9}
\end{equation*}
$$

Fair [10] recommends calculating the average density, $\bar{\rho}_{t p}$, at a vapor weight fraction equal to one-third the value at the reboiler exit.

The friction loss is obtained by integrating the two-phase pressure gradient over the boiling zone, but it, too, can be approximated, in this case using an average two-phase multiplier:

$$
\begin{equation*}
\Delta P_{f, C D}=\int_{z_{C}}^{z_{D}} \phi_{L O}^{2}\left(\Delta P_{f} / L\right)_{L O} d z \cong \frac{f_{t} L_{C D} G_{t}^{2} \bar{\phi}_{L O}^{2}}{7.5 \times 10^{12} D_{t} s_{L}} \tag{10.10}
\end{equation*}
$$

Fair [10] recommends calculating $\bar{\phi}_{L O}^{2}$ at a vapor weight fraction equal to two-thirds the value at the reboiler exit.

The pressure change due to acceleration of the fluid resulting from vapor formation is given by the following equation [10]:

$$
\begin{equation*}
\Delta P_{a c c, C D}=\frac{G_{t}^{2} \gamma}{144 g_{c} \rho_{L}}=\frac{G_{t}^{2} \gamma}{144 g_{c} \rho_{w a t e r} s_{L}}=\frac{G_{t}^{2} \gamma}{3.75 \times 10^{12} s_{L}} \tag{10.11}
\end{equation*}
$$

where

$$
\begin{equation*}
\gamma=\frac{\left(1-x_{e}\right)^{2}}{1-\varepsilon_{V, e}}+\frac{\rho_{L} x_{e}^{2}}{\rho_{V} \varepsilon_{V, e}}-1 \tag{10.12}
\end{equation*}
$$

In this equation, $x_{e}$ and $\varepsilon_{V, e}$ are the vapor mass fraction and the void fraction at the reboiler exit.
The pressure difference, $P_{A}-P_{D}$, includes static head, friction, and acceleration effects. Since it is common practice (except for vacuum operation) to maintain the liquid level in the column sump near the elevation of the upper tubesheet in the reboiler, the static head effect is neglected. The effect of the velocity change from the reboiler tubes to the return line is accounted for explicitly. Other losses are lumped with the friction loss term by means of an equivalent length, $L_{e x}$. The result is as follows:

$$
\begin{equation*}
P_{A}-P_{D}=\frac{\left(G_{t}^{2}-G_{e x}^{2}\right)(\gamma+1)}{3.75 \times 10^{12} s_{L}}-\frac{f_{e x} L_{e x} G_{e x}^{2} \phi_{L O, e x}^{2}}{7.50 \times 10^{12} D_{e x} s_{L}} \tag{10.13}
\end{equation*}
$$

In this equation, the subscript " $e x$ " designates conditions in the exit line from the reboiler.
Substituting for the four pressure differences in Equation (10.5) and combining terms leads to the following result:

$$
\begin{align*}
& \frac{\rho_{L} g L_{A C}-\bar{\rho}_{t p} g L_{C D}}{144 g_{c}}-\frac{G_{e x}^{2}(\gamma+1)-G_{t}^{2}}{3.75 \times 10^{12} s_{L}}-\frac{f_{i n} L_{i n} G_{i n}^{2}}{7.50 \times 10^{12} D_{i n} s_{L}} \\
& \quad-\frac{f_{t} L_{B C} G_{t}^{2}}{7.50 \times 10^{12} D_{t} s_{L}}-\frac{f_{t} L_{C D} G_{t}^{2} \bar{\phi}_{L O}^{2}}{7.50 \times 10^{12} D_{t} s_{L}}-\frac{f_{e x} L_{e x} G_{e x}^{2} \phi_{L O, e x}^{2}}{7.50 \times 10^{12} D_{e x} s_{L}}=0 \tag{10.14}
\end{align*}
$$

This equation provides a relationship between the circulation rate and the exit vapor fraction in the reboiler. It can be solved explicitly for the circulation rate if the dependence of the friction factors on flow rate is neglected. The solution is:
$\dot{m}_{i}^{2}=\frac{3.2 \times 10^{10} D_{t}^{5} s_{L}\left(g / g_{c}\right)\left(\rho_{L} L_{A C}-\bar{\rho}_{t p} L_{C D}\right)}{2 D_{t}\left\{(\gamma+1)\left(\frac{D_{t}}{D_{e x}}\right)^{4}-\frac{1}{n_{t}^{2}}\right\}+f_{i n} L_{i n}\left(\frac{D_{t}}{D_{i n}}\right)^{5}+\left(\frac{f_{t}}{n_{t}^{2}}\right)\left(L_{B C}+L_{C D} \bar{\phi}_{L O}^{2}\right)+f_{e x} L_{e x} \phi_{L O, e x}^{2}\left(\frac{D_{t}}{D_{e x}}\right)^{5}}$
where
$\dot{m}_{i}=$ tube-side mass flow rate ( $\mathrm{lbm} / \mathrm{h}$ )
$n_{t}=$ number of tubes in reboiler
$\rho_{L}, \bar{\rho}_{t p} \propto \mathrm{lbm} / \mathrm{ft}^{3}$
$L_{A C}, L_{C D}, L_{B C}, L_{i n}, L_{e x} \propto \mathrm{ft}$
$D_{t}, D_{i n}, D_{e x} \propto \mathrm{ft}$
For SI units, change the constant in Equation (10.15) from $3.2 \times 10^{10}$ to 1234. This will give $\dot{m}_{i}$ in $\mathrm{kg} / \mathrm{s}$ when lengths and diameters are in m and densities are in $\mathrm{kg} / \mathrm{m}^{3}$. Note that the factor $g / g_{c}$ equals 1.0 in English units and 9.81 in SI units.

Equation (10.15) can be solved iteratively to obtain the circulation rate and exit vapor fraction. For computer implementation, the integrals appearing in Equations (9.9) and (9.10) can be evaluated by numerical integration rather than using approximate average values of $\rho_{t p}$ and $\phi_{L O}^{2}$.

### 10.5.3 Sensible heating zone

In order to calculate the circulation rate using Equation (10.15), the length, $L_{B C}$, of the sensible heating zone must be determined. Fair's [10] method for estimating $L_{B C}$ is described here. Boiling is assumed to begin when the liquid in the tubes becomes saturated; subcooled boiling is not considered, which is a conservative approach for design purposes.

In flowing from point $B$ to $C$, the fluid pressure decreases due to the elevation change and friction effects. At the same time, the fluid temperature increases due to heat transfer. A linear relationship between the temperature and pressure is assumed:

$$
\begin{equation*}
\frac{T_{C}-T_{B}}{P_{C}-P_{B}}=\frac{(\Delta T / L)}{(\Delta P / L)} \tag{10.16}
\end{equation*}
$$

The saturation curve is linearized about point $A$ to obtain:

$$
\begin{equation*}
\frac{T_{s a t}-T_{A}}{P_{s a t}-P_{A}}=(\Delta T / \Delta P)_{s a t} \tag{10.17}
\end{equation*}
$$

Now at point C, the fluid reaches saturation, so that $T_{C}=T_{s a t}$ and $P_{C}=P_{s a t}$. If heat losses in the reboiler feed line are neglected, then it also follows that $T_{A}=T_{B}$. With these equalities, Equations (10.16) and (10.17) can be combined to obtain the following expression for the pressure at point C:

$$
\begin{equation*}
\frac{P_{B}-P_{C}}{P_{B}-P_{A}}=\frac{(\Delta T / \Delta P)_{s a t}}{(\Delta T / \Delta P)_{s a t}-\frac{(\Delta T / L)}{(\Delta P / L)}} \tag{10.18}
\end{equation*}
$$

If friction losses are neglected, then the pressure differences on the left side of this equation are proportional to elevation differences, i.e.,

$$
\begin{equation*}
\left(P_{B}-P_{C}\right) /\left(P_{B}-P_{A}\right) \cong L_{B C} /\left(z_{A}-z_{B}\right) \tag{10.19}
\end{equation*}
$$

Furthermore, if the liquid level in the column sump is kept at approximately the upper tubesheet level, then $\left(z_{A}-z_{B}\right) \cong L_{B C}+L_{C D}=$ tube length. Equation (10.18) can then be written as:

$$
\begin{equation*}
\frac{L_{B C}}{L_{B C}+L_{C D}} \cong \frac{(\Delta T / \Delta P)_{s a t}}{(\Delta T / \Delta P)_{s a t}-\frac{(\Delta T / L)}{(\Delta P / L)}} \tag{10.20}
\end{equation*}
$$

The left side of this equation is the fractional tube length required for sensible heating.
In order to evaluate $(\Delta T / \Delta P)_{\text {sat }}$, two points on the saturation curve are needed in the vicinity of ( $T_{A}, P_{A}$ ). If the latter point is known from column design calculations, then only one additional point is needed at a temperature somewhat higher than $T_{A}$. For a pure component, this simply entails calculation of the vapor pressure at an appropriate temperature. For a mixture, a bubble-point pressure calculation is required.
The pressure gradient in the sensible heating zone is calculated as follows:

$$
\begin{equation*}
-(\Delta P / L)=\rho_{L}\left(g / g_{c}\right)+\Delta P_{f, B C} / L \tag{10.21}
\end{equation*}
$$

The friction loss term in this equation can usually be neglected. Note that friction losses were neglected in deriving Equation (10.20).
The temperature gradient in the sensible heating zone is estimated as follows:

$$
\begin{equation*}
\Delta T / L=\frac{n_{t} \pi D_{o} U_{D} \Delta T_{m}}{\dot{m}_{i} C_{P, L}} \tag{10.22}
\end{equation*}
$$

Here, $U_{D}$ and $\Delta T_{m}$ are the overall coefficient and mean driving force, respectively, for the sensible heating zone.

### 10.5.4 Mist flow limit

The mist flow regime is avoided in reboiler design due to the large drop in heat-transfer coefficient that accompanies tube wall dryout. Fair [10] presented a simple empirical correlation for the onset of mist flow. Although the correlation was based on a very limited amount of data, it was later verified by Palen et al. [15] over a wide range of data for hydrocarbons, alcohols, water, and their mixtures. The correlation is as follows:

$$
\begin{equation*}
G_{t, m i s t}=1.8 \times 10^{6} X_{t t} \tag{10.23a}
\end{equation*}
$$

where
$G_{t, \text { mist }}=$ tube-side mass flux at onset of mist flow (lbm/h $\cdot \mathrm{ft}^{2}$ )
$X_{t t}=$ Lockhart-Martinelli parameter, Equation (9.37)
In terms of SI units, the corresponding equation is:

$$
\begin{equation*}
G_{t, m i s t}=2.44 \times 10^{3} X_{t t} \tag{10.23b}
\end{equation*}
$$

where $G_{t, \text { mist }} \propto \mathrm{kg} / \mathrm{s} \cdot \mathrm{m}^{2}$. The tube-side mass flux should be kept safely below the value given by Equation (10.23). This will ensure that dryout does not occur, but it is still possible that the design heat flux may exceed the low-vapor-fraction critical heat flux. Hence, the critical heat flux should also be computed and compared with the design heat flux.

### 10.5.5 Flow instabilities

Two-phase flow in pipes is subject to several types of instability that result from compressibility effects and the shape of the pressure-drop-versus-flow-rate relationship [13]. In thermosyphon reboilers, flow instability can result in "chugging" and "geysering", conditions that are characterized by periodic changes in the flow pattern. These conditions occur primarily in the slug flow and plug flow regimes when large slugs of liquid are alternately accelerated and decelerated. These instabilities can cause operational problems in the distillation column, and hence, must be prevented.

The flow in reboiler tubes tends to become more stable as the inlet pressure is reduced. Therefore, a valve or other flow restriction is often placed in the feed line to the reboiler to help stabilize the flow. The valve can also be used to compensate for discrepancies in the system pressure balance.

### 10.5.6 Size limitations

As previously noted, vertical thermosyphon reboilers are subject to size limitations related to support and height considerations. General guidelines are that a maximum of three shells operating in parallel can be supported on a single distillation column, with a maximum total heat-transfer area of approximately $25,000 \mathrm{ft}^{2}$. Tube lengths are usually in the range of $8-20 \mathrm{ft}$, with values of $8-16 \mathrm{ft}$ being most common.

### 10.5.7 Design strategy

The design procedure consists of three main steps: preliminary design, calculation of the circulation rate, and stepwise calculation of the rate of heat transfer and pressure drop in the reboiler tubes.

## Preliminary design

An initial configuration for the reboiler proper is obtained in the usual manner using an approximate overall heat-transfer coefficient along with an overall driving force to estimate the required surface area. The configuration of the feed and return lines must also be established. For recirculating units, the lines can be sized using an initial estimate for the recirculation rate (or equivalently, the exit vapor fraction).

## Circulation rate

The length of the sensible heating zone is first calculated using Equation (10.20). Then Equation (10.15) is solved iteratively to obtain the circulation rate and exit vapor fraction. The mass flux in the tubes should be checked against the value given by Equation (10.23) to ensure that the flow is not in or near the mist flow regime. If the calculated circulation rate and vapor fraction are not acceptable, the piping configuration is modified and the calculations repeated.

## Stepwise calculations

A zone analysis is performed by selecting an increment, $\Delta x$, of the vapor weight fraction. In each vapor-fraction interval, the arithmetic average vapor fraction is used to calculate the boiling heattransfer coefficient, two-phase density, and friction loss. The overall heat-transfer coefficient and average driving force for the interval are used to calculate the tube length required to achieve the increment in vapor fraction.

The pressure drop for each interval is calculated by summing the static, friction, and acceleration losses. The acceleration loss for a given interval, $k$, is calculated using the following modification of Equation (10.11):

$$
\begin{equation*}
\Delta P_{a c c, k}=\frac{G_{t}^{2} \Delta \gamma_{k}}{3.75 \times 10^{12} s_{L}} \tag{10.24}
\end{equation*}
$$

Here $\Delta \gamma_{k}=\Delta\left(\gamma_{k}+1\right)$ is the change in $\gamma$ from the beginning to the end of the $k$ th interval.
For mixtures, thermodynamic (flash) calculations are required to determine the phase compositions and fluid temperature for each interval. These values are needed to obtain fluid physical properties, which in turn are needed for heat-transfer and pressure-drop calculations.

The calculations for each interval are iterative in nature. A value for the heat flux must be assumed to calculate the boiling heat-transfer coefficient, which is needed to calculate the tube length for the interval. From the tube length, a new value for the heat flux is obtained, thereby closing the iterative loop. The thermodynamic and pressure-drop calculations constitute another iterative sequence.

The sum of the pressure drops for all intervals provides an improved estimate for the pressure difference, $P_{D}-P_{C}$, and this value, when combined with the other terms in Equation (10.5), should satisfy the pressure balance. If there is a significant discrepancy, a new circulation rate is computed and the zone analysis is repeated.

Similarly, the sum of the tube lengths for all intervals, including the sensible heating zone, should equal or be slightly less than the actual tube length. If this is not the case, the reboiler configuration is modified and the calculations are repeated. Note that this will require the calculation of a new circulation rate. For an acceptable design, it is also necessary that the heat flux in each zone be less then the critical heat flux.

The accuracy of the stepwise calculations depends on the number of intervals used. A single interval, though generally not very accurate, is the most expedient option for hand calculations. In this case, the circulation rate is not adjusted (unless the reboiler configuration is modified) and only the heat-transfer calculations for the zone are performed.

The following example is a slightly modified version of a problem originally presented by Fair [10]. It involves some simplifying features, e.g., the boiling-side fluid is a pure component, the sizes of the feed and return lines are specified in the problem statement, and constant fluid properties are assumed.

## Example 10.4

A reboiler is required to supply $15,000 \mathrm{lb} / \mathrm{h}$ of vapor to a distillation column that separates cyclohexane as the bottoms product. The heating medium will be steam at a design pressure of 18 psia .

The temperature and pressure below the bottom tray in the column are $182^{\circ} \mathrm{F}$ and 16 psia . Physical property data for cyclohexane at these conditions are given in the following table:

| Property | Liquid | Vapor |
| :--- | :---: | :---: |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 45.0 | 0.200 |
| $\mu(\mathrm{cp})$ | 0.40 | 0.0086 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.45 | - |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.086 | - |
| $\sigma(\mathrm{lbf} / \mathrm{ft})$ | 0.00124 | - |
| $\lambda(\mathrm{Btu} / \mathrm{lbm})$ | 154 | - |
| $\operatorname{Pr}$ | 5.063 | - |

The vapor pressure of cyclohexane is given by the following equation [16], where $P_{s a t} \propto$ torr and $T \propto \mathrm{~K}$ :

$$
P_{\text {sat }}=\exp \left[15.7527-\frac{2766.63}{T-50.50}\right]
$$

The critical pressure of cyclohexane is 590.5 psia.
The feed line to the reboiler will consist of 100 equivalent feet of 6 -in. schedule 40 pipe, and the return line will consist of 50 equivalent feet of $10-\mathrm{in}$. schedule 40 pipe. Design a recirculating vertical thermosyphon reboiler for this service.

## Solution

(a) Make initial specifications.
(i) Fluid placement

Cyclohexane will flow in the tubes with steam in the shell.
(ii) Tubing

One-inch, 14 BWG tubes with a length of 8 ft are specified. Relatively short tubes are used in order to minimize the liquid height in the column sump.
(iii) Shell and head types

A TEMA E-shell is chosen for a vertical thermosyphon reboiler. Since condensing steam is a clean fluid, a fixed-tubesheet configuration can be used. Channel-type heads are selected for ease of tubesheet access. Thus, an AEL configuration is specified. A somewhat less expensive NEN configuration could also be used.
(iv) Tube layout

A triangular layout with a tube pitch of 1.25 in. is specified since mechanical cleaning of the external tube surfaces is not required.
(v) Baffles

Segmental baffles with a $35 \%$ cut and a spacing of $B / D_{s} \cong 0.4$ are specified based on the recommendation for condensing vapors given in Figure 5.4.
(vi) Sealing strips

None are required for a fixed-tubesheet exchanger.
(vii) Construction materials

Since neither stream is corrosive, plain carbon steel is specified for all components.
(b) Energy balance and steam flow rate.

The reboiler duty is obtained from the vapor generation rate and the latent heat of vaporization for cyclohexane:

$$
q=\dot{m}_{V} \lambda=15,000 \times 154=2.31 \times 10^{6} \mathrm{Btu} / \mathrm{h}
$$

From Table A.8, the latent heat of condensation for steam at 18 psia is $963.7 \mathrm{Btu} / \mathrm{lbm}$. Therefore, the steam flow rate is:

$$
\dot{m}_{\text {steam }}=q / \lambda_{\text {steam }}=2.31 \times 10^{6} / 963.7=2397 \mathrm{lbm} / \mathrm{h}
$$

(c) Mean temperature difference.

From Table A.8, the temperature of saturated steam at 18 psia is $222.4^{\circ} \mathrm{F}$. Assuming that cyclohexane vaporizes at a constant temperature of $182^{\circ} \mathrm{F}$, i.e., neglecting pressure effects in the reboiler system, we have:

$$
\Delta T_{m}=222.4-182=40.4^{\circ} \mathrm{F}
$$

(d) Heat-transfer area and number of tubes.

Based on Table 3.5, an overall heat-transfer coefficient of $250 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ is assumed. The required area is then:

$$
A=\frac{q}{U_{D} \Delta T_{m}}=\frac{2.31 \times 10^{6}}{250 \times 40.4}=228.7 \mathrm{ft}^{2}
$$

The corresponding number of tubes is:

$$
n_{t}=\frac{A}{\pi D_{o} L}=\frac{228.7}{\pi(1 / 12) \times 8} \cong 109
$$

(e) Number of tube passes and actual tube count.

A single tube pass is used for a vertical thermosyphon reboiler. From Table C.6, the closest tube count is 106 tubes in a 15.25 -in. shell.

This completes the preliminary design of the reboiler system. Since the piping configuration was specified in the problem statement, sizing of the feed and return lines is not required here. The circulation rate is calculated in the steps that follow; only the final iteration is presented.
(f) Estimated circulation rate.

Assume an exit vapor fraction of $13.2 \%$, i.e., $x_{e}=0.132$. The corresponding circulation rate is:

$$
\dot{m}_{i}=\frac{\dot{m}_{V}}{x_{e}}=\frac{15,000}{0.132}=113,636 \mathrm{lbm} / \mathrm{h}
$$

(g) Friction factors.

The internal diameters for the tubes, inlet line, and exit line are obtained from Tables B. 1 and B.2:

$$
\begin{aligned}
& D_{t}=0.834 \mathrm{in} .=0.0695 \mathrm{ft} \\
& D_{\text {in }}=6.065 \mathrm{in} .=0.5054 \mathrm{ft} \\
& D_{e x}=10.02 \text { in. }=0.835 \mathrm{ft}
\end{aligned}
$$

The corresponding Reynolds numbers are computed next, based on all-liquid flow:

$$
\begin{aligned}
R e_{t} & =\frac{4 \dot{m}_{i}}{n_{t} \pi D_{t} \mu_{L}}=\frac{4 \times 113,636}{106 \times \pi \times 0.0695 \times 0.4 \times 2.419}=20,297 \\
R e_{i n} & =\frac{4 \dot{m}_{i}}{\pi D_{i n} \mu_{L}}=\frac{4 \times 113,636}{\pi \times 0.5054 \times 0.4 \times 2.419}=295,866 \\
R e_{L o, e x} & =\frac{4 \dot{m}_{i}}{\pi D_{e x} \mu_{L}}=\frac{4 \times 113,636}{\pi \times 0.835 \times 0.4 \times 2.419}=179,079
\end{aligned}
$$

Equations (4.8) and (5.2) are used to calculate the friction factors for the pipes and tubes, respectively:

$$
\begin{aligned}
f_{t} & =0.4137 R e_{t}^{-0.2585}=0.4137(20,297)^{-0.2585}=0.0319 \\
f_{i n} & =0.3673 R e_{i n}^{-0.2314}=0.3673(295,866)^{-0.2314}=0.0199 \\
f_{e x} & =0.3673 R e_{L O, e x}^{-0.2314}
\end{aligned}=0.3673(179,079)^{-0.2314}=0.0224
$$

(h) Sensible heating zone.
(i) Slope of saturation curve

Conditions in the column sump are first checked by calculating the vapor pressure of cyclohexane at the given temperature of $182^{\circ} \mathrm{F}=356.7 \mathrm{~K}$ :

$$
\begin{aligned}
& P_{\text {sat }}=\exp \left[15.7527-\frac{2766.63}{356.7-50.50}\right]=826.6 \text { torr } \\
& P_{\text {sat }}=826.6 \text { torr } \times \frac{14.696 \mathrm{psi} / \mathrm{atm}}{760 \mathrm{torr} / \mathrm{atm}}=15.98 \mathrm{psia}
\end{aligned}
$$

This value is in close agreement with the stated pressure of 16 psia below the bottom tray in the column. Next, the vapor pressure is calculated at a somewhat higher temperature, $192^{\circ} \mathrm{F}=362.2 \mathrm{~K}$ :

$$
\begin{aligned}
& P_{\text {sat }}=\exp \left[15.7527-\frac{2766.63}{362.2-50.50}\right]=969.5 \text { torr } \\
& P_{\text {sat }}=969.5 \times 14.696 / 760=18.75 \mathrm{psia}
\end{aligned}
$$

The required slope is obtained as follows:

$$
(\Delta T / \Delta P)_{s a t}=\frac{192-182}{18.75-15.98}=3.61^{\circ} \mathrm{F} / \mathrm{psi}
$$

(ii) Pressure gradient

The pressure gradient in the sensible heating zone is estimated using Equation (10.21), neglecting the friction loss term:

$$
-(\Delta P / L)=\frac{\rho_{L}\left(g / g_{c}\right)}{144}=\frac{45 \times 1.0}{144}=0.3125 \mathrm{psi} / \mathrm{ft}
$$

(iii) Temperature gradient

To estimate the temperature gradient in the sensible heating zone, the heat-transfer coefficient for all-liquid flow in the tubes is calculated using the Seider-Tate equation:

$$
\begin{aligned}
h_{L O} & =\left(k_{L} / D_{t}\right) \times 0.023 \operatorname{Re}_{t}^{0.8} \operatorname{Pr}_{L}^{1 / 3} \\
& =(0.086 / 0.0695) \times 0.023(20,297)^{0.8}(5.063)^{1 / 3} \\
h_{L O} & =136 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

The overall coefficient is calculated assuming a film coefficient (including fouling) of $1500 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ for steam and a fouling allowance for cyclohexane of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ :

$$
\begin{aligned}
U_{D} & =\left[\left(D_{o} / D_{t}\right)\left(\frac{1}{h_{L O}}+R_{D i}\right)+\frac{D_{o} \ln \left(D_{o} / D_{t}\right)}{2 k_{\text {tube }}}+\left(1 / h_{o}+R_{D o}\right)\right]^{-1} \\
& =\left[(1.0 / 0.834)\left(\frac{1}{136}+0.001\right)+\frac{(1 / 12) \ln (1.0 / 0.834)}{2 \times 26}+\frac{1}{1500}\right]^{-1} \\
U_{D} & \cong 91 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

The temperature gradient is calculated using Equation (10.22) with a mean temperature difference of approximately $40^{\circ} \mathrm{F}$ :

$$
\Delta T / L=\frac{n_{t} \pi D_{o} U_{D} \Delta T_{m}}{\dot{m}_{i} C_{P, L}}=\frac{106 \pi(1 / 12) \times 91 \times 40}{113,636 \times 0.45}=1.975^{\circ} \mathrm{F} / \mathrm{ft}
$$

(iv) Length of sensible heating zone

The fractional length of the sensible heating zone is estimated using Equation (10.20):

$$
\begin{aligned}
\frac{L_{B C}}{L_{B C}+L_{C D}} & =\frac{(\Delta T / \Delta P)_{s a t}}{(\Delta T / \Delta P)_{s a t}-\frac{(\Delta T / L)}{(\Delta P / L)}} \\
\frac{L_{B C}}{8} & =\frac{3.61}{3.61+\frac{1.975}{0.3125}}=0.364 \\
L_{B C} & \cong 2.9 \mathrm{ft}
\end{aligned}
$$

It follows that $L_{C D} \cong L_{A C} \cong 5.1 \mathrm{ft}$. It is assumed that the liquid level in the column sump is maintained at approximately the elevation of the upper tubesheet in the reboiler.
(i) Average two-phase density.

The two-phase density is calculated at a vapor fraction of $x_{e} / 3=0.044$. The Lockhart-Martinelli parameter is calculated using Equation (9.37):

$$
\begin{aligned}
X_{t t} & =\left(\frac{1-x}{x}\right)^{0.9}\left(\rho_{V} / \rho_{L}\right)^{0.5}\left(\mu_{L} / \mu_{V}\right)^{0.1} \\
& =\left(\frac{1-0.044}{0.044}\right)^{0.9}(0.2 / 45)^{0.5}(0.4 / 0.0086)^{0.1} \\
X_{t t} & =1.563
\end{aligned}
$$

Since this value is greater than unity, the Chisholm correlation, Equation (9.63), gives the slip ratio as:

$$
S R=\left(\rho_{L} / \rho_{\mathrm{hom}}\right)^{0.5}
$$

The homogeneous density is given by Equation (9.51):

$$
\begin{aligned}
\rho_{\mathrm{hom}} & =\left[x / \rho_{V}+(1-x) / \rho_{L}\right]^{-1}=[0.044 / 0.2+0.956 / 45]^{-1} \\
\rho_{\mathrm{hom}} & =4.1452 \mathrm{lbm} / \mathrm{ft}^{3}
\end{aligned}
$$

Substitution into the above equation gives the slip ratio:

$$
S R=(45 / 4.1452)^{0.5}=3.295
$$

Next, the void fraction is computed using Equation (9.59).

$$
\begin{aligned}
& \varepsilon_{V}=\frac{x}{x+S R(1-x) \rho_{V} / \rho_{L}}=\frac{0.044}{0.044+3.295 \times 0.956 \times 0.2 / 45} \\
& \varepsilon_{V}=0.7586
\end{aligned}
$$

Finally, the two-phase density is computed from Equation (9.54):

$$
\begin{aligned}
& \bar{\rho}_{t p}=\varepsilon_{V} \rho_{V}+\left(1-\varepsilon_{V}\right) \rho_{L}=0.7586 \times 0.2+0.2414 \times 45 \\
& \bar{\rho}_{t p}=11.01 \mathrm{lbm} / \mathrm{ft}^{3}
\end{aligned}
$$

(j) Average two-phase multiplier.

The two-phase multiplier is calculated at a vapor fraction of $2 x_{e} / 3=0.088$. The MüllerSteinhagen and Heck (MSH) correlation, Equation (9.53), is used here:

$$
\bar{\phi}_{L O}^{2}=Y^{2} x^{3}+\left[1+2 x\left(Y^{2}-1\right)\right](1-x)^{1 / 3}
$$

The Chisholm parameter, $Y$, is calculated using Equation (9.42) with $n=0.2585$ for heatexchanger tubes:

$$
\begin{aligned}
& Y=\left(\rho_{L} / \rho_{V}\right)^{0.5}\left(\mu_{V} / \mu_{L}\right)^{n / 2}=(45 / 0.2)^{0.5}(0.0086 / 0.4)^{0.2585 / 2} \\
& Y=9.13
\end{aligned}
$$

Substituting in the MSH correlation gives:

$$
\begin{aligned}
& \bar{\phi}_{L O}^{2}=(9.13)^{2}(0.088)^{3}+\left\{1+2 \times 0.088\left((9.13)^{2}-1\right)\right\}(0.912)^{1 / 3} \\
& \bar{\phi}_{L O}^{2}=15.08
\end{aligned}
$$

(k) Two-phase multiplier for exit line.

The above calculation is repeated with $x=x_{e}=0.132$. For the exit pipe, however, the Chisholm parameter is calculated with $n=0.2314$. Thus,

$$
\begin{aligned}
& Y=(45 / 0.2)^{0.5}(0.0086 / 0.4)^{0.2314 / 2}=9.62 \\
& \phi_{L O_{e x}}^{2}=(9.62)^{2}(0.132)^{3}+\left\{1+2 \times 0.132\left((9.62)^{2}-1\right)\right\}(0.868)^{1 / 3} \\
& \phi_{L O_{e x}}^{2}= 24.22
\end{aligned}
$$

(l) Exit void fraction.

At $x=x_{e}=0.132$, the Lockhart-Martinelli parameter is:

$$
X_{t t}=\left(\frac{1-0.132}{0.132}\right)^{0.9}(0.2 / 45)^{0.5}(0.4 / 0.0086)^{0.1}=0.533
$$

Since this value is less than 1.0 , the Chisholm correlation gives the slip ratio as:

$$
S R=\left(\rho_{L} / \rho_{V}\right)^{0.25}=(45 / 0.2)^{0.25}=3.873
$$

From Equation (9.59), the void fraction is:

$$
\begin{aligned}
& \varepsilon_{V, e}=\frac{x_{e}}{x_{e}+S R\left(1-x_{e}\right) \rho_{V} / \rho_{L}}=\frac{0.132}{0.132+3.873 \times 0.868 \times 0.2 / 45} \\
& \varepsilon_{V, e}=0.8983
\end{aligned}
$$

(m) Acceleration parameter.

The acceleration parameter, $\gamma$, is given by Equation (10.12):

$$
\begin{aligned}
& \gamma=\frac{\left(1-x_{e}\right)^{2}}{1-\varepsilon_{V, e}}+\frac{\rho_{L} x_{e}^{2}}{\rho_{V} \varepsilon_{V, e}}-1=\frac{0.868}{0.1017}+\frac{45(0.132)^{2}}{0.2 \times 0.8983}-1 \\
& \gamma=10.77
\end{aligned}
$$

(n) Circulation rate.

Equation (10.15) is used to obtain a new estimate of the circulation rate. Due to the complexity of the equation, the individual terms are computed separately, starting with the numerator:

$$
\begin{aligned}
\text { numerator } & =3.2 \times 10^{10} D_{t}^{5} s_{L}\left(g / g_{c}\right)\left(\rho_{L} L_{A C}-\bar{\rho}_{t p} L_{C D}\right) \\
& =3.2 \times 10^{10}(0.0695)^{5}(45 / 62.43)(1.0)(45 \times 5.1-11.01 \times 5.1) \\
\text { numerator } & =6,483,575
\end{aligned}
$$

Each of the four terms in the denominator is computed next:

$$
\begin{aligned}
& \text { term } 1=2 D_{t}\left\{(\gamma+1)\left(\frac{D_{t}}{D_{e x}}\right)^{4}-\frac{1}{n_{t}^{2}}\right\}=2 \times 0.0695\left\{11.77\left(\frac{0.0695}{0.835}\right)^{4}-\frac{1}{(106)^{2}}\right\} \\
& \text { term } 1=6.6150 \times 10^{-5} \\
& \text { term } 2=f_{\text {in }} L_{\text {in }}\left(D_{t} / D_{i n}\right)^{5}=0.0199 \times 100(0.0695 / 0.5054)^{5} \\
& \text { term } 2=9.7859 \times 10^{-5} \\
& \text { term } 3=\left(f_{t} / n_{t}^{2}\right)\left(L_{B C}+L_{C D} \bar{\phi}_{L O}^{2}\right)=\frac{0.0319}{(106)^{2}}(2.9+5.1 \times 15.08) \\
& \text { term } 3=2.2658 \times 10^{-4}=22.658 \times 10^{-5} \\
& \text { term } 4=f_{e x} L_{e x} \phi_{L O, e x}^{2}\left(D_{t} / D_{e x}\right)^{5}=0.0224 \times 50 \times 24.22(0.0695 / 0.835)^{5} \\
& \text { term } 4=1.0836 \times 10^{-4}=10.836 \times 10^{-5}
\end{aligned}
$$

Substituting the above values into Equation (10.15) gives:

$$
\begin{aligned}
\dot{m}_{i}^{2} & =\frac{6,483,575}{(6.6150+9.7859+22.658+10.836) \times 10^{-5}}=1.2994 \times 10^{10} \\
\dot{m}_{i} & =113,991 \mathrm{lbm} / \mathrm{h}
\end{aligned}
$$

This value agrees with the assumed flow rate of $113,636 \mathrm{lbm} / \mathrm{h}$ to within about $0.3 \%$, which is more than adequate for convergence. The average of the assumed and calculated values is taken as the final value, i.e.,

$$
\dot{m}_{i}=\frac{113,991+113,636}{2} \cong 113,814 \mathrm{lbm} / \mathrm{h}
$$

(o) Mist flow limit.

The mass flux at the onset of mist flow is given by Equation (10.23a):

$$
G_{t, m i s t}=1.8 \times 10^{6} X_{t t}=1.8 \times 10^{6} \times 0.533=959,400 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

The actual mass flux in the tubes is:

$$
G_{t}=\frac{\dot{m}_{i}}{n_{t}(\pi / 4) D_{t}^{2}}=\frac{113,814}{106(\pi / 4)(0.0695)^{2}}=283,029 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

The actual mass flux is far below the mist flow limit, as would be expected with a vapor fraction of only about $13 \%$.

This completes the circulation rate calculation. The following steps deal with the zone analysis (stepwise calculations). To simplify matters, a single boiling zone is used. In this case, the pressure drop in the tubes is not recalculated and the circulation rate is not adjusted. Therefore, only heattransfer calculations are involved in the zone analysis.
(p) Duty in boiling zone.

The cyclohexane temperature in the boiling zone is estimated based on the temperature gradient calculated above:

$$
T_{c y h x}=182+(\Delta T / L) L_{B C}=182+1.975 \times 2.9 \cong 187.7^{\circ} \mathrm{F}
$$

Hence, the duty in the sensible heating zone is that required to raise the temperature of the liquid by $5.7^{\circ} \mathrm{F}$ :

$$
q_{B C}=\dot{m}_{i} C_{P, L} \Delta T_{B C}=113,814 \times 0.45 \times 5.7=291,933 \mathrm{Btu} / \mathrm{h}
$$

The duty for the boiling zone is the total duty minus the duty for the sensible heating zone. Thus,

$$
q_{C D}=q-q_{B C}=2.31 \times 10^{6}-291,933 \cong 2.018 \times 10^{6} \mathrm{Btu} / \mathrm{h}
$$

(q) Boiling heat-transfer coefficient.

Since the boiling fluid is a pure component, the Liu-Winterton correlation, Equation (9.80), is used to calculate the heat-transfer coefficient. The average vapor weight fraction for the zone is used in the calculations, i.e., $x=0.132 / 2=0.066$.

$$
h_{b}=\left[\left(S_{L W} h_{n b}\right)^{2}+\left(E_{L W} h_{L}\right)^{2}\right]^{1 / 2}
$$

(i) The enhancement factor

The convective enhancement factor, $E_{L W}$, is given by Equation (9.82):

$$
\begin{aligned}
E_{L W} & =\left[1+x \operatorname{Pr}_{L}\left(\rho_{L}-\rho_{V}\right) / \rho_{V}\right]^{0.35} \\
& =[1+0.066 \times 5.063(45-0.2) / 0.2]^{0.35} \\
E_{L W} & =4.550
\end{aligned}
$$

(ii) The suppression factor

The nucleate boiling suppression factor, $S_{L W}$, is given by Equation (9.81):

$$
S_{L W}=\left[1+0.055 E_{L W}^{0.1} R e_{L}^{0.16}\right]^{-1}
$$

The Reynolds number is calculated for the liquid phase flowing alone in the tubes:

$$
\begin{aligned}
& R e_{L}=\frac{4(1-x)\left(\dot{m}_{i} / n_{t}\right)}{\pi D_{t} \mu_{l}}=\frac{4(1-0.066)(113,814 / 106)}{\pi \times 0.0695 \times 0.4 \times 2.419} \\
& R e_{L}=18,987
\end{aligned}
$$

Substituting into the above equation for $S_{L W}$ gives:

$$
S_{L W}=\left[1+0.055(4.550)^{0.1}(18,987)^{0.16}\right]^{-1}=0.7636
$$

(iii) Convective heat-transfer coefficient

The Dittus-Boelter correlation, Equation (9.75), is used in conjunction with the Liu-Winterton correlation to calculate $h_{L}$.

$$
\begin{aligned}
h_{L} & =0.023\left(k_{L} / D_{t}\right) R e_{L}^{0.8} \operatorname{Pr}_{L}^{0.4} \\
& =0.023(0.086 / 0.0695)(18,987)^{0.8}(5.063)^{0.4} \\
h_{L} & =144 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(iv) Nucleate boiling heat-transfer coefficient

The Cooper correlation in the form of Equation (9.6a) is used to calculate $h_{n b}$ :

$$
h_{n b}=21 \hat{q}^{0.67} P_{r}^{0.12}\left(-\log _{10} P_{r}\right)^{-0.55} M^{-0.5}
$$

For cyclohexane, the molecular weight is $M=84$. The pressure in the boiling zone is estimated as the vapor pressure of cyclohexane at $187.7^{\circ} \mathrm{F}=359.8 \mathrm{~K}$ :

$$
P_{\text {sat }}=\exp \left[15.7527-\frac{2766.63}{359.8-50.50}\right]=904.96 \text { torr }=17.5 \mathrm{psia}
$$

The reduced pressure is then:

$$
P_{r}=P / P_{c}=17.5 / 590.5=0.0296
$$

The heat flux is estimated using the total duty and total tube length, as follows:

$$
\hat{q} \cong \frac{2.31 \times 10^{6}}{106 \pi \times 0.0695 \times 8}=12,476 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

Substituting into the above equation for $h_{n b}$ gives:

$$
\begin{aligned}
& h_{n b}=21(12,476)^{0.67}(0.0296)^{0.12}\left(-\log _{10} 0.0296\right)^{-0.55}(84)^{-0.5} \\
& h_{n b}=660 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(v) Convective boiling coefficient

Substituting the results from the above steps into the Liu-Winterton correlation gives the following result for $h_{b}$ :

$$
h_{b}=\left[(0.7636 \times 660)^{2}+(4.550 \times 144)^{2}\right]^{1 / 2}=827 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(r) Overall coefficient.

Due to the higher velocity and greater agitation in the boiling zone, a fouling factor of $0.0005 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is deemed appropriate for cyclohexane. A film coefficient, including fouling allowance, of $1500 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ is again assumed for steam. The overall heat-transfer coefficient for the boiling zone is then:

$$
\begin{aligned}
U_{D} & =\left[\frac{D_{o}}{D_{i}}\left(\frac{1}{h_{i}}+R_{D i}\right)+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k_{\text {tube }}}+\left(\frac{1}{h_{o}}+R_{D o}\right)\right]^{-1} \\
& =\left[\frac{1.0}{0.834}\left(\frac{1}{827}+0.0005\right)+\frac{(1 / 12) \ln (1.0 / 0.834)}{2 \times 26}+\frac{1}{1500}\right]^{-1} \\
U_{D} & =332.6 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(s) Check heat flux and iterate if necessary.

The mean temperature difference for the boiling zone is taken as:

$$
\Delta T_{m}=T_{\text {steam }}-T_{\text {cyhx }}=222.4-187.7=34.7^{\circ} \mathrm{F}
$$

Since the saturation temperature decreases with decreasing pressure, both the steam and cyclohexane temperatures will vary somewhat over the length of the boiling zone due to the pressure drops experienced by the two streams. These effects are neglected here. Thus, the heat flux is:

$$
\hat{q}=U_{D} \Delta T_{m}=332.6 \times 34.7=11,541 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

This value is within $10 \%$ of the initial estimate of $12,476 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$. After a few more iterations, the following converged values are obtained:

$$
\begin{aligned}
h_{n b} & =622 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
h_{b} & =809 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
U_{D} & =329 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\hat{q} & =11,416 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

(t) Tube length.

The tube length required for the boiling zone is calculated as follows:

$$
L_{\text {req }}=\frac{q_{C D}}{n_{t} \pi D_{o} U_{D} \Delta T_{m}}=\frac{2.018 \times 10^{6}}{106 \pi(1 / 12) \times 329 \times 34.7} \cong 6.4 \mathrm{ft}
$$

This value is greater than the available length of 5.1 ft , indicating that the reboiler is somewhat under-sized.
(u) Critical heat flux.

For brevity, the critical heat flux is estimated using Palen's method as given by Equation (9.84a):

$$
\begin{aligned}
\hat{q}_{c} & =16,070\left(D_{t}^{2} / L\right)^{0.35} P_{c}^{0.61} P_{r}^{0.25}\left(1-P_{r}\right) \\
& =16,070\left[(0.0695)^{2} / 8\right]^{0.35}(590.5)^{0.61}(0.0296)^{0.25}(1-0.0296) \\
\hat{q}_{c} & \cong 23,690 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\hat{q} / \hat{q}_{c} & =11,416 / 23,690 \cong 0.48
\end{aligned}
$$

Thus, the heat flux is safely below the critical value.
(v) Design modification.

Based on the above calculations, the only problem with the initial design is that the unit is under-sized. The under-surfacing is due to the presence of a significant sensible heating zone that was not considered in the preliminary design. Although a more rigorous analysis using more zones might yield a different result, it is assumed here that some modification of the initial design is required. Three possible design changes are the following:
(i) Increase the tube length from 8 to 10 ft . This change will increase the static head and, hence, the degree of subcooling at the reboiler entrance. It will thus tend to increase the length of the sensible heating zone.
(ii) Increase the number of tubes. From the tube-count table, the next largest unit is a $17.25-\mathrm{in}$. shell containing 147 tubes. This represents an increase of about $39 \%$ in heattransfer area, whereas the initial design is under-surfaced by less than $20 \%$.
(iii) Raise the steam temperature by $5-8^{\circ} \mathrm{F}$, corresponding to a steam pressure of $20-21 \mathrm{psia}$. This change will reduce the tube length required in both the sensible heating and boiling zones. Of the three options considered here, this one appears to be the simplest and most cost effective.
Each of the above changes will affect the circulation rate; therefore, verification requires essentially complete recalculation for each case. Due to the lengthiness of the calculations, no further analysis is presented here.

### 10.6 Computer Software

### 10.6.1 HEXTRAN

The shell-and-tube module in HEXTRAN is used for reboilers and condensers, as well as for singlephase heat exchangers. For streams defined as compositional type, the software automatically detects phase changes and uses the appropriate computational methods. A zone analysis is always performed for operations involving a phase change. The HEXTRAN documentation states that Chen's method is used for boiling heat-transfer calculations, but little additional information is provided.

Connecting piping is not integrated with the heat-exchanger modules in HEXTRAN. A separate piping module exists that can be used to calculate pressure losses in the reboiler feed and return lines. Pipe fittings are handled by means of either flow resistance coefficients or equivalent lengths, and two-phase flow calculations are performed automatically. Pressure changes due to friction, acceleration, and elevation change are accounted for. However, the software does not automatically calculate the circulation rate for a thermosyphon reboiler, which is a significant drawback for design work.

The following two examples examine some of the attributes of HEXTRAN (version 9.1) with regard to reboiler applications.

## Example 10.5

Use HEXTRAN to rate the kettle reboiler designed in Example 10.2, and compare the results with those obtained previously by hand.

## Solution

Under Units of Measure, the English system of units is selected. Then, under Components and Thermodynamics, propane, $i$-butane, and $n$-butane are selected from the list of library components by double-clicking on each desired component. (Note that water is not required as a component for this problem.) The Peng-Robinson (PR) equation of state is selected as the principal thermodynamic method for the light hydrocarbon mixture. Thus, a New Method Slate called (arbitrarily) SET1 is defined on the Method tab and the options shown below are chosen from the pop-up lists obtained by right-clicking on the items in the thermodynamic data tree.


The API method for liquid density is chosen because it should be more reliable than the PR method for hydrocarbons. For transport properties, the Library method designates that property values are obtained from the program's pure-component databank. No methods are required for entropy or inspection property data in this problem.

After setting up the flowsheet, the tube-side feed stream is defined as a Water/Steam stream by right-clicking on the stream and selecting Change Configuration from the pop-up menu. Doubleclicking on the stream brings up the Specifications form, where the pressure is set to 20 psia , and the flow rate is specified as $5645 \mathrm{lb} / \mathrm{h}$ of steam. Saturated steam tables will automatically be used by the program to obtain property values for this stream.

The shell-side feed stream is defined as a compositional stream, i.e., a stream having a defined composition, which is the default category. On the Specifications form its thermal condition is set by entering the pressure ( 250 psia ) for the first specification and selecting Bubble Point for the second specification. The total stream flow rate $(96,000 \mathrm{lb} / \mathrm{h})$ is also entered. The stream composition is specified by entering the mole percent of each component in place of the component (molar) flow
rates. When these values sum to 100 , they are automatically interpreted as percentages by the program.

Data for the exchanger are obtained from Example 10.2 and entered on the appropriate forms, with the exception of the shell ID, which is not specified. The reason is that when the correct value of 23.25 in . is entered, the program gives an error message and fails to generate a solution, apparently due to a bug in the software. When the shell ID is not specified, the program calculates the diameter based on the tube data supplied. In the present case it calculates a diameter of 23 in., which is essentially the correct result. In addition to the data from Example 10.2, a fouling factor of $0.0005 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is specified for steam. Fouling factors for both streams are entered on the Film Options form.

Finally, under Input/Calculation Options, the maximum number of iterations for the flowsheet is set to 100 because the default value of 30 proved to be insufficient for this problem.

The input file generated by the HEXTRAN GUI is given below, followed by a summary of results extracted from the HEXTRAN output file. From the latter it can be seen that the reboiler generates $48,571 \mathrm{lb} / \mathrm{h}$ of vapor, which is slightly more than the required rate of $48,000 \mathrm{lb} / \mathrm{h}$. Thus, it appears that the unit is sized almost perfectly. In fact, however, the amount of vapor generated by the unit is limited by the amount of steam supplied, rather than by the available heat-transfer area. Referring to the zone analysis data given below, it is seen that all the steam condenses in the first five zones, leaving only condensate to be subcooled in the last zone. The area contained in the last zone is $117.2 \mathrm{ft}^{2}$, which is about $16 \%$ of the total surface area in the reboiler. Thus, according to HEXTRAN, the unit is about $16 \%$ over-sized. Indeed, if the steam flow rate is increased to $6850 \mathrm{lb} / \mathrm{h}$, the subcooled condensate zone is eliminated and the amount of vapor generated increases to $58,349 \mathrm{lb} / \mathrm{h}$.

The following table compares results from HEXTRAN with those obtained by hand in Example 10.2 . As expected, the boiling heat-transfer coefficient calculated by hand is considerably more conservative than the value computed by HEXTRAN. However, the effective coefficient for steam used in Example 10.2 is actually much higher than the value computed by HEXTRAN. This result is due to the fouling factor used for steam in the present example, without which the effective steam coefficient for HEXTRAN would be about $1760 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. The steam-side pressure drop found by HEXTRAN is comparable to the value estimated by hand. Not surprisingly, the boiling-side pressure drop calculated by HEXTRAN is much smaller than the value assumed (as an upper bound) in the hand calculations. Finally, the mean temperature difference used in the hand calculations is quite close to the weighted average value from HEXTRAN.

| Item | Hand | HEXTRAN |
| :--- | :---: | :---: |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 523 | $936^{\mathrm{a}}$ |
| $\left\{\left(D_{o} / D_{i}\right)\left(1 / \mathrm{h} i+R_{D i}\right)\right\}^{-1}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 1,500 (assumed) | $857^{\mathrm{a}}$ |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 297 | $335^{\mathrm{a}}$ |
| $\Delta P_{i}(\mathrm{psi})$ | 0.3 | 0.43 |
| $\Delta P_{o}(\mathrm{psi})($ (friction + acceleration $)$ | $0.2^{\mathrm{b}}$ (assumed) | 0.05 |
| $\Delta T_{m}\left({ }^{\circ} \mathrm{F}\right)$ | 25.6 | $27.1^{\mathrm{a}}$ |

${ }^{\text {a }}$ Area-weighted average over first five zones; subcooled condensate zone not included.
${ }^{\mathrm{b}}$ Excluding nozzle losses.

## HEXTRAN Input File for Example 10.5

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=Example 10-5, PROBLEM=Kettle Reboiler, SITE=
$
```

```
HEXTRAN Input File for Example 10.5 (continued)
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
        ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
        PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
        UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=CP, WT=LB, *
        XDENSITY=API, STDVAPOR=379.490
$
PRINT ALL, *
        RATE=M
$
CALC PGEN=New, WATER=Saturated
$
$ Component Data Section
$
COMPONENT DATA
$
    LIBID 1, PROPANE /*
        2, IBUTANE /*
        3, BUTANE
$
$ Thermodynamic Data Section
$
THERMODYNAMIC DATA
$
    METHODS SET=SET1, KVALUE=PR, ENTHALPY(L) =PR, ENTHALPY(V)=PR, *
                                    DENSITY(L)=API, DENSITY(V)=PR, VISCOS(L)=LIBRARY, *
                                    VISCOS(V)=LIBRARY, CONDUCT(L)=LIBRARY, CONDUCT(V)=LIBRARY, *
                                    SURFACE=LIBRARY
$
    WATER DECANT=ON, SOLUBILITY = Simsci, PROP = Saturated
$
$Stream Data Section
$
STREAM DATA
$
    PROP STRM=PROD, NAME=PROD
$
    PROP STRM=CONDENSATE, NAME=CONDENSATE
$
    PROP STRM=STEAM, NAME=STEAM, PRES=20.000, STEAM=5645.000
$
    PROP STRM=FEED, NAME=FEED, PRES=250.000, PHASE=L, *
                RATE (W)=96000.000, *
        COMP (M) = 1, 15 / *
                        2, 25 / 3, 60
$
$ Calculation Type Section
$
SIMULATION
$
    TOLERANCE TTRIAL=0.01
$
    LIMITS AREA=200.00, 6000.00, SERIES=1, 10, PDAMP=0.00, *
                TTRIAL=100
$
    CALC TWOPHASE=New, DPSMETHOD=Stream, MINFT=0.80
$
    PRINT UNITS, ECONOMICS, STREAM, STANDARD, *
        EXTENDED, ZONES
$
```


## HEXTRAN Input File for Example 10.5 (continued)

```
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR
$
    UTCOST OIL=3.50, GAS=3.50, ELECTRICITY=0.10, *
        WATER=0.03, HPSTEAM=4.10, MPSTEAM=3.90, *
        LPSTEAM=3.60, REFRIGERANT=0.00, HEATINGMEDIUM=0.00
$
    HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        EXPONENT=0.60, CONSTANT=0.00, UNIT
$
$ Unit Operations Data
$
UNIT OPERATIONS
$
STE UID=KETTLE
    TYPE Old, TEMA=BKU, HOTSIDE=Tubeside, ORIENTATION=Horizontal, *
        FLOW=Countercurrent, *
        UESTIMATE=50.00, USCALER=1.00
    TUBE FEED=STEAM, PRODUCT=CONDENSATE, *
        LENGTH=13.00, OD=1.000, *
        BWG=14, NUMBER=212, PASS=2, PATTERN=90, *
        PITCH=1.2500, MATERIAL=1, *
        FOUL=0.0005, LAYER=0, *
        DPSCALER=1.00
$
SHELL FEED=FEED, PRODUCT=PROD, *
    SERIES=1, PARALLEL=1, *
    MATERIAL=1, *
    FOUL=0.0005, LAYER=0, *
    DPSCALER=1.00
$
    BAFF NONE
$
    TNOZZ TYPE=Conventional, ID=6.065, 3.068, NUMB=1, 1
$
    SNOZZ TYPE=Conventional , ID=5.047, 6.065, NUMB=2, 2
$
    LNOZZ ID=4.026, NUMB=1
$
    CALC TWOPHASE=New, *
        DPSMETHOD=Stream, *
        MINFT=0.80
$
    PRINT STANDARD, *
        EXTENDED, *
        ZONES
$
    COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        CONSTANT=0.00, EXPONENT=0.60, Unit
$
$ End of keyword file...
```


## HEXTRAN Output Data for Example 10.5



## HEXTRAN Output Data for Example 10.5 (continued)



## HEXTRAN Output Data for Example 10.5 (continued)

|  | ZONE ANALYSIS FOR EXCHANGER KETTLE |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | TEMPERATURE - PRESSURE SUMMARY |  |  |  |  |
| ZONE | TEMPERATURE IN/OUT DEG F |  | PRESSURE | IN / OUT | PSIA |
|  | SHELL-SIDE | TUBE-SIDE | SHELL-SIDE |  | BE-SIDE |
| 1 | 201.0/ 202.4 | 228.3/228.0 | 250.0/ 249 |  | 0.0/ 19.9 |
| 2 | 200.8/ 201.0 | 228.0/ 228.0 | 250.0/ 250 |  | 9.9/ 19.9 |
| 3 | 199.5/ 200.8 | 228.0/ 227.7 | 250.0/ 250 |  | 9.9/ 19.8 |
| 4 | 199.2/ 199.5 | 227.7/ 227.7 | 250.0/ 250 |  | 9.8/ 19.8 |
| 5 | 197.7/ 199.2 | 227.7/ 227.5 | 250.0/ 250 |  | 9.8/ 19.7 |
| 6 | 197.6/ 197.7 | 227.5/ 217.2 | 250.0/ 250 |  | 9.7/ 19.6 |

HEAT TRANSFER AND PRESSURE DROP SUMMARY

ZONE

| HEAT TRANSFER MECHANISM | PRESSURE DROP (TOTAL)PSIA |  | FILM COEFF.$\mathrm{BTU} / \mathrm{HR}-\mathrm{FT} 2-\mathrm{F}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| SHELL-SIDE TUBE-SIDE | SHELL-SIDE | TUBE-SIDE | SHELL-SIDE | TUBE-SIDE |
| PORIZATION CONDENSATION | 0.02 | 0.10 | 936.62 | 2093.49 |
| PORIZATION CONDENSATION | 0.00 | 0.02 | 936.31 | 2027.16 |
| PORIZATION CONDENSATION | 0.01 | 0.08 | 936.02 | 2294.64 |
| PORIZATION CONDENSATION | 0.00 | 0.02 | 935.34 | 2528.96 |
| PORIZATION CONDENSATION | 0.02 | 0.08 | 934.55 | 1897.63 |
| PORIZATION LIQ. SUBCOOL | 0.00 | 0.13 | 4763.73 | 25.78 |
| TOTAL PRESSURE DROP | 0.05 | 0.43 |  |  |

HEAT TRANSFER SUMMARY (CONTD.)

| ZONE | $\begin{aligned} & ------ \text { DUTY } \\ & \text { MMBTU /HR } \end{aligned}$ | PERCENT | $\begin{gathered} \text { U-VALUE } \\ \text { BTU/HR-FT2-F } \end{gathered}$ | AREA FT2 | LMTD <br> DEG F | FT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.81 | 33.0 | 334.22 | 208.2 | 26.4 | 0.982 |
| 2 | 0.29 | 5.3 | 332.10 | 32.9 | 27.1 | 0.982 |
| 3 | 1.52 | 27.7 | 339.84 | 163.8 | 27.7 | 0.982 |
| 4 | 0.29 | 5.3 | 345.44 | 30.0 | 28.4 | 0.982 |
| 5 | 1.52 | 27.7 | 327.49 | 162.0 | 29.1 | 0.982 |
| 6 | 0.06 | 1.1 | 20.80 | 117.2 | 24.4 | 0.982 |
| TOTAL | 5.48 | 100.0 |  | 714.1 |  |  |
| WEIGHTED |  |  | 282.91 |  | 27.6 | 0.982 |
| OVERALL |  |  |  |  | 22.6 | 0.982 |
| INSTALLED |  |  |  | 714.9 |  |  |

```
TOTAL DUTY = (WT. U-VALUE) (TOTAL AREA) (WT. LMTD) (OVL. FT)
    ZONE DUTY = (ZONE U-VALUE) (ZONE AREA) (ZONE LMTD) (OVL. FT)
```


## Example 10.6

Use HEXTRAN to rate the horizontal thermosyphon reboiler of Example 10.3 and compare the results with those obtained previously by hand. Assay data (ASTM D86 distillation at atmospheric pressure) for the petroleum fraction fed to the reboiler are given in the following table. The feed stream has an average API gravity of $60^{\circ}$.

| Volume percent distilled | Temperature $\left({ }^{\circ} \mathrm{F}\right)$ |
| :---: | :---: |
| 0 | $158.8^{\mathrm{a}}$ |
| 10 | 210 |
| 30 | 240 |
| 50 | 260 |
| 70 | 275 |
| 90 | 290 |
| 100 | $309^{\mathrm{b}}$ |

${ }^{a}$ Initial boiling point.
${ }^{\mathrm{b}}$ End point.

## Solution

For this problem, the tube-side feed (Therminol ${ }^{\circledR}$ ) is defined as a bulk property stream and the values of $C_{P}, k, \mu$, and $\rho\left(55.063 \mathrm{lbm} / \mathrm{ft}^{3}\right)$ given in Example 10.3 are entered as average liquid properties on the appropriate form. Note that the density, not the specific gravity, must be entered. Additional data required for this stream are the flow rate $(425,000 \mathrm{lb} / \mathrm{h})$, temperature $\left(420^{\circ} \mathrm{F}\right)$ and pressure. Since the stream pressure was not specified in Example 10.3, a value of 40 psia is (arbitrarily) assumed.

The shell-side feed (petroleum fraction) is defined as an assay stream, and its flow rate ( $300,000 \mathrm{lb} / \mathrm{h}$ ) and pressure ( 35 psia ) are entered on the Specifications form. To complete the thermal specification of the stream, Bubble Point is selected from the list of available specifications. Next, under Components and Thermodynamics, the Assay tab is selected and a new assay name (A1) is entered. Clicking on the $A d d$ button activates the data entry tree that includes the listings Distillation and Gravity, as shown below. Clicking on each of these items in turn brings up the panels where the ASTM distillation data and average API gravity are entered. HEXTRAN uses the assay data to determine a set of pseudo components that represent the composition of the stream.


The assay name, A1, is also entered on the Specifications form for the feed stream in order to link the assay with the stream to which it applies.

A set of thermodynamic procedures is also required for the assay stream. The PR EOS is selected as the method for equilibrium, enthalpy, and vapor density calculations; the API method is chosen for calculating liquid density. The petroleum method is selected for all transport properties (viscosity, thermal conductivity, and surface tension).

Data for the heat exchanger are entered as given in Example 10.3, including the number of tubes (290) and the shell ID ( 23.25 in ). A type A front head and no baffles are assumed. Tubesheet thickness and shell-side nozzles are left unspecified; HEXTRAN will determine suitable values for these items, which were not specified in Example 10.3. Fouling factors from Example 10.3 are entered on the Film Options form.

The input file generated by the HEXTRAN GUI is given below, followed by a summary of results extracted from the HEXTRAN output file. It is seen that the reboiler generates $82,390 \mathrm{lb} / \mathrm{h}$ of vapor, about $37 \%$ more than the $60,000 \mathrm{lb} / \mathrm{h}$ required. The tube-side pressure drop is 9.34 psi , which is less than the maximum of 10 psi specified for the unit. HEXTRAN does not compute a critical heat flux, so this check must be done by hand. In the present case, the heat flux is approximately $13,000 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$, well below the critical value of $36,365 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}$ calculated by hand in Example 10.3. (In actual operation, the heat flux would be about $37 \%$ lower.) Therefore, the reboiler is suitable for the service, in agreement with the result obtained in Example 10.3.
Results from HEXTRAN are compared with those calculated by hand in the following table. The shell-side (boiling) heat-transfer coefficient calculated by hand is very conservative compared with the value given by HEXTRAN, but the overall coefficients differ by only about $17 \%$. The mean temperature difference used in the hand calculations is slightly higher than the value calculated by HEXTRAN. However, the heat flux ( $U_{D} \Delta T_{m}$ ) calculated by hand is on the safe side, about $10 \%$ below the HEXTRAN value. Notice that virtually all of the shell-side pressure drop occurs in the nozzles. If two pairs of nozzles ( $6-\mathrm{in}$. inlet, $10-\mathrm{in}$. outlet) are assumed instead of the single pair used by HEXTRAN, the shell-side pressure drop is reduced to 0.33 psi .

| Item | Hand | HEXTRAN |
| :--- | :---: | :---: |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 346 | 346.2 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 278 | $555^{\mathrm{a}}$ |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 113 | $132^{\mathrm{a}}$ |
| $\Delta P_{i}(\mathrm{psi})$ | 8.4 | 9.34 |
| $\Delta P_{o}(\mathrm{psi})$ | - | 1.39 |
| $\Delta T_{m}\left({ }^{\circ} \mathrm{F}\right)$ | 104.2 | $98.5^{\mathrm{a}}$ |
| $U_{D} \Delta T_{m}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}\right)$ | 11,775 | 13,002 |

${ }^{\text {a }}$ Area-weighted average from zone analysis.

## HEXTRAN Input File for Example 10.6

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=Example 10-6, PROBLEM=Horizontal Thermosyphon Reboiler, SITE=
$
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
    ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
    PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
    UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=CP, WT=LB, *
```

```
HEXTRAN Input File for Example 10.6 (continued)
    XDENSITY=API, STDVAPOR=379.490
$
PRINT ALL, *
    RATE=M
$
CALC PGEN=New, WATER=Saturated
$
$ Component Data Section
$
COMPONENT DATA
$
$
    ASSAY FIT= SPLINE, CHARACTERIZE=SIMSCI, MW= SIMSCI, *
    CONVERSION= API87, GRAVITY= WATSONK, TBPIP=1, TBPEP=98
$
    TBPCUTS 100.00, 800.00, 28 /*
    1200.00, 8 /*
    1600.00, 4
$
$ Thermodynamic Data Section
$
THERMODYNAMIC DATA
$
    METHODS SET=SET1, KVALUE=PR, ENTHALPY(L) =PR, ENTHALPY(V)=PR, *
                                    DENSITY(L) =API, DENSITY(V)=PR, VISCOS(L)=PETRO, *
                                    VISCOS (V)=PETRO, CONDUCT (L) =PETRO, CONDUCT (V)=PETRO, *
                                    SURFACE=PETRO
$
    WATER DECANT=ON, SOLUBILITY = Simsci, PROP = Saturated
$
$Stream Data Section
$
STREAM DATA
$
    PROP STRM=THERM_COLD, NAME=THERM_COLD
$
    PROP STRM=PROD, NAME=PROD
$
    PROP STRM=FEED, NAME=FEED, PRES=35.000, PHASE=L, *
                                    RATE (W) =300000.000, ASSAY=LV, BLEND
    D86 STRM=FEED, *
    DATA= 0.0, 158.80 / 10.0, 210.00 / 30.0, 240.00 / 50.0, 260.00 / *
                        70.0, 275.00 / 90.0, 290.00 / 100.0, 309.00
    API STRM=FEED, AVG=60.000
$
    PROP STRM=THERMINOL, NAME=THERMINOL, TEMP=420.00, PRES=40.000, *
                                LIQUID (W) =425000.000, LCP (AVG) =0.534, Lcond (AVG) =0.0613, *
                                Lvis(AVG)=0.84, Lden(AVG) =55.063
$
$ Calculation Type Section
$
SIMULATION
$
    TOLERANCE TTRIAL=0.01
$
```


## HEXTRAN Input File for Example 10.6 (continued)

```
    LIMITS AREA=200.00, 6000.00, SERIES=1, 10, PDAMP=0.00, *
        TTRIAL=30
$
    CALC TWOPHASE=New, DPSMETHOD=Stream, MINFT=0.80
$
    PRINT UNITS, ECONOMICS, STREAM, STANDARD, *
        EXTENDED, ZONES
$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR
$
    UTCOST OIL=3.50, GAS=3.50, ELECTRICITY=0.10, *
        WATER=0.03, HPSTEAM=4.10, MPSTEAM=3.90, *
        LPSTEAM=3.60, REFRIGERANT=0.00, HEATINGMEDIUM=0.00
$
    HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        EXPONENT=0.60, CONSTANT=0.00, UNIT
$
$ Unit Operations Data
$
UNIT OPERATIONS
$
STE UID=REBOILER
    TYPE Old, TEMA=AXU, HOTSIDE=Tubeside, ORIENTATION=Horizontal, *
    FLOW=Countercurrent, *
    UESTIMATE=50.00, USCALER=1.00
    TUBE FEED=THERMINOL, PRODUCT=THERM_COLD, *
        LENGTH=16.00, OD=0.750, *
        BWG=14, NUMBER=290, PASS=2, PATTERN=90, *
        PITCH=1.0000, MATERIAL=1, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
SHELL FEED=FEED, PRODUCT=PROD, *
        ID=23.25, SERIES=1, PARALLEL=1, *
        MATERIAL=1, *
        FOUL=0.0005, LAYER=0, *
        DPSCALER=1.00
$
    BAFF NONE
$
    TNOZZ TYPE=Conventional, ID=6.065, 6.065, NUMB=1, 1
$
    CALC TWOPHASE=New, *
        DPSMETHOD=Stream, *
        MINFT=0.80
$
    PRINT STANDARD, *
        EXTENDED, *
        ZONES
$
    COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        CONSTANT=0.00, EXPONENT=0.60, Unit
$
$ End of keyword file...
```


## HEXTRAN Output Data for Example 10.6

## SHELL AND TUBE EXCHANGER DATA SHEET



## HEXTRAN Output Data for Example 10.6 (continued)



## HEXTRAN Output Data for Example 10.6 (continued)



```
TOTAL DUTY = (WT. U-VALUE) (TOTAL AREA) (WT. LMTD) (OVL. FT)
    ZONE DUTY = (ZONE U-VALUE) (ZONE AREA) (ZONE LMTD) (OVL. FT)
```


### 10.6.2 HTFS/Aspen

The TASC module of the HTFS software package is used for shell-and-tube reboiler calculations. Although the TASC documentation provides no information regarding the correlations used in performing the thermal and hydraulic analyses, some general information concerning thermosyphon calculations is given. Additional information can be ascertained from the detailed output file generated by the software.

For kettle reboilers, a recirculation model is used in which the internal circulation rate in the unit is determined by a pressure balance. The boiling-side heat-transfer coefficient is calculated based on the internal circulation rate in the kettle. Incremental (stepwise) calculations are performed in both the vertical and horizontal (axial) directions, and profiles of stream temperatures, tube wall temperature, and heat-transfer coefficients are generated. For each tube pass, the largest local value of the heat flux ratio, $\hat{q} / \hat{q}_{c}$, is computed to determine whether the critical heat flux has been exceeded.


Figure 10.9 Elevations required to specify the configuration of a horizontal thermosyphon reboiler in TASC (Source: TASC 5.01 Help File).


Figure 10.10 Elevations required to specify the configuration of a vertical thermosyphon reboiler in TASC (Source: TASC 5.01 Help File).

For thermosyphon reboilers, a special rating procedure is implemented when Thermosyphon is chosen as the calculation mode. In this mode, details of the piping configuration for the reboiler system are entered as input and the program calculates the circulation rate as part of the rating procedure. Three elevations are required to specify the overall system configuration as shown in Figures 10.9 and 10.10 for horizontal and vertical thermosyphons, respectively. Any number of pipe sections can be used to model the connecting piping, and fittings can be specified by means of either
flow resistance coefficients or equivalent lengths of pipe. In addition to calculating the circulation rate, TASC also performs a stability assessment to determine the potential for various types of flow instability in the hydraulic circuit. Two-phase flow regimes are also determined for return lines and reboiler tubes (for tube-side boiling).

The design procedure for thermosyphon reboilers using TASC is similar to that for single-phase exchangers described in Example 7.6. An initial configuration for the reboiler proper is obtained by running TASC in design mode. Since the circulation rate is unknown (for a recirculating unit) at this point, an initial estimate for the boiling-side flow rate is used based on an assumed exit vapor fraction. The initial configuration is then rated by running TASC in thermosyphon mode. Here, details of the connecting piping must be supplied, and the circulation rate, exchanger duty, and pressure drops are calculated. Based on the results of the rating calculations, design modifications for the exchanger and pipe work are made as needed, and the rating calculations are repeated. It may be necessary to re-start the design procedure by running TASC in design mode using an improved estimate of the circulation rate obtained in the thermosyphon mode. After an acceptable configuration for the reboiler system has been achieved, mechanical design calculations are performed using TASC Mechanical. If problems are indicated, additional design modifications are made and the unit is re-rated.
The following examples illustrate the use of TASC for reboiler applications.

## Example 10.7

Use TASC to rate the kettle reboiler designed in Example 10.2, and compare the results with those obtained previously by other methods.

## Solution

Data from Example 10.2 were entered on the appropriate TASC input forms as indicated below. Parameters not listed were either left at their default settings or left unspecified to be calculated by the software.
(a) Start up.

Calculation Mode: Simulation
Basic Input Mode: Not checked
(b) Exchanger Geometry.
(i) Exchanger General

Type: BKU
No. Exchangers in Series: 1
No. Exchangers in Parallel: 1
Shell Inside Diameter: 23.25 in.
Side for Hot Stream: Tube-side Hot
(ii) Kettle Details

Weir height above bundle: 1 in .
Kettle large shell diameter: 37 in.
(c) Bundle Geometry.
(i) Tube Details

Tube Outside Diameter: 1 in.
Tube Wall Thickness: 0.083 in.
Tube Pitch: 1.25 in.
Tube Pattern: Square
Tube Length: 156 in.
(ii) Bundle Layout

Number of Tube-side Passes: 2
Number of Sealing Strip Pairs: 0
(iii) Bundle Size

Tube Count (effective): 212
(iv) Transverse Baffles

Baffle Type: Unbaffled/Low pressure drop
(v) Special Baffles/Supports

Number of Midspace Interm. Supports: 3
(d) Nozzles.

On the tube side, one inlet nozzle ( $\mathrm{ID}=6.065 \mathrm{in}$.) and one outlet nozzle ( $\mathrm{ID}=3.068 \mathrm{in}$.) are specified. On the shell side, two inlet nozzles ( $\mathrm{ID}=5.047 \mathrm{in}$.), two vapor outlet nozzles ( $\mathrm{ID}=6.065 \mathrm{in}$.) and one liquid outlet nozzle ( $\mathrm{ID}=4.026 \mathrm{in}$.) are specified.
(e) Process.

|  | Hot stream | Cold stream |
| :--- | :--- | :--- |
| Total mass flow rate $(\mathrm{lb} / \mathrm{h})$ | 5645 | 96,000 |
| Inlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 228 | 197.6 |
| Inlet pressure $(\mathrm{psia})$ | 20 | 250 |
| Inlet mass quality | 1 | 0 |
| Fouling resistance $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ | 0.0005 | 0.0005 |

(f) Physical Properties.

For the hot stream (steam), the Stream Data Source is set to $<$ Water (NEL 40) $>$ and pressure levels of 20 and 19 psi are specified. No other entries are required for this stream.

For the cold stream, the COMThermo interface is opened by clicking the $A d d$ button under Stream Data Source. The components (propane, $i$-butane, and $n$-butane) are selected from the list of components, and the Peng-Robinson thermodynamic package is chosen from the list of available methods. Returning to the TASC properties input form, the mole fractions $\left(\mathrm{C}_{3}: 0.15\right.$, $i-\mathrm{C}_{4}: 0.25, n-\mathrm{C}_{4}: 0.60$ ) are entered and pressure levels of 250 and 240 psi are specified. Using the Options button, a temperature range for fluid properties of $190-210^{\circ} \mathrm{F}$ is specified. The fluid properties are generated by clicking on the Get Properties button.

When TASC is run with the above input data, the incremental calculations fail to converge. It is necessary to increase the steam flow rate to about $6100 \mathrm{lb} / \mathrm{h}$ in order to obtain a converged solution. The results summary for this case is given below, from which it can be seen that the outlet quality on the shell side is 0.5538 . The corresponding vapor generation rate is $53,165 \mathrm{lb} / \mathrm{h}$, which is about $10 \%$

TASC Results Summary for Example 10.7: Simulation Run

| TASC Version 5.01 - SIMULATION |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Shell type/series/parallel | BKU |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 23.3 | in | 156.0 | in | 759.5 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 2 |  | 212 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 1.25 (90) | in |
| No of baffles/pitch/cut | 0 |  |  | in | 25 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 95999.9 | $\mathrm{lb} / \mathrm{h}$ | 6100.0 | lb/h |  |  |
| Inlet temperature shell/tube | 197.48 | ${ }^{\circ} \mathrm{F}$ | 228.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 202.62 | ${ }^{\circ} \mathrm{F}$ | 204.94 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 0.0/0.55 |  | 1.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 0.482 | psi | 0.364 | psi |  |  |
| Velocity highest shell xflow/tube | 0.19 | $\mathrm{ft} / \mathrm{s}$ | 84.71 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 997 | Btu/h ft ${ }^{\circ} \mathrm{F}$ | 1490 | Btu/ $\mathrm{ftt}^{2}{ }^{\circ} \mathrm{F}$ | 3828 | Btu/ $\mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 2000 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 1668 | Btu/h ft ${ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 516.7 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 329.5 | Btu/h ft ${ }^{\circ} \mathrm{F}$ | 329.5 | Btu/hft ${ }^{2}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 5998 | kBtu/h | 24.04 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 0.989 |  | 1.024 |  |  |  |

higher than the required rate of $48,000 \mathrm{lb} / \mathrm{h}$. However, the heat transfer is limited by the amount of steam supplied rather than the available heat-transfer area. Condensate subcooling occurs for steam flow rates below about $7275 \mathrm{lb} / \mathrm{h}$. At this steam rate, the vapor generation rate is $62,122 \mathrm{lb} / \mathrm{h}$, which is $29 \%$ more than required.

A converged solution can also be obtained by running TASC in checking mode using the original steam flow rate of $5645 \mathrm{lb} / \mathrm{h}$ while keeping all other input data the same as above. The results summary for this run is shown below. In checking mode, the area ratio (actual/required) gives the over-design for the unit, which is about $37 \%$ in this case. (The area ratio is the same as the duty-to-service overall coefficient ratio. In checking mode the value calculated for the service overall coefficient is equal to $U_{\text {req. }}$.)

## TASC Results Summary for Example 10.7: Checking Run

| TASC Version 5.01- CHECKING |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Shell type/series/parallel | BKU |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 23.3 | in | 156.0 | in | 759.5 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 2 |  | 212 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 1.25 (90) | in |
| No of baffles/pitch/cut | 0 |  |  | in | 25 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 95999.9 | lb/h | 5645.0 | lb/h |  |  |
| Inlet temperature shell/tube | 197.48 | ${ }^{\circ} \mathrm{F}$ | 228.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 202.21 | ${ }^{\circ} \mathrm{F}$ | 227.04 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 0.0/0.4999 |  | 1.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 0.494 | psi | 0.35 | psi |  |  |
| Velocity highest shell xflow/tube | 0.19 | $\mathrm{ft} / \mathrm{s}$ | 78.36 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 1146 | Btu/ $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 3147 | Btu/hft ${ }^{\circ}{ }^{\circ} \mathrm{F}$ | 3831 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 2000 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 1668 | Btu/hft ${ }^{\circ}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 688.9 | $\mathrm{Btu} / \mathrm{hft}{ }^{\circ} \mathrm{F}$ | 392.0 | $\mathrm{Btu} / \mathrm{hft}{ }^{\circ} \mathrm{F}$ | 285.6 | $\mathrm{Btu} / \mathrm{hft}{ }^{\text {o }} \mathrm{F}$ |
| Heat load/eff wtd mtd | 5422 | kBtu/h | 25.35 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req) | 1.372 |  |  |  |  |  |

The following table compares results from the TASC checking run with those obtained by hand in Example 10.2 and from HEXTRAN in Example 10.5. The boiling-side heat-transfer coefficient calculated by hand is, as expected, quite conservative compared with the value computed by TASC. The situation is reversed for the effective steam coefficients, due primarily to the fouling factor used for steam in the present example. From the results summary given above, the steam coefficient (referred to the external tube surface) calculated by TASC in checking mode is $3147 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. The values obtained by hand and by TASC for tube-side pressure drop, mean temperature difference, and heat flux ratio are in close agreement.

Comparison of results from TASC and HEXTRAN is obfuscated to some extent by condensate subcooling and the different computational modes and steam flow rates used. However, TASC clearly predicts a somewhat higher rate of heat transfer since condensate subcooling persists up to a steam flow rate of $7275 \mathrm{lb} / \mathrm{h}$ compared with $6850 \mathrm{lb} / \mathrm{h}$ in HEXTRAN. The corresponding vapor generation rates are $62,122 \mathrm{lb} / \mathrm{h}$ for TASC and $58,349 \mathrm{lb} / \mathrm{h}$ for HEXTRAN, a difference of about $6 \%$.

TASC generated a tube layout (shown below) containing 210 tubes ( 105 U-tubes), which agrees well with the value of 212 obtained from the tube-count table in Example 10.2. TASC Mechanical was run to perform the mechanical design calculations for the unit. The results show that schedule

| Item | Hand | HEXTRAN | TASC |
| :--- | :--- | :--- | :--- |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 523 | $936^{\mathrm{a}}$ | 1146 |
| $\left[\left(D_{o} / D_{i}\right)\left(1 / h_{i}+R_{D i}\right)\right]^{-1}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 1500 (assumed) | $857^{\mathrm{a}}$ | 1090 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 297 | $335^{\mathrm{a}}$ | 392 |
| $\Delta P_{i}(\mathrm{psi})$ | 0.3 | 0.43 | 0.35 |
| $\Delta P_{o}(\mathrm{psi})^{\mathrm{b}}$ | 0.2 (assumed) | 0 | 0.055 |
| $\Delta T_{m}\left({ }^{\circ} \mathrm{F}\right)$ | 25.6 | $27.1^{\mathrm{a}}$ | 25.4 |
| $U_{D} \Delta T_{m}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}\right)$ | 7603 | $9079^{\mathrm{a}}$ | 9957 |
| $\left(\hat{a} / q_{c}\right)_{\text {max }}$ | 0.11 | - | 0.085 |

${ }^{\text {a }}$ Area-weighted average over first five zones; subcooled condensate zone not included.
${ }^{\mathrm{b}}$ Friction and acceleration, excluding nozzle losses.

40 pipe is inadequate for the shell-side nozzles. The configuration generated by the program uses schedule 160 pipe for the inlet and liquid exit nozzles, and schedule XXS pipe for the vapor exit nozzles. However, less robust nozzles can be specified without incurring error messages from TASC (as low as schedule 120 for the inlet and liquid exit nozzles, and schedule 80 for the vapor exit nozzles). If schedule 160 inlet nozzles are used, 6 -in. pipe is required in order to satisfy $\rho V_{n}^{2}<500 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{s}^{2}$. If schedule 120 nozzles are used, 5 -in. pipe will suffice.

## TASC Tube Layout for Kettle Reboiler



## Example 10.8

Use TASC to rate the initial configuration for the vertical thermosyphon reboiler of Example 10.4 and compare the results with those obtained previously by hand.

## Solution

For this problem, TASC was run in thermosyphon mode with input data as given below. Parameters not listed were either left at their default values or left unspecified to be calculated by the software.
(a) Start up.

Calculation Mode: Thermosyphon
Basic Input Mode: Not checked
(b) Exchanger Geometry.
(i) Exchanger General

Type: AEL
Shell Orientation: Vertical No. Exchangers in Series: 1 No. Exchangers in Parallel: 1 Shell Inside Diameter: 15.25 in. Side for Hot Stream: Shell-side Hot
(c) Bundle Geometry.
(i) Tube Details

Tube Outside Diameter: 1 in.
Tube Wall Thickness: 0.083 in.
Tube Pitch: 1.25 in.
Tube Pattern: Triangular
Tube Length: 96 in.
(ii) Bundle Layout

Number of Tube-side Passes: 1
Number of Sealing Strip Pairs: 0
Tube Layout Data: Revise from input
(iii) Bundle Size

Tube Count (effective): 106
(iv) Transverse Baffles

Baffle Pitch: 6.1 in.
Baffle Cut: 35\%
(d) Nozzles.

Tube side: 6 -in. schedule 40 inlet, 10 -in. schedule 40 outlet
Shell side: 4 -in. schedule 40 inlet, 2 -in. schedule 40 outlet
(e) Process.

|  | Hot stream | Cold stream |
| :--- | :--- | :--- |
| Total mass flow rate $(\mathrm{lb} / \mathrm{h})$ | 2397 | 113,814 |
| Inlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 222.4 | 182 |
| Inlet pressure psia$)$ | 18 | 0 |
| Inlet mass quality | 1 | 0.0005 |
| Fouling resistance $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ | 0 |  |

The circulation rate computed in Example 10.4 is entered for the cold stream mass flow rate. This value serves as an initial estimate for the circulation rate, the final value of which will be calculated by the software. Note that the inlet pressure of the cold stream need not be given as it is calculated by the program in thermosyphon mode. Also, a fouling factor of zero is specified for steam to provide a better match of total steam-side resistance with the value used in the hand calculations.
(f) Thermosyphon Details.
(i) $\mathrm{T} / \mathrm{S}$ specification

Height of Exchanger Inlet: 0 in.
Pressure at Liquid Surface: 16 psia
Height of Liquid Surface in Column: 96 in.
Height of Vapor Return to Column: 120 in.
Note that the arbitrary reference line for elevations (Figure 10.10) is taken at the reboiler inlet, and the liquid level in the column sump is assumed to be at the upper tubesheet elevation. The return line is assumed to be centered a distance of 2 ft above the surface of the liquid in the column. (The value assumed for this distance has a relatively small effect on the calculations. In practice, however, the bottom of the return line should be at least 6 in. above the highest liquid level expected in the column sump.)
(ii) Inlet and outlet circuits

| Element 1 | Inlet | Outlet |
| :--- | :--- | :--- |
| Circuit element | Pipe | Horizontal pipe |
| Internal diameter (in.) | 6.065 | 10.02 |
| Length (in.) | 1200 | 600 |
| Number of elements in series | 1 | 1 |
| Number of elements in parallel | 1 | 1 |

(g) Physical properties.

For steam, $<$ Water (NEL 40) $>$ is selected as the Stream Data Source and pressure levels of 20,18 , and 16 psia are specified.

For the cold stream, the COMThermo interface is opened, cyclohexane is selected from the list of components and Peng-Robinson is selected from the list of available methods. A temperature range of $180-200^{\circ} \mathrm{F}$ is specified at pressure levels of 20,18 , and 16 psia .

The TASC results summary corresponding to the above input data is given below, from which it can be seen that the reboiler is under-sized. The amount of vapor generated is $12,256 \mathrm{lb} / \mathrm{h}$, which

## TASC Results Summary for Example 10.8

| TASC Version 5.01 - THERMOSYPHON |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Shell type/series/parallel | AEL |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 15.3 | in | 96.0 | in | 222.0 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 1 |  | 106 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 1.25(30) | in |
| No of baffles/pitch/cut | 14 |  | 6.1 | in | 36 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 2397.0 | $\mathrm{lb} / \mathrm{h}$ | 114973.3 | $\mathrm{lb} / \mathrm{h}$ |  |  |
| Inlet temperature shell/tube | 222.41 | ${ }^{\circ} \mathrm{F}$ | 182.71 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 218.96 | ${ }^{\circ} \mathrm{F}$ | 183.53 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 1.0/0.1 |  | 0.0/0.1066 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 1.165 | psi | 2.153 | psi |  |  |
| Velocity highest shell xflow/tube | 114.57 | $\mathrm{ft} / \mathrm{s}$ | 43.03 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 1584 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 413 | Btu/ $\mathrm{ftt}^{2}{ }^{\circ} \mathrm{F}$ | 3876 | Btu/ $\mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube |  | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 1668 | Btu/ $\mathrm{ftt}^{2}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 302.0 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 255.7 | Btu/ $\mathrm{fft}^{2} \mathrm{~F}$ | 255.7 | Btu/ $\mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 1894 | kBtu/h | 33.99 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.002 |  | 0.819 |  |  |  |

is about $82 \%$ of the $15,000 \mathrm{lb} / \mathrm{h}$ required. On the heating side, about $18 \%$ of the steam fed to the unit fails to condense. Thus, according to TASC the unit is under-surfaced by about $18 \%$, which is comparable to the result obtained by hand in Example 10.4.

The following table provides a more detailed comparison of results from TASC and the hand calculations. Some of the data in this table were obtained from the detailed output file generated by TASC. Note that all heat-transfer coefficients given by TASC are based on the external surface area of the tubes. Thus, the value of $413 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ for the tube-side coefficient given above in the results summary is actually $h_{i} D_{i} / D_{o}$, so that $h_{i}=495 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$. Also, note that the tube-side pressure drop of 2.153 psi in the results summary includes the static head loss in the tubes as well as acceleration, friction, and nozzle losses.

| Item | Hand | TASC |
| :--- | :--- | :--- |
| Circulation rate $(\mathrm{lb} / \mathrm{h})$ | 113,814 | 114,973 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | $565^{\mathrm{a}}$ | 495 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 1,500 (assumed) | 1,584 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{\circ} \cdot{ }^{\circ} \mathrm{F}\right)$ | $243^{\mathrm{a}}$ | 255.7 |
| $\Delta P_{i}(\mathrm{psi})^{\mathrm{c}}$ | 0.86 | 0.894 |
| $\Delta P_{o}(\mathrm{psi})$ | - | 1.165 |
| $\Delta T_{m}\left({ }^{\circ} \mathrm{F}\right)$ | $34.7^{\mathrm{b}}$ | 34 |
| $\left(\hat{q} / \hat{q}_{c}\right)_{\text {max }}$ | 0.48 | 0.217 |

${ }^{\text {a Area-weighted average of values for sensible heating and boiling zones. }}$
${ }^{\mathrm{b}}$ Value for boiling zone.
${ }^{\mathrm{c}}$ Friction and acceleration, excluding nozzle losses.

The largest differences between the values calculated by hand and by TASC are in the boiling-side heat-transfer coefficient and the critical heat flux. Clearly, the critical heat flux estimated using Palen's correlation in Example 10.4 is very conservative compared with the value computed by TASC. Conversely, the average boiling-side heat-transfer coefficient calculated by hand is about $14 \%$ higher than the value computed by TASC. Nevertheless, the average overall heat-transfer coefficient calculated by hand differs by only about $5 \%$ from the value computed by TASC.

The tube-side pressure drop was not explicitly calculated in Example 10.4, although all parameters needed for the calculation were evaluated. For completeness, the friction and acceleration losses are computed here.

$$
\Delta P_{a c c}=\frac{G_{t}^{2} \gamma}{3.75 \times 10^{12} s_{L}}=\frac{(283,029)^{2} \times 10.77}{3.75 \times 10^{12} \times 0.7208}=0.3192 \mathrm{psi}
$$

For the sensible heating zone, the friction loss is:

$$
\Delta P_{f, B C}=\frac{f_{t} L_{B C} G_{t}^{2}}{7.50 \times 10^{12} D_{t} s_{L}}=\frac{0.0319 \times 2.9(283,029)^{2}}{7.50 \times 10^{12} \times 0.0695 \times 0.7208}=0.0197 \mathrm{psi}
$$

For the boiling zone, the friction loss is:

$$
\Delta P_{f, C D}=\frac{f_{t} L_{C D} G_{t}^{2} \bar{\phi}_{L O}^{2}}{7.50 \times 10^{12} D_{t} s_{L}}=\frac{0.0319 \times 5.1(283,029)^{2} \times 15.08}{7.50 \times 10^{12} \times 0.0695 \times 0.7208}=0.5231 \mathrm{psi}
$$

The total friction loss is:

$$
\Delta P_{f}=\Delta P_{f, B C}+\Delta P_{f, C D}=0.0197+0.5231=0.5428 \mathrm{psi}
$$

Therefore,

$$
\Delta P_{a c c}+\Delta P_{f}=0.3192+0.5428 \cong 0.86 \mathrm{psi}
$$

## Example 10.9

Use TASC to design a vertical thermosyphon reboiler for the service of Example 10.4.

## Solution

An initial design consisting of a $15.25-\mathrm{in}$. shell containing 106 tubes ( $1-\mathrm{in}$. OD, $14 \mathrm{BWG}, 8 \mathrm{ft}$ long) was rated in Example 10.8 and found to be too small. Therefore, we need to only modify the initial design until a suitable configuration is obtained. We begin by increasing the shell size, one size at a time, while keeping other design parameters fixed. Input data are the same as in Example 10.8, with the following exceptions:

- A fouling factor of $0.0005 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is included for steam to provide an additional safety margin.
- The number of tubes is left unspecified, thereby allowing TASC to determine the tube count based on the detailed tube layout.
- The baffle pitch is adjusted to maintain $B / d_{s}$ in the range $0.35-0.40$, and the number of baffles is adjusted to fit between the shell-side nozzles as indicated on the setting plan generated by TASC Mechanical.
- The shell-side nozzles are specified to be on the same side or on opposite sides of the shell, depending on whether the number of baffles is odd or even.

Running TASC in thermosyphon mode, it is found that shell sizes of 17.25 and 19.25 in . are both too small. However, with a 19.25 -in. shell, the heat transfer is limited by the amount of steam provided rather than the available heat-transfer area. TASC also gives the following warning message:

Consider using a V type rear head ( $30^{\circ}$ cone) to avoid excessive nozzle/cylinder thickness due to having to reinforce a large opening.

Note: The conical head is a standard item. However, type V is not a TEMA designation for this type of head.
Therefore, the following design changes are made:

- Change exchanger type to AEV.
- Increase shell ID to 19.25 in .
- Increase baffle pitch to 7.0 in .
- Increase steam flow rate from 2397 to $2500 \mathrm{lb} / \mathrm{h}$.

With these changes, the unit generates about $15,300 \mathrm{lbm} / \mathrm{h}$ of vapor, slightly more than the $15,000 \mathrm{lbm} / \mathrm{h}$ required. Running TASC Mechanical shows that the shell-side outlet nozzle should be schedule 80 , and a tubesheet thickness of 1.54 in . is required as opposed to the value of 0.93 in . calculated by TASC Thermal. No other errors are indicated. Hence, with these minor modifications, the design is acceptable. The TASC thermal results summary for this case (including the aforementioned modifications) follows.

## TASC Results Summary for Example 10.9: Design 1

| TASC Version 5.01-THERMOSYPHON |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Shell type/series/parallel | AEV |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 19.3 | in | 96.0 | in | 366.5 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 1 |  | 175 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 1.25 (30) | in |
| No of baffles/pitch/cut | 10 |  | 7.0 | in | 36 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 2500.0 | lb/h | 143049.9 | lb/h |  |  |
| Inlet temperature shell/tube | 222.41 | ${ }^{\circ} \mathrm{F}$ | 182.71 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 214.19 | ${ }^{\circ} \mathrm{F}$ | 184.65 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 1.0/0.0 |  | 0.0/0.1065 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 0.426 | psi | 1.73 | psi |  |  |
| Velocity highest shell xflow/tube | 83.1 | $\mathrm{ft} / \mathrm{s}$ | 31.67 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 1116 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 365 | Btu/ $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 3876 | Btu/h ft ${ }^{2} \mathrm{~F}$ |
| Fouling coeff shell/tube | 2000 | Btu/ $\mathrm{ftt}^{2} \mathrm{~F}$ | 1668 | Btu/h ft ${ }^{\text {o }}$ F |  |  |
| Overall coefficient clean/dirty/service | 256.8 | Btu/hft ${ }^{2} \mathrm{~F}$ | 200.2 | Btu/h ft ${ }^{\circ} \mathrm{F}$ | 200.2 | Btu/h ft ${ }^{2} \mathrm{~F}$ |
| Heat load/eff wtd mtd | 2430 | kBtu/h | 34.55 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.009 |  | 1.008 |  |  |  |

Next we consider increasing the steam design pressure from 18 to 20 psia as suggested in Example 10.4. Starting from the same initial configuration and proceeding to increase the shell size stepwise as before, it is found that the smallest feasible unit consists of a $17.25-\mathrm{in}$. shell containing 140 tubes. The TASC results summary for this case is shown below.

TASC Results Summary for Example 10.9: Design 2

| Geometric details |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shell type/series/parallel | AEV |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 17.3 | in | 96.0 | in | 293.2 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 1 |  | 140 |  |  |  |
| Tube id/od/pitch (pattern) | 0.834 | in | 1.0 | in | 1.25(30) | in |
| No of baffles/pitch/cut | 11 |  | 6.4 | in | 37 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 2450.0 | $\mathrm{lb} / \mathrm{h}$ | 129637.0 | lb/h |  |  |
| Inlet temperature shell/tube | 228.0 | ${ }^{\circ} \mathrm{F}$ | 182.71 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 212.26 | ${ }^{\circ} \mathrm{F}$ | 184.29 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 1.0/0.0 |  | 0.0/0.1173 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 0.43 | psi | 1.889 | psi |  |  |
| Velocity highest shell xflow/tube | 89.43 | $\mathrm{ft} / \mathrm{s}$ | 39.57 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 1011 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 421 | Btu/ $\mathrm{fft}^{2}$ م F | 3876 | Btu/hft ${ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 2000 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 1668 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 275.9 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 211.7 | Btu/ $\mathrm{ftt}^{2} \mathrm{~F}$ | 211.7 | Btu/ $\mathrm{ftt}^{2}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 2391 | kBtu/h | 40.18 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.008 |  | 1.016 |  |  |  |

Both of the above designs are summarized in the following table. Tube layouts and setting plans (from TASC Mechanical) are also shown.

| Item | Design 1 | Design 2 |
| :--- | :--- | :--- |
| Steam design pressure (psia) | 18 | 20 |
| Exchanger type | AEV | AEV |
| Shell size (in.) | 19.25 | 17.25 |
| Surface area (ft ${ }^{2}$ ) | 367 | 293 |
| Number of tubes | 175 | 140 |
| Tube OD (in.) | 1.0 | 1.0 |
| Tube length (ft) | 8 | 8 |
| Tube BWG | 14 | 14 |
| Tube passes | 1 | 1 |
| Tube pitch (in.) | 1.25 | 1.25 |
| Tube layout | Triangular | Triangular |
| Tubesheet thickness (in.) | 1.54 | 1.54 |
| Number of baffles | 10 | 11 |
| Baffle cut (\%) | 36 | 37 |
| Baffle thickness (in.) | 0.1875 | 0.1875 |
| Central baffle spacing (in.) | 7.00 | 6.40 |
| End baffle spacing (in.) | 14.90 | 14.40 |
| Sealing strip pairs | 0 | 0 |
| Tube-side inlet nozzle | 6 -in. schedule 40 | 6 -in. schedule 40 |
| Tube-side outlet nozzle | 10 -in. schedule 40 | 10 -in. schedule 40 |
| Shell-side inlet nozzle | 4 -in. schedule 40 | 4 -in. schedule 40 |
| Shell-side outlet nozzle | 2 -in. schedule 80 | 2 -in. schedule 80 |
| $\Delta P_{i}$ (psi) | 1.73 | 1.89 |
| $\Delta P_{o}$ (psi) | 0.43 | 0.43 |
| Circulation rate (lbm/h) | 143,050 | 129,637 |
| Exit vapor fraction | 0.1065 | 0.1173 |
| Vapor generation rate (lbm/h) | 15,235 | 15,206 |
| Steam flow rate (lbm/h) | 2,500 | 2,450 |
| $\left(\hat{q} / \hat{q}_{c}\right)_{\text {max }}$ | 0.15 | 0.20 |
| Flow stability assessment | Stable | Stable |
| Two-phase flow regimes | Slug, churn, annular | Slug, churn, annular |

## Setting Plan and Tube Layout for Design 1




## Setting Plan and Tube Layout for Design 2




Note that a shell-side vent nozzle (nozzle S3 on the setting plans) is provided for these units to purge any non-condensable gases that may enter with the steam. (Vents and drains can be added on the TASC Mechanical input forms.) Also, an impingement plate is included at the steam inlet nozzle, as required for a saturated vapor. (An impingement plate is automatically included when the nozzle type is specified as Plain + Impingement.) Cost estimates generated by TASC indicate that the $19.25-\mathrm{in}$. exchanger is about $13 \%$ more expensive than the smaller unit.

Consideration of the third design modification suggested in Example 10.4, namely, increasing the tube length, is left as an exercise for the reader.

### 10.6.3 HTRI

The Xist module of the HTRI Xchanger Suite is used for shell-and-tube reboilers. Although the HTRI technology is proprietary, some information has been published regarding the methodology used for kettle reboilers [17] and horizontal thermosyphon reboilers [12]. Additional information can be inferred from the detailed output files generated by the program. The general approach used for reboilers is similar to that of TASC described above.

For kettle reboilers, a recirculation model is used in which the internal circulation rate in the kettle is determined by a pressure balance. The internal circulation rate forms the basis for calculating the boiling heat-transfer coefficient, which is composed of nucleate boiling and convective terms, with correction factors for nucleate boiling suppression, convective enhancement, and mixture effects. As with single-phase exchangers, Xist performs incremental (stepwise) calculations using a threedimensional grid. This feature allows local temperature gradients and heat-transfer coefficients to be computed and greatly improves the reliability of the method, especially for multi-component systems. Reliable simulation is possible with any type of heating medium, including multi-component condensing process streams [17].

For thermosyphon reboilers, the piping configuration is specified as input and the program calculates the circulation rate. Either a detailed or simplified piping configuration can be used. In the latter, only the total liquid head and the equivalent lengths of feed and return lines are entered. In the former, complete details of both lines are entered using equivalent lengths for pipe fittings. Either user-specified equivalent lengths or default values contained in the program can be used.

For all types of reboilers, the actual and critical heat fluxes are computed at each increment, along with the flow regime (bubble, slug, etc.) and the boiling mechanism (nucleate, film, etc.). For thermosyphons, a stability assessment is also performed to determine the potential for various types of flow instability in the hydraulic circuit.

The following examples illustrate the use of Xist for reboiler applications.

## Example 10.10

Use Xist to rate the kettle reboiler designed in Example 10.2, and compare the results with those obtained previously by other methods.

## Solution

Data from Example 10.2 are entered on the appropriate Xist input forms as indicated below. Parameters not listed are either left at their default settings or left unspecified to be calculated by the program.
(a) Geometry/Shell.

Case mode: Rating
TEMA type: BKU
Shell ID: 23.25 in.
Hot fluid location: Tube side
(b) Geometry/Reboiler.

Kettle diameter: 37 in.
Number of boiling components: 3
(c) Geometry/Tubes.

Tube OD: 1 in.
Average wall thickness: 0.083 in.
Tube pitch: 1.25 in.
Tube layout angle: $90^{\circ}$
Inlet pressure location: At inlet nozzle
(d) Geometry/Baffles.

Baffle type: None (This is the only option available for a kettle.)
Support plates/baffle space: User set: 3
(e) Geometry/Nozzles.

Shell side
Inlet ID: 5.047 in .
Number: 2
Outlet ID: 6.065 in.
Number: 2
Liquid outlet ID: 4.026 in.
Radial position of inlet nozzle: Bottom
(f) Process.

|  | Hot fluid | Cold fluid |
| :--- | :--- | :--- |
| Fluid name | Steam | Distillation Bottoms |
| Phase | Condensing | Boiling |
| Flow rate $(1000 \mathrm{lb} / \mathrm{h})$ | 5.645 | 96 |
| Inlet fraction vapor | 1 | 0 |
| Outlet fraction vapor | 0 |  |
| Inlet pressure (psia) | 20 | 250 |
| Fouling resistance $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ | 0.0005 | 0.0005 |

(g) Hot fluid properties.

Physical property input option: Component by component
Heat release input method: Program calculated
Clicking on the Property Generator button opens the property generator as shown below. VMG Thermo is selected as the property package and Steam95 is selected from the list of thermodynamic methods for both the vapor and liquid phases. This method uses steam tables to obtain fluid properties.


On the composition form, water is selected from the list of components as shown below. Since it is the only component in the hot stream, its mole fraction is 1.0 .


On the conditions form, two pressure levels, 20 and 19 psia , are specified and the temperature range for fluid properties is set as shown below. The number of points in this range at which properties are to be generated is set at 20 .


Clicking on the Generate Properties button produces the results shown below. The Transfer button is clicked to transfer the data to Xist. (Note that a maximum of 30 data points can be transferred.) Finally, clicking the Done button closes the property generator and returns control to the Xist input menu.

(h) Cold fluid properties.

Properties of the hydrocarbon stream are generated in the same manner as for steam. In this case, the Advanced Peng-Robinson thermodynamic method is chosen for both the vapor and liquid phases. On the conditions form, two pressure levels, 250 and 240 psia , are specified with a temperature range of $195-225^{\circ} \mathrm{F}$. The number of data points is again set at 20 .

The Xist output summary for this case is given below, from which it is found that the over-design for the unit is about $33 \%$. Xist produced a tube layout containing 206 tubes ( 103 U-tubes), which agrees well with the tube layout generated by TASC (210 tubes) and the tube-count table (212 tubes).

## Xist Output Summary for Example 10.10

| Xist E Ver. 4.00 SP2 10/17/2005 18:34 SN: 1600201024 <br> US Units <br> Rating - Horizontal Multipass Flow TEMA BKU Shell With No Baffles |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| See Data Check Messages Report for Warning Messages. See Runtime Message Report for Warning Messages. |  |  |  |  |  |
| Process Conditions Fluid name |  | Cold Shellside Distillation Bottoms |  | Hot Tubeside |  |
|  |  | steam |  |
| Flow rate | (1000 lb/hr) |  | 0.000 | 96.0000 | 5.6450 |
| Inlet/Outlet Y | (Wt. frac vap.) | 0.000 | 0.500 | $1.000$ | 0.000 |
| Inlet/Outlet T | (Deg F) | 196.60 | 201.69 | 227.90 | 226.98 |
| Inlet P/Avg | (psia) | 250.000 | 249.937 | 20.000 | 19.832 |
| dP/Allow. | (psi) | 0.126 | 0.000 | 0.337 | 0.000 |
| Fouling | (ft2-hr-F/Btu) |  | 0.00050 |  | 0.00050 |
| Exchanger Performance |  |  |  |  |  |
| Shell h | (Btu/ft2-hr-F) | 1006.60 | Actual U | (Btu/ft2-hr-F) | 361.84 |
| Tube h | (Btu/ft2-hr-F) | 2709.10 | Required U | (Btu/ft2-hr-F) | 272.12 |
| Hot regime | (-) | Transition | Duty | (MM Btu/hr) | 5.4240 |
| Cold regime | (-) | Flow | Area | (ft2) | 746.925 |
| EMTD | (Deg F) | 26.7 | Overdesign | (\%) | 32.97 |
| Shell Geometry |  |  | Baffle Geometry |  |  |
| TEMA type | (-) | BKU | Baffle type | (-) | Support |
| Shell ID | (inch) | 23.2500 | Baffle cut | (Pct Dia.) |  |
| Series | (-) | 1 | Baffle orientation | n (-) |  |
| Parallel | (-) | 1 | Central spacing | (inch) | 38.5000 |
| Orientation | (deg) | 0.00 | Crosspasses | (-) | 1 |
| Tube Geometry |  |  | Nozzles |  |  |
| Tube type | (-) | Plain | Shell inlet | (inch) | 5.0470 |
| Tube OD | (inch) | 1.0000 | Shell outlet | (inch) | 6.0650 |
| Length | (ft) | 13.000 | Inlet height | (inch) | 0.8750 |
| Pitch ratio | (-) | 1.2500 | Outlet height | (inch) | 14.4303 |
| Layout | (deg) | 90 | Tube inlet | (inch) | 6.0650 |
| Tubecount | (-) | 212 | Tube outlet | (inch) | 3.0680 |
| Tube Pass | (-) | 2 |  |  |  |
| Thermal Resistance, \% |  | Velocities, ft/sec |  | Flow Fractions |  |
| Shell | 35.95 | Shellside | 0.99 | A | 0.000 |
| Tube | 16.01 | Tubeside | 41.62 | B | 1.000 |
| Fouling | 39.79 | Crossflow | 0.69 | C | 0.000 |
| Metal | 8.254 | Window | 0.00 | E | 0.000 |
|  |  |  |  | F | 0.000 |

The following table compares the results from Xist with those obtained in previous examples using other methods. It can be seen that the three computer solutions are in reasonably good agreement, with the values calculated by Xist generally falling between those from HEXTRAN and TASC. Xist is somewhat more conservative than TASC with respect to both the boiling and condensing heat-transfer coefficients.

| Item | Hand | HEXTRAN | TASC | Xist |
| :--- | :--- | :--- | :--- | :--- |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 523 | $936^{\mathrm{a}}$ | 1146 | 1007 |
| $\left[\left(D_{o} / D_{i}\right)\left(1 / h_{i}+R_{D i}\right)\right]^{-1}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 1500 | $857^{\mathrm{a}}$ | 1090 | 957 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 297 | $335^{\mathrm{a}}$ | 392 | 362 |
| $\Delta P_{i}(\mathrm{psi})$ | 0.3 | 0.43 | 0.35 | 0.34 |
| $\Delta P_{o}(\mathrm{psi})^{\mathrm{b}}$ | 0.2 | 0 | 0.055 | 0.022 |
| $\Delta T_{m}\left({ }^{\circ} \mathrm{F}\right)$ | 25.6 | $27.1^{\mathrm{a}}$ | 25.4 | 26.7 |
| $U_{D} \Delta T_{m}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2}\right)$ | 7603 | $9079^{\mathrm{a}}$ | 9957 | 9665 |
| $\left(\hat{q} / \hat{q}_{c}\right)_{\text {max }}$ | 0.11 | - | 0.085 | $0.10^{\mathrm{c}}$ |

[^1]
## Example 10.11

Use Xist to rate the initial configuration for the vertical thermosyphon reboiler of Example 10.4 and compare the results with those obtained previously by other methods.

## Solution

Data from Example 10.4 are entered on the Xist input forms as indicated below.
(a) Geometry/Shell.

Case mode: Rating
Shell orientation: Vertical
TEMA type: AEL Hot fluid location: Shell side
Shell ID: 15.25 in.
(b) Geometry/Reboiler.

Reboiler type: Thermosyphon reboiler
Number of boiling components: 1
Required liquid static head: 8 ft
Inlet pressure location: At column bottom
Note: The static head for a vertical thermosyphon reboiler is the vertical distance between the lower tubesheet and the liquid level in the column sump.
(c) Geometry/Tubes.

Tube OD: 1 in.
Average wall thickness: 0.083 in.
Tube pitch: 1.25 in.
Tube passes: 1

Tube layout angle: $30^{\circ}$
(d) Geometry/Baffles.

Baffle cut: 35\%
Central baffle spacing: 6.1 in.
(e) Geometry/Clearances.

Pairs of sealing strips: None
(f) Geometry/Nozzles.

Shell side
Inlet ID: 4.026 in .
Number: 1
Outlet ID: 2.067 in.
Number: 1

Tube side
Inlet ID: 6.065 in.
Number: 1
Outlet ID: 10.02 in.
Number: 1
(g) Piping.

The detailed piping forms are used here to illustrate the procedure. They are invoked by checking the box for detailed piping on the main piping form. The inlet piping form is shown below:


The piping elements are selected from a list box that appears when a blank field in the first column is clicked. In this case there are only three elements because the straight pipe equivalent length is assumed to account for all entrance, exit, and fitting losses. Height changes are negative in the downward direction and positive in the upward direction. Height changes of individual elements are arbitrary here as long as they total to negative 8 ft . This puts the lower tubesheet a vertical distance of 8 ft below the liquid surface in the column sump. The outlet piping form is similar and is shown below:

| - Input Summary-Piping-Outlet |  |  |  |  |  |  |  | - $\square$ [] $\times$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Standard | 01-ANSI_B36_10.table |  |  | Schedule STD |  | $\square$ |  | $\wedge$ |
|  | $\begin{aligned} & \text { Element } \\ & \text { Type } \end{aligned}$ | Inside Diamete <br> (inch) |  | Equivalent Length <br> (ft) | Height Change <br> (t) | Number of Increments | Friction Factor Multiplier | Friction Factor |
| 1 | Header (height only) |  | $\ldots$ |  | 2 |  |  |  |
| 2 | Straight pipe | 10.02 | ... | 50 | 0 | 1 |  |  |
| 3 |  |  | ... |  |  |  |  |  |
| 4 |  |  | ... |  |  |  |  |  |
| 5 |  |  | ... |  |  |  |  |  |

The outlet header extends from the upper tubesheet to the return pipe. Since the upper tubesheet is at the same elevation as the liquid surface in the column sump, the specified height change puts the return pipe a vertical distance of 2 ft above the surface of the liquid in the sump. (Note that the inlet and outlet piping specifications given here are completely equivalent to those used with TASC in Examples 10.8 and 10.9.)
(h) Process.

|  | Hot fluid | Cold fluid |
| :--- | :--- | :--- |
| Fluid name | Steam | Cyclohexane |
| Phase | Condensing | Boiling |
| Flow rate $(1000 \mathrm{lb} / \mathrm{h})$ | 2.397 | 113.814 |
| Inlet fraction vapor | 1 | 0 |
| Outlet fraction vapor | 0 |  |
| Inlet pressure (psia) | 18 | 16 |
| Fouling resistance $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ | 0 | 0.0005 |

(i) Hot fluid properties.

VMG Thermo and Steam95 are selected for the property package. Pressure levels of 20, 18, and 16 psia are specified with a temperature range of $200-230^{\circ} \mathrm{F}$, and the number of data points is set at 20 .
(j) Cold fluid properties.

VMG Thermo and the Advanced Peng-Robinson method are selected for the cyclohexane stream. Pressure levels of 20,18 , and 16 psia are specified with a temperature range of $180-$ $220^{\circ} \mathrm{F}$, and 20 data points are again used.

The Xist output summary for this case is shown below, from which the unit is seen to be under-designed by about $21 \%$. Data from the output summary and detailed output files were used to prepare the results comparison shown in the table below. The heat-transfer coefficients calculated by Xist are close to those computed by TASC. However, the circulation rates from the two programs differ by more than a factor of two. Despite this fact, the total tube-side pressure drop is nearly the same in both cases, 2.15 versus 2.17 psia . (The Xist value includes the nozzle losses but not the static head losses in the inlet and outlet headers. The latter are included with the inlet and outlet piping. Hence, the pressure drops reported by TASC and Xist are equivalent.)

| Item | Hand | TASC | Xist |
| :--- | :--- | :--- | :--- |
| Circulation rate $(\mathrm{lb} / \mathrm{h})$ | 113,814 | 114,973 | 52,694 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | $565^{\mathrm{a}}$ | 495 | 501 |
| $h_{0}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 1500 (assumed) | 1584 | 1290 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | $243^{\mathrm{a}}$ | 255.7 | 250 |
| $\Delta P_{i}(\mathrm{psi})^{\mathrm{c}}$ | 0.86 | 0.894 | 0.74 |
| $\Delta P_{o}(\mathrm{psi})$ | - | 1.165 | 0.55 |
| $\Delta T_{m}\left({ }^{( } \mathrm{F}\right)$ | $34.7^{\mathrm{F}}$ | 34 | 33.8 |
| $\left(\hat{q} / \hat{q}_{c}\right)_{\text {max }}$ | 0.48 | 0.217 | 0.38 |

[^2]
## Xist Output Summary for Example 10.11

| Xist E Ver. 4.00 SP2 10/24/2005 20:42 SN: 1600201024 US Units <br> Rating - Vertical Thermosiphon Reboiler TEMA AEL Shell With Single-Segmental Baffles |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No Data Check Messages. See Runtime Message Report for Warning Messages. |  |  |  |  |  |
| Process Conditions <br> Fluid name |  | Hot Shellside Steam |  | Cold Tubeside Cyclohexane |  |
| Flow rate | (1000 lb/hr) |  | 2.3970 |  | 52.6936* |
| Inlet/Outlet Y | (Wt. frac vap.) | 1.000 | 0.000 | 0.000 | 0.288 |
| Inlet/Outlet T | (Deg F) | 222.34 | 220.66 | 182.51 | 183.60 |
| Inlet P/Avg | (psia) | 18.000 | 17.725 | 18.470 | 17.383 |
| dP/Allow. | (psi) | 0.551 | 0.000 | 2.172 | 0.000 |
| Fouling | (ft2-hr-F/Btu) |  | 0.00000 |  | 0.00050 |
| Exchanger Performance |  |  |  |  |  |
| Shell h | (Btu/ft2-hr-F) | 1289.83 | Actual U | (Btu/ft2-hr-F) | 250.34 |
| Tube h | (Btu/ft2-hr-F) | 501.26 | Required U | (Btu/ft2-hr-F) | 317.86 |
| Hot regime | $(-)$ | Gravity | Duty | (MM Btu/hr) | 2.3116 |
| Cold regime | $(-)$ | Nucl | Area | (ft2) | 214.952 |
| EMTD | (Deg F) | 33.8 | Overdesign | (\%) | -21.24 |
| Shell Geometry |  |  | Baffle Geometry |  |  |
| TEMA type | (-) | AEL | Baffle type | (-) | Single-Seg. |
| Shell ID | (inch) | 15.2500 | Baffle cut | (Pct Dia.) | 35.00 |
| Series | $(-)$ | 1 | Baffle orientation | (-) | PARALLEL |
| Parallel | (-) | 1 | Central spacing | (inch) | 6.1000 |
| Orientation | (deg) | 90.00 | Crosspasses | (-) | 13 |
| Tube Geometry |  |  | Nozzles |  |  |
| Tube type | (-) | Plain | Shell Inlet | (inch) | 4.0260 |
| Tube OD | (inch) | 1.0000 | Shell outlet | (inch) | 2.0670 |
| Length | (ft) | 8.000 | Inlet height | (inch) | 1.6250 |
| Pitch ratio | (-) | 1.2500 | Outlet height | (inch) | 0.2500 |
| Layout | (deg) | 30 | Tube inlet | (inch) | 6.0650 |
| Tubecount | $(-)$ | 106 | Tube outlet | (inch) | 10.0200 |
| Tube Pass | (-) | 1 |  |  |  |
| Thermal Resistance, \% |  | Velocities, ft/sec |  | Flow Fractions |  |
| Shell | 19.44 | Shellside | 41.88 | A | 0.136 |
| Tube | 59.82 | Tubeside | 18.89 | B | 0.630 |
| Fouling | 15.03 | Crossflow | 49.66 | C | 0.106 |
| Metal | 5.706 | Window | 29.84 | E | 0.128 |
|  |  |  |  | F | 0.000 |

## Example 10.12

Use Xist to obtain a final design for the vertical thermosyphon reboiler of Example 10.4.

## Solution

Starting from the $15.25-\mathrm{in}$. unit rated in the previous example, the shell size is increased one size at a time until a suitable configuration is obtained. Based on the results of previous examples, the following additional changes are made to the input data:

- The tube count is left unspecified so that it will be determined by the program based on the detailed tube layout.
- The central baffle spacing is adjusted to maintain $B / d_{s}$ in the range $0.35-0.40$, and the baffle cut is adjusted accordingly.
- A fouling factor of $0.0005 \mathrm{~h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is included for steam to provide an added safety margin.
- The steam pressure is increased to 20 psia and the flow rate is increased to $2450 \mathrm{lb} / \mathrm{h}$.

With these settings, the smallest viable unit is found to be a 19.25-in. exchanger. The Xist output summary for this case using the actual tube layout (after adding tie rods) as input is given below, from which the over-design for the unit is seen to be about $10 \%$. The detailed output file from Xist was used to compile the design summary shown in the following table. The setting plan and tube layout generated by Xist are also given. Minor changes in some design parameters are to be expected pending mechanical design calculations.

## Xist Output Summary for Example 10.12

| Xist E Ver. 4.00 SP2 10/26/2005 18:51 SN: 1600201024 |  |  |  |  | US Units |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Rating - Vertical Thermosiphon Reboiler TEMA AEL Shell With Single-Segmental Baffles |  |  |  |  |  |
| No Data Check Messages. See Runtime Message Report for Warning Messages. |  |  |  |  |  |
|  |  |  |  |  |  |
| Process Conditions Fluid name |  | Hot Shellside |  | Cold Tubeside |  |
| Flow rate | $00 \mathrm{lb} / \mathrm{hr})$ |  | 2.4500 |  | 1813* |
|  |  |  |  |  |  |
| Inlet/Outlet Y | (Wt. frac vap.) | 1.000 | 0.000 | 0.000 | 0.203 |
| Inlet/Outlet T | (Deg F) | 227.90 | 226.92 | 182.51 | 184.01 |
| Inlet P/Avg | (psia) | 20.000 | 19.825 | 18.428 | 17.418 |
| dP/Allow. | (psi) | 0.350 | 0.000 | 2.020 | 0.000 |
| Fouling | (ft2-hr-F/Btu) |  | 0.00050 |  | 0.00050 |
| Exchanger Performance |  |  |  |  |  |
| Shell h | (Btu/ft2-hr-F) | 1232.22 | Actual U | (Btu/ft2-hr-F) | 181.77 |
| Tube h | (Btu/ft2-hr-F) | 356.63 | Required U | (Btu/ft2-hr-F) | 164.76 |
| Hot regime | (-) | Gravity | Duty | (MM Btu/hr) | 2.3531 |
| Cold regime | (-) | Nucl | Area | (ft2) | 355.841 |
| EMTD | (Deg F) | 40.1 | Overdesign | (\%) | 10.33 |
| Shell Geometry |  |  | Baffle Geometry |  | Single-Seg. |
| TEMA type |  | AEL | Baffle type | (-) |  |
| Shell ID | (inch) | 19.2500 | Baffle cut | (Pct Dia.) | 35.00 |
| Series | (-) | 1 | Baffle orientation | (-) | PERPEND. |
| Parallel | (-) | 1 | Central spacing | (inch) | 7.0000 |
| Orientation | (deg) | 90.00 | Crosspasses | (-) | 11 |
| Tube Geometry |  |  | Nozzles |  |  |
| Tube type | (-) | Plain | Shell Inlet | (inch) | 4.0260 |
| Tube OD | (inch) | 1.0000 | Shell outlet | (inch) | 2.0670 |
| Length | (ft) | 8.000 | Inlet height | (inch) | 1.6715 |
| Pitch ratio | (-) | 1.2500 | Outlet height | (inch) | 0.3406 |
| Layout | (deg) | 30 | Tube inlet | (inch) | 6.0650 |
| Tubecount | (-) | 177 | Tube outlet | (inch) | 10.0200 |
| Tube Pass | (-) | 1 |  |  |  |
| Thermal Resistance, \% |  | Velocities, ft/sec |  | Flow Fractions |  |
| Shell | 14.76 | Shellside | 26.43 | A | 0.158 |
| Tube | 61.08 | Tubeside | 12.05 | B | 0.613 |
| Fouling | 20.00 | Crossflow | 33.66 | C | 0.050 |
| Metal | 4.150 | Window | 18.54 | E | 0.179 |
|  |  |  |  | F | 0.000 |

The design obtained using Xist is similar to the 19.25 -in. unit designed using TASC. However, with 20 -psia steam, a $17.25-\mathrm{in}$. exchanger was found to be adequate using TASC. Thus, Xist yields a more conservative design in this case. Also, Xist does not issue a recommendation to consider a conical head as was used in the TASC design. In fact, Xist does not provide an option for this type of head. However, a similar result can be achieved by specifying an axial tube-side exit nozzle on the Geometry/Nozzles form. Using an axial nozzle gives a slightly smaller tube-side pressure drop ( 2.017 psi ) with corresponding differences in the circulation rate ( $78,786 \mathrm{lb} / \mathrm{h}$ ) and exit vapor fraction (0.194). Since these changes are insignificant, design parameters for this modification are not listed in the table below. However, the setting plan for this case is included to illustrate the nozzle configuration.

| Item | Value |
| :--- | :--- |
| Steam design pressure (psia) | 20 |
| Exchanger type | AEL |
| Shell size (in.) | 19.25 |
| Surface area (ft ${ }^{2}$ ) | 355.8 |
| Number of tubes | 177 |
| Tube OD (in.) | 1.0 |
| Tube length (ft) | 8 |
| Tube BWG | 14 |
| Tube passes | 1 |
| Tube pitch (in.) | 1.25 |
| Tube layout | Triangular |
| Tubesheet thickness (in.) | 1.925 |
| Number of baffles | 10 |
| Baffle cut (\%) | 35 |
| Baffle thickness (in.) | 0.1875 |
| Central baffle spacing (in.) | 7.00 |
| Inlet baffle spacing (in.) | 16.28 |
| Outlet baffle spacing (in.) | 12.87 |
| Sealing strip pairs | 0 |
| Tube-side inlet nozzle | 6 -in. schedule 40 |
| Tube-side outlet nozzle | 10 -in. schedule 40 |
| Shell-side inlet nozzle | 4 -in. schedule 40 |
| Shell-side outlet nozzle | 2 -in. schedule 40 |
| $\Delta P_{i}$ (psi) | 2.02 |
| $\Delta P_{o}$ (psi) | 0.35 |
| Circulation rate (lbm/h) | 75,181 |
| Exit vapor fraction | 0.203 |
| Vapor generation rate (lbm/h) | 15,262 |
| Steam flow rate (lbm/h) | 2450 |
| $\left(\hat{q} / \hat{q}_{c}\right)_{\text {max }}$ | 0.195 |
| Flow stability assessment | Stable |
| Two-phase flow regimes | Bubble, slug, annular |
| Boiling regime | Nucleate |

## Setting Plans and Tube Layout for Example 10.12



Axial tube-side exit nozzle


## References

1. Palen, J. W., Shell-and-tube reboilers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
2. Sloley, A. W., Properly design thermosyphon reboilers, Chem. Eng. Prog., 93, No. 3, 52-64, 1997.
3. Kister, H. Z., Distillation Operation, McGraw-Hill, New York, 1990.
4. Fair, J. R., Vaporizer and reboiler design: Part 1, Chem. Eng., 70, No. 14, 119-124, 1963.
5. Palen, J. W. and W. M. Small, A new way to design kettle and internal reboilers, Hydrocarbon Proc., 43, No. 11, 199-208, 1964.
6. Bell, K. J. and A. J. Mueller, Wolverine Engineering Data Book II, Wolverine Tube, Inc., www.wlv.com, 2001.
7. Shinskey, F. G., Distillation Control, McGraw-Hill, New York, 1977.
8. Lee, D. C., J. W. Dorsey, G. Z. Moore and F. D. Mayfield, Design data for thermosyphon reboilers, Chem. Eng. Prog., 52, No. 4, 160-164, 1956.
9. Dowlati, R. and M. Kawaji, Two-phase flow and boiling heat transfer in tube bundles, Chapter 12 in Handbook of Phase Change: Boiling and Condensation, S. G. Kandlikar, M. Shoji and V. K. Dhir, eds, Taylor and Francis, Philadelphia, PA, 1999.
10. Fair, J. R., What you need to design thermosyphon reboilers, Pet. Refiner, 39, No. 2, 105-123, 1960.
11. Fair, J. R. and A. Klip, Thermal design of horizontal reboilers, Chem. Eng. Prog., 79, No. 3, 86-96, 1983.
12. Yilmaz, S. B., Horizontal shellside thermosyphon reboilers, Chem. Eng. Prog., 83, No. 11, 64-70, 1987.
13. Hewitt, G. F., G. L. Shires and T. R. Bott, Process Heat Transfer, CRC Press, Boca Raton, FL, 1994.
14. Collins, G. K., Horizontal thermosyphon reboiler design, Chem. Eng., 83, No. 15, 149-152, 1976.
15. Palen, J. W., C. C. Shih and J. Taborek, Mist flow in thermosyphon reboilers, Chem. Eng. Prog., 78, No. 7, 59-61, 1982.
16. Poling, B. E., J. M. Prausnitz and J. P. O'Connell, The Properties of Gases and Liquids, 5th edn, McGraw-Hill, New York, 2000.
17. Palen, J. W. and D. L. Johnson, Evolution of kettle reboiler design methods and present status, Paper No. 13i, AIChE National Meeting, Houston, March 14-18, 1999.
18. Perry, R. H. and C. H. Chilton, eds, Chemical Engineers' Handbook, 5th edn, McGraw-Hill, New York, 1973.

Appendix 10.A Areas of Circular Segments.

| $h / D$ | A | $h /$ | $A$ | $h / D$ | $A$ | W | $A$ |  | A |  | A |  | $A$ |  | $A$ |  | $A$ | , | A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0. | 0. | 0. | 0. | 0. | 0. | 0. |  | 0.2 | 0. | 0.300 | 0.19817 | 0.350 | 0.24498 |  | 7 |  |  |
|  | 0. | 0.05 | 0.01 | 0.102 | 0.0 | 0.152 | 0. | 0.202 | 0. | 0.2 | 0.15528 | 0.302 | 0.20000 | 0.352 | 0.24689 | 0.402 | 0.29533 | 2 | 477 |
| 0.004 | 0.000 | 0.05 | 0.01646 | 0.104 | 0.04 | 0.154 | 0.07 | 0.204 | 0.11504 | 0.25 | 0.15702 | 0.304 | 0.20184 | 0.354 | 0.24880 | 0.404 | 0.29729 | 4 | 0.34676 |
| 006 | 0.00062 | 0.05 | 0.01737 | 0.106 | 0.04452 | 0.156 | 0.07819 | 0.206 | 0.11665 | 0.256 | 0.15 | 0.306 | 0.20368 | 0.356 | 0.25071 | 0.406 | 226 | 6 | 0.34876 |
| 0.008 | 0.00095 | 0.058 | 0.01830 | 0.108 | 0.04576 | 0.158 | 0.07965 | 0.208 | 0.11827 | 0.258 | 0.16051 | 0.308 | 0.20553 | 0.358 | 0.25263 | 0.408 | 0.30122 | 0.458 | 0.35075 |
| 0.010 | 0.00 | 0.06 | 0.0 | 0.1 | 0.04 | 0.1 | 0.0 | 0.2 | 0.1199 | 0.26 | 0.16 | 0.3 | 0.20738 | 0.360 | 0.25455 | 0. | 0.3031 | 0.460 | 0.35274 |
| 0.012 | 0.00175 | 0.062 | 0.02020 | 0.112 | 0.04826 | 0.162 | 0.08258 | 0.212 | 0.12153 | 0.262 | 0.16402 | 0.312 | 0.20923 | 0.362 | 0.25647 | 0.412 | 0.30516 | 0.462 | 0.35474 |
| 0.014 | 0.00220 | 0.064 | 0.02117 | 0.114 | 0.04953 | 0.164 | 0.08406 | 0.214 | 0.12317 | 0.264 | 0.16578 | 0.314 | 0.21108 | 0.364 | 0.25839 | 0.414 | 0.30712 | 0.464 | 0.35673 |
| 0.016 | 0.00268 | 0.066 | 0.02215 | 0.116 | 0.05080 | 0.166 | 0.08554 | 0.216 | 0.12481 | 0.266 | 0.16755 | 0.316 | 0.21294 | 0.366 | 0.26032 | 0.416 | 0.30910 | 0.466 | 0.35873 |
| 0.018 | 0.00320 | 0.068 | 0.02315 | 0.118 | 0.05209 | 0.168 | 0.08704 | 0.218 | 0.12646 | 0.268 | 0.16932 | 0.318 | 0.21480 | 0.368 | 0.26225 | 0.418 | 0.31107 | 0.468 | 0.36072 |
| 0.020 | 0.00375 | 0.07 | 0.02417 | 0.12 | 0.05 | 0.170 | . | 0.2 |  | 0.270 |  | 0.320 | 0.21667 | 0.370 |  |  |  |  | 0.36272 |
| 0.022 | 0.00432 | 0.07 | 0.02520 | 0.12 | 0.05469 | 0.172 | 0.09004 | 0.222 | 0.12977 | 0.272 | 0.17287 | 0.322 | 0.21853 | 0.372 | 0.26611 | 0.422 | 0.31502 | 0.472 | 0.36471 |
| 0.024 | 0.00492 | 0.07 | 0.02624 | 0.124 | 0.05600 | 0.174 | 0.09155 | 0.224 | 0.13144 | 0.274 | 0.17465 | 0.324 | 0.22040 | 0.374 | 0.26805 | 0.424 | 0.31699 | 0.474 | 0.36671 |
| 0.026 | 0.00555 | 0.076 | 0.02729 | 0.126 | 0.05733 | 0.176 | 0.09307 | 0.226 | 0.13311 | 0.276 | 0.17644 | 0.326 | 0.22228 | 0.376 | 0.26998 | 0.426 | 0.31897 | 0.476 | 0.36871 |
| 0.028 | 0.00619 | 0.078 | 0.02836 | 0.128 | 0.05866 | 0.178 | 0.09460 | 0.228 | 0.13478 | 0.278 | 0.17823 | 0.328 | 0.22415 | 0.378 | 0.27192 | 0.428 | 0.32095 | 0.478 | 0.37071 |
| 0. | 0.00687 | 0.08 | 0.02943 | 0.13 | 0.0600 | 0.180 | 0.0961 | 0.230 | 0.13646 | 0.280 | 0.18002 | 0.330 | 0.22603 | 0.380 | 0.27386 | 0.430 | 0.32293 | 0.48 | 0.37270 |
| 0.032 | 0.00756 | 0.082 | 0.03053 | 0.132 | 0.06135 | 0.182 | 0.09767 | 0.232 | 0.13815 | 0.282 | 0.18182 | 0.332 | 0.22792 | 0.382 | 0.27580 | 0.432 | 0.32491 | 0.482 | 0.37470 |
| 0.034 | 0.00827 | 0.084 | 0.03163 | 0.13 | 0.06271 | 0.184 | 0.09922 | 0.234 | 0.13984 | 0.284 | 0.18362 | 0.334 | 0.22980 | 0.384 | 0.27775 | 0.434 | 0.32689 | 0.484 | 0.37670 |
| 0.036 | 0.00901 | 0.086 | 0.03275 | 0.136 | 0.06407 | 0.186 | 0.10077 | 0.236 | 0.14154 | 0.286 | 0.18542 | 0.336 | 0.23169 | 0.386 | 0.27969 | 0.436 | 0.32887 | 0.486 | 0.37870 |
| 0.038 | 0.00976 | 0.08 | 0.03387 | 0.13 | 0.0654 | 0.18 | 0.1023 | 0.23 | 0.1432 | 0.288 | 0.18723 | 0.338 | 0.23358 | 0.388 | 0.28164 | 0.438 | 0.33086 | 0.488 | 0.38070 |
| 40 | 0.01054 | 0.090 | 0.03501 | 0.140 | 0.0668 | 0.190 | 0.10390 | 0.240 | 0.14494 | 0.290 | 0.18905 | 0.340 | 0.23547 | 0.390 | 0.28359 | 0.440 | 0.33284 | 0.490 | 0.38270 |
| 0.042 | 0.01133 | 0.092 | 0.03616 | 0.142 | 0.06822 | 0.192 | 0.10547 | 0.242 | 0.14666 | 0.292 | 0.19086 | 0.342 | 0.23737 | 0.392 | 0.28554 | 0.442 | 0.33483 | 0.492 | 0.38470 |
| 0.044 | 0.01214 | 0.094 | 0.03732 | 0.144 | 0.06963 | 0.194 | 0.10705 | 0.244 | 0.14837 | 0.294 | 0.19268 | 0.344 | 0.23927 | 0.394 | 0.28750 | 0.444 | 0.33682 | 0.494 | 0.38670 |
| 0.046 | 0.01297 | 0.096 | 0.03850 | 0.146 | 0.07103 | 0.196 | 0.10864 | 0.246 | 0.15009 | 0.296 | 0.19451 | 0.346 | 0.24117 | 0.396 | 0.28945 | 0.446 | 0.33880 | 0.496 | 0.38870 |
| 0.048 | 0.01382 | 0.098 | 0.03968 | 0.148 | 0.07245 | 0.198 | 0.11023 | 0.248 | 0.15182 | 0.298 | 0.19634 | 0.348 | 0.24307 | 0.398 | 0.29141 | 0.448 | 0.34079 | 0.498 | 0.39070 |
| 0.050 | 0.01468 | 0.100 | 0.04087 | 0.150 | 0.07387 | 0.200 | 0.11182 | 0.250 | 0.15355 | 0.300 | 0.19817 | 0.350 | 0.24498 | 0.400 | 0.29337 | 0.450 | 0.34278 | 0.500 | 0.39270 |

[^3]
## Notations

A Heat-transfer surface area; circular sector area factor
$A_{\text {flow }} \quad$ Flow area
$B \quad$ Baffle spacing
$B R \quad$ Boiling range
$C_{P} \quad$ Heat capacity at constant pressure
$C_{P, L} \quad$ Heat capacity of liquid
$C_{1} \quad$ Parameter in Equation (9.20)
$D$ Diameter
$D_{b} \quad$ Diameter of tube bundle
$D_{e x} \quad$ Internal diameter of reboiler exit line
$D_{i} \quad$ Internal diameter of tube
$D_{i n} \quad$ Internal diameter of reboiler inlet line
$D_{o} \quad$ External diameter of tube
$D_{s} \quad$ Internal diameter of shell
$D_{t} \quad$ Internal diameter of tube in vertical thermosyphon reboiler
$E_{L W} \quad$ Convective enhancement factor in Liu-Winterton correlation
$F \quad$ LMTD correction factor
$F_{b} \quad$ Factor defined by Equation (9.20) that accounts for convective effects in boiling on tube bundles
$F_{m} \quad$ Mixture correction factor for Mostinski correlation
$F_{P} \quad$ Pressure correction factor for Mostinski correlation
$f \quad$ Darcy friction factor
$f_{e x} \quad$ Darcy friction factor for reboiler exit line
$f_{i n} \quad$ Darcy friction factor for reboiler inlet line
$f_{t} \quad$ Darcy friction factor for flow in vertical thermosyphon reboiler tubes
$G \quad$ Mass flux
$G_{e x} \quad$ Mass flux in reboiler exit line
$G_{i n} \quad$ Mass flux in reboiler inlet line
$G_{n} \quad$ Mass flux in nozzle
$G_{t} \quad$ Mass flux in vertical thermosyphon reboiler tubes
$G_{t, \text { mist }}$ Tube-side mass flux at onset of mist flow
$g \quad$ Gravitational acceleration
$g_{c} \quad$ Unit conversion factor
$H \quad$ Specific enthalpy
$H_{F} \quad$ Specific enthalpy of reboiler feed stream
$H_{L} \quad$ Specific enthalpy of liquid
$H_{V} \quad$ Specific enthalpy of vapor
$h \quad$ Height of circular sector
$h_{b} \quad$ Convective boiling heat-transfer coefficient
$h_{i} \quad$ Tube-side heat-transfer coefficient
$h_{L O} \quad$ Heat-transfer coefficient for total flow as liquid
$h_{n b} \quad$ Nucleate boiling heat-transfer coefficient
$h_{n c} \quad$ Natural convection heat-transfer coefficient
$h_{o} \quad$ Shell-side heat-transfer coefficient
$k \quad$ Thermal conductivity
$k_{L} \quad$ Thermal conductivity of liquid
$k_{\text {tube }} \quad$ Thermal conductivity of tube wall
$L \quad$ Tube length
$L_{B C} \quad$ Length of sensible heating zone in vertical thermosyphon reboiler
$L_{C D} \quad$ Length of boiling zone in vertical thermosyphon reboiler
$L_{e x} \quad$ Equivalent length of reboiler exit line
$L_{i n} \quad$ Equivalent length of reboiler inlet line

| $L_{\text {req }}$ | Required tube length |
| :---: | :---: |
| $L_{s}$ | Shell length required for liquid overflow reservoir in kettle reboiler |
| M | Molecular weight |
| $\dot{m}$ | Mass flow rate |
| $\dot{m}_{F}$ | Mass flow rate of reboiler feed stream |
| $\dot{m}_{i}$ | Mass flow rate of tube-side fluid |
| $\dot{m}_{L}$ | Mass flow rate of liquid |
| $\dot{m}_{\text {steam }}$ | Mass flow rate of steam |
| $\dot{m}_{T h}$ | Mass flow rate of Therminol ${ }^{\circledR}$ heat-transfer fluid |
| $\dot{m}_{V}$ | Mass flow rate of vapor |
| $N_{n}$ | Number of pairs (inlet/outlet) of nozzles |
| $N u$ | Nusselt number |
| $n_{p}$ | Number of tube passes |
| $n_{t}$ | Number of tubes in bundle |
| $P_{A}, P_{B}, P_{C}, P_{D}$ | Pressure at point $A, B, C, D$ in vertical thermosyphon reboiler system (Figure 10.8) |
| $P_{c}$ | Critical pressure |
| $P_{c, i}$ | Critical pressure of $i$ th component in mixture |
| $P_{p c}$ | Pseudo-critical pressure |
| $P_{p r}$ | Pseudo-reduced pressure |
| $P_{r}$ | Reduced pressure |
| $P_{L}$ | Prandtl number of liquid |
| $P_{\text {sat }}$ | Saturation pressure |
| $P_{T}$ | Tube pitch |
| $q$ | Rate of heat transfer |
| $q_{B C}$ | Rate of heat transfer in sensible heating zone of vertical thermosyphon reboiler |
| $q_{C D}$ | Rate of heat transfer in boiling zone of vertical thermosyphon reboiler |
| $\hat{q}$ | Heat flux |
| $\hat{q}_{c}$ | Critical heat flux |
| $\hat{q}_{c, \text { bundle }}$ | Critical heat flux for boiling on tube bundle |
| $\hat{q}_{\text {c,tube }}$ | Critical heat flux for boiling on a single tube |
| $R_{\text {Di }}$ | Fouling factor for tube-side fluid |
| $R_{\text {Do }}$ | Fouling factor for shell-side fluid |
| $R e$ | Reynolds number |
| $R e_{i}$ | Reynolds number for tube-side fluid |
| $R e_{\text {in }}$ | Reynolds number for flow in reboiler inlet line |
| $R e_{L}$ | Reynolds number for liquid phase flowing alone |
| $R e_{L O, e x}$ | Reynolds number for total flow as liquid in reboiler exit line |
| $R e_{n}$ | Reynolds number for flow in nozzle |
| SA | Dome segment area in kettle reboiler |
| $S_{L W}$ | Nucleate boiling suppression factor in Liu-Winterton correlation |
| SR | Slip ratio |
| $s$ | Specific gravity |
| $s_{L}$ | Specific gravity of liquid |
| T | Temperature |
| $T_{B}$ | Bubble-point temperature; temperature at inlet tubesheet (Figure 10.8) |
| $T_{C}$ | Temperature at end of sensible heating zone (Figure 10.8) |
| $T_{\text {cyhx }}$ | Temperature of cyclohexane |
| $T_{D}$ | Dew-point temperature |
| $T_{\text {sat }}$ | Saturation temperature |
| $U_{D}$ | Overall heat-transfer coefficient for design |
| $U_{\text {req }}$ | Required overall heat-transfer coefficient |
| V | Fluid velocity |
| $V L$ | Vapor loading |


| $V_{\max }$ | Maximum fluid velocity |
| :--- | :--- |
| $X_{t t}$ | Lockhart-Martinelli parameter |
| $x_{\text {ave }}$ | Average value of vapor mass fraction |
| $x_{e}$ | Vapor mass fraction at reboiler exit |
| $Y$ | Chisholm parameter |
| $z$ | Distance in vertical (upward) direction |
| $z_{A}, z_{B}, z_{C}, z_{D}$ | Elevation at point $A, B, C, D$ in vertical thermosyphon reboiler system |
| (Figure 10.8) |  |

## Greek Letters

| $\alpha_{r}$ | Number of velocity heads allocated for minor losses on tube side |
| :---: | :---: |
| $\gamma$ | Acceleration parameter defined by Equation (10.12) |
| $\Delta h$ | Elevation difference between liquid surface in column sump and surface of boiling liquid in kettle reboiler. |
| $\Delta h_{L}$ | Available liquid head in kettle reboiler system |
| $\Delta P_{\text {acc }}$ | Pressure loss due to fluid acceleration |
| $\Delta P_{a c c, k}$ | Pressure loss due to fluid acceleration in $k$ th interval of vapor weight fraction |
| $\Delta P_{f}$ | Pressure loss due to fluid friction in straight sections of tubes |
| $\Delta P_{\text {feed }}$ | Total frictional pressure loss in reboiler feed lines |
| $\Delta P_{i}$ | Total pressure drop for tube-side fluid |
| $\Delta P_{n}$ | Pressure loss in nozzles |
| $\Delta P_{r}$ | Pressure drop due to minor losses on tube side |
| $\Delta P_{\text {reboiler }}$ | Shell-side pressure drop due to friction and acceleration in kettle reboiler |
| $\Delta P_{\text {return }}$ | Total frictional pressure loss in return lines from reboiler |
| $\Delta P_{\text {static }}$ | Total pressure difference due to static heads in kettle reboiler system |
| $\Delta P_{\text {total }}$ | Total pressure loss in kettle reboiler system due to friction, acceleration, and static heads |
| $\Delta P_{t p}$ | Pressure difference due to static head of boiling fluid in kettle reboiler |
| $\Delta P_{V}$ | Pressure difference due to static head of vapor in kettle reboiler |
| $\left(\Delta P_{f} / L\right)_{L O}$ | Frictional pressure gradient for total flow as liquid |
| $\Delta T$ | Temperature difference |
| $\Delta T_{B C}$ | Temperature difference across sensible heating zone in vertical thermosyphon reboiler |
| $\Delta T_{\text {ln }}$ | Logarithmic mean temperature difference |
| $\left(\Delta T_{\ln }\right)_{c f}$ | Logarithmic mean temperature difference for counter-current flow |
| ( $\left.\Delta T_{\ln }\right)_{\text {co-current }}$ | Logarithmic mean temperature difference for co-current flow |
| $\Delta T_{m}$ | Mean temperature difference |
| $(\Delta T / \Delta P)_{s a t}$ | Slope of saturation curve |
| $\Delta \gamma_{k}$ | Change in $\gamma$ for $k$ th vapor-weight-fraction interval |
| $\varepsilon_{V}$ | Void fraction |
| $\varepsilon_{V, e}$ | Void fraction at reboiler exit |
| $\lambda$ | Latent heat of vaporization or condensation |
| $\lambda_{\text {steam }}$ | Latent heat of condensation of steam |
| $\mu$ | Viscosity |
| $\mu_{w}$ | Fluid viscosity at average tube wall temperature |
| $\rho$ | Density |
| $\rho a v e$ | Estimated average density of boiling fluid in kettle reboiler |
| $\rho_{\text {hom }}$ | Homogeneous two-phase density |
| $\rho_{L}$ | Density of liquid |
| $\bar{\rho}_{t p}$ | Average two-phase density in boiling zone of vertical thermosyphon reboiler |
| $\rho_{V}$ | Density of vapor |
| $\rho_{\text {water }}$ | Density of water |
| $\sigma$ | Surface tension |

$\phi_{b} \quad$ Correction factor for critical heat flux in tube bundles
$\phi_{i} \quad$ Viscosity correction factor for tube-side fluid
$\phi_{L O}$ Square root of two-phase multiplier applied to pressure gradient for total flow as liquid
$\bar{\phi}_{L O}^{2} \quad$ Average two-phase multiplier for boiling zone of vertical thermosyphon reboiler
$\phi_{L O, e x}$ Square root of two-phase multiplier in reboiler exit line
$\psi_{b} \quad$ Dimensionless bundle geometry parameter

## Problems

(10.1) A kettle reboiler is being designed to generate $75,000 \mathrm{lb} / \mathrm{h}$ of vapor having a density of $0.40 \mathrm{lbm} / \mathrm{ft}^{3}$. The liquid leaving the reboiler has a density of $41.3 \mathrm{lbm} / \mathrm{ft}^{3}$ and a surface tension of 16 dyne $/ \mathrm{cm}$. The length of the tube bundle is 15 ft and the diameter plus clearance is 32 in .
(a) Calculate the vapor loading and dome segment area.
(b) Calculate the diameter required for the enlarged section of the K-shell.
(c) How many pairs of shell-side nozzles should be used?

Ans. (a) $572.9 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{3}$ and $8.73 \mathrm{ft}^{2}$. (b) 63 in. (c) 2.
(10.2) The reboiler of Problem 10.1 is being designed for $65 \%$ vaporization. The feed to the reboiler has a density of $41.2 \mathrm{lbm} / \mathrm{ft}^{3}$ and a viscosity of 0.25 cp . Assuming schedule 40 pipe is used:
(a) What size inlet nozzles are required to meet TEMA specifications without using impingement plates?
(b) The primary feed line from the column sump to the reboiler will contain 35 linear feet of pipe, two $90^{\circ}$ elbows and a tee. The secondary lines (from the tee to the inlet nozzles) will each contain 4 linear feet of pipe, one $90^{\circ}$ elbow and (if necessary) a reducer. The secondary lines will be sized to match the inlet nozzles. Size the primary line to give a fluid velocity of about $5 \mathrm{ft} / \mathrm{s}$.
(c) Calculate the friction loss in the feed lines.

Ans. (a) 5-in. (b) All lines 5 -in. (c) 0.58 psi .
(10.3) The horizontal thermosyphon reboiler of Example 10.3 contains two shell-side exit nozzles. The return lines from the exit nozzles meet at a tee, from which the combined stream flows back to the distillation column. Each section of line between exit nozzle and tee contains 8 linear feet of $8-\mathrm{in}$. schedule 40 pipe and one $90^{\circ}$ elbow. Between the tee and the column there is an $8 \times 10$ expander, 50 linear feet of $10-\mathrm{in}$. schedule 40 pipe and one $90^{\circ}$ elbow. Calculate the total friction loss in the return lines.
(10.4) For the reboiler of Example 10.3 and Problem 10.3, the vertical distance between the reboiler exit and the point at which the center of the return line enters the distillation column is 8 ft . Calculate the pressure drop in the return line due to the static head.
Ans. 0.30 psi .
(10.5) Considering the large uncertainty associated with convective boiling correlations, it might be deemed prudent for design purposes to include a safety factor, $F_{s f}$, in the Liu-Winterton correlation as follows:

$$
h_{b}=F_{s f}\left[\left(S_{L W} h_{n b}\right)^{2}+\left(E_{L W} h_{L}\right)^{2}\right]^{0.5}
$$

In Example 10.4, repeat steps (q)-v through ( t ) using a safety margin of $20 \%\left(F_{s f}=0.8\right)$ with the Liu-Winterton correlation.

Ans. $L_{\text {req }}=7.3 \mathrm{ft}$.
(10.6) In Example 10.4, repeat steps (q) through ( t ) using the Chen correlation in place of the Liu-Winterton correlation.
(10.7) In Example 10.4, repeat step (u) using the Katto-Ohno correlation to calculate the critical heat flux. Compare the resulting value of $\hat{q} / \hat{q}_{c}$ with the value of 0.217 obtained in Example 10.8 using TASC.
(10.8) For the vertical thermosyphon reboiler of Example 10.4, suppose the tube length is increased from 8 ft to 12 ft and the surface of the liquid in the column sump is adjusted to remain at the level of the upper tubesheet.
(a) Assuming an exit vapor fraction of 0.132 corresponding to a circulation rate of $113,636 \mathrm{lbm} / \mathrm{h}$, calculate a new circulation rate using Equation (10.15).
(b) Continue the iterations begun in part (a) to obtain a converged value for the circulation rate.
(c) Use the result obtained in part (b) to calculate the tube length required in the boiling zone and compare this value with the available tube length.

Ans. (a) $126,435 \mathrm{lbm} / \mathrm{h}$.
(10.9) A kettle reboiler is required to supply $55,000 \mathrm{lb} / \mathrm{h}$ of hydrocarbon vapor to a distillation column. $80,000 \mathrm{lb} / \mathrm{h}$ of liquid at $360^{\circ} \mathrm{F}$ and 150 psia will be fed to the reboiler, and the duty is $6.2 \times 10^{6} \mathrm{Btu} / \mathrm{h}$. Heat will be supplied by steam at a design pressure of 275 psia . An existing carbon steel kettle containing 390 tubes is available at the plant site. The tubes are $1-\mathrm{in}$. OD, 14 BWG, 12 ft long on $1.25-\mathrm{in}$. square pitch, and the bundle diameter is 30 in . Will this unit be suitable for the service?

## Data for boiling-side fluid

Bubble point at $150 \mathrm{psia}: 360^{\circ} \mathrm{F}$
Dew point at $150 \mathrm{psia}: 380^{\circ} \mathrm{F}$
Vapor exit temperature: $370^{\circ} \mathrm{F}$
Pseudo-critical pressure: 470 psia
(10.10) A reboiler must supply $15,000 \mathrm{~kg} / \mathrm{h}$ of vapor to a distillation column at an operating pressure of 250 kPa . The reboiler duty is $5.2 \times 10^{6} \mathrm{~kJ} / \mathrm{h}$ and the flow rate of the bottom product, which consists of an aromatic petroleum fraction, is specified to be $6000 \mathrm{~kg} / \mathrm{h}$. Heat will be supplied by a liquid organic heat-transfer fluid flowing on the tube side with a range of $220-190^{\circ} \mathrm{C}$. A carbon steel kettle reboiler containing 510 tubes is available at the plant site. The tubes are $25.4-\mathrm{mm}$ OD, $14 \mathrm{BWG}, 4.57 \mathrm{~m}$ long on a $31.75-\mathrm{mm}$ square pitch, and the bundle diameter is 863 mm . In this unit the organic heat-transfer fluid will provide a tube-side coefficient of $1100 \mathrm{~W} / \mathrm{m}^{2}$. K with an acceptable pressure drop. Will the reboiler be suitable for this service?

## Data for boiling-side fluid

Bubble point at $250 \mathrm{kPa}: 165^{\circ} \mathrm{C}$
Dew point at $250 \mathrm{kPa}: 190^{\circ} \mathrm{C}$
Vapor exit temperature: $182^{\circ} \mathrm{C}$
Pseudo-critical pressure: 2200 kPa
(10.11) A reboiler must supply $80,000 \mathrm{lb} / \mathrm{h}$ of vapor to a distillation column at an operating pressure of 30 psia . The column bottoms, consisting of an aromatic petroleum fraction, will enter the reboiler as a (nearly) saturated liquid and the vapor fraction at the reboiler exit will be 0.2 . Heat will be supplied by steam at a design pressure of 235 psia. A used horizontal thermosyphon reboiler consisting of an X-shell containing 756 carbon steel tubes is available at the plant site. The tubes are $1-\mathrm{in}$. OD, $14 \mathrm{BWG}, 16 \mathrm{ft}$ long on $1.25-\mathrm{in}$. square pitch, and the bundle diameter is 40.4 in . Will the unit be suitable for this service?

Data for boiling-side fluid
Bubble point at 30 psia: $335^{\circ} \mathrm{F}$
Dew point at 30 psia: $370^{\circ} \mathrm{F}$
Saturation temperature at 30 psia and 0.2 vapor fraction: $344^{\circ} \mathrm{F}$
Enthalpy of liquid at $335^{\circ} \mathrm{F}: 245 \mathrm{Btu} / \mathrm{lbm}$
Enthalpy of liquid at $344^{\circ} \mathrm{F}: 250 \mathrm{Btu} / \mathrm{lbm}$
Enthalpy of vapor at $344^{\circ} \mathrm{F}: 385 \mathrm{Btu} / \mathrm{lbm}$
Pseudo-critical pressure: 320 psia
(10.12) $105,000 \mathrm{lb} / \mathrm{h}$ of a distillation bottoms having the following composition will be partially vaporized in a kettle reboiler.

| Component | Mole \% | Critical pressure (psia) |
| :--- | :--- | :--- |
| Toluene | 84 | 595.9 |
| $m$-Xylene | 12 | 513.6 |
| $o$-Xylene | 4 | 541.4 |

The stream will enter the reboiler as a (nearly) saturated liquid at 35 psia . The dew-point temperature of the stream at 35 psia is $304.3^{\circ} \mathrm{F}$. Saturated steam at a design pressure of 115 psia will be used as the heating medium. The reboiler must supply $75,000 \mathrm{lb} / \mathrm{h}$ of vapor to the distillation column. Physical property data are given in the following table. Design a kettle reboiler for this service.

| Property | Reboiler feed | Liquid overflow | Vapor return |
| :--- | :--- | :--- | :--- |
| $T\left({ }^{\circ} \mathrm{F}\right)$ | 298.6 | 302.1 | 302.1 |
| $H(\mathrm{Btu} / \mathrm{lbm})$ | 117.6 | 119.6 | 26.1 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.510 | 0.512 | 0.390 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.057 | 0.057 | 0.011 |
| $\mu(\mathrm{cp})$ | 0.192 | 0.191 | 0.00965 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 46.5 | 46.4 | 0.429 |
| $\sigma($ dyne $/ \mathrm{cm})$ | 14.6 | 14.5 | - |
| Molecular weight | 94.39 | 95.42 | 93.98 |

(10.13) The feed line for the reboiler of Problem 10.12 will contain approximately 30 linear feet of pipe while the vapor return line will require about 25 linear feet of pipe. The available elevation difference between the liquid level in the column sump and the reboiler inlet is 8 ft . Size the feed and return lines for the unit.
(10.14) $100,000 \mathrm{lb} / \mathrm{h}$ of a distillation bottoms having the following composition will be partially vaporized in a kettle reboiler.

| Component | Mole \% | Critical pressure (psia) |
| :--- | :--- | :--- |
| Cumene | 60 | 465.4 |
| $m$-diisopropylbenzene | 20 | 355.3 |
| $p$-diisopropylbenzene | 20 | 355.3 |

The stream will enter the reboiler as a (nearly) saturated liquid at 60 psia. The dew-point temperature of the stream at 60 psia is $480.3^{\circ} \mathrm{F}$. Saturated steam at a design pressure of 760 psia will be used as the heating medium. The reboiler must supply $60,000 \mathrm{lb} / \mathrm{h}$ of vapor to the distillation column. Physical property data are given in the following table. Design a kettle reboiler for this service.

| Property | Reboiler feed | Liquid overflow | Vapor return |
| :--- | :---: | :---: | :---: |
| $T\left({ }^{\circ} \mathrm{F}\right)$ | 455.3 | 471.4 | 471.4 |
| $H(\mathrm{Btu} / \mathrm{lbm})$ | 213.9 | 225.3 | 330.1 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.621 | 0.632 | 0.516 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.0481 | 0.0481 | 0.0158 |
| $\mu(\mathrm{cp})$ | 0.153 | 0.150 | 0.010 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 41.8 | 41.5 | 0.905 |
| $\sigma(\mathrm{dyne} / \mathrm{cm})$ | 8.66 | 8.20 | - |
| Molecular weight | 137.0 | 143.5 | 133.8 |

(10.15) For the reboiler of Problem 10.14, the feed line will contain approximately 27 linear feet of pipe while the vapor return line will require about 24 linear feet of pipe. The available elevation difference between the liquid level in the column sump and the reboiler inlet is 7.5 ft . Size the feed and return lines for the unit.
(10.16) Use TASC, Xist, HEXTRAN, or other available software to design a kettle reboiler for the service of Problem 10.12.
(10.17) Use TASC, Xist, HEXTRAN, or other available software to design a kettle reboiler for the service of Problem 10.14.
(10.18) A distillation column bottoms having the composition specified in Problem 10.12 will be fed to a horizontal thermosyphon reboiler operating at 35 psia . The reboiler must supply $240,000 \mathrm{lb} / \mathrm{h}$ of vapor to the column. The lengths of feed and return lines, as well as the liquid level in the column sump, are as specified in Problem 10.13. Use Xist, TASC, or other suitable software to design a reboiler system for this service.
(10.19) A distillation column bottoms having the composition specified in Problem 10.14 will be fed to a horizontal thermosyphon reboiler operating at 60 psia . The reboiler must supply $180,000 \mathrm{lb} / \mathrm{h}$ of vapor to the column. The length of feed and return lines, as well as the liquid level in the column sump, are as specified in Problem 10.15. Use Xist, TASC, or other suitable software to design a reboiler system for this service.
(10.20) A distillation column bottoms has an average API gravity of $48^{\circ}$ and the following assay (ASTM D86 distillation at atmospheric pressure).

| Volume \% distilled | Temperature $\left({ }^{\circ} \mathrm{F}\right)$ |
| :--- | :--- |
| 0 | 100 |
| 10 | 153 |
| 20 | 190 |
| 30 | 224 |
| 40 | 257 |
| 50 | 284 |
| 60 | 311 |
| 70 | 329 |
| 80 | 361 |
| 90 | 397 |
| 100 | 423 |

This stream will be fed to a horizontal thermosyphon reboiler operating at a pressure of 25 psia . At this pressure, the bubble- and dew-point temperatures of the feed are $218.2^{\circ} \mathrm{F}$ and $353.6^{\circ} \mathrm{F}$, respectively. The reboiler must supply $200,000 \mathrm{lb} / \mathrm{h}$ of vapor to the distillation column. Saturated steam at a design pressure of 70 psia will be used as the heating medium, and approximately $20 \%$ by weight of the feed will be vaporized in the reboiler. Physical properties of the feed and return streams are given in the following table. Design a reboiler for this service.

| Property | Reboiler feed | Liquid return | Vapor return |
| :--- | :---: | :--- | :--- |
| $T\left({ }^{\circ} \mathrm{F}\right)$ | 218.2 | 254.5 | 254.5 |
| $H(\mathrm{Btu} / \mathrm{lbm})$ | 89.1 | 107.3 | 247.2 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.516 | 0.533 | 0.437 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.061 | 0.058 | 0.013 |
| $\mu(\mathrm{cp})$ | 0.250 | 0.245 | 0.0092 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 44.5 | 44.2 | 0.287 |
| $\sigma(\mathrm{dyne} / \mathrm{cm})$ | 16.9 | 16.2 | - |
| $P_{p c}(\mathrm{psia})$ | 466.4 | - | - |

(10.21) Use HEXTRAN or other available software to design a horizontal thermosyphon reboiler for the service of Problem 10.20.
(10.22) For the service of Problem 10.20, the reboiler feed and return lines will each contain approximately 35 linear feed of pipe, and the available elevation difference between the liquid level in the column sump and the reboiler inlet will be 9.0 ft . Use TASC or other available software to design a horizontal thermosyphon reboiler system for this service. The size and configuration of the feed and return lines, along with the circulation rate, are to be determined in the design process.
Note: TASC cannot handle assay streams when used on a stand-alone basis. Therefore, the software must be interfaced with either HYSYS or Aspen Plus in order to solve this problem.
(10.23) Use TASC, Xist, or other suitable software to design a vertical thermosyphon reboiler for the service of Problem 10.12. Assume that the liquid level in the column sump will be maintained at approximately the elevation of the upper tubesheet in the reboiler. Also assume that the reboiler feed line will consist of 100 equivalent feet of pipe, while the return line will comprise

50 equivalent feet of pipe. Pipe diameters and circulation rate are to be determined in the design process.
(10.24) Use Xist, TASC, or other suitable software to design a vertical thermosyphon reboiler for the service of Problem 10.14. The assumptions specified in Problem 10.23 are applicable here as well.
(10.25) A reboiler is required to supply $30,000 \mathrm{lb} / \mathrm{h}$ of vapor to a distillation column at an operating pressure of 23 psia . The reboiler feed will have the following composition:

| Component | Mole \% |
| :--- | :---: |
| Ethanol | 1 |
| Isopropanol | 2 |
| 1-Propanol | 57 |
| 2-Methyl-1-propanol | 16 |
| 1-Butanol | 24 |

Saturated steam at a design pressure of 55 psia will be used as the heating medium. Use Xist, TASC, or other suitable software to design a vertical thermosyphon reboiler for this service. The assumptions stated in Problem 10.23 are also applicable to this problem. At operating pressure, the bubble point of the reboiler feed is $238^{\circ} \mathrm{F}$ and the dew point is $244^{\circ} \mathrm{F}$. The specific enthalpy of the bubble-point liquid is $139.5 \mathrm{Btu} / \mathrm{lbm}$ and that of the dew-point vapor is $408.5 \mathrm{Btu} / \mathrm{lbm}$.
(10.26) Rework Problem 10.14 for the case in which the heating medium is hot oil ( $30^{\circ} \mathrm{API}$, $K_{w}=12.0$ ) with a range of $600-500^{\circ} \mathrm{F}$. Properties of the oil are given in the following table. Assume that the oil is available at a pressure of 50 psia .

| Oil property | Value at $500^{\circ} \mathrm{F}$ | Value at $600^{\circ} \mathrm{F}$ |
| :--- | :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.69 | 0.75 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.049 | 0.044 |
| $\mu(\mathrm{cp})$ | 0.49 | 0.31 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 43.2 | 40.4 |

(10.27) Rework Problem 10.17 for the case in which the heating medium is hot oil as specified in Problem 10.26.
(10.28) Rework problem 10.19 for the case in which the heating medium is hot oil as specified in Problem 10.26.
(10.29) For the kettle reboiler of Example 10.2, a possible design modification (see step (n) of the solution) is to use a $21.25-\mathrm{in}$. bundle containing 172 tubes. Determine the suitability of this configuration.
(10.30) In Example 10.4 one of the suggested design modifications was to increase the tube length. Use TASC or Xist to implement this modification and obtain a final design for the reboiler.
(10.31) Treating the vapor and liquid phases separately, show that the term $G_{t}^{2} \gamma / \rho_{L}$ in Equation (10.11) represents the difference in total momentum flux (mass flow rate $\times$ velocity/cross sectional area) across the boiling zone in a vertical thermosyphon reboiler tube.

This page intentionally left blank

## 11

## CONDENSERS

Contents
11.1 Introduction ..... 540
11.2 Types of Condensers ..... 540
11.3 Condensation on a Vertical Surface: Nusselt Theory ..... 545
11.4 Condensation on Horizontal Tubes ..... 549
11.5 Modifications of Nusselt Theory ..... 552
11.6 Condensation Inside Horizontal Tubes ..... 562
11.7 Condensation on Finned Tubes ..... 568
11.8 Pressure Drop ..... 569
11.9 Mean Temperature Difference ..... 571
11.10 Multi-component Condensation ..... 590
11.11 Computer Software ..... 595

### 11.1 Introduction

Condensers are used in a variety of operations in chemical and petroleum processing, including distillation, refrigeration, and power generation. Virtually, every distillation column employs either a partial or total condenser to liquefy some, or all, of the overhead vapor stream, thereby providing reflux for the column and (often) a liquid product stream. In refrigeration operations, condensers are used to liquefy the high-pressure refrigerant vapor leaving the compressor. Heat exchangers referred to as surface condensers are used to condense the exhaust from steam turbines that generate in-house power for plant operations.

Condensation is the reverse of boiling, and the condensing curve is the same as the boiling curve. Thus, many of the computational difficulties encountered in the analysis of reboilers are present in condensers as well. For wide-boiling mixtures, in particular, the nonlinearity of the condensing curve and the variation of liquid and vapor properties over the condensing range mean that a zone or incremental analysis is required for rigorous calculations. Mass-transfer effects may also be significant in the condensation of mixtures, as they are in nucleate boiling of mixtures.

On the other hand, condensing and boiling differ in important respects. In particular, condensation is more amenable to fundamental analysis, and useful heat-transfer correlations can be derived from first principles.

### 11.2 Types of Condensers

Most condensers used in the chemical process industries are shell-and-tube exchangers or aircooled exchangers. In the latter, the condensing vapor flows inside a bank of finned tubes and ambient air blown across the tubes by fans serves as the coolant. Other types of equipment, such as double-pipe exchangers, plate-and-frame exchangers, and direct contact condensers are less frequently used. In direct contact condensing, the coolant is sprayed directly into the condensing vapor. This method is sometimes used for intermediate heat removal from distillation and absorption columns by means of pumparounds. While direct contacting provides a high rate of heat transfer with low-pressure drop, it is obviously limited to applications in which mixing of coolant and condensate is permissible.

Surface condensers are tubular exchangers, but their construction differs somewhat from shell-and-tube equipment used to condense process vapors. They are most often designed for vacuum operation on the shell (steam) side, and hence must handle a large volumetric flow rate of vapor with very low-pressure drop. Smaller units may have circular cross-flow shells similar to X-shells, but larger units usually employ a box-type shell.

In the remainder of this chapter, consideration is restricted to shell-and-tube condensers used for condensation of process vapors. These units are classified according to orientation (horizontal versus vertical) and placement of condensing vapor (shell side versus tube side).

### 11.2.1 Horizontal shell-side condenser

Most large condensers in the process industries are oriented horizontally in order to minimize the cost of support structures and facilitate maintenance operations. The condensing vapor is often an organic compound or mixture and the coolant is most often water, a combination that favors the use of finned tubes. Therefore, the condensing vapor is most frequently placed in the shell (the finned side) and the cooling water, which is usually more prone to fouling, flows in the tubes.

The baffled E-shell condenser (Figure 11.1) is widely used and the least expensive type of horizontal condenser. It may have a floating head, as shown, or fixed tubesheets. The baffles are usually cut vertically for side-to-side flow and notched at the bottom to facilitate drainage of the condensate. An extra nozzle at the top of the shell near the rear head is used to vent non-condensable gases. A properly situated vent is required in all condensers to prevent accumulation of non-condensables that would otherwise impair the performance of the unit. Impingement protection is also required since the vapor generally enters the shell at or near its dew point.


Figure 11.1 Horizontal shell-side condenser, type AES (Source: Ref. [1]).


Figure 11.2 Horizontal shell-side condenser with split flow (type J) shell (Source: Ref. [2]).

If shell-side pressure drop is a problem, double-cut segmental baffles, or rod baffles can be used. Alternatively, a J-shell (Figure 11.2) or X-shell (Figure 11.3) can be used. An X-shell provides very low pressure drop and, hence, is often used for vacuum services. Venting can be a problem with these units, however, as the vent must be located on the side of the shell above the level of the condensate.

### 11.2.2 Horizontal tube-side condenser

This configuration, illustrated in Figure 11.4, is sometimes used to condense high-pressure or corrosive vapors. It also occurs in kettle and horizontal thermosyphon reboilers when the heating medium is steam or a condensing process stream. Multiple tube-side passes (usually two) can be used as well as the single pass shown in Figure 11.4. Two-phase flow regimes are an important consideration in design of these units since flow instabilities can cause operational problems [1].

### 11.2.3 Vertical shell-side condenser

This configuration, illustrated in Figure 11.5, is most commonly encountered in vertical thermosyphon reboilers when the heating medium is steam or a condensing process stream. It is not widely used for condensing, per se. Vapor enters at the top of the shell and flows downward


Figure 11.3 Horizontal shell-side condenser with cross flow (type X) shell (Source: Ref. [3]).


Figure 11.4 Horizontal tube-side condenser (Source: Ref. [2]).
along with the condensate, which is removed at the bottom. The vent is placed near the bottom of the shell, but above the condensate level. The tube bundle may be either baffled or unbaffled.

### 11.2.4 Vertical tube-side downflow condenser

This configuration (Figure 11.6) is often used in the chemical industry [4]. It consists of an E-shell with either a floating head or fixed tubesheets. The lower head is over-sized to accommodate the condensate and a vent for non-condensables. The upper tubesheet is also provided with a vent to prevent any non-condensable gas, such as air, that may enter with the coolant from accumulating in the space between the tubesheet and the upper coolant nozzle.

The condensate flows down the tubes in the form of an annular film of liquid, thereby maintaining good contact with both the cooling surface and the remaining vapor. Hence, this configuration tends to promote the condensation of light components from wide-boiling mixtures. Disadvantages are


Figure 11.5 Vertical shell-side condenser (Source: Ref. [2]).


Figure 11.6 Vertical tube-side downflow condenser (Source: Ref. [1]).


Figure 11.7 Reflux condenser (Source: Ref. [1]).
that the coolant, which is often more prone to fouling, is on the shell side, and the use of finned tubes is precluded.

### 11.2.5 Reflux condenser

A reflux condenser, also called a vent condenser or knockback condenser, is a vertical tube-side condenser in which the vapor flows upward, as indicated in Figure 11.7. These units are typically used when relatively small amounts of light components are to be separated from a vapor mixture. The heavier components condense and flow downward along the tube walls, while the light components remain in the vapor phase and exit through the vent in the upper header. In distillation applications they are most often used as internal condensers [4], where the condensate drains back into the top of the distillation column to supply the reflux, or as secondary condensers attached to accumulators (Figure 11.8). These units have excellent venting characteristics, but the vapor velocity must be kept low to prevent excessive entrainment of condensate and the possibility of flooding. The fluid placement (coolant in shell) entails the same disadvantages as the tube-side downflow condenser.


Figure 11.8 A reflux condenser used as a secondary condenser on an accumulator (Source: Ref. [4])


Figure 11.9 Film condensation on a vertical wall.

### 11.3 Condensation on a Vertical Surface: Nusselt Theory

### 11.3.1 Condensation on a plane wall

The basic heat-transfer correlations for film condensation were first derived by Nusselt [5]. Consider the situation depicted in Figure 11.9, in which a pure-component saturated vapor condenses on a vertical wall, forming a thin film of condensate that flows downward due to gravity. The following assumptions are made:
(i) The flow in the condensate film is laminar.
(ii) The temperature profile across the condensate film is linear. This assumption is reasonable for a very thin film.
(iii) The shear stress at the vapor-liquid interface is negligible.
(iv) The fluid velocity in the film is small so that the inertial terms (terms of second degree in velocity) in the Navier-Stokes equations are negligible.
(v) Only latent heat is transferred, i.e., subcooling of the condensate is neglected.
(vi) Fluid properties and the wall temperature, $T_{w}$, are constant.
(vii) The wall is flat (no curvature).
(viii) The system is at steady state.

The heat flux, $\hat{q}_{y}$, at the wall is given by Fourier's law:

$$
\begin{equation*}
\hat{q}_{y}=-\left.k_{L} \frac{d T}{d y}\right|_{y=0} \tag{11.1}
\end{equation*}
$$

It follows from assumption (ii) that the temperature gradient in the condensate film is independent of $y$ and equal to:

$$
\begin{equation*}
\frac{d T}{d y}=\frac{\Delta T}{\Delta y}=\frac{T_{V}-T_{w}}{\delta} \tag{11.2}
\end{equation*}
$$

Therefore,

$$
\begin{equation*}
\hat{q}_{y}=-\frac{k_{L}\left(T_{V}-T_{w}\right)}{\delta} \tag{11.3}
\end{equation*}
$$

Letting $\hat{q}=\left|\hat{q}_{y}\right|$ and introducing the local heat-transfer coefficient, $h_{z}$, Equation (11.3) can be expressed as follows:

$$
\begin{equation*}
\hat{q}=h_{z}\left(T_{V}-T_{W}\right)=\frac{k_{L}\left(T_{V}-T_{w}\right)}{\delta} \tag{11.4}
\end{equation*}
$$

Therefore,

$$
\begin{equation*}
h_{z}=k_{L} / \delta \tag{11.5}
\end{equation*}
$$

Thus, the problem of determining the heat-transfer coefficient is equivalent to computing the film thickness, $\delta$, which is a function of vertical position, $z$. To this end, the heat flux is written in terms of the condensation rate, $\hat{W}$ : per unit area and the latent heat of vaporization, $\lambda$. By assumption (v):

$$
\begin{equation*}
\hat{q}=\hat{W} \lambda \tag{11.6}
\end{equation*}
$$

Combining Equations (11.4) and (11.6) gives:

$$
\begin{equation*}
\hat{W}=\frac{k_{L}\left(T_{V}-T_{w}\right)}{\lambda \delta} \tag{11.7}
\end{equation*}
$$

Next, an equation for the average velocity, $\bar{u}$, of the condensate is needed. The velocity in the film varies from zero at the wall to a maximum at the vapor-liquid interface. The velocity profile can be found by solving the Navier-Stokes equations using assumption (iv) and boundary conditions of zero velocity at the wall $(y=0)$ and zero shear stress at the vapor-liquid interface $(y=\delta)$. This is a standard problem in fluid mechanics, and the solution for the average velocity is [6]:

$$
\begin{equation*}
\bar{u}=\frac{\left(\rho_{L}-\rho_{V}\right) g \delta^{2}}{3 \mu_{L}} \tag{11.8}
\end{equation*}
$$

A condensate mass balance is now made on a differential control volume of length $\Delta z$, as shown in Figure 11.10. The width of the wall is denoted by $w$ and the balance is written for steady-state conditions (assumption (viii)).

$$
\begin{equation*}
\{\text { rate of mass entering }\}=\{\text { rate of mass leaving }\} \tag{11.9}
\end{equation*}
$$



Figure 11.10 Control volume for condensate mass balance.

$$
\begin{gather*}
\left(\rho_{L} \bar{u} \delta w\right)_{z}^{\prime}+\hat{W} w \Delta z=\left(\rho_{L} \bar{u} \delta w\right)^{\prime}{ }_{z+\Delta z}  \tag{11.10}\\
\frac{\left(\rho_{L} \bar{u} \delta\right)^{\prime}{ }_{z+\Delta z}-\left(\rho_{L} \bar{u} \delta\right)_{z}^{\prime}}{\Delta z}=\hat{W} \tag{11.11}
\end{gather*}
$$

Taking the limit as $\Delta z \rightarrow 0$ gives:

$$
\begin{equation*}
\frac{d}{d z}\left(\rho_{L} \bar{u} \delta\right)=\hat{W} \tag{11.12}
\end{equation*}
$$

Substituting for $\bar{u}$ and $\hat{W}$ using Equations (11.7) and (11.8) yields:

$$
\begin{equation*}
\frac{d}{d z}\left[\frac{\rho_{L}\left(\rho_{L}-\rho_{V}\right) g \delta^{3}}{3 \mu_{L}}\right]=\frac{k_{L}\left(T_{V}-T_{w}\right)}{\lambda \delta} \tag{11.13}
\end{equation*}
$$

Since $\rho_{L}, \rho_{V}$, and $\mu_{L}$ are constant by assumption (iv), they can be taken outside the derivative. Differentiating $\delta^{3}$ then gives:

$$
\begin{gather*}
{\left[\frac{\rho_{L}\left(\rho_{L}-\rho_{V}\right) g}{3 \mu_{L}}\right] \times 3 \delta^{2} \frac{d \delta}{d z}=\frac{k_{L}\left(T_{V}-T_{w}\right)}{\lambda \delta}}  \tag{11.14}\\
\delta^{3} \frac{d \delta}{d z}=\frac{\mu_{L} k_{L}\left(T_{V}-T_{w}\right)}{\rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda} \tag{11.15}
\end{gather*}
$$

Now all the terms on the right side of Equation (11.15) are constant. Hence, separating the variables and integrating gives:

$$
\begin{equation*}
\frac{\delta^{4}}{4}=\left[\frac{\mu_{L} k_{L}\left(T_{V}-T_{w}\right)}{\rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}\right] z+\mathrm{constant} \tag{11.16}
\end{equation*}
$$

Applying the boundary condition $\delta=0$ at $z=0$, the constant of integration is zero and the equation for the film thickness becomes:

$$
\begin{equation*}
\delta=\left[\frac{4 \mu_{L} k_{L}\left(T_{V}-T_{w}\right) z}{\rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}\right]^{1 / 4} \tag{11.17}
\end{equation*}
$$

Substituting the above expression for the film thickness into Equation (11.5) gives the desired result for the local heat-transfer coefficient:

$$
\begin{equation*}
h_{z}=\frac{k}{\delta}=\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{4 \mu_{L}\left(T_{V}-T_{w}\right)}\right]^{1 / 4} z^{-1 / 4} \tag{11.18}
\end{equation*}
$$

Notice that the heat-transfer coefficient decreases with distance down the wall because the thermal resistance is proportional to the film thickness, which increases with distance due to condensate accumulation.

The average heat-transfer coefficient, $h$, for the condensate film can now be obtained by integrating the local coefficient over the length, $L$, of the wall:

$$
\begin{align*}
h & =\frac{1}{L} \int_{0}^{L} h_{z} d z \\
& =\frac{1}{L}\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{4 \mu_{L}\left(T_{V}-T_{w}\right)}\right]^{1 / 4} \int_{0}^{L} z^{-1 / 4} d z \\
& =\frac{1}{L}\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{4 \mu_{L}\left(T_{V}-T_{w}\right)}\right]^{1 / 4}(4 / 3) L^{3 / 4} \\
h & =0.943\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{\mu_{L}\left(T_{V}-T_{w}\right) L}\right]^{1 / 4} \tag{11.19}
\end{align*}
$$

The total rate of heat transfer across the condensate film is given by :

$$
\begin{equation*}
q=h w L\left(T_{V}-T_{w}\right) \tag{11.20}
\end{equation*}
$$

Equation (11.19) can be reformulated in terms of the condensation rate rather than the temperature difference across the film. This alternate formulation is often more convenient for computational purposes. Since the rate of heat transfer is $\lambda W$, it follows from Equation (11.20) that

$$
\begin{equation*}
L\left(T_{V}-T_{w}\right)=\frac{q}{h w}=\frac{\lambda W}{h w} \tag{11.21}
\end{equation*}
$$

Substituting this result for $L\left(T_{V}-T_{w}\right)$ in Equation (11.19) gives:

$$
\begin{equation*}
h=0.943\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g h w}{\mu_{L} W}\right]^{1 / 4} \tag{11.22}
\end{equation*}
$$

A Reynolds number can be introduced at this point as follows:

$$
\begin{equation*}
R e=\frac{D_{e} G}{\mu_{L}}=\frac{4 W}{w \mu_{L}}=\frac{4 \Gamma}{\mu_{L}} \tag{11.23}
\end{equation*}
$$

where

$$
\begin{align*}
D_{e} & =\frac{4 \times \text { Flow Area }}{\text { Wetted Perimeter }}=\frac{4 A_{f}}{w}  \tag{11.24}\\
G & =W / A_{f} \\
A_{f} & =\text { flow area for condensate } \\
\Gamma & =W / w=\text { condensation rate per unit width of surface }
\end{align*}
$$

In terms of $R e$, Equation (11.22) becomes:

$$
\begin{equation*}
h=0.943\left[\frac{4 k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g h}{\mu_{L}^{2} R e}\right]^{1 / 4} \tag{11.25}
\end{equation*}
$$

Solving for $h$ yields:

$$
\begin{equation*}
h=1.47\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g}{\mu_{L}^{2} R e}\right]^{1 / 3} \tag{11.26}
\end{equation*}
$$

### 11.3.2 Condensation on vertical tubes

For tube diameters of practical interest, the effect of wall curvature on the condensate film thickness is negligible. Hence, Equation (11.19) can be used for condensation on either the internal or external surfaces of vertical heat-exchanger tubes. The alternate form, Equation (11.26) is also applicable with the appropriate modification in equivalent diameter. For a bank of $n_{t}$ tubes, the wetted perimeter is $n_{t} \pi D$, where $D$ is either the inner- or outer-tube diameter, depending on whether condensation occurs inside or outside the tubes. Hence, Equations (11.23) and (11.24) are replaced by:

$$
\begin{align*}
D_{e} & =\frac{4 A_{f}}{n_{t} \pi D}  \tag{11.27}\\
R e & =\frac{D_{e} G}{\mu_{L}}=\frac{4 W}{n_{t} \pi D \mu_{L}}=\frac{4 \Gamma}{\mu_{L}} \tag{11.28}
\end{align*}
$$

where now

$$
\begin{equation*}
\Gamma=\frac{W}{n_{t} \pi D} \tag{11.29}
\end{equation*}
$$

### 11.4 Condensation on Horizontal Tubes

The Nusselt analysis for condensation on the external surface of a horizontal tube is similar to that for a vertical surface. The result corresponding to Equation (11.19) is:

$$
\begin{equation*}
h=0.728\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{\mu_{L}\left(T_{V}-T_{w}\right) D_{o}}\right]^{1 / 4} \tag{11.30}
\end{equation*}
$$

The coefficient in this equation is often given as 0.725 , which Nusselt [5] obtained by numerical integration over the tube periphery. The more accurate value of 0.728 was obtained later by performing the integration analytically [7], but for practical purposes the difference is insignificant.

The alternate form corresponding to Equation (11.26) is:

$$
\begin{equation*}
h=1.52\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g}{\mu_{L}^{2} R e}\right]^{1 / 3} \tag{11.31}
\end{equation*}
$$

where

$$
\begin{align*}
R e & =\frac{4 \Gamma}{\mu_{L}} \\
\Gamma & =\frac{W}{n_{t} L}  \tag{11.32}\\
n_{t} & =\text { number of tubes } \\
L & =\text { tube length }
\end{align*}
$$

Equations (11.30) and (11.31) apply to a single tube or a single row of tubes. When tubes are stacked vertically, condensate drainage from tubes above causes an increase in the loading and film thickness on the lower tube rows. Nusselt [5] analyzed the situation for $N_{r}$ tube rows stacked vertically by assuming that condensate flows downward in a continuous uniform sheet from tube to tube, and that the film remains laminar on all tubes. He found that the average heat-transfer coefficient, $h_{N r}$, for the array of $N_{r}$ tube rows is:

$$
\begin{equation*}
h_{N r}=h_{1} N_{r}^{-1 / 4} \tag{11.33}
\end{equation*}
$$

Here, $h_{1}$ is the heat-transfer coefficient for a single tube row calculated from Equation (11.30) or (11.31). In reality, condensate tends to drain from tubes in droplets and rivulets that disturb the film on the tubes below and promote turbulence. As a result, Equation (11.33) generally underestimates the heat-transfer coefficient. Based on experience with industrial condensers, Kern [8,9] proposed the following relationship:

$$
\begin{equation*}
h_{N r}=h_{1} N_{r}^{-1 / 6} \tag{11.34}
\end{equation*}
$$

Butterworth [10] showed that this equation agrees well with experimental data for water and a refrigerant condensing on a tube bank with $N_{r}=20$.

The circular tube bundles used in shell-and-tube condensers consist of a number of vertical stacks of tubes of different heights. For this situation, Kern [8,9] proposed calculating the average heattransfer coefficient using Equation (11.31) with a modified condensate loading term, $\Gamma^{*}$, to account for the effects of condensate drainage. The result is:

$$
\begin{equation*}
h=1.52\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g}{4 \mu_{L} \Gamma^{*}}\right]^{1 / 3} \tag{11.35}
\end{equation*}
$$

where

$$
\begin{equation*}
\Gamma^{*}=\frac{W}{L n_{t}^{2 / 3}} \tag{11.36}
\end{equation*}
$$

In effect, the number of tubes is replaced by $n_{t}^{2 / 3}$ in Nusselt's equation. For a single stack of $N_{r}=n_{t}$ tubes, Equations (11.35) and (11.36) are equivalent to Equation (11.34). To see this, substitute $N_{r}^{2 / 3}$ for $N_{r}$ in the Nusselt relationship, Equation (11.33).

## Example 11.1

A stream consisting of $5000 \mathrm{lb} / \mathrm{h}$ of saturated n-propyl alcohol (1-propanol) vapor at $207^{\circ} \mathrm{F}$ and approximately atmospheric pressure will be condensed using a tube bundle containing 3769 tubes arranged for a single pass. The tubes are 0.75 in . OD, 14 BWG , with a length of 12 ft . Physical properties of the condensate are as follows:

$$
\begin{aligned}
k_{L} & =0.095 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F} \\
\rho_{L} & =49 \mathrm{bm} / \mathrm{ft}^{3} \\
\mu_{L} & =0.5 \mathrm{cp}
\end{aligned}
$$

Estimate the condensing-side heat-transfer coefficient for the following cases:
(a) The tube bundle is vertical and condensation occurs inside the tubes.
(b) The tube bundle is horizontal and condensation occurs outside the tubes.

## Solution

(a) Since the tubes are vertical and the condensation rate is given, Equation (11.26) will be used to calculate $h$. The condensate loading per tube is first calculated using Equation (11.29) with $D=D_{i}=0.584$ in. from Table B.1.

$$
\Gamma=\frac{W}{n_{t} \pi D}=\frac{5000}{3769 \pi(0.584 / 12)}=8.677 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~h}
$$

The Reynolds number is given by Equation (11.28):

$$
R e=\frac{4 \Gamma}{\mu_{L}}=\frac{4 \times 8.677}{0.5 \times 2.419}=28.70
$$

In Equation (11.26), the vapor density is neglected in comparison with the liquid density since the pressure is low ( 1 atm ). Thus,

$$
\begin{aligned}
& h=1.47\left[\frac{k_{L}^{3} \rho_{L}^{2} g}{\mu_{L}^{2} R e}\right]^{1 / 3}=1.47\left[\frac{(0.095)^{3}(49)^{2}\left(4.17 \times 10^{8}\right)}{(0.5 \times 2.419)^{2}(28.70)}\right]^{1 / 3} \\
& h=402 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(b) The calculation for the horizontal tube bundle utilizes Equations (11.35) and (11.36). The vapor density is again neglected.

$$
\begin{aligned}
\Gamma^{*} & =\frac{W}{L n_{t}^{2 / 3}}=\frac{5000}{12(3769)^{2 / 3}}=1.720 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~h} \\
h & =1.52\left[\frac{k_{L}^{3} \rho_{L}^{2} g}{4 \mu_{L} \Gamma^{*}}\right]^{1 / 3}=1.52\left[\frac{(0.095)^{3}(49)^{2}\left(4.17 \times 10^{8}\right)}{4(0.5 \times 2.419)(1.720)}\right]^{1 / 3} \\
h & =713 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

The horizontal configuration provides a substantial advantage under these conditions, which were chosen to ensure laminar flow of condensate in the vertical tube bundle. While the horizontal
configuration is generally advantageous in this respect, in practice other factors such as interfacial shear and turbulence in the vertical condensate film may act to mitigate the effect of condenser orientation.

### 11.5 Modifications of Nusselt Theory

The basic Nusselt theory of film condensation has been modified by a number of workers, including Nusselt himself, in order to relax some of the assumptions made in the basic theory. These modifications are considered in the following subsections.

### 11.5.1 Variable fluid properties

The fluid properties, $k_{L}, \rho_{L}$, and $\mu_{L}$, are functions of temperature, which varies across the condensate film. Of the three properties, viscosity is the most temperature sensitive. In practice, the condensate properties are evaluated at a weighted average film temperature, $T_{f}$, defined by:

$$
\begin{equation*}
T_{f}=\beta T_{w}+(1-\beta) T_{s a t} \tag{11.37}
\end{equation*}
$$

The value of the weight factor, $\beta$, recommended in the literature ranges from 0.5 to 0.75 . The latter value will be used herein, i.e.,

$$
\begin{equation*}
T_{f}=0.75 T_{w}+0.25 T_{s a t} \tag{11.38}
\end{equation*}
$$

### 11.5.2 Inclined surfaces

For condensation on an inclined surface making an angle, $\theta$, with the vertical, where $0^{\circ} \leq \theta \leq 45^{\circ}$, Equations (11.22) and (11.26) can be used by replacing $g$ with $g \cos \theta$. For condensation outside an inclined tube making an angle, $\theta^{\prime}$, with the horizontal, Equations (11.30) and (11.31) can be used if $g$ is replaced with $g \cos \theta^{\prime}$, provided $L / D>1.8 \tan \theta^{\prime}$ [10].

### 11.5.3 Turbulence in condensate film

For condensation on vertical surfaces having lengths typical of industrial heat-transfer equipment, the flow in the condensate film may become turbulent at some distance from the top of the surface. The portion of the surface experiencing turbulent conditions becomes significant at film Reynolds numbers exceeding about 1600. However, ripples and waves that form and propagate along the surface of the condensate film begin to affect the heat transfer at a much lower Reynolds number of about 30 . Thus, the following three-flow regimes are recognized:

- Laminar wave free $(R e \leq 30)$
- Laminar wavy $(30<R e \leq 1600)$
- Turbulent ( $R e>1600$ )

The Nusselt relations, Equations (11.19) and (11.26), are valid for the laminar regime ( $R e \leq 30$ ). For the laminar wavy regime, the average heat-transfer coefficient for the entire film, including the laminar wave-free portion, can be obtained from the following semi-empirical correlation [10]:

$$
\begin{equation*}
h=\frac{\operatorname{Re}\left[k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g / \mu_{L}^{2}\right]^{1 / 3}}{1.08 R e^{1.22}-5.2} \tag{11.39}
\end{equation*}
$$

A similar correlation is available [10] for the turbulent regime ( $R e>1600$ ):

$$
\begin{equation*}
h=\frac{\operatorname{Re}\left[k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g / \mu_{L}^{2}\right]^{1 / 3}}{8750+58 \operatorname{Pr}_{L}^{-0.5}\left(\operatorname{Re}^{0.75}-253\right)} \tag{11.40}
\end{equation*}
$$

In this equation, $h$ is again an average value for the entire film, including the laminar portions, and $P r_{L}$ is the Prandtl number for the condensate. Equation (11.40) is valid for $P r_{L} \leq 10$, which includes most cases for which a turbulent condensate film is likely to occur. For higher Prandtl numbers, it will tend to overestimate $h$. Therefore, if $\operatorname{Pr}_{L}>10$, Equation (11.40) should be used with $\operatorname{Pr}_{L}=10$ [10].

More complex correlations for the wavy and turbulent regimes have been developed (see, e.g., Ref. [11]). However, the correlations given above are easy to use and are sufficiently accurate for most purposes.
For condensation on horizontal tubes, the Nusselt relations, Equations (11.30) and (11.31), are valid for Reynolds numbers up to 3200, beyond which the condensate film becomes turbulent. This value is unlikely to be exceeded for a single tube or tube row, but higher Reynolds numbers may occur on tubes in a vertical stack due to cumulative condensate loading. Nevertheless, the usual practice is to use Equation (11.35) for horizontal tube bundles regardless of the Reynolds number.

### 11.5.4 Superheated vapor

When the vapor is superheated, condensation can still take place if the wall temperature is below the saturation temperature. In this case, heat is transferred from the bulk vapor at $T_{V}$ to the vaporliquid interface at $T_{s a t}$, and then through the condensate film to the wall at $T_{w}$. The total amount of heat transferred consists of the latent heat of condensation plus the sensible heat to cool the vapor from $T_{V}$ to $T_{s a t}$. Thus,

$$
\begin{equation*}
q=W \lambda+W C_{P, V}\left(T_{V}-T_{s a t}\right)=W \lambda^{\prime} \tag{11.41}
\end{equation*}
$$

where

$$
\begin{equation*}
\lambda^{\prime} \equiv \lambda\left[1+\frac{C_{P, V}\left(T_{V}-T_{s a t}\right)}{\lambda}\right] \tag{11.42}
\end{equation*}
$$

Repeating the Nusselt analysis of Section 11.3 .1 with $\lambda^{\prime}$ replacing $\lambda$ leads to the following expression for the average heat-transfer coefficient:

$$
\begin{equation*}
h=0.943\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda^{\prime}}{\mu_{L}\left(T_{\text {sat }}-T_{w}\right) L}\right]^{1 / 4} \tag{11.43}
\end{equation*}
$$

Comparing this result with Equation (11.19), it follows that:

$$
\begin{equation*}
\frac{h}{h_{N u}}=\left(\lambda^{\prime} / \lambda\right)^{1 / 4}=\left[1+\frac{C_{P, V}\left(T_{V}-T_{s a t}\right)}{\lambda}\right]^{1 / 4} \tag{11.44}
\end{equation*}
$$

where $h_{N u}$ is the heat-transfer coefficient given by the basic Nusselt theory, Equation (11.19). The total rate of heat transfer is given by:

$$
\begin{equation*}
q=h w L\left(T_{s a t}-T_{w}\right) \tag{11.45}
\end{equation*}
$$

Equation (11.44) also holds for condensation on horizontal tubes. Because the sensible heat is usually small compared with the latent heat, the effect of vapor superheat on the heat-transfer coefficient is usually small. Equation (11.44) does not account for the heat-transfer resistance in the vapor phase, which is generally small compared with the resistance of the condensate film.

### 11.5.5 Condensate subcooling

The temperature in the condensate film drops from $T_{s a t}$ at the vapor-liquid interface to $T_{w}$ at the wall. Therefore, the average condensate temperature, $T_{L}$, is less than $T_{s a t}$, and hence the condensate
leaving the surface is subcooled. Accounting for subcooling, the rate of heat transfer is:

$$
\begin{equation*}
q=W \lambda+W C_{P, L}\left(T_{s a t}-T_{L}\right) \tag{11.46}
\end{equation*}
$$

The effect of subcooling on the heat-transfer coefficient was first considered by Nusselt [5], and subsequently by a number of other researchers. Sadisivan and Lienhard [12] used a boundary-layer analysis, which accounted for both subcooling and inertial effects, to derive the following equation:

$$
\begin{equation*}
\frac{h}{h_{N u}}=\left[1+\left(0.683-0.228 \operatorname{Pr}_{L}^{-1}\right) \varepsilon\right]^{1 / 4} \tag{11.47}
\end{equation*}
$$

where

$$
\begin{aligned}
\varepsilon & =\frac{C_{P, L}\left(T_{s a t}-T_{w}\right)}{\lambda} \\
\operatorname{Pr}_{L} & =\frac{C_{P, L} \mu_{L}}{k_{L}}
\end{aligned}
$$

Equation (11.47) is valid for $\operatorname{Pr}_{L}>0.6$, and thus includes virtually all condensates except liquid metals, which have very small Prandtl numbers. It predicts an effect of subcooling that is similar to the effect of vapor superheat, i.e., a (usually) small increase in the heat-transfer coefficient over the value given by the basic Nusselt theory.

Chen [13] also used boundary-layer theory to study the condensation process. He replaced the boundary condition of zero shear stress at the vapor-liquid interface with that of zero vapor velocity far from the interface. His analysis thus included the effect of vapor drag on the condensate as well as subcooling and inertial effects. The following equation closely approximates the boundary-layer solutions for both a vertical plane wall and a single horizontal tube [13]:

$$
\begin{equation*}
\frac{h}{h_{N u}}=\left(\frac{1+0.68 \varepsilon+0.02 \varepsilon^{2} P r_{L}^{-1}}{1+0.85 \varepsilon P r_{L}^{-1}-0.15 \varepsilon^{2} P r_{L}^{-1}}\right)^{1 / 4} \tag{11.48}
\end{equation*}
$$

The range of validity for this equation is as follows:

$$
\begin{aligned}
\varepsilon & \leq 2 \\
\varepsilon & \leq 20 P r_{L} \\
P r_{L} & \geq 1 \quad \text { or } \quad P r_{L} \leq 0.05
\end{aligned}
$$

Most condensates have Prandtl numbers of 1.0 or higher, and for these fluids Equations (11.47) and (11.48) both predict a relatively small effect on the heat-transfer coefficient (less than $14 \%$ for $\varepsilon \leq 1.0$ ). In contrast to Equation (11.47), however, Equation (11.48) predicts that $h$ is slightly less than $h_{N u}$ for Prandtl numbers near unity.

Most liquid metals have Prandtl numbers below 0.05, and for these fluids Equation (11.48) predicts that $h$ can be much less than $h_{N u}$. This prediction is in qualitative agreement with experimental data [13].

## Example 11.2

A stream consisting of $5000 \mathrm{lb} / \mathrm{h}$ of saturated n-propyl alcohol (1-propanol) vapor at $207^{\circ} \mathrm{F}$ will be condensed using a tube bundle containing 109 tubes arranged for one pass. The tubes are 0.75 in .

OD, 14 BWG, with a length of 12 ft . Estimate the condensing-side heat-transfer coefficient for the following cases:
(a) The tube bundle is vertical and condensation occurs inside the tubes.
(b) The tube bundle is horizontal and condensation occurs outside the tubes.

## Solution

(a) The physical properties given in Example 11.1 will be used as a first approximation. Values of $k_{L}$ and $\rho_{L}$ will be assumed constant, but the variation of $\mu_{L}$ with temperature will be accounted for. As in Example 11.1, the density of the vapor will be neglected compared with that of the liquid. The first step is to compute the Reynolds number:

$$
\begin{aligned}
\Gamma & =\frac{W}{n_{t} \pi D_{i}}=\frac{5000}{109 \pi(0.584 / 12)}=300.0 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~h} \\
R e & =\frac{4 \Gamma}{\mu_{L}}=\frac{4 \times 300.0}{0.5 \times 2.419}=992.1
\end{aligned}
$$

The flow regime is wavy laminar, so Equation (11.39) is used to calculate the heat-transfer coefficient:

$$
\begin{aligned}
h & =\frac{\operatorname{Re}\left[k_{L}^{3} \rho_{L}^{2} g / \mu_{L}^{2}\right]^{1 / 3}}{1.08 R e^{1.22}-5.2} \\
& =\frac{992.1\left[(0.095)^{3}(49)^{2}\left(4.17 \times 10^{8}\right) /(0.5 \times 2.419)^{2}\right]^{1 / 3}}{1.08(992.1)^{1.22}-5.2} \\
h & =170 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Next, the temperature drop across the condensate film is calculated. From Table A.17, the latent heat of vaporization is:

$$
\lambda=164.36 \mathrm{cal} / \mathrm{g} \times 1.8 \frac{\mathrm{Btu} / \mathrm{lbm}}{\mathrm{cal} / \mathrm{g}}=295.85 \mathrm{Btu} / \mathrm{lbm}
$$

Neglecting the sensible heat of subcooling, the duty is:

$$
\begin{aligned}
q & =W \lambda=5000 \times 295.85=1,479,250 \mathrm{Btu} / \mathrm{lbm} \\
q & =h n_{t} \pi D_{i} L \Delta T \\
\Delta T & =\frac{q}{h n_{t} \pi D_{i} L}=\frac{1,479,250}{170 \times 109 \pi(0.584 / 12) \times 12}=43.5^{\circ} \mathrm{F}
\end{aligned}
$$

Therefore, the wall temperature is:

$$
T_{w}=207-43.5=163.5^{\circ} \mathrm{F}
$$

The weighted average film temperature is calculated from Equation (11.38):

$$
\begin{aligned}
& T_{f}=0.75 T_{w}+0.25 T_{\text {sat }}=0.75 \times 163.5+0.25 \times 207 \\
& T_{f}=174.4^{\circ} \mathrm{F}
\end{aligned}
$$

From Figure A.1, the condensate viscosity at this temperature is 0.7 cp . A second iteration is made using this value of $\mu_{L}$ :

$$
\begin{aligned}
R e & =\frac{4 \times 300.0}{0.7 \times 2.419}=708.7 \Rightarrow \text { wavy laminar flow } \\
h & =\frac{708.7\left[(0.095)^{3}(49)^{2}\left(4.17 \times 10^{8}\right) /(0.7 \times 2.419)^{2}\right]^{1 / 3}}{1.08(708.7)^{1.22}-5.2} \cong 146 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\Delta T & =\frac{1,479,250}{146 \times 109 \pi(0.584 / 12) \times 12}=50.7^{\circ} \mathrm{F} \\
T_{w} & =207-50.7=156.3^{\circ} \mathrm{F} \\
T_{f} & =0.75 \times 156.3+0.25 \times 207 \cong 169^{\circ} \mathrm{F}
\end{aligned}
$$

At this value of $T_{f}$, the condensate viscosity is 0.73 cp . Results of the third iteration are given below:

$$
\begin{aligned}
R e & =679.6 \\
h & \cong 144 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\Delta T & =51.4^{\circ} \mathrm{F} \\
T_{w} & =155.6^{\circ} \mathrm{F} \\
T_{f} & =168.5^{\circ} \mathrm{F}
\end{aligned}
$$

Since the new value of $T_{f}$ is close to the previous value, no further iterations are required.
To check the effect of subcooling on $h$, the condensate Prandtl number is computed next. The heat capacity of liquid n-propyl alcohol at $T_{f} \cong 169^{\circ} \mathrm{F}$ is found from Figure A.3: $C_{P, L}=0.72 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$. Thus,

$$
\begin{aligned}
\operatorname{Pr}_{L} & =\frac{C_{P, L} \mu_{L}}{k_{L}}=\frac{0.72(0.73 \times 2.419)}{0.095}=13.4 \\
\varepsilon & =\frac{C_{P, L}\left(T_{s a t}-T_{w}\right)}{\lambda}=\frac{0.72(207-155.6)}{295.85}=0.125
\end{aligned}
$$

Using Equation (11.47) we obtain:

$$
\begin{aligned}
h / h_{N u} & =\left[1+\left(0.683-0.228 \operatorname{Pr}_{L}^{-1}\right) \varepsilon\right]^{1 / 4} \\
& =[1+(0.683-0.228 / 13.4) \times 0.125]^{1 / 4} \\
h / h_{N u} & =1.020
\end{aligned}
$$

For comparison, the calculation is also done using Equation (11.48):

$$
\begin{aligned}
h / h_{N u} & =\left(\frac{1+0.68 \varepsilon+0.02 \varepsilon^{2} \operatorname{Pr}_{L}^{-1}}{1+0.85 \varepsilon \operatorname{Pr}_{L}^{-1}-0.15 \varepsilon^{2} \operatorname{Pr}_{L}^{-1}}\right)^{1 / 4} \\
& =\left\{\frac{1+0.68 \times 0.125+0.02(0.125)^{2} / 13.4}{1+0.85 \times 0.125 / 13.4-0.15(0.125)^{2} / 13.4}\right\}^{1 / 4} \\
h / h_{N u} & =1.019
\end{aligned}
$$

Thus, both methods predict an increase in $h$ of about $2 \%$ due to condensate subcooling. Including this effect gives $h \cong 147 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. This correction is not large enough to warrant further iteration.
(b) The physical properties from Example 11.1 are again used to initialize the calculations and the vapor density is neglected. The heat-transfer coefficient is computed using Equations (11.35) and (11.36):

$$
\begin{aligned}
\Gamma^{*} & =\frac{W}{L n_{t}^{2 / 3}}=\frac{5000}{12(109)^{2 / 3}}=18.26 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~h} \\
h & =1.52\left[\frac{k_{L}^{3} \rho_{L}^{2} g}{4 \mu_{L} \Gamma^{*}}\right]^{1 / 3}=1.52\left[\frac{(0.095)^{3}(49)^{2}\left(4.17 \times 10^{8}\right)}{4(0.5 \times 2.419) \times 18.26}\right]^{1 / 3} \\
h & =324 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Next, the temperature difference across the condensate film is calculated:

$$
\begin{aligned}
\Delta T & =T_{s a t}-T_{w}=\frac{q}{h n_{t} \pi D_{o} L}=\frac{1,479,250}{324 \times 109 \pi(0.75 / 12) \times 12} \\
\Delta T & =17.8^{\circ} \mathrm{F} \\
T_{w} & =207-17.8=189.2^{\circ} \mathrm{F} \\
T_{f} & =0.75 T_{w}+0.25 T_{\text {sat }}=0.75 \times 189.2+0.25 \times 207=193.7^{\circ} \mathrm{F}
\end{aligned}
$$

From Figure A.1, the condensate viscosity at $T_{f}$ is 0.58 cp . The above calculations are repeated using this value of viscosity.

$$
\begin{aligned}
h & =1.52\left[\frac{(0.095)^{3}(49)^{2}\left(4.17 \times 10^{8}\right)}{4(0.58 \times 2.419) \times 18.26}\right]^{1 / 3} \cong 309 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \\
\Delta T & =\frac{1,479,250}{309 \times 109 \pi(0.75 / 12) \times 12}=18.6^{\circ} \mathrm{F} \\
T_{w} & =207-18.6=188.4^{\circ} \mathrm{F} \\
T_{f} & =0.75 \times 188.4+0.25 \times 207=193^{\circ} \mathrm{F}
\end{aligned}
$$

Since the new value of $T_{f}$ is close to the previous value, the calculations have converged.
Using Equation (11.47) to estimate the effect of condensate subcooling for this case yields $h / h_{N u}=1.0076$. Including this minor correction gives $h=311 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Clearly, the effect of condensate subcooling is negligible in this case.

### 11.5.6 Interfacial shear

In the basic Nusselt theory interfacial shear is neglected and the condensate is assumed to drain from the surface under the influence of gravity alone. By contrast, at very high vapor velocities the effect of interfacial shear is predominant and gravitational effects can be neglected. Methods for computing the heat-transfer coefficient under the latter conditions are presented in the following subsections. At intermediate velocities, the effects of both gravity and interfacial shear may be
significant. In this situation, the following formula is often used to represent the combined effects of gravity and interfacial shear:

$$
\begin{equation*}
h=\left(h_{s h}^{2}+h_{g r}^{2}\right)^{1 / 2} \tag{11.49}
\end{equation*}
$$

In this equation $h_{s h}$ and $h_{g r}$ are the heat-transfer coefficients for shear-controlled and gravitycontrolled film condensation, respectively. A more conservative approach that may be preferable for design purposes is to use either $h_{g r}$ or $h_{s h}$, whichever is larger.

## Condensation in vertical tubes with vapor upflow

Low vapor velocities are generally employed with this configuration in order to prevent flooding (the condition wherein condensate is forced out the top of the tubes rather than draining freely from the bottom). As a result, interfacial shear effects can usually be neglected in this type of condenser.

## Condensation in vertical tubes with vapor downflow

In this configuration the interfacial shear stress tends to accelerate the flow of condensate down the tube wall and decrease the critical Reynolds number for the onset of turbulence. As a result, the heat-transfer coefficient tends to be enhanced.

For shear-controlled condensation, the correlation of Boyko and Kruzhilin [14] provides a simple method to estimate the average heat-transfer coefficient. The local coefficient is given by the following correlation:

$$
\begin{equation*}
h=h_{L O}\left[1+x\left(\rho_{L}-\rho_{V}\right) / \rho_{V}\right]^{0.5} \tag{11.50}
\end{equation*}
$$

where
$x=$ vapor weight fraction
$h_{L O}=$ heat-transfer coefficient for total flow as liquid
The value of $h_{L O}$ can be computed using a correlation for single-phase heat transfer, e.g., the Seider-Tate correlation. Turbulent flow is assumed to exist at all positions along the length of the tube, including the region in a total condenser where condensation is complete and the flow is all liquid. The average coefficient for the entire tube is the arithmetic average of the coefficients computed at inlet and outlet conditions [14]. This average coefficient can be equated with $h_{\text {sh }}$ in Equation (11.49).

The basis for the Boyko-Kruzhilin method is the analogy between heat transfer and fluid flow (momentum transfer). Many similar correlations have been published, some of which are discussed in Section 11.6.

## Condensation outside horizontal tubes

In horizontal shell-side condensers employing a J- or X-shell, the vapor flow is primarily perpendicular to the tubes, as it is between baffle tips of units employing an E-shell. At high vapor velocities, this cross flow causes condensate to be blown off the tubes, resulting in a very complex flow pattern in the tube bundle [2]. Despite this complexity, McNaught [15] developed the following simple correlation for shear-controlled condensation in tube bundles:

$$
\begin{equation*}
h / h_{L}=1.26 X_{t t}^{-0.78} \tag{11.51}
\end{equation*}
$$

where
$X_{t t}=$ Lockhart-Martinelli parameter, Equation (9.37)
$h_{L}=$ heat-transfer coefficient for the liquid phase flowing alone through the bundle
The value of $h_{L}$ can be computed by any of the methods discussed in Chapters 5,6 , and 7 . Since $X_{t t}$ depends on vapor quality, Equation (11.51) provides a local heat-transfer coefficient suitable for
use with a zone analysis. It can also be used to assess the significance of interfacial shear at any position in a condenser where the quality is known or specified.

Equation (11.51) is based on experimental data for condensation of steam in downflow over tube bundles laid out on square and triangular patterns. In conjunction with Equation (11.49), it correlated $90 \%$ of the data to within $\pm 25 \%$ [15].

## Example 11.3

Evaluate the significance of interfacial shear for the conditions of Example 11.2 and the following specifications:
(a) For the vertical condenser, the vapor flows downward through the tubes.
(b) For the horizontal shell-side condenser, the unit consists of an E-shell with an ID of 12 in . The condenser has $20 \%$ cut segmental baffles with a spacing of 4.8 in ., and a triangular tube layout with a pitch of 1.0 in .

## Solution

(a) The following data are obtained from Example 11.2, part (a):

$$
\begin{array}{rlrl}
T_{V} & =T_{\text {sat }}=207^{\circ} \mathrm{F} & \mu_{L} & =0.73 \mathrm{cp} \\
T_{f} & \cong 169^{\circ} \mathrm{F} & P r_{L} & =13.4 \\
T_{w} & \cong 156^{\circ} \mathrm{F} & D_{i} & =0.584 \mathrm{in} . \\
P_{s a t} & \cong 1 \mathrm{~atm}=14.7 \mathrm{psia} & L & =12 \mathrm{ft} \\
k_{L} & =0.095 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F} & n_{t} & =109 \\
\rho_{L} & =49 \mathrm{lbm} / \mathrm{ft}^{3} & &
\end{array}
$$

Additional data needed for the calculations are:
Molecular weight of propyl alcohol $=60$

$$
\begin{aligned}
\mu_{w} & =0.85 \mathrm{cp} \text { at } T_{w}=156^{\circ} \mathrm{F} \quad \text { from Figure A. } 1 \\
\rho_{V} & =\frac{P M}{\widetilde{R} T}=\frac{14.7 \times 60}{10.73(207+460)}=0.123 \mathrm{lbm} / \mathrm{ft}^{3}
\end{aligned}
$$

The shear-controlled heat-transfer coefficient is given by Equation (11.50), which involves the coefficient, $h_{L O}$, for the total flow ( $5000 \mathrm{lb} / \mathrm{h}$ ) as liquid. The Reynolds number is calculated first:

$$
R e_{L O}=\frac{4 \dot{m} / n_{t}}{\pi D_{i} \mu_{L}}=\frac{4 \times 5000 / 109}{\pi(0.584 / 12) \times 0.73 \times 2.419}=679.6
$$

Since the total condensate flow is laminar, the Boyko-Kruzhilin correlation is not strictly applicable. However, a conservative estimate for the shear-controlled coefficient can be obtained by using Equation (11.50) along with a laminar-flow correlation to calculate $h_{L O}$. (See Problem 11.2 for an alternative approach.) Hence, Equation (2.36) is used as follows:

$$
\begin{aligned}
N u_{L O} & =1.86\left(\operatorname{Re}_{L O} \operatorname{Pr}_{L} D_{i} / L\right)^{1 / 3}\left(\mu_{L} / \mu_{w}\right)^{0.14} \\
& =1.86[679.6 \times 13.4(0.584 / 12) / 12]^{1 / 3}(0.73 / 0.85)^{0.14}
\end{aligned}
$$

$$
\begin{aligned}
N u_{L O} & =6.06 \\
h_{L O} & =6.06 \times k_{L} / D_{i}=6.06 \times 0.095 /(0.584 / 12)=11.8 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

At the condenser inlet, the vapor fraction is $x_{i n}=1.0$. Hence, from Equation (11.50):

$$
\begin{aligned}
h_{\text {in }} & =h_{L O}\left[1+x_{\text {in }}\left(\rho_{L}-\rho_{V}\right) / \rho_{V}\right]^{0.5} \\
& =11.8[1+1.0(49-0.123) / 0.123]^{0.5} \\
h_{\text {in }} & =236 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

At the condenser outlet the vapor fraction is zero, and therefore:

$$
h_{\text {out }}=h_{L O}=11.8 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

The average heat-transfer coefficient for shear-controlled condensation is the arithmetic average of the inlet and outlet values:

$$
h_{\text {sh }}=0.5\left(h_{\text {in }}+h_{\text {out }}\right)=0.5(236+11.8)=124 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot \circ \mathrm{~F}
$$

This result is the same order of magnitude as the average coefficient for gravity-controlled condensation ( $147 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ ) calculated in Example 11.2, part (a). Therefore, both gravity and interfacial shear effects are significant, and Equation (11.49) can be used to estimate the resultant heat-transfer coefficient:

$$
h=\left(h_{s h}^{2}+h_{g r}^{2}\right)^{1 / 2}=\left[(124)^{2}+(147)^{2}\right]^{1 / 2}=192 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot \circ \mathrm{~F}
$$

This value is about $30 \%$ higher than the result based on gravity-controlled condensation alone. Comparison with other methods (see Problems 11.1 and 11.2 for two examples) indicates that the calculated value of $h$ is, in fact, somewhat conservative.
(b) The following data are obtained from Example 11.2, part (b):

$$
T_{f}=193^{\circ} \mathrm{F} \quad T_{w} \cong 188^{\circ} \mathrm{F} \quad \mu_{L}=0.58 \mathrm{cp}
$$

Additional data needed for the calculations are:

$$
\begin{array}{rlrl}
C_{P, L} & =0.75 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} & & \text { from Figure A. } 3 \\
\mu_{V} & =0.0095 \mathrm{cp} & & \text { from Figure A. } 2 \\
\mu_{w} & =0.60 \mathrm{cp} \text { at } T_{w}=188^{\circ} \mathrm{F} & & \text { from Figure A. } 1 \\
P r_{L} & =\frac{C_{P, L} \mu_{L}}{k_{L}}=\frac{0.75 \times 0.58 \times 2.419}{0.095} \cong 11.1
\end{array}
$$

Other data are the same as in part (a).
The shear-controlled heat-transfer coefficient is given by Equation (11.51), which involves the coefficient, $h_{L}$, for the liquid phase flowing alone. The Simplified Delaware method is used here to calculate $h_{L}$. A vapor weight fraction of 0.9 is selected, giving a liquid flow rate of:

$$
\dot{m}_{L}=(1-x) \dot{m}=0.1 \times 5000=500 \mathrm{lbm} / \mathrm{h}
$$

The flow area through the tube bundle is:

$$
a_{s}=\frac{d_{s} C^{\prime} B}{144 P_{T}}=\frac{12 \times 0.25 \times 4.8}{144 \times 1.0}=0.10 \mathrm{ft}^{2}
$$

The mass flux is:

$$
G_{L}=\dot{m}_{L} / a_{s}=500 / 0.10=5000 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

From Figure 3.12, the equivalent diameter is $D_{e}=0.99 / 12=0.0825 \mathrm{ft}$. Thus, the Reynolds number is:

$$
R e_{L}=\frac{D_{e} G_{L}}{\mu_{L}}=\frac{0.0825 \times 5000}{0.58 \times 2.419}=294.0
$$

Next, the Colburn $j$-factor is calculated using Equation (3.21) with $B / d_{s}=4.8 / 12=0.4$.

$$
\begin{aligned}
j_{H} & =0.5\left(1+B / d_{s}\right)\left(0.08 R e_{L}^{0.6821}+0.7 R e_{L}^{0.1772}\right) \\
& =0.5(1+0.4)\left\{0.08(294)^{0.6821}+0.7(294)^{0.1772}\right\} \\
j_{H} & =4.04
\end{aligned}
$$

Equation (3.20) is used to calculate $h_{L}$ :

$$
\begin{aligned}
h_{L} & =j_{H}\left(k_{L} / D_{e}\right) P r_{L}^{1 / 3}\left(\mu_{L} / \mu_{w}\right)^{0.14} \\
& =4.04(0.095 / 0.0825)(11.1)^{1 / 3}(0.58 / 0.60)^{0.14} \\
h_{L} & =10.3 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Next, the Lockhart-Martinelli parameter is computed from Equation (9.37):

$$
\begin{aligned}
X_{t t} & =\left(\frac{1-x}{x}\right)^{0.9}\left(\rho_{V} / \rho_{L}\right)^{0.5}\left(\mu_{L} / \mu_{V}\right)^{0.1} \\
& =\left(\frac{1-0.9}{0.9}\right)^{0.9}(0.123 / 49)^{0.5}(0.58 / 0.0095)^{0.1} \\
X_{t t} & =0.0105
\end{aligned}
$$

Substituting the values of $h_{L}$ and $X_{t t}$ in Equation (11.51) gives the local coefficient for shearcontrolled condensation:

$$
\begin{aligned}
& h_{s h}=1.26 X_{t t}^{-0.78} h_{L}=1.26(0.0105)^{-0.78} \times 10.3 \\
& h_{s h}=454 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

This value is about $44 \%$ higher than the value of $315 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ found for the average coefficient based on gravity-controlled condensation in Example 11.2. Thus, interfacial shear effects are significant at this point in the condenser.

Repeating the above calculations for vapor weight fractions of 0.5 and 0.1 yields the following results:

| $x=0.5$ | $x=0.1$ |
| :--- | :--- |
| $\dot{m}_{L}=2500 \mathrm{lbm} / \mathrm{h}$ | $\dot{m}_{L}=4500 \mathrm{lbm} / \mathrm{h}$ |
| $G_{L}=25,000 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$ | $G_{L}=45,000 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$ |
| $R e_{L}=1470$ | $R e_{L}=2646$ |
| $j_{H}=9.89$ | $j_{H}=14.1$ |
| $h_{L}=25.3 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ | $h_{L}=36.0 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ |
| $X_{t t}=0.076$ | $X_{t t}=0.546$ |
| $h_{\text {sh }}=238 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ | $h_{\text {sh }}=73 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ |

Interfacial shear effects are negligible at $x=0.1$, but they are clearly significant over a large portion of the condensing range.

### 11.6 Condensation Inside Horizontal Tubes

### 11.6.1 Flow regimes

The analysis of condensation in horizontal tubes is complicated by the variety of two-phase flow regimes that can exist in this geometry. The flow pattern typically changes as condensation proceeds due to the increase in the amount of liquid present and the decrease in vapor velocity. Initially, the condensate forms an annular film around the tube periphery while the vapor flows in the core of the tube. Liquid droplets are normally entrained in the vapor due to the high shear forces, with the amount of entrainment decreasing as the vapor velocity falls. This flow regime is referred to as annular or mist-annular, depending on the amount of entrainment. In this regime the condensation is shear controlled.

As condensation proceeds and vapor shear decreases, the condensate begins to accumulate at the bottom of the tube due to gravity, causing an increasing asymmetry in the condensate film. At high flow rates, the flow pattern eventually changes to slug flow, followed by plug flow. In the final stages of condensation, the vapor flows as bubbles that are elongated in the flow direction and entrained in a continuous liquid phase. At lower flow rates, annular flow gradually changes to a stratified regime in which most of the condensate flows along the bottom portion of the tube with vapor above. The condensate finally drains from the tube under gravity. As noted by Butterworth [10], however, if the condensate discharges into a liquid-filled header, it will not drain freely, but will accumulate in the tube and be forced out under pressure as intermittent slugs of liquid. In the stratified flow regime, the condensation is gravity controlled.

Breber et al. [16] developed a simplified classification scheme for the flow regimes in horizontal tube-side condensation, as illustrated in Figure 11.11. The prevailing flow regime is determined by two parameters, the Lockhart-Martinelli parameter, $X$, and a dimensionless vapor mass flux, $j^{*}$, defined as follows:

$$
\begin{equation*}
j^{*}=\frac{x G}{\left[D_{i} g \rho_{V}\left(\rho_{L}-\rho_{V}\right)\right]^{0.5}} \tag{11.52}
\end{equation*}
$$

In this equation, $G$ is the total mass flux of vapor and liquid based on the entire tube cross section. The Lockhart-Martinelli parameter is correlated with the liquid fraction of the flow, while $j^{*}$ is directly related to the ratio of shear force to gravitational force [16].

Quantitative criteria for determining the flow regime are given in Table 11.1. In addition to the four zones shown in Figure 11.11, the transition regions between zones I and II and between zones II and III are of practical importance. According to Breber et al. [16], the bubble regime, zone IV, occurs only at high reduced pressures.


Figure 11.11 Simplified flow regime diagram for condensation in a horizontal tube. (Source: Ref. [16].)
Table 11.1 Flow Regime Criteria for Condensation in Horizontal Tubes

| Zone | Criterion |
| :--- | :--- |
| I | $j^{*}>1.5$ and $X<1.0$ |
| II | $j^{*}<0.5$ and $X<1.0$ |
| III | $j^{*}<0.5$ and $X>1.5$ |
| IV | $j^{*}>1.5$ and $X>1.5$ |
| Transition (I, II) | $0.5 \leq j^{*} \leq 1.5$ and $X<1.0$ |
| Transition (II, III) | $j^{*}<0.5$ and $1.0 \leq X \leq 1.5$ |

### 11.6.2 Stratified flow

For stratifying flow conditions, the condensation is gravity controlled and a Nusselt-type analysis can be used to derive an equation for the heat-transfer coefficient. As shown in Figure 11.12, the condensate forms a thin film on the upper portion of the tube wall and drains into the stratified layer that covers the bottom portion of the tube. The heat transfer across the stratified layer is usually negligible compared with that across the condensate film. Thus, the average heat-transfer coefficient over the entire circumference of the tube is given by a modified version of Equation (11.30):

$$
\begin{equation*}
h=\Omega\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{\mu_{L}\left(T_{V}-T_{w}\right) D_{i}}\right]^{1 / 4} \tag{11.53}
\end{equation*}
$$

It is assumed here that the vapor is saturated and the effect of condensate subcooling is neglected. The coefficient, $\Omega$, depends on the angle, $\phi$, shown in Figure 11.12. It is also related to the void fraction in the tube by the following simple formula [10]:

$$
\begin{equation*}
\Omega=0.728 \varepsilon_{V}^{0.75} \tag{11.54}
\end{equation*}
$$



Figure 11.12 Illustration of condensate cross-sectional profile in the stratified flow regime. (Source: Ref. [3])

Methods for calculating the void fraction are given in Chapter 9. An alternative that provides a somewhat conservative approximation is to use a constant value of $\Omega=0.56$ [16].

### 11.6.3 Annular flow

For the shear-controlled annular flow regime, Breber et al. [16] recommend the following correlation based on the analogy between heat transfer and fluid flow:

$$
\begin{equation*}
h=h_{L}\left(\phi_{L}^{2}\right)^{0.45}=h_{L O}\left(\phi_{L O}^{2}\right)^{0.45} \tag{11.55}
\end{equation*}
$$

In this equation $\phi_{L}^{2}$ and $\phi_{L O}^{2}$ are two-phase multipliers for the pressure gradient; they can be calculated by the methods given in Chapter 9. The exponent of 0.45 in Equation (11.55) was chosen to provide a conservative estimate of $h$ for design work [16]. An exponent of 0.5 actually gives a better fit to experimental data.

The Boyko-Kruzhilin correlation, Equation (11.50), is also applicable in the annular flow regime. A number of other correlations have been developed for this regime; see, e.g., Refs. [17-22]. Among these, the empirical correlation of Shah [22] is notable for the variety of fluids (water, methanol, ethanol, benzene, toluene, trichloroethylene, and several refrigerants) studied and the number [21] of independent data sets analyzed. The correlation had a mean deviation of less than $17 \%$ for 474 data points, although for some data sets it was in excess of $25 \%$. The correlation can be stated as follows:

$$
\begin{equation*}
h=h_{L O}\left\{(1-x)^{0.8}+3.8 x^{0.76}(1-x)^{0.04} P_{r}^{-0.38}\right\} \tag{11.56}
\end{equation*}
$$

where $P_{r}$ is the reduced pressure. Shah used the Dittus-Boelter correlation, Equation (9.75), to calculate $h_{L O}$ with all fluid properties evaluated at the saturation temperature. The Dittus-Boelter correlation is valid for turbulent flow, and values of $R e_{L O}$ ranged from 100 to 63,000 in the data sets analyzed by Shah. Although Shah reported satisfactory results using this procedure, he recommended using the correlation only for $R e_{L O} \geq 350$. A conservative approach would be to use a laminar-flow correlation to calculate $h_{L O}$ for $R e_{L O}<350$. Equation (11.56) can be used for both vertical and horizontal tubes and qualities from zero to 0.999 . Notice that the correlation breaks down as the quality approaches 1.0 , since it predicts $h=0$ for $x=1.0$.

### 11.6.4 Other flow regimes

Specific correlations for the flow regimes of zones III and IV are not available, but Breber et al. [16] recommend using Equation (11.55) as an approximation for these cases.

For the transition region between zones I and II, the following linear interpolation formula is recommended [16]:

$$
\begin{equation*}
h=h_{I}+\left(j^{*}-1.5\right)\left(h_{I}-h_{I I}\right) \tag{11.57}
\end{equation*}
$$

where $h_{I}$ and $h_{I I}$ are the heat-transfer coefficients for zones I and II, respectively. A similar procedure can be used for the transition region between zones II and III:

$$
\begin{equation*}
h=h_{I I}+2(1-X)\left(h_{I I}-h_{I I I}\right) \tag{11.58}
\end{equation*}
$$

## Example 11.4

The tube bundle of Example 11.2 will be used to condense $50,000 \mathrm{lb} / \mathrm{h}$ of saturated n-propyl alcohol vapor at $207^{\circ} \mathrm{F}$. The bundle will be oriented horizontally and condensation will take place inside the tubes. Estimate the condensing-side heat-transfer coefficient at a position in the condenser where the quality is 0.06 and the tube wall temperature is $156^{\circ} \mathrm{F}$.

## Solution

The first step is to determine the flow regime by computing $j^{*}$ and $X$. The total mass flux, which is needed to compute $j^{*}$ is:

$$
G=\frac{\dot{m}}{n_{t}(\pi / 4) D_{i}^{2}}=\frac{50,000}{109(\pi / 4)(0.584 / 12)^{2}}=246,598 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

From Equation (11.52):

$$
\begin{aligned}
j^{*} & =\frac{x G}{\left[D_{i} g \rho_{V}\left(\rho_{L}-\rho_{V}\right)\right]^{0.5}}=\frac{0.06 \times 246,598}{\left[(0.584 / 12) \times 4.17 \times 10^{8} \times 0.123(49-0.123)\right]^{0.5}} \\
j^{*} & =1.34
\end{aligned}
$$

To compute the Lockhart-Martinelli parameter, the Reynolds numbers of the liquid and vapor fractions flowing alone are calculated. From Examples 11.2 and $11.3, \mu_{L}=0.73 \mathrm{cp}$ and $\mu_{V}=0.0095 \mathrm{cp}$ :

$$
\begin{aligned}
R e_{L} & =D_{i} G_{L} / \mu_{L}=(0.584 / 12)(0.94 \times 246,598) /(0.73 \times 2.419) \\
R e_{L} & =6388 \\
R e_{V} & =D_{i} G_{V} / \mu_{V}=(0.584 / 12)(0.06 \times 246,598) /(0.0095 \times 2.419) \\
R e_{V} & =31,334
\end{aligned}
$$

According to the Lockhart-Martinelli criteria given in Table 9.2, the flow is turbulent in both phases. Therefore, $X=X_{t t}$ is given by Equation (9.37).

$$
\begin{aligned}
X_{t t} & =\left(\frac{1-x}{x}\right)^{0.9}\left(\frac{\rho_{V}}{\rho_{L}}\right)^{0.5}\left(\frac{\mu_{L}}{\mu_{V}}\right)^{0.1} \\
& =\left(\frac{1-0.06}{0.06}\right)^{0.9}\left(\frac{0.123}{49}\right)^{0.5}\left(\frac{0.73}{0.0095}\right)^{0.1} \\
X_{t t} & =0.92
\end{aligned}
$$

For the computed values of $j^{*}$ and $X$, Table 11.1 shows that the flow is in the transition region between zones I and II. Therefore, heat-transfer coefficients must be calculated for both stratified and
annular flow regimes. For the stratified flow calculation, the void fraction is required. Using the Chisholm correlation, Equation (9.63), the slip ratio is:

$$
S R=\left(\rho_{L} / \rho_{V}\right)^{0.25}=(49 / 0.123)^{0.25}=4.468
$$

The void fraction is obtained from Equation (9.59):

$$
\begin{aligned}
\varepsilon_{V} & =\frac{x}{x+S R(1-x) \rho_{V} / \rho_{L}}=\frac{0.06}{0.06+4.468 \times 0.94 \times 0.123 / 49} \\
\varepsilon_{V} & =0.85
\end{aligned}
$$

The heat-transfer coefficient for zone II is given by the following equation obtained by combining Equations (11.53) and (11.54):

$$
\begin{aligned}
h_{I I} & =0.728 \varepsilon_{V}^{0.75}\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{\mu_{L}\left(T_{V}-T_{w}\right) D_{i}}\right]^{1 / 4} \\
& =0.728(0.85)^{0.75}\left[\frac{(0.095)^{3} \times 49(49-0.123) \times 4.17 \times 10^{8} \times 295.85}{0.73 \times 2.419(207-156)(0.584 / 12)}\right]^{1 / 4} \\
h_{I I} & =316 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Equation (11.55) will be used for the zone I calculation. To calculate $h_{L O}$, the appropriate Reynolds number is:

$$
\begin{aligned}
& R e_{L O}=D_{i} G / \mu_{L}=(0.584 / 12) \times 246,598 /(0.73 \times 2.419) \\
& R e_{L O}=6796
\end{aligned}
$$

Since this value is in the transition region for heat transfer in tubular flow, the Hausen correlation, Equation (2.37) is used. Needed physical property data are obtained from Example 11.3:

$$
\begin{aligned}
N u & =0.116\left[\operatorname{Re}^{2 / 3}-125\right] \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{W}\right)^{0.14}\left\{1+\left(D_{i} / L\right)^{2 / 3}\right\} \\
& =0.116\left\{(6796)^{2 / 3}-125\right\}(13.4)^{1 / 3}(0.73 / 0.85)^{0.14}\left\{1+[0.584 /(12 \times 12)]^{2 / 3}\right\} \\
N u & =64.66 \\
h_{L O} & =N u\left(k_{L} / D_{i}\right)=64.66 \times 0.095 /(0.584 / 12) \\
h_{L O} & \cong 126 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

The Müller-Steinhagen and Heck (MSH) correlation will be used to calculate the two-phase multiplier, $\phi_{L O}^{2}$. First, the Chisholm parameter is calculated from Equation (9.42) with $n=0.2585$ for turbulent flow in heat-exchanger tubes:

$$
\begin{aligned}
& Y=\left(\rho_{L} / \rho_{V}\right)^{0.5}\left(\mu_{V} / \mu_{L}\right)^{n / 2}=(49 / 0.123)^{0.5}(0.0095 / 0.73)^{0.1293} \\
& Y=11.39
\end{aligned}
$$

The two-phase multiplier is given by Equation (9.35):

$$
\begin{aligned}
\phi_{L O}^{2} & =Y^{2} x^{3}+\left[1+2 x\left(Y^{2}-1\right)\right](1-x)^{1 / 3} \\
& =(11.39)^{2}(0.06)^{3}+\left\{1+2 \times 0.06\left((11.39)^{2}-1\right)\right\}(0.94)^{1 / 3} \\
\phi_{L O}^{2} & =16.14
\end{aligned}
$$

The heat-transfer coefficient for zone I is obtained from Equation (11.55):

$$
h_{I}=h_{L O}\left(\phi_{L O}^{2}\right)^{0.45}=126(16.14)^{0.45}=440 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

Finally, the heat-transfer coefficient for the transition region is estimated by Equation (11.57):

$$
\begin{aligned}
h & =h_{I}+\left(j^{*}-1.5\right)\left(h_{I}-h_{I I}\right) \\
& =440+(1.34-1.5)(440-316) \\
h & =420 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

## Example 11.5

Compare the correlations of Breber et al., Boyko and Kruzhilin, and Shah for the conditions of Example 11.4. The critical pressure of $n$-propyl alcohol is 51.0 atm .

## Solution

All three correlations give the heat-transfer coefficient as the product of $h_{L O}$ and an effective twophase multiplier for heat transfer. For the correlation of Breber et al., the multiplier is:

$$
\left(\phi_{L O}^{2}\right)^{0.45}=(16.14)^{0.45}=3.50
$$

However, this correlation includes a built-in safety factor for design work that the other two correlations lack. Hence, using an exponent of 0.5 in this method provides a fairer comparison:

$$
\left(\phi_{L O}^{2}\right)^{0.5}=(16.14)^{0.5}=4.02
$$

The safety factor in this case amounts to roughly $15 \%$.
From Equation (11.50), the multiplier in the Boyko-Kruzhilin correlation is:

$$
\left[1+x\left(\rho_{L}-\rho_{V}\right) / \rho_{V}\right]^{0.5}=[1+0.06(49-0.123) / 0.123]^{0.5}=4.98
$$

From Equation (11.56), the multiplier for the Shah correlation is:

$$
\begin{aligned}
(1-x)^{0.8}+3.8 x^{0.76}(1-x)^{0.04} P_{r}^{-0.38} & =(0.94)^{0.8}+3.8(0.06)^{0.76}(0.94)^{0.04}(1 / 51.0)^{-0.38} \\
& =2.94
\end{aligned}
$$

Using the value of $h_{L O}=126 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}{ }^{2} \cdot{ }^{\circ} \mathrm{F}$ from Example 11.4, the two-phase heat-transfer coefficients for the Breber et al. and Boyko-Kruzhilin methods are as shown in the table below. The Shah correlation includes very specific instructions for calculating $h_{L O}$ : use the Dittus-Boelter correlation
with all fluid properties evaluated at the saturation temperature. At $T_{\text {sat }}=207^{\circ} \mathrm{F}$, we have $\mu_{L}=0.5 \mathrm{cp}$ and $C_{P, L}=0.77 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$. Using these values gives:

$$
\begin{aligned}
R e_{L O} & =D_{i} G / \mu_{L}=(0.584 / 12) \times 246,598 /(0.5 \times 2.419)=9922 \\
\operatorname{Pr}_{L} & =C_{P, L} \mu_{L} / k_{L}=0.77 \times 0.5 \times 2.419 / 0.095=9.80 \\
h_{L O} & =0.023 \operatorname{Re}_{L O}^{0.8} \operatorname{Pr}_{L}^{0.4}\left(k_{L} / D_{i}\right)=0.023(9922)^{0.8}(9.80)^{0.4} \times 0.095 /(0.584 / 12) \\
h_{L O} & =176 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} \\
h & =176 \times 2.94=517 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .^{\circ} \mathrm{F}
\end{aligned}
$$

The results are summarized in the following table.

| Method | $\mathrm{h}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :--- | :--- |
| Breber et al., exponent $=0.45$ | 440 |
| Breber et al., exponent $=0.50$ | 506 |
| Boyko-Kruzhilin | 627 |
| Shah | 517 |

With no safety factor, the predictions of the three methods agree to within $25 \%$. The close agreement between results from the Shah and Breber et al. methods is probably fortuitous, as the uncertainties associated with all methods of this type are substantial. For design work, a safety factor of $15-25 \%$ appears warranted.

### 11.7 Condensation on Finned Tubes

Horizontal shell-side condensers equipped with radial low-fin tubes are commonly used to condense refrigerants and other organic fluids. The surface tension of these condensates is typically less than about 35 dyne $/ \mathrm{cm}$. With fluids having elevated surface tension, the condensate may bridge the gap between fins, resulting in poor condensate drainage, and heat-transfer coefficients that are lower than for plain tubes. Hence, fin spacing is an important consideration for these condensates. For example, with condensing steam ( $\sigma_{\text {water }} \cong 60$ dyne $/ \mathrm{cm}$ at $100^{\circ} \mathrm{C}$ and atmospheric pressure) a fin density no greater than 16 fpi should be used [23].

Beatty and Katz [24] studied the condensation of propane, n-butane, n-pentane, sulfur dioxide, methyl chloride, and Freon- 22 on single horizontal finned tubes, and developed a modified Nusselt correlation that fit the experimental data to within $\pm 10 \%$. The correlation is based on an equivalent diameter that allows the heat transfer from both fins and prime surface to be represented by a single average heat-transfer coefficient. The correlation can be stated as follows:

$$
\begin{equation*}
h=0.689\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \lambda}{\mu_{L} \Delta T_{f} D_{e}}\right]^{1 / 4} \tag{11.59}
\end{equation*}
$$

Here $\Delta T_{f}$ is the temperature difference across the condensate film and the equivalent diameter, $D_{e}$, is defined by the following equation:

$$
\begin{equation*}
D_{e}^{-0.25}=\frac{1.30 \eta_{f} A_{\text {fins }} E^{-0.25}+A_{\text {prime }} D_{r}^{-0.25}}{\eta_{w} A_{\text {Tot }}} \tag{11.60}
\end{equation*}
$$

where
$\eta_{f}=$ fin efficiency
$\eta_{w}=$ weighted efficiency of finned surface
$A_{\text {fins }}=$ Area of all fins
$A_{\text {Tot }}=A_{\text {fins }}+A_{\text {prime }}$
$D_{r}=$ root-tube diameter
$E=\pi\left(r_{2}^{2}-r_{1}^{2}\right) /\left(2 r_{2}\right)$
$r_{2}=$ fin radius
$r_{1}=D_{r} / 2=$ root-tube radius
The rate of heat transfer across the condensate film is given by:

$$
\begin{equation*}
q=W \lambda=h n_{t} \eta_{w} A_{T o t} \Delta T_{f} \tag{11.61}
\end{equation*}
$$

Rearranging this equation gives:

$$
\begin{equation*}
\lambda / \Delta T_{f}=h n_{t} \eta_{w} A_{T o t} / W=h \eta_{w} A_{T o t} /(\Gamma L) \tag{11.62}
\end{equation*}
$$

Here, $\Gamma=W / n_{t} L$ is the condensate loading per tube. Substituting this result in Equation (11.59) gives:

$$
h=0.689\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \eta_{w}\left(A_{T o t} / L\right)}{\mu_{L} D_{e} \Gamma}\right]^{1 / 4} h^{1 / 4}
$$

Solving for $h$, we obtain:

$$
\begin{equation*}
h=0.609\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \eta_{w}\left(A_{T o t} / L\right)}{\mu_{L} D_{e} \Gamma}\right]^{1 / 3} \tag{11.63}
\end{equation*}
$$

This equation is valid for a single row of tubes. For a horizontal tube bundle, $\Gamma$ is replaced by the effective loading, $\Gamma^{*}=W / L n_{t}^{2 / 3}$.

Condensing coefficients for finned tubes tend to be substantially higher than for plain tubes, provided there is good condensate drainage from the finned surface. However, the Beatty-Katz correlation does not account for the effect of surface tension on condensate drainage. As a result, it may over-predict the heat-transfer coefficient at very small fin spacings if the surface tension of the condensate is relatively high. Correlations that include the effects of surface tension are discussed by Kraus et al. [23], who also present a method for estimating the minimum fin spacing that is compatible with good drainage for a given condensate.

### 11.8 Pressure Drop

The pressure change in a condensing fluid is comprised of three parts, namely, the static head, the momentum change, and the friction loss. Since the fluid velocity decreases from inlet to outlet in a condenser, the momentum change results in a pressure gain rather than a loss. This effect is generally small, and with the exception of vacuum operations, can be safely neglected.

For condensation inside vertical and horizontal tubes, the friction loss can be calculated using the methods given in Chapter 9 for two-phase flow. Since the quality usually changes greatly from inlet to outlet, an incremental or zone analysis is required for rigorous calculations. If desuperheating or subcooling zones are present, they must be treated separately as single-phase flow regimes. In calculating the friction loss, the effect of mass transfer due to condensation is neglected, although it can be significant in some circumstances [25]. For vertical units, calculation of the static head effect involves integration of the two-phase density over the length of the condensing zone. The procedure is essentially the same as that used in the analysis of vertical thermosyphon reboilers in Chapter 10. The contributions from desuperheating and subcooling zones must be added. For horizontal tube-side condensers, the static head is essentially determined by the height of liquid in the outlet header, and the corresponding pressure difference can usually be neglected.

Table 11.2 Values of Parameters in Chisholm Correlation for Calculating Friction Losses in Shell-side Condensers

| Flow geometry | Flow regimes | $B$ | $n$ |
| :--- | :--- | :--- | :--- |
| Cross flow, vertical | Spray, bubbly | 1.0 | 0.37 |
| Cross flow, horizontal | Spray, bubbly | 0.75 | 0.46 |
| Cross flow, horizontal | Stratified, stratified spray | 0.25 | 0.46 |
| Baffle window, vertical cut* | All | $2 /(Y+1)$ | 0 |
| Baffle window, horizontal cut** | All | $\rho_{\text {hom }} / \rho_{L}$ | 0 |

*Side-to-side flow pattern
**Up-and-down flow pattern
A method for calculating the friction loss in shell-side condensers based on the Chisholm correlation is presented in Refs. [1,2]. The Chisholm correlation for the two-phase pressure gradient multiplier was presented in Chapter 9 and is repeated here for convenience.

$$
\begin{equation*}
\phi_{L O}^{2}=1+\left(Y^{2}-1\right)\left\{B[x(1-x)]^{(2-n) / 2}+x^{2-n}\right\} \tag{9.43}
\end{equation*}
$$

Values of the parameters $B$ and $n$ to be used for flow across tube banks and in baffle windows are given in Table 11.2. The homogeneous two-phase density, $\rho_{\text {hom }}$, appearing in this table is calculated according to Equation (9.51).

The flow regime can be determined using flow pattern maps given in Ref. [2]. However, the accuracy achievable with this procedure is limited, and hence, a conservative alternative is suggested here. For horizontal cross flow, use the values for the spray and bubbly flow regimes when vapor shear is significant and use the values for the stratified flow regimes when it is not. As discussed under "Condensation outside horizontal tubes", the significance of vapor shear can be determined using Equation (11.51). For vertical cross flow characteristic of X-shell condensers, use the values for spray and bubbly flow in all situations, as no alternative is available. Note that for baffled E- and J-shell condensers, the two-phase multipliers must be applied individually in the cross-flow zones between baffle tips and in the baffle windows. Therefore, the method must be used in conjunction with either the Stream Analysis method or the Delaware method for single-phase pressure drop, both of which calculate the individual pressure drops for cross-flow and window zones. Combined with an incremental analysis, such a procedure obviously requires computer implementation.

An approximate method suitable for hand calculations is based on the pressure drop, $\left(\Delta P_{f}\right)_{V O}$, calculated for the total flow as vapor at inlet conditions:

$$
\begin{equation*}
\Delta P_{f}=\bar{\phi}_{V O}^{2}\left(\Delta P_{f}\right)_{V O} \tag{11.64}
\end{equation*}
$$

For shell-side condensation with a saturated vapor feed, Bell and Mueller [26] present a graph for the average two-phase multiplier, $\bar{\phi}_{V O}^{2}$, as a function of the exit vapor fraction, $x_{e}$. The following equation was obtained by regression analysis using values read from the graph:

$$
\begin{equation*}
\bar{\phi}_{V O}^{2}=0.33+0.22 x_{e}+0.61 x_{e}^{2} \quad\left(0 \leq x_{e} \leq 0.95\right) \tag{11.65}
\end{equation*}
$$

Although based on experimental data, this correlation involves a number of assumptions [26], including constant condensation rate throughout the tube bundle. Note that for a total condenser, $x_{e}=0$ and Equation (11.65) gives $\bar{\phi}_{V O}^{2}=0.33$. Kern and Kraus [27] noted that if the vapor velocity varies linearly from inlet to outlet, then the two-phase multiplier should be equal to $1 / 3$ for a total condenser, which is consistent with Equation (11.65). However, they also noted that in actuality the multiplier tends to be slightly higher, and recommended a value of 0.5 as a conservative approximation for total condensers. If a more conservative estimate is desired for a partial condenser, the larger of 0.5 and the value given by Equation (11.65) can be used.

For tube-side condensation of saturated vapors, the following equation can be used to estimate the average two-phase multiplier [28]:

$$
\begin{equation*}
\bar{\phi}_{V O}^{2}=0.5\left(1+u_{V, o u t} / u_{V, \text { in }}\right) \tag{11.66}
\end{equation*}
$$

where $u_{V, i n}$ and $u_{V, \text { out }}$ are the vapor velocities at the condenser inlet and outlet, respectively. For a total condenser, Equation (11.66) reduces to $\bar{\phi}_{V O}^{2}=0.5$. In fact, this method was used to estimate the pressure drop for condensing steam in Example 10.2.

### 11.9 Mean Temperature Difference

When one stream in a heat exchanger is isothermal, the LMTD correction factor is equal to 1.0 regardless of the flow pattern. This situation is closely approximated in the condensation of a saturated pure-component vapor because the pressure drop is generally small on the condensing side. In this case, the mean temperature difference in the condenser is simply the LMTD.

When a significant desuperheating or subcooling zone exists in the condenser, or when a multi-component vapor is condensed, the temperature of the condensing stream usually varies substantially from inlet to outlet. Furthermore, the stream enthalpy varies nonlinearly with temperature in these situations, so the mean temperature difference is not equal to $F\left(\Delta T_{\ln }\right)_{c f}$ as in a single-phase heat exchanger. (In a single phase exchanger with constant stream heat capacities, the specific enthalpy, $\hat{H}$, of each stream is linear in temperature since it satisfies $\Delta \hat{H}=C_{P} \Delta T$. This is one of the fundamental assumptions upon which the methodology for single-phase exchangers is based.) The upshot is that a zone analysis is generally required for these cases, and with multiple coolant passes this is an iterative procedure suitable for computer implementation but not easily adapted to hand calculation.

In certain types of application, simplifying assumptions can be made to avoid a zone analysis and facilitate hand calculations. Two of these are the following:

- For shell-side condensation of a pure-component vapor in a horizontal E-shell unit, it can be assumed that all the heat is transferred at the saturation temperature in the shell. Provided that a condensate film exists over the entire desuperheating section, the temperature at the vaporliquid interface will be $T_{s a t}$, the same as in the condensing section. Dry-wall desuperheating is possible if the tube wall temperature exceeds $T_{s a t}$. However, as discussed by Rubin [29], a dry desuperheating zone is unlikely to exist in a standard E-shell condenser due to mixing of the inlet vapor with condensate in the shell. Therefore, the above assumption is generally acceptable for this type of unit. It is reasonable for other types of condensers as well, provided that conditions permitting a dry desuperheating zone do not exist.
- For narrow-boiling mixtures, the condensing curve (a plot of stream temperature versus the amount of heat removed from the stream, equivalent to a temperature-enthalpy plot) may be approximately linear. Figure 11.13 shows the condensing curve for a mixture of 30 mole percent n-butane and 70 mole percent n-pentane at a pressure of 75 psia . Although some curvature is present, a straight line provides a reasonable approximation to the graph. If such a mixture is condensed without substantial desuperheating or subcooling zones, the LMTD correction factor can be used to estimate the mean temperature difference, as in a single-phase heat exchanger. For E-shell units, the method given in Chapter 3 is used to calculate the LMTD correction factor. Procedures for J - and X -shell units are given in Appendix 11.A.

For situations in which a zone analysis is unavoidable, Gulley [30] presented an approximate method for calculating a weighted mean temperature difference in multi-pass condensers that does not require iteration, and hence, is amenable to hand calculation. Even with this simplification, calculations for multi-component, multi-zone condensers can be very laborious, and will not be considered further here.


Figure 11.13 Condensing curve for mixture of butane and pentane.

When using the above approximation for condensing mixtures, Bell and Mueller [26] recommend the following procedure to account for the thermal resistance due to the sensible heat transfer involved in cooling the vapor over the condensing range. The overall coefficient, $U_{D}$, is replaced with a modified design coefficient, $U_{D}^{\prime}$, defined by:

$$
\begin{equation*}
U_{D}^{\prime}=\left[U_{D}^{-1}+\left(q_{s e n} / q_{T o t}\right) h_{V}^{-1}\right]^{-1} \tag{11.67}
\end{equation*}
$$

where
$q_{\text {sen }}=$ sensible heat duty for vapor cooling
$q_{\text {Tot }}=$ total duty
$h_{V}=$ heat-transfer coefficient for vapor calculated using the average vapor flow rate
The sensible heat duty is estimated using the average heat capacity, $\bar{C}_{P, V}$, and average flow rate of the vapor:

$$
\begin{equation*}
q_{\text {sen }}=0.5 \bar{C}_{P, V}\left(\dot{m}_{V, \text { in }}+\dot{m}_{V, \text { out }}\right)\left(T_{V, \text { in }}-T_{V, \text { out }}\right) \tag{11.68}
\end{equation*}
$$

## Example 11.6

$180,000 \mathrm{lb} / \mathrm{h}$ of a saturated vapor consisting of 30 mole percent n-butane and 70 mole percent n pentane are to be condensed at a pressure of 75 psia . The condensing range at feed conditions is from $183.5^{\circ} \mathrm{F}$ to $168^{\circ} \mathrm{F}$, and the enthalpy difference between saturated vapor and saturated liquid is $143 \mathrm{Btu} / \mathrm{lbm}$. Cooling water is available at $85^{\circ} \mathrm{F}$ and 60 psia . Tubing material is specified to be $90 / 10$ copper-nickel alloy ( $k=30 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ), and a fouling factor of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is recommended for the cooling water. Maximum pressure drops of 5 psi for the hydrocarbon stream and 10 psi for the coolant are specified. Physical properties of the feed and condensate are given in the table below. The viscosity of the condensate can be estimated using the following equation:

$$
\mu_{L}(\mathrm{cp})=0.00941 \exp \left[1668 / T\left({ }^{\circ} R\right)\right]
$$

The other condensate properties may be assumed constant at the tabled values. Design a condenser for this service using plain (un-finned) tubes.

| Property | Feed | Condensate |
| :--- | :--- | :---: |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.486 | 0.61 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.0119 | 0.057 |
| $\mu(\mathrm{cp})$ | 0.0085 | - |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 0.845 | 35.5 |
| $\operatorname{Pr}$ | 0.84 | - |

## Solution

(a) Make initial specifications.
(i) Fluid placement

A horizontal shell-side condenser will be used. Therefore, the condensing vapor is placed in the shell and cooling water in the tubes.
(ii) Shell and head types

An E-shell unit is specified since it is generally the most economical type of condenser. The difference between the inlet temperatures of the two streams is nearly $100^{\circ} \mathrm{F}$ at design conditions, and could be significantly higher if the temperature of the cooling water decreases during cold weather. Therefore, U-tubes are specified to allow for differential thermal expansion. Thus, an AEU exchanger is specified.
(iii) Tubing

For water service, $3 / 4$-in., 16 -BWG tubes are selected with a length of 16 ft .
(iv) Tube layout

Since the shell-side fluid is clean, triangular pitch is specified. A tube pitch of either $15 / 16$ or 1.0 in . can be used. The smaller value is selected because it provides more heat-transfer surface for a given shell size. (See tube-count tables in Appendix C.)
(v) Baffles

Segmental baffles with a spacing of 0.4 times the shell diameter and a cut of $35 \%$ are appropriate for a condensing vapor (see Figure 5.4).
(vi) Sealing strips

The bundle-to-shell clearance in U-tube exchangers is generally small. However, impingement protection is required for a condenser, and some tubes will have to be omitted from the bundle to provide adequate flow area above the impingement plate for the entering vapor. Depending on the size of the resulting gap in the tube bundle, sealing strips may be needed to block the bundle bypass flow.
(vii) Construction materials

The 90/10 cupro-nickel alloy specified for the tubes will provide corrosion resistance and allow a maximum water velocity of $10 \mathrm{ft} / \mathrm{s}$ (Table 5.B1). For compatibility, this material is also specified for the tubesheets. Plain carbon steel is adequate for the shell, heads, and all other components.
(b) Energy balances.

The duty is calculated using the given enthalpy difference between saturated vapor and saturated liquid. Condensate subcooling is neglected, as is the effect of pressure drop on saturation temperature:

$$
q=\dot{m} \Delta \hat{H}=180,000 \times 143=25.74 \times 10^{6} \mathrm{Btu} / \mathrm{h}
$$

Neither the outlet temperature nor the flow rate of the cooling water is specified in this problem. The outlet temperature is frequently limited to $110-125^{\circ} \mathrm{F}$ in order to minimize fouling due to deposition of minerals contained in the water. Economic considerations are also involved, since a higher outlet temperature reduces the amount of cooling water used (which tends to lower the operating cost), while also lowering the mean temperature difference in the exchanger (which tends to increase the capital cost). For the purpose of this example, an
outlet temperature of $120^{\circ} \mathrm{F}$ will be used, giving an average water temperature of $102.5^{\circ} \mathrm{F}$. The properties of water at this temperature are as follows:

| Property | Water at $102.5^{\circ} \mathrm{F}$ |
| :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 1.0 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.37 |
| $\mu(\mathrm{cp})$ | 0.72 |
| Specific gravity | 0.99 |
| $P r$ | 4.707 |

The cooling water flow rate is obtained from the energy balance:

$$
\begin{aligned}
q & =25.74 \times 10^{6}=\left(\dot{m} C_{P} \Delta T\right)_{\text {water }}=\dot{m}_{\text {water }} \times 1.0 \times 35 \\
\dot{m}_{\text {water }} & =735,429 \mathrm{lbm} / \mathrm{h}
\end{aligned}
$$

(c) Mean temperature difference.

Since the condensing curve for this system (Figure 11.13) is approximately linear, the mean temperature difference is estimated as follows:

$$
\begin{aligned}
\Delta T_{m} & \cong F\left(\Delta T_{\ln }\right)_{c f} \\
\left(\Delta T_{\ln }\right)_{c f} & =\frac{83-63.5}{\ln (83 / 63.5)}=72.8^{\circ} \mathrm{F} \\
R & =\frac{T_{a}-T_{b}}{t_{b}-t_{a}}=\frac{183.5-168}{120-85}=0.443 \\
P & =\frac{t_{b}-t_{a}}{T_{a}-t_{a}}=\frac{120-85}{183.5-85}=0.355
\end{aligned}
$$

From Figure 3.9, $F \cong 0.98$. Therefore,

$$
\Delta T_{m} \cong 0.98 \times 72.8=71.3^{\circ} \mathrm{F}
$$

(d) Approximate overall heat-transfer coefficient.

From Table 3.5, for a condenser with low-boiling hydrocarbons on the shell side and cooling water on the tube side, $80 \leq U_{D} \leq 200 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Taking the mid-range value gives $U_{D}=140 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(e) Heat-transfer area and number of tubes.

$$
\begin{aligned}
A & =\frac{q}{U_{D} \Delta T_{m}}=\frac{25.74 \times 10^{6}}{140 \times 71.3}=2579 \mathrm{ft}^{2} \\
n_{t} & =\frac{A}{\pi D_{o} L}=\frac{2579}{\pi(0.75 / 12) \times 16}=821
\end{aligned}
$$

(f) Number of tube passes.

$$
\begin{aligned}
& D_{i}=0.620 \text { in. }=0.0517 \mathrm{ft} \quad(\text { Table B.1) } \\
& R e=\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 735,429\left(n_{p} / 821\right)}{\pi \times 0.0517 \times 0.72 \times 2.419}=12,666 n_{p}
\end{aligned}
$$

Therefore, two tube passes will suffice to give fully turbulent flow in the tubes.
Checking the fluid velocity,

$$
V=\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\rho \pi D_{i}^{2} / 4}=\frac{(735,429 / 3600)(2 / 821)}{0.99 \times 62.43 \times \pi(0.0517)^{2} / 4}=3.84 \mathrm{ft} / \mathrm{s}
$$

The velocity is acceptable, and therefore two passes will be used. (Note that four passes could also be used, giving a velocity of about $7.7 \mathrm{ft} / \mathrm{s}$.)
(g) Shell size and tube count.

From Table C.2, the closest count is 846 tubes in a $31-\mathrm{in}$. shell.
(h) Required overall coefficient.

$$
U_{r e q}=\frac{q}{n_{t} \pi D_{o} L \Delta T_{m}}=\frac{25.74 \times 10^{6}}{846 \times \pi \times(0.75 / 12) \times 16 \times 71.3}=136 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(i) Calculate $h_{i}$ assuming $\phi_{i}=1.0$.

$$
\begin{aligned}
R e & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 735,429(2 / 846)}{\pi \times 0.0517 \times 0.72 \times 2.419}=24,584 \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =(0.37 / 0.0517) \times 0.023(24,584)^{0.8}(4.707)^{1 / 3} \times 1.0 \\
h_{i} & =898 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .^{\circ} \mathrm{F}
\end{aligned}
$$

(j) Calculate $h_{o}$.

The basic Nusselt theory will be used to obtain a conservative estimate for the condensing heat-transfer coefficient. A tube wall temperature of $125^{\circ} \mathrm{F}$ is assumed to start the calculation. The average film temperature is calculated using the average vapor temperature of $175.75^{\circ} \mathrm{F}$ :

$$
T_{f}=0.75 T_{w}+0.25 T_{V}=0.75 \times 125+0.25 \times 175.75=137.7^{\circ} \mathrm{F}
$$

The condensate viscosity at this temperature is:

$$
\mu_{L}=0.00941 \exp [1668 /(137.7+460)]=0.153 \mathrm{cp}
$$

The modified condensate loading is calculated from Equation (11.36):

$$
\Gamma^{*}=\frac{W}{L n_{t}^{2 / 3}}=\frac{180,000}{16(846)^{2 / 3}}=125.77 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}
$$

The heat-transfer coefficient is given by Equation (11.35):

$$
\begin{aligned}
& h_{o}=1.52\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g}{4 \mu_{L} \Gamma^{*}}\right]^{1 / 3}=1.52\left[\frac{(0.057)^{3} \times 35.5(35.5-0.845) \times 4.17 \times 10^{8}}{4 \times 0.153 \times 2.419 \times 125.77}\right]^{1 / 3} \\
& h_{o}=121 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

The shell-side coefficient is less than $U_{\text {req }}$, indicating that the condenser is severely under-sized. Therefore, no further calculations will be made with the initial configuration.

The low value of $h_{o}$ suggests that the value of $U_{D}$ is likely to be less than $100 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. The number of tubes needed to give $U_{\text {req }}$ a value of, say, $90 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ is:

$$
\left(n_{t}\right)_{r e q}=846(136 / 90)=1278
$$

With this many tubes, four tube passes will be required to keep the water velocity above $3 \mathrm{ft} / \mathrm{s}$. Referring to the tube-count table, a 39-in. shell containing 1336 tubes is selected for the next trial.

## Second trial

(a) Required overall coefficient.

$$
U_{\text {req }}=\frac{q}{n_{t} \pi D_{o} L \Delta T_{m}}=\frac{25.74 \times 10^{6}}{1336 \times \pi(0.75 / 12) \times 16 \times 71.3}=86 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(b) Calculate $h_{i}$ assuming $\phi_{i}=1.0$.

$$
\begin{aligned}
R e & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 735,429(4 / 1336)}{\pi \times 0.0517 \times 0.72 \times 2.419}=31,135 \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =(0.37 / 0.0517) \times 0.023(31,135)^{0.8}(4.707)^{1 / 3} \times 1.0 \\
h_{i} & =1085 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .^{\circ} \mathrm{F}
\end{aligned}
$$

(c) Calculate $h_{o}$.

As before, a wall temperature of $125^{\circ} \mathrm{F}$ is assumed, giving an average film temperature of $137.7^{\circ} \mathrm{F}$, at which $\mu_{L}=0.153 \mathrm{cp}$.

$$
\begin{aligned}
\Gamma^{*} & =\frac{W}{L n_{t}^{2 / 3}}=\frac{180,000}{16(1336)^{2 / 3}}=92.74 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft} \\
h_{o} & =1.52\left[\frac{(0.057)^{3} \times 35.5(35.5-0.845) \times 4.17 \times 10^{8}}{4 \times 0.153 \times 2.419 \times 92.74}\right]^{1 / 3} \\
h_{o} & =134 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(d) Calculate $T_{w}$ and $T_{f}$.

$$
\begin{aligned}
T_{w} & =\frac{h_{i} t_{a v e}+h_{o}\left(D_{o} / D_{i}\right) T_{\text {ave }}}{h_{i}+h_{o}\left(D_{o} / D_{i}\right)}=\frac{1085 \times 102.5+134(0.75 / 0.62) \times 175.75}{1085+134(0.75 / 0.62)} \\
T_{w} & =112^{\circ} \mathrm{F} \\
T_{f} & =0.75 \times 112+0.25 \times 175.75=128^{\circ} \mathrm{F}
\end{aligned}
$$

(e) Recalculate $h_{o}$.

The value of $\mu_{L}$ at $128^{\circ} \mathrm{F}$ is:

$$
\mu_{L}=0.00941 \exp [1668 /(128+460)]=0.161 \mathrm{cp}
$$

The corresponding value of $h_{o}$ is:

$$
h_{o}=1.52\left[\frac{(0.057)^{3} \times 35.5(35.5-0.845) \times 4.17 \times 10^{8}}{4 \times 0.161 \times 2.419 \times 92.74}\right]^{1 / 3}=132 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}
$$

Since this value is close to the previous one, no further iterations are required.
(f) Viscosity correction factor for cooling water.

Since the tube wall temperature is close to the bulk water temperature, the viscosity correction factor is neglected.
(g) Overall coefficient.

The recommended fouling factor for the cooling water was given in the problem statement as $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$. Since the condensing vapor is a very clean stream, a fouling factor of $0.0005 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is appropriate. Thus,

$$
\begin{aligned}
U_{D} & =\left[\frac{D_{o}}{h_{i} D_{i}}+\frac{D_{o} \ln \left(D_{o} / D_{i}\right)}{2 k_{\text {tube }}}+\frac{1}{h_{o}}+\frac{R_{D i} \times D_{o}}{D_{i}}+R_{D o}\right]^{-1} \\
& =\left[\frac{0.75}{1085 \times 0.62}+\frac{(0.75 / 12) \ln (0.75 / 0.62)}{2 \times 30}+\frac{1}{132}+\frac{0.001 \times 0.72}{0.62}+0.0005\right]^{-1} \\
U_{D} & =94 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(h) Correction for sensible heat transfer.

The effect of interfacial shear was neglected in calculating $h_{o}$, which will more than offset the effect of sensible heat transfer. Hence, this step could be omitted, but is included here to illustrate the procedure. The rate of sensible heat transfer is estimated using Equation (11.68). For convenience, the heat capacity at vapor inlet conditions is used as an approximation for $\bar{C}_{P, V}$ :

$$
\begin{aligned}
q_{\text {sen }} & =0.5 \bar{C}_{P, V}\left(\dot{m}_{V, \text { in }}+\dot{m}_{V, \text { out }}\right)\left(T_{V, \text { in }}-T_{V, \text { out }}\right) \\
& =0.5 \times 0.486 \times 180,000(183.5-168) \\
q_{\text {sen }} & =677,970 \mathrm{Btu} / \mathrm{h} \\
q_{\text {sen }} / q_{T o t} & =677,970 / 25.74 \times 10^{6} \cong 0.026
\end{aligned}
$$

The Simplified Delaware method will be used to calculate $h_{V}$. Since the baffle cut is greater than $20 \%$, this method will tend to overestimate $h_{V}$. However, the safety factor built into the method will help to compensate for this error:

$$
\begin{aligned}
B & =0.4 d_{s}=0.4 \times 39=15.6 \mathrm{in} \\
C^{\prime} & =P_{T}-D_{o}=15 / 16-0.75=0.1875 \mathrm{in} \\
a_{s} & =\frac{d_{s} C^{\prime} B}{144 P_{T}}=\frac{39 \times 0.1875 \times 15.6}{144 \times 15 / 16}=0.845 \mathrm{ft}^{2} \\
D_{e} & =0.55 / 12=0.04583 \mathrm{ft} \quad(\text { from Figure } 3.12)
\end{aligned}
$$

The average vapor flow rate of $90,000 \mathrm{lb} / \mathrm{h}$ is used to calculate $h_{V}$. Physical properties of the vapor are taken at inlet conditions for convenience:

$$
\begin{aligned}
G & =\dot{m} / a_{s}=90,000 / 0.845=106,509 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =\frac{D_{e} G}{\mu_{V}}=\frac{0.04583 \times 106,509}{0.0085 \times 2.419}=237,400 \\
j_{H} & =0.5\left(1+B / d_{S}\right)\left(0.08 R e^{0.6821}+0.7 \mathrm{Re}^{0.1772}\right) \\
& =0.5(1+0.4)\left\{0.08(237,400)^{0.6821}+0.7(237,400)^{0.1772}\right\} \\
j_{H} & =264.3 \\
h_{V} & =j_{H}\left(k / D_{e}\right) \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =264.3(0.0119 / 0.04583)(0.84)^{1 / 3}(1.0) \\
h_{V} & =65 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

The modified overall coefficient is given by Equation (11.67):

$$
\begin{aligned}
U_{D}^{\prime} & =\left[U_{D}^{-1}+\left(q_{s e n} / q_{T o t}\right) h_{V}^{-1}\right]^{-1} \\
& =\left[(94)^{-1}+0.026(65)^{-1}\right]^{-1} \\
U_{D}^{\prime} & =91 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Since $U_{D}^{\prime}>U_{r e q}$, the condenser is thermally acceptable.
(i) Tube-side pressure drop.

$$
\begin{aligned}
f & =0.4137 R e^{-0.2585}=0.4137(31,135)^{-0.2585}=0.0285 \\
G & =\frac{\dot{m}\left(n_{p} / n_{t}\right)}{A_{f}}=\frac{735,429(4 / 1336)}{(\pi / 4)(0.0517)^{2}}=1,048,874 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.0285 \times 4 \times 16(1,048,874)^{2}}{7.50 \times 10^{12} \times 0.0517 \times 0.99 \times 1.0} \\
\Delta P_{f} & =5.23 \mathrm{psi} \\
\Delta P_{r} & =1.334 \times 10^{-13} \alpha_{r} G^{2} / s
\end{aligned}
$$

From Table 5.1, for turbulent flow in U-tubes:

$$
\alpha_{r}=1.6 n_{p}-1.5=1.6 \times 4-1.5=4.9
$$

Hence,

$$
\Delta P_{r}=1.334 \times 10^{-13} \times 4.9(1,048,874)^{2} / 0.99=0.75 \mathrm{psi}
$$

Table 5.3 indicates that $10-\mathrm{in}$. nozzles are appropriate for this unit. Assuming that schedule 40 pipe is used, the Reynolds number for the nozzles is:

$$
\begin{aligned}
R e_{n} & =\frac{4 \dot{m}}{\pi D_{i} \mu}=\frac{4 \times 735,429}{\pi(10.02 / 12) \times 0.72 \times 2.419}=643,867 \\
G_{n} & =\frac{\dot{m}}{(\pi / 4) D_{i}^{2}}=\frac{735,429}{(\pi / 4)(10.02 / 12)^{2}}=1,343,006 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

Since the flow is turbulent, Equation (5.4) is used to estimate the pressure loss in the nozzles:

$$
\begin{aligned}
& \Delta P_{n}=2.0 \times 10^{-13} N_{s} G_{n}^{2} / s=2.0 \times 10^{-13} \times 1(1,343,006)^{2} / 0.99 \\
& \Delta P_{n}=0.36 \mathrm{psi}
\end{aligned}
$$

The total tube-side pressure drop is:

$$
\Delta P_{i}=\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=5.23+0.73+0.36 \cong 6.3 \mathrm{psi}
$$

(j) Shell-side pressure drop.

Equation (11.64) will be used to estimate the pressure drop, and the Simplified Delaware method will be used to calculate $\left(\Delta P_{f}\right)_{V O}$. Due to the relatively large baffle cut, the Simplified Delaware method will tend to overestimate the actual pressure drop. (The full Delaware method could be used to obtain a more accurate estimate of the pressure drop, but the additional computational effort is not justified in the present context.) From step (h) we have:

$$
\begin{aligned}
B & =15.6 \mathrm{in} . \\
a_{s} & =0.845 \mathrm{ft}^{2} \\
D_{e} & =0.04583 \mathrm{ft} \\
G & =\dot{m}_{V} / a_{s}=180,000 / 0.845=213,018 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =\frac{D_{e} G}{\mu_{V}}=\frac{0.04583 \times 213,018}{0.0085 \times 2.419}=474,801
\end{aligned}
$$

The friction factor is calculated using Equations (5.7) and (5.9). Note that since the shell diameter exceeds 23.25 in ., $d_{s}$ is set to 23.25 in Equation (5.9):

$$
\begin{aligned}
f_{1} & =\left(0.0076+0.000166 d_{s}\right) R e^{-0.125} \\
& =(0.0076+0.000166 \times 39)(474,801)^{-0.125} \\
f_{1} & =0.00275 \mathrm{ft}^{2} / \mathrm{in}^{2} \\
f_{2} & =\left(0.0016+5.8 \times 10^{-5} d_{s}\right) R e^{-0.157} \\
& =\left(0.0016+5.8 \times 10^{-5} \times 23.25\right)(474,801)^{-0.157} \\
f_{2} & =0.000379 \mathrm{ft}^{2} / \mathrm{in}^{2} \\
f & =144\left\{f_{1}-1.25\left(1-B / d_{s}\right)\left(f_{1}-f_{2}\right)\right\} \\
& =144\{0.00275-1.25(1-0.4)(0.00275-0.000379)\} \\
f & =0.140
\end{aligned}
$$

The number of baffle spaces is estimated as:

$$
n_{b}+1=L / B=\frac{16 \times 12}{15.6} \cong 12.3 \Rightarrow 12
$$

The pressure drop for the total flow as vapor is calculated from Equation (5.6):

$$
\begin{aligned}
\left(\Delta P_{f}\right)_{V O} & =\frac{f G^{2} d_{s}\left(n_{B}+1\right)}{7.50 \times 10^{12} D_{e} s \phi}=\frac{0.140(213,018)^{2}(39 / 12)(12)}{7.50 \times 10^{12} \times 0.04583(0.845 / 62.43)(1.0)} \\
\left(\Delta P_{f}\right)_{V O} & =53.3 \mathrm{psi}
\end{aligned}
$$

From Equation (11.65), $\bar{\phi}_{V O}^{2}=0.33$ for a total condenser. Therefore,

$$
\Delta P_{f}=\bar{\phi}_{V O}^{2}\left(\Delta P_{f}\right)_{V O}=0.33 \times 53.3=17.6 \mathrm{psi}
$$

The shell-side pressure drop greatly exceeds the allowable value of 5 psi . Therefore, we consider increasing the baffle spacing. From Appendix 5.C, the maximum unsupported tube length for $3 / 4-\mathrm{in}$. copper alloy tubes is 52 in. Since the tubes in the baffle windows are supported by every other baffle, the maximum allowable baffle spacing is 26 in ., which is less than the shell diameter. So in this case, the baffle spacing is limited by tube support considerations. When adjusted for an integral number of baffles, the maximum spacing is decreased to 24 in ., and this is too small to reduce the pressure drop to the required level.

Next we consider using a split-flow (type J) shell. The inlet vapor stream is divided into two parts that are fed to opposite ends of the shell and flow toward the center. Since both the flow rate and length of the flow path are halved, the shell-side pressure drop is reduced by a factor of approximately eight compared with an E-shell of the same size. Therefore, for the third trial an AJU exchanger with a 39-in. shell, 1336 tubes and four tube passes is specified. The baffle spacing is decreased somewhat to provide better tube support with seven baffle spaces in each half of the shell. Thus,

$$
B=\frac{16 \times 12}{14}=13.7 \mathrm{in}
$$

The middle baffle is a full circle baffle, as shown in Figure 11.2. These changes have no effect on the calculations for $h_{i}, \Delta P_{i}$, and $h_{o}$. However, $F, h_{V}$, and $\Delta P_{o}$ must be recalculated.

## Third trial

(a) LMTD correction factor.

From the graph in Appendix 11.A for a J shell with an even number of tube passes, $F \cong 0.98$, which is essentially the same as the value for the E shell. Therefore, the required overall coefficient remains unchanged at $86 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(b) Correction for sensible heat transfer.

$$
a_{s}=\frac{d_{s} C^{\prime} B}{144 P_{T}}=\frac{39 \times 0.1875 \times 13.7}{144 \times 15 / 16}=0.742 \mathrm{ft}^{2}
$$

Half the average vapor flow rate of $90,000 \mathrm{lb} / \mathrm{h}$ is used to calculate $h_{V}$. Thus,

$$
\begin{aligned}
G & =\dot{m} / a_{s}=\frac{0.5 \times 90,000}{0.742}=60,647 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =\frac{D_{e} G}{\mu_{V}}=\frac{0.04583 \times 60,647}{0.0085 \times 2.419}=135,177 \\
B / d_{s} & =13.7 / 39=0.351
\end{aligned}
$$

$$
\begin{aligned}
j_{H} & =0.5\left(1+B / d_{s}\right)\left(0.08 R e^{0.6821}+0.7 R e^{0.1772}\right) \\
& =0.5(1+0.351)\left\{0.08(135,177)^{0.6821}+0.7(135,177)^{0.1772}\right\} \\
j_{H} & =174.6 \\
h_{V} & =j_{H}\left(k / D_{e}\right) \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
h_{V} & =174.6(0.0119 / 0.04583)(0.84)^{1 / 3}(1.0) \\
h_{V} & \cong 43 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

The modified overall coefficient then becomes:

$$
\begin{aligned}
U_{D}^{\prime} & =\left[U_{D}^{-1}+\left(q_{s e n} / q_{T o t}\right) h_{V}^{-1}\right]^{-1}=\left[(94)^{-1}+0.026(43)^{-1}\right] \\
U_{D}^{\prime} & =89 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Since $U_{D}^{\prime}>U_{r e q}$, the unit is thermally acceptable.
(c) Shell-side pressure drop.

Half the total mass flow rate of vapor entering the condenser is used to compute $\left(\Delta P_{f}\right)_{V O}$ for the J shell. Thus,

$$
\begin{aligned}
G & =0.5 \dot{m}_{V} / a_{s}=0.5 \times 180,000 / 0.742=121,294 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =\frac{D_{e} G}{\mu_{V}}=\frac{0.04583 \times 121,294}{0.0085 \times 2.419}=270,355 \\
f_{1} & =\left(0.0076+0.000166 d_{s}\right) R e^{-0.125} \\
& =(0.0076+0.000166 \times 39)(270,355)^{-0.125} \\
f_{1} & =0.00295 \mathrm{ft}^{2} / \mathrm{in}^{2} \\
f_{2} & =\left(0.0016+5.8 \times 10^{-5} d_{s}\right) R e^{-0.157} \\
& =\left(0.0016+5.8 \times 10^{-5} \times 23.25\right)(270,355)^{-0.157} \\
f_{2} & =0.000414 \mathrm{ft}^{2} / \mathrm{in} .^{2} \\
f & =144\left\{f_{1}-1.25\left(1-B / d_{s}\right)\left(f_{1}-f_{2}\right)\right\} \\
& =144\{0.00295-1.25(1-0.351)(0.00295-0.000414)\} \\
f & =0.1285 \\
\left(\Delta P_{f}\right)_{V O} & =\frac{f G^{2} d_{s}\left(n_{b}+1\right)}{7.50 \times 10^{12} D_{e} s \phi}=\frac{0.1285(121,294)^{2}(39 / 12)(7)}{7.50 \times 10^{12} \times 0.04583(0.845 / 62.43)(1.0)} \\
\left(\Delta P_{f}\right)_{V O} & =9.24 \mathrm{psi}
\end{aligned}
$$

Notice that $\left(n_{b}+1\right)=7$ here, rather than 14 , because the flow traverses only half the length of the J-shell.

$$
\Delta P_{f}=\bar{\phi}_{V O}^{2}\left(\Delta P_{f}\right)_{V O}=0.33 \times 9.24=3.05 \mathrm{psi}
$$

Assuming 10-in. schedule 40 nozzles for the vapor and allowing one velocity head for the inlet loss gives:

$$
\begin{aligned}
G_{n, i n} & =\frac{90,000}{(\pi / 4)(10.02 / 12)^{2}}=164,354 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{n, \text { in }} & =1334 \times 10^{-13} G_{n, \text { in }}^{2} / s_{V}=\frac{1.334 \times 10^{-13}(164,354)^{2}}{(0.845 / 62.43)} \\
\Delta P_{n, \text { in }} & =0.266 \mathrm{psi}
\end{aligned}
$$

For the condensate, a 6 -in. schedule 40 nozzle is assumed and half a velocity head is allowed for the exit loss. Thus,

$$
\begin{aligned}
G_{n, \text { out }} & =\frac{180,000}{(\pi / 4)(6.065 / 12)^{2}}=897,188 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{n, \text { out }} & =0.5 \times 1.334 \times 10^{-13} G_{n, \text { out }}^{2} / s_{L}=0.5 \times 1.334 \times 10^{-13}(897,188)^{2} / 0.57 \\
\Delta P_{n, \text { out }} & =0.094 \mathrm{psi}
\end{aligned}
$$

The total shell-side pressure drop is:

$$
\Delta P_{o}=\Delta P_{f}+\Delta P_{n, \text { in }}+\Delta P_{n, \text { out }}=3.05+0.266+0.094 \cong 3.4 \mathrm{psi}
$$

All design criteria are satisfied and the over-design is approximately $3.5 \%$. Hence, the unit is acceptable as configured.

## Final design summary

Tube-side fluid: cooling water
Shell-side fluid: condensing hydrocarbons
Shell: Type AJU, 39 in. ID, oriented horizontally
Number of tubes: 1336
Tube size: 0.75 in . OD, $16 \mathrm{BWG}, 16$-ft long
Tube layout: 15/16-in. triangular pitch
Tube passes: 4
Baffles: 35\% cut segmental type with vertical cut; middle baffle is full circle
Baffle spacing: approximately 13.7 in.
Number of baffles: 13
Sealing strips: as required based on detailed tube layout
Tube-side nozzles: $10-\mathrm{in}$. schedule 40 inlet and outlet
Shell-side nozzles: two $10-\mathrm{in}$. schedule 40 inlet (top), one 6 -in. schedule 40 outlet (bottom)
Materials: Tubes and tubesheets, $90 / 10$ copper-nickel alloy; all other components, carbon steel
Note: An additional nozzle must be provided on the shell (top middle) for venting non-condensable gases. A 2-in. nozzle should be adequate for this purpose. If condensate is to drain from the unit by gravity, a larger shell-side outlet nozzle should be provided; refer to Appendix 11.B for details. (See also Problem 11.42.)

## Example 11.7

Design a finned-tube condenser for the service of Example 11.6.

## Solution

(a) Make initial specifications.

The following changes are made to the initial specifications of Example 11.6.
(i) Shell and head types

Based on the results of Example 11.6 and the fact that a smaller shell will result from the use of finned tubes, difficulty in meeting the shell-side pressure drop specification while providing adequate tube support is anticipated. Therefore, a cross-flow shell is selected and an AXU configuration is specified.
(ii) Tubing

Referring to Table B.5, $3 / 4$-in, 16BWG, 26 fpi tubing is selected; the corresponding part number is 265065. A tube length of 16 ft and a triangular layout with tube pitch of 15/16 in. are also specified.
(iii) Baffles

Tube support plates are used in a cross-flow exchanger rather than standard baffles. A sufficient number of plates must be provided for adequate tube support and suppression of tube vibration. Considering the potential for tube vibration problems in this application, a plate spacing of 24 in . is a reasonable initial estimate, but this figure has no effect on the thermal or hydraulic calculations.
(b) Energy balances.

From Example 11.6 we have:

$$
\begin{aligned}
q & =25.74 \times 10^{6} \mathrm{Btu} / \mathrm{h} \\
\dot{m}_{\text {water }} & =735,729 \mathrm{lbm} / \mathrm{h}
\end{aligned}
$$

(c) Mean temperature difference.

The following data are obtained from Example 11.6:

$$
\begin{aligned}
\left(\Delta T_{\ln }\right)_{c f} & =72.8^{\circ} \mathrm{F} \\
R & =0.443 \quad P=0.355
\end{aligned}
$$

The LMTD correction factor chart for an X-shell in Appendix 11.A is for a single tube pass; no chart is available for an X-shell with an even number of tube passes. However, with the given values of $R$ and $P, F$ will not differ greatly from the value of approximately 0.98 for a single tube pass. Therefore,

$$
\Delta T_{m} \cong 0.98 \times 72.8=71.3^{\circ} \mathrm{F}
$$

(d) Approximate overall heat-transfer coefficient.

Based on the results of Example 11.6, the following values are estimated for the film coefficients:

$$
h_{i} \cong 1000 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \quad h_{o} \cong 250 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

The value of $h_{o}$ for finned tubes is expected to be significantly higher than the value of $132 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ calculated for plain tubes, while the value of $h_{i}$ should be similar to that for plain tubes ( $1085 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}{ }^{2} \cdot{ }^{\circ} \mathrm{F}$ ). The following data are obtained from Table B. 5 for \#265065 finned tubes:

$$
\begin{aligned}
A_{T o t} / L & =0.596 \mathrm{ft}^{2} / \mathrm{ft}=\text { external surface area per unit length } \\
A_{T o t} / A_{i} & =4.35
\end{aligned}
$$

$$
\begin{aligned}
& D_{r}=0.652 \mathrm{in} .=0.0543 \mathrm{ft}=\text { root-tube diameter } \\
& D_{i}=0.522 \text { in. }=0.0435 \mathrm{ft}
\end{aligned}
$$

Using Equation (4.25) and assuming $\eta_{w} \cong 1.0$ we obtain:

$$
\begin{aligned}
U_{D} & =\left[\frac{A_{T o t}}{h_{i} A_{i}}+\frac{R_{D i} A_{T o t}}{A_{i}}+\frac{A_{T o t} \ln \left(D_{r} / D_{i}\right)}{2 \pi k_{t u b e} L}+\frac{1}{h_{o} \eta_{w}}+\frac{R_{D o}}{\eta_{w}}\right]^{-1} \\
& =\left[\frac{4.35}{1000}+0.001 \times 4.35+\frac{0.596 \ln (0.652 / 0.522)}{2 \pi \times 30}+\frac{1}{250 \times 1.0}+\frac{0.0005}{1.0}\right]^{-1} \\
U_{D} & =72 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot \circ \mathrm{~F}
\end{aligned}
$$

(e) Heat-transfer area and number of tubes.

$$
\begin{aligned}
& A=\frac{q}{U_{D} \Delta T_{m}}=\frac{25.74 \times 10^{6}}{72 \times 71.3}=5014 \mathrm{ft}^{2} \\
& n_{t}=\frac{A}{\left(A_{\text {Tot }} / L\right) \times L}=\frac{5014}{0.596 \times 16}=526
\end{aligned}
$$

(f) Number of tube passes.

Assuming two tube passes, the velocity is:

$$
V=\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\rho \pi\left(D_{i}^{2} / 4\right)}=\frac{(735,429 / 3600)(2 / 526)}{0.99 \times 62.43 \times \pi(0.0435)^{2} / 4}=8.5 \mathrm{ft} / \mathrm{s}
$$

Since the velocity is in the acceptable range for the tubing material, two tube passes will be used.
(g) Shell size and tube count.

From Table B. 6 , the closest tube count is 534 tubes in a $25-\mathrm{in}$. shell. In order to provide adequate entrance and distribution space for the vapor, however, the next largest shell ( 27 in .) will be used with this tube bundle.
(h) Required overall coefficient.

$$
U_{\text {req }}=\frac{q}{n_{t}\left(A_{\text {Tot }} / L\right) \Delta T_{m}}=\frac{25.74 \times 10^{6}}{534 \times 0.596 \times 16 \times 71.3}=71 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(i) Calculate $h_{i}$ assuming $\phi_{i}=1.0$.

$$
\begin{aligned}
R e & =\frac{4 \dot{m}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 735,429(2 / 534)}{\pi \times 0.0435 \times 0.72 \times 2.419}=46,289 \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =(0.37 / 0.0435) \times 0.023(46,289)^{0.8}(4.707)^{1 / 3} \times 1.0 \\
h_{i} & =1770 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(j) Calculate $h_{o}$.

For finned tubes, the equivalent diameter defined by Equation (11.60) is required:

$$
D_{e}^{-0.25}=\frac{1.30 \eta_{f} A_{\text {fins }} E^{-0.25}+A_{\text {prime }} D_{r}^{-0.25}}{\eta_{w} A_{\text {Tot }}}
$$

The fin efficiency for low-fin tubes is usually quite high unless the material of construction has a relatively low thermal conductivity. Therefore, $\eta_{f}$ and $\eta_{w}$ can be set to unity as a first approximation. The remaining parameters are calculated from the tube and fin dimensions:

$$
\begin{aligned}
& E=\pi\left(r_{2}^{2}-r_{1}^{2}\right) / 2 r_{2} \\
& r_{1}=D_{r} / 2=0.652 / 2=0.326 \mathrm{in} . \\
& r_{2}=0.75 / 2=0.375 \mathrm{in} . \\
& E=\pi\left\{(0.375)^{2}-(0.326)^{2}\right\} /(2 \times 0.375) \\
& E=0.14388 \mathrm{in} .=0.0120 \mathrm{ft}
\end{aligned}
$$

For convenience, the fin and prime surface areas are calculated per inch of tube length:

$$
\begin{aligned}
A_{\text {fins }} & =2 N_{f} \pi\left(r_{2}^{2}-r_{1}^{2}\right)=2 \times 26 \pi\left\{(0.375)^{2}-(0.326)^{2}\right\}=5.611 \mathrm{in} .{ }^{2} \\
\tau & =\text { fin thickness }=0.013 \text { in. (Table B.5) } \\
A_{\text {prime }} & =2 \pi r_{1}\left(L-N_{f} \tau\right)=2 \pi \times 0.326(1.0-26 \times 0.013)=1.356 \mathrm{in} .^{2} \\
A_{\text {fins }} / A_{T o t} & =5.611 /(5.611+1.356)=0.805 \\
A_{\text {prime }} / A_{T o t} & =1-A_{\text {fins }} / A_{\text {Tot }}=0.195
\end{aligned}
$$

Substituting into the above equation for $D_{e}$ gives:

$$
\begin{aligned}
D_{e}^{-0.25} & =\frac{1.30 \times 1.0 \times 0.805(0.0120)^{-0.25}+0.195(0.0543)^{-0.25}}{1.0}=3.5658 \mathrm{ft}^{-0.25} \\
D_{e} & =(3.5658)^{-4}=0.0062 \mathrm{ft}
\end{aligned}
$$

Next, the modified condensate loading is computed:

$$
\Gamma^{*}=\frac{W}{L\left(n_{t}\right)^{2 / 3}}=\frac{180,000}{16(534)^{2 / 3}}=170.92 \mathrm{lbm} / \mathrm{ft} \cdot \mathrm{~h}
$$

From Example 11.6, a tube wall temperature of $112^{\circ} \mathrm{F}$ is assumed, which gives $T_{f}=128^{\circ} \mathrm{F}$ and $\mu_{L}=0.161 \mathrm{cp}$. The shell-side heat-transfer coefficient is calculated using Equation (11.63) with $\Gamma$ replaced by $\Gamma^{*}$ :

$$
\begin{aligned}
h_{o} & =0.609\left[\frac{k_{L}^{3} \rho_{L}\left(\rho_{L}-\rho_{V}\right) g \eta_{w}\left(A_{T o t} / L\right)}{\mu_{L} D_{e} \Gamma^{*}}\right]^{1 / 3} \\
& =0.609\left[\frac{(0.057)^{3} \times 35.5(35.5-0.845) \times 4.17 \times 10^{8} \times 1.0 \times 0.596}{0.161 \times 2.419 \times 0.0062 \times 170.92}\right]^{1 / 3} \\
h_{o} & =314 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(k) Calculate $T_{p}, T_{w t d}$, and $T_{f}$.

For $\eta_{w}=1.0$, Equations (4.38) and (4.39) give:

$$
\begin{aligned}
& T_{p}=T_{w t d}=\frac{h_{i} t_{\text {ave }}+h_{o}\left(A_{\text {Tot }} / A_{i}\right) T_{\text {ave }}}{h_{i}+h_{o}\left(A_{\text {Tot }} / A_{i}\right)}=\frac{1770 \times 102.5+314 \times 4.35 \times 175.75}{1770+314 \times 4.35} \\
& T_{p}=T_{w t d}=134.4^{\circ} \mathrm{F} \\
& T_{f}=0.75 T_{w t d}+0.25 T_{V}=0.75 \times 134.4+0.25 \times 175.75 \cong 145^{\circ} \mathrm{F}
\end{aligned}
$$

At this value of $T_{f}, \mu_{L}=0.148 \mathrm{cp}$. Using this value to recalculate $h_{o}$ and the wall temperatures gives:

$$
\begin{aligned}
& h_{o}=323 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} \\
& T_{p}=T_{w t d}=134.9^{\circ} \mathrm{F} \\
& T_{f}=145.1^{\circ} \mathrm{F}
\end{aligned}
$$

Since the two values of $T_{f}$ are essentially the same, no further iteration is required.
(1) Calculate fin efficiency.

Equation (2.27) is used to calculate the fin efficiency.

$$
\begin{aligned}
r_{2 c} & =r_{2}+\tau / 2=0.375+0.013 / 2=0.3815 \mathrm{in} . \\
\tau & =0.013 / 12=0.001083 \mathrm{ft} \\
\psi & =\left(r_{2 c}-r_{1}\right)\left[1+0.35 \ln \left(r_{2 c} / r_{1}\right)\right]=(0.3815-0.326)[1+0.35 \ln (0.3815 / 0.326)] \\
\psi & =0.5855 \mathrm{in} .=0.004879 \mathrm{ft} \\
m & =\left(2 h_{o} / k \tau\right)^{0.5}=(2 \times 323 / 30 \times 0.001083)^{0.5}=141.0 \mathrm{ft}^{-1} \\
m \psi & =141.0 \times 0.004879=0.6879 \\
\eta_{f} & =\tanh (m \psi) /(m \psi)=\tanh (0.6879) / 0.6879=0.867
\end{aligned}
$$

The weighted efficiency of the finned surface is computed using Equation (2.31):

$$
\eta_{w}=\left(A_{\text {prime }} / A_{\text {Tot }}\right)+\eta_{f}\left(A_{\text {fins }} / A_{\text {Tot }}\right)=0.195+0.867 \times 0.805 \cong 0.893
$$

(m) Recalculate $h_{o}$ and fin efficiency.

Repeating steps ( j ) and ( k ) with $\eta_{f}=0.867$ and $\eta_{w}=0.893$ yields the following results:

$$
\begin{array}{rlr}
D_{e} & =0.0065 \mathrm{ft} & T_{p}
\end{array}=132.2^{\circ} \mathrm{F} \quad T_{f}=146.6^{\circ} \mathrm{F}
$$

Repeating step (l) with the new value of $h_{o}$ gives:

$$
\eta_{f}=0.871 \quad \eta_{w}=0.896
$$

Since the new values of efficiency are essentially the same as the previous set, no further iteration is required and the above results are accepted as final.
(n) Viscosity correction factor for cooling water.

At $132^{\circ} \mathrm{F}$, the viscosity of water is 0.52 cp from Figure A.1. Hence,

$$
h_{i}=1770(0.72 / 0.52)^{0.14}=1853 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}
$$

(o) Overall heat-transfer coefficient.

$$
\begin{aligned}
U_{D} & =\left[\frac{A_{\text {Tot }}}{h_{i} A_{i}}+\frac{R_{D i} A_{\text {Tot }}}{A_{i}}+\frac{\left(A_{\text {Tot }} / L\right) \ln \left(D_{r} / D_{i}\right)}{2 \pi k_{\text {tube }}}+\frac{1}{h_{o} \eta_{w}}+\frac{R_{D o}}{\eta_{w}}\right]^{-1} \\
& =\left[\frac{4.35}{1852}+0.001 \times 4.35+\frac{0.596 \ln (0.652 / 0.522)}{2 \pi \times 30}+\frac{1}{311 \times 0.896}+\frac{0.0005}{0.896}\right]^{-1} \\
U_{D} & =86.6 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot \circ \mathrm{~F}
\end{aligned}
$$

(p) Correction for sensible heat transfer.

The effect of sensible heat transfer is neglected here since the effects of interfacial shear and condensate subcooling have also been neglected, which will compensate for this factor. Therefore, since $U_{D}>U_{\text {req }}$, the condenser is thermally acceptable, but somewhat over-sized (over-design $=22 \%$ ).
(q) Tube-side pressure drop.

$$
\begin{aligned}
f & =0.4137 R e^{-0.2585}=0.4137(46,289)^{-0.2585}=0.0257 \\
G & =\frac{\dot{m}\left(n_{p} / n_{t}\right)}{A_{f}}=\frac{735,429(2 / 534)}{(\pi / 4)(0.0435)^{2}}=1,853,366 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.0257 \times 2 \times 16(1,853,366)^{2}}{7.50 \times 10^{12} \times 0.0435 \times 0.99 \times 1.0} \\
\Delta P_{f} & =8.40 \mathrm{psi} \\
\Delta P_{r} & =1.334 \times 10^{-13}\left(1.6 n_{P}-1.5\right) G^{2} / \mathrm{s} \\
& =1.334 \times 10^{-13}(1.6 \times 2-1.5)(1,853,366)^{2} / 0.99 \\
\Delta P_{r} & =0.79 \mathrm{psi}
\end{aligned}
$$

Assuming 10-in. schedule 40 nozzles are used, the nozzle losses will be the same as calculated in Example 11.6, namely:

$$
\Delta P_{n}=0.36 \mathrm{psi}
$$

The total tube-side pressure drop is:

$$
\begin{aligned}
& \Delta P_{i}=\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=8.4+0.79+0.36 \\
& \Delta P_{i} \cong 9.6 \mathrm{psi}
\end{aligned}
$$

(r) Shell-side pressure drop.

The ideal tube bank correlations in Chapter 6 can be used to calculate the pressure drop in a cross-flow shell. The cross-flow area, $S_{m}$, is approximated by $a_{s}$ with the baffle spacing equal to the length of the shell. For finned tubes, an effective clearance is used that accounts for the area occupied by the fins:

$$
C_{e f f}^{\prime}=P_{T}-D_{r e}
$$

where
$D_{r e}=D_{r}+2 n_{f} b \tau=$ equivalent root-tube diameter
$n_{f}=$ number of fins per unit length

Note that $B C_{\text {eff }}^{\prime}$ is the flow area between two adjacent tubes in one baffle space. Substituting the values of the parameters in the present problem gives:

$$
\begin{aligned}
D_{r e} & =0.652+2 \times 26 \times 0.049 \times 0.013=0.6851 \mathrm{in} \\
C_{e f f}^{\prime} & =15 / 16-0.6851=0.2524 \mathrm{in} \\
a_{s} & =\frac{d_{s} C_{e f f}^{\prime} B}{144 P_{T}}=\frac{27 \times 0.2524 \times(16 \times 12)}{144 \times 15 / 16}=9.69 \mathrm{ft}^{2} \\
G & =\dot{m}_{V} / a_{s}=180,000 / 9.69=18,576 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
\end{aligned}
$$

In calculating the Reynolds number for finned tubes, the equivalent root-tube diameter is used in place of $D_{o}$ [31]:

$$
R e_{V}=\frac{D_{r e} G}{\mu_{V}}=\frac{(0.6851 / 12) \times 18,576}{0.0085 \times 2.419}=51,579
$$

The friction factor for plain tubes is obtained from Figure 6.2: $f_{\text {ideal }}=0.10$. The friction factor for finned tubes is estimated as 1.4 times the value for plain tubes [31]. Thus,

$$
f_{\text {ideal }}^{\prime}=1.4 f_{\text {ideal }}=1.4 \times 0.10=0.14
$$

The number of tube rows crossed is estimated using Equation (6.8) with the baffle cut taken as zero and a shell ID of 25 in ., rather than the actual ID of 27 in ., to more accurately represent the size of the tube bundle.

$$
N_{c}=\frac{d_{s}\left(1-2 B_{c}\right)}{P_{T} \cos \theta_{t p}}=\frac{25}{(15 / 16) \cos 30^{\circ}}=30.8
$$

The pressure drop for all-vapor flow is calculated using Equation (6.7). The effect of the bundle bypass flow is neglected here:

$$
\begin{aligned}
& \left(\Delta P_{f}\right)_{V O}=\frac{2 f_{\text {ideal }}^{\prime} N_{c} G^{2}}{g_{c} \rho_{V} \phi}=\frac{2 \times 0.14 \times 30.8(18,576)^{2}}{4.17 \times 10^{8} \times 0.845 \times 1.0} \\
& \left(\Delta P_{f}\right)_{V O}=8.45 \mathrm{lbf} / \mathrm{ft}^{2}=0.059 \mathrm{psi}
\end{aligned}
$$

The two-phase friction loss is calculated using an average two-phase multiplier of 0.33 for a total condenser:

$$
\Delta P_{f}=\bar{\phi}_{V O}^{2}\left(\Delta P_{f}\right)_{V O}=0.33 \times 0.059=0.019 \mathrm{psi}
$$

As would be expected, the pressure drop in the X -shell is very small. Assuming two $10-\mathrm{in}$. schedule 40 inlet nozzles are used, the nozzle losses will be the same as calculated in Example 11.6, namely:

$$
\Delta P_{n, \text { in }}=0.266 \mathrm{psi}
$$

Assuming two 4-in. schedule 40 nozzles are used for the condensate and allowing half a velocity head for the exit loss, we obtain:

$$
G_{n, o u t}=\frac{0.5 \dot{m}}{(\pi / 4) D_{n}^{2}}=\frac{0.5 \times 180,000}{(\pi / 4)(4.026 / 12)^{2}}=1,018,046 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}
$$

$$
\begin{aligned}
\Delta P_{n, \text { out }} & =0.5 \times 1.334 \times 10^{-13} G_{n, \text { out }}^{2} / s_{L} \\
& =0.5 \times 1.334 \times 10^{-13}(1,018,046)^{2} / 0.57 \\
\Delta P_{n, \text { out }} & =0.121 \mathrm{psi}
\end{aligned}
$$

The total shell-side pressure drop is:

$$
\begin{aligned}
& \Delta P_{o}=\Delta P_{f}+\Delta P_{n, \text { in }}+\Delta P_{n, \text { out }}=0.019+0.266+0.121 \\
& \Delta P_{o}=0.41 \mathrm{psi}
\end{aligned}
$$

All design criteria are satisfied; however, the condenser is somewhat over-sized. The number of tubes cannot be reduced because the tube-side pressure drop is close to the maximum. Therefore, we consider using shorter tubes. The required tube length is:

$$
\begin{aligned}
& L_{r e q}=\frac{q}{\left(A_{\text {Tot }} / L\right) n_{t} U_{D} \Delta T_{m}}=\frac{25.74 \times 10^{6}}{0.596 \times 534 \times 86.6 \times 71.3} \\
& L_{r e q}=13.1 \mathrm{ft}
\end{aligned}
$$

Hence, the tube length is reduced to 14 ft . This change will decrease the tube-side pressure drop and increase the shell-side pressure drop slightly. Although these changes will not affect the viability of the design, the new pressure drops are calculated here for completeness. For the tube side, we have:

$$
\begin{aligned}
\Delta P_{f} & =8.40(14 / 16)=7.35 \mathrm{psi} \\
\Delta P_{i} & =\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=7.35+0.79+0.36 \\
\Delta P_{i} & =8.5 \mathrm{psi}
\end{aligned}
$$

For the shell side:

$$
\begin{aligned}
a_{s} & =\frac{27 \times 0.2524(14 \times 12)}{144(15 / 16)}=8.48 \mathrm{ft}^{2} \\
G & =180,000 / 8.48=21,226 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e & =\frac{(0.6851 / 12) \times 21,226}{0.0085 \times 2.419}=58,937 \\
f_{\text {ideal }} & \cong 0.098(\text { Figure } 6.2) \\
f_{\text {ideal }}^{\prime} & =1.4 f_{\text {ideal }}=1.4 \times 0.098=0.137 \\
\left(\Delta P_{f}\right)_{V O} & =\frac{2 \times 0.137 \times 30.8(21,226)^{2}}{4.17 \times 10^{8} \times 0.845 \times 1.0} \\
\left(\Delta P_{f}\right)_{V O} & =10.8 \mathrm{lbf} / \mathrm{ft}^{2}=0.075 \mathrm{psi} \\
\Delta P_{f} & =0.33 \times 0.075=0.025 \mathrm{psi} \\
\Delta P_{o} & =0.025+0.266+0.121 \cong 0.41 \mathrm{psi}
\end{aligned}
$$

The final design parameters are summarized below.

## Final design summary

Tube-side fluid: cooling water
Shell-side fluid: condensing hydrocarbon
Shell: type AXU, 27-in. ID, oriented horizontally
Number of tubes: 534
Tube size: 0.75 in., 16 BWG, radial low-fin tubes, 14 ft long
Fins: 26 fpi, 0.049 in. high, 0.013 in. thick
Tube layout: 15/16-in. triangular pitch
Tube passes: 2
Baffles/support plates: 6 support plates (subject to revision pending vibration analysis)
Sealing strips: as needed based on tube layout
Tube-side nozzles: $10-\mathrm{in}$. schedule 40 inlet and outlet
Shell-side nozzles: two $10-\mathrm{in}$. schedule 40 inlet (top), two 4 -in. schedule 40 outlet (bottom)
Materials: tubes and tubesheets, 90/10 copper-nickel alloy; all other components, carbon steel
Note: An additional nozzle must be provided on the shell (top middle) for venting non-condensable gases. A 2-in. nozzle should be adequate for this purpose. If condensate is to drain by gravity, larger outlet nozzles should be provided (see Appendix 11.B and Problem 11.42).

### 11.10 Multi-component Condensation

### 11.10.1 The general problem

Analysis of the condensation process for a general multi-component mixture entails a much greater level of complexity compared to pure-component condensation. Among the factors responsible for the added complexity are the following:

- As previously noted, multi-component condensation is always non-isothermal, and the condensing range can be large (greater than $100^{\circ} \mathrm{F}$ ). Thus, there are sensible heat effects in both the vapor and liquid phases. Sensible heat transfer in the vapor phase can have a significant effect on the condensation process due to the low heat-transfer coefficients that are typical for gases.
- The compositions of both phases vary from condenser inlet to outlet because the less volatile components condense preferentially. As a result, the physical properties of both phases can vary significantly over the length of the condenser.
- As discussed in the previous section, the condensing curve may be highly nonlinear, invalidating the use of the LMTD correction factor for calculating the mean temperature difference.
- Thermodynamic (equilibrium flash) calculations are required to obtain the condensing curve and determine the phase compositions. Equilibrium ratios (K-values) and enthalpies are needed for this purpose, and the mixture may be highly non-ideal.
- Equilibrium exists at the vapor-liquid interface, not between the bulk phases. Hence, the thermodynamic calculations should be performed at the interfacial temperature, which is unknown.
- Since the interfacial composition differs from the bulk phase compositions, there are masstransfer as well as heat-transfer resistances in both the vapor and liquid phases. Therefore, mass-transfer coefficients are needed in addition to heat-transfer coefficients in order to model the process. Furthermore, the heat and mass-transfer effects are coupled, and the equations describing the transport processes are complex. Thus, there are computational difficulties involved, as well as a lack of data for mass-transfer coefficients.

A rigorous formulation of the general multi-component condensation problem has been presented by Taylor et al. [32]. Due to the inherent complexity of the model, however, it has not been widely
used for equipment design. An approximate method developed by Bell and Ghaly [33] has formed the basis for the condenser algorithms used in most commercial software packages. This method is described in the following subsection.

### 11.10.2 The Bell-Ghaly method

The Bell-Ghaly method neglects the mass-transfer resistances, but attempts to compensate by overestimating the thermal resistances, primarily the vapor-phase resistance. The following approximations are made [33]:

- Vapor and liquid phases are assumed to be in equilibrium at the temperature, $T_{V}$, of the bulk vapor phase, rather than at the interfacial temperature. Thus, the thermodynamic calculations are performed at $T_{V}$.
- The liquid and vapor properties are assumed to be those of the equilibrium phases at temperature $T_{V}$.
- The heat-transfer coefficient for sensible heat transfer in the vapor phase is calculated assuming that the vapor flows alone through the condenser. In effect, a two-phase multiplier of unity is assumed for vapor-phase heat transfer, which tends to significantly overestimate the corresponding thermal resistance.
- The entire heat load (latent and sensible heats) is assumed to be transferred through the entire thickness of the condensate film. This assumption produces a slight overestimation of the thermal resistance in the liquid phase.

A differential analysis is employed. The rate of heat transfer from the bulk vapor phase to the vapor-liquid interface in a differential condenser element of area $d A$ is:

$$
\begin{equation*}
d q_{V}=h_{V} d A\left(T_{V}-T_{s a t}\right) \tag{11.69}
\end{equation*}
$$

where
$d q_{V}=$ rate of sensible heat transfer in element of area $d A$ due to vapor cooling
$h_{V}=$ vapor-phase heat-transfer coefficient
The total rate of heat transfer in the differential element is given by:

$$
\begin{equation*}
d q=U_{D} d A\left(T_{s a t}-T_{c}\right) \tag{11.70}
\end{equation*}
$$

where
$d q=$ total rate of heat transfer in element of area $d A$
$U_{D}=$ overall coefficient between the vapor-liquid interface and the coolant, including fouling allowances
$T_{c}=$ coolant temperature
Equation (11.69) can be solved for the interfacial temperature to yield:

$$
\begin{equation*}
T_{s a t}=T_{V}-\left(1 / h_{V}\right) \frac{d q_{V}}{d A} \tag{11.71}
\end{equation*}
$$

Substituting this expression for $T_{s a t}$ in Equation (11.70) gives:

$$
\begin{align*}
& d q=U_{D} d A\left(T_{V}-T_{c}-\left(1 / h_{V}\right) \frac{d q_{V}}{d A}\right) \\
& d q=U_{D} d A\left(T_{V}-T_{c}\right)-\frac{U_{D} d q_{V}}{h_{V}} \tag{11.72}
\end{align*}
$$

Now let $\Lambda \equiv d q_{V} / d q$ and substitute in Equation (11.72) to obtain:

$$
\begin{align*}
& d q=U_{D} d A\left(T_{V}-T_{c}\right)-\left(U_{D} \Lambda / h_{V}\right) d q \\
& d q\left(1+U_{D} \Lambda / h_{V}\right)=U_{D} d A\left(T_{V}-T_{c}\right) \tag{11.73}
\end{align*}
$$

Solving Equation (11.73) for $d A$ yields:

$$
\begin{equation*}
d A=\frac{\left(1+U_{D} \Lambda / h_{V}\right)}{U_{D}\left(T_{V}-T_{c}\right)} d q \tag{11.74}
\end{equation*}
$$

The total heat-transfer area is obtained by integrating Equation (11.74) from $q=0$ to $q=q_{\text {Tot }}$, where $q_{T o t}$ is the total duty:

$$
\begin{equation*}
A=\int_{0}^{A} d A=\int_{0}^{q_{T o t}} \frac{\left(1+U_{D} \Lambda / h_{V}\right)}{U_{D}\left(T_{V}-T_{c}\right)} d q \tag{11.75}
\end{equation*}
$$

In practice the design integral is evaluated numerically by performing an incremental analysis. For counter-current flow of vapor and coolant, the computational procedure is straightforward, while for multi-pass condensers it is somewhat more involved. Procedures for both cases are given in Ref. [33]. Due to the complexity of the overall procedure, which includes the thermodynamic calculations, implementation is practical only with the use of commercial software.

Bell and Ghaly [33] report that tests of the method using the HTRI data bank showed that it gives results for the heat-transfer area that range from correct to about $100 \%$ high. They also state that proprietary modifications of the method made by HTRI greatly improve the accuracy.

Following is a highly simplified example designed to illustrate the basic computational procedure.

## Example 11.8

$100,000 \mathrm{lb} / \mathrm{h}$ of saturated vapor consisting of 30 mole percent n-butane and 70 mole percent n-pentane are to be condensed at a pressure of 75 psia . A single-pass horizontal shell-and-tube condenser will be used with the condensing vapor in the shell. Cooling water with a range of $85-120^{\circ} \mathrm{F}$ will flow in the tubes. The flow area across the tube bundle is $a_{s}=0.572 \mathrm{ft}^{2}$, the equivalent diameter is $D_{e}=0.06083 \mathrm{ft}$ and the baffle spacing is $B / d_{s}=0.45$. The bundle contains $107 \mathrm{ft}^{2}$ of external surface area per foot of length. The overall heat-transfer coefficient between the vapor-liquid interface and coolant is $U_{D}=120 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Use the Bell-Ghaly method to calculate the required surface area and length of the condenser.

## Solution

For convenience, the condensing range $\left(183.5-168^{\circ} \mathrm{F}\right)$ is divided into three intervals: $168-173^{\circ} \mathrm{F}$, $173-178^{\circ} \mathrm{F}$, and $178-183.5^{\circ} \mathrm{F}$. Equilibrium flash calculations are then performed at each of the above four temperatures using a flowsheet simulator (PRO II by SimSci-Esscor). The results are summarized in the following table. (Note that physical properties of the condensate are not required because $U_{D}$ is given in this problem.)

| $T_{V}$ <br> $\left({ }^{\circ} \mathrm{F}\right)$ | $\dot{m}_{V}$ <br> $(\mathrm{lbm} / \mathrm{h})$ | Duty <br> $(\mathrm{Btu} / \mathrm{h})$ | $C_{P, V}$ <br> $\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | $k_{V}$ <br> $\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | $\mu_{V}$ <br> $(\mathrm{cp})$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 183.5 | 100,000 | 0 | 0.486 | 0.01194 | 0.00853 |
| 178 | 54,590 | $6,373,860$ | 0.483 | 0.01185 | 0.00851 |
| 173 | 24,850 | $10,661,170$ | 0.480 | 0.01177 | 0.00850 |
| 168 | 0 | $14,314,980$ | 0.477 | 0.01168 | 0.00848 |

The flow rate of the cooling water is obtained from the overall energy balance:

$$
\dot{m}_{c}=\frac{q}{C_{P, c} \Delta T_{c}}=\frac{14,314,980}{1.0(120-85)}=408,999 \mathrm{lbm} / \mathrm{h}
$$

Next, the temperature profile for the cooling water is determined using energy balances over the individual temperature intervals. Counter-current flow and constant heat capacity of the cooling water are assumed. For the interval from $168^{\circ} \mathrm{F}$ to $173^{\circ} \mathrm{F}$, we have:

$$
\begin{aligned}
\Delta q & =14,314,980-10,661,170=3,653,810 \mathrm{Btu} / \mathrm{h} \\
\Delta T_{c} & =\frac{\Delta q}{\dot{m}_{c} C_{P, c}}=\frac{3,653,810}{408,999 \times 1.0}=8.93^{\circ} \mathrm{F} \\
T_{c, \text { out }} & =85+8.93=93.93^{\circ} \mathrm{F}
\end{aligned}
$$

Similarly, for the interval from $173^{\circ} \mathrm{F}$ to $178^{\circ} \mathrm{F}$ we obtain:

$$
\begin{aligned}
\Delta q & =10,661,170-6,373,860=4,287,310 \mathrm{Btu} / \mathrm{h} \\
\Delta T_{c} & =\frac{4,287,310}{408,999 \times 1.0}=10.48^{\circ} \mathrm{F} \\
T_{c, \text { out }} & =93.93+10.48=104.41^{\circ} \mathrm{F}
\end{aligned}
$$

The temperature profiles of the vapor and cooling water are summarized in the following table.

| $T_{V}\left({ }^{\circ} \mathrm{F}\right)$ | $T_{c}\left({ }^{\circ} \mathrm{F}\right)$ |
| :--- | :--- |
| 183.5 | 120 |
| 178 | 104.41 |
| 173 | 93.93 |
| 168 | 85 |

The calculations for the temperature interval from $168^{\circ} \mathrm{F}$ to $173^{\circ} \mathrm{F}$ are performed next. The rate of sensible heat transfer to cool the vapor in this interval is calculated using the average vapor flow rate and heat capacity for the interval. The averages are:

$$
\begin{aligned}
\bar{C}_{P, V} & =0.5(0.477+0.480)=0.4785 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F} \\
\left(\dot{m}_{V}\right)_{a v e} & =0.5(0+24,850)=12,425 \mathrm{lbm} / \mathrm{h}
\end{aligned}
$$

Hence, the rate of sensible heat transfer is:

$$
\Delta q_{V}=\left(\dot{m}_{V}\right)_{a v e} \bar{C}_{P, V} \Delta T_{V}=12,425 \times 0.4785 \times 5=29,727 \mathrm{Btu} / \mathrm{h}
$$

The value of $\Lambda$ for the interval is:

$$
\Lambda=\Delta q_{V} / \Delta q=29,727 / 3,653,810=0.0081
$$

The Reynolds number for the vapor is computed next using the average vapor flow rate and average viscosity for the interval.

$$
\begin{aligned}
\bar{\mu}_{V} & =0.5(0.00848+0.00850)=0.00849 \mathrm{cp} \\
R e_{V} & =\frac{D_{e}\left\{\left(\dot{m}_{V}\right)_{a v e} / a_{s}\right\}}{\bar{\mu}_{V}}=\frac{0.06083\{12,425 / 0.572\}}{0.00849 \times 2.419}=64,339
\end{aligned}
$$

Equations (3.20) and (3.21) are used to calculated the heat-transfer coefficient for the vapor phase:

$$
\begin{aligned}
j_{H} & =0.5\left(1+B / d_{s}\right)\left(0.08 R e^{0.6821}+0.7 R e^{0.1772}\right) \\
& =0.5(1+0.45)\left\{0.08(64,339)^{0.6821}+0.7(64,339)^{0.1772}\right\} \\
j_{H} & =114.09 \\
\bar{k}_{V} & =0.5(0.01168+0.01177)=0.011725 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F} \\
\operatorname{Pr}_{V} & =\frac{\bar{C}_{P, V} \bar{\mu}_{V}}{\bar{k}_{V}}=\frac{0.4785 \times 0.00849 \times 2.419}{0.011725}=0.8381 \\
h_{V} & =\frac{j_{H} \bar{k}_{V} P_{V}^{1 / 3} \phi}{D_{e}}=\frac{114.09 \times 0.011725(0.8381)^{1 / 3} \times 1.0}{0.06083} \\
h_{V} & =20.7 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} . \circ \mathrm{F}
\end{aligned}
$$

The heat-transfer area required for the temperature interval is obtained from the finite difference form of Equation (11.74) using the average vapor and coolant temperatures:

$$
\begin{aligned}
& \Delta A=\left\{\frac{1+U_{D} \Lambda / h_{V}}{U_{D}\left(T_{V, \text { ave }}-T_{c, \text { ave }}\right)}\right\} \Delta q \\
& \Delta A=\left\{\frac{1+120 \times 0.0081 / 20.7}{120(170.5-89.465)}\right\} \times 3,653,810 \\
& \Delta A=393.4 \mathrm{ft}^{2}
\end{aligned}
$$

The above calculations are repeated for the other two temperature intervals to obtain the results shown in the following table.

| Parameter | Temperature interval |  |  |
| :--- | :--- | :--- | :--- |
|  | $168-173{ }^{\circ} \mathrm{F}$ | $173-178^{\circ} \mathrm{F}$ | $178-183.5^{\circ} \mathrm{F}$ |
| $\left(\dot{m}_{V}\right)_{\text {ave }}(\mathrm{lbm} / \mathrm{h})$ | 12,425 | 39,720 | 77,295 |
| $\Delta q_{V}(\mathrm{Btu} / \mathrm{h})$ | 29,727 | 95,626 | 205,972 |
| $\Delta q(\mathrm{Btu} / \mathrm{h})$ | $3,653,810$ | $4,287,310$ | $6,373,860$ |
| $\Lambda$ | 0.0081 | 0.0223 | 0.0323 |
| $R e_{V}$ | 64,339 | 205,315 | 398,839 |
| $j_{H}$ | 114.09 | 248.23 | 388.46 |
| $h_{V}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 20.7 | 45.5 | 71.7 |
| $T_{V, \text { ave }}\left({ }^{\circ} \mathrm{F}\right)$ | 170.5 | 175.5 | 180.75 |
| $\left.T_{c, \text { ave }}{ }^{\circ} \mathrm{F}\right)$ | 89.465 | 99.17 | 112.205 |
| $\Delta A\left(\mathrm{ft}^{2}\right)$ | 393.4 | 495.6 | 816.8 |

The total heat-transfer area required in the exchanger is the sum of the incremental areas:

$$
A=393.4+495.6+816.8 \cong 1706 \mathrm{ft}^{2}
$$

The required length of the exchanger is:

$$
L=\frac{A}{(A / L)}=\frac{1706}{107}=15.9 \cong 16 \mathrm{ft}
$$

### 11.11 Computer Software

Condenser design can be accomplished using any of the commercial software packages discussed in previous chapters. HEXTRAN, HTFS/Aspen, and HTRI Xchanger Suite are considered in this section.
The shell-and-tube module (STE) in HEXTRAN is used for segmentally baffled or unbaffled condensers. A separate module is available for rod-baffle units, but it supports only single-phase operation on the shell side. The software automatically detects the phase change for a condensing stream and uses the appropriate computational methods. A zone analysis is always performed for applications involving a phase change.

The TASC module of the HTFS/Aspen software package is used for all types of shell-and-tube condensers. Phase changes are automatically detected and the appropriate computational methods are used. An incremental analysis is performed in the axial direction along the length of the condenser. Like HEXTRAN, TASC is unable to handle rod-baffle exchangers with shell-side condensation; only single-phase operation on the shell-side of these units is supported.

The Xist module of the HTRI Xchanger Suite is used for all types of shell-and-tube condensers. The phase change (condensation in this case) is specified on the Process input form. Xist performs a three-dimensional incremental analysis for condensers as well as other types of exchangers. It is also the only program among those considered here that supports two-phase operation on the shell side of rod-baffle exchangers. A number of options for calculating the condensing heat-transfer coefficient are available on the Control/Methods form. The default (RPM) is a proprietary method developed by HTRI and is recommended for all cases. Among the alternatives, the Rose-Briggs method is noteworthy in that it provides improved accuracy for condensation on low-finned tubes. It is an HTRI-modified version of a method available in the open literature [23]. A special method (REFLUX) is also provided for reflux condensers.
The following examples illustrate the use of Xist, TASC, and HEXTRAN for condenser calculations.

## Example 11.9

Use HEXTRAN, TASC, and Xist to rate the final design for the $\mathrm{C}_{4}-\mathrm{C}_{5}$ condenser obtained in Example 11.6, and compare the results with those from the hand calculations.

## Solution

The problem setup in HEXTRAN is done in the usual manner using the data from Example 11.6. The cooling water stream is defined as a Water/Steam stream to invoke the SimSci databank for the thermodynamic data and transport properties of water. The hydrocarbon stream is defined as a compositional stream and the Peng-Robinson equation of state is selected as the principal thermodynamic method. The API method is chosen for liquid density of the hydrocarbon stream, and the Library method is selected for all transport properties to designate that the property values are to be obtained from the program's databank.
A J-shell with two inlet nozzles and one outlet nozzle is designated as type J2 in HEXTRAN. Hence, a type AJ2U exchanger is specified. A single shell-side inlet nozzle is specified because HEXTRAN automatically uses half the total flow rate to calculate the nozzle pressure drop. If two inlet nozzles are specified, the pressure drop is incorrectly calculated. The default settings for calculation
options (TWOPHASE $=$ New and DPSMETHOD $=$ Stream) are used. Zero pairs of sealing strips are specified.

The problem setup in TASC is similar to examples worked in previous chapters. For this calculation, TASC is run in simulation mode. For physical properties of the cooling water, <Water (NEL $40)>$ is selected as the Stream Data Source, and pressure levels of 60 and 50 psia are specified. For the hydrocarbon stream, the COMThermo interface is used and the Peng-Robinson equation of state is selected as the thermodynamic method. A temperature range of $120-185^{\circ} \mathrm{F}$ is specified with 20 data points (under Options). Two pressure levels, 75 and 70 psia are specified.

TASC designates a J-shell with two inlet nozzles and one outlet nozzle as an I-shell. Hence, a type AIU exchanger is specified. For the shell-side inlet nozzles, type Plain + Impingement is specified to indicate that impingement plates are to be used. The orientation of the shell-side nozzles is specified as Top of Shell for the inlet nozzles and Bottom of Shell for the outlet nozzle. Zero pairs of sealing strips are specified.
Xist is run in simulation mode for this case in order to facilitate comparison with the other two programs. Xist designates a J-shell with two inlet nozzles and one outlet nozzle as a J21 shell. Hence, a type AJ21U exchanger is specified on the Geometry/Shell form. On the Geometry/Clearances form, the option for pairs of sealing strips is set to None. On the Geometry/Nozzles form, the shellside inlet nozzles are specified to be on the top of the shell with the outlet nozzle on the opposite side. An impingement plate is specified on the Geometry/Impingement form. VMG Thermo is used for both fluids. For cooling water, the Steam95 property package is selected and pressure levels of 50 and 60 psia are specified. A temperature range of $80-160^{\circ} \mathrm{F}$ is used with 20 data points. For the hydrocarbon stream, the Advanced Peng-Robinson method is chosen with pressure levels of 70 and 75 psia . A temperature range of $85-185^{\circ} \mathrm{F}$ is used with 20 data points.

Results summaries obtained from the three programs are given below, along with the HEXTRAN input file. Data from the output files were used to construct the following table comparing the computer solutions with the hand calculations of Example 11.6. Perusal of this table reveals that the hand calculations for both shell-side heat transfer and pressure drop are very conservative compared with the computer solutions. The basic Nusselt theory was used to calculate $h_{o}$ in Example 11.6, and this method tends to significantly underestimate the heat-transfer coefficient in baffled condensers. Thus, the results for shell-side heat transfer are as expected. The difference in $\Delta P_{o}$ between the hand and computer calculations is primarily due to the difference between the Delaware and Stream Analysis methods in the calculation of the vapor-phase pressure drop, $\left(\Delta P_{f}\right)_{V O}$. The Delaware method yields a value for this problem that is roughly three times the value given by the Stream Analysis method, and this difference is reflected in the Simplified Delaware method that was used in the hand calculations.

| Item | Hand | HEXTRAN | TASC | Xist |
| :--- | :---: | :---: | :---: | :---: |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 1085 | 1143 | 1292 | 1285 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 132 | $240^{* *}$ | 184 | 226 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | $89^{*}$ | $132.7^{* *}$ | 120.8 | 138 |
| $\Delta P_{i}(\mathrm{psi})$ | 6.3 | 7.29 | 6.13 | 6.77 |
| $\Delta P_{o}(\mathrm{psi})$ | 3.4 | 0.62 | 0.96 | 1.55 |
| $\Delta T_{m}\left({ }^{\circ} \mathrm{F}\right)$ | 71.3 | 54.5 | 58.6 | 51.2 |
| $U_{D} \Delta T_{m}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 6346 | 7232 | 7079 | 7066 |

*Corrected for sensible heat transfer
**Area weighted average over all four zones

Although there are significant differences among the results from the three computer programs, they all show that the condenser is over-sized (as evidenced by the large amount of condensate subcooling) and the shell-side pressure drop is quite low. (In checking mode, TASC gives an overdesign of $74 \%$; the corresponding value from Xist is $76 \%$.) HEXTRAN is the least conservative of the
three for both shell-side heat transfer and pressure drop in this case. The tube vibration analyses performed by Xist and TASC both predict flow-induced vibration problems in this exchanger.

The mean temperature difference computed by hand is significantly higher than the values calculated by the computer programs, but this is largely due to the over-sizing, which reduces the difference in outlet temperatures of the two streams in the computer solutions. When the condenser is properly sized in the computer simulations, the mean temperature difference is close to the value estimated by hand (see Example 11.10 below). The same is true when TASC is run in checking mode ( $\Delta T_{m}=74.3^{\circ} \mathrm{F}$ ) or Xist is run in rating mode ( $\Delta T_{m}=70.6^{\circ} \mathrm{F}$ ).

It will be noticed that the inlet temperature of the hydrocarbon stream is given as $184.97^{\circ} \mathrm{F}$ in the TASC results summary, rather then $183.5^{\circ} \mathrm{F}$. This discrepancy is the result of differences in the SimSci and COMThermo thermodynamic packages. The COMThermo Peng-Robinson method gives a condensing range of (approximately) $185-171^{\circ} \mathrm{F}$, whereas the SimSci version used by HEXTRAN gives a range of $183.5-168^{\circ} \mathrm{F}$. TASC automatically adjusts the inlet temperature of the hydrocarbon stream to obtain the specified vapor quality, which is 1.0 in this case.

Xist Output Summary for Example 11.9


## HEXTRAN Input file for Example 11.9

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=EX11-9, PROBLEM=CONDENSER, SITE=
$
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
    ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
    PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
    UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=CP, WT=LB, *
    XDENSITY=API, STDVAPOR=379.490
$
PRINT GENERAL, PROPERTY, STREAM, UNIT, *
        RATE=M
$
CALC PGEN=New, WATER=Saturated
$
$ Component Data Section
$
COMPONENT DATA
$
    LIBID 1, BUTANE /*
        2, PENTANE
$
$
$ Thermodynamic Data Section
$
THERMODYNAMIC DATA
$
    METHODS SET=SET1, KVALUE=PR, ENTHALPY(L) =PR, ENTHALPY(V)=PR, *
                                    DENSITY(L)=API, DENSITY(V)=PR, VISCOS(L)=LIBRARY, *
                                    VISCOS(V)=LIBRARY, CONDUCT(L)=LIBRARY, *
                                    CONDUCT(V)=LIBRARY, SURFACE=LIBRARY
$
    WATER DECANT=ON, SOLUBILITY = Simsci, PROP = Saturated
$
$Stream Data Section
$
STREAM DATA
$
    PROP STRM=1, NAME=1, TEMP=85.00, PRES=60.000, *
            WATER=735429.000
$
    PROP STRM=3, NAME=3, LFRAC(M)=0.001, PRES=75.000, *
                            RATE (W) =180000.000, *
        COMP (M) = 1, 0.3 / *
            2, 0.7, NORMALIZE
$
    PROP STRM=2, NAME=2
$
    PROP STRM=4, NAME=4
$
$ Calculation Type Section
$
SIMULATION
$
    TOLERANCE TTRIAL=0.01
```

```
HEXTRAN Input file for Example 11.9 (continued)
$
    LIMITS AREA=200.00, 6000.00, SERIES=1, 10, PDAMP=0.00, *
        TTRIAL=30
$
    CALC TWOPHASE=New, DPSMETHOD=Stream, MINFT=0.80
$
    PRINT UNITS, ECONOMICS, STREAM, STANDARD, *
        EXTENDED, ZONES
$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR
$
    UTCOST OIL=3.50, GAS=3.50, ELECTRICITY=0.10, *
        WATER=0.03, HPSTEAM=4.10, MPSTEAM=3.90, *
        LPSTEAM=3.60, REFRIGERANT=0.00, HEATINGMEDIUM=0.00
$
    HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        EXPONENT=0.60, CONSTANT=0.00, UNIT
$
$ Unit Operations Data
$
UNIT OPERATIONS
$
STE UID=CONDENSER
    TYPE Old, TEMA=AJ2U, HOTSIDE=Shellside, ORIENTATION=Horizontal, *
    FLOW=Countercurrent, *
    UESTIMATE=50.00, USCALER=1.00
    TUBE FEED=1, PRODUCT=2, *
        LENGTH=16.00, OD=0.750, *
        BWG=16, NUMBER=1336, PASS=4, PATTERN=30, *
        PITCH=0.9380, MATERIAL=32, *
        FOUL=0.001, LAYER=0, *
        DPSCALER=1.00
$
SHELL FEED=3, PRODUCT=4, *
    ID=39.00, SERIES=1, PARALLEL=1, *
    SEALS=0, MATERIAL=1, *
    FOUL=0.0005, LAYER=0, *
    DPSCALER=1.00
$
    BAFF Segmental=Single, *
        CUT=0.35, *
        SPACING=13.700, *
        THICKNESS=0.1875
$
    TNOZZ TYPE=Conventional, ID=10.020, 10.020, NUMB=1, 1
$
    SNOZZ TYPE=Conventional , ID=10.020, 6.065, NUMB=1, 1
$
    CALC TWOPHASE=New, *
        DPSMETHOD=Stream, *
        MINFT=0.80
$
    PRINT STANDARD, *
        EXTENDED, *
        ZONES
$
    COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        CONSTANT=0.00, EXPONENT=0.60, Unit
$
$ End of keyword file...
```


## HEXTRAN Output Data for Example 11.9



## HEXTRAN Output Data for Example 11.9 (continued)


 ZONE ANALYSIS FOR EXCHANGER CONDENSER

| ZONE | TEMPERATURE IN/OUT DEG F |  | PRESSURE |  | IN/OUT PSIA |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | SHELL-SIDE | TUBE-SIDE | SHELL- | IDE | TUB |  |
| 1 | 183.5/ 178.3 | 111.2/ 126.0 | $75.0 /$ | 74 | 955 | 52.7 |
| 2 | 178.3/ 173.1 | 100.3/ 111.2 | $74.9 /$ | 74. |  | 55.3 |
| 3 | 173.1/ 167.8 | 90.9/ 100.3 | $74.8 /$ | 74. |  | 57.3 |
| 4 | 167.8/ 128.9 | 85.0/ 90.9 | $74.8 /$ | 74. |  | 59.0 |

HEAT TRANSFER AND PRESSURE DROP SUMMARY

| ZONE | HEAT TRANSFER MECHANISM | PRESSURE DROP (TOTAL)PSIA |  | FILM COEFF.$\mathrm{BTU} / \mathrm{HR}-\mathrm{FT} 2-\mathrm{F}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | SHELL-SIDE TUBE-SIDE | SHELL-SIDE | TUBE-SIDE | SHELL-SIDE | TUBE-SIDE |
| 1 | CONDENSATION LIQ. HEATING | 0.08 | 2.63 | 400.77 | 1234.75 |
| 2 | CONDENSATION LIQ. HEATING | 0.08 | 1.95 | 263.89 | 1150.49 |
| 3 | CONDENSATION LIQ. HEATING | 0.08 | 1.67 | 174.81 | 1081.78 |
| 4 | LIQ. SUBCOOL LIQ. HEATING | 0.39 | 1.05 | 109.82 | 1025.66 |
|  | TOTAL PRESSURE DROP | 0.62 | 7.29 |  |  |


| HEAT TRANSFER SUMMARY (CONTD.) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ZONE | $\begin{aligned} & ------ \text { DUTY } \\ & \text { MMBTU /HR } \end{aligned}$ | PERCENT | $\begin{gathered} \text { U-VALUE } \\ \text { BTU/HR-FT2-F } \end{gathered}$ | $\begin{array}{r} \text { AREA } \\ \text { FT2 } \end{array}$ | $\begin{aligned} & \text { LMTD } \\ & \text { DEG F } \end{aligned}$ | FT |
| 1 | 10.86 | 36.1 | 184.73 | 1148.3 | 62.1 | 0.824 |
| 2 | 8.05 | 26.7 | 147.51 | 947.7 | 69.9 | 0.824 |
| 3 | 6.88 | 22.9 | 113.93 | 979.1 | 74.8 | 0.824 |
| 4 | 4.32 | 14.4 | 81.81 | 1088.8 | 58.9 | 0.824 |
| TOTAL | 30.11 | 100.0 |  | 4163.9 |  |  |
| WEIGHTED |  |  | 132.70 |  | 66.1 | 0.824 |
| OVERALL |  |  |  |  | 50.4 | 0.824 |
| INSTALLED |  |  |  | 4143.9 |  |  |

```
TOTAL DUTY = (WT. U-VALUE) (TOTAL AREA) (WT. LMTD) (OVL. FT)
    ZONE DUTY = (ZONE U-VALUE) (ZONE AREA) (ZONE LMTD) (OVL. FT)
```


## TASC Results Summary for Example 11.9

## TASC Version 5.01 - SIMULATION

Geometric details

Shell type/series/parallel Shell diam/tube length/total area No of passes/no of plain tubes Tube id/od/pitch (pattern) No of baffles/pitch/cut

Process details
Total mass flowrates shell/tube

| AIU |  | 1 |  | 1 |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 39.0 | in | 192.0 | in | 4481.2 | $\mathrm{ft}^{2}$ |
| 4 |  | 1336 |  |  |  |
| 0.62 | in | 0.75 | in | $0.9375(30)$ | in |
| 13 |  | 13.7 | in | 35 | $\%$ |

$179999.7 \mathrm{lb} / \mathrm{h} \quad 735429.1 \mathrm{lb} / \mathrm{h}$

TASC Results Summary for Example 11.9 (continued)

| Inlet temperature shell/tube | 184.97 | ${ }^{\circ} \mathrm{F}$ | 85.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlet temperature shell/tube | 123.49 | ${ }^{\circ} \mathrm{F}$ | 127.32 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 1.0/0.0 |  | 0.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 0.959 | psi | 6.134 | psi |  |  |
| Velocity highest shell xflow/tube | 32.44 | $\mathrm{ft} / \mathrm{s}$ | 4.74 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 184 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 1068 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 5043 | Btu/h ft ${ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 2000 | Btu/ $\mathrm{ftt}^{2}{ }^{\circ} \mathrm{F}$ | 827 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 152.2 | Btu/ $\mathrm{ftt}^{2} \mathrm{~F}$ | 120.8 | Btu/ $\mathrm{hft}^{2}{ }^{\circ} \mathrm{F}$ | 120.8 | Btu/hft ${ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 31073 | kBtu/h | 58.64 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 1.006 |  | 0.983 |  |  |  |

## Example 11.10

Use TASC to obtain a final design for the $\mathrm{C}_{4}-\mathrm{C}_{5}$ condenser of Example 11.9.

## Solution

Using TASC to rate the 39 -in. J-shell condenser in the previous example, the following problems were identified from the thermal results summary and the detailed output file:

- The condenser is over-sized.
- The end baffle spaces are too small.
- The vibration analysis predicts tube vibration problems.

Due to the propensity for tube vibration problems in this system, finding an acceptable configuration for the condenser is not entirely straightforward. The following design modifications were arrived at after a considerable amount of trial and error.

- The shell size is reduced from 39 to 33 in.
- The number of tubes is left unspecified, allowing TASC to determine the tube count from the tube layout.
- The tube length is reduced from 16 to 15 ft .
- The number of tube passes is reduced from 4 to 2 for compatibility with the lower tube count in the $33-\mathrm{in}$. shell.
- The number of baffles is reduced from 13 to 11.
- The baffle spacing is changed from 13.7 to 13.8 in .
- The baffle cut is increased from $35 \%$ to $40 \%$.
- The number of extra U-bend supports is increased from 0 to 5 .

In order to prevent all types of tube vibration problems while achieving the appropriate degree of shell-side heat transfer requires a rather delicate balance. The cross-flow velocity must be kept low enough to prevent vibration-induced tube damage while providing just the right amount of tube support to avoid resonant vibration frequencies. Adding sealing strips, for example, significantly improves the rate of heat transfer, but the resulting increase in cross-flow velocity causes vibration problems. Likewise, even fairly small changes in baffle cut or baffle spacing result in predicted vibration problems. It should be noted, however, that there is significant uncertainty associated with the vibration analyses in both TASC and Xist. Hence, a predicted vibration problem may not represent a serious problem in practice. More rigorous analyses can be performed using specialized software to confirm the presence of a vibration problem or the lack thereof. (Note: Running TASC in design mode with exchanger type AIU specified does not result in any configurations that are totally free of vibration problems with either $3 / 4-\mathrm{in}$. or $1-\mathrm{in}$. tubes.)

With the above design changes, running TASC in simulation mode shows that all design criteria are satisfied and the only warning message pertains to a low cross-flow fraction in the shell-side flow model. As noted above, this situation is actually advantageous with respect to tube vibration. After
transferring the data to TASC Mechanical, a 2-in. vent nozzle is added to the input data for the shell, and the mechanical design calculations are then executed. No further problems are identified, but the results show that schedule 20 pipe can be used for the tube-side nozzles, while schedule 30 pipe is adequate for the shell-side inlet nozzles. Schedule 160 pipe is required for the vent nozzle. (As an alternative, it is found by rerunning TASC Mechanical that $2.5-\mathrm{in}$. schedule 80 pipe can also be used for this nozzle.) In addition, the tubesheet thickness can be reduced from the value of 2.52 in. calculated by TASC Thermal to 1.97 in. After making these minor changes, rerunning TASC Thermal confirms that the unit is acceptable as configured. The TASC thermal results summary for this case is given below.

## TASC Results Summary for Example 11.10: Design 1 (AJU Condenser)

| TASC Version 5.01 - SIMULATION |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Shell type/series/parallel | AIU |  | 1 |  | 1 |  |
| Shell diam/tube length/total area | 33.0 | in | 180.0 | in | 2707.2 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 2 |  | 870 |  |  |  |
| Tube id/od/pitch (pattern) | 0.62 | in | 0.75 | in | 0.9375(30) | in |
| No of baffles/pitch/cut | 11 |  | 13.8 | in | 40 | \% |
| Process details |  |  |  |  |  |  |
| Total mass flowrates shell/tube | 179999.7 | $\mathrm{lb} / \mathrm{h}$ | 735429.1 | lb/h |  |  |
| Inlet temperature shell/tube | 184.97 | ${ }^{\circ} \mathrm{F}$ | 85.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 169.74 | ${ }^{\circ} \mathrm{F}$ | 120.35 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 1.0/0.0 |  | 0.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 0.826 | psi | 2.003 | psi |  |  |
| Velocity highest shell xflow/tube | 28.17 | $\mathrm{ft} / \mathrm{s}$ | 3.63 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 217 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 852 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 5043 | Btu/hft ${ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 2000 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 827 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 167.0 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 129.9 | Btu/ $\mathrm{fft}^{2}{ }^{\circ} \mathrm{F}$ | 129.9 | Btu/h ft ${ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 25962 | kBtu/h | 74.27 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 0.995 |  | 0.821 |  |  |  |

The J-shell condenser is very prone to tube vibration problems, and there is considerable uncertainty associated with the vibration analysis. Therefore, an X-shell unit is considered in which tube support plates can be used to dampen tube vibrations. Running TASC in design mode with exchanger type AXU specified does not yield a converged solution. In this case, however, it is easy to obtain a good design by trial-and-error. Starting with a $33-\mathrm{in}$. shell and a maximum tube length of 20 ft , the smallest usable shell size is found to be 29 in . with a tube count of 666 . Tube support plates (called intermediate supports in TASC) and extra U-bend supports are then added until the vibration analysis indicates that tube vibration problems have been eliminated. The TASC thermal results summary for this case is shown below.

## TASC Results Summary for Example 11.10: Design 2 (AXU Condenser)

TASC Version 5.01 - SIMULATION

| Geometric details |  |  |  |  | 1 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Shell type/series/parallel | AXU |  | 1 |  |  |  |
| Shell diam/tube length/total area | 29.0 | in | 216.0 | in | 2449.9 | $\mathrm{ft}^{2}$ |
| No of passes/no of plain tubes | 2 |  | 666 |  |  |  |
| Tube id/od/pitch (pattern) | 0.62 | in | 0.75 | in | $0.9375(30)$ | in |
| No of baffles/pitch/cut | 0 | in |  |  | 25 | $\%$ |

TASC Results Summary for Example 11.10: Design 2 (AXU Condenser) (continued)

| Process details |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total mass flowrates shell/tube | 179999.7 | lb/h | 735429.1 | lb/h |  |  |
| Inlet temperature shell/tube | 184.97 | ${ }^{\circ} \mathrm{F}$ | 85.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Outlet temperature shell/tube | 170.48 | ${ }^{\circ} \mathrm{F}$ | 120.24 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Inlet/outlet quality shell/tube | 1.0/0.0 |  | 0.0/0.0 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop shell/tube | 0.537 | psi | 3.402 | psi |  |  |
| Velocity highest shell xflow/tube | 8.38 | $\mathrm{ft} / \mathrm{s}$ | 4.74 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients shell/tube/wall | 228 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 1050 | Btu/hft ${ }^{\circ} \mathrm{F}$ | 5043 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ |
| Fouling coeff shell/tube | 2000 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 827 | $\mathrm{Btu} / \mathrm{hft}{ }^{\circ} \mathrm{F}$ |  |  |
| Overall coefficient clean/dirty/service | 180.3 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ | 137.8 | $\mathrm{Btu} / \mathrm{hft}{ }^{\circ} \mathrm{F}$ | 137.8 | Btu/h $\mathrm{ft}^{2}{ }^{\circ} \mathrm{F}$ |
| Heat load/eff wtd mtd | 25877 | kBtu/h | 75.1 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Area ratio (act/req)/Duty ratio (act/initial) | 0.972 |  | 0.818 |  |  |  |

Design details for both the J -shell and X -shell units are summarized in the table below. Tube layouts and setting plans from TASC Mechanical are also shown. Cost estimates generated by TASC indicate that the J -shell condenser is about $15 \%$ more expensive than the X -shell unit. In addition to being less expensive, the X -shell condenser is much more robust with respect to potential tube vibration problems. Although the over-design for this unit is negligible, the tube length can be increased to provide whatever safety margin is desired. (Note that additional support plates may be required if the tube length is increased.) Since the tube-side pressure drop is quite low, the cooling water flow rate can also be increased to provide a larger mean temperature difference in the exchanger, thereby further enhancing its performance.

| Item | Design 1 | Design 2 |
| :--- | :--- | :--- |
| Exchanger type | AJU | AXU |
| Shell size (in.) | 33 | 29 |
| Surface area (ft ${ }^{2}$ ) | 2707 | 2450 |
| Number of tubes | 870 | 666 |
| Tube OD (in.) | 0.75 | 0.75 |
| Tube length (ft) | 15 | 18 |
| Tube BWG | 16 | 16 |
| Tube passes | 2 | 2 |
| Tube pitch (in.) | $15 / 16$ | $15 / 16$ |
| Tube layout | Triangular | Triangular |
| Tubesheet thickness (in.) | 1.97 | 1.81 |
| Number of baffles | 11 | - |
| Number of support plates | -- | 10 |
| Baffle cut (\%) | 40 | - |
| Baffle thickness (in.) | 0.3125 | - |
| Central baffle spacing (in.) | 13.8 | - |
| End baffle spacing (in.) | 19.76 | 0 |
| Sealing strip pairs | 0 | 10 in. schedule 20 |
| Tube-side nozzles | 10 in. schedule 20 | 10 in. schedule 30 (2) |
| Shell-side inlet nozzles | 10 in. schedule 30 (2) | 5 in. schedule 40 (2) |
| Shell-side outlet nozzle(s) | 6 in. schedule 40 (1) | 2 in. schedule 160 |
| Shell-side vent nozzle | 2 in. schedule 160 | 2 |
| Extra U-bend supports | 5 | 4.7 |
| Tube-side velocity (ft/s) | 3.6 | 34,149 |
| $\left(R e_{i}\right)_{\text {ave }}$ | 26,158 | 3.4 |
| $\Delta P_{i}$ (psi) | 2.0 | 0.54 |
| $\Delta P_{o}$ (psi) | 0.83 |  |

## Setting Plan and Tube Layout for Design 1 (AJU Condenser)



## Setting Plan and Tube Layout for Design 2 (AXU Condenser)



## References

1. Mueller, A. C., Condensers, in Heat Exchanger Design Handbook, Vol.3, Hemisphere Publishing Corp., New York, 1988.
2. Hewitt, G. F., G. L. Shires and T. R. Bott, Process Heat Transfer, CRC Press, Boca Raton, FL, 1994.
3. Kakac, S. and H. Liu, Heat Exchangers: Selection, Rating and Thermal Design, CRC Press, Boca Raton, FL, 1998.
4. Kister, H. Z., Distillation Operation, McGraw-Hill, New York, 1990.
5. Nusselt, W., Die Obertlachenkondensation des Wasserdamtes, parts I and II, Z. Ver. Deut. Ing., 60, 541-546 and 569-575, 1916.
6. Bird, R. B., W. E. Stewart and E. N. Lightfoot, Transport Phenomena, Wiley, New York, 1960.
7. Rose, J., Laminar film condensation of pure vapors, in Handbook of Phase Change: Boiling and Condensation, S. G. Kandlikar, M. Shoji and V. K. Dhir, eds., Taylor and Francis, Philadelphia, 1999.
8. Kern, D. Q., Process Heat Transfer, McGraw-Hill, New York, 1950.
9. Kern, D. Q., Mathematical development of tube loading in horizontal condensers, AIChE J., 4, 157-160, 1958.
10. Butterworth, D., Film condensation of pure vapor, in Heat Exchanger Design Handbook, Vol. 2, Hemisphere Publishing Corp., New York, 1988.
11. Uehara, H., Transition and turbulent film condensation, in Handbook of Phase Change: Boiling and Condensation, S. G. Kandlikar, M. Shoji and V. K. Dhir, eds., Taylor and Francis, Philadelphia, 1999.
12. Sadisivan, P. and J. H. Lienhard, Sensible heat correction in laminar film boiling and condensation, J. Heat Transfer, 109, 545-547, 1987.
13. Chen, M. M., An analytical study of laminar film condensation: Part 1 - flat plates; Part 2 - single and multiple horizontal tubes, J. Heat Transfer, 83, 48-60, 1961.
14. Boyko, L. D. and G. N. Kruzhilin, Heat transfer and hydraulic resistance during condensation of steam in a horizontal tube and in a bundle of tubes, Int. J. Heat Mass Transfer, 10, 361-373, 1967.
15. McNaught, J. M., Two-phase forced convection heat transfer during condensation on horizontal tube bundles, Proc. Seventh Int. Heat Transfer Conf., 5, 125-131, Hemisphere Publishing Corp., New York, 1982.
16. Breber, G., J. W. Palen and J. Taborek, Prediction of horizontal tubeside condensation of pure components using flow regime criteria, J. Heat Transfer, 102, 471-476, 1980.
17. Akers, W. W., H. A. Deans and O. K. Crosser, Condensation heat transfer within horizontal tubes, Chem. Eng. Prog. Symposium Series, 55, No. 29, 171-176, 1959.
18. Akers, W. W. and H. F. Rosson, Condensation inside a horizontal tube, Chem. Eng. Prog. Symposium Series, 56, No. 30, 145-149, 1960.
19. Soliman, M., J. R. Schuster and P. J. Berenson, A general heat transfer correlation for annular flow condensation, J. Heat Transfer, 90, 267-279, 1968.
20. Traviss, D. P., W. M. Rhosenow and A. B. Baron, Forced convection condensation inside tubes: a heat transfer equation for condenser design, ASHRAE Trans., 79, 157-165, 1972.
21. Cavallini, A. and R. Zecchin, A dimensionless correlation for heat transfer in forced convection condensation, Proc. 5th Int. Heat Transfer Conf., Tokyo, 309-313, 1974.
22. Shah, M. M., A general correlation for heat transfer during film condensation inside pipes, Int. J. Heat Mass Transfer, 22, 547-556, 1979.
23. Kraus, A. D., A. Aziz and J. Welty, Extended Surface Heat Transfer, Wiley, New York, 2001.
24. Beatty, K. O. and D. L. Katz, Condensation of vapors on outside of finned tubes, Chem. Eng. Prog., 44, No. 1, 55-70, 1948.
25. Collier, J. G. and J. R. Thome, Convective Boiling and Condensation, 3rd edn, Clarendon Press, Oxford, 1994.
26. Bell, K. J. and A. J. Mueller, Wolverine Engineering Data Book II, Wolverine Tube, Inc., www.wlv.com, 2001.
27. Kern, D. Q. and A. D. Kraus, Extended Surface Heat Transfer, McGraw-Hill, New York, 1972.
28. Minton, P.E., Heat Exchanger Design, in Heat Transfer Design Methods, J. J. McKetta, ed., Marcel Dekker, New York, 1991.
29. Rubin, F. L., Multizone condensers: desuperheating, condensing, subcooling, Heat Transfer Eng., 3, No. 1, 49-58, 1981.
30. Gulley, D. L., How to calculate weighted MTD's, Hydrocarbon Processing, 45, No. 6, 116-122, 1966.
31. Taborek, J., Shell-and-tube heat exchangers, in Heat Exchanger Design Handbook, Vol. 3, Hemisphere Publishing Corp., New York, 1988.
32. Taylor, R., R. Krishnamurthy, J. S. Furno and R. Krishna, Condensation of vapor mixtures: 1. nonequilibrium models and design procedures; 2. comparison with experiment, Ind. Eng. Chem. Process Des. Dev., 25, 83-101, 1986.
33. Bell, K. J. and M. A. Ghaly, An approximate generalized design method for multicomponent / partial condensers, AIChE Symposium Series, 69, No. 131, 72-79, 1972.
34. Taborek, J., Mean temperature difference, in Heat Exchanger Design Handbook Vol. 1, Hemisphere Publishing Corp., New York, 1988.
35. Diehl, J. E. and C. R. Koppany, Flooding velocity correlation for gas-liquid counterflow in vertical tubes, Chem. Eng. Prog. Symposium Series, 65, No. 92, 77-83, 1969.

## Appendix 11.A LMTD Correction Factors for TEMA J- and X-Shells

The following notation is used for the charts:
$A=$ heat-transfer surface area in exchanger
$C_{1}=\left(\dot{m} C_{P}\right)_{1}=$ heat capacity flow rate of shell-side fluid
$C_{2}=\left(\dot{m} C_{P}\right)_{2}=$ heat capacity flow rate of tube-side fluid
$\Delta T_{m}=F\left(\Delta T_{\mathrm{ln}}\right)_{c f}=$ mean temperature difference in exchanger
$U=$ overall heat-transfer coefficient
All other symbols are explicitly defined on the charts themselves.
When the outlet temperatures of both streams are known, the lower charts can be used to obtain the LMTD correction factor in the usual manner. When the outlet temperatures are unknown but the product $U A$ is known, the upper charts can be used to obtain $\theta$, from which the mean temperature difference, $\Delta T_{m}$, can be found. The exchanger duty is then obtained as $q=U A \Delta T_{m}$, and the outlet temperatures are computed using the energy balances on the two streams.


$$
P=\frac{\left(T_{2}\right)_{o}-\left(T_{2}\right)_{i}}{\left(T_{1}\right)_{i}-\left(T_{2}\right)_{i}}
$$

Figure 11.A. 1 Mean temperature difference relationships for a TEMA J-shell exchanger with one tube pass (Source: Ref. [34]).


Figure 11.A.2 Mean temperature difference relationships for a TEMA J-shell exchanger with an even number of tube passes (Source: Ref. [34]).


Figure 11.A.3 Mean temperature difference relationships for a TEMA $X$-shell exchanger with one tube pass (Source: Ref. [34]).

The F-factor for J-shells is the same if the flow direction of the shell-side fluid is reversed so that there are two entrance nozzles and one exit nozzle, as in a condenser. However, the F-factor for J -shells is not symmetric with respect to fluid placement; switching the fluids between tubes and shell will change the value of $F$.
The equations from which the charts were constructed are given by Taborek [34]. The equations for J-shells are readily solvable on a scientific calculator. For an X -shell, the equations are rather intractable, and mathematical software such as MATHCAD is recommended in this case. The following definitions are used in the equations:

$$
\begin{array}{ll}
\Psi=\frac{R-1}{\ln [(1-P) /(1-P R)]} & (R \neq 1) \\
\Psi=(1-P) / P & (R=1) \\
\Phi=\exp (1 / F \Psi) & \tag{11.A.3}
\end{array}
$$

For these configurations, the equations are solved explicitly for $P$, but are implicit in $F$.
(1) J-Shell with single tube pass

$$
\begin{gather*}
P=1-\left(\frac{2 R-1}{2 R+1}\right)\left[\frac{2 R+\Phi^{-(R+0.5)}}{2 R-\Phi^{-(R+0.5)}}\right] \quad(R \neq 0.5)  \tag{11.A.4}\\
P=1-\left(\frac{1+\Phi^{-1}}{2+\ln \Phi}\right) \quad(R=0.5) \tag{11.A.5}
\end{gather*}
$$

(2) J-shell with even number of tube passes

$$
\begin{equation*}
P=\left(\frac{R \Phi^{R}}{\Phi^{R}-1}+\frac{\Phi}{\Phi-1}-\frac{1}{\ln \Phi}\right)^{-1} \tag{11.A.6}
\end{equation*}
$$

(3) X-shell with single tube pass

The equation for this configuration represents the situation in which the streams flow perpendicular to one another and both streams flow through a large number of channels with no mixing between channels. This situation is referred to as unmixed-unmixed cross flow.

$$
\begin{equation*}
P=\frac{1}{R \ln \Phi} \sum_{n=0}^{\chi}\left\{\left[1-\Phi^{-1} \sum_{m=0}^{n} \frac{(\ln \Phi)^{m}}{m!}\right]\left[1-\Phi^{-R} \sum_{m=0}^{n} \frac{(R \ln \Phi)^{m}}{m!}\right]\right\} \tag{11.A.7}
\end{equation*}
$$

The graph for this case was constructed with the number of channels, $\chi$, set to 10 [34].
To calculate the F-factor for given values of $P$ and $R$, the applicable equation is solved for $\Phi$, from which $F$ is easily obtained by taking logarithms.

## Example 11.A. 1

Calculate the LMTD correction factor for the following cases:
(a) A J-shell with one tube pass, $R=0.5$ and $P=0.75$.
(b) A J-shell with two tube passes, $R=1.0$ and $P=0.5$.

## Solution

(a) Equation (11.A.5) is applicable for this case. Setting $P=0.75$ gives the following equation for $\Phi$ :

$$
0.75=1-\left(\frac{1+\Phi^{-1}}{2+\ln \Phi}\right)
$$

Using the nonlinear equation solver on a TI-80 series calculator, the solution is found to be $\Phi=10.728$, and $\ln \Phi=2.37286$. Next, $\Psi$ is calculated using Equation (11.A.1):

$$
\Psi=\frac{0.5-1.0}{\ln [(1-0.75) /(1-0.75 \times 0.5)]}=0.54568
$$

Finally, Equation (11.A.3) is solved for $F$ :

$$
F=(\Psi \ln \Phi)^{-1}=(0.54568 \times 2.37286)^{-1}=0.7723
$$

(b) Equation (11.A.6) is applicable for this case. Setting $R=1.0$ and $P=0.5$ gives the following equation for $\Phi$ :

$$
0.5=\left(\frac{\Phi}{\Phi-1}+\frac{\Phi}{\Phi-1}-\frac{1}{\ln \Phi}\right)^{-1}
$$

The solution is found using a TI calculator: $\Phi=3.51286$, from which $\ln \Phi=1.25643$. Since $R=1.0$, the value of $\Psi$ is obtained from Equation (11.A.2):

$$
\Psi=(1-P) / P=(1-0.5) / 0.5=1.0
$$

The LMTD correction factor is found by solving Equation (11.A.3) as before:

$$
F=(\Psi \ln \Phi)^{-1}=(1.0 \times 1.25643)^{-1}=0.7959
$$

The reader can verify that the calculated values of $F$ are in agreement with the graphs.

## APPENDIX 11.B. Other Design Considerations

(1) Condensate nozzle sizing

Condensate often flows by gravity from a condenser to an accumulator (reflux drum). In this situation the condensate nozzle(s) must be properly sized to prevent excessive liquid accumulation in the condenser and to ensure that the condensate line will be self-venting. A self-venting line does not run full of liquid; hence, any vapor that is entrained with the liquid can disengage and flow freely through the line. The following equation can be used to size condensate nozzles for gravity drainage [28]:

$$
\begin{equation*}
D_{n}=0.92 v_{L}^{0.4} \tag{11.B.1}
\end{equation*}
$$

where
$D_{n}=$ nozzle internal diameter, in.
$\dot{v}_{L}=$ volumetric condensate flow rate, gpm.
This equation is essentially the same as a widely used graphical correlation that can be found in the book by Kister [4].
(2) Flooding in reflux condensers

As noted in the text, the vapor velocity in a reflux condenser must be kept low enough to prevent excessive liquid entrainment and flooding of the tubes. The flooding correlation of Diehl and Koppany [35] can be used to estimate the vapor velocity at which flooding begins. This correlation, which is based on experimental data that cover a wide range of operating conditions, is as follows:

$$
\begin{align*}
V_{f} & =F_{1} F_{2}\left(\sigma / \rho_{V}\right)^{0.5} & & \text { for } F_{1} F_{2}\left(\sigma / \rho_{V}\right)^{0.5} \geq 10  \tag{11.B.2}\\
& =1.0 & & \text { otherwise } \\
F_{1} & =\left(80 D_{i} / \sigma\right)^{0.4} & & \text { for } 80 D_{i} / \sigma<1.0  \tag{11.B.3}\\
& =1.0 & & \text { otherwise } \\
F_{2} & =\left(G_{V} / G_{L}\right)^{0.25} & & \tag{11.B.4}
\end{align*}
$$

where
$V_{f}=$ vapor superficial velocity at incipient flooding, $\mathrm{ft} / \mathrm{s}$
$D_{i}=$ tube internal diameter, in.
$\rho_{V}=$ Vapor density, $\mathrm{lbm} / \mathrm{ft}^{3}$
$\sigma=$ liquid surface tension, dyne $/ \mathrm{cm}$
The flooding velocity can be increased by tapering the ends of the tubes to facilitate condensate drainage. For a tapering angle of $70^{\circ}$ with the horizontal, the flooding velocity can be estimated by the following equation that was obtained by curve fitting the graphical correlation in Ref. 35.

$$
\begin{equation*}
V_{f, 70} / V_{f}=0.692+0.058 \sigma-0.00127 \sigma^{2}+9.34 \times 10^{-6} \sigma^{3} \tag{11.B.5}
\end{equation*}
$$

where
$V_{f, 70}=$ flooding velocity for tapered tube
$V_{f}=$ flooding velocity for un-tapered tube from Equation (11.B.2)
$\sigma=$ surface tension of liquid, dyne/cm
Equation (11.B.5) is valid for systems with liquid surface tension between 6 and 60 dyne/ cm . The effect of tapering is negligible for surface tension below about 6 dyne $/ \mathrm{cm}$. Based on the data reported by Diehl and Koppany [35], the tapering angle should be in the range of $60^{\circ}-75^{\circ}$. Over this range, the effect of tapering angle on flooding velocity is insignificant.

A reflux condenser should be designed to operate at a vapor velocity that is safely below the flooding velocity. Thus, an operating velocity in the range of $50-70 \%$ of the flooding velocity should be used for design purposes. The amount of liquid entrainment decreases with decreasing vapor velocity. At $50 \%$ of the flooding velocity, the entrainment ratio (mass of entrained liquid per unit mass of vapor) is approximately 0.005 [35].

| Notations |  |
| :---: | :---: |
| A | Heat-transfer surface area |
| $A_{f}$ | Flow Area |
| $A_{\text {fins }}$ | Surface area of all fins |
| $A_{i}$ | Internal surface area of tube |
| $A_{\text {prime }}$ | Prime surface area |
| $A_{\text {Tot }}$ | Total area of fins and prime surface |
| $a_{s}$ | Flow area across-tube bundle |
| $B$ | Baffle spacing; parameter in Chisholm correlation for two-phase pressure drop |
| $B_{c}$ | Baffle cut |
| $B_{\text {in }}$ | Inlet baffle spacing |
| $B_{\text {out }}$ | Outlet baffle spacing |
| $C_{P, c}$ | Heat capacity of coolant |
| $C_{P, L}$ | Heat capacity of condensate |
| $C_{P, V}$ | Heat capacity of vapor |
| $\bar{C}_{P, V}$ | Average heat capacity of vapor |
| $C^{\prime}$ | Tube clearance |
| $C_{\text {eff }}^{\prime}$ | Effective clearance for finned-tube bundle |
| D | Diameter |
| $D_{e}$ | Equivalent diameter |
| $D_{i}$ | Internal diameter of tube |
| $D_{o}$ | External diameter of tube |
| $D_{r}$ | Root-tube diameter |
| $D_{r e}$ | Equivalent root-tube diameter |
| $d_{s}$ | Internal diameter of shell |
| E | Parameter in Beatty-Katz correlation |
| $F$ | LMTD correction factor |
| $F_{1}, F_{2}$ | Parameters in flooding correlation for reflux condensers |
| $f$ | Darcy friction factor |
| $f_{\text {ideal }}$ | Fanning friction factor for ideal flow through bank of plain tubes |
| $f_{\text {ideal }}^{\prime}$ | Fanning friction factor for ideal flow through bank of finned tubes |
| $f_{1}, f_{2}$ | Friction factors from Figure 5.1 for $B / d_{s}$ of 1.0 and 0.2 , respectively |
| G | Mass flux |
| $G_{L}$ | Mass flux of condensate |
| $G_{n}$ | Mass flux in nozzle |
| $G_{n, \text { in }}, G_{n, \text { out }}$ | Mass flux in inlet and outlet nozzle, respectively |
| $G_{V}$ | Mass flux of vapor |
| $g$ | Gravitational acceleration |
| $g_{c}$ | Unit conversion factor |
| $\hat{H}$ | Specific enthalpy |
| $h$ | Heat-transfer coefficient |
| $h_{g r}$ | Heat-transfer coefficient for gravity-controlled condensation |
| $h_{i}$ | Tube-side heat-transfer coefficient |
| $h_{\text {in }}$ | Heat-transfer coefficient at condenser inlet |
| $h_{L}$ | Heat-transfer coefficient for liquid phase flowing alone |
| $h_{L O}$ | Heat-transfer coefficient for total flow as liquid |
| $h_{N r}$ | Heat-transfer coefficient for condensation on a vertical stack of $N_{r}$ tube rows |
| $h_{N u}$ | Heat-transfer coefficient given by basic Nusselt theory |
| $h_{\text {out }}$ | Heat-transfer coefficient at condenser outlet |
| $h_{\text {sh }}$ | Heat-transfer coefficient for shear-controlled condensation |
| $h_{V}$ | Heat-transfer coefficient for vapor phase |
| $h_{z}$ | Local heat-transfer coefficient for condensation on a vertical surface |
| $h_{1}$ | Heat-transfer coefficient for condensation on single tube row |


| $h_{\text {I }}, h_{\text {II }}, h_{\text {III }}$ | Heat-transfer coefficient for condensation in horizontal tube with flow regime corresponding to zones I, II and III, respectively |
| :---: | :---: |
| $j_{H}$ | Modified Colburn factor for shell-side heat transfer |
| ${ }^{*}{ }^{*}$ | Dimensionless vapor mass flux defined by Equation (11.52) |
| $k$ | Thermal conductivity |
| $k_{L}$ | Thermal conductivity of condensate |
| $k_{\text {tube }}$ | Thermal conductivity of tube wall |
| $\bar{k}_{V}$ | Average thermal conductivity of vapor |
| $L$ | Length |
| M | Molecular weight |
| $\dot{m}$ | Mass flow rate |
| $\dot{m}_{c}$ | Mass flow rate of coolant |
| $\dot{m}_{L}$ | Mass flow rate of liquid phase |
| $\dot{m}_{V}$ | Mass flow rate of vapor phase |
| $\dot{m}_{V, i n}$ | Mass flow rate of vapor entering condenser |
| $\dot{m}_{V, \text { out }}$ | Mass flow rate of vapor leaving condenser |
| $N_{c}$ | Number of tube rows crossed in flow between two baffle tips |
| $N_{f}$ | Number of fins |
| $N_{r}$ | Number of tube rows in vertical direction |
| Nu | Nusselt number |
| $N u_{L O}$ | Nusselt number for total flow as liquid |
| $n$ | Exponent in friction factor Versus Reynolds number relationship |
| $n_{b}$ | Number of baffles |
| $n_{f}$ | Number of fins per unit length of tube |
| $n_{p}$ | Number of tube passes |
| $n_{t}$ | Number of tubes in bundle |
| $\left(n_{t}\right)_{\text {req }}$ | Required number of tubes |
| $P$ | Pressure; parameter used to calculate LMTD correction factor |
| $P_{r}$ | Reduced pressure |
| $P r$ | Prandtl number |
| $P r_{L}$ | Prandtl number of condensate |
| $\mathrm{Pr}_{V}$ | Prandtl number of vapor |
| $P_{s a t}$ | Saturation pressure |
| $P_{T}$ | Tube pitch |
| $q$ | Rate of heat transfer |
| $q_{\text {sen }}$ | Rate of sensible heat transfer |
| $q_{\text {Tot }}$ | Total condenser duty |
| $\hat{q}$ | Heat flux |
| $\hat{q}^{\prime}$ | Heat flux in y-direction |
| $R$ | Parameter used to calculate LMTD correction factor |
| $\widetilde{R}$ | Universal gas constant |
| $R_{\text {Di }}, R_{\text {Do }}$ | Fouling factor for tube-side and shell-side, respectively |
| $R e$ | Reynolds number |
| $R_{L}$ | Reynolds number for liquid phase flowing alone |
| $R e_{L O}$ | Reynolds number for total flow as liquid |
| $R e_{V}$ | Reynolds number for vapor |
| $r_{1}$ | Root-tube radius |
| $r_{2}$ | fin radius |
| $r_{2 c}$ | Corrected fin radius |
| SR | Slip ratio |
| $s$ | Specific gravity |
| T | Temperature |
| $T_{a}, T_{b}$ | Inlet and outlet temperatures of shell-side fluid |


| $T_{\text {ave }}$ | Average bulk temperature of shell-side fluid |
| :--- | :--- |
| $T_{c}$ | Coolant temperature |
| $T_{c, \text { ave }}$ | Average coolant temperature in a condenser zone |
| $T_{c, \text { out }}$ | Temperature of coolant leaving a condenser zone |
| $T_{f}$ | Film temperature |
| $T_{L}$ | Condensate temperature |
| $T_{p}$ | Average temperature of prime surface |
| $T_{\text {sat }}$ | Saturation temperature |
| $T_{V}$ | Temperature of vapor |
| $T_{V, i n}, T_{V, \text { out }}$ | Temperature of vapor at condenser inlet and outlet, respectively |
| $T_{w}$ | Wall temperature |
| $T_{w t d}$ | Weighted average temperature of finned surface |
| $t_{a}, t_{b}$ | Inlet and outlet temperatures of tube-side fluid |
| $t_{a v e}$ | Average bulk temperature of tube-side fluid |
| $U$ | Overall heat-transfer coefficient |
| $U_{D}$ | Design overall heat-transfer coefficient |
| $U_{D}^{\prime}$ | Design overall heat-transfer coefficient modified to account |
| $U_{r e q}$ | for thermal resistance due to vapor cooling |
| $u_{V, i n}, u_{V, \text { out }}$ | Required overall heat-transfer coefficient |
| $V$, | Fluid velocity at condenser inlet and outlet, respectively |
| $V_{f}$ | Flooding velocity in reflux condenser |
| $V_{f, 70}$ | Flooding velocity in reflux condenser having tubes with $70 \%$ taper |
| $\dot{v}_{L}$ | Volumetric flow rate of condensate |
| $W$ | Condensation rate |
| $\hat{W}$ | Condensation rate per unit area |
| $w$ | Width of vertical wall |
| $X$ | Lockhart-Martinelli parameter |
| $X_{t t}$ | Lockhart-Martinelli parameter for turbulent flow in both phases |
| $x$ | Vapor weight fraction |
| $x_{e}$ | Vapor weight fraction at condenser exit |
| $x_{i n}$ | Vapor weight fraction at condenser inlet |
| $Y$ | Chisholm parameter |
| $y$ | Coordinate in direction normal to condensing surface |
| $z$ | Coordinate in vertically downward direction |
|  |  |

## Greek Letters

$\alpha_{r} \quad$ Number of velocity heads allocated for tube-side minor pressure losses
$\beta \quad$ Weight factor used to calculate film temperature
$\Gamma \quad$ Condensation rate per unit width of surface
$\Gamma^{*} \quad$ Modified condensate loading defined by Equation (11.36)
$\Delta \hat{H} \quad$ Specific enthalpy difference
$\Delta P_{f} \quad$ Frictional pressure drop in straight sections of tubes or in shell
$\left(\Delta P_{f}\right)_{V O} \quad$ Frictional pressure drop for total flow as vapor
$\Delta P_{i} \quad$ Total tube-side pressure drop
$\Delta P_{n} \quad$ Pressure drop in nozzle
$\Delta P_{n, \text { in }}, \Delta P_{n, \text { out }} \quad$ Pressure losses in inlet and outlet nozzles, respectively
$\Delta P_{o} \quad$ Total shell-side pressure drop
$\Delta P_{r} \quad$ Tube-side pressure drop due to entrance, exit and return losses
$\Delta q \quad$ Duty in a condenser zone
$\Delta q_{V} \quad$ Duty due to vapor cooling in a condenser zone
$\Delta T \quad$ Temperature difference
$\Delta T_{c} \quad$ Coolant temperature difference

| $\Delta T_{f}$ | Temperature difference across condensate film |
| :---: | :---: |
| $\Delta T_{m}$ | Mean temperature difference |
| $\left(\Delta T_{\ln }\right)_{c f}$ | Logarithmic mean temperature difference for counter-current flow |
| $\Delta y, \Delta z$ | Difference in y - or z-coordinate value |
| $\delta$ | Thickness of condensate film |
| $\varepsilon$ | $C_{P, L}\left(T_{\text {sat }}-T_{w}\right) / \lambda$ |
| $\varepsilon_{V}$ | Void fraction |
| $\eta_{f}$ | Fin efficiency |
| $\eta_{w}$ | Weighted efficiency of finned surface |
| $\theta$ | Angle between an inclined surface and the vertical direction |
| $\theta^{\prime}$ | Angle between an inclined tube and the horizontal direction |
| $\theta_{t p}$ | Tube layout angle |
| $\Lambda$ | $d q_{V} / d q$ |
| $\lambda$ | Latent heat of condensation |
| $\lambda^{\prime}$ | $\lambda+C_{P, V}\left(T_{V}-T_{s a t}\right)$ |
| $\mu_{L}$ | Viscosity of condensate |
| $\mu_{V}$ | Viscosity of vapor |
| $\bar{\mu}_{V}$ | Average viscosity of vapor |
| $\mu_{w}$ | Viscosity of fluid at average wall temperature |
| $\rho_{L}$ | Density of condensate |
| $\rho_{V}$ | Density of vapor |
| $\rho_{\text {hom }}$ | Homogenous two-phase density |
| $\sigma$ | Surface tension |
| $\tau$ | Fin thickness |
| $\Phi$ | Parameter used to calculate LMTD correction factor for J- and X-shell exchangers |
| $\phi$ | Viscosity correction factor; angle defined in Figure 11.12 |
| $\phi_{L}^{2}$ | Two-phase multiplier for pressure gradient based on liquid phase flowing alone |
| $\phi_{L O}^{2}$ | Two-phase multiplier for pressure gradient based on total flow as liquid |
| $\bar{\phi}_{V O}^{2}$ | Average two-phase pressure-drop multiplier in Equation (11.64) |
| $\chi$ | Number of flow channels in unmixed-unmixed cross-flow configuration |
| $\Psi$ | Parameter used to calculate LMTD correction factor for J- and X-shell exchangers |
| $\psi$ | Parameter in equation for efficiency of annular fin |
| $\Omega$ | Parameter in correlation for condensation in stratified flow regime, Equation (11.53) |

## Other Symbols

${ }^{\prime} z$ Evaluated at $\mathbf{z}$

## Problems

(11.1) Use Shah's method to estimate the condensing-side heat-transfer coefficient for the condenser of Example 11.3 (a). Do the calculation for three positions in the condenser where the quality is, respectively, $75 \%, 50 \%$, and $25 \%$. Fluid properties can be obtained from Example 11.5.

Ans. $50 \%$ quality: $h=288 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} \quad 25 \%$ quality: $h=185 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(11.2) The average heat-transfer coefficient for a condensing vapor flowing downward in a vertical tube can be estimated using the correlation of Carpenter and Colburn (Carpenter, E. F.
and A. P. Colburn, Proc. of General Discussion on Heat Transfer, I Mech E/ASME, 1951, 20-26):

$$
\begin{aligned}
\frac{h \mu_{L}}{k_{L} \rho_{L}^{0.5}} & =0.065\left(\frac{C_{P, L} \mu_{L}}{k_{L}}\right)^{0.5} \tau_{i}^{0.5} \\
\tau_{i} & =\frac{f_{V} \bar{G}_{V}^{2}}{8 \rho_{V}}=\text { average interfacial shear stress } \\
\bar{G}_{V} & =\left(\frac{G_{V, \text { in }}^{2}+G_{V, \text { in }} G_{V, \text { out }}+G_{V, \text { out }}^{2}}{3}\right)^{0.5} \\
f_{V} & =0.4137 R e_{V}^{-0.2585}=0.4137\left(\frac{D_{i} \bar{G}_{V}}{\mu_{V}}\right)^{-0.2585}
\end{aligned}
$$

Note that for a total condenser, $\bar{G}_{V}=0.58 G_{V, i n}$, where $G_{V, i n}$ is the inlet mass flux of vapor. The Carpenter-Colburn correlation is strictly valid for shear-controlled condensation; it may under-predict the heat-transfer coefficient when this condition is not satisfied. Use the Carpenter-Colburn method to estimate the average heat-transfer coefficient for the condenser of Example 11.3(a).

Ans. $\quad h=217 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(11.3) The condenser of Examples 11.2 and 11.3 is oriented horizontally and the propyl alcohol condenses inside the tubes. At a position in the condenser where the quality is $50 \%$, use the method of Breber et al. to determine the flow regime. Note that the Lockhart-Martinelli parameter for this situation was computed in Problem 9.5.

Ans. Transition region between zones I and II.
(11.4) Akers and Rosson [18] developed a correlation for convective condensation in horizontal tubes that is valid for both laminar and turbulent condensate films. It utilizes a vapor-phase Reynolds number, $R e_{V}^{*}$, defined as follows:

$$
R e_{V}^{*}=\frac{D_{i} G_{V}\left(\rho_{L} / \rho_{V}\right)^{0.5}}{\mu_{L}}
$$

The correlation consists of the following three equations, the choice of which depends on the values of $R e_{V}^{*}$ and $R e_{L}$.
For $R e_{L} \leq 5000$ and $1000 \leq R e_{V}^{*} \leq 20,000$ :

$$
N u=13.8 P r_{L}^{1 / 3}\left(R e_{V}^{*}\right)^{0.2}\left(\frac{\lambda}{C_{P, L} \Delta T}\right)^{1 / 6}
$$

For $R e_{L} \leq 5000$ and $20,000<R e_{V}^{*} \leq 100,000$ :

$$
N u=0.1 P r_{L}^{1 / 3}\left(\operatorname{Re}_{V}^{*}\right)^{2 / 3}\left(\frac{\lambda}{C_{P, L} \Delta T}\right)^{1 / 6}
$$

For $R e_{L}>5000$ and $R e_{V}^{*} \geq 20,000$ :

$$
N u=0.026 \operatorname{Pr}_{L}^{1 / 3}\left(R e_{V}^{*}+R e_{L}\right)^{0.8}
$$

In these equations, $\Delta T=T_{s a t}-T_{w}$ and $N u=h D_{i} / k_{L}$.
(a) For the conditions specified in Problem 11.3, assume $\Delta T=51^{\circ} \mathrm{F}$ and calculate $h$ using the Akers-Rosson correlation.
(b) Using the value of $h$ obtained in part (a), calculate a new value of $\Delta T$. Iterate to obtain converged values of $h$ and $\Delta T$.

Ans. (a) $h=526 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(11.5) $20,000 \mathrm{lb} / \mathrm{h}$ of saturated cyclohexane vapor will be condensed at $182^{\circ} \mathrm{F}$ and 16 psia using a tube bundle containing 147 tubes arranged for a single pass. The tubes are $1.0-\mathrm{in}$. OD, 14 BWG with a length of 20 ft . Physical properties of cyclohexane at these conditions are given in Example 10.4, and all properties may be assumed constant at these values. For the purpose of this problem, the effects of condensate subcooling and interfacial shear are to be neglected. Calculate the condensing-side heat-transfer coefficient for the following cases:
(a) The tube bundle is vertical and condensation occurs inside the tubes.
(b) The tube bundle is horizontal and condensation occurs outside the tubes.

Ans. (a) $185 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (b) $238 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(11.6) Repeat problem 11.5 taking into account the variation of condensate viscosity with temperature. Use the viscosity data in Figure A. 1 for this purpose. Assume all other physical properties remain constant and neglect the effects of condensate subcooling and interfacial shear.

Ans. (a) $204 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. (b) $249 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(11.7) Estimate the effect of condensate subcooling on the heat-transfer coefficients computed in problem 11.6.

Ans. (a) $h / h_{N u}=1.01$. (b) $h / h_{N u}=1.007$.
(11.8) Use the Boyko-Kruzhilin correlation to estimate the effect of interfacial shear in the vertical condenser of problem 11.6. Assume that the vapor flows downward through the tubes.

Ans. $h_{\text {sh }}=148 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} ; h=h_{i}=252 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(11.9) Use the McNaught correlation to evaluate the significance of interfacial shear in the horizontal condenser of problem 11.5. The tube bundle resides in an E-shell with an ID of 17.25 in . The tubes are laid out on $1.25-\mathrm{in}$. triangular pitch. Baffles are $20 \%$ cut segmental type with a spacing of 8.6 in . Make the calculation for a point in the condenser where the vapor weight fraction is 0.5 . Use the physical property data given in Example 10.4 and neglect the viscosity correction factor.

Ans. $h_{s h}=310 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$.
(11.10) $50,000 \mathrm{lb} / \mathrm{h}$ of saturated acetone vapor will be condensed at $80^{\circ} \mathrm{C}$ and 31 psia using a tube bundle containing 316 tubes arranged for a single pass. The tubes are $1.0-\mathrm{in}$. OD, 16 BWG
with a length of 25 ft . The molecular weight of acetone is 58.08 and the liquid specific gravity is 0.79 . For the purpose of this problem, assume constant physical properties and neglect the effects of condensate subcooling and interfacial shear. Calculate the condensing-side heat-transfer coefficient for the following cases:
(a) The tube bundle is vertical and condensation occurs inside the tubes.
(b) The tube bundle is horizontal and condensation occurs outside the tubes.
(11.11) Repeat problem 11.10 taking into account the variation of condensate viscosity with temperature. Assume all other physical properties remain constant and neglect the effects of condensate subcooling and interfacial shear.
(11.12) Estimate the effect of condensate subcooling on the heat-transfer coefficients computed in Problem 11.11.
(11.13) Use the Boyko-Kruzhilin correlation to estimate the effect of interfacial shear in the vertical condenser of Problem 11.10. Assume that the vapor flows downward through the tubes.
(11.14) Use the McNaught correlation to evaluate the effect of interfacial shear in the horizontal condenser of Problem 11.10. The tube bundle resides in an E-shell with an ID of 25 in . and the tubes are laid out on $1.25-\mathrm{in}$. triangular pitch. Baffles are $20 \%$ cut segmental type with a spacing of 10 in . Make the calculation for a point in the condenser where the quality is $25 \%$.
(11.15) Use the Shah correlation to calculate the condensing-side heat-transfer coefficient at a quality of $50 \%$ for:
(a) The vertical cyclohexane condenser of Problems 11.5-11.8.
(b) The vertical acetone condenser of Problems 11.10-11.13.

The critical pressure of cyclohexane is 40.4 atm , and that of acetone is 47.0 atm .
(11.16) Use the Carpenter-Colburn correlation given in problem 11.2 to estimate the average condensing-side heat-transfer coefficient for:
(a) The vertical cyclohexane condenser of Problems 11.5-11.8.
(b) The vertical acetone condenser of Problems 11.10-11.13.

Assume that the vapor flows downward through the tubes in each case.
(11.17) The Shah correlation, Equation (11.56), can be integrated over the length of the condenser to obtain an average heat-transfer coefficient. If the quality varies linearly with distance along the condenser from $100 \%$ at the inlet to zero at the outlet, the result is:

$$
h=h_{L O}\left(0.55+2.09 P_{r}^{-0.38}\right)
$$

Values obtained from this equation differ by only about $5 \%$ from those calculated by Equation (11.56) for a quality of $50 \%$. Use the above equation to estimate the average heat-transfer coefficient for:
(a) The vertical propanol condenser of Examples 11.3-11.5.
(b) The vertical cyclohexane condenser of Problems 11.5-11.8.
(c) The vertical acetone condenser of Problems 11.9-11.13.

Critical pressures of cyclohexane and acetone are given in Problem 11.15. Make a table comparing your results with the average heat-transfer coefficients calculated using the

Carpenter-Colburn correlation in problems 11.2 and 11.16, and with the values obtained using Equation (11.56) for a quality of $50 \%$ in Problems 11.1 and 11.15.
(11.18) The condenser of Problem 11.5 is oriented horizontally and the cyclohexane condenses inside the tubes. At a position where the quality is $50 \%$ :
(a) Use the method of Breber et al. to determine the flow regime.
(b) Estimate the value of the condensing-side heat-transfer coefficient.
(11.19) The condenser of Problem 11.10 is oriented horizontally and the acetone condenses inside the tubes. At a position where the quality is $25 \%$ :
(a) Use the method of Breber et al. to determine the flow regime.
(b) Estimate the value of the condensing-side heat-transfer coefficient.
(11.20) Use the Simplified Delaware method in conjunction with Equations (11.64) and (11.65) to estimate the nozzle-to nozzle shell-side pressure drop for the horizontal condenser of Problems 11.5 and 11.9. Consider the following cases:
(a) Complete condensation.
(b) Partial condensation with an exit quality of $30 \%$.

Ans. (a) 13 psi . (b) 17.8 psi .
(11.21) Use Equations (11.64) and (11.66) to estimate the nozzle-to-nozzle tube-side pressure drop for the horizontal tube-side condenser of problem 11.18. Assume complete condensation.

Ans. 0.2 psi .
(11.22) Use the Simplified Delaware method in conjunction with Equations (11.64) and (11.65) to estimate the nozzle-to-nozzle shell-side pressure drop for the horizontal condenser of Problems 11.10 and 11.14. Consider the following cases:
(a) Complete condensation.
(b) Partial condensation with an exit quality of $50 \%$.
(11.23) Use Equations (11.64) and (11.66) to estimate the nozzle-to-nozzle tube-side pressure drop for the horizontal tube-side condenser of Problem 11.19. Assume complete condensation.
(11.24) The horizontal tube bundle of problem 11.5 contains 26 -fpi finned tubes, part number 267065 (Table B.5), made of 90-10 copper-nickel alloy. Assuming constant physical properties, calculate the condensing-side heat-transfer coefficient, the fin efficiency and the weighted efficiency of the finned surface. Neglect the effects of condensate subcooling and interfacial shear.
Ans. $\quad h=676 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} ; \eta_{f}=0.761 ; \eta_{w}=0.808$.
(11.25) The horizontal tube bundle of Problem 11.10 contains 19-fpi finned tubes, Catalog Number 60-197065 (Table B.4), made of plain carbon steel. Assuming constant physical properties, calculate the condensing-side heat-transfer coefficient, the fin efficiency, and the weighted efficiency of the finned surface. Neglect the effects of condensate subcooling and interfacial shear.
(11.26) $50,000 \mathrm{lb} / \mathrm{h}$ of saturated acetone vapor will be completely condensed at $80^{\circ} \mathrm{C}$ and 31 psia . A used heat exchanger consisting of a 33-in. ID E-shell containing 730 tubes arranged for a
single pass is available at the plant site. The tubes are $3 / 4-\mathrm{in}$. OD, 14 BWG with a length of 20 ft . The tube-side nozzles are made of 8 -in. schedule 40 pipe. Material of construction is plain carbon steel throughout. The unit will be oriented vertically and the condensing vapor will flow downward inside the tubes. A coolant will flow through the shell with a range of $80-140^{\circ} \mathrm{F}$, providing a shell-side heat-transfer coefficient of $400 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. A fouling factor of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for the coolant, and a maximum pressure drop of 5 psi is specified for the acetone stream. Condensate will drain from the condenser by gravity. Determine the unit's thermal and hydraulic suitability for this service. Neglect the effects of condensate subcooling and interfacial shear in the analysis. The specific gravity of liquid acetone is 0.79 .
(11.27) A used heat exchanger consisting of a 29-in. ID J-shell containing 416 tubes is available for the service of Problem 11.26. The tubes are $1-\mathrm{in}$. OD, 16 BWG laid out on 1.25 -in. triangular pitch with a length of 20 ft . There are 8 baffles on each side of the central (full circle) baffle with a spacing of 13.3 in. On the shell side, the two inlet nozzles consist of 6 -in. schedule 40 pipe and the single outlet nozzle is made of 8 -in. schedule 40 pipe. Material of construction is plain carbon steel throughout. Acetone will flow in the shell and a coolant with a range of $80-140^{\circ} \mathrm{F}$ will flow through the tubes, providing an inside heat-transfer coefficient of $500 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Other specifications are the same as given in Problem 11.26. Determine the thermal and hydraulic suitability of the unit for this service. Neglect the effects of condensate subcooling and interfacial shear in the analysis.
(11.28) $70,000 \mathrm{lb} / \mathrm{h}$ of saturated cyclohexane vapor will be completely condensed at $196^{\circ} \mathrm{F}$ and 20 psia. A used carbon steel heat exchanger consisting of a $35-\mathrm{in}$. ID E-shell containing 645 tubes arranged for a single pass is available for this service. The tubes are $1-\mathrm{in}$. OD, 16 BWG with a length of 16 ft . Tube-side nozzles are $10-\mathrm{in}$. schedule 40 pipe. The unit will be oriented vertically and the condensing vapor will flow downward inside the tubes. A cold process liquid will flow in the shell with a range of $100-175^{\circ} \mathrm{F}$, providing a shellside heat-transfer coefficient of $300 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. A fouling factor of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for the coolant, and a maximum pressure drop of 4 psi is specified for the cyclohexane stream. Gravity drainage of condensate will be employed. Determine the thermal and hydraulic suitability of the unit for this service. Neglect the effects of condensate subcooling and interfacial shear in the analysis. At inlet conditions the density of cyclohexane vapor is $0.25 \mathrm{lbm} / \mathrm{ft}^{3}$, the viscosity is 0.0087 cp and the latent heat of condensation is $149 \mathrm{Btu} / \mathrm{lbm}$. Liquid viscosity data for cyclohexane are available in Figure A.1. Values of other physical properties for cyclohexane given in Example 10.4 may be used for this problem.
(11.29) A used heat exchanger consisting of a 31-in. ID J-shell containing 774 tubes is available for the service of Problem 11.28 . The tubes are $3 / 4-\mathrm{in}$. OD, 14 BWG on $1.0-\mathrm{in}$. triangular pitch with a length of 18 ft . There are 8 baffles on each side of the central (full circle) baffle with a spacing of 12 in. On the shell side, the two inlet nozzles consist of 6 -in. schedule 40 pipe and the single outlet nozzle is 10 -inch schedule 40 pipe. The tubes and tubesheets are made of 90-10 copper-nickel alloy; all other components are plain carbon steel. Cyclohexane will flow in the shell and a coolant with a range of $100-175^{\circ} \mathrm{F}$ will flow through the tubes, providing a tube-side heat-transfer coefficient of $400 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Other specifications are the same as in Problem 11.28. Determine the thermal and hydraulic suitability of the unit for this service. Neglect the effects of condensate subcooling and interfacial shear in the analysis.
(11.30) Consider a horizontal shell-side condenser in which the coolant makes two passes through the exchanger. Assume the coolant and vapor enter at the same end of the condenser and
denote the coolant temperature in the first and second passes by $T_{c}^{\prime}$ and $T_{c}^{\prime \prime}$, respectively. The temperature profiles along the length of the condenser are as shown below.


If the surface area is equally divided between the two passes and the overall coefficient is assumed to be the same for both passes, the rate of heat transfer in a differential condenser element can be written as:

$$
d q=\frac{1}{2} U_{D} d A\left(T_{V}-T_{c}^{\prime}\right)+\frac{1}{2} U_{D} d A\left(T_{V}-T_{c}^{\prime \prime}\right)
$$

or

$$
\begin{equation*}
d q=\frac{1}{2} U_{D} d A\left(2 T_{V}-T_{c}^{\prime}-T_{c}^{\prime \prime}\right) \tag{i}
\end{equation*}
$$

(a) Using Equation (i) in place of Equation (11.70), show that the relationship corresponding to Equation (11.75) is:

$$
\begin{equation*}
A=2 \int_{0}^{q_{T_{o t}}} \frac{\left(1+U_{D} \Lambda / h_{V}\right)}{U_{D}\left(2 T_{V}-T_{c}^{\prime}-T_{c}^{\prime \prime}\right)} d q \tag{ii}
\end{equation*}
$$

(b) Differential energy balances for the coolant are as follows:

$$
d q=\dot{m}_{c} C_{P, c}\left(d T_{c}^{\prime}-d T_{c}^{\prime \prime}\right)
$$

or

$$
\begin{gather*}
d T_{c}^{\prime}-d T_{c}^{\prime \prime}=\frac{d q}{\dot{m}_{c} C_{P, c}}  \tag{iii}\\
\dot{m}_{c} C_{P, c} d T_{c}^{\prime}=\frac{1}{2} U_{D} d A\left(T_{V}-T_{c}^{\prime}\right)  \tag{iv}\\
\dot{m}_{c} C_{P, c}\left(-d T_{c}^{\prime \prime}\right)=\frac{1}{2} U_{D} d A\left(T_{V}-T_{c}^{\prime \prime}\right) \tag{v}
\end{gather*}
$$

Dividing Equation (iv) by Equation (v) gives:

$$
\begin{equation*}
\frac{d T_{c}^{\prime}}{-d T_{c}^{\prime \prime}}=\frac{T_{V}-T_{c}^{\prime \prime}}{T_{V}-T_{c}^{\prime \prime}} \tag{vi}
\end{equation*}
$$

Show that Equations (iii) and (vi) can be solved for $d T_{c}^{\prime}$ and $d T_{c}^{\prime \prime}$ to obtain the following results:

$$
\begin{align*}
d T_{c}^{\prime} & =\left(\frac{d q}{\dot{m}_{c} C_{P, c}}\right)\left(\frac{T_{V}-T_{c}^{\prime}}{2 T_{V}-T_{c}^{\prime}-T_{c}^{\prime \prime}}\right)  \tag{vii}\\
d T_{c}^{\prime \prime} & =-\left(\frac{d q}{\dot{m}_{c} C_{P, c}}\right)\left(\frac{T_{V}-T_{c}^{\prime \prime}}{2 T_{V}-T_{c}^{\prime}-T_{c}^{\prime \prime}}\right) \tag{viii}
\end{align*}
$$

In practice, Equations (vii) and (viii) are applied to a condenser element of finite size to obtain $\Delta T_{c}^{\prime}$ and $\Delta T_{c}^{\prime \prime}$. The values of $T_{V}, T_{c}^{\prime}$ and $T_{c}^{\prime \prime}$ on the right-hand side are taken at the beginning of the element. The temperature profiles in the two coolant passes are easily determined in this manner starting from the inlet end of the condenser where $T_{V}=T_{V, i n}, T_{c}^{\prime}=T_{c, \text { in }}$ and $T_{c}^{\prime \prime}=T_{c, \text { out }}$
(c) Assume that the coolant in Example 11.8 makes two passes through the condenser. Using the same three temperature intervals, calculate the temperature profiles in the two coolant passes and determine the temperature in the return header.

Ans. At the return header, $T_{c}^{\prime}=T_{c}^{\prime \prime}=105.17^{\circ} \mathrm{F}$.
(d) Use the temperature profiles obtained in part (c) together with the data from Example 11.8 to compute the required surface area for the condenser according to Equation (ii).

Ans. $A=1742 \mathrm{ft}^{2}$.

| $T_{V}\left({ }^{\circ} \mathrm{F}\right)$ | Duty $(\mathrm{Btu} / \mathrm{h})$ |
| :--- | :--- |
| 300 | 0 |
| 270 | $6.5 \times 10^{6}$ |
| 240 | $12.0 \times 10^{6}$ |
| 210 | $15.5 \times 10^{6}$ |

A condenser is to be designed based on the above condensing curve. Water with a range of $75-125^{\circ} \mathrm{F}$ will be used as the coolant. Determine the temperature profile for the cooling water for the following cases:
(a) A single coolant pass and counter-current flow.
(b) Two coolant passes with coolant and vapor entering at the same end of the condenser. (Refer to Problem 11.30.)
(11.32) Use any available software to design a condenser for the service of problem 11.26. For the coolant, use water that is available from a cooling tower at $85^{\circ} \mathrm{F}$. Assume an inlet pressure of 50 psia and a maximum allowable pressure drop of 10 psi for the coolant.
(11.33) Use any available software to design a condenser for the service of problem 11.28. For the coolant, use water that is available from a cooling tower at $85^{\circ} \mathrm{F}$. Assume an inlet pressure of 50 psia and a maximum allowable pressure drop of 10 psi for the coolant.
(11.34) A stream with a flow rate of $150,000 \mathrm{lb} / \mathrm{h}$ having the following composition is to be condensed.

| Component | Mole percent |
| :--- | :---: |
| Propane | 15 |
| i-Butane | 25 |
| n-Butane | 60 |

The stream will enter the condenser as a saturated vapor at 150 psia and is to leave as a subcooled liquid with a minimum $10^{\circ} \mathrm{F}$ of subcooling. A maximum pressure drop of 2 psi is specified. Cooling will be supplied by water from a cooling tower entering at $80^{\circ} \mathrm{F}$ and 50 psia, with a maximum allowable pressure drop of 10 psi . Use any available software to design a condenser for this service.
(11.35) A petroleum fraction has an average API gravity of $40^{\circ}$ and the following assay (ASTM D85 distillation at atmospheric pressure):

| Volume \% distilled | $T\left({ }^{\circ} \mathrm{F}\right)$ |
| :---: | :---: |
| 0 | 112 |
| 10 | 157 |
| 20 | 201 |
| 30 | 230 |
| 40 | 262 |
| 50 | 291 |
| 60 | 315 |
| 70 | 338 |
| 80 | 355 |
| 90 | 376 |
| 100 | 390 |

$90,000 \mathrm{lb} / \mathrm{h}$ of this material will be condensed using cooling water available at $80^{\circ} \mathrm{F}$. The petroleum fraction will enter the condenser as a saturated vapor at 20 psia , and is to be completely condensed with a pressure drop of 3 psi or less. Maximum allowable pressure drop for the cooling water is 10 psia . Use HEXTRAN or other appropriate software to design a condenser for this service.
(11.36) Using any available software package, do the following.
(a) Rate the final configuration for the finned-tube condenser of Example 11.7 and compare the results with those from the hand calculations in the text.
(b) Modify the condenser configuration as appropriate and obtain a final design for the unit.
(11.37)

Astream with a flow rate of $65,000 \mathrm{lb} / \mathrm{h}$ having the following composition is to be condensed.

| Component | Mole percent |
| :--- | :---: |
| Ethanol | 32 |
| Isopropanol | 10 |
| 1-Propanol | 23 |
| 2-Methyl-1-Propanol | 19 |
| 1-Butanol | 16 |

The stream will enter the condenser as a saturated vapor at 18 psia , and a maximum pressure drop of 2 psia is specified. The temperature of the condensate leaving the unit should not exceed $180^{\circ} \mathrm{F}$. Cooling will be supplied by water from a cooling tower entering at $90^{\circ} \mathrm{F}$ and 40 psia , with a maximum allowable pressure drop of 10 psia . Use any available software to design a condenser for this service.
(11.38) $40,000 \mathrm{lb} / \mathrm{h}$ of refrigerant 134 a (1,1,1,2-tetrafluoroethane) will enter a condenser as a superheated vapor at $180^{\circ} \mathrm{F}$ and 235 psia . The condensate is to leave the unit as a subcooled liquid with a minimum of $10^{\circ} \mathrm{F}$ of subcooling. A maximum pressure drop of 3 psia is specified. The coolant will be water from a cooling tower entering at $80^{\circ} \mathrm{F}$ and 50 psia , with a maximum allowable pressure drop of 10 psia. Use any available software package to design a condenser for this service. Develop one or more designs for each of the following condenser types and select the best option for the service. Give the rationale for your selection.
(a) Vertical tube-side downflow condenser
(b) Horizontal shell-side condenser
(c) Horizontal tube-side condenser
(11.39) $230,000 \mathrm{lb} / \mathrm{h}$ of propane will enter a condenser as a superheated vapor at $180^{\circ} \mathrm{F}$ and 210 psia . The condensate is to leave the condenser as a subcooled liquid at a temperature of $95^{\circ} \mathrm{F}$ or less, and a maximum pressure drop of 5 psi is specified. The coolant will be water from a cooling tower entering at $80^{\circ} \mathrm{F}$ and 40 psia , with a maximum allowable pressure drop of 10 psi . Use any available software to design a condenser for this service.
(11.40) Use Xist to do the following:
(a) Rate the J-shell condenser designed using TASC in Example 11.10. Is the unit thermally acceptable? Is it hydraulically acceptable? Are there potential tube vibration problems?
(b) Repeat part (a) for the X-shell condenser designed using TASC in Example 11.10.
(c) Obtain a final design for the condenser of Example 11.10.
(11.41) For the service of Example 11.6, use Xist to design a rod-baffle condenser with:
(a) Plain tubes.
(b) Finned tubes.
(11.42) Assuming the condensate is to drain by gravity, size the condensate nozzles for:
(a) The AJU condenser of Example 11.6.
(b) The AXU condenser of Example 11.7.

Assume that the nozzles will be made from schedule 40 pipe.
Ans. (a) One 14-in. nozzle. (b) Two 10 -in. nozzles.

## AIR-COOLED HEAT EXCHANGERS

## Contents

12.1 Introduction ..... 630
12.2 Equipment Description ..... 630
12.3 Air-Side Heat-Transfer Coefficient ..... 637
12.4 Air-Side Pressure Drop ..... 638
12.5 Overall Heat-Transfer Coefficient ..... 640
12.6 Fan and Motor Sizing ..... 640
12.7 Mean Temperature Difference ..... 643
12.8 Design Guidelines ..... 643
12.9 Design Strategy ..... 644
12.10 Computer Software ..... 653

### 12.1 Introduction

Air-cooled heat exchangers are second only to shell-and-tube exchangers in frequency of occurrence in chemical and petroleum processing operations. These units are used to cool and/or condense process streams with ambient air as the cooling medium rather than water. Cooling with air is often economically advantageous, e.g., in arid or semi-arid locations, in areas where the available water requires extensive treatment to reduce fouling, or when additional investment would otherwise be required to expand a plant's existing cooling-water supply. Regulations governing water use and discharge of effluent streams to the environment also tend to favor air cooling. Although the capital cost of an air-cooled exchanger is generally higher, the operating cost is usually significantly lower compared with a water-cooled exchanger. Hence, high energy cost relative to capital cost favors air cooling. Air cooling also eliminates the fouling and corrosion problems associated with cooling water, and there is no possibility of leakage and mixing of water with the process fluid. Thus, maintenance costs are generally lower for air-cooled exchangers.

### 12.2 Equipment Description

### 12.2.1 Overall configuration

In an air-cooled heat exchanger, the hot process fluid flows through a bank of finned tubes, and ambient air is blown across the tubes by one or more axial-flow fans. For applications involving only sensible heat transfer, the tubes are oriented horizontally as shown in Figures 12.1 and 12.2. For condensers, an A-frame configuration (Figure 12.3) is often used, with the condensing vapor flowing downward through the tubes, which are oriented at an angle of $60^{\circ}$ with the horizontal.

In units employing horizontal tubes, the fan may be located either below (forced draft) or above (induced draft) the tube bank. In either case, the air flows upward across the tubes. The fan drive assembly in an induced-draft unit may be mounted below the tube bundle (either on the ground as shown in Figure 12.2 or suspended from the framework), or it may be mounted above the fan. With the former arrangement, the drive assembly is easily accessible for inspection and maintenance, and it is not exposed to the heated air leaving the unit. However, the drive shaft passes through the tube bundle, requiring omission of some tubes, and the relatively long shaft is more susceptible to vibration problems.

The forced-draft configuration provides the simplest and most convenient fan arrangement. With all blower components located below the tube bundle, they are easily accessible for maintenance and are not exposed to the heated air leaving the unit. However, these exchangers are susceptible to hot air recirculation due to the low velocity of the air leaving the unit. Induced-draft operation gives more uniform air flow over the tube bundle and the exit air velocity is several times higher than in forced-draft operation, thereby reducing the potential for hot air to be recirculated back to


Figure 12.1 Configuration of a forced-draft air-cooled heat exchanger (Source: Ref. [1]).
the intake of the unit or other nearby units. Hot air recirculation tends to reduce the capacity of the heat exchanger, thereby requiring a higher air flow rate and/or more heat-transfer surface. The induced-draft configuration also provides some protection from the elements for the tube bundle, which helps to stabilize the operation of the unit when sudden changes in ambient conditions occur.

For a given mass flow rate of air, induced-draft operation in principle entails greater power consumption than forced-draft operation due to the higher volumetric flow rate of the heated air that is handled by the induced-draft fan. In practice, however, this potential disadvantage tends to be offset by the more uniform flow distribution and lower potential for hot gas recirculation obtained


Figure 12.2 Configuration of an induced-draft air-cooled heat exchanger (Source: Ref. [1]).


Figure 12.3 Configuration of an A-frame air-cooled condenser (Source: Spiro-Gills, Ltd. Originally published in Ref. [2]).
with induced-draft operation. As a result, induced-draft units typically do not require significantly more power than forced-draft units, and in some cases may actually require less power [3].

### 12.2.2 High-fin tubing

Finned tubes are almost always used in air-cooled exchangers to compensate for the low air-side heat-transfer coefficient. Radial (annular) fins arranged in a helical pattern along the tube are used. The fin height is significantly larger than that of the low-fin tubes used in shell-and-tube exchangers. Hence, this type of tubing is referred to as high-fin tubing.
Various types of high-fin tubing are available, including:

- Integrally finned
- Bimetallic
- Tension-wound fin
- Embedded fin
- Brazed fin

Integrally finned (K-fin) tubing is made by extruding the fins from the tube metal. It is generally made from copper or aluminum alloys that are relatively soft and easily worked. Since the fins are integral with the root tube, perfect thermal contact is ensured under any operating conditions.

Bimetallic (E-fin) tubes consist of an inner tube, or liner, and an outer tube, or sleeve. The inner tube may be made from any tubing material and has the same dimensions as standard heatexchanger tubing. The outer tube is integrally finned and is usually made of aluminum alloy. The sleeve thickness beneath and between the fins is usually $0.04-0.05 \mathrm{in}$. Since the contact between the two tubes is not perfect, there is a contact resistance at the interface between the tubes. Although this resistance is negligible at low temperatures, it can amount to $10-25 \%$ of the total thermal resistance in operations involving high tube-side fluid temperatures [4]. Hence, this type of tubing is not recommended for tube-side temperatures above $600^{\circ} \mathrm{F}$.

Tension-wound finned tubing is widely used due to its relatively low cost. The fins are formed by winding a strip of the fin material around the tube under tension. The metal strip may be either straight (edge-wound or I-fin) or bent in the shape of the letter L (L-footed or L-fin) as shown in Figure 12.4. The latter configuration provides more contact area between the fin strip and tube surface and also helps protect the tube wall from atmosphere corrosion. Better adhesion and corrosion protection can be achieved by overlapping the "feet" of the L's (LL-fin). The strip metal is subjected to controlled deformation under tension to provide good contact between the strip and the tube wall. Collars at both ends of the tube hold the fin strip in place and maintain the tension. Nevertheless, since the fins are held in place solely by the tension in the metal strip, they can be loosened by operation at high temperatures or by temperature cycling. Therefore, this type of tubing is used for continuous services with tube-side temperatures below $400^{\circ} \mathrm{F}$ (below $250^{\circ} \mathrm{F}$ in the case of I-fin).

Embedded-fin (G-fin) tubing is made by winding a strip of the fin metal into a helical groove machined in the surface of the tube and then securing the strip in place by backfilling the groove with the tube metal (peening). This type of tubing is much more robust than tension-wound tubing and is widely used for this reason. It is applicable for tube-side temperatures up to $750^{\circ} \mathrm{F}$ and in services involving cyclic operation. As shown in Figure 12.4, shoulder-grooved-fin tubing is a type of embedded-fin tubing that combines the characteristics of L - and G -fin tubing. To accommodate the groove in the surface, an additional wall thickness of 1 BWG is used for embedded-fin tubing. Thus, for hydrocarbon liquids, 13 BWG tubes are normally used rather than 14 BWG tubes.

Brazed-fin tubing is made by first winding a trip of the fin material around the tube under tension. The fin and tube metal are then bonded together by brazing. This metallurgical bond minimizes contact resistance and allows operation under more severe conditions than is possible with standard tension-wound or embedded tubing. Tube-side temperatures up to $1000^{\circ} \mathrm{F}$ are permissible with copper fins and up to $1500^{\circ} \mathrm{F}$ with stainless steel fins.

In addition to loosening of the fins, corrosion at the base of the fins may cause the performance of an air-cooled heat exchanger to deteriorate over time. Tension-wound finned tubes are the most


Figure 12.4 High-fin tubing: (a) L-fin, (b) G-fin, (c) Shoulder-grooved fin, and (d) E-fin (bimetallic). I-fin is similar to G-fin except that the fins are not embedded in the tube wall (Source: ACOL 6.30 Help File).
susceptible to corrosion since moisture can penetrate between the fin material and tube wall even with overlapping (LL) fins. Embedded-fin tubing is less susceptible to fin-root corrosion, while bimetallic tubing is very corrosion resistant.

High-fin tubing is made in a variety of sizes and configurations using both tubes and pipes as root stock. Diameters range from 0.5 to 8 in . with fin heights of $0.25-1.5 \mathrm{in}$. The number of fins per inch varies from less than 2 to 12, and the average fin thickness typically ranges from 0.012 to about 0.035 in., although tubing with thicker fins is available from some manufacturers. However, 1 -in. OD tubing with a fin height of 0.5 or 0.625 in . is by far the most widely used in air-cooled heat exchangers. The tube layout is usually triangular with a clearance of $0.125-0.375 \mathrm{in}$. between fin tips. Increasing the clearance reduces air-side pressure drop but increases the size of the tube bundle. The tubes are arranged in shallow rectangular bundles with the number of tube rows usually between three and six. A small number of tube rows is used in order to keep the air-side pressure drop low. The axial-flow fans used in air-cooled heat exchangers are capable of developing a static pressure of 1 in . of water or less, and a maximum pressure drop of $0.5 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$ on the air side is often used as a design specification.
Typical values of parameters for the most common tubing configurations used in air-cooled heat exchangers are given in Table 12.1.

### 12.2.3 Tube bundle construction

Tube bundles are rectangular in shape and usually $6-12 \mathrm{ft}$ wide. Since tube bundles are factory assembled and shipped to the plant site, maximum bundle width is limited by transportation requirements. (In the US the maximum load width for truck transport is 14 ft in most states, but in some

Table 12.1 Characteristics of Typical High-Fin Tube Arrays (Source: Ref. [5])

| Root tube OD (in.) | 1.0 | 1.0 |
| :--- | :--- | :--- |
| Fin height (in.) | 0.500 | 0.625 |
| Fin OD (in.) | 2.00 | 2.25 |
| Average fin height (in.) | $0.012-0.014$ | $0.012-0.014$ |
| Tension wound or embedded | $0.015-0.025$ | $0.015-0.025$ |
| Bimetallic or integral* | 9 | 10 |
| Fins per inch | $30^{\circ}$ | $30^{\circ}$ |
| Tube layout angle | 2.25 | 2.50 |
| Tube pitch (in.) | 3.80 | 5.58 |
| $A_{\text {Tot }} / L$ | 14.5 | 21.4 |
| $A_{\text {Tot }} / A_{o}$ |  |  |
| $A_{\text {Tot }} / A_{i}$ | 17.9 | 26.3 |
| 13 BWG | 17.4 | 25.6 |
| 14 BWG | 16.7 | 24.5 |
| 16 BWG |  |  |
| External surface area per unit bundle face area |  | 80.4 |
| Three tube rows | 60.6 | 107.2 |
| Four tube rows | 80.8 | 134.0 |
| Five tube rows | 101.0 | 160.8 |
| Six tube rows | 121.2 |  |

*Dimensions in this table are approximate for these types of tubing. The root tube OD of integrally finned tubing may be somewhat greater or less than 1 in . The root tube OD is greater for bimetallic tubes due to the sleeve thickness.


Figure 12.5 Typical construction of a tube bundle with plug-type box headers (Source: Ref. [3]).
states it is only 12 ft .) The tubes are either welded to or rolled into long rectangular tubesheets that are welded to box-type headers. Both front and rear headers are equipped with screwed plugs that are aligned with the tube holes as illustrated in Figure 12.5. The plugs can be removed to provide access to the tubes for cleaning and other maintenance.

Headers are also available with flanged end plates that can be removed to provide unencumbered access to the tubesheets. In addition to being more expensive, this type of header is prone to leakage because the long rectangular gasket is difficult to seat properly. It is normally used only


Figure 12.6 Some typical configurations of fan bays in air-cooled heat exchangers (Source: Ref. [5]).
when frequent tube-side maintenance is required and the operating pressure is relatively low. Box headers become impractical at pressures above about 4000 psia due to the large wall thickness required. For these high-pressure applications, the tubes are welded directly into a section of pipe of appropriate schedule number that serves as the header.

For multi-pass operation, the headers are equipped with pass partition plates as shown in Figure 12.5. The tubes are partitioned so that the process fluid flows from the top tube row to lower tube rows. The downward flow of process fluid in combination with the upward flow of air gives an overall flow pattern that is a combination of counter-current and cross flow, and maximizes the mean temperature difference in the heat exchanger.

Tube supports and spacers are provided to hold the tubes securely in place and to dampen tube vibration. The bundle is held together and given structural integrity by side members that are bolted or welded to the headers, tube supports, and the framework that supports the unit.

### 12.2.4 Fans and drivers

Axial-flow fans with four or six blades and diameters of 6-18ft are typically employed in air-cooled heat exchangers, although larger and smaller fans are occasionally used as well. Plastic fan blades are used for air temperatures up to $175^{\circ} \mathrm{F}$; metal (usually aluminum) blades are required for higher air temperatures.

Electric motors are most frequently used as fan drivers, but steam turbines are also used. Motor size is generally $50 \mathrm{hp}(37 \mathrm{~kW}$ ) or less. Speed reduction is usually accomplished using V-belts, high-torque-drive (HTD) belts, or reduction gear boxes. Hydraulic variable-speed drives may also be used. V-belt drives are limited to motor sizes of $30 \mathrm{hp}(22 \mathrm{~kW}$ ) or less, while HTD can be used with motor sizes up to 50 hp [6] and is the most widespread.

Variable-pitch fans are commonly used to provide process-side temperature control in air-cooled exchangers. The blade pitch is automatically adjusted to provide the required air flow to maintain the desired outlet temperature of the process fluid. This is accomplished using a temperature controller and a pneumatically operated blade adjustment mechanism. Reducing air flow also reduces power consumption when the ambient temperature is low. Similar results can be achieved using variablespeed drives.

The fans are situated in bays, which are self-contained sections of an air-cooled heat exchanger. A bay consists of one or more tube bundles, the fans and drive assemblies that supply air to the bundles, and the associated framework and support structures. Except in unusual circumstances, multiple tube bundles are placed side by side in the bay. Bays are usually designed for one to three fans, with two-fan bays being most common.

Fan bays can be preassembled and shipped to the plant site provided they are small enough to meet transportation requirements. Otherwise, they must be assembled in the field, which adds to the cost of the heat exchanger. An air-cooled heat exchanger consists of one or more fan bays, with multiple bays operating in parallel. Some typical configurations are illustrated in Figure 12.6.


Figure 12.7 Configuration of a forced-draft air-cooled heat exchanger designed for external recirculation of warm air during cold weather. The coil in the diagram is the tube bundle (Source: Ref. [5]).

Additional equipment associated with each fan includes the fan casing (also called the fan ring or shroud) and the plenum. The casing forms a cylindrical enclosure around the fan blades. It is often tapered on the intake end to reduce the pressure loss. A bell-shaped inlet is the most effective for this purpose, but conical and other types of inlets are also used. The plenum is the structure that connects the fan with the tube bundle. In forced-draft operation, the plenum serves to distribute the air delivered by the fan across the face of the tube bundle. With induced-draft operation, the plenum delivers the air from the top to the tube bundle to the fan intake. Box-type plenums are used most frequently in forced-draft units, whereas tapered plenums are the norm for induced-draft operation.

Induced-draft fans are sometimes equipped with diffusers in order to reduce power consumption. A diffuser is essentially a short stack with an expanding cross-section that serves to lower the velocity of the exhaust air. Although there is some friction loss in the diffuser, the net result is an increase in the static pressure of the exhaust air and a concomitant reduction in the power consumed by the fan.

### 12.2.5 Equipment for cold climates

Air-cooled heat exchangers are designed to operate over a wide range of environmental conditions, including ambient temperatures from $-60^{\circ} \mathrm{F}$ to $130^{\circ} \mathrm{F}$. Special design features are employed for operation in cold climates in order to prevent freezing of the process fluid. If the wall temperature of a tube carrying a hydrocarbon stream reaches the pour point of the hydrocarbon, the liquid will congeal around the wall, thereby reducing the flow area and increasing the tube-side pressure drop. If water is present in the process stream, ice can form around the tube wall with similar effect. Likewise, methane hydrates can form on the tube walls of natural gas coolers.

The standard method for preventing freezing is to intentionally recirculate some of the warm air leaving the unit in order to raise the temperature of the intake air. This can be accomplished in a number of ways, depending on whether forced-draft or induced-draft operation is employed and the severity of the winter climate [7]. Figure 12.7 shows a typical configuration for a forced-draft unit with external recirculation, which provides the most reliable freeze protection. The unit is completely contained in an enclosure equipped with adjustable louvers to control both exhaust and intake air rates. The manual louvers are adjusted seasonally while the automatic louvers are adjusted continuously via pneumatic mechanisms directed by a temperature controller that maintains the temperature of the air entering the tube bundle at an appropriate level. A recirculation chamber projects beyond the front and rear headers, providing ducts where cold ambient air mixes with warm recirculated air. The flow rate of recirculated air is controlled by internal louvers in the ducts
that open as the external intake louvers close. Either variable-pitch or variable-speed fans are used in these units. The pitch or speed is automatically adjusted by a second temperature controller that maintains the outlet temperature of the process fluid at the desired temperature.

A row of steam tubes is installed below the tube bundle to warm the air stream during startups and shutdowns in cold weather. These tubes are typically the same type and size as those in the tube bundle, but with a pitch equal to twice that of the bundle. The steam tubes are commonly referred to as a steam coil.

### 12.3 Air-Side Heat-Transfer Coefficient

The flow of air over banks of finned tubes has been extensively studied and numerous correlations for this geometry are available in the open literature. Among these, the correlation of Briggs and Young [8] has been widely used:

$$
\begin{equation*}
N u=0.134 \operatorname{Re}^{0.681} \operatorname{Pr}^{1 / 3}(\ell / b)^{0.2}(\ell / \tau)^{0.1134} \tag{12.1}
\end{equation*}
$$

where

$$
\begin{aligned}
N u & =h_{o} D_{r} / k \\
R e & =D_{r} V_{\max } \rho / \mu
\end{aligned}
$$

$V_{\max }=$ maximum air velocity in tube bank
$\ell=$ fin spacing
$b=$ fin height
$\tau=$ fin thickness
$k=$ thermal conductivity of air
$\rho=$ density of air
$\mu=$ viscosity of air
$h_{o}=$ air-side heat-transfer coefficient
The correlation is based on experimental data for tube banks containing six rows of tubes laid out on equilateral triangular pitch. The data covered the following ranges of parameters:

$$
\begin{aligned}
1000 & \leq R e \leq 18,000 \\
0.438 \mathrm{in} . & \leq D_{r} \leq 1.61 \mathrm{in} . \\
0.056 \mathrm{in} . & \leq b \leq 0.6525 \mathrm{in} . \\
0.013 \mathrm{in} . & \leq \tau \leq 0.0795 \mathrm{in} . \\
0.035 \mathrm{in} . & \leq \ell \leq 0.117 \mathrm{in} . \\
0.96 \mathrm{in} . & \leq P_{T} \leq 4.37 \mathrm{in} .
\end{aligned}
$$

The fin spacing is related to the number, $n_{f}$, of fins per unit length by the following equation:

$$
\begin{equation*}
\ell=1 / n_{f}-\tau \tag{12.2}
\end{equation*}
$$

The maximum air velocity in the tube bank is related to the face velocity (the average air velocity approaching the first row of tubes) by the following equation:

$$
\begin{equation*}
V_{\max } / V_{\text {face }}=A_{\text {face }} / A_{\min } \tag{12.3}
\end{equation*}
$$

where $A_{\min }$ is the minimum flow area in the tube bank and $A_{\text {face }}$ is the face area. For equilateral triangular pitch, the minimum flow area is the open area between two adjacent tubes. The clearance between adjacent tubes is the tube pitch minus the root diameter, giving a gross gap area of $\left(P_{T}-D_{r}\right) L$, where $L$ is the tube length. The area occupied by the fins on both tubes is approximately $2 n_{f} L b \tau$, giving:

$$
\begin{equation*}
A_{\min }=\left(P_{T}-D_{r}\right) L-2 n_{f} L b \tau \tag{12.4}
\end{equation*}
$$

The air that flows through this gap approaches the tube bank over the rectangle of length $L$ and width $P_{T}$, extending from the center of one tube to the center of the adjacent tube. Thus, the face area corresponding to two adjacent tubes is simply $P_{T} L$. Substituting this value and $A_{\text {min }}$ from Equation (12.4) into Equation (12.3) gives:

$$
\begin{equation*}
V_{\max }=\frac{P_{T} V_{\text {face }}}{P_{T}-D_{r}-2 n_{f} b \tau} \tag{12.5}
\end{equation*}
$$

Based on a study conducted at HTRI, the following correlation is recommended by Ganguli et al. [9]:

$$
\begin{equation*}
N u=0.38 \operatorname{Re}^{0.6} \operatorname{Pr}^{1 / 3}\left(A_{T o t} / A_{o}\right)^{-0.15} \tag{12.6}
\end{equation*}
$$

where
$A_{\text {Tot }}=$ total external surface area of finned tube
$A_{o}=\pi D_{r} L=$ total external surface area of root tube
Equation (12.6) is valid for tube banks with three or more rows of tubes on triangular pitch and is based on data covering the following parameter ranges [10]:

$$
\begin{aligned}
1800 & \leq R e \leq 10^{5} \\
0.44 \text { in. } & \leq D_{r} \leq 2.0 \mathrm{in} . \\
0.23 \text { in. } & \leq b \leq 0.75 \mathrm{in} . \\
0.01 \text { in. } & \leq \tau \leq 0.022 \mathrm{in} . \\
1.08 \text { in. } & \leq P_{T} \leq 3.88 \mathrm{in} . \\
1 & \leq A_{T o t} / A_{o} \leq 50 \\
7 & \leq \text { fins per inch } \leq 11
\end{aligned}
$$

### 12.4 Air-Side Pressure Drop

The pressure drop for flow across a bank of high-finned tubes is given by the following equation:

$$
\begin{equation*}
\Delta P_{f}=\frac{2 f N_{r} G^{2}}{g_{c} \rho \phi} \tag{12.7}
\end{equation*}
$$

where
$f=$ Fanning friction factor
$N_{r}=$ number of tube rows
$G=\rho V_{\text {max }}$
$g_{c}=$ unit conversion factor
$\phi=$ viscosity correction factor
This equation is essentially the same as Equation (6.7). In air-cooled heat exchangers, the viscosity correction on the air side is negligible and, hence, $\phi$ can be set to unity. Furthermore, when English units are used, the pressure drop in these exchangers is usually expressed in inches of water. It is convenient for design work to incorporate the unit conversion factors into the constant in Equation (12.7) to obtain:

$$
\begin{equation*}
\Delta P_{f}=\frac{9.22 \times 10^{-10} f N_{r} G^{2}}{\rho} \tag{12.8a}
\end{equation*}
$$

where
$\Delta P_{f} \propto$ in. $\mathrm{H}_{2} \mathrm{O}$
$G \propto \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2}$
$\rho \propto \mathrm{lbm} / \mathrm{ft}^{3}$
The corresponding relationship in SI units is:

$$
\begin{equation*}
\Delta P_{f}=\frac{2 f N_{r} G^{2}}{\rho} \tag{12.8b}
\end{equation*}
$$

where

```
\(\Delta P_{f} \propto \mathrm{~Pa}\)
    \(G \propto \mathrm{~kg} / \mathrm{s} \cdot \mathrm{m}^{2}\)
    \(\rho \propto \mathrm{kg} / \mathrm{m}^{3}\)
```

For the flow of air across tube banks with equilateral triangular pitch, the friction factor correlation of Robinson and Briggs [11] has been widely used:

$$
\begin{equation*}
f=18.93 R e^{-0.316}\left(P_{T} / D_{r}\right)^{-0.927} \tag{12.9}
\end{equation*}
$$

The correlation is based on experimental data for tube banks containing six rows of tubes with the following ranges of parameters:

$$
\begin{aligned}
2000 & \leq R e \leq 50,000 \\
0.734 \mathrm{in} . & \leq D_{r} \leq 1.61 \mathrm{in} . \\
0.4135 \mathrm{in} . & \leq b \leq 0.588 \mathrm{in} . \\
0.0158 \mathrm{in} . & \leq \tau \leq 0.0235 \mathrm{in} . \\
0.0729 \mathrm{in} . & \leq \ell \leq 0.1086 \mathrm{in} . \\
1.687 \mathrm{in} . & \leq P_{T} \leq 4.500 \mathrm{in} .
\end{aligned}
$$

An alternative correlation was developed by Ganguli et al. [9]:

$$
\begin{equation*}
f=\left\{1+\frac{2 e^{-(a / 4)}}{1+a}\right\}\left\{0.021+\frac{27.2}{R e_{e f f}}+\frac{0.29}{R e_{e f f}^{0.2}}\right\} \tag{12.10}
\end{equation*}
$$

where

$$
\begin{aligned}
a & =\left(P_{T}-D_{f}\right) / D_{r} \\
R e_{e f f} & =\operatorname{Re}(\ell / b) \\
D_{f} & =D_{r}+2 b=\text { fin OD }
\end{aligned}
$$

The parameter ranges covered by the data upon which this correlation is based were not given by Ganguli et al., but the database included that of Robinson and Briggs [8]. Hence, the parameter ranges exceed those given above for the Robinson-Briggs correlation.

In addition to the tube bank, other sources of friction loss on the air side include the following:

- The support structure and enclosure (including louvers, screens, and/or fencing if present)
- Fan casings and fan supports
- The plenums
- The steam coil (if present)
- Screens used as fan guards or hail guards for the tube bundle (if present)
- Other obstructions in the air flow path, such as the drive assemblies and walkways
- Diffusers (if present)

Although the friction loss due to each of these factors is usually small compared with the pressure loss in the tube bank, in aggregate the losses often amount to between $10 \%$ and $25 \%$ of the bundle pressure drop. Procedures for estimating these losses can be found in Ref. [10]; they will not be given here.

### 12.5 Overall Heat-Transfer Coefficient

Equation (4.26) is used to calculate the overall design heat-transfer coefficient for low-fin tubing. This equation is modified for high-fin tubing by adding a term to account for the contact resistance between the fin and the tube wall. The result is:

$$
\begin{equation*}
U_{D}=\left[\left(\frac{1}{h_{i}}+R_{D i}\right) \frac{A_{T o t}}{A_{i}}+\frac{A_{T o t} \ln \left(D_{r} / D_{i}\right)}{2 \pi k_{t u b e} L}+\frac{R_{\text {con }} A_{T o t}}{A_{c o n}}+\frac{1}{\eta_{w} h_{o}}+\frac{R_{D o}}{\eta_{w}}\right]^{-1} \tag{12.11}
\end{equation*}
$$

where
$R_{\text {con }}=$ contact resistance between fin and tube wall
$A_{\text {con }}=$ contact area between fin and tube wall
Equation (12.11) is applicable to all types of high-fin tubing with the exception of bimetallic (E-fin) tubes. (Note that for integrally finned tubes, the contact resistance is zero.) For E-fin tubing, the thermal resistance of the outer tube, or sleeve, must also be accounted for. In this case, the contact resistance is between the inner tube and the sleeve, so that $A_{\text {con }}=\pi D_{o} L=$ external surface area of inner tube. Thus,

$$
\begin{equation*}
U_{D}=\left[\left(\frac{1}{h_{i}}+R_{D i}\right) \frac{A_{T o t}}{A_{i}}+\frac{A_{T o t} \ln \left(D_{o} / D_{i}\right)}{2 \pi k_{t u b e} L}+\frac{A_{T o t} \ln \left(D_{o, s l} / D_{i, s l}\right)}{2 \pi k_{s l} L}+\frac{R_{c o n} A_{T o t}}{\pi D_{o} L}+\frac{1}{\eta_{w} h_{o}}+\frac{R_{D o}}{\eta_{w}}\right]^{-1} \tag{12.12}
\end{equation*}
$$

where
$D_{o}=$ external diameter of inner tube
$D_{i, s l}=$ inner sleeve diameter
$D_{o, s l}=$ outer sleeve diameter
$k_{s l}=$ thermal conductivity of sleeve
It is common practice to neglect contact resistance unless data are available from the tubing manufacturer. If available, an upper bound for the contact resistance can be used to provide a conservative estimate for the overall coefficient.

Approximate values of the overall heat-transfer coefficient suitable for preliminary design calculations are given in Table 12.2. These values are based on 1 in . OD tubes with 10 fins per inch and a fin height of 0.625 in . (Note: Overall heat-transfer coefficients are sometimes quoted on the basis of bare tube surface area. Such values are about 20 times larger than those given here, which are based on total external surface area.)

### 12.6 Fan and Motor Sizing

Fan performance is characterized in terms of the fan static pressure. The total pressure in a flowing fluid is defined as the sum of the static pressure and the dynamic (or velocity) pressure, the latter comprising the kinetic energy term in Bernoulli's equation. Thus,

$$
\begin{equation*}
P_{\text {Total }}=P+\frac{\alpha \rho V^{2}}{2 g_{c}} \tag{12.13}
\end{equation*}
$$

Table 12.2 Typical Values of Overall Heat-transfer Coefficient in Air-cooled Heat Exchangers (Source: Ref. 5 and Hudson Products Corporation, Sugarland, TX, www.hudsonproducts.com)

| Service | $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :--- | :--- |
| Liquid Coolers |  |
| Engine jacket water | $6.1-7.3$ |
| Process water | $5.7-6.8$ |
| Ethylene glycol (50\%) - water | $4.4-4.9$ |
| Light hydrocarbons | $4.2-5.7$ |
| Light gas oil | $3.3-4.2$ |
| Light naphtha | 4.2 |
| Hydroformer and platformer liquids | 4.0 |
| Residuum | $0.5-1.4$ |
| Tar | $0.2-0.5$ |
| Gas coolers |  |
| Air or flue gas, 50 psig $(\Delta P=1 \mathrm{psi})$ | 0.5 |
| Air or flue gas, 100 psig $(\Delta P=2$ psi) | 0.9 |
| Air or flue gas, 100 psig $(\Delta P=3 \mathrm{psi})$ | 1.4 |
| Hydrocarbon gases, $15-50 \mathrm{psig}(\Delta P=1 \mathrm{psi})$ | $1.4-1.9$ |
| Hydrocarbon gases, $50-250 \mathrm{psig}(\Delta P=3 \mathrm{psi})$ | $2.3-2.8$ |
| Hydrocarbon gases, 250-1500 psig $(\Delta P=5 \mathrm{psi})$ | $3.3-4.2$ |
| Ammonia reactor stream | $4.2-5.2$ |
| Condensers |  |
| Light hydrocarbons | $4.5-5.0$ |
| Light gasoline | 4.5 |
| Light naphtha | $3.8-4.7$ |
| Heavy naphtha | $3.3-4.2$ |
| Reactor effluent (platformers, hydroformers, | $3.8-4.7$ |
| reformers |  |
| Ammonia | $5.0-5.9$ |
| Amine reactivator | $4.7-5.7$ |
| Freon 12 | $3.5-4.2$ |
| Pure steam (0-20 psig $)$ | $6.3-9.4$ |
| Steam with non-condensables | 3.3 |

where
$\alpha=$ kinetic energy correction factor
$\rho=$ fluid density
$V=$ mass-average fluid velocity

The kinetic energy correction factor depends on the velocity profile and is equal to unity for a uniform profile, which is usually a reasonable approximation for turbulent flow. The fan static pressure, $F S P$, is defined as follows:

$$
\begin{equation*}
F S P=\left(\Delta P_{\text {Total }}\right)_{f a n}-\frac{\alpha_{f r} \rho_{f r} V_{f r}^{2}}{2 g_{c}} \tag{12.14}
\end{equation*}
$$

where
$\left(\Delta P_{\text {Total }}\right)_{\text {fan }}=$ change in total pressure between fan inlet and outlet
The subscript "fr" denotes conditions for the air leaving the fan ring. Note that FSP is the rise in static pressure across the fan only if the air velocity at the fan inlet is zero.

Assuming that the ambient air velocity is zero and neglecting the static pressure difference in the ambient air at inlet and outlet elevations, a pressure balance around an air-cooled heat exchanger yields the following result:

$$
\begin{equation*}
F S P=\sum_{j} \Delta P_{j}+\frac{\alpha_{e x} \rho_{e x} V_{e x}^{2}}{2 g_{c}}-\frac{\alpha_{f r} \rho_{f r} V_{f r}^{2}}{2 g_{c}} \tag{12.15}
\end{equation*}
$$

where
$\sum_{j} \Delta P_{j}=$ sum of all air-side losses in the unit
The subscript "ex" denotes conditions for the exhaust air leaving the unit. The two kinetic energy terms partially cancel one another and are often neglected; with this approximation, the fan static pressure is equal to the total air-side pressure loss in the unit.

The power that must be supplied to the fan (the brake power) is given by the following equation:

$$
\begin{equation*}
\dot{W}_{f a n}=\frac{\left(\Delta P_{\text {Total }}\right)_{f a n} \dot{v}_{f a n}}{\eta_{f a n}} \tag{12.16a}
\end{equation*}
$$

where
$\dot{v}_{f a n}=$ volumetric flow rate of air through fan
$\eta_{f a n}=($ total $)$ fan efficiency
With the pressure loss expressed in Pascals and the volumetric flow rate in cubic meters per second, Equation (12.16a) gives the brake power in Watts. For use with English units, it is convenient to include a unit conversion factor in the equation as follows:

$$
\begin{equation*}
\dot{W}_{f a n}=\frac{\left(\Delta P_{\text {Total }}\right)_{f a n} \dot{v}_{f a n}}{6342 \eta_{f a n}} \tag{12.16b}
\end{equation*}
$$

where

$$
\begin{aligned}
& \left(\Delta P_{\text {Total }}\right)_{\text {fan }} \propto \text { in. } \mathrm{H}_{2} \mathrm{O} \\
& \dot{\dot{f}}_{\text {fan }} \propto \mathrm{acfm} \text { (actual cubic feet per minute) } \\
& \dot{W}_{\text {fan }} \propto \mathrm{hp} \text { (horsepower) }
\end{aligned}
$$

Note: Two fan efficiencies are in common use, the total efficiency used here and the static efficiency. The latter is used in Equation (12.16) with the fan static pressure replacing the total pressure change in the numerator. The static efficiency is always lower than the total efficiency.

The power that must be supplied by the motor is:

$$
\begin{equation*}
\dot{W}_{\text {motor }}=\frac{\dot{W}_{\text {fan }}}{\eta_{s r}} \tag{12.17}
\end{equation*}
$$

where $\eta_{s r}$ is the efficiency of the speed reducer. Finally, the power drawn by the motor is given by:

$$
\begin{equation*}
\dot{W}_{\text {used }}=\frac{\dot{W}_{\text {motor }}}{\eta_{\text {motor }}} \tag{12.18}
\end{equation*}
$$

where $\eta_{\text {motor }}$ is the motor efficiency. For estimation purposes, reasonable values for the efficiencies are $70-75 \%$ for the fan and $95 \%$ each for the motor and speed reducer.

Fan selection is accomplished by means of fan performance curves and tables that are supplied by fan manufacturers. For each fan model, these graphs and/or tables present the relationships among air volumetric flow rate, fan static pressure, fan speed, brake power, and fan efficiency. The data are for air at standard conditions of $1 \mathrm{~atm}, 70^{\circ} \mathrm{F}$, and $50 \%$ relative humidity, for which the density is $0.075 \mathrm{lbm} / \mathrm{ft}^{3}$. Hence, corrections must be made for differences in air density between actual operating conditions and standard conditions. Another important aspect of fan selection is fan noise, which depends on blade-tip speed, number of blades, and blade design. To simplify matters, most fan manufacturers offer fan-selection software that is free upon request or in some cases can be downloaded directly from the manufacturer's website. These programs will select the best fan (or fans) for a specified service from the company's product line. A choice of power consumption, fan noise, or cost is usually offered for the selection criterion.
Another consideration in fan selection is the need to achieve a good distribution of air flow across the face of the tube bundle. The fan diameter should be such that the area covered by the fans is at least $40 \%$ of the total bundle face area. In addition, the fan diameter must be at least 6 in . less than the total width of all tube bundles in the fan bay.

Motors are rated according to their output power, which is calculated by Equation (12.17). The calculated value must be rounded upward to a standard motor size (see Appendix 12.B). Motors are frequently oversized to provide operational flexibility and allowance for contingencies.

### 12.7 Mean Temperature Difference

The LMTD correction factor for an air-cooled heat exchanger depends on the number of tube rows, the number of tube passes, the pass arrangement, and whether the tube-side fluid is mixed (in a header) or unmixed (in U-tubes) between passes. Charts for a number of industrially significant configurations are given by Taborek [12], and the most important of these are reproduced in Appendix 12.A. The charts can be grouped into three categories as follows:
(1) One tube pass and three (Figure 12.A.1), four (Figure 12.A.2), or more tube rows. With more than four tube rows, the $F$-factor is nearly the same as for unmixed-unmixed cross flow. Hence, the chart for an X-shell exchanger given in Appendix 11.A can be used for these cases.
(2) Multiple tube passes with one pass per tube row. Charts are given for three rows and three passes (Figure 12.A.3) and four rows and four passes (Figure 12.A.4). With more than four passes, the flow pattern approaches true counter flow [12], and the $F$-factor should be close to unity for most practical configurations. Figure 12.A. 4 provides a conservative (lower bound) estimate of $F$ for these cases.
(3) Multiple tube passes with multiple tube rows per pass. Of the many possible arrangements of this type, a chart is available only for the case of four tube rows and two passes with two rows per pass. The tube-side fluid is mixed (in a return header) between passes as shown in Figure 12.A.5. This chart also provides a conservative estimate of F for two other common configurations, namely, six tube rows with two passes (three tube rows per pass) and six tube rows with three passes (two tube rows per pass), both cases involving mixing of the tube-side fluid between passes.

### 12.8 Design Guidelines

### 12.8.1 Tubing

Tubing selection should be based on the tube-side fluid temperature and the potential for corrosion of the external tube surface as discussed in Section 12.2.2. Furthermore, it is recommended to choose one of the tubing configurations given in Table 12.1.

### 12.8.2 Air flow distribution

In order to obtain an even distribution of air flow across the tube bundle, the fan area should be at least $40 \%$ of the bundle face area as previously noted. In addition, for two-fan bays, the ratio of tube length to bundle width should be in the range of $3-3.5$. It is also desirable to have a minimum of four tube rows.

Note: In chemical plants and petroleum refineries, air-cooled heat exchangers are often mounted on pipe racks in order to conserve plot space. In this situation, the configuration of the unit may be dictated by the width of the pipe rack.

### 12.8.3 Design air temperature

An air-cooled heat exchanger must be designed to operate at summertime conditions. However, using the highest annual ambient air temperature to size the unit generally produces a very conservative and overly expensive design. Therefore, the usual practice is to use an air temperature corresponding to the 97 th or 98 th percentile, i.e., a temperature that is exceeded only $2-3 \%$ of the time. The appropriate design temperature can be determined from meteorological data for the plant site.

### 12.8.4 Outlet air temperature

For induced-draft operation, the outlet air temperature should be limited to about $220^{\circ} \mathrm{F}$ in order to prevent damage to fan blades and bearings. These parts may nevertheless be exposed to high temperatures in the event of fan failure. Therefore, forced-draft operation should be considered if the tube-side fluid temperature is greater than $350^{\circ} \mathrm{F}$.

### 12.8.5 Air velocity

The air velocity based on bundle face area and air at standard conditions is usually between 400 and $800 \mathrm{ft} / \mathrm{min}$, with a value of $500-700 \mathrm{ft} / \mathrm{min}$ being typical for units with four to six tube rows. A value in this range will usually provide a reasonable balance between air-side heat transfer and pressure drop.

### 12.8.6 Construction standards

Most air-cooled heat exchangers for industrial applications, in petroleum refineries and elsewhere, are manufactured in accordance with API Standard 661, Air-cooled Heat Exchangers for General Refinery Services, published by the American Petroleum Institute (www.api.org). Similar to the TEMA standards for shell-and-tube exchangers, API 661 provides specifications for the design, fabrication, and testing of air-cooled heat exchangers. The recommendations given in this chapter are consistent with this standard, which should be consulted for further details, particularly in regard to structural and mechanical aspects of design. One additional item of note relates to differential thermal expansion. If the tube-side fluid temperatures entering one pass and leaving the next pass differ by more than $200^{\circ} \mathrm{F}$, a split header is required. Such a header consists of two separate headers, one above the other, each containing the tubes from one of the two passes in question. This arrangement allows the tubes in each of the two passes to expand independently of one another, thereby preventing damage due to thermal stresses.

### 12.9 Design Strategy

The basic design procedure for air-cooled heat exchangers is similar to that for shell-and-tube exchangers. An initial configuration for the unit is obtained using an approximate overall heattransfer coefficient together with the design guidelines given above. Rating calculations are then performed and the initial design is modified as necessary until an acceptable configuration is arrived at.

An important preliminary step in the design process is the selection of the outlet air temperature. This parameter has a major effect on exchanger economics. Increasing the outlet air temperature
reduces the amount of air required, which reduces the fan power and, hence, the operating cost. However, it also reduces the air-side heat-transfer coefficient and the mean temperature difference in the exchanger, which increases the size of the unit and, hence, the capital investment. The same situation exists with water-cooled heat exchangers, but the feasible range of outlet temperatures tends to be significantly greater for air-cooled exchangers. Thus, optimization with respect to outlet air temperature (or equivalently, air flow rate) is an important aspect of air-cooled heat-exchanger design. In this chapter the primary concern is obtaining a workable (and reasonable) design rather than an optimal design. However, the importance of optimization in this context should not be overlooked.

## Example 12.1

A liquid hydrocarbon stream with a flow rate of $250,000 \mathrm{lb} / \mathrm{h}$ is to be cooled from $250^{\circ} \mathrm{F}$ to $150^{\circ} \mathrm{F}$ in an air-cooled heat exchanger. The unit will be mounted at grade and there are no space limitations at the site. The design ambient air temperature is $95^{\circ} \mathrm{F}$ and the site elevation is 250 ft above mean sea level. An outlet air temperature of $150^{\circ} \mathrm{F}$ is specified for the purpose of this example. Average properties of the hydrocarbon and air are given in the table below. A fouling factor of $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ is required for the hydrocarbon, which is not corrosive, and a maximum pressure drop of 20 psi is specified for this stream. Inlet pressure will be 50 psia . The maximum allowable air-side pressure drop is $0.5 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$. Design an air-cooled heat exchanger for this service:

| Property | Hydrocarbon at $200^{\circ} \mathrm{F}$ | Air at $122.5^{\circ} \mathrm{F}^{*}$ |
| :--- | :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.55 | 0.241 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.082 | 0.0161 |
| $\mu(\mathrm{lbm} / \mathrm{ft} \cdot \mathrm{h})$ | 1.21 | 0.0467 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 49.94 | 0.0685 |
| $P r$ | 8.12 | 0.70 |

*Data are for $\mathrm{T}=120^{\circ} \mathrm{F}$ from Table A.5.

## Solution

(a) Make initial specifications.
(i) Tubing type

G-fin tubing with carbon steel tubes and aluminum fins is specified based on its excellent durability. It is assumed that the environment at the plant site is not highly corrosive; otherwise, bimetallic tubing would be a better choice.
(ii) Tube size and layout

One inch OD, 13 BWG tubes with 10 fins per inch and a fin height of 0.625 in . are specified with reference to Table 12.1. The tube layout is triangular $\left(30^{\circ}\right)$ with a tube pitch of 2.5 in .
(iii) Draft type

Since the process fluid temperature is below $350^{\circ} \mathrm{F}$, an induced-draft unit will be used. For simplicity, diffusers are not specified and it is assumed that winterization of the unit is unnecessary.
(iv) Headers

The pressure is low and based on the specified tube-side fouling factor, frequent cleaning is not anticipated. Therefore, plug-type headers will be used.
(b) Energy balances.

$$
q=\left(\dot{m} C_{P} \Delta T\right)_{H C}=250,000 \times 0.55 \times 100=13,750,000 \mathrm{Btu} / \mathrm{h}
$$

For the specified outlet air temperature of $150^{\circ} \mathrm{F}$, the required mass flow rate of air is:

$$
\dot{m}_{a i r}=\frac{q}{\left(C_{P} \Delta T\right)_{\text {air }}}=\frac{13,750,000}{0.241 \times 55}=1,037,344 \mathrm{lbm} / \mathrm{h}
$$

(c) LMTD.

$$
\left(\Delta T_{\ln }\right)_{c f}=\frac{100-55}{\ln (100 / 55)}=75.27^{\circ} \mathrm{F}
$$

(d) LMTD correction factor.

This factor depends on the number of tube rows and tube passes, which have not yet been established. Therefore, in order to estimate the required heat-transfer surface area, $F=0.9$ is assumed.
(e) Estimate $U_{D}$.

Based on Table 12.2 , a value of $4.5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ is assumed, which is in the expected range for light hydrocarbon liquid coolers.
(f) Calculate heat-transfer area.

$$
A=\frac{q}{U_{D} F\left(\Delta T_{\ln }\right)_{c f}}=\frac{13,750,000}{4.5 \times 0.9 \times 75.27}=45,105 \mathrm{ft}^{2}
$$

(g) Number of tube rows, tube length, and number of tubes.

The bundle face area required for a given (standard) face velocity is:

$$
A_{f a c e}=\frac{\dot{m}_{\text {air }}}{\rho_{\text {std }} V_{\text {face }}}
$$

Assuming a (standard) face velocity of $600 \mathrm{ft} / \mathrm{min}$ from the design guidelines gives:

$$
A_{\text {face }}=\frac{1,037,344 / 60}{0.075 \times 600}=384.2 \mathrm{ft}^{2}
$$

Thus, the ratio of heat-transfer surface area to bundle face area is:

$$
A / A_{\text {face }}=45,105 / 384.2=117.4
$$

From Table 12.1, the closest ratio is 107.2 for four tube rows. Using this value, the required face area is:

$$
A_{\text {face }}=45,105 / 107.2=420.8 \mathrm{ft}^{2}
$$

Based on the design guidelines, a tube length, $L$, of three times the bundle width, $W$, is assumed, giving:

$$
A_{\text {face }}=420.8=W L=3 W^{2}
$$

Thus,

$$
\begin{aligned}
W & =11.84 \mathrm{ft} \\
L & =3 \times 11.84 \cong 36 \mathrm{ft}
\end{aligned}
$$

The number of tubes is found using the value of $A_{\text {Tot }} / L=5.58$ from Table 12.1.

$$
n_{t}=\frac{A}{\left(A_{T o t} / L\right) \times L}=\frac{45,105}{5.58 \times 36}=224.5
$$

Taking the closest integer divisible by four gives 224 tubes with 56 tubes per row. The corresponding bundle width is the tube pitch times the number of tubes per row. Allowing 2 in . for side clearances gives:

$$
W=2.5 \times 56+2=142 \mathrm{in} .=11.83 \mathrm{ft}
$$

The actual bundle face area and (standard) face velocity are:

$$
\begin{gathered}
A_{\text {face }}=W L=11.83 \times 36 \cong 426 \mathrm{ft}^{2} \\
V_{\text {face }, \text { std }}=\frac{\dot{m}_{\text {air }}}{\rho_{\text {std }} A_{\text {face }}}=\frac{1,037,344 / 60}{0.075 \times 426}=541 \mathrm{ft} / \mathrm{min}
\end{gathered}
$$

Note: It is assumed that the fan drives will be located above the tube bundle. Therefore, no allowance is made for blade-shaft lanes in the tube bundle.
(h) Number of tube passes.

The tube-side fluid velocity is:

$$
V=\frac{\dot{m}_{i}\left(n_{p} / n_{t}\right)}{\rho \pi D_{i}^{2} / 4}=\frac{(250,000 / 3600)\left(n_{p} / 224\right)}{49.94 \times \pi(0.810 / 12)^{2} / 4}=1.73 n_{p} \mathrm{ft} / \mathrm{s}
$$

Two, three, or four passes will give a velocity in the range of $3-8 \mathrm{ft} / \mathrm{s}$. Since the tube-side pressure drop allowance is fairly generous, four passes are chosen for the first trial in order to maximize the heat-transfer coefficient and minimize fouling. Checking the Reynolds number:

$$
R e=\frac{4 \dot{m}_{i}\left(n_{p} / n_{t}\right)}{\pi D_{i} \mu}=\frac{4 \times 250,000(4 / 224)}{\pi(0.81 / 12) \times 1.21}=69,594
$$

The flow is fully turbulent and, hence, the configuration is satisfactory. This completes the preliminary design calculations.
(i) LMTD correction factor.

The correct value of the LMTD correction factor can now be determined using Figure 12.A5.:

$$
\begin{aligned}
& R=\frac{250-150}{150-95} \cong 1.82 \\
& P=\frac{150-95}{250-95} \cong 0.35 \\
& F \cong 0.99 \text { from chart }
\end{aligned}
$$

(j) Calculate required overall coefficient.

$$
U_{\text {req }}=\frac{q}{A F\left(\Delta T_{\ln }\right)_{c f}}=\frac{13,750,000}{(224 \times 5.58 \times 36) \times 0.99 \times 75.27}=4.10 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

(k) Calculate $h_{i}$.

$$
\begin{aligned}
D_{i} & =0.81 / 12=0.0675 \mathrm{ft} \\
R e & =69,594 \text { from step }(\mathrm{h}) \\
h_{i} & =\left(k / D_{i}\right) \times 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{1 / 3}\left(\mu / \mu_{w}\right)^{0.14} \\
& =(0.082 / 0.0675) \times 0.023(69,594)^{0.8}(8.12)^{1 / 3}(1.0) \\
h_{i} & =420 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(l) Calculate $h_{o}$.

The maximum air velocity in the tube bundle is calculated using Equation (12.5). The face velocity is first converted from standard conditions to conditions at the average air temperature. The fin thickness is taken as 0.013 in .

$$
\begin{aligned}
V_{\text {face }, \text { ave }} & =V_{\text {face,std }}\left(\rho_{\text {std }} / \rho_{\text {ave }}\right)=541(0.075 / 0.0685)=592 \mathrm{ft} / \mathrm{min} \\
V_{\max } & =\frac{P_{T} V_{\text {face,ave }}}{P_{T}-D_{r}-2 n_{f} b \tau}=\frac{2.5 \times 592}{2.5-1.0-2 \times 10 \times 0.625 \times 0.013} \\
V_{\max } & =1106.5 \mathrm{ft} / \mathrm{min}=66,390 \mathrm{ft} / \mathrm{h} \\
R e & =\frac{D_{r} V_{\max } \rho}{\mu}=\frac{(1.0 / 12) \times 66,390 \times 0.0685}{0.0467}=8115
\end{aligned}
$$

Note: The air density should be corrected for the average atmospheric pressure at the elevation of the plant site (see Appendix 12.C). In the present case, the site elevation ( 250 ft ) is such that the pressure does not differ significantly from one atmosphere and, hence, no correction is needed.

Equation (12.6) is used to calculate the air-side heat-transfer coefficient with $A_{T o t} / A_{o}=21.4$ from Table 12.1:

$$
\begin{aligned}
N u & =0.38 \operatorname{Re}^{0.6} \operatorname{Pr}^{1 / 3}\left(A_{T o t} / A_{o}\right)^{-0.15}=0.38(8115)^{0.6}(0.7)^{1 / 3}(21.4)^{-0.15} \\
N u & =47.22 \\
h_{o} & =\left(k / D_{r}\right) N u=\frac{0.0161 \times 47.22}{(1.0 / 12)} \cong 9.12 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
\end{aligned}
$$

(m) Calculate fin efficiency.

Equations (2.27) and (5.12) are used to calculate the fin efficiency. From Table A.1, the thermal conductivity of aluminum is:

$$
k \cong 238 \times 0.57782=137.5 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}
$$

This value is slightly optimistic because the aluminum alloys used for fining have somewhat lower thermal conductivities than the pure metal. However, the difference is not large enough
to significantly affect the results.

$$
\begin{gathered}
r_{1}=\text { root tube radius }=0.5 \mathrm{in} . \\
r_{2}=r_{1}+\text { fin height }=0.5+0.625=1.125 \mathrm{in} . \\
r_{2 c}=r_{2}+\tau / 2=1.125+0.013 / 2=1.1315 \mathrm{in} . \\
\psi=\left(r_{2 c}-r_{1}\right)\left[1+0.35 \ln \left(r_{2 c} / r_{1}\right)\right] \\
=(1.1315-0.5)[1+0.35 \ln (1.1315 / 0.5)] \\
\psi=0.812 \mathrm{in} .=0.0677 \mathrm{ft} . \\
m=\left(2 h_{o} / k \tau\right)^{0.5}=\left(\frac{2 \times 9.12}{137.5 \times(0.013 / 12)}\right)^{0.5}=11.07 \mathrm{ft}^{-1} \\
m \psi=11.07 \times 0.0677=0.7494 \\
\eta_{f}=\frac{\tanh (m \psi)}{m \psi}=\frac{\tanh (0.7494)}{0.7494}=0.8471
\end{gathered}
$$

The extended and prime surface areas per inch of tube length are estimated as follows:

$$
\begin{aligned}
& A_{\text {fins }}=2 N_{f} \pi\left(r_{2 c}^{2}-r_{1}^{2}\right)=2 \times 10 \pi\left\{(1.1315)^{2}-(0.5)^{2}\right\}=64.735 \mathrm{in} . .^{2} \\
& A_{\text {prime }}=2 \pi r_{1}\left(L-N_{f} \tau\right)=2 \pi \times 0.5(1.0-10 \times 0.013)=2.733 \mathrm{in} .^{2} \\
& A_{\text {fins }} / A_{\text {Tot }}=\frac{64.735}{64.735+2.733} \cong 0.96 \\
& A_{\text {prime }} / A_{\text {Tot }}=1-0.96=0.04
\end{aligned}
$$

The weighted efficiency of the finned surface is given by Equation (2.31):

$$
\eta_{w}=\left(A_{\text {prime }} / A_{\text {Tot }}\right)+\eta_{f}\left(A_{\text {fins }} / A_{\text {Tot }}\right)=0.04+0.8471 \times 0.96 \cong 0.853
$$

(n) Wall temperatures and viscosity correction factors.

The wall temperatures, $T_{p}$ and $T_{w t d}$, used to obtain viscosity correction factors are given by Equations (4.38) and (4.39). However, no viscosity correction is required for the air-side heattransfer coefficient, so only $T_{p}$ is needed for the tube-side correction. In the present case, no viscosity data were given for the tube-side fluid. Therefore, $\phi_{i}$ is assumed to be 1.0 and the wall temperature is not calculated.
(o) Calculate the clean overall coefficient.

The clean overall coefficient is given by Equation (12.12) with the fouling factors omitted. The contact resistance is neglected and $A_{\text {Tot }} / A_{i}=26.3$ is obtained from Table 12.1.

$$
\begin{aligned}
U_{C} & =\left[\frac{\left(A_{\text {Tot }} / A_{i}\right)}{h_{i}}+\frac{\left(A_{\text {Tot }} / L\right) \ln \left(D_{r} / D_{i}\right)}{2 \pi k_{\text {tube }}}+\frac{1}{\eta_{w} h_{o}}\right]^{-1} \\
& =\left[\frac{26.3}{420}+\frac{5.58 \ln (1.0 / 0.81)}{2 \pi \times 26}+\frac{1}{0.853 \times 9.12}\right]^{-1} \\
U_{C} & =5.04 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}
\end{aligned}
$$

Since $U_{C}>U_{r e q}$, continue.
(p) Fouling allowance.

The tube-side fouling factor was specified in the problem statement as $0.001 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$. Except in unusual circumstances, air-side fouling is minimal and, therefore, $R_{D o}$ is taken as zero. Thus, the total fouling allowance is:

$$
R_{D}=R_{D i}\left(A_{T o t} / A_{i}\right)+R_{D o} / \eta_{w}=0.001 \times 26.3+0=0.0263 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}
$$

(q) Calculate the design overall coefficient.

$$
U_{D}=\left(1 / U_{C}+R_{D}\right)^{-1}=(1 / 5.04+0.0263)^{-1}=4.45 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

Since $U_{D}>U_{\text {req }}=4.10 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$, the heat exchanger is thermally workable.
(r) Over-surface and over-design.

$$
\begin{aligned}
\text { Over-surface } & =U_{C} / U_{\text {req }}-1=5.04 / 4.10-1 \cong 23 \% \\
\text { Over-design } & =U_{D} / U_{\text {req }}-1=4.45 / 4.10-1 \cong 8.5 \%
\end{aligned}
$$

Both values are reasonable and, hence, the unit is thermally acceptable.
(s) Tube-side pressure drop.

Equations (5.1)-(5.4) are used to calculate the tube-side pressure drop:

$$
\begin{aligned}
f & =0.4137 \mathrm{Re}^{-0.2585}=0.4137(69,594)^{-0.2585}=0.02317 \\
G & =\frac{\dot{m}\left(n_{p} / n_{t}\right)}{\left(\pi D_{i}^{2} / 4\right)}=\frac{250,000(4 / 224)}{\left[\pi(0.0675)^{2} / 4\right]}=1,247,540 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
s & =49.94 / 62.43=0.80 \\
\Delta P_{f} & =\frac{f n_{p} L G^{2}}{7.50 \times 10^{12} D_{i} s \phi}=\frac{0.02317 \times 4 \times 36(1,247,540)^{2}}{7.50 \times 10^{12} \times 0.0675 \times 0.80 \times 1.0}=12.82 \mathrm{psi} \\
\Delta P_{r} & =1.334 \times 10^{-13}\left(2 n_{p}-1.5\right) G^{2} / s=1.334 \times 10^{-13}(6.5)(1,247,540)^{2} / 0.80 \\
\Delta P_{r} & =1.69 \mathrm{psi}
\end{aligned}
$$

Assuming 5-in. schedule 40 nozzles are used, the flow area per nozzle from Table B. 1 is $0.1390 \mathrm{ft}^{2}$. Hence,

$$
\begin{aligned}
G_{n} & =250,000 / 0.1390=1,798,561 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
R e_{n} & =\frac{D_{i} G_{n}}{\mu}=\frac{(5.047 / 12) \times 1,798,561}{1.21}=625,161 \\
\Delta P_{n} & =2.0 \times 10^{-13} G_{n}^{2} / s=2.0 \times 10^{-13}(1,798,561)^{2} / 0.80=0.81 \mathrm{psi} \\
\Delta P_{i} & =\Delta P_{f}+\Delta P_{r}+\Delta P_{n}=12.82+1.69+0.81=15.3 \mathrm{psi}
\end{aligned}
$$

(t) Air-side pressure drop.

Equation (12.10) will be used to calculate the friction factor. The parameters $a$ and $R e_{\text {eff }}$ are computed first.

$$
\begin{aligned}
D_{f} & =D_{r}+2 b=1.0+2 \times 0.625=2.25 \mathrm{in} \\
a & =\left(P_{T}-D_{f}\right) / D_{r}=(2.5-2.25) / 1.0=0.25
\end{aligned}
$$

The fin spacing is obtained from Equation (12.2):

$$
\begin{aligned}
& l=1 / n_{f}-\tau=1 / 10-0.013=0.087 \mathrm{in} . \\
& \operatorname{Re} e_{e f f}=\operatorname{Re}(l / b)=8115(0.087 / 0.625)=1130 \\
f= & \left\{1+\frac{2 e^{-(a / 4)}}{1+a}\right\}\left\{0.021+\frac{27.2}{R e_{e f f}}+\frac{0.29}{R e_{e f f}^{0.2}}\right\} \\
= & \left\{1+\frac{2 e^{-(0.25 / 4)}}{1+0.25}\right\}\left\{0.021+\frac{27.2}{1130}+\frac{0.29}{(1130)^{0.2}}\right\} \\
f= & 0.291
\end{aligned}
$$

The pressure drop across the tube bundle is calculated using Equation (12.8a). The air mass flux is computed first:

$$
\begin{aligned}
G & =\rho V_{\max }=0.0685 \times 66,390=4548 \mathrm{lbm} / \mathrm{h} \cdot \mathrm{ft}^{2} \\
\Delta P_{f} & =\frac{9.22 \times 10^{-10} f N_{r} G^{2}}{\rho}=\frac{9.22 \times 10^{-10} \times 0.291 \times 4(4548)^{2}}{0.0685} \\
\Delta P_{f} & \cong 0.324 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}
\end{aligned}
$$

This unit will not require louvers, steam coils, fan guards, or hail guards. Enclosure losses will be small, and other losses will be due primarily to the fan casings, plenums, and obstructions such as fan supports and walkways. Therefore, a relatively small allowance of $10 \%$ is made for other air-side losses, giving:

$$
\Delta P_{o} \cong 1.1 \Delta P_{f}=1.1 \times 0.324 \cong 0.36 \text { in. } \mathrm{H}_{2} \mathrm{O}
$$

Both tube-side and air-side pressure drops are below the specified maximum values. Therefore, the unit is hydraulically acceptable.
(u) Fan sizing.

The fans should cover at least $40 \%$ of the bundle face area. Assuming a two-fan bay, this condition gives the following relation for the fan diameter:

$$
\begin{gathered}
2\left(\pi D_{\text {fan }}^{2} / 4\right) \geq 0.4 A_{\text {face }}=0.4 \times 426=170.4 \mathrm{ft}^{2} \\
D_{f a n} \geq 10.4 \mathrm{ft}
\end{gathered}
$$

Therefore, two fans with diameters of 10.5-11.0 ft are required.
The fan static pressure is given by Equation (12.15). For induced-draft operation without diffusers, the two velocity terms in this equation exactly cancel, and the fan static pressure is equal to the total air-side pressure loss. Thus, $F S P=0.36$ in. $\mathrm{H}_{2} \mathrm{O}$.

The induced-draft fans handle air at the outlet temperature of $150^{\circ} \mathrm{F}$, for which the density is $0.065 \mathrm{lbm} / \mathrm{ft}^{3}$ from Table A.5. Since there are two fans, the volumetric flow rate per fan is:

$$
\dot{v}_{\text {fan }}=\frac{0.5 \dot{m}_{\text {air }}}{\rho_{\text {air }}}=\frac{0.5(1,037,344 / 60)}{0.065}=132,993 \mathrm{acfm}
$$

Thus, each fan must deliver about 133,000 acfm at a static pressure of $0.36 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$.
(v) Motor sizing.

From Equation (12.14), the total pressure change across the fans is:

$$
\left(\Delta P_{\text {Total }}\right)_{f a n}=F S P+\frac{\alpha_{f r} \rho_{f r} V_{f r}^{2}}{2 g_{c}}
$$

For a fan diameter of 10.5 ft , the air velocity in the fan ring is (neglecting the clearance between the blades and the housing):

$$
V_{f r}=\frac{\dot{\imath}_{f a n}}{\pi D_{f r}^{2} / 4}=\frac{132,993}{\pi(10.5)^{2} / 4}=1536 \mathrm{ft} / \mathrm{min}=25.6 \mathrm{ft} / \mathrm{s}
$$

Thus, the velocity pressure is:

$$
\begin{aligned}
& \frac{\alpha_{f r} \rho_{f r} V_{f r}^{2}}{2 g_{c}} \cong \frac{1.0 \times 0.065(25.6)^{2}}{2 \times 32.174}=0.662 \mathrm{lbf} / \mathrm{ft}^{2} \\
& \frac{\alpha_{f r} \rho_{f r} V_{f r}^{2}}{2 g_{c}}=0.662 \mathrm{lbf} / \mathrm{ft}^{2} \times 0.1922 \frac{\mathrm{in} . \mathrm{H}_{2} \mathrm{O}}{\mathrm{lbf} / \mathrm{ft}^{2}}=0.127 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}
\end{aligned}
$$

The total pressure difference across the fan is:

$$
\left(\Delta P_{\text {Total }}\right)_{\text {fan }}=0.36+0.127 \cong 0.49 \text { in. } \mathrm{H}_{2} \mathrm{O}
$$

The brake power is calculated using Equation (12.16b); a fan efficiency of 70\% is assumed:

$$
\dot{W}_{\text {fan }}=\frac{\left(\Delta P_{\text {Total }}\right)_{\text {fan }} \dot{v}_{\text {fan }}}{6342 \eta_{\text {fan }}}=\frac{0.49 \times 132,993}{6.342 \times 0.7}=14.7 \mathrm{hp}
$$

The power supplied by the moor is given by Equation (12.17); an efficiency of $95 \%$ is assumed for the speed reducer:

$$
\dot{W}_{\text {motor }}=\frac{\dot{W}_{\text {fan }}}{\eta_{s r}}=\frac{14.7}{0.95}=15.5 \mathrm{hp}
$$

The next largest standard motor size is 20 hp (Appendix 12.B). This motor size will provide an adequate allowance for operational flexibility and contingencies. Therefore, each fan will be equipped with a 20 hp motor. This result is preliminary pending actual fan selection. Final values for fan efficiency and motor size will be based on the fan manufacturer's data. A fan that is well matched with the service may have a total efficiency as high as $80-85 \%$. In that case, 15 hp motors might be sufficient.

The main design parameters for the unit are summarized below.

## Design Summary

Number of fan bays: 1
Number of tube bundles per bay: 1
Number of fans per bay: 2
Bundle width and length: $11.8 \mathrm{ft} \times 37 \mathrm{ft}$ (including headers)
Number of tube rows: 4
Number of tube passes: 4
Number of tubes: 224

Tubing type: G-fin
Tube size: 1 in . OD, 13 BWG, 36 ft long
Tube layout: Equilateral triangular with 2.5-in. pitch
Fins: 10 fpi, 0.625 in. high, 0.013 in. thick
Heat-transfer surface area: $45,000 \mathrm{ft}^{2}$
Draft type: Induced draft
Fan diameter: 10.5 ft
Motor size: 20 hp
Tube-side nozzles: 5 -in. schedule 40
Headers: Plug-type box headers
Materials: Carbon steel tubes, aluminum fins, carbon steel headers, tubesheets, pass partitions, and nozzles

### 12.10 Computer Software

### 12.10.1 HEXTRAN

The air-cooled heat-exchanger module (ACE) in HEXTRAN is configured in a similar manner to the shell-and-tube exchanger module. It can operate in either rating mode (TYPE=Old) or design mode (TYPE=New). In design mode the following parameters can be varied automatically between user-specified limits to meet a given performance specification (usually tube-side outlet temperature or duty) and pressure drop constraints:

- Area per tube bundle
- Number of tube passes
- Number of tube rows
- Tube length
- Width of tube bundle
- Number of fan bays in parallel

HEXTRAN does not have a special thermodynamic package for air. Air is treated as a pure component, and methods must be selected for computing thermodynamic and transport properties. For the latter, the pure component data bank should be used by selecting the LIBRARY method. The choice of thermodynamic method is not critical. The SRKS method, which is a modified Soave-Redlich-Kwong cubic equation of state developed by SimSci-Esscor, is suggested here, but any equation-of-state method other than IDEAL can be used with similar results.
Two different tube pitches must be entered to specify the tube layout in HEXTRAN. The transverse pitch is the center-to-center distance between adjacent tubes in the same row. The longitudinal pitch is the center-to-center distance between adjacent tube rows. For an equilateral triangular layout, this is the height of an equilateral triangle with the length of a side equal to the transverse pitch, i.e.,

$$
\begin{equation*}
\text { longitudinal pitch }=0.5 \times(\text { transverse pitch }) \times \tan 60^{\circ} \tag{12.19}
\end{equation*}
$$

In general, however, both tube pitches can be independently specified.
Unlike the other two computer programs considered in the following subsections, HEXTRAN has no provision for entering data needed to calculate air-side pressure losses other than the pressure drop across the tube bundle. Also, the only orientation allowed for the tube bundle is horizontal. Therefore, an A-frame condenser cannot be simulated.
HEXTRAN version 9.1 is used in the following example.

## Example 12.2

Use HEXTRAN to rate the air-cooled heat exchanger designed by hand in Example 12.1.

## Solution

The English system of units is selected and for convenience, the unit of viscosity is changed from cp to $\mathrm{lb} / \mathrm{ft} \cdot \mathrm{h}$. Under Components and Thermodynamics, air is selected from the list of components and a New Method Slate called SET1 is defined on the Method form. The SRKS equation of state is specified as the thermodynamic method and LIBRARY is specified for transport properties.
The flowsheet is constructed in the usual manner. The hydrocarbon feed is defined as a bulk property stream and the flow rate, temperature, pressure, and physical properties are entered on the appropriate forms. The inlet air is defined (by default) as a compositional stream and the composition ( $100 \%$ air), flow rate, temperature, and pressure ( 14.7 psia) are entered on the appropriate form.
Data for the air-cooled heat exchanger are obtained from Example 12.1 and entered on the appropriate forms as follows: Items not listed are either left at the default settings or left unspecified, in which case they are calculated by the program.
(a) Tube side

Tube length: 36 ft
Transverse pitch: 2.5 in.
Longitudinal pitch: 2.165 in .
(b) Air side

Number of tubes/bundle: 224
Number of passes/bundle: 4
Number of rows/bundle: 4

## Pattern: Staggered

Outside diameter: 1 in. BWG: 13

Flow direction: Counter current
Hotside: Tube side
(c) Tube side nozzles

The inside diameter ( 5.047 in .) of inlet and outlet nozzles is entered on this form. The number (1) of each type of nozzle is the default setting.
(d) Fins

Number of fins/length: 10/in.
Height above root: 0.625 in .

Thickness: 0.013 in.
Area/length: 5.58

The area/length entry is optional and will be calculated by the program if not given.
(e) Material

The default materials of construction, carbon steel for the tubes and aluminum alloy $1060-\mathrm{H} 14$ for the fins, are used.
(f) Film options

The fouling factors, $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}$ for the tube side and zero for the air side, are entered here.
(g) Fans

Draft type: Induced
Number of fans/bay: 2
Efficiency: 57\%
Fan diameter: 10.5 ft
The efficiency entered here is the product of the fan static efficiency (estimated as $60 \%$ ) and the speed reducer efficiency ( $95 \%$ ). HEXTRAN uses this value to calculate the power supplied by the fan motors. Although it is not stated in the program documentation, the static efficiency should be used here because HEXTRAN does not include the velocity pressure in the calculation of fan power.
(h) Multi-bundle

Number of bundles in series/bay: 1
Number of bundles in parallel/bay: 1
Number of bays in parallel: 1
These are the default settings in the program.

Finally, under Global Options, the Water Decant Option switch is unchecked (OFF). Water decanting is not relevant to this problem, but if the switch is left in the default (ON) position, an error results because the SRKS method does not support this option.

The input file generated by the HEXTRAN GUI is given below followed by a summary of results in the form of the Exchanger Data Sheet and Extended Data Sheet. The data sheets were extracted from the HEXTRAN output file and used to prepare the following comparison between computer and hand calculations:

| Item | Hand | HEXTRAN |
| :--- | :--- | :--- |
| $R e_{i}$ | 69,594 | 69,596 |
| $R e_{o}$ | 8115 | 8080 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 420 | 420.1 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 9.12 | 7.2 |
| $U_{D}\left(\mathrm{Btu} \cdot \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 4.45 | 4.05 |
| $\Delta P_{i}(\mathrm{psi})$ | 15.3 | 15.7 |
| $\Delta P_{o}\left(\mathrm{n} . \mathrm{H}_{2} \mathrm{O}\right)$ | 0.36 | 0.40 |
| $\dot{W}_{\text {motor }}(\mathrm{hp})$ | $15.5^{\mathrm{a}}$ | $14.8^{\mathrm{b}}$ |
| Over-design $(\%)$ | 8.5 | 0 |

${ }^{\text {a }}$ Based on fan total efficiency of $70 \%$.
${ }^{\mathrm{b}}$ Based on fan static efficiency of $60 \%$.
Overall, the two sets of results are in reasonably good agreement, but there are significant differences in the air-side heat-transfer coefficient ( $26 \%$ ) and pressure drop ( $10 \%$ ). Notice that the outlet temperature of the hydrocarbon stream calculated by HEXTRAN is $150^{\circ} \mathrm{F}$. Thus, in agreement with the hand calculations, the heat exchanger is workable, but the over-design is essentially zero according to HEXTRAN.

## HEXTRAN Input File for Example 12.2

```
$ GENERATED FROM HEXTRAN KEYWORD EXPORTER
$
$ General Data Section
$
TITLE PROJECT=Ex12-2, PROBLEM=HC-Cooler, SITE=
$
DIME English, AREA=FT2, CONDUCTIVITY=BTUH, DENSITY=LB/FT3, *
    ENERGY=BTU, FILM=BTUH, LIQVOLUME=FT3, POWER=HP, *
    PRESSURE=PSIA, SURFACE=DYNE, TIME=HR, TEMPERATURE=F, *
    UVALUE=BTUH, VAPVOLUME=FT3, VISCOSITY=LBFH, WT=LB, *
    XDENSITY=API, STDVAPOR=379.490
$
PRINT ALL, *
    RATE=M
$
CALC PGEN=New, WATER=Saturated
$
$ Component Data Section
$
COMPONENT DATA
$
```


## HEXTRAN Input File for Example 12.2 (continued)

```
    LIBID 1, AIR
$
$
$ Thermodynamic Data Section
$
THERMODYNAMIC DATA
$
    METHODS SET=SET1, KVALUE=SRKS, ENTHALPY(L) =SRKS, ENTHALPY(V)=SRKS, *
                                    ENTROPY (L) =SRKS, ENTROPY(V)=SRKS, DENSITY(L)=API, *
                                    DENSITY(V)=SRKS, VISCOS (L) = LIBRARY, VISCOS (V)=LIBRARY, *
                                    CONDUCT (L) =LIBRARY, CONDUCT (V)=LIBRARY, SURFACE=LIBRARY
$
    WATER DECANT=OFF
$
$Stream Data Section
$
STREAM DATA
$
    PROP STRM=HC, NAME=HC, TEMP=250.00, PRES=50.000, *
        LIQUID (W) =250000.000, LCP (AVG)=0.55, Lcond (AVG) =0.082, *
    Lvis(AVG)=1.21, Lden(AVG) =49.94
$
    PROP STRM=HCOUT, NAME=HCOUT
$
    PROP STRM=AIR, NAME=AIR, TEMP=95.00, PRES=14.700, *
                            SET=SET1, RATE (W)=1037344.000, *
        COMP (M) = 1, 100, *
```

                        NORMALIZE
    $\$$
PROP STRM=AIROUT, NAME=AIROUT
\$
\$ Calculation Type Section
\$
SIMULATION
$\$$
TOLERANCE TTRIAL=0.01
\$
LIMITS AREA $=200.00,6000.00, \operatorname{SERIES}=1,10, \operatorname{PDAMP}=0.00$, *
TTRIAL=30
$\$$
CALC TWOPHASE=New, DPSMETHOD=Stream, MINFT=0.80
$\$$
PRINT UNITS, ECONOMICS, STREAM, STANDARD, *
EXTENDED, ZONES
\$
ECONOMICS DAYS=350, EXCHANGERATE=1.00, CURRENCY=USDOLLAR
\$

## HEXTRAN Input File for Example 12.2 (continued)

```
    UTCOST OIL=3.50, GAS=3.50, ELECTRICITY=0.10, *
        WATER=0.03, HPSTEAM=4.10, MPSTEAM=3.90, *
        LPSTEAM=3.60, REFRIGERANT=0.00, HEATINGMEDIUM=0.00
$
    HXCOST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
        EXPONENT=0.60, CONSTANT=0.00, UNIT
$
$ Unit Operations Data
$
UNIT OPERATIONS
$
ACE UID=ACE1
    TYPE Old, HOTSIDE=Tubeside, *
    FLOW=Countercurrent,
    UESTIMATE=5.00, USCALER=1.00
    TUBE FEED=HC, PRODUCT=HCOUT, *
    LENGTH=36.00, *
    OD=1.000, BWG=13, *
    NUMBER=224, PASS=4, ROWS=4, PATTERN=Staggered, *
    PARA=1, SERIES=1, *
    TPITCH=2.500, LPITCH=2.165, MATERIAL=1, *
    FOUL=0.001, LAYER=0, *
    DPSCALER=1.00
$
    FINS NUMBER=10.00, AREA=5.580, HEIGHT=0.625, *
        THICKNESS=0.013, BOND=0.000, *
        MATERIAL=20
$
    AIRS FEED=AIR, PRODUCT=AIROUT, *
        PARALLEL=1, *
        FOUL=0, LAYER=0, *
        DPSCALER=1.00
$
    FAN DRAFT=Induced, DIAM=10.50, NUMBER=2, EFFI=57.00
$
TNOZZ ID=5.047, 5.047 NUMBER=1, I
$
    CALC TWOPHASE=New, *
        MINFT=0.80
$
    PRINT STANDARD, *
    EXTENDED, *
    ZONES
$
    COST BSIZE=1000.00, BCOST=0.00, LINEAR=50.00, *
    CONSTANT=0.00, EXPONENT=0.60, Unit
$
$ End of keyword file...
```


## HEXTRAN Output Data for Example 12.2



## HEXTRAN Output Data for Example 12.2 (continued)



### 12.10.2 HTFS/Aspen

The HTFS/Aspen program called ACOL is used for design and rating of air-cooled heat exchangers. This program is similar in structure and format to the shell-and-tube exchanger program, TASC, except that ACOL does not have an option for mechanical design calculations. An incremental analysis is always performed along the length of the tube bundle, and proprietary correlations for heat transfer and pressure drop are used on both tube and air sides. The methods for handling tube-side fluid properties in ACOL are exactly the same as in TASC. The air-side properties are generated automatically by ACOL.

ACOL can operate in checking, simulation, and design modes. The checking mode is essentially the same as in TASC. However, there are nine simulation options available. The Standard Simulation option corresponds to the simulation mode in TASC and is the one most often used. In this mode the outlet temperatures and pressures of the two streams are computed from the given inlet temperatures, pressures, flow rates, and exchanger configuration. The other simulation options
allow different sets of specified and computed parameters. Other parameters that can be calculated by the program are:

- Air mass flow rate
- Tube-side mass flow rate
- Tube-side inlet temperature
- Tube-side fouling factor

There is also an option for natural convection that can be used to simulate an air-cooled exchanger with the fans turned off.

In design mode ACOL generates a graphical design envelope from which one or more feasible designs can be obtained using the mouse. The user must specify the type, size and material for tubing and fins, tube pitches, number of tube rows and passes, maximum tube-side pressure drop, and minimum and maximum tube-side velocities. The design envelope is a plot of overall exchanger width versus tube length, with the feasible design region bounded by lines of minimum and maximum tube-side velocity, maximum tube-side pressure drop, and heat duty. Clicking on a point in the feasible region (as indicated by the display below the graph) brings up a screen showing values of design parameters for the selected design. The design can then be run in simulation mode for verification by clicking the Simulate button at the bottom of the form.
ACOL accounts for air-side pressure losses from a number of factors in addition to the tube bundle: fan rings, plenums, steam coil, fan guards, fan supports, and louvers. The user must supply a pressure loss coefficient for the fan guards and for the fan supports. A typical value of 0.2 is given for the latter in the online help file. If louvers are present, the type of louver is chosen from a list box and either the louver angle or a loss coefficient must be given. The type of fan inlet is chosen from a list box; the default is a conical inlet. Of the inlet options given (other than "none"), the conical inlet gives the largest pressure loss, followed by shallow radius, deep radius, shallow ellipse, and deep ellipse (smallest loss).
ACOL can simulate both air coolers and condensers, and it is the only program of those considered in this work that has a specific option for an A-frame configuration. This configuration cannot be used in design mode, however. Therefore, to design an A-frame condenser the program is first run in design mode to obtain an initial configuration with a horizontal tube bundle, which is then converted to an A-frame configuration. The A-frame configuration is then verified using simulation mode, and the initial design is modified as necessary.

Similar to TASC Thermal, ACOL generates a cost estimate and approximate setting plan for the heat exchanger. The setting plan is useful for determining the overall dimensions of the unit and visualizing the layout, but it is not a substitute for mechanical design calculations, for which a separate computer program is required.

## Example 12.3

Use ACOL to rate the air-cooled heat exchanger designed in Example 12.1 and compare the results with those obtained previously by other methods.

## Solution

ACOL is run in checking mode for this problem and dry air is selected as the X -side option on the Startup form for consistency with the hand calculations and HEXTRAN. Data obtained from Example 12.1 are entered on the appropriate input forms as indicated below. Items not listed are either left at their default settings or left blank to be computed by the program.
(a) Bundle geometry
(i) Nozzles/Headers

The number (1) and inside diameter (5.047 in.) of the inlet and outlet nozzles are entered and plug is selected from the list of header types.
(ii) Bundle Setup

Number of Passes: 4
Number of Tubes: 224
Number of Rows: 4
Rows per Pass: 1
(iii) Tube Details

Tube ID: 0.81 in .
Tube OD: 1 in.
Longitudinal Pitch: 2.165 in.
Total Length: 432 in.
Transverse Pitch: 2.5 in.

Note: Either longitudinal pitch or tube layout angle can be given here.
(iv) Materials

Tube: Carbon Steel First Fin: Aluminum
Header: Carbon Steel
These are the default settings. The program uses aluminum alloy 3003 as the default fin material; the only other aluminum alloy available is alloy 6061.
(b) Extended Surfaces

First type of fin or stud: G-fin (default)
Fin or stud crown frequency: 10/in.
Mean fin or stud thickness: 0.013 in.
Fin or stud tip diameter: 2.25 in .
(c) ACHE Geometry
(i) Unit Configuration

Number of Bays per Unit: 1 Number of Bundles per Bay: 1
Number of Fans per Bay: 2 Fan Configuration: Induced Draught
(ii) Fan Details

Fan Support Loss Coefficient: 0.2
Fan Drive Eefficiency: 95\%
Approximate Fan Static Efficiency: 60\%
Exchanger Fan Diameter: 126 in.
Fan Inlet Type: Conical
The loss coefficient for fan supports is taken from the online help file. Since the type of fan inlet was not specified in Example 12.1, the default (conical) is chosen. A fan static efficiency of $60 \%$ is used, as in the previous example.
(d) Process Data
(i) Process Streams

|  | Tube-side stream | X-side stream |
| :--- | :---: | :---: |
| Total mass flow (lb/h) | 250,000 | $1,037,344$ |
| Inlet mass quality | 0 | - |
| Outlet mass quality | 0 | - |
| Inlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 250 | - |
| Outlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 150 | - |
| Inlet pressure (psia) | 50 | - |
| Estimated pressure drop (psi) | 20 | - |

(ii) Tube-side Fouling

Fouling Resistance: $0.001 \mathrm{~h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F} / \mathrm{Btu}$
(iii) Air Stream Conditions

Inlet Dry Bulb Design Temperature: $95^{\circ} \mathrm{F}$
Altitude: 250 ft

The program uses the altitude to determine the inlet air pressure and density. The default is a pressure of 1 atm .
(e) Options
(i) Main Output Options

Units of Output: British/US
(f) Physical properties

The bulk properties of the hydrocarbon stream are entered by selecting <Direct Input> for the Stream Data Source. A single level ( 50 psia ) is entered and values for the density ( $49.94 \mathrm{lb} / \mathrm{ft}^{3}$ ), liquid specific heat ( $0.55 \mathrm{Btu} / \mathrm{lb} \cdot{ }^{\circ} \mathrm{F}$ ), liquid viscosity ( 0.5 cp ), and liquid thermal conductivity ( $0.082 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ) are entered on the spreadsheet at a temperature of $200^{\circ} \mathrm{F}$. No entries are required for the air stream. Hence, this completes the data entry for this problem.

Running ACOL with the above input data generates the results summary shown below.

## ACOL Results Summary for Example 12.3

| Version 6.30 - CHECKING OPTION |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Geometric details |  |  |  |  |  |  |
| Fans/Bundles/Bays | 2 |  | 1 |  | 1 |  |
| Draught/Bare HT area/bundle/ Area ratio | Induced |  | 2111.1 | $\mathrm{ft}^{2}$ | 21.5 |  |
| Tube length/Tube OD/Tube ID | 432 | in | 1.000 | in | 0.810 | in |
| Rows/Tubes/Passes | 4 |  | 224 |  | 4 |  |
| Trans.pitch/Long.pitch/ Layout angle | 2.500 | in | 2.165 | in | 30 | deg |
| Fin frequency/ Tip diam./Mean thickness | 10 | /in | 2.250 | in | 0.013 | in |
| Process details | X-SIDE |  | TUBESIDE |  | WALL |  |
| Total mass flowrates | 1037358 | $\mathrm{lb} / \mathrm{h}$ | 250004 | $\mathrm{lb} / \mathrm{h}$ |  |  |
| Pressure (In/Out) | 14.56/14.55 | psia | 50.0/34.4 | psia |  |  |
| Temperature (In/Out) | 95.0/150.0 | ${ }^{\circ} \mathrm{F}$ | 250.0/150.0 | ${ }^{\circ} \mathrm{F}$ |  |  |
| Humidity/Quality (In/Out) | 0.000/0.000 |  | 0.00/0.00 |  |  |  |
| Results |  |  |  |  |  |  |
| Total pressure drop | 0.416 | in $\mathrm{H}_{2} \mathrm{O}$ | 15.618 | psi |  |  |
| Maximum Velocity | 19.9 | $\mathrm{ft} / \mathrm{s}$ | 6.9 | $\mathrm{ft} / \mathrm{s}$ |  |  |
| Coefficients | 162 | $\mathrm{Btu} / \mathrm{hft}{ }^{2} \mathrm{~F}$ | 400 | Btu/hft ${ }^{\text {o }} \mathrm{F}$ |  |  |
| Resistances(ref:tubeOD) : fouling/Wall | 0.0000000 | $\mathrm{hft}{ }^{2} \mathrm{~F} / \mathrm{Btu}$ | 0.0012346 | $\mathrm{hft}{ }^{2} \mathrm{~F} / \mathrm{Btu}$ | 0.0002948 | $\mathrm{hft}{ }^{2} \mathrm{~F} / \mathrm{Btu}$ |
| Performance |  |  |  |  |  |  |
| Overall coefficient: clean/dirty | 111 | Btu/ $\mathrm{ftt}^{2}{ }^{\circ} \mathrm{F}$ | 98 | Btu/hft ${ }^{\text {o }} \mathrm{F}$ |  |  |
| Heat duty/eff wtd mtd/ Heat balance | 13745 | $10^{3} \mathrm{Btu} / \mathrm{h}$ | 74.7 | ${ }^{\circ} \mathrm{F}$ | 0.0 | \% |
| Area ratio, PD ratio, Max.power/fan | 1.12 | (act/req) | 0.78 | (calc/allow) | 15.4 | hp |

The manner in which the heat-transfer coefficients are presented in this file requires some explanation. All coefficients are referenced to the external bare (unfinned) tube surface. Thus, the
value of $400 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ listed for the tube-side coefficient is actually $h_{i} D_{i} / D_{o}$. The value of $h_{i}$ is therefore:

$$
h_{i}=400\left(D_{o} / D_{i}\right)=400(1.0 / 0.81) \cong 494 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

The value of $98 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ listed for the dirty overall coefficient represents $U_{D}\left(A_{T o t} / A_{o}\right)$, where $U_{D}$ is the overall coefficient based on the total external surface area. Hence, this value must be divided by the area ratio to obtain $U_{D}$. The area ratio calculated by ACOL is given as 21.5 in the second line of the results summary. Therefore:

$$
U_{D}=98 /\left(A_{T o t} / A_{o}\right)=98 / 21.5=4.56 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

The listed value of $162 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ for the air-side film coefficient is referenced to the bare tube surface, i.e.,

$$
162=\eta_{w} h_{o}\left(A_{T o t} / A_{o}\right)
$$

The weighted efficiency of the finned surface computed by ACOL is given in the full output file as 0.818 . Therefore:

$$
h_{o}=\frac{162}{\eta_{w}\left(A_{T o t} / A_{o}\right)}=\frac{162}{0.818 \times 21.5}=9.21 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}
$$

Data from the results summary and the full output file were used to prepare the results comparison shown in the following table.

| Item | Hand | HEXTRAN | ACOL |
| :--- | :--- | :--- | :--- |
| $R e_{i}$ | 69,594 | 69,596 | 69,622 |
| $R e_{o}$ | 8115 | 8080 | 8155 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 420 | 420 | 494 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 9.12 | 7.2 | 9.21 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 4.45 | 4.05 | 4.56 |
| $\Delta P_{i}(\mathrm{psi})$ | 15.3 | 15.7 | 15.6 |
| $\Delta P_{o}\left(\mathrm{in} . \mathrm{H}_{2} \mathrm{O}\right)$ | 0.36 | 0.40 | 0.42 |
| $\dot{W}_{\text {motor }}(\mathrm{hp})$ | $15.5^{\mathrm{a}}$ | $14.8^{\mathrm{b}}$ | $15.4^{\mathrm{b}}$ |
| Over-design (\%) | 8.5 | 0 | 12 |

${ }^{\text {a }}$ Based on fan total efficiency of $70 \%$.
${ }^{\mathrm{b}}$ Based on fan static efficiency of 60\%.

Both the tube-side and air-side heat-transfer coefficients predicted by ACOL are significantly higher than those computed by HEXTRAN, whereas the pressure drops predicted by the two programs are in close agreement. Overall, the ACOL results agree better with the hand calculations than with the results from HEXTRAN.

It will be noticed that the stream flow rates in the ACOL results summary are slightly in error. The heat duty also differs from the correct value by a small amount. These discrepancies are probably due to unit conversions carried out within the program. Internally, the program most likely uses SI units.
The (approximate) setting plan generated by ACOL is shown below. The structures beneath the tube bundle are walkways. Additional walkways that are used to service the headers are shown at the two ends of the unit.

## ACOL Setting Plan (Dimensions in inches)

Side view


Plan view


### 12.10.3 HTRI

The Xace module of Xchanger Suite is used for design and rating of air-cooled heat exchangers. The program is similar in structure and format to the Xist module discussed in previous chapters. As in Xist, the computational method in Xace is fully incremental, and the same proprietary correlations for tube-side heat transfer and pressure drop are used in both programs. Proprietary correlations
are also used for air-side calculations. The methods for handling tube-side fluid properties are identical in the two programs; the properties of air are generated automatically by Xace.

Xace can operate in rating, simulation, or design mode. The rating and simulation modes are the same as in Xist. Two options are available for design mode, namely, classic design and grid design. In classic design, the only parameters that can be varied are bundle width, air face velocity and number of tube passes, and the parameter ranges are controlled by the program. In grid design, transverse and longitudinal tube pitch, tube length, tube diameter, and number of tube rows can also be varied. Furthermore, the parameter ranges are user-specified.

Xace accounts for air-side pressure losses from a number of factors in addition to the tube bundle, namely, fan rings, plenums, steam coil, louvers, fan guard, hail screen, and fan area blockage. The user must supply values for the percent open area in the fan guard and hail screen, and the percentage of the fan area that is blocked by obstructions if these items are to be included in the pressure drop calculation. The type of plenum (box or tapered) and fan ring inlet (straight, flanged, $15^{\circ}$ cone, $30^{\circ}$ cone, bell) must always be specified.
Fin geometry can be specified by the user on the appropriate input form. However, Xace has a built-in databank of finned tubing that is available from selected manufacturers, and the user has the option of selecting the fin geometry from this databank.

Like Xist, Xace generates a tube layout that can be modified by the user. Also, for tube-side condensing, the inclination of the tube bundle can be specified in the range of $1-89^{\circ}$. A unique feature in Xace is an interface with software from several fan manufacturers. If the user selects one of the available manufacturers, a list of fan models that will meet the requirements of the unit is printed in the output file. The list includes pertinent information such as fan size, efficiency, speed, and power.

## Example 12.4

Use Xace to rate the air-cooled heat exchanger designed by hand in Example 12.1 and compare the results with those obtained previously by other methods.

## Solution

Xace is run in rating mode (the default option) for this problem. Data obtained from Example 12.1 are entered on the appropriate input forms as indicated below. Items not listed are either left at their default values or left blank to be computed by the program.
(a) Geometry/Unit

Fan arrangement: Induced
Number of bays in parallel per unit: 1 (default)
Number of bundles in parallel per bay: 1 (default)
Number of tube passes per bundle: 4
The number (1) and ID ( 5.047 in .) of the tube-side inlet and outlet nozzles are also given on this form.
(b) Geometry/Fans

Number of fans per bay: 2 (default)
Fan diameter: 10.5 ft
Total combined fan and drive efficiency: 66.5\%
Fan ring type: $15^{\circ}$ cone
Although it is not stated in the Xace documentation, the total fan efficiency (estimated here as $70 \%$ ) is used in this program. The type of fan ring entrance was not specified in Example 12.1. A $15^{\circ}$ conical inlet is chosen for consistency with the previous example and because it gives a pressure loss in the mid-range of the values for the available options. The straight entrance has by far the greatest loss, while the bell-shaped entrance has the least.
(c) Geometry/Optional

The only entry made on this form is the selection of a tapered plenum, which is standard for an induced-draft fan.
(d) Geometry/Bundle

Number of tube rows/tube passes: $4 / 4$
Number of tubes in each odd/even numbered row: 56/56
Tube layout: Staggered (default)
Tube form: Straight (default)
Side seals: Yes (default)
Tube length: 36 ft
(e) Geometry/Tube Type/Tubes

Tube type: High-finned
Tube material: Carbon steel (Default)
Wall thickness: 0.095 in.
Transverse pitch: 2.5 in.
Tube OD: 1 in.
(f) Geometry/Tube Type/High Fins

Fin type: Circular fin
Fin density: 10 fin/in.
Fin height: 0.625 in .

Longitudinal pitch: 2.165 in .

Fin base thickness: 0.013 in.
Fin tip thickness: 0.013 in.
Material: Aluminum 1060-H14

Aluminum alloy $1060-\mathrm{H} 14$ is the default fin material. The fins are actually tapered from base to tip, but they are represented here as straight (untapered) fins having the average thickness of 0.013 in ., which is the only dimension that is known.
(g) Process

|  | Tube-side fluid | Air |
| :--- | :--- | :--- |
| Phase/air-side flow-rate units | Sensible liquid | Mass flow rate |
| Flow rate $(1000 \mathrm{lb} / \mathrm{h})$ | 250 | 1037.344 |
| Inlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 250 | 95 |
| Outlet temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 150 | - |
| Inlet pressure/altitude of unit | 50 psia | 250 ft |
| Fouling resistance $\left(\mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F} / \mathrm{Btu}\right)$ | 0.001 | 0 |

If the altitude of the unit above mean sea level is given here, the program accounts for the variation of atmospheric pressure with altitude in determining the air density.
(h) Hot Fluid Properties

Bulk properties of the hydrocarbon stream are entered using the component-by-component option. On the Components form, <USER DEFINED $>$ is selected and on the Liquid Properties form the density ( $49.94 \mathrm{lbm} / \mathrm{ft}^{3}$ ), viscosity ( 0.5 cp ), thermal conductivity ( $0.082 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}$ ), and heat capacity ( $0.55 \mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}$ ) are entered at a single temperature of $200^{\circ} \mathrm{F}$.

This completes the data entry. No input data are required for the properties of air, which are automatically generated by the program.

The Output Summary for this case is given below along with the tube layout produced by Xace. The output data were used to construct the results comparison shown in the following table. Note that the air-side heat-transfer coefficient of $7.26 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} .{ }^{\circ} \mathrm{F}$ given in the output file is the effective outside coefficient, i.e., $\eta_{w} h_{o}$. The weighted efficiency is not available in the Xace output files, but the fin efficiency computed by the program is given as $81.1 \%$ in the output summary. Using the percentages of fin (96\%) and prime (4\%) surface area calculated in Example 12.1 gives $\eta_{w}=0.8186$,
from which $h_{o}=8.87 \mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ :

| Item | Hand | HEXTRAN | ACOL | Xace |
| :--- | :--- | :--- | :--- | :--- |
| $R e_{i}$ | 69,594 | 69,596 | 69,622 | 69,594 |
| $R e_{o}$ | 8115 | 8080 | 8155 | 8404 |
| $h_{i}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 420 | 420 | 494 | 490 |
| $h_{o}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 9.12 | 7.2 | 9.21 | 8.87 |
| $U_{D}\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}\right)$ | 4.45 | 4.05 | 4.56 | 4.46 |
| $\Delta P_{i}(\mathrm{psi})$ | 15.3 | 15.7 | 15.6 | 15.6 |
| $\Delta P_{o}\left(\mathrm{in} . \mathrm{H}_{2} \mathrm{O}\right)$ | 0.36 | 0.40 | 0.42 | 0.32 |
| $\dot{W}_{\text {motor }}(\mathrm{hp})$ | $15.5^{\mathrm{a}}$ | $14.8^{\mathrm{b}}$ | $15.4^{\mathrm{b}}$ | $14.2^{\mathrm{a}}$ |
| Over-design $(\%)$ | 8.5 | 0 | 12 | 7.9 |

${ }^{\text {a }}$ Based on fan total efficiency of $70 \%$.
${ }^{\mathrm{b}}$ Based on fan static efficiency of 60\%.
With the exception of air-side pressure drop, the results from Xace and ACOL are in good agreement. The difference in air-side heat-transfer coefficients calculated by the two programs is less than $5 \%$. Both tube-side and air-side heat-transfer coefficients from HEXTRAN are significantly more conservative than those from the other two programs. The tube-side results are consistent with those from examples in previous chapters.

The near equality between the overall heat-transfer coefficients from Xace and the hand calculations must be considered fortuitous in light of the differences in film coefficients found by the two methods. Despite the close agreement in $U_{D}$ values, Xace gives a smaller over-design than that found by hand. The reason is that Xace uses the effective tube length, which in this case is 7 in . less than the total tube length, to calculate the heat-transfer surface area and $U_{r e q}$. The 7-in. difference is comprised of the total tubesheet thickness ( 1 inch for each tubesheet) and the width of five tube supports (each 1 in . wide). The tubesheet thickness and the number and width of tube supports are all calculated by Xace.

The air-side pressure drop computed by Xace is significantly lower than the values obtained from the other two programs. The difference is somewhat exaggerated because no allowance for fan area blockage was included in the Xace calculation for this example.

## Xace Output Summary for Example 12.4



## Xace Output Summary for Example 12.4 (continued)



## Xace Tube Layout for Example 12.4



## References

1. Kraus, A. D., A. Aziz and J. Welty, Extended Surface Heat Transfer, Wiley, New York, 2001.
2. Hewitt, G. F., G. L. Shires and T. R. Bott, Process Heat Transfer, CRC Press, Boca Raton, FL, 1994.
3. Minton, P. E., Heat exchanger design, in Heat Transfer Design Methods, J. J. McKetta, ed., Marcel Dekker, New York, 1991.
4. Bell, K. J. and A. C. Mueller, Wolverine Engineering Data Book II, Wolverine Tube, Inc., www.wlv.com, 2001.
5. Anonymous, Engineering Data Book, 11th edn., Gas Processors Suppliers Association, Tulsa, OK, 1998.
6. Mukherjee, R., Effectively design air-cooled heat exchangers, Chem. Eng. Prog., 93, No. 2, 26-47, 1987.
7. Shipes, K. V., Air-cooled exchangers in cold climates, Chem. Eng. Prog., 70, No. 7, 53-58, 1974.
8. Briggs, D. E. and E. H. Young, Convection heat transfer and pressure drop of air flowing across triangular pitch banks of finned tubes, Chem. Eng. Prog. Symp. Ser., 59, No. 41, 1-10, 1963.
9. Ganguli, A., S. S. Tung and J. Taborek, Parametric study of air-cooled heat exchanger finned tube geometry, AIChE Symp. Ser., 81, No. 245, 122-128, 1985.
10. Kröger, D. G., Air-Cooled Heat Exchangers and Cooling Towers, distributed by Begell House, Inc., New York, 1998.
11. Robinson, K. K. and D. E. Briggs, Pressure drop of air flowing across triangular pitch banks of finned tubes, Chem. Eng. Prog. Symp. Ser., 62, No. 64, 177-184, 1965.
12. Taborek, J., Mean temperature difference, in Heat Exchanger Design Handbook, Vol. 1, Hemisphere Publishing Corp., New York, 1988.
13. Roetzel, W. and J. Neubert, Calculation of mean temperature difference in air-cooled cross-flow heat exchangers, J. Heat Transfer, 101, 511-513, 1979.

## Appendix 12.A LMTD Correction Factors for Air-Cooled Heat Exchangers

The following notation is used for the charts:

$$
\begin{aligned}
A & =\text { heat-transfer surface area in exchanger } \\
C_{1} & =\left(\dot{m} C_{P}\right)_{1}=\text { heat capacity flow rate of tube-side fluid } \\
C_{2} & =\left(\dot{m} C_{P}\right)_{2}=\text { heat capacity flow rate of cross-flow stream (air) } \\
\Delta T_{m} & =F\left(\Delta T_{\text {ln }}\right)_{c f}=\text { mean temperature difference in exchanger } \\
U & =\text { overall heat-transfer coefficient }
\end{aligned}
$$

All other symbols are explicitly defined on the charts themselves.

When the outlet temperatures of both streams are known, the lower charts can be used to obtain the LMTD correction factor in the usual manner. When the outlet temperatures are unknown but the product $U A$ is known, the upper charts can be used to obtain $\theta$, from which the mean temperature difference, $\Delta T_{m}$, can be found. The exchanger duty is then obtained as $q=U A \Delta T_{m}$, and the outlet temperatures are computed using the energy balances on the two streams.

The equations from which the charts were constructed are given by Taborek [12]. Unfortunately, some of the equations contain errors; therefore, the original sources listed in Ref. [12] should be consulted if the equations are to be used. An alternative computational method is given in Ref. [13] and is reproduced in Ref. [10]. Although approximate, this method is well suited for computer calculations. Neither the exact nor the approximate method is convenient for hand calculations. Therefore, only the charts are presented here.


Figure 12.A.1 Mean temperature difference relationships for cross flow: three tube rows and one tube pass (Source: Ref. [12]).


$$
\mathrm{P}=\frac{\left(T_{2}\right)_{o}-\left(T_{2}\right)_{i}}{\left(T_{1}\right)_{i}-\left(T_{2}\right)_{i}}
$$

Figure 12.A. 2 Mean temperature difference relationships for cross flow: four tube rows and one tube pass (Source: Ref. [12]).


Figure 12.A.3 Mean temperature difference relationships for cross flow: three tube rows and three tube passes (Source: Ref. [12]).


Figure 12.A.4 Mean temperature difference relationships for cross flow: four tube rows and four tube passes (Source: Ref. [12]).

$$
R=\frac{C_{2}}{C_{1}}=\frac{\left(T_{1}\right)_{i}-\left(T_{1}\right)_{o}}{\left(T_{2}\right)_{o}-\left(T_{2}\right)_{i}}
$$

$T_{1}$ and $T_{2}$ are not interchangeable



$$
\mathrm{P}=\frac{\left(T_{2}\right)_{o}-\left(T_{2}\right)_{i}}{\left(T_{1}\right)_{i}-\left(T_{2}\right)_{i}}
$$

Figure 12.A. 5 Mean temperature difference relations for cross flow: four tube rows, two tube passes, two rows per pass, tube-side fluid mixed at return header (Source: Ref. [12]).

## Appendix 12.B Standard US Motor Sizes

| Motor size (hp) | Motor size (hp) |
| :--- | :--- |
| 0.5 | 30 |
| 0.75 | 40 |
| 1.0 | 50 |
| 1.5 | 60 |
| 2 | 75 |
| 3 | 100 |
| 5 | 150 |
| 7.5 | 200 |
| 10 | 250 |
| 15 | 300 |
| 20 | 400 |
| 25 | 500 |

## Appendix 12.C Correction of Air Density for Elevation

The variation of pressure with altitude in the atmosphere depends on the lapse rate, which is the rate of decrease of temperature with altitude. For an isothermal atmosphere (zero lapse rate), the pressure (and, hence, the density) decreases exponentially with altitude according to the following equation:

$$
\begin{equation*}
\frac{\rho}{\rho_{o}}=\frac{P}{P_{o}}=\exp \left[\frac{-M\left(g / g_{c}\right) z}{\widetilde{R} T}\right] \tag{12.C.1}
\end{equation*}
$$

where
$M=$ molecular weight of air $\cong 29.0$
$\tilde{R}=$ gas constant $=1545 \frac{\mathrm{ft} \cdot \mathrm{lbf}}{\mathrm{lbmol} \cdot{ }^{\circ} \mathrm{R}}=8314 \frac{\mathrm{~J}}{\mathrm{~kg} \mathrm{~mol} \cdot \mathrm{~K}}$
$T=$ absolute temperature, ${ }^{\circ} \mathrm{R}(\mathrm{K})$
$z=$ elevation above mean sea level, ft (m)
$P_{o}, \rho_{o}=$ pressure and density of air at temperature $T$ and mean sea level
$P, \rho=$ pressure and density of air at temperature $T$ and elevation $z$
Assuming $P_{o}$ is essentially one atmosphere, Equation (12.C.1) gives the air density at any elevation in terms of the density, $\rho_{o}$, at one atmosphere.

## Example 12.C. 1

Estimate the density of dry air at $100^{\circ} \mathrm{F}$ and an elevation of 3500 ft .

## Solution

Equation (12.C.1) is used with $T=100^{\circ} \mathrm{F} \cong 560^{\circ} \mathrm{R}$ and $z=3500 \mathrm{ft}$

$$
\frac{\rho}{\rho_{o}}=\exp \left[\frac{-M\left(g / g_{c}\right) z}{\widetilde{R} T}\right]=\exp \left[\frac{-29(1.0) \times 3500}{1545 \times 560}\right]=0.8893
$$

From Table A.5, the density of air at $100^{\circ} \mathrm{F}$ and 1 atm is $\rho_{o}=0.0709 \mathrm{lbm} / \mathrm{ft}^{3}$. Hence,

$$
\rho=0.0709 \times 0.8893 \cong 0.0631 \mathrm{lbm} / \mathrm{ft}^{3}
$$

## Notations

A Heat-transfer surface area
$A_{\text {con }} \quad$ Contact area between fin and tube wall
$A_{\text {face }} \quad$ Tube bundle face area
$A_{\text {fins }} \quad$ Surface area of fins
$A_{i} \quad \pi D_{i} L=$ Internal surface area of tube
$A_{\min } \quad$ Minimum flow area in tube bank
$A_{o} \quad \pi D_{r} L=$ External surface area of root tube
$A_{\text {prime }} \quad$ Prime surface area
$A_{\text {Tot }} \quad$ Total external surface area of finned tube
$a \quad\left(P_{T}-D_{f}\right) / D_{r}=$ Parameter in Equation (12.10)
$B W G$ Birmingham wire gage
$b \quad$ Fin height
$C_{1}, C_{2}$ Heat capacity flow rate of fluid 1 and fluid 2
$C_{P} \quad$ Heat capacity at constant pressure
$D_{f} \quad$ Outer fin diameter
$D_{f a n} \quad$ Fan diameter
$D_{i} \quad$ Internal diameter of tube
$D_{i, s l} \quad$ Internal diameter of sleeve on bimetallic tube
$D_{0} \quad$ External diameter of inner tube in bimetallic tube
$D_{o, s l} \quad$ External diameter of sleeve on bimetallic tube
$D_{r} \quad$ External diameter of root tube
$F \quad$ LMTD correction factor
$F S P$ Fan static pressure
$f \quad$ Friction factor
$G \quad$ Mass flux
$G_{n} \quad$ Mass flux in nozzle
$g \quad$ Gravitational acceleration
$g_{c} \quad$ Unit conversion factor
$h_{i} \quad$ Tube-side heat-transfer coefficient
$h_{o} \quad$ Air-side heat-transfer coefficient
$k \quad$ Thermal conductivity
$k_{s l} \quad$ Thermal conductivity of sleeve on bimetallic tube
$k_{\text {tube }} \quad$ Thermal conductivity of tube wall
$L$ Tube length
$l \quad$ Fin spacing
$M \quad$ Molecular weight of air
$m \quad\left(2 h_{o} / k \tau\right)^{0.5}=$ Fin parameter
$\dot{m} \quad$ Mass flow rate
$\dot{m}_{\text {air }} \quad$ Mass flow rate of air
$\dot{m}_{i} \quad$ Mass flow rate of tube-side fluid
$N_{f} \quad$ Number of fins
$N_{r} \quad$ Number of tube rows
$N u \quad$ Nusselt number
$n_{f} \quad$ Number of fins per unit length
$n_{p} \quad$ Number of tube passes
$n_{t} \quad$ Number of tubes
$P \quad$ Pressure; parameter used to calculated LMTD correction factor
$P_{o} \quad$ Atmospheric pressure at mean sea level
Pr Prandtl number
$P_{T} \quad$ Tube pitch
$P_{\text {Total }} \quad$ Sum of static and velocity pressures
$q \quad$ Rate of heat transfer
$R \quad$ Parameter used to calculate LMTD correction factor

| $\widetilde{R}$ | Universal gas constant |
| :--- | :--- |
| $R_{\text {con }}$ | Contact resistance |
| $R_{D}$ | Total fouling allowance |
| $R_{D i}$ | Tube-side fouling factor |
| $R_{D o}$ | Air-side fouling factor |
| $R e$ | Reynolds number |
| $R e_{e f f}$ | $R e(1 / \mathrm{b})=$ Effective Reynolds number used in Equation (12.10) |
| $R e_{n}$ | Nozzle Reynolds number |
| $r_{1}$ | Inner radius of fin |
| $r_{2}$ | Outer radius of fin |
| $r_{2 c}$ | $r_{2}+\tau / 2=$ Corrected fin radius |
| $s$ | Specific gravity |
| $T$ | Temperature |
| $U$ | Overall heat-transfer coefficient |
| $U_{C}$ | Clean overall heat-transfer coefficient |
| $U_{D}$ | Design overall heat-transfer coefficient |
| $U_{\text {req }}$ | Required overall heat-transfer coefficient |
| $V$ | Fluid velocity |
| $V_{e x}$ | Velocity of exhaust air leaving heat exchanger |
| $V_{\text {face }}$ | Air face velocity |
| $V_{\text {face }}$ ave | Air face velocity based on average air temperature |
| $V_{\text {face, std }}$ | Air face velocity based on standard conditions $\left(70^{\circ} \mathrm{F}, 1 \mathrm{~atm}\right)$ |
| $V_{f r}$ | Velocity of air leaving fan ring |
| $V_{\text {max }}$ | Maximum velocity of air in tube bundle |
| $W$ | Width of tube bundle |
| $\dot{W}_{\text {fan }}$ | Fan brake power |
| $\dot{W}_{\text {motor }}$ | Power delivered by motor |
| $\dot{W}_{u s e d}$ | Power used by motor |

## Greek Letters

| $\alpha$ | Kinetic energy correction factor |
| :--- | :--- |
| $\alpha_{f r}$ | Kinetic energy correction factor for air leaving fan ring |
| $\alpha_{e x}$ | Kinetic energy correction factor for exhaust air leaving heat exchanger |
| $\Delta P_{f}$ | Pressure drop due to fluid friction in straight sections of tubes or in flow |
| $\Delta P_{i}$ | across tube bundle |
| $\Delta P_{n}$ | Total pressure drop for tube-side fluid |
| $\Delta P_{o}$ | Pressure loss in tube-side nozzles |
| $\Delta P_{r}$ | Total air-side pressure loss |
| $\left(\Delta P_{\text {Total }}\right)_{\text {fan }}$ | Tube-side pressure drop due to tube entrance, exit, and return losses |
| $\Delta T$ | Temperature difference between fan entrance and exit |
| $\Delta T_{m}$ | Mean temperature difference in heat exchanger |
| $\left(\Delta T_{\text {ln }}\right)_{c f}$ | Logarithmic mean temperature difference for counter-current flow |
| $\eta_{f}$ | Fin efficiency |
| $\eta_{f a n}$ | Total fan efficiency |
| $\eta_{m o t o r}$ | Motor efficiency |
| $\eta_{s r}$ | Efficiency of speed reducer |
| $\eta_{w}$ | Weighted efficiency of finned surface |
| $\mu$ | Viscosity |
| $\mu_{w}$ | Fluid viscosity evaluated at average temperature of tube wall |
| $\rho$ | Fluid density |
| $\rho_{a i r}$ | Density of air |


| $\rho_{a v e}$ | Density of air at average air temperature |
| :--- | :--- |
| $\rho_{e x}$ | Density of exhaust air leaving heat exchanger |
| $\rho_{f r}$ | Density of air leaving fan ring |
| $\rho_{o}$ | Density of ambient air at mean sea level |
| $\rho_{s t d}$ | Density of air at standard conditions $\left(70^{\circ} \mathrm{F}, 1 \mathrm{~atm}\right)$ |
| $\tau$ | Fin thickness |
| $\phi$ | Viscosity correction factor |
| $\psi$ | Parameter in equation for efficiency of annular fins |

## Problems

(12.1) For Example 12.1:
(a) Repeat step (k) using Equation (2.38) to calculate the tube-side heat-transfer coefficient.
(b) Repeat step (l) using Equation (12.1) to calculate the air-side heat-transfer coefficient.
(c) Repeat step ( t ) using Equation (12.9) to calculate the air-side friction factor.

Compare the results of the above calculations with those obtained in Examples 12.1 through 12.4.
(12.2) Design an air-cooled heat exchanger for the service of Problem 5.6. Use the properties of dry air at one atmosphere pressure and assume an ambient air temperature of $100^{\circ} \mathrm{F}$ for design purposes. The air-side pressure loss should not exceed $0.5 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$. The unit will be mounted at grade and there are no space limitations at the plant site.
(12.3) Design an air-cooled heat exchanger for the service of Problem 5.11. Use the properties of dry air at one atmosphere pressure and assume an ambient air temperature of $95^{\circ} \mathrm{F}$ for design purposes. The air-side pressure loss should not exceed $0.5 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$. Assume that the unit will be mounted at grade and that there are no space limitations at the site.
(12.4) Rate the heat exchanger designed in Problem 12.3 using:
(a) HEXTRAN.
(b) ACOL.
(c) Xace.
(12.5) Design an air-cooled heat exchanger for the service of Problem 5.23. The unit will be situated on the US Gulf Coast (a relatively corrosive environment). Design ambient air temperature is $95^{\circ} \mathrm{F}$ and the maximum air-side pressure loss is $0.5 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$. Assume that the unit will be mounted at grade and that there are no space limitations at the site. Properties of the hydrocarbon stream are given in Problem 7.20.
(12.6) Rate the heat exchanger designed in Problem 12.5 using:
(a) HEXTRAN.
(b) ACOL.
(c) Xace.
(12.7) A stream consisting of $275,000 \mathrm{lb} / \mathrm{h}$ of a hydrocarbon liquid at $200^{\circ} \mathrm{F}$ is to be cooled to $130^{\circ} \mathrm{F}$ in an air-cooled heat exchanger. Four induced-draft fan bays are available on the used equipment lot. Each bay contains a single tube bundle having four rows of tubes with 45 tubes per row arranged for two passes. The root tubes are 1-in. OD, 14 BWG
and are made of carbon steel. The tubes contain nine aluminum fins per inch with a height of 0.5 in . and an average thickness of 0.012 in . The tubes are laid out on $2.25-\mathrm{in}$. equilateral triangular pitch. Two of the bays each contain 24 ft long tubes and two 7.5 ft diameter fans equipped with 10 hp motors. The other two bays each contain 16 ft long tubes and two 6 ft diameter fans equipped with 7.5 hp motors. Design specifications include maximum pressure drops of 10 psi on the tube side and $0.5 \mathrm{in} \cdot \mathrm{H}_{2} \mathrm{O}$ on the air side.

Average properties of the hydrocarbon are as follows:

| Hydrocarbon property | Value at $165{ }^{\circ} \mathrm{F}$ |
| :--- | :--- |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.53 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.080 |
| $\mu(\mathrm{cp})$ | 0.91 |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 48.5 |

Use HEXTRAN or other suitable software to determine if the existing heat exchangers are suitable for this service and if so, how they should be arranged. For the calculations, use dry air at one atmosphere pressure and an ambient air temperature of $95^{\circ} \mathrm{F}$.
(a) For the service of Example 12.1, run each of the following computer programs in design mode.
(i) HEXTRAN
(ii) ACOL
(iii) Xace
(b) Based on the results obtained in part (a), develop a final design for the heat exchanger using each of the computer programs and compare the results with the design obtained by hand in Example 12.1.
(12.9) Use any available software to solve Problem 12.2.
(12.10) Use any available software to solve Problem 12.3.
(12.11) Use any available software to solve Problem 12.5.
(12.12) Design an air-cooled condenser for the service of Problem 11.26 using:
(a) ACOL.
(b) Xace.

The elevation at the plant site is 1500 ft and ambient air at a temperature of $98^{\circ} \mathrm{F}$ with a relative humidity of $40 \%$ should be used for design purposes. The air-side pressure loss should not exceed $0.5 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$.
(12.13) Design an air-cooled condenser for the service of Problem 11.28 using:
(a) ACOL.
(b) Xace.

Design conditions are the same as in Problem 12.12.
(12.14) Design an air-cooled condenser for the service of Problem 11.37 using:
(a) ACOL.
(b) Xace.

Design conditions are as specified in Problem 12.12.
(12.15) Design an air-cooled condenser for the service of Problem 11.38 using:
(a) ACOL.
(b) Xace.

The elevation at the plant site is 2500 ft and ambient air at a temperature of $95^{\circ} \mathrm{F}$ with a relative humidity of $40 \%$ should be used for design purposes. The air-side pressure loss should not exceed $0.5 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}$.

## APPENDIX

## Contents

Appendix A: Thermophysical Properties of Materials ..... 682
Appendix B: Dimensions of Pipe and Tubing ..... 717
Appendix C: Tube-Count Tables ..... 729
Appendix D: Equivalent Lengths of Pipe Fittings ..... 737
Appendix E: Properties of Petroleum Streams ..... 740

## Appendix A: Thermophysical Properties of Materials

Table A. 1 Properties of Metallic Elements

| Element ${ }^{\text {a }}$ | Thermal Conductivity $k(\mathrm{~W} / \mathrm{m} \cdot \mathrm{K})^{\text {b }}$ |  |  |  |  |  |  | Properties at $293 \mathrm{~K}\left(20^{\circ} \mathrm{C}\right)$ |  |  |  | Melting <br> Temperature (K) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 200 \mathrm{~K} \\ & -73^{\circ} \mathrm{C} \end{aligned}$ | $\begin{aligned} & 273 \mathrm{~K} \\ & 0^{\circ} \mathrm{C} \end{aligned}$ | $\begin{aligned} & 400 \mathrm{~K} \\ & 127^{\circ} \mathrm{C} \end{aligned}$ | $\begin{aligned} & 600 \mathrm{~K} \\ & 327^{\circ} \mathrm{C} \end{aligned}$ | $\begin{aligned} & 800 \mathrm{~K} \\ & 527^{\circ} \mathrm{C} \end{aligned}$ | $\begin{aligned} & 1000 \mathrm{~K} \\ & 727^{\circ} \mathrm{C} \end{aligned}$ | $\begin{aligned} & 1200 \mathrm{~K} \\ & 927^{\circ} \mathrm{C} \end{aligned}$ | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & c \\ & (\mathrm{~J} / \mathrm{kg} \cdot \mathrm{~K}) \end{aligned}$ | k $(\mathrm{W} / \mathrm{m} \cdot \mathrm{~K})$ | $\begin{gathered} \alpha \times 10^{6} \\ \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{gathered}$ |  |
| Aluminum | 237 | 236 | 240 | 232 | 220 |  |  | 2702 | 896 | 236 | 97.5 | 933 |
| Antimony | 30.2 | 25.5 | 21.2 | 18.2 | 16.8 |  |  | 6684 | 208 | 24.6 | 17.7 | 904 |
| Beryllium | 301 | 218 | 161 | 126 | 107 | 89 | 73 | 1850 | 1750 | 205 | 63.3 | 1550 |
| Bismuth ${ }^{\text {c }}$ | 9.7 | 8.2 |  |  |  |  |  | 9780 | 124 | 7.9 | 6.51 | 545 |
| Boron ${ }^{\text {c }}$ | 52.5 | 31.7 | 18.7 | 11.3 | 8.1 | 6.3 | 5.2 | 2500 | 1047 | 28.6 | 10.9 | 2573 |
| Cadmium ${ }^{\text {c }}$ | 99.3 | 97.5 | 94.7 |  |  |  |  | 8650 | 231 | 97 | 48.5 | 594 |
| Cesium | 36.8 | 36.1 |  |  |  |  |  | 1873 | 230 | 36 | 83.6 | 302 |
| Chromium | 111 | 94.8 | 87.3 | 80.5 | 71.3 | 65.3 | 62.4 | 7160 | 440 | 91.4 | 29.0 | 2118 |
| Cobalt ${ }^{\text {c }}$ | 122 | 104 | 84.8 |  |  |  |  | 8862 | 389 | 100 | 29.0 | 1765 |
| Copper | 413 | 401 | 392 | 383 | 371 | 357 | 342 | 8933 | 383 | 399 | 116.6 | 1356 |
| Germanium | 96.8 | 66.7 | 43.2 | 27.3 | 19.8 | 17.4 | 17.4 | 5360 |  | 61.6 |  | 1211 |
| Gold | 327 | 318 | 312 | 304 | 292 | 278 | 262 | 19300 | 129 | 316 | 126.9 | 1336 |
| Hafnium | 24.4 | 23.3 | 22.3 | 21.3 | 20.8 | 20.7 | 20.9 | 13280 |  | 23.1 |  | 2495 |
| Indium | 89.7 | 83.7 | 74.5 |  |  |  |  | 7300 |  | 82.2 |  | 430 |
| Iridium | 153 | 148 | 144 | 138 | 132 | 126 | 120 | 22500 | 134 | 147 | 48.8 | 2716 |
| Iron | 94 | 83.5 | 69.4 | 54.7 | 43.3 | 32.6 | 28.2 | 7870 | 452 | 81.1 | 22.8 | 1810 |
| Lead | 36.6 | 35.5 | 33.8 | 31.2 |  |  |  | 11340 | 129 | 35.3 | 24.1 | 601 |
| Lithium | 88.1 | 79.2 | 72.1 |  |  |  |  | 534 | 3391 | 77.4 | 42.7 | 454 |
| Magnesium | 159 | 157 | 153 | 149 | 146 |  |  | 1740 | 1017 | 156 | 88.2 | 923 |
| Manganese | 7.17 | 7.68 |  |  |  |  |  | 7290 | 486 | 7.78 | 2.2 | 1517 |
| Mercury ${ }^{\text {c }}$ | 28.9 |  |  |  |  |  |  | 13546 |  |  |  | 234 |


| Molybdenum | 143 | 139 | 134 | 126 | 118 | 112 | 105 | 10240 | 251 | 138 | 53.7 | 2883 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: | ---: |
| Nickel | 106 | 94 | 80.1 | 65.5 | 67.4 | 71.8 | 76.1 | 8900 | 446 | 91 | 22.9 | 1726 |
| Niobium | 52.6 | 53.3 | 55.2 | 58.2 | 61.3 | 64.4 | 67.5 | 8570 | 270 | 53.6 | 23.2 | 2741 |
| Palladium | 75.5 | 75.5 | 75.5 | 75.5 | 75.5 | 75.5 |  | 12020 | 247 | 75.5 | 25.4 | 1825 |
| Platinum | 72.4 | 71.5 | 71.6 | 73.0 | 75.5 | 78.6 | 82.6 | 21450 | 133 | 71.4 | 25.0 | 2042 |
| Potassium | 104 | 104 | 52 |  |  |  |  | 860 | 741 | 103 | 161.6 | 337 |
| Rhenium | 51 | 48.6 | 46.1 | 44.2 | 44.1 | 44.6 | 45.7 | 21100 | 137 | 48.1 | 16.6 | 3453 |
| Rhodium | 154 | 151 | 146 | 136 | 127 | 121 | 115 | 12450 | 248 | 150 | 48.6 | 2233 |
| Rubidium | 58.9 | 58.3 |  |  |  |  |  | 1530 | 348 | 58.2 | 109.3 | 312 |
| Silicon | 264 | 168 | 98.9 | 61.9 | 42.2 | 31.2 | 25.7 | 2330 | 703 | 153 | 93.4 | 1685 |
| Silver | 403 | 428 | 420 | 405 | 389 | 374 | 358 | 10500 | 234 | 427 | 173.8 | 1234 |
| Sodium | 138 | 135 |  |  |  |  |  | 971 | 1206 | 133 | 113.6 | 371 |
| Tantalum | 57.5 | 57.4 | 57.8 | 58.6 | 59.4 | 60.2 | 61 | 16600 | 138 | 57.5 | 251 | 3269 |
| Tin $^{\text {c }}$ | 73.3 | 68.2 | 62.2 |  |  |  |  | 5750 | 227 | 67.0 | 51.3 | 505 |
| Titanium $^{\text {c }}$ | 24.5 | 22.4 | 20.4 | 19.4 | 19.7 | 20.7 | 22 | 4500 | 611 | 22.0 | 8.0 | 1953 |
| Tungsten $^{\text {c }}$ | 197 | 182 | 162 | 139 | 128 | 121 | 115 | 19300 | 134 | 179 | 69.2 | 3653 |
| Uranium $^{\text {c }}$ | 25.1 | 27 | 29.6 | 34 | 38.8 | 43.9 | 49 | 19070 | 113 | 27.4 | 12.7 | 1407 |
| Vanadium $^{31.5}$ | 31.3 | 32.1 | 34.2 | 36.3 | 38.6 | 41.2 | 6100 | 502 | 31.4 | 10.3 | 2192 |  |
| Zinc $^{23}$ | 123 | 122 | 116 | 105 |  |  |  | 7140 | 385 | 121 | 44.0 | 693 |
| Zirconium $^{\text {c }}$ | 25.2 | 23.2 | 21.6 | 20.7 | 21.6 | 23.7 | 25.7 | 6570 | 272 | 22.8 | 12.8 | 2125 |

${ }^{\text {a }}$ Purity for all elements exceeds $99 \%$.
${ }^{\mathrm{b}}$ The expected percent errors in the thermal conductivity values are approximately within $\pm 5 \%$ of the true values near room temperature and within about $\pm 10 \%$ at other temperatures.
${ }^{\mathrm{c}}$ For crystalline materials, the values are given for the polycrystalline materials.
Source: Refs. [1-4].

Table A. 2 Properties of Alloys

| Metal | Composition (\%) | Properties at $293 \mathrm{~K}\left(20^{\circ} \mathrm{C}\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \quad{ }_{(\mathrm{J} / \mathrm{kg} \cdot \mathrm{~K})} \end{aligned}$ | $\begin{aligned} & k \\ & (\mathrm{~W} / \mathrm{m} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{gathered} \alpha \times 10^{5} \\ \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{gathered}$ |
| Aluminum |  |  |  |  |  |
| Duralumin | 94-96 A1, 3-5 Cu, trace Mg | 2787 | 833 | 164 | 6.676 |
| Silumin | $87 \mathrm{~A} 1,13 \mathrm{Si}$ | 2659 | 871 | 164 | 7.099 |
| Copper |  |  |  |  |  |
| Aluminum bronze | $95 \mathrm{Cu}, 5 \mathrm{~A} 1$ | 8666 | 410 | 83 | 2.330 |
| Bronze | $75 \mathrm{Cu}, 25 \mathrm{Sn}$ | 8666 | 343 | 26 | 0.859 |
| Red brass | $85 \mathrm{Cu}, 9 \mathrm{Sn}, 5 \mathrm{Zn}$ | 8714 | 385 | 61 | 1.804 |
| Brass | $70 \mathrm{Cu}, 30 \mathrm{Zn}$ | 8522 | 385 | 111 | 3.412 |
| German silver | $62 \mathrm{Cu}, 15 \mathrm{Ni}, 22 \mathrm{Zn}$ | 8618 | 394 | 24.9 | 0.733 |
| Constantan | $60 \mathrm{Cu}, 40 \mathrm{Ni}$ | 8922 | 410 | 22.7 | 0.612 |
| Iron |  |  |  |  |  |
| Cast iron | $\sim 4 \mathrm{C}$ | 7272 | 420 | 52 | 1.702 |
| Wrought iron |  | 7849 | 460 | 59 | 1.626 |
| Steel |  |  |  |  |  |
| Carbon steel | 1 C | 7801 | 473 | 43 | 1.172 |
|  | 1.5 C | 7753 | 486 | 36 | 0.970 |
| Chrome steel | 1 Cr | 7865 | 460 | 61 | 1.665 |
|  | 5 Cr | 7833 | 460 | 40 | 1.110 |
|  | 10 Cr | 7785 | 460 | 31 | 0.867 |
| Chrome-nickel steel | $15 \mathrm{Cr}, 10 \mathrm{Ni}$ | 7865 | 460 | 19 | 0.526 |
|  | $20 \mathrm{Cr}, 15 \mathrm{Ni}$ | 7833 | 460 | 15.1 | 0.415 |
| Nickel steel | 10 Ni | 7945 | 460 | 26 | 0.720 |
|  | 20 Ni | 7993 | 460 | 19 | 0.526 |
|  | 40 Ni | 8169 | 460 | 10 | 0.279 |
|  | 60 Ni | 8378 | 460 | 19 | 0.493 |
| Nickel-chrome steel | $80 \mathrm{Ni}, 15 \mathrm{Cr}$ | 8522 | 460 | 17 | 0.444 |
|  | $60 \mathrm{Ni}, 15 \mathrm{Cr}$ | 8266 | 460 | 12.8 | 0.333 |
|  | $40 \mathrm{Ni}, 15 \mathrm{Cr}$ | 8073 | 460 | 11.6 | 0.305 |
|  | $20 \mathrm{Ni}, 15 \mathrm{Cr}$ | 7865 | 460 | 14.0 | 0.390 |
| Manganese steel | 1 Mn | 7865 | 460 | 50 | 1.388 |
|  | 5 Mn | 7849 | 460 | 22 | 0.637 |
| Silicon steel | 1 Si | 7769 | 460 | 42 | 1.164 |
|  | 5 Si | 7417 | 460 | 19 | 0.555 |
| Stainless steel | Type 304 | 7817 | 461 | 14.4 | 0.387 |
|  | Type 347 | 7817 | 461 | 14.3 | 0.387 |
| Tungsten steel | 1 W | 7913 | 448 | 66 | 1.858 |
|  | 5 W | 8073 | 435 | 54 | 1.525 |

[^4]Table A. 3 Properties of Insulations and Building Materials


Table A. 3 (Continued)

| Substance | Temperature <br> $\left({ }^{( } \mathrm{C}\right)$ | $k$ | $\rho$ | $c$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | $\left(\mathrm{~W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}\right)$ | ${ }^{\left(\mathrm{kg} / \mathrm{m}^{3}\right)}$ | ${ }^{\left(\mathrm{kJ} / \mathrm{kg} \cdot{ }^{\circ} \mathrm{C}\right)}$ | $\alpha \times 10^{7}$ <br> $\left(\mathrm{~m}^{2} / \mathrm{s}\right)$ |

## Insulating materials

Asbestos

| Loosely packed | $\begin{gathered} -45 \\ 0 \end{gathered}$ | 0.149 0.154 | 470-570 | 0.816 | 3.3-4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 100 | 0.161 |  |  |  |
| Asbestos-cement boards | 20 | 0.74 |  |  |  |
| Sheets | 51 | 0.166 |  |  |  |
| Felt, 40 laminations/in. | 38 | 0.057 |  |  |  |
|  | 150 | 0.069 |  |  |  |
|  | 260 | 0.083 |  |  |  |
| 20 laminations/in. | 38 | 0.078 |  |  |  |
|  | 150 | 0.095 |  |  |  |
|  | 260 | 0.112 |  |  |  |
| Corrugated, 4 plies/in. | 38 | 0.087 |  |  |  |
|  | 93 | 0.100 |  |  |  |
|  | 150 | 0.119 |  |  |  |
| Asbestos cement | - | 2.08 |  |  |  |
| Balsam wool, $2.2 \mathrm{lb} / \mathrm{ft}^{3}$ | 32 | 0.04 | 35 |  |  |
| Cardboard, corrugated | - | 0.064 |  |  |  |
| Celotex | 32 | 0.048 |  |  |  |
| Corkboard, $10 \mathrm{lb} / \mathrm{ft}^{3}$ | 30 | 0.043 | 160 |  |  |
| Cork, regranulated | 32 | 0.045 | 45-120 | 1.88 | 2-5.3 |
| Ground | 32 | 0.043 | 150 |  |  |
| Diatomaceous earth (Silo-cel) | 0 | 0.061 | 320 |  |  |
| Felt, hair | 30 | 0.036 | 130-200 |  |  |
| Wool | 30 | 0.052 | 330 |  |  |
| Fiber, insulating board | 20 | 0.048 | 240 |  |  |
| Glass wool, $1.5 \mathrm{lb} / \mathrm{ft}^{3}$ | 23 | 0.038 | 24 | 0.7 | 22.6 |
| Insulex, dry | 32 | 0.064 |  |  |  |
|  |  | 0.144 |  |  |  |
| Kapok | 30 | 0.035 |  |  |  |
| Magnesia, 85\% | 38 | 0.067 | 270 |  |  |
|  | 93 | 0.071 |  |  |  |
|  | 150 | 0.074 |  |  |  |
|  | 204 | 0.080 |  |  |  |
| Rock wool, $10 \mathrm{lb} / \mathrm{ft}^{3}$ | 32 | 0.040 | 160 |  |  |
| Loosely packed | 150 | 0.067 | 64 |  |  |
|  | 260 | 0.087 |  |  |  |
| Sawdust | 23 | 0.059 |  |  |  |
| Silica aerogel | 32 | 0.024 | 140 |  |  |
| Wood shavings | 23 | 0.059 |  |  |  |

[^5]Table A. 4 Properties of Dry Air at Atmospheric Pressure: SI Units

| $T$ |  | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \beta \times 10^{3} \\ & (1 / \mathrm{K}) \end{aligned}$ | $C_{P}$ <br> (J/kg $\cdot \mathrm{K}$ ) | $\begin{aligned} & k \\ & (\mathrm{~W} / \mathrm{m} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{aligned} & \alpha \times 10^{6} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | $\begin{aligned} & \mu \times 10^{6} \\ & \left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right) \end{aligned}$ | $\begin{aligned} & v \times 10^{6} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | Pr | $\begin{aligned} & g \beta / v^{2} \times 10^{-8} \\ & \left(1 / \mathrm{K} \cdot \mathrm{~m}^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (K) | $\left({ }^{\circ} \mathrm{C}\right)$ |  |  |  |  |  |  |  |  |  |
| 273 | 0 | 1.252 | 3.66 | 1011 | 0.0237 | 19.2 | 17.456 | 13.9 | 0.71 | 1.85 |
| 293 | 20 | 1.164 | 3.41 | 1012 | 0.0251 | 22.0 | 18.240 | 15.7 | 0.71 | 1.36 |
| 313 | 40 | 1.092 | 3.19 | 1014 | 0.0265 | 24.8 | 19.123 | 17.6 | 0.71 | 1.01 |
| 333 | 60 | 1.025 | 3.00 | 1017 | 0.0279 | 27.6 | 19.907 | 19.4 | 0.71 | 0.782 |
| 353 | 80 | 0.968 | 2.83 | 1019 | 0.0293 | 30.6 | 20.790 | 21.5 | 0.71 | 0.600 |
| 373 | 100 | 0.916 | 2.68 | 1022 | 0.0307 | 33.6 | 21.673 | 23.6 | 0.71 | 0.472 |
| 473 | 200 | 0.723 | 2.11 | 1035 | 0.0370 | 49.7 | 25.693 | 35.5 | 0.71 | 0.164 |
| 573 | 300 | 0.596 | 1.75 | 1047 | 0.0429 | 68.9 | 39.322 | 49.2 | 0.71 | 0.0709 |
| 673 | 400 | 0.508 | 1.49 | 1059 | 0.0485 | 89.4 | 32.754 | 64.6 | 0.72 | 0.0350 |
| 773 | 500 | 0.442 | 1.29 | 1076 | 0.0540 | 113.2 | 35.794 | 81.0 | 0.72 | 0.0193 |
| 1273 | 1000 | 0.268 | 0.79 | 1139 | 0.0762 | 240 | 48.445 | 181 | 0.74 | 0.00236 |

Source: Refs. [1] and [3].

Table A. 5 Properties of Dry Air at Atmospheric Pressure: English Units

| $\mathrm{T}\left({ }^{\circ} \mathrm{F}\right)$ | $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | $\mu(\mathrm{lbm} / \mathrm{ft} \cdot \mathrm{h})$ | $\rho\left(\mathrm{lbm} / \mathrm{ft}{ }^{3}\right)$ | $P r$ |
| ---: | :--- | :--- | :--- | :--- | :--- |
| 0 | 0.241 | 0.0131 | 0.0387 | 0.0864 | 0.71 |
| 20 | 0.241 | 0.0136 | 0.0402 | 0.0828 | 0.71 |
| 40 | 0.241 | 0.0141 | 0.0416 | 0.0795 | 0.71 |
| 60 | 0.241 | 0.0147 | 0.0428 | 0.0764 | 0.70 |
| 80 | 0.241 | 0.0152 | 0.0440 | 0.0735 | 0.70 |
| 100 | 0.241 | 0.0156 | 0.0455 | 0.0709 | 0.70 |
| 120 | 0.241 | 0.0161 | 0.0467 | 0.0685 | 0.70 |
| 140 | 0.242 | 0.0171 | 0.0491 | 0.0662 | 0.70 |
| 160 | 0.242 | 0.0176 | 0.0503 | 0.0640 | 0.69 |
| 180 | 0.242 | 0.0180 | 0.0515 | 0.0620 | 0.69 |
| 200 | 0.242 | 0.0203 | 0.0544 | 0.0601 | 0.69 |
| 250 | 0.243 | 0.0214 | 0.0573 | 0.0559 | 0.69 |
| 300 | 0.244 | 0.0235 | 0.0600 | 0.69 |  |
| 350 | 0.245 | 0.0246 | 0.0653 | 0.0490 | 0.69 |
| 400 | 0.246 | 0.0266 | 0.0677 | 0.0461 | 0.69 |
| 450 | 0.247 | 0.0285 | 0.0723 | 0.0436 | 0.68 |
| 500 | 0.248 | 0.0303 | 0.0767 | 0.0374 | 0.68 |
| 600 | 0.251 | 0.0320 | 0.0810 | 0.0342 | 0.68 |
| 700 | 0.254 | 0.0337 | 0.0849 | 0.0315 | 0.69 |
| 800 | 0.257 | 0.0885 | 0.0292 | 0.69 |  |
| 900 | 0.260 |  |  | 0.0272 | 0.69 |
| 1000 | 0.263 |  |  |  |  |

[^6]Table A. 6 Properties of Steam at Atmospheric Pressure

| $T$ |  | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \beta \times 10^{3} \\ & (1 / \mathrm{K}) \end{aligned}$ | $C_{P}$ <br> (J/kg $\cdot \mathrm{K}$ ) | $\begin{aligned} & k \\ & (\mathrm{~W} / \mathrm{m} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{gathered} \alpha \times 10^{4} \\ \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{gathered}$ | $\begin{aligned} & \mu \times 10^{6} \\ & \left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right) \end{aligned}$ | $\begin{aligned} & \nu \times 10^{6} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | Pr | $\begin{aligned} & g \beta / v^{2} \times 10^{-6} \\ & \left(1 / \mathrm{K} \cdot \mathrm{~m}^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (K) | $\left({ }^{\circ} \mathrm{C}\right)$ |  |  |  |  |  |  |  |  |  |
| 373 | 100 | 0.5977 |  | 2034 | 0.0249 | 0.204 | 12.10 | 20.2 | 0.987 |  |
| 380 | 107 | 0.5863 |  | 2060 | 0.0246 | 0.204 | 12.71 | 21.6 | 1.060 |  |
| 400 | 127 | 0.5542 | 2.50 | 2014 | 0.0261 | 0.234 | 13.44 | 24.2 | 1.040 | 41.86 |
| 450 | 177 | 0.4902 | 2.22 | 1980 | 0.0299 | 0.307 | 15.25 | 31.1 | 1.010 | 22.51 |
| 500 | 227 | 0.4405 | 2.00 | 1985 | 0.0339 | 0.387 | 17.04 | 38.6 | 0.996 | 13.16 |
| 550 | 277 | 0.4005 | 1.82 | 1997 | 0.0379 | 0.475 | 18.84 | 47.0 | 0.991 | 8.08 |
| 600 | 327 | 0.3652 | 1.67 | 2026 | 0.0422 | 0.573 | 20.67 | 56.6 | 0.986 | 5.11 |
| 650 | 377 | 0.3380 | 1.54 | 2056 | 0.0464 | 0.666 | 22.47 | 66.4 | 0.995 | 3.43 |
| 700 | 427 | 0.3140 | 1.43 | 2085 | 0.0505 | 0.772 | 24.26 | 77.2 | 1.000 | 2.35 |
| 750 | 477 | 0.2931 | 1.33 | 2119 | 0.0549 | 0.883 | 26.04 | 88.8 | 1.005 | 1.65 |
| 800 | 527 | 0.2739 | 1.25 | 2152 | 0.0592 | 1.001 | 27.86 | 102.0 | 1.010 | 1.18 |
| 850 | 577 | 0.2579 | 1.18 | 2186 | 0.0637 | 1.130 | 29.69 | 115.2 | 1.019 | 0.872 |

Source: Refs. [1] and [2].

Table A. 7 Properties of Liquid Water at Saturation Pressure: SI Units

| $T$ |  | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \beta \times 10^{4} \\ & (1 / \mathrm{K}) \end{aligned}$ | $\begin{aligned} & C_{P} \\ & (\mathrm{~J} / \mathrm{kg} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{aligned} & k \\ & (\mathrm{~W} / \mathrm{m} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{gathered} \alpha \times 10^{6} \\ \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{gathered}$ | $\begin{aligned} & \mu \times 10^{6} \\ & \left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right) \end{aligned}$ | $\begin{aligned} & v \times 10^{6} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | Pr | $\begin{aligned} & g \beta / v^{2} \times 10^{-9} \\ & \left(1 / \mathrm{K} \cdot \mathrm{~m}^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |
| (K) | $\left({ }^{\circ} \mathrm{C}\right)$ |  |  |  |  |  |  |  |  |  |
| 273 | 0 | 999.9 | $-0.7$ | 4226 | 0.558 | 0.131 | 1794 | 1.789 | 13.7 | - |
| 278 | 5 | 1000 | - | 4206 | 0.568 | 0.135 | 1535 | 1.535 | 11.4 | - |
| 283 | 10 | 999.7 | 0.95 | 4195 | 0.577 | 0.137 | 1296 | 1.300 | 9.5 | 0.551 |
| 288 | 15 | 999.1 | - | 4187 | 0.585 | 0.141 | 1136 | 1.146 | 8.1 | - |
| 293 | 20 | 998.2 | 2.1 | 4182 | 0.597 | 0.143 | 993 | 1.006 | 7.0 | 2.035 |
| 298 | 25 | 997.1 | - | 4178 | 0.606 | 0.146 | 880.6 | 0.884 | 6.1 | - |
| 303 | 30 | 995.7 | 3.0 | 4176 | 0.615 | 0.149 | 792.4 | 0.805 | 5.4 | 4.540 |
| 308 | 35 | 994.1 | - | 4175 | 0.624 | 0.150 | 719.8 | 0.725 | 4.8 | - |
| 313 | 40 | 992.2 | 3.9 | 4175 | 0.633 | 0.151 | 658.0 | 0.658 | 4.3 | 8.833 |
| 318 | 45 | 990.2 | - | 4176 | 0.640 | 0.155 | 605.1 | 0.611 | 3.9 | - |
| 323 | 50 | 988.1 | 4.6 | 4178 | 0.647 | 0.157 | 555.1 | 0.556 | 3.55 | 14.59 |
| 348 | 75 | 974.9 | - | 4190 | 0.671 | 0.164 | 376.6 | 0.366 | 2.23 | - |
| 373 | 100 | 958.4 | 7.5 | 4211 | 0.682 | 0.169 | 277.5 | 0.294 | 1.75 | 85.09 |
| 393 | 120 | 943.5 | 8.5 | 4232 | 0.685 | 0.171 | 235.4 | 0.244 | 1.43 | 140.0 |
| 413 | 140 | 926.3 | 9.7 | 4257 | 0.684 | 0.172 | 201.0 | 0.212 | 1.23 | 211.7 |
| 433 | 160 | 907.6 | 10.8 | 4285 | 0.680 | 0.173 | 171.6 | 0.191 | 1.10 | 290.3 |
| 453 | 180 | 886.6 | 12.1 | 4396 | 0.673 | 0.172 | 152.0 | 0.173 | 1.01 | 396.5 |
| 473 | 200 | 862.8 | 13.5 | 4501 | 0.665 | 0.170 | 139.3 | 0.160 | 0.95 | 517.2 |
| 493 | 220 | 837.0 | 15.2 | 4605 | 0.652 | 0.167 | 124.5 | 0.149 | 0.90 | 671.4 |
| 513 | 240 | 809.0 | 17.2 | 4731 | 0.634 | 0.162 | 113.8 | 0.141 | 0.86 | 848.5 |
| 533 | 260 | 779.0 | 20.0 | 4982 | 0.613 | 0.156 | 104.9 | 0.135 | 0.86 | 1076 |
| 553 | 280 | 750.0 | 23.8 | 5234 | 0.588 | 0.147 | 98.07 | 0.131 | 0.89 | 1360 |
| 573 | 300 | 712.5 | 29.5 | 5694 | 0.564 | 0.132 | 92.18 | 0.128 | 0.98 | 1766 |

Source: Refs. [1] and [3].

Table A. 8 Properties of Saturated Steam and Water: English Units

| Absolute pressure |  | Vacuum (in. Hg ) | Temperature ( $\left.{ }^{\circ} \mathrm{F}\right)$ | Heat of the liquid (Btu/lb) | Latent heat of evaporation (Btu/lb) | Total heat of steam (Btu/lb) | Specific volume |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (psi) | (in. Hg ) |  |  |  |  |  | Water $\left(\mathrm{ft}^{3} / \mathrm{lb}\right)$ | Steam <br> (ft ${ }^{3} / \mathrm{lb}$ ) |
| 0.08859 | 0.02 | 29.90 | 32.018 | 0.0003 | 1075.5 | 1075.5 | 0.016022 | 3302.4 |
| 0.10 | 0.20 | 29.72 | 35.023 | 3.026 | 1073.8 | 1076.8 | 0.016020 | 2945.5 |
| 0.15 | 0.31 | 29.61 | 45.453 | 13.498 | 1067.9 | 1081.4 | 0.016020 | 2004.7 |
| 0.20 | 0.41 | 29.51 | 53.160 | 21.217 | 1053.5 | 1084.7 | 0.016025 | 1526.3 |
| 0.25 | 0.51 | 29.41 | 59.323 | 27.382 | 1060.1 | 1087.4 | 0.016032 | 1235.5 |
| 0.30 | 0.61 | 29.31 | 64.484 | 32.541 | 1057.1 | 1089.7 | 0.016040 | 1039.7 |
| 0.35 | 0.71 | 29.21 | 68.939 | 36.992 | 1054.6 | 1091.6 | 0.016048 | 898.6 |
| 0.40 | 0.81 | 29.11 | 72.869 | 40.917 | 1052.4 | 1093.3 | 0.016056 | 792.1 |
| 0.45 | 0.92 | 29.00 | 76.387 | 44.430 | 1050.5 | 1094.9 | 0.016063 | 708.8 |
| 0.50 | 1.02 | 28.90 | 79.586 | 47.623 | 1048.6 | 1096.3 | 0.016071 | 641.5 |
| 0.60 | 1.22 | 28.70 | 85.218 | 53.245 | 1045.5 | 1098.7 | 0.016085 | 540.1 |
| 0.70 | 1.43 | 28.49 | 90.09 | 58.10 | 1042.7 | 1100.8 | 0.016099 | 466.94 |
| 0.80 | 1.63 | 28.29 | 94.38 | 62.39 | 1040.3 | 1102.6 | 0.016112 | 411.69 |
| 0.90 | 1.83 | 28.09 | 98.24 | 66.24 | 1038.1 | 1104.3 | 0.016124 | 368.43 |
| 1.0 | 2.04 | 27.88 | 101.74 | 69.73 | 1036.1 | 1105.8 | 0.016136 | 333.60 |
| 1.2 | 2.44 | 27.48 | 107.91 | 75.90 | 1032.6 | 1108.5 | 0.016158 | 280.96 |
| 1.4 | 2.85 | 27.07 | 113.26 | 81.23 | 1029.5 | 1110.7 | 0.016178 | 243.02 |
| 1.6 | 3.26 | 26.66 | 117.98 | 85.95 | 1026.8 | 1112.7 | 0.016196 | 214.33 |
| 1.8 | 3.66 | 26.26 | 122.22 | 90.18 | 1024.3 | 1114.5 | 0.016213 | 191.85 |
| 2.0 | 4.07 | 25.85 | 126.07 | 94.03 | 1022.1 | 1116.2 | 0.016230 | 173.76 |
| 2.2 | 4.48 | 25.44 | 129.61 | 97.57 | 1020.1 | 1117.6 | 0.016245 | 158.87 |
| 2.4 | 4.89 | 25.03 | 132.88 | 100.84 | 1018.2 | 1119.0 | 0.016260 | 146.40 |
| 2.6 | 5.29 | 24.63 | 135.93 | 103.88 | 1016.4 | 1120.3 | 0.016274 | 135.80 |
| 2.8 | 5.70 | 24.22 | 138.78 | 106.73 | 1014.7 | 1121.5 | 0.016287 | 126.67 |
| 3.0 | 6.11 | 23.81 | 141.47 | 109.42 | 1013.2 | 1122.6 | 0.016300 | 118.73 |
| 3.5 | 7.13 | 22.79 | 147.56 | 115.51 | 1009.6 | 1125.1 | 0.016331 | 102.74 |
| 4.0 | 8.14 | 21.78 | 152.96 | 120.92 | 1006.4 | 1127.3 | 0.016358 | 90.64 |
| 4.5 | 9.16 | 20.76 | 157.82 | 125.77 | 1003.5 | 1129.3 | 0.016384 | 83.03 |
| 5.0 | 10.18 | 19.74 | 162.24 | 130.20 | 1000.9 | 1131.1 | 0.016407 | 73.532 |
| 5.5 | 11.20 | 18.72 | 166.29 | 134.26 | 998.5 | 1132.7 | 0.016430 | 67.249 |
| 6.0 | 12.22 | 17.70 | 170.05 | 138.03 | 996.2 | 1134.2 | 0.016451 | 61.984 |
| 6.5 | 13.23 | 16.69 | 173.56 | 141.54 | 994.1 | 1135.6 | 0.016472 | 57.506 |
| 7.0 | 14.25 | 15.67 | 176.84 | 144.83 | 992.1 | 1136.9 | 0.016491 | 53.650 |
| 7.5 | 15.27 | 14.65 | 179.93 | 147.93 | 990.2 | 1138.2 | 0.016510 | 50.294 |
| 8.0 | 16.29 | 13.63 | 182.86 | 150.87 | 988.5 | 1139.3 | 0.016527 | 47.345 |
| 8.5 | 17.31 | 12.61 | 185.63 | 153.65 | 986.8 | 1140.4 | 0.016545 | 44.733 |
| 9.0 | 18.32 | 11.60 | 188.27 | 156.30 | 985.1 | 1141.4 | 0.016561 | 42.402 |
| 9.5 | 19.34 | 10.58 | 190.80 | 158.84 | 983.6 | 1142.4 | 0.016577 | 40.310 |
| 10.0 | 20.36 | 9.56 | 193.21 | 161.26 | 982.1 | 1143.3 | 0.016592 | 38.420 |
| 11.0 | 22.40 | 7.52 | 197.75 | 165.82 | 979.3 | 1145.1 | 0.016622 | 35.142 |
| 12.0 | 24.43 | 5.49 | 201.96 | 170.05 | 976.6 | 1146.7 | 0.016650 | 32.394 |
| 13.0 | 26.47 | 3.45 | 205.88 | 174.00 | 974.2 | 1148.2 | 0.016676 | 30.057 |
| 14.0 | 28.50 | 1.42 | 209.56 | 177.71 | 971.9 | 1149.6 | 0.016702 | 28.043 |

Table A. 8 (Continued)

| Pressure (psi) |  | Temperature ( $\left.{ }^{\circ} \mathrm{F}\right)$ | Heat of the liquid (Btu/lb) | Latent heat of evaporation (Btu/lb) | Total heat of steam (Btu/lb) | Specific volume |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Absolute | Gage |  |  |  |  | Water (ft ${ }^{3} / \mathrm{lb}$ ) | Steam (ft $\left.{ }^{3} / \mathrm{lb}\right)$ |
| 14.696 | 0.0 | 212.00 | 180.17 | 970.3 | 1150.3 | 0.016719 | 26.799 |
| 15.0 | 0.3 | 213.03 | 181.21 | 969.7 | 1150.9 | 0.016726 | 26.290 |
| 16.0 | 1.3 | 216.32 | 184.52 | 967.6 | 1152.1 | 0.016749 | 24.750 |
| 17.0 | 2.3 | 219.44 | 187.66 | 965.6 | 1153.2 | 0.016771 | 23.385 |
| 18.0 | 3.3 | 222.41 | 190.66 | 963.7 | 1154.3 | 0.016793 | 22.168 |
| 19.0 | 4.3 | 225.24 | 193.52 | 961.8 | 1155.3 | 0.016814 | 21.074 |
| 20.0 | 5.3 | 227.96 | 196.27 | 960.1 | 1156.3 | 0.016834 | 20.087 |
| 21.0 | 6.3 | 230.57 | 198.90 | 958.4 | 1157.3 | 0.016854 | 19.190 |
| 22.0 | 7.3 | 233.07 | 201.44 | 956.7 | 1158.1 | 0.016873 | 18.373 |
| 23.0 | 8.3 | 235.49 | 203.88 | 955.1 | 1159.0 | 0.016891 | 17.624 |
| 24.0 | 9.3 | 237.82 | 206.24 | 953.6 | 1159.8 | 0.016909 | 16.936 |
| 25.0 | 10.3 | 240.07 | 208.52 | 952.1 | 1160.6 | 0.016927 | 16.301 |
| 26.0 | 11.3 | 242.25 | 210.7 | 950.6 | 1161.4 | 0.016944 | 15.7138 |
| 27.0 | 12.3 | 244.36 | 212.9 | 949.2 | 1162.1 | 0.016961 | 15.1684 |
| 28.0 | 13.3 | 246.41 | 214.9 | 947.9 | 1162.8 | 0.016977 | 14.6607 |
| 29.0 | 14.3 | 248.40 | 217.0 | 946.5 | 1163.5 | 0.016993 | 14.1869 |
| 30.0 | 15.3 | 250.34 | 218.9 | 945.2 | 1164.1 | 0.017009 | 13.7436 |
| 31.0 | 16.3 | 252.22 | 220.8 | 943.9 | 1164.8 | 0.017024 | 13.3280 |
| 32.0 | 17.3 | 254.05 | 222.7 | 942.7 | 1165.4 | 0.017039 | 12.9376 |
| 33.0 | 18.3 | 255.84 | 224.5 | 941.5 | 1166.0 | 0.017054 | 12.5700 |
| 34.0 | 19.3 | 257.58 | 226.3 | 940.3 | 1166.6 | 0.017069 | 12.2234 |
| 35.0 | 20.3 | 259.29 | 228.0 | 939.1 | 1167.1 | 0.017083 | 11.8959 |
| 36.0 | 21.3 | 260.95 | 229.7 | 938.0 | 1167.7 | 0.017097 | 11.5860 |
| 37.0 | 22.3 | 262.58 | 231.4 | 936.9 | 1168.2 | 0.017111 | 11.2923 |
| 38.0 | 23.3 | 264.17 | 233.0 | 935.8 | 1168.8 | 0.017124 | 11.0136 |
| 39.0 | 24.3 | 265.72 | 234.6 | 934.7 | 1169.3 | 0.017138 | 10.7487 |
| 40.0 | 25.3 | 267.25 | 236.1 | 933.6 | 1169.8 | 0.017151 | 10.4965 |
| 41.0 | 26.3 | 268.74 | 237.7 | 932.6 | 1170.2 | 0.017164 | 10.2563 |
| 42.0 | 27.3 | 270.21 | 239.2 | 931.5 | 1170.7 | 0.017177 | 10.0272 |
| 43.0 | 28.3 | 271.65 | 240.6 | 930.5 | 1171.2 | 0.017189 | 9.8083 |
| 44.0 | 29.3 | 273.06 | 242.1 | 929.5 | 1171.6 | 0.017202 | 9.5991 |
| 45.0 | 30.3 | 274.44 | 243.5 | 928.6 | 1172.0 | 0.017214 | 9.3988 |
| 46.0 | 31.3 | 275.80 | 244.9 | 927.6 | 1172.5 | 0.017226 | 9.2070 |
| 47.0 | 32.3 | 277.14 | 246.2 | 926.6 | 1172.9 | 0.017238 | 9.0231 |
| 48.0 | 33.3 | 278.45 | 247.6 | 925.7 | 1173.3 | 0.017250 | 8.8465 |
| 49.0 | 34.3 | 279.74 | 248.9 | 924.8 | 1173.7 | 0.017262 | 8.6770 |
| 50.0 | 35.3 | 281.02 | 250.2 | 923.9 | 1174.1 | 0.017274 | 8.5140 |
| 51.0 | 36.3 | 282.27 | 251.5 | 923.0 | 1174.5 | 0.017285 | 8.3571 |
| 52.0 | 37.3 | 283.50 | 252.8 | 922.1 | 1174.9 | 0.017296 | 8.2061 |
| 53.0 | 38.3 | 284.71 | 254.0 | 921.2 | 1175.2 | 0.017307 | 8.0606 |
| 54.0 | 39.3 | 285.90 | 255.2 | 920.4 | 1175.6 | 0.017319 | 7.9203 |
| 55.0 | 40.3 | 287.08 | 256.4 | 919.5 | 1175.9 | 0.017329 | 7.7850 |
| 56.0 | 41.3 | 288.24 | 257.6 | 918.7 | 1176.3 | 0.017340 | 7.6543 |
| 57.0 | 42.3 | 289.38 | 258.8 | 917.8 | 1176.6 | 0.017351 | 7.5280 |
| 58.0 | 43.3 | 290.50 | 259.9 | 917.0 | 1177.0 | 0.017362 | 7.4059 |
| 59.0 | 44.3 | 291.62 | 261.1 | 916.2 | 1177.3 | 0.017372 | 7.2879 |

Table A. 8 (Continued)

| Pressure (psi) |  | Temperature$\left({ }^{\circ} \mathrm{F}\right)$ | Heat of the liquid (Btu/lb) | Latent heat of evaporation (Btu/lb) | Total heat of steam (Btu/lb) | Specific volume |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Absolute | Gage |  |  |  |  | Water ( $\mathrm{ft}^{3} / \mathrm{lb}$ ) | $\begin{aligned} & \text { Steam } \\ & \left(\mathrm{ft}^{3} / \mathrm{lb}\right) \end{aligned}$ |
| 60.0 | 45.3 | 292.71 | 262.2 | 915.4 | 1177.6 | 0.017383 | 7.1736 |
| 61.0 | 46.3 | 293.79 | 263.3 | 914.6 | 1177.9 | 0.017393 | 7.0630 |
| 62.0 | 47.3 | 294.86 | 264.4 | 913.8 | 1178.2 | 0.017403 | 6.9558 |
| 63.0 | 48.3 | 295.91 | 265.5 | 913.0 | 1178.6 | 0.017413 | 6.8519 |
| 64.0 | 49.3 | 296.95 | 266.6 | 912.3 | 1178.9 | 0.017423 | 6.7511 |
| 65.0 | 50.3 | 297.98 | 267.6 | 911.5 | 1179.1 | 0.017433 | 6.6533 |
| 66.0 | 51.3 | 298.99 | 268.7 | 910.8 | 1179.4 | 0.017443 | 6.5584 |
| 67.0 | 52.3 | 299.99 | 269.7 | 910.0 | 1179.7 | 0.017453 | 6.4662 |
| 68.0 | 53.3 | 300.99 | 270.7 | 909.3 | 1180.0 | 0.017463 | 6.3767 |
| 69.0 | 54.3 | 301.96 | 271.7 | 908.5 | 1180.3 | 0.017472 | 6.2896 |
| 70.0 | 55.3 | 302.93 | 272.7 | 907.8 | 1180.6 | 0.017482 | 6.2050 |
| 71.0 | 56.3 | 303.89 | 273.7 | 907.1 | 1180.8 | 0.017491 | 6.1226 |
| 72.0 | 57.3 | 304.83 | 274.7 | 906.4 | 1181.1 | 0.017501 | 6.0425 |
| 73.0 | 58.3 | 305.77 | 275.7 | 905.7 | 1181.4 | 0.017510 | 5.9645 |
| 74.0 | 59.3 | 306.69 | 276.6 | 905.0 | 1181.6 | 0.017519 | 5.8885 |
| 75.0 | 60.3 | 307.61 | 277.6 | 904.3 | 1181.9 | 0.017529 | 5.8144 |
| 76.0 | 61.3 | 308.51 | 278.5 | 903.6 | 1182.1 | 0.017538 | 5.7423 |
| 77.0 | 62.3 | 309.41 | 279.4 | 902.9 | 1182.4 | 0.017547 | 5.6720 |
| 78.0 | 63.3 | 310.29 | 280.3 | 902.3 | 1182.6 | 0.017556 | 5.6034 |
| 79.0 | 64.3 | 311.17 | 281.3 | 901.6 | 1182.8 | 0.017565 | 5.5364 |
| 80.0 | 65.3 | 312.04 | 282.1 | 900.9 | 1183.1 | 0.017573 | 5.4711 |
| 81.0 | 66.3 | 312.90 | 283.0 | 900.3 | 1183.3 | 0.017582 | 5.4074 |
| 82.0 | 67.3 | 313.75 | 283.9 | 899.6 | 1183.5 | 0.017591 | 5.3451 |
| 83.0 | 68.3 | 314.60 | 284.8 | 899.0 | 1183.8 | 0.017600 | 5.2843 |
| 84.0 | 69.3 | 315.43 | 285.7 | 898.3 | 1184.0 | 0.017608 | 5.2249 |
| 85.0 | 70.3 | 316.26 | 286.5 | 897.7 | 1184.2 | 0.017617 | 5.1669 |
| 86.0 | 71.3 | 317.08 | 287.4 | 897.0 | 1184.4 | 0.017625 | 5.1101 |
| 87.0 | 72.3 | 317.89 | 288.2 | 896.4 | 1184.6 | 0.017634 | 5.0546 |
| 88.0 | 73.3 | 318.69 | 289.0 | 895.8 | 1184.8 | 0.017642 | 5.0004 |
| 89.0 | 74.3 | 319.49 | 289.9 | 895.2 | 1185.0 | 0.017651 | 4.9473 |
| 90.0 | 75.3 | 320.28 | 290.7 | 894.6 | 1185.3 | 0.017659 | 4.8953 |
| 91.0 | 76.3 | 321.06 | 291.5 | 893.9 | 1185.5 | 0.017667 | 4.8445 |
| 92.0 | 77.3 | 321.84 | 292.3 | 893.3 | 1185.7 | 0.017675 | 4.7947 |
| 93.0 | 78.3 | 322.61 | 293.1 | 892.7 | 1185.9 | 0.017684 | 4.7459 |
| 94.0 | 79.3 | 323.37 | 293.9 | 892.1 | 1186.0 | 0.017692 | 4.6982 |
| 95.0 | 80.3 | 324.13 | 294.7 | 891.5 | 1186.2 | 0.017700 | 4.6514 |
| 96.0 | 81.3 | 324.88 | 295.5 | 891.0 | 1186.4 | 0.017708 | 4.6055 |
| 97.0 | 82.3 | 325.63 | 296.3 | 890.4 | 1186.6 | 0.017716 | 4.5606 |
| 98.0 | 83.3 | 326.36 | 297.0 | 889.8 | 1186.8 | 0.017724 | 4.5166 |
| 99.0 | 84.3 | 327.10 | 297.8 | 889.2 | 1187.0 | 0.017732 | 4.4734 |
| 100.0 | 85.3 | 327.82 | 298.5 | 888.6 | 1187.2 | 0.017740 | 4.4310 |
| 101.0 | 86.3 | 328.54 | 299.3 | 888.1 | 1187.3 | 0.01775 | 4.3895 |
| 102.0 | 87.3 | 329.26 | 300.0 | 887.5 | 1187.5 | 0.01776 | 4.3487 |
| 103.0 | 88.3 | 329.97 | 300.8 | 886.9 | 1187.7 | 0.01776 | 4.3087 |
| 104.0 | 89.3 | 330.67 | 301.5 | 886.4 | 1187.9 | 0.01777 | 4.2695 |

Table A. 8 (Continued)

| Pressure (psi) |  | Temperature$\left({ }^{\circ} \mathrm{F}\right)$ | Heat of the liquid (Btu/lb) | Latent heat of evaporation (Btu/lb) | Total heat of steam (Btu/lb) | Specific volume |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Absolute | Gage |  |  |  |  | Water (ft $\left.{ }^{3} / \mathrm{lb}\right)$ | Steam (ft $\left.{ }^{3} / \mathrm{lb}\right)$ |
| 105.0 | 90.3 | 331.37 | 302.2 | 885.8 | 1188.0 | 0.01778 | 4.2309 |
| 106.0 | 91.3 | 332.06 | 303.0 | 885.2 | 1188.2 | 0.01779 | 4.1931 |
| 107.0 | 92.3 | 332.75 | 303.7 | 884.7 | 1188.4 | 0.01779 | 4.1560 |
| 108.0 | 93.3 | 333.44 | 304.4 | 884.1 | 1188.5 | 0.01780 | 4.1195 |
| 109.0 | 94.3 | 334.11 | 305.1 | 883.6 | 1188.7 | 0.01781 | 4.0837 |
| 110.0 | 95.3 | 334.79 | 305.8 | 883.1 | 1188.9 | 0.01782 | 4.0484 |
| 111.0 | 96.3 | 335.46 | 306.5 | 882.5 | 1189.0 | 0.01782 | 4.0138 |
| 112.0 | 97.3 | 336.12 | 307.2 | 882.0 | 1189.2 | 0.01783 | 3.9798 |
| 113.0 | 98.3 | 336.78 | 307.9 | 881.4 | 1189.3 | 0.01784 | 3.9464 |
| 114.0 | 99.3 | 337.43 | 308.6 | 880.9 | 1189.5 | 0.01785 | 3.9136 |
| 115.0 | 100.3 | 338.08 | 309.3 | 880.4 | 1189.6 | 0.01785 | 3.8813 |
| 116.0 | 101.3 | 338.73 | 309.9 | 879.9 | 1189.8 | 0.01786 | 3.8495 |
| 117.0 | 102.3 | 339.37 | 310.6 | 879.3 | 1189.9 | 0.01787 | 3.8183 |
| 118.0 | 103.3 | 340.01 | 311.3 | 878.8 | 1190.1 | 0.01787 | 3.7875 |
| 119.0 | 104.3 | 340.64 | 311.9 | 878.3 | 1190.2 | 0.01788 | 3.7573 |
| 120.0 | 105.3 | 341.27 | 312.6 | 877.8 | 1190.4 | 0.01789 | 3.7275 |
| 121.0 | 106.3 | 341.89 | 313.2 | 877.3 | 1190.5 | 0.01790 | 3.6983 |
| 122.0 | 107.3 | 342.51 | 313.9 | 876.8 | 1190.7 | 0.01790 | 3.6695 |
| 123.0 | 108.3 | 343.13 | 314.5 | 876.3 | 1190.8 | 0.01791 | 3.6411 |
| 124.0 | 109.3 | 343.74 | 315.2 | 875.8 | 1190.9 | 0.01792 | 3.6132 |
| 125.0 | 110.3 | 344.35 | 315.8 | 875.3 | 1191.1 | 0.01792 | 3.5857 |
| 126.0 | 111.3 | 344.95 | 316.4 | 874.8 | 1191.2 | 0.01793 | 3.5586 |
| 127.0 | 112.3 | 345.55 | 317.1 | 874.3 | 1191.3 | 0.01794 | 3.5320 |
| 128.0 | 113.3 | 346.15 | 317.7 | 873.8 | 1191.5 | 0.01794 | 3.5057 |
| 129.0 | 114.3 | 346.74 | 318.3 | 873.3 | 1191.6 | 0.01795 | 3.4799 |
| 130.0 | 115.3 | 347.33 | 319.0 | 872.8 | 1191.7 | 0.01796 | 3.4544 |
| 131.0 | 116.3 | 347.92 | 319.6 | 872.3 | 1191.9 | 0.01797 | 3.4293 |
| 132.0 | 117.3 | 348.50 | 320.2 | 871.8 | 1192.0 | 0.01797 | 3.4046 |
| 133.0 | 118.3 | 349.08 | 320.8 | 871.3 | 1192.1 | 0.01798 | 3.3802 |
| 134.0 | 119.3 | 349.65 | 321.4 | 870.8 | 1192.2 | 0.01799 | 3.3562 |
| 135.0 | 120.3 | 350.23 | 322.0 | 870.4 | 1192.4 | 0.01799 | 3.3325 |
| 136.0 | 121.3 | 350.79 | 322.6 | 869.9 | 1192.5 | 0.01800 | 3.3091 |
| 137.0 | 122.3 | 351.36 | 323.2 | 869.4 | 1192.6 | 0.01801 | 3.2861 |
| 138.0 | 123.3 | 351.92 | 323.8 | 868.9 | 1192.7 | 0.01801 | 3.2634 |
| 139.0 | 124.3 | 352.48 | 324.4 | 868.5 | 1192.8 | 0.01802 | 3.2411 |
| 140.0 | 125.3 | 353.04 | 325.0 | 868.0 | 1193.0 | 0.01803 | 3.2190 |
| 141.0 | 126.3 | 353.59 | 325.5 | 867.5 | 1193.1 | 0.01803 | 3.1972 |
| 142.0 | 127.3 | 354.14 | 326.1 | 867.1 | 1193.2 | 0.01804 | 3.1757 |
| 143.0 | 128.3 | 354.69 | 326.7 | 866.6 | 1193.3 | 0.01805 | 3.1546 |
| 144.0 | 129.3 | 355.23 | 327.3 | 866.2 | 1193.4 | 0.01805 | 3.1337 |
| 145.0 | 130.3 | 355.77 | 327.8 | 865.7 | 1193.5 | 0.01806 | 3.1130 |
| 146.0 | 131.3 | 356.31 | 328.4 | 865.2 | 1193.6 | 0.01806 | 3.0927 |
| 147.0 | 132.3 | 356.84 | 329.0 | 864.8 | 1193.8 | 0.01807 | 3.0726 |
| 148.0 | 133.3 | 357.38 | 329.5 | 864.3 | 1193.9 | 0.01808 | 3.0528 |
| 149.0 | 134.3 | 357.91 | 330.1 | 863.9 | 1194.0 | 0.01808 | 3.0332 |

Table A. 8 (Continued)

| Pressure (psi) |  | Temperature ( $\left.{ }^{\circ} \mathrm{F}\right)$ | Heat of the liquid (Btu/lb) | Latent heat of evaporation (Btu/lb) | Total heat of steam (Btu/lb) | Specific volume |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Absolute | Gage |  |  |  |  | Water (ft ${ }^{3} / \mathrm{lb}$ ) | Steam (ft ${ }^{3} / \mathrm{lb}$ ) |
| 150.0 | 135.3 | 358.43 | 330.6 | 863.4 | 1194.1 | 0.01809 | 3.0139 |
| 152.0 | 137.3 | 359.48 | 331.8 | 862.5 | 1194.3 | 0.01810 | 2.9760 |
| 154.0 | 139.3 | 360.51 | 332.8 | 861.6 | 1194.5 | 0.01812 | 2.9391 |
| 156.0 | 141.3 | 361.53 | 333.9 | 860.8 | 1194.7 | 0.01813 | 2.9031 |
| 158.0 | 143.3 | 362.55 | 335.0 | 859.9 | 1194.9 | 0.01814 | 2.8679 |
| 160.0 | 145.3 | 363.55 | 336.1 | 859.0 | 1195.1 | 0.01815 | 2.8336 |
| 162.0 | 147.3 | 364.54 | 337.1 | 858.2 | 1195.3 | 0.01817 | 2.8001 |
| 164.0 | 149.3 | 365.53 | 338.2 | 857.3 | 1195.5 | 0.01818 | 2.7674 |
| 166.0 | 151.3 | 366.50 | 339.2 | 856.5 | 1195.7 | 0.01819 | 2.7355 |
| 168.0 | 153.3 | 367.47 | 340.2 | 855.6 | 1195.8 | 0.01820 | 2.7043 |
| 170.0 | 155.3 | 368.42 | 341.2 | 854.8 | 1196.0 | 0.01821 | 2.6738 |
| 172.0 | 157.3 | 369.37 | 342.2 | 853.9 | 1196.2 | 0.01823 | 2.6440 |
| 174.0 | 159.3 | 370.31 | 343.2 | 853.1 | 1196.4 | 0.01824 | 2.6149 |
| 176.0 | 161.3 | 371.24 | 344.2 | 852.3 | 1196.5 | 0.01825 | 2.5864 |
| 178.0 | 163.3 | 372.16 | 345.2 | 851.5 | 1196.7 | 0.01826 | 2.5585 |
| 180.0 | 165.3 | 373.08 | 346.2 | 850.7 | 1196.9 | 0.01827 | 2.5312 |
| 182.0 | 167.3 | 373.98 | 347.2 | 849.9 | 1197.0 | 0.01828 | 2.5045 |
| 184.0 | 169.3 | 374.88 | 348.1 | 849.1 | 1197.2 | 0.01830 | 2.4783 |
| 186.0 | 171.3 | 375.77 | 349.1 | 848.3 | 1197.3 | 0.01831 | 2.4527 |
| 188.0 | 173.3 | 376.65 | 350.0 | 847.5 | 1197.5 | 0.01832 | 2.4276 |
| 190.0 | 175.3 | 377.53 | 350.9 | 846.7 | 1197.6 | 0.01833 | 2.4030 |
| 192.0 | 177.3 | 378.40 | 351.9 | 845.9 | 1197.8 | 0.01834 | 2.3790 |
| 194.0 | 179.3 | 379.26 | 352.8 | 845.1 | 1197.9 | 0.01835 | 2.3554 |
| 196.0 | 181.3 | 380.12 | 353.7 | 844.4 | 1198.1 | 0.01836 | 2.3322 |
| 198.0 | 183.3 | 380.96 | 354.6 | 843.6 | 1198.2 | 0.01838 | 2.3095 |
| 200.0 | 185.3 | 381.80 | 355.5 | 842.8 | 1198.3 | 0.01839 | 2.28728 |
| 205.0 | 190.3 | 383.88 | 357.7 | 840.9 | 1198.7 | 0.01841 | 2.23349 |
| 210.0 | 195.3 | 385.91 | 359.9 | 839.1 | 1199.0 | 0.01844 | 2.18217 |
| 215.0 | 200.3 | 387.91 | 362.1 | 837.2 | 1199.3 | 0.01847 | 2.13315 |
| 220.0 | 205.3 | 389.88 | 364.2 | 835.4 | 1199.6 | 0.01850 | 2.08629 |
| 225.0 | 210.3 | 391.80 | 366.2 | 833.6 | 1199.9 | 0.01852 | 2.04143 |
| 230.0 | 215.3 | 393.70 | 368.3 | 831.8 | 1200.1 | 0.01855 | 1.99846 |
| 235.0 | 220.3 | 395.56 | 370.3 | 830.1 | 1200.4 | 0.01857 | 1.95725 |
| 240.0 | 225.3 | 397.39 | 372.3 | 828.4 | 1200.6 | 0.01860 | 1.91769 |
| 245.0 | 230.3 | 399.19 | 374.2 | 826.6 | 1200.9 | 0.01863 | 1.87970 |
| 250.0 | 235.3 | 400.97 | 376.1 | 825.0 | 1201.1 | 0.01865 | 1.84317 |
| 255.0 | 240.3 | 402.72 | 378.0 | 823.3 | 1201.3 | 0.01868 | 1.80802 |
| 260.0 | 245.3 | 404.44 | 379.9 | 821.6 | 1201.5 | 0.01870 | 1.77418 |
| 265.0 | 250.3 | 406.13 | 381.7 | 820.0 | 1201.7 | 0.01873 | 1.74157 |
| 270.0 | 255.3 | 407.80 | 383.6 | 818.3 | 1201.9 | 0.01875 | 1.71013 |
| 275.0 | 260.3 | 409.45 | 385.4 | 816.7 | 1202.1 | 0.01878 | 1.67978 |
| 280.0 | 265.3 | 411.07 | 387.1 | 815.1 | 1202.3 | 0.01880 | 1.65049 |
| 285.0 | 270.3 | 412.67 | 388.9 | 813.6 | 1202.4 | 0.01882 | 1.62218 |
| 290.0 | 275.3 | 414.25 | 390.6 | 812.0 | 1202.6 | 0.01885 | 1.59482 |
| 295.0 | 280.3 | 415.81 | 392.3 | 810.4 | 1202.7 | 0.01887 | 1.56835 |

Table A. 8 (Continued)

| Pressure (psi) |  | Temperature <br> ( ${ }^{\circ} \mathrm{F}$ ) | Heat of the liquid (Btu/lb) | Latent heat of evaporation (Btu/lb) | Total heat of steam (Btu/lb) | Specific volume |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Absolute | Gage |  |  |  |  | Water (ft ${ }^{3} / \mathrm{lb}$ ) | Steam <br> (ft ${ }^{3} / \mathrm{lb}$ ) |
| 300.0 | 285.3 | 417.35 | 394.0 | 808.9 | 1202.9 | 0.01889 | 1.54274 |
| 320.0 | 305.3 | 423.31 | 400.5 | 802.9 | 1203.4 | 0.01899 | 1.44801 |
| 340.0 | 325.3 | 428.99 | 406.8 | 797.0 | 1203.8 | 0.01908 | 1.36405 |
| 360.0 | 345.3 | 434.41 | 412.8 | 791.3 | 1204.1 | 0.01917 | 1.28910 |
| 380.0 | 365.3 | 439.61 | 418.6 | 785.8 | 1204.4 | 0.01925 | 1.22177 |
| 400.0 | 385.3 | 444.60 | 424.2 | 780.4 | 1204.6 | 0.01934 | 1.16095 |
| 420.0 | 405.3 | 449.40 | 429.6 | 775.2 | 1204.7 | 0.01942 | 1.10573 |
| 440.0 | 425.3 | 454.03 | 434.8 | 770.0 | 1204.8 | 0.01950 | 1.05535 |
| 460.0 | 445.3 | 458.50 | 439.8 | 765.0 | 1204.8 | 0.01959 | 1.00921 |
| 480.0 | 465.3 | 462.82 | 444.7 | 760.0 | 1204.8 | 0.01967 | 0.96677 |
| 500.0 | 485.3 | 467.01 | 449.5 | 755.1 | 1204.7 | 0.01975 | 0.92762 |
| 520.0 | 505.3 | 471.07 | 454.2 | 750.4 | 1204.5 | 0.01982 | 0.89137 |
| 540.0 | 525.3 | 475.01 | 458.7 | 745.7 | 1204.4 | 0.01990 | 0.85771 |
| 560.0 | 545.3 | 478.84 | 463.1 | 741.0 | 1204.2 | 0.01998 | 0.82637 |
| 580.0 | 565.3 | 482.57 | 467.5 | 736.5 | 1203.9 | 0.02006 | 0.79712 |
| 600.0 | 585.3 | 486.20 | 471.7 | 732.0 | 1203.7 | 0.02013 | 0.76975 |
| 620.0 | 605.3 | 489.74 | 475.8 | 727.5 | 1203.4 | 0.02021 | 0.74408 |
| 640.0 | 625.3 | 493.19 | 479.9 | 723.1 | 1203.0 | 0.02028 | 0.71995 |
| 660.0 | 645.3 | 496.57 | 483.9 | 718.8 | 1202.7 | 0.02036 | 0.69724 |
| 680.0 | 665.3 | 499.86 | 487.8 | 714.5 | 1202.3 | 0.02043 | 0.67581 |
| 700.0 | 685.3 | 503.08 | 491.6 | 710.2 | 1201.8 | 0.02050 | 0.65556 |
| 720.0 | 705.3 | 506.23 | 495.4 | 706.0 | 1201.4 | 0.02058 | 0.63639 |
| 740.0 | 725.3 | 509.32 | 499.1 | 701.9 | 1200.9 | 0.02065 | 0.61822 |
| 760.0 | 745.3 | 512.34 | 502.7 | 697.7 | 1200.4 | 0.02072 | 0.60097 |
| 780.0 | 765.3 | 515.30 | 506.3 | 693.6 | 1199.9 | 0.02080 | 0.58457 |
| 800.0 | 785.3 | 518.21 | 509.8 | 689.6 | 1199.4 | 0.02087 | 0.56896 |
| 820.0 | 805.3 | 521.06 | 513.3 | 685.5 | 1198.8 | 0.02094 | 0.55408 |
| 840.0 | 825.3 | 523.86 | 516.7 | 681.5 | 1198.2 | 0.02101 | 0.53988 |
| 860.0 | 845.3 | 526.60 | 520.1 | 677.6 | 1197.7 | 0.02109 | 0.52631 |
| 880.0 | 865.3 | 529.30 | 523.4 | 673.6 | 1197.0 | 0.02116 | 0.51333 |
| 900.0 | 885.3 | 531.95 | 526.7 | 669.7 | 1196.4 | 0.02123 | 0.50091 |
| 920.0 | 905.3 | 534.56 | 530.0 | 665.8 | 1195.7 | 0.02130 | 0.48901 |
| 940.0 | 925.3 | 537.13 | 533.2 | 661.9 | 1195.1 | 0.02137 | 0.47759 |
| 960.0 | 945.3 | 539.65 | 536.3 | 658.0 | 1194.4 | 0.02145 | 0.46662 |
| 980.0 | 965.3 | 542.14 | 539.5 | 654.2 | 1193.7 | 0.02152 | 0.45609 |
| 1000.0 | 985.3 | 544.58 | 542.6 | 650.4 | 1192.9 | 0.02159 | 0.44596 |
| 1050.0 | 1035.3 | 550.53 | 550.1 | 640.9 | 1191.0 | 0.02177 | 0.42224 |
| 1100.0 | 1085.3 | 556.28 | 557.5 | 631.5 | 1189.1 | 0.02195 | 0.40058 |
| 1150.0 | 1135.3 | 561.82 | 564.8 | 622.2 | 1187.0 | 0.02214 | 0.38073 |
| 1200.0 | 1185.3 | 567.19 | 571.9 | 613.0 | 1184.8 | 0.02232 | 0.36245 |
| 1250.0 | 1235.3 | 572.38 | 578.8 | 603.8 | 1182.6 | 0.02250 | 0.34556 |
| 1300.0 | 1285.3 | 577.42 | 585.6 | 594.6 | 1180.2 | 0.02269 | 0.32991 |
| 1350.0 | 1335.3 | 582.32 | 592.2 | 585.6 | 1177.8 | 0.02288 | 0.31536 |
| 1400.0 | 1385.3 | 587.07 | 598.8 | 567.5 | 1175.3 | 0.02307 | 0.30178 |
| 1450.0 | 1435.3 | 591.70 | 605.3 | 567.6 | 1172.9 | 0.02327 | 0.28909 |

## Table A. 8 (Continued)

| Pressure (psi) |  | Temperature ( ${ }^{\circ} \mathrm{F}$ ) | Heat of the liquid (Btu/lb) | Latent heat of evaporation (Btu/lb) | Total heat of steam (Btu/lb) | Specific volume |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Absolute | Gage |  |  |  |  | Water (ft $\left.{ }^{3} / \mathrm{lb}\right)$ | Steam (ft $\left.{ }^{3} / \mathrm{lb}\right)$ |
| 1500.0 | 1485.3 | 596.20 | 611.7 | 558.4 | 1170.1 | 0.02346 | 0.27719 |
| 1600.0 | 1585.3 | 604.87 | 624.2 | 540.3 | 1164.5 | 0.02387 | 0.25545 |
| 1700.0 | 1685.3 | 613.13 | 636.5 | 522.2 | 1158.6 | 0.02428 | 0.23607 |
| 1800.0 | 1785.3 | 621.02 | 648.5 | 503.8 | 1152.3 | 0.02472 | 0.21861 |
| 1900.0 | 1885.3 | 628.56 | 660.4 | 485.2 | 1145.6 | 0.02517 | 0.20278 |
| 2000.0 | 1985.3 | 635.80 | 672.1 | 466.2 | 1138.3 | 0.02565 | 0.18831 |
| 2100.0 | 2085.3 | 642.76 | 683.8 | 446.7 | 1130.5 | 0.02615 | 0.17501 |
| 2200.0 | 2185.3 | 649.45 | 695.5 | 426.7 | 1122.2 | 0.02669 | 0.16272 |
| 2300.0 | 2285.3 | 655.89 | 707.2 | 406.0 | 1113.2 | 0.02727 | 0.15133 |
| 2400.0 | 2385.3 | 662.11 | 719.0 | 384.8 | 1103.7 | 0.02790 | 0.14076 |
| 2500.0 | 2485.3 | 668.11 | 731.7 | 361.6 | 1093.3 | 0.02859 | 0.13068 |
| 2600.0 | 2585.3 | 673.91 | 744.5 | 337.6 | 1082.0 | 0.02938 | 0.12110 |
| 2700.0 | 2685.3 | 679.53 | 757.3 | 312.3 | 1069.7 | 0.03029 | 0.11194 |
| 2800.0 | 2785.3 | 684.96 | 770.7 | 285.1 | 1055.8 | 0.03134 | 0.10305 |
| 2900.0 | 2885.3 | 690.22 | 785.1 | 254.7 | 1039.8 | 0.03262 | 0.09420 |
| 3000.0 | 2985.3 | 695.33 | 801.8 | 218.4 | 1020.3 | 0.03428 | 0.08500 |
| 3100.0 | 3085.3 | 700.28 | 824.0 | 169.3 | 993.3 | 0.03681 | 0.07452 |
| 3200.0 | 3185.3 | 705.08 | 875.5 | 56.1 | 931.6 | 0.04472 | 0.05663 |
| 3208.2 | 3193.5 | 705.47 | 906.0 | 0.0 | 906.0 | 0.05078 | 0.05078 |

[^7]Table A. 9 Viscosities of Steam and Water: English Units

| Temperature$\left({ }^{\circ} \mathrm{F}\right)$ | Viscosity of steam and water in centipoise |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 psia | $2$ <br> psia | 5 psia | $\begin{aligned} & 10 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 20 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 50 \\ & \mathrm{psia} \end{aligned}$ | $\begin{aligned} & 100 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 200 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 500 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 1000 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 2000 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 5000 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 7500 \\ & \text { psia } \end{aligned}$ | 10000 psia | 12000 psia |
| Saturated water | 0.667 | 0.524 | 0.388 | 0.313 | 0.255 | 0.197 | 0.164 | 0.138 | 0.111 | 0.094 | 0.078 |  |  |  | $\ldots$ |
| Saturated steam | 0.010 | 0.010 | 0.011 | 0.012 | 0.012 | 0.013 | 0.014 | 0.015 | 0.017 | 0.019 | 0.023 |  |  |  |  |
| $1500^{\circ}$ | 0.041 | 0.041 | 0.041 | 0.041 | 0.041 | 0.041 | 0.041 | 0.041 | 0.042 | 0.042 | 0.042 | 0.044 | 0.046 | 0.048 | 0.050 |
| 1450 | 0.040 | 0.040 | 0.040 | 0.040 | 0.040 | 0.040 | 0.040 | 0.040 | 0.040 | 0.041 | 0.041 | 0.043 | 0.045 | 0.047 | 0.049 |
| 1400 | 0.039 | 0.039 | 0.039 | 0.039 | 0.039 | 0.039 | 0.039 | 0.039 | 0.039 | 0.040 | 0.040 | 0.042 | 0.044 | 0.047 | 0.049 |
| 1350 | 0.038 | 0.038 | 0.038 | 0.038 | 0.038 | 0.038 | 0.038 | 0.038 | 0.038 | 0.038 | 0.039 | 0.041 | 0.044 | 0.046 | 0.049 |
| 1300 | 0.037 | 0.037 | 0.037 | 0.037 | 0.037 | 0.037 | 0.037 | 0.037 | 0.037 | 0.037 | 0.038 | 0.040 | 0.043 | 0.045 | 0.048 |
| 1250 | 0.035 | 0.035 | 0.035 | 0.035 | 0.035 | 0.035 | 0.035 | 0.036 | 0.036 | 0.036 | 0.037 | 0.039 | 0.042 | 0.045 | 0.048 |
| 1200 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.035 | 0.035 | 0.036 | 0.038 | 0.041 | 0.045 | 0.048 |
| 1150 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.034 | 0.037 | 0.041 | 0.045 | 0.049 |
| 1100 | 0.032 | 0.032 | 0.032 | 0.032 | 0.032 | 0.032 | 0.032 | 0.032 | 0.033 | 0.033 | 0.034 | 0.037 | 0.040 | 0.045 | 0.050 |
| 1050 | 0.031 | 0.031 | 0.031 | 0.031 | 0.031 | 0.031 | 0.031 | 0.031 | 0.032 | 0.032 | 0.033 | 0.036 | 0.040 | 0.047 | 0.052 |
| 1000 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.031 | 0.032 | 0.035 | 0.041 | 0.049 | 0.055 |
| 950 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.030 | 0.031 | 0.035 | 0.042 | 0.052 | 0.059 |
| 900 | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0.029 | 0.035 | 0.045 | 0.057 | 0.064 |
| 850 | 0.026 | 0.026 | 0.026 | 0.026 | 0.026 | 0.026 | 0.027 | 0.027 | 0.027 | 0.027 | 0.028 | 0.035 | 0.052 | 0.064 | 0.070 |
| 800 | 0.025 | 0.025 | 0.025 | 0.025 | 0.025 | 0.025 | 0.025 | 0.025 | 0.026 | 0.026 | 0.027 | 0.040 | 0.062 | 0.071 | 0.075 |
| 750 | 0.024 | 0.024 | 0.024 | 0.024 | 0.024 | 0.024 | 0.024 | 0.024 | 0.025 | 0.025 | 0.026 | 0.057 | 0.071 | 0.078 | 0.081 |
| 700 | 0.023 | 0.023 | 0.023 | 0.023 | 0.023 | 0.023 | 0.023 | 0.023 | 0.023 | 0.024 | $0.026{ }^{\circ}$ | 0.071 | 0.079 | 0.085 | 0.086 |
| 650 | 0.022 | 0.022 | 0.022 | 0.022 | 0.022 | 0.022 | 0.022 | 0.022 | 0.023 | 0.023 | $\underline{0.023}$ | 0.082 | 0.088 | 0.092 | 0.096 |
| 600 | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0.087 | 0.091 | 0.096 | 0.101 | 0.104 |
| 550 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | $\underline{0.019}$ | 0.095 | 0.101 | 0.105 | 0.109 | 0.113 |
| 500 | 0.019 | 0.019 | 0.019 | 0.019 | 0.019 | 0.019 | 0.019 | 0.018 | $\underline{0.018}$ | 0.103 | 0.105 | 0.111 | 0.114 | 0.119 | 0.122 |
| 450 | 0.018 | 0.018 | 0.018 | 0.018 | 0.017 | 0.017 | 0.017 | 0.017 | 0.115 | 0.116 | 0.118 | 0.123 | 0.127 | 0.131 | 0.135 |
| 400 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | $\underline{0.016}$ | 0.131 | 0.132 | 0.134 | 0.138 | 0.143 | 0.147 | 0.150 |
| 350 | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 | $\underline{0.015}$ | 0.152 | 0.153 | 0.154 | 0.155 | 0.160 | 0.164 | 0.168 | 0.171 |
| 300 | 0.014 | 0.014 | 0.014 | 0.014 | 0.014 | $\underline{0.014}$ | 0.182 | 0.183 | 0.183 | 0.184 | 0.185 | 0.190 | 0.194 | 0.198 | 0.201 |
| 250 | 0.013 | 0.013 | 0.013 | 0.013 | $\underline{0.013}$ | 0.228 | 0.228 | 0.228 | 0.228 | 0.229 | 0.231 | 0.235 | 0.238 | 0.242 | 0.245 |
| 200 | 0.012 | 0.012 | $\underline{0.012}$ | $\underline{0.012}$ | 0.300 | 0.300 | 0.300 | 0.300 | 0.301 | 0.301 | 0.303 | 0.306 | 0.310 | 0.313 | 0.316 |
| 150 | 0.011 | $\underline{0.011}$ | 0.427 | 0.427 | 0.427 | 0.427 | 0.427 | 0.427 | 0.427 | 0.428 | 0.429 | 0.431 | 0.434 | 0.437 | 0.439 |
| 100 | 0.680 | 0.680 | 0.680 | 0.680 | 0.680 | 0.680 | 0.680 | 0.680 | 0.680 | 0.680 | 0.680 | 0.681 | 0.682 | 0.683 | 0.683 |
| 50 | 1.299 | 1.299 | 1.299 | 1.299 | 1.299 | 1.299 | 1.299 | 1.299 | 1.299 | 1.298 | 1.296 | 1.289 | 1.284 | 1.279 | 1.275 |
| 32 | 1.753 | 1.753 | 1.753 | 1.753 | 1.753 | 1.753 | 1.753 | 1.752 | 1.751 | 1.749 | 1.745 | 1.733 | 1.723 | 1.713 | 1.705 |

$\bigcirc$ Values directly below underscored viscosities are for water.
${ }^{\odot}$ Critical point.
Source: Ref. [8].

Table A. 10 Properties of Carbon Dioxide at One Atmosphere

| $T$ |  | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \beta \times 10^{3} \\ & (1 / \mathrm{K}) \end{aligned}$ | $C_{P}$ <br> ( $\mathrm{J} / \mathrm{kg} \cdot \mathrm{K}$ ) | $k$ | $\begin{aligned} & \alpha \times 10^{4} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | $\begin{aligned} & \mu \times 10^{6} \\ & \left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right) \end{aligned}$ | $\begin{aligned} & v \times 10^{6} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | Pr | $\begin{aligned} & g \beta / v^{2} \times 10^{-6} \\ & \left(1 / \mathrm{K} \cdot \mathrm{~m}^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | (W/m•K) |  |  |  |  |  |
| 220 | -53 | 2.4733 | - | 783 | 0.010805 | 0.0558 | 11.105 | 4.490 | 0.818 | - |
| 250 | -23 | 2.1657 | - | 804 | 0.012884 | 0.0740 | 12.590 | 5.813 | 0.793 | - |
| 300 | 27 | 1.7973 | 3.33 | 871 | 0.016572 | 0.1059 | 14.958 | 8.321 | 0.770 | 472 |
| 350 | 77 | 1.5362 | 2.86 | 900 | 0.02047 | 0.1481 | 17.205 | 11.19 | 0.755 | 224 |
| 400 | 127 | 1.3424 | 2.50 | 942 | 0.02461 | 0.1946 | 19.32 | 14.39 | 0.738 | 118 |
| 450 | 177 | 1.1918 | 2.22 | 980 | 0.02897 | 0.2480 | 21.34 | 17.90 | 0.721 | 67.9 |
| 500 | 227 | 1.0732 | 2.00 | 1013 | 0.03352 | 0.3083 | 23.26 | 21.67 | 0.702 | 41.8 |
| 550 | 277 | 0.9739 | 1.82 | 1047 | 0.03821 | 0.3747 | 25.08 | 25.74 | 0.685 | 26.9 |
| 600 | 327 | 0.8938 | 1.67 | 1076 | 0.04311 | 0.4483 | 26.83 | 30.02 | 0.668 | 18.2 |

Source: Refs. [1] and [2].

Table A. 11 Properties of Ammonia Vapor at Atmospheric Pressure

| $T$ <br> $(\mathrm{~K})$ | $\rho$ <br> $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$ | $C_{P}$ <br> $(\mathrm{~J} / \mathrm{kg} \cdot \mathrm{K})$ | $\mu \times 10^{7}$ <br> $\left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right)$ | $\nu \times 10^{6}$ <br> $\left(\mathrm{~m}^{2} / \mathrm{s}\right)$ | $k \times 10^{3}$ <br> $(\mathrm{~W} / \mathrm{m} \cdot \mathrm{K})$ | $\alpha \times 10^{6}$ <br> $\left(\mathrm{~m}^{2} / \mathrm{s}\right)$ | $P r$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 300 | 0.6894 | 2158 | 101.5 | 14.7 | 24.7 | 16.6 | 0.887 |
| 320 | 0.6448 | 2170 | 109 | 16.9 | 27.2 | 19.4 | 0.870 |
| 340 | 0.6059 | 2192 | 116.5 | 19.2 | 29.3 | 22.1 | 0.872 |
| 360 | 0.5716 | 2221 | 124 | 21.7 | 31.6 | 24.9 | 0.872 |
| 380 | 0.5410 | 2254 | 131 | 24.2 | 34.0 | 27.9 | 0.869 |
| 400 | 0.5136 | 2287 | 138 | 26.9 | 37.0 | 31.5 | 0.853 |
| 420 | 0.4888 | 2322 | 145 | 29.7 | 40.4 | 35.6 | 0.833 |
| 440 | 0.4664 | 2357 | 152.5 | 32.7 | 43.5 | 39.6 | 0.826 |
| 460 | 0.4460 | 2393 | 159 | 35.7 | 46.3 | 43.4 | 0.822 |
| 480 | 0.4273 | 2430 | 166.5 | 39.0 | 49.2 | 47.4 | 0.822 |
| 500 | 0.4101 | 2467 | 173 | 42.2 | 52.5 | 51.9 | 0.813 |
| 520 | 0.3942 | 2504 | 180 | 45.7 | 54.5 | 55.2 | 0.827 |
| 540 | 0.3795 | 2540 | 186.5 | 49.1 | 57.5 | 59.7 | 0.824 |
| 560 | 0.3708 | 2577 | 193 | 52.0 | 60.6 | 63.4 | 0.827 |
| 580 | 0.3533 | 2613 | 199.5 | 56.5 | 63.8 | 69.1 | 0.817 |

[^8]Table A. 12 Properties of Saturated Liquid Freon $12\left(\mathrm{CCl}_{2} \mathrm{~F}_{2}\right)$

| $T$ |  | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \beta \times 10^{3} \\ & (1 / \mathrm{K}) \end{aligned}$ | $C_{P}$ <br> (J/kg $\cdot \mathrm{K}$ ) | $\begin{aligned} & k \\ & (\mathrm{~W} / \mathrm{m} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{aligned} & \alpha \times 10^{8} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | $\begin{aligned} & \mu \times 10^{4} \\ & \left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right) \end{aligned}$ | $\begin{aligned} & \nu \times 10^{6} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | Pr | $\begin{aligned} & g \beta / v^{2} \times 10^{-10} \\ & \left(1 / \mathrm{K} \cdot \mathrm{~m}^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\left({ }^{\circ} \mathrm{C}\right)$ |  |  |  |  |  |  |  |  |  |
| 223 | -50 | 1547 | 2.63 | 875.0 | 0.067 | 5.01 | 4.796 | 0.310 | 6.2 | 26.84 |
| 233 | -40 | 1519 |  | 884.7 | 0.069 | 5.14 | 4.238 | 0.279 | 5.4 |  |
| 243 | -30 | 1490 |  | 895.6 | 0.069 | 5.26 | 3.770 | 0.253 | 4.8 |  |
| 253 | -20 | 1461 |  | 907.3 | 0.071 | 5.39 | 3.433 | 0.235 | 4.4 |  |
| 263 | -10 | 1429 |  | 920.3 | 0.073 | 5.50 | 3.158 | 0.221 | 4.0 |  |
| 273 | 0 | 1397 | 3.10 | 934.5 | 0.073 | 5.57 | 2.990 | 0.214 | 3.8 | 6.68 |
| 283 | 10 | 1364 |  | 949.6 | 0.073 | 5.60 | 2.769 | 0.203 | 3.6 |  |
| 293 | 20 | 1330 |  | 965.9 | 0.073 | 5.60 | 2.633 | 0.198 | 3.5 |  |
| 303 | 30 | 1295 |  | 983.5 | 0.071 | 5.60 | 2.512 | 0.194 | 3.5 |  |
| 313 | 40 | 1257 |  | 1001.9 | 0.069 | 5.55 | 2.401 | 0.191 | 3.5 |  |
| 323 | 50 | 1216 |  | 1021.6 | 0.067 | 5.45 | 2.310 | 0.190 | 3.5 |  |

[^9]Table A.13 Properties of Selected Organic Liquids at $20^{\circ} \mathrm{C}$

| Liquid | Chemical formula | $\begin{aligned} & \rho \\ & \left(\mathrm{kg} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \beta \times 10^{4} \\ & (1 / \mathrm{K}) \end{aligned}$ | $\begin{aligned} & C_{P} \\ & (\mathrm{~J} / \mathrm{kg} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{aligned} & k \\ & (\mathrm{~W} / \mathrm{m} \cdot \mathrm{~K}) \end{aligned}$ | $\begin{gathered} \alpha \times 10^{9} \\ \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{gathered}$ | $\begin{aligned} & \mu \times 10^{4} \\ & \left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right) \end{aligned}$ | $\begin{aligned} & v \times 10^{6} \\ & \left(\mathrm{~m}^{2} / \mathrm{s}\right) \end{aligned}$ | Pr | $\begin{aligned} & g \beta / v^{2} \times 10^{-8} \\ & \left(1 / \mathrm{K} \cdot \mathrm{~m}^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Acetic acid | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}_{2}$ | 1049 | 10.7 | 2031 | 0.193 | 90.6 | - | - | - | - |
| Acetone | $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}$ | 791 | 14.3 | 2160 | 0.180 | 105.4 | 3.31 | 0.418 | 3.97 | 802.6 |
| Aniline | $\mathrm{C}_{6} \mathrm{H}_{7} \mathrm{~N}$ | 1022 | 8.5 | 2064 | 0.172 | 81.5 | 44.3 | 4.34 | 53.16 | 4.43 |
| Benzene | $\mathrm{C}_{6} \mathrm{H}_{6}$ | 879 | 10.6 | 1738 | 0.154 | 100.8 | 6.5 | 0.739 | 7.34 | 190.3 |
| $n$-Butyl alcohol | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ | 810 | 8.1 | 2366 | 0.167 | 87.1 | 29.5 | 3.64 | 41.79 | 5.99 |
| Chloroform | $\mathrm{CHCl}_{3}$ | 1489 | 12.8 | 967 | 0.129 | 89.6 | 5.8 | 0.390 | 4.35 | 825.3 |
| Ethyl acetate | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$ | 900 | 13.8 | 2010 | 0.137 | 75.7 | 4.49 | 0.499 | 6.59 | 543.5 |
| Ethyl alcohol | $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$ | 790 | 11.0 | 2470 | 0.182 | 93.3 | 12.0 | 1.52 | 16.29 | 46.7 |
| Ethylene glycol | $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}$ | 1115 | - | 2382 | 0.258 | 97.1 | 199 | 17.8 | 183.7 |  |
| Glycerine | $\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}_{3}$ | 1260 | 5.0 | 2428 | 0.285 | 93.2 | 14,800 | 1175 | 12,609 | 0.0000355 |
| $n$-Heptane | $\mathrm{C}_{7} \mathrm{H}_{14}$ | 684 | 12.4 | 2219 | 0.140 | 92.2 | 4.09 | 0.598 | 6.48 | 340.1 |
| $n$-Hexane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 660 | 13.5 | 1884 | 0.137 | 110.2 | 3.20 | 0.485 | 4.40 | 562.8 |
| Isobutyl alcohol | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ | 804 | 9.4 | 2303 | 0.134 | 72.4 | 39.5 | 4.91 | 67.89 | 3.82 |
| Methyl alcohol | $\mathrm{CH}_{4} \mathrm{O}$ | 792 | 11.9 | 2470 | 0.212 | 108.4 | 5.84 | 0.737 | 6.8 | 214.9 |
| n-Octane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 720 | 11.4 | 2177 | 0.147 | 93.8 | 5.4 | 0.750 | 8.00 | 198.8 |
| n-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 626 | 16.0 | 2177 | 0.136 | 99.8 | 2.29 | 0.366 | 3.67 | 1171 |
| Toluene | $\mathrm{C}_{7} \mathrm{H}_{8}$ | 866 | 10.8 | 1675 | 0.151 | 104.1 | 5.86 | 0.677 | 6.5 | 231.1 |
| Turpentine | $\mathrm{C}_{10} \mathrm{H}_{16}$ | 855 | 9.7 | 1800 | 0.128 | 83.2 | 14.87 | 1.74 | 20.91 | 31.4 |

Source: Refs. [1] and [3].

## Table A. 14 Properties of Selected Saturated Liquids

| $T$ | $\rho$ | $C_{P}$ | $\mu \times 10^{2}$ | $v \times 10^{6}$ | $k \times 10^{3}$ | $\alpha \times 10^{7}$ | $\operatorname{Pr}$ | $\beta \times 10^{3}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $(\mathrm{~K})$ | $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$ | $(\mathrm{kJ} / \mathrm{kg} \cdot \mathrm{K})$ | $\left(\mathrm{N} \cdot \mathrm{s} / \mathrm{m}^{2}\right)$ | $\left(\mathrm{m}^{2} / \mathrm{s}\right)$ | $(\mathrm{W} / \mathrm{m} \cdot \mathrm{K})$ | $\left(\mathrm{m}^{2} / \mathrm{s}\right)$ | $\left(\mathrm{K}^{-1}\right)$ |  |


| Engine oil (unused) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 273 | 899.1 | 1.796 | 385 | 4280 | 147 | 0.910 | 47,000 | 0.70 |
| 280 | 895.3 | 1.827 | 217 | 2430 | 144 | 0.880 | 27,500 | 0.70 |
| 290 | 890.0 | 1.868 | 99.9 | 1120 | 145 | 0.872 | 12,900 | 0.70 |
| 300 | 884.1 | 1.909 | 48.6 | 550 | 145 | 0.859 | 6400 | 0.70 |
| 310 | 877.9 | 1.951 | 25.3 | 288 | 145 | 0.847 | 3400 | 0.70 |
| 320 | 871.8 | 1.993 | 14.1 | 161 | 143 | 0.823 | 1965 | 0.70 |
| 330 | 865.8 | 2.035 | 8.36 | 96.6 | 141 | 0.800 | 1205 | 0.70 |
| 340 | 859.9 | 2.076 | 5.31 | 61.7 | 139 | 0.779 | 793 | 0.70 |
| 350 | 853.9 | 2.118 | 3.56 | 41.7 | 138 | 0.763 | 546 | 0.70 |
| 360 | 847.8 | 2.161 | 2.52 | 29.7 | 138 | 0.753 | 395 | 0.70 |
| 370 | 841.8 | 2.206 | 1.86 | 22.0 | 137 | 0.738 | 300 | 0.70 |
| 380 | 836.0 | 2.250 | 1.41 | 16.9 | 136 | 0.723 | 233 | 0.70 |
| 390 | 830.6 | 2.294 | 1.10 | 13.3 | 135 | 0.709 | 187 | 0.70 |
| 400 | 825.1 | 2.337 | 0.874 | 10.6 | 134 | 0.695 | 152 | 0.70 |
| 410 | 818.9 | 2.381 | 0.698 | 8.52 | 133 | 0.682 | 125 | 0.70 |
| 420 | 812.1 | 2.427 | 0.564 | 6.94 | 133 | 0.675 | 103 | 0.70 |
| 430 | 806.5 | 2.471 | 0.470 | 5.83 | 132 | 0.662 | 88 | 0.70 |

Ethylene glycol $\left[\mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{OH})_{2}\right]$

| 273 | 1130.8 | 2.294 | 6.51 | 57.6 | 242 | 0.933 | 617 | 0.65 |
| :--- | :--- | :--- | :--- | :---: | :--- | :---: | :--- | :--- |
| 280 | 1125.8 | 2.323 | 4.20 | 37.3 | 244 | 0.933 | 400 | 0.65 |
| 290 | 1118.8 | 2.368 | 2.47 | 22.1 | 248 | 0.936 | 236 | 0.65 |
| 300 | 1114.4 | 2.415 | 1.57 | 14.1 | 252 | 0.939 | 151 | 0.65 |
| 310 | 1103.7 | 2.460 | 1.07 | 9.65 | 255 | 0.939 | 103 | 0.65 |
| 320 | 1096.2 | 2.505 | 0.757 | 6.91 | 258 | 0.940 | 73.5 | 0.65 |
| 330 | 1089.5 | 2.549 | 0.561 | 5.15 | 260 | 0.936 | 55.0 | 0.65 |
| 340 | 1083.8 | 2.592 | 0.431 | 3.98 | 261 | 0.929 | 42.8 | 0.65 |
| 350 | 1079.0 | 2.637 | 0.342 | 3.17 | 261 | 0.917 | 34.6 | 0.65 |
| 360 | 1074.0 | 2.682 | 0.278 | 2.59 | 261 | 0.906 | 28.6 | 0.65 |
| 370 | 1066.7 | 2.728 | 0.228 | 2.14 | 262 | 0.900 | 23.7 | 0.65 |
| 373 | 1058.5 | 2.742 | 0.215 | 2.03 | 263 | 0.906 | 22.4 | 0.65 |

## Glycerin $\left[\mathrm{C}_{3} \mathrm{H}_{5}(\mathrm{OH})_{3}\right]$

| 273 | 1276.0 | 2.261 | 1060 | 8310 | 282 | 0.977 | 85,000 | 0.47 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 280 | 1271.9 | 2.298 | 534 | 4200 | 284 | 0.972 | 43,200 | 0.47 |
| 290 | 1265.8 | 2.367 | 185 | 1460 | 286 | 0.955 | 15,300 | 0.48 |
| 300 | 1259.9 | 2.427 | 79.9 | 634 | 286 | 0.935 | 6780 | 0.48 |
| 310 | 1253.9 | 2.490 | 35.2 | 281 | 286 | 0.916 | 3060 | 0.49 |
| 320 | 1247.2 | 2.564 | 21.0 | 168 | 287 | 0.897 | 1870 | 0.50 |

[^10]Table A. 15 Thermal Conductivities of Liquids

| Liquid | $T\left({ }^{\circ} \mathrm{F}\right)$ | $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | Liquid | $T\left({ }^{\circ} \mathrm{F}\right)$ | $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Acetic acid 100\% | 68 | 0.099 | Ethyl alcohol 40\% | 68 | 0.224 |
| Acetic acid 50\% | 68 | 0.20 | Ethyl alcohol 20\% | 68 | 0.281 |
| Acetone | 86 | 0.102 | Ethyl alcohol 100\% | 122 | 0.087 |
|  | 167 | 0.095 | Ethyl benzene | 86 | 0.086 |
| Allyl alcohol | 77-86 | 0.104 |  | 140 | 0.082 |
| Ammonia | 5-86 | 0.29 | Ethyl bromide | 68 | 0.070 |
| Ammonia, aqueous 26\% | 68 | 0.261 | Ethyl ether | 86 | 0.080 |
|  | 140 | 0.29 |  | 167 | 0.078 |
| Amyl acetate | 50 | 0.083 | Ethyl iodide | 104 | 0.064 |
| Amyl alcohol ( $n$-) | 86 | 0.094 |  | 167 | 0.063 |
|  | 212 | 0.089 | Ethylene glycol | 32 | 0.153 |
| Amyl alcohol (iso-) | 86 | 0.088 | Gasoline | 86 | 0.078 |
|  | 167 | 0.087 | Glycerol 100\% | 68 | 0.164 |
| Aniline | 32-68 | 0.100 | Glycerol 80\% | 68 | 0.189 |
| Benzene | 86 | 0.092 | Glycerol 60\% | 68 | 0.220 |
|  | 140 | 0.087 | Glycerol 40\% | 68 | 0.259 |
| Bromobenzene | 86 | 0.074 | Glycerol 20\% | 68 | 0.278 |
|  | 212 | 0.070 | Glycerol 100\% | 212 | 0.164 |
| Butyl acetate ( $n$-) | 77-86 | 0.085 | Heptane ( $n$-) | 86 | 0.081 |
| Butyl alcohol ( $n$-) | 86 | 0.097 | Heptane ( $n$ - | 140 | 0.079 |
|  | 167 | 0.095 | Hexane ( $n$-) | 86 | 0.080 |
| Butyl alcohol (iso-) | 50 | 0.091 |  | 140 | 0.078 |
| Calcium chloride brine 30\% |  |  | Heptyl alcohol (n-) | 86 | 0.094 |
|  | 86 | 0.32 |  | 167 | 0.091 |
| 15\% | 86 | 0.34 | Hexyl alcohol (n-) | 86 | 0.093 |
| Carbon disulfide | 86 | 0.093 |  | 167 | 0.090 |
|  | 167 | 0.088 | Kerosene | 68 | 0.086 |
| Carbon tetrachloride | 32 | 0.107 |  | 167 | 0.081 |
|  | 154 | 0.094 |  |  |  |
| Chlorobenzene | 50 | 0.083 | Mercury | 82 | 4.83 |
| Chloroform | 86 | 0.080 | Methyl alcohol 100\% | 68 | 0.124 |
| Cymene (para-) | 86 | 0.078 | Methyl alcohol 80\% | 68 | 0.154 |
|  | 140 | 0.079 | Methyl alcohol 60\% | 68 | 0.190 |
| Decane ( $n$-) | 86 | 0.085 | Methyl alcohol 40\% | 68 | 0.234 |
|  | 140 | 0.083 | Methyl alcohol 20\% | 68 | 0.284 |
|  |  |  | Methyl alcohol 100\% | 122 | 0.114 |
| Dichlorodifluoromethane | 20 | 0.057 | Methyl alcohol chloride | 5 | 0.111 |
|  | 60 | 0.053 |  | 86 | 0.089 |
|  | 100 | 0.048 | Nitrobenzene | 86 | 0.095 |
|  | 140 | 0.043 |  | 212 | 0.038 |
|  | 180 | 0.038 | Nitromethane | 86 | 0.125 |
| Dichloroethane | 122 | 0.082 |  | 140 | 0.120 |
| Dichloromethane | 5 | 0.111 | Nonane ( $n$-) | 86 | 0.084 |
|  | 86 | 0.096 |  | 140 | 0.082 |
| Ethyl acetate | 68 | 0.101 | Octane ( $n$-) | 86 | 0.083 |
| Ethyl alcohol 100\% | 68 | 0.105 |  | 140 | 0.081 |
| Ethyl alcohol 80\% | 68 | 0.137 |  |  |  |
| Ethyl alcohol 60\% | 68 | 0.176 |  |  |  |

## Table A. 15 (Continued)

| Liquid | $T\left({ }^{\circ} \mathrm{F}\right)$ | $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | Liquid | $T\left({ }^{\circ} \mathrm{F}\right)$ | $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Oils | 86 | 0.079 | Sulfuric acid 90\% | 86 | 0.21 |
| Oils, castor | 68 | 0.104 | Sulfuric acid 60\% | 86 | 0.25 |
|  | 212 | 0.100 | Sulfuric acid 30\% | 86 | 0.30 |
| Oils, Olive | 68 | 0.097 | Sulfur dioxide | 5 | 0.128 |
|  | 212 | 0.095 |  | 86 | 0.111 |
| Paraldehyde | 86 | 0.084 | Toluene | 86 | 0.086 |
|  | 212 | 0.078 |  | 167 | 0.084 |
| Pentane ( $n$-) | 86 | 0.078 | $\beta$-Trichloroethane | 122 | 0.077 |
|  | 167 | 0.074 | Trichloroethylene | 122 | 0.080 |
| Perchloroethylene | 122 | 0.092 | Turpentine | 59 | 0.074 |
| Petroleum ether | 86 | 0.075 | Vaseline | 59 | 0.106 |
|  | 167 | 0.073 |  | 59 | 0.106 |
| Propyl alcohol ( $n$ - | 86 | 0.099 | Water | 32 | 0.343 |
|  | 167 | 0.095 |  | 100 | 0.363 |
| Propyl alcohol (iso-) | 86 | 0.091 |  | 200 | 0.393 |
|  | 140 | 0.090 |  | 300 | 0.395 |
| Sodium | 212 | 49 |  | 420 | 0.376 |
|  | 410 | 46 |  | 620 | 0.275 |
| Sodium chloride brine 25.0\% |  |  | Xylene (ortho-) | 68 | 0.090 |
|  | 86 | 0.33 | Xylene (meta-) | 68 | 0.090 |
| 12.5\% | 86 | 0.34 |  |  |  |

Source: Ref. [11].

## Table A. 16 Thermal Conductivities of Tubing Materials

| Material | $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | Material | $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ |
| :--- | :--- | :--- | :--- |
| Carbon steel | $24-30$ | Inconel 800 | $6.7-8$ |
| 304 Stainless steel | $8.6-12$ | Inconel 825 | 7.2 |
| 309 Stainless steel | 29 | Hastelloy B | $6.1-9$ |
| 310 Stainless steel | $7.3-11$ | Hastelloy C | $5.9-10$ |
| 316 and 317 Stainless steel | $7.7-12$ | Alloy 904L | $7.5-9$ |
| 321 and 347 Stainless steel | $8-12$ | Alloy 28 | $6.5-9$ |
| 25Cr-12Ni Steel | $6.5-10$ | Cr-Mo Alloy XM-27 | 11.3 |
| 22Cr-5Ni-3Mo Steel | 9.5 | Alloy 20CB | 7.6 |
| 3.5Ni Steel | 23.5 | Copper | 225 |
| Carbon-0.5Mo Steel | 25 | $90-10 \mathrm{Cu}-\mathrm{Ni}$ | 30 |
| 1.0 \& 1.25Cr-0.5Mo Steel | 21.5 | $70-30 \mathrm{Cu}-\mathrm{Ni}$ |  |
| 2.25Cr-1.0Mo Steel | 21 | Admirality brass | 18 |
| 5Cr-0.5Mo Steel | $16.9-19$ | Naval brass | $64-75$ |
| 12Cr \& 13Cr Steel | 15.3 | Muntz metal (60Cu-40Zn) | $71-74$ |
| 15Cr Steel | 14.4 | Aluminum bronze | 71 |
| 17Cr Steel | 13 | Al-Ni Bronze | 71 |
| Nickel alloy 200 | 38.5 | Aluminum alloy 3003 | 72 |
| Nickel alloy 400 | $12.6-15$ | Aluminum alloy 6061 | $102-106$ |
| Inconel 600 | $95-9$ | Titanium | $96-102$ |
| Inconel 625 | $7.5-12.5$ |  |  |

This table lists typical values of thermal conductivity that can be used to estimate the thermal resistance of tube and pipe walls. These values may not be appropriate for operation at very high or very low temperatures.

Table A. 17 Latent Heats of Vaporization of Organic Compounds

|  | Formula | Temperature ( ${ }^{\circ} \mathrm{C}$ ) | $\lambda$ (cal./g) |
| :---: | :---: | :---: | :---: |
| Hydrocarbon compounds |  |  |  |
| Paraffins |  |  |  |
| Methane | $\mathrm{CH}_{4}$ | -161.6 | 121.87 |
| Ethane | $\mathrm{C}_{2} \mathrm{H}_{6}$ | -88.9 | 116.87 |
| Propane | $\mathrm{C}_{3} \mathrm{H}_{8}$ | 25 | 81.76 |
|  |  | -42.1 | 101.76 |
| $n$-Butane | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 25 | 86.63 |
|  |  | -0.50 | 92.09 |
| 2-Methylpropane (isobutane) | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 25 | 78.63 |
|  |  | -11.72 | 87.56 |
| $n$-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 25 | 87.54 |
|  |  | 36.08 | 85.38 |
| 2-Methylbutane (isopentane) | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 25 | 81.47 |
|  |  | 27.86 | 80.97 |
| 2,2-Dimethylpropane (neopentane) | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 25 | 72.15 |
|  |  | 9.45 | 75.37 |
| $n$-Hexane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 25 | 87.50 |
|  |  | 68.74 | 80.48 |
| 2-Methylpentane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 25 | 82.83 |
|  |  | 60.27 | 76.89 |
| 3-Methylpentane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 25 | 83.96 |
|  |  | 63.28 | 78.42 |
| 2,2-Dimethylbutane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 25 | 76.79 |
|  |  | 49.74 | 73.75 |
| 2,3-Dimethylbutane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 25 | 80.77 |
|  |  | 57.99 | 76.53 |
| $n$-Heptane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 87.18 |
|  |  | 98.43 | 76.45 |
| 2-Methylhexane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 83.02 |
|  |  | 90.05 | 73.4 |
| 3-Methylhexane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 83.68 |
|  |  | 91.95 | 74.1 |
| 3-Ethylpentane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 84.02 |
|  |  | 93.47 | 74.3 |
| 2,2-Dimethylpentane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 77.36 |
|  |  | 79.20 | 69.7 |
| 2,3-Dimethylpentane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 81.68 |
|  |  | 89.79 | 72.9 |
| 2,4-Dimethylpentane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 78.44 |
|  |  | 80.51 | 70.9 |
| 3,3-Dimethylpentane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 78.76 |
|  |  | 86.06 | 70.6 |
| 2,2,3-Trimethylbutane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 25 | 76.42 |
|  |  | 80.88 | 69.3 |
| $n$-Octane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 86.80 |
|  |  | 125.66 | 73.19 |
| 2-Methylheptane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 83.02 |
|  |  | 117.64 | 70.3 |

Table A. 17 (Continued)

|  | Formula | Temperature ( ${ }^{( } \mathrm{C}$ ) | $\lambda(\mathrm{cal} . / \mathrm{g})$ |
| :---: | :---: | :---: | :---: |
| 3-Methylheptane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 83.35 |
|  |  | 118.92 | 71.3 |
| 4-Methylheptane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 83.01 |
|  |  | 117.71 | 70.91 |
| 3-Ethylhexane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 82.95 |
|  |  | 118.53 | 71.7 |
| 2,2-Dimethylhexane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 78.02 |
|  |  | 106.84 | 67.7 |
| 2,3-Dimethylhexane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 81.17 |
|  |  | 115.60 | 70.2 |
| 2,4-Dimethylhexane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 79.02 |
|  |  | 109.43 | 68.5 |
| 2,5-Dimethylhexane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 79.21 |
|  |  | 109.10 | 68.6 |
| 3,3-Dimethylhexane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 78.54 |
|  |  | 111.97 | 68.5 |
| 3,4-Dimethylhexane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 81.55 |
|  |  | 117.72 | 70.2 |
| 2-Methyl-3-ethylpentane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 80.60 |
|  |  | 115.65 | 69.7 |
| 3-Methyl-3-ethylpentane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 79.49 |
|  |  | 118.26 | 69.3 |
| 2,2,3-Trimethylpentane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 77.24 |
|  |  | 109.84 | 67.3 |
| 2,2,4-Trimethylpentane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 73.50 |
|  |  | 99.24 | 64.87 |
| 2,3,3-Trimethylpentane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 77.87 |
|  |  | 114.76 | 68.1 |
| 2,3,4-Trimethylpentane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 25 | 78.90 |
|  |  | 113.47 | 68.37 |
| 2,2,3,3-Tetramethylbutane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 106.30 | 66.2 |
| Alkyl benzenes |  |  |  |
| Benzene | $\mathrm{C}_{6} \mathrm{H}_{6}$ | 25 | 103.57 |
|  |  | 80.10 | 94.14 |
| Methylbenzene (toluene) | $\mathrm{C}_{7} \mathrm{H}_{8}$ | 25 | 98.55 |
|  |  | 110.62 | 86.8 |
| Ethylbenzene | $\mathrm{C}_{8} \mathrm{H}_{10}$ | 25 | 95.11 |
|  |  | 136.19 | 81.0 |
| 1,2-Dimethylbenzene ( $o$-xylene) | $\mathrm{C}_{8} \mathrm{H}_{10}$ | 25 | 97.79 |
|  |  | 144.42 | 82.9 |
| 1,3-Dimethylbenzene ( $m$-xylene) | $\mathrm{C}_{8} \mathrm{H}_{10}$ | 25 | 96.03 |
|  |  | 139.10 | 82.0 |
| 1,4-Dimethylbenzene ( $p$-xylene) | $\mathrm{C}_{8} \mathrm{H}_{10}$ | 25 | 95.40 |
|  |  | 138.35 | 81.2 |
| $n$-Propylbenzene | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 91.93 |
|  |  | 159.22 | 76.0 |
| Isopropylbenzene | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 89.77 |
|  |  | 152.40 | 74.6 |
|  |  |  | Continued) |

Table A. 17 (Continued)

|  | Formula | Temperature ( ${ }^{\circ} \mathrm{C}$ ) | $\lambda$ (cal./g) |
| :---: | :---: | :---: | :---: |
| 1-Methyl-2-ethylbenzene | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 94.9 |
|  |  | 165.15 | 77.3 |
| 1-Methyl-3-ethylbenzene | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 93.3 |
|  |  | 161.30 | 76.6 |
| 1-Methyl-4-ethylbenzene | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 92.7 |
|  |  | 162.05 | 76.4 |
| 1,2,3-Trimethylbenzene | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 97.56 |
|  |  | 176.15 | 79.6 |
| 1,2,4-Trimethylbenzene (pseudocumene) | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 95.33 |
|  |  | 169.25 | 78.0 |
| 1,3,5-Trimethylbenzene (mesitylene) | $\mathrm{C}_{9} \mathrm{H}_{12}$ | 25 | 94.40 |
|  |  | 164.70 | 77.6 |
| Alkyl cyclopentanes |  |  |  |
| Cyclopentane | $\mathrm{C}_{5} \mathrm{H}_{10}$ | 25 | 97.1 |
|  |  | 49.26 | 93.1 |
| Methylcyclopentane | $\mathrm{C}_{6} \mathrm{H}_{12}$ | 25 | 89.83 |
|  |  | 71.81 | 83.2 |
| Ethylcyclopentane | $\mathrm{C}_{7} \mathrm{H}_{14}$ | 25 | 88.6 |
|  |  | 103.45 | 78.3 |
| 1,1-Dimethylcyclopentane | $\mathrm{C}_{7} \mathrm{H}_{14}$ | 25 | 82.5 |
|  |  | 87.5 | 74.6 |
| cis-1,2-Dimethylcyclopentane | $\mathrm{C}_{7} \mathrm{H}_{14}$ | 25 | 86.4 |
|  |  | 99.3 | 77.0 |
| trans-1,2-Dimethylcyclopentane | $\mathrm{C}_{7} \mathrm{H}_{14}$ | 25 | 83.9 |
|  |  | 91.9 | 75.5 |
| trans-1,3-Dimethylcyclopentane | $\mathrm{C}_{7} \mathrm{H}_{14}$ | 25 | 83.6 |
|  |  | 90.8 | 75.3 |
| Alkyl cyclohexanes |  |  |  |
| Cyclohexane | $\mathrm{C}_{6} \mathrm{H}_{12}$ | 25 | 93.81 |
|  |  | 80.74 | 85.6 |
| Methylcyclohexane | $\mathrm{C}_{7} \mathrm{H}_{14}$ | 25 | 86.07 |
|  |  | 100.94 | 76.9 |
| Ethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | 25 | 86.21 |
|  |  | 131.79 | 73.7 |
| 1,1-Dimethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | $25$ | 80.9 |
|  |  | 119.50 | 70.7 |
| cis-1,2-Dimethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | 25 | 84.59 |
|  |  | 129.73 | 72.9 |
| trans-1,2-Dimethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | 25 | 81.70 |
|  |  | 123.42 | 71.1 |
| cis-1,3-Dimethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | 25 | 83.49 |
|  |  | 124.45 | 72.1 |
| trans-1,3-Dimethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | 25 | 81.42 |
|  |  | 120.09 | 70.9 |
| cis-1,4-Dimethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | 25 | 83.13 |
|  |  | 124.32 | 71.9 |
| trans-1,4-Dimethylcyclohexane | $\mathrm{C}_{8} \mathrm{H}_{16}$ | 25 | 80.67 |
|  |  | 119.35 | 70.4 |

Table A. 17 (Continued)

|  | Formula | Temperature ( ${ }^{\circ} \mathrm{C}$ ) | $\lambda(\mathrm{cal} . / \mathrm{g})$ |
| :---: | :---: | :---: | :---: |
| Monoolefins |  |  |  |
| Ethene (ethylene) | $\mathrm{C}_{2} \mathrm{H}_{4}$ | -103.71 | 115.39 |
| Propene (propylene) | $\mathrm{C}_{3} \mathrm{H}_{6}$ | -47.70 | 104.62 |
| 1-Butene | $\mathrm{C}_{4} \mathrm{H}_{8}$ | 25 | 86.8 |
|  |  | -6.25 | 93.36 |
| cis-2-Butene | $\mathrm{C}_{4} \mathrm{H}_{8}$ | 25 | 94.5 |
|  |  | 3.72 | 99.46 |
| trans-2-Butene | $\mathrm{C}_{4} \mathrm{H}_{8}$ | 25 | 91.8 |
|  |  | 0.88 | 96.94 |
| 2-Methylpropene (isobutene) | $\mathrm{C}_{4} \mathrm{H}_{8}$ | 25 | 87.7 |
|  |  | -6.90 | 94.22 |
| Non-hydrocarbon compounds |  |  |  |
| Acetal | $\mathrm{C}_{6} \mathrm{H}_{14} \mathrm{O}_{2}$ | 102.9 | 66.18 |
| Acetaldehyde | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}$ | 21 | 136.17 |
| Acetic acid | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}_{2}$ | 118.3 | 96.75 |
|  |  | 140 | 94.37 |
|  |  | 220 | 81.23 |
|  |  | 321 | 0 |
| Acetic anhydride | $\mathrm{C}_{4} \mathrm{H}_{6} \mathrm{O}_{3}$ | 137 | 92.2 |
| Acetone | $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}$ | 0 | 134.74 |
|  |  | 20 | 131.87 |
|  |  | 40 | 128.05 |
|  |  | 60 | 123.51 |
|  |  | 80 | 118.26 |
|  |  | 100 | 112.76 |
|  |  | 235 | 0 |
| Acetonitrile | $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{~N}$ | 80 | 173.68 |
| Acetophenone | $\mathrm{C}_{8} \mathrm{H}_{8} \mathrm{O}$ | 203.7 | 77.16 |
| Acetyl chloride | $\mathrm{C}_{3} \mathrm{H}_{3} \mathrm{CIO}$ | 51 | 78.84 |
| Air | - | - | 51.0 |
| Allyl alcohol | $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}$ | 96 | 163.41 |
| Amyl alcohol ( $n$-) | $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{OH}$ | 131 | 120.17 |
| Amyl alcohol ( $t$-) | $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{OH}$ | 102 | 105.83 |
| Amyl amine ( $n$-) | $\mathrm{C}_{5} \mathrm{H}_{13} \mathrm{~N}$ | 95 | 98.67 |
| Amyl bromide ( $n$-) | $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{Br}$ | 129 | 48.26 |
| Amyl ether ( $n$-) | $\mathrm{C}_{10} \mathrm{H}_{22} \mathrm{O}$ | 170 | 69.52 |
| Amyl iodide ( $n$-) | $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{I}$ | 155 | 47.54 |
| Amyl methyl ketone ( $n$-) | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}$ | 149.2 | 82.66 |
| Amylene | $\mathrm{C}_{5} \mathrm{H}_{10}$ | 12.5 | 75.01 |
| Anethole ( $p$-) | $\mathrm{C}_{10} \mathrm{H}_{12} \mathrm{O}$ | 232 | 71.43 |
| Aniline | $\mathrm{C}_{6} \mathrm{H}_{7} \mathrm{~N}$ | 183 | 103.68 |
| Benzaldehyde | $\mathrm{C}_{7} \mathrm{H}_{6} \mathrm{O}$ | 179 | 86.48 |
| Benzonitrile | $\mathrm{C}_{7} \mathrm{H}_{5} \mathrm{~N}$ | 189 | 87.68 |
| Benzyl alcohol | $\mathrm{C}_{7} \mathrm{H}_{8} \mathrm{O}$ | 204.3 | 112.28 |
| Butyl acetate ( $n$ - | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 124 | 73.82 |
| Butyl alcohol ( $n$-) | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ | 116.8 | 141.26 |
| Butyl alcohol (s-) | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ | 98.1 | 134.38 |
| Butyl alcohol (t-) | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ | 83 | 130.44 |

Table A. 17 (Continued)

|  | Formula | Temperature ( ${ }^{\circ} \mathrm{C}$ ) | $\lambda$ (cal./g) |
| :---: | :---: | :---: | :---: |
| Butyl formate | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}_{2}$ | 105.1 | 86.74 |
| Butyl methyl ketone ( $n$-) | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}$ | 127 | 82.42 |
| Butyl propionate ( $n-$ ) | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ | 144.9 | 71.74 |
| Butyric acid ( $n$-) | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$ | 163.5 | 113.96 |
| Butyronitrile ( $n$-) | $\mathrm{C}_{4} \mathrm{H}_{7} \mathrm{~N}$ | 117.4 | 114.91 |
| Bromobenzene | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Br}$ | 155.9 | 57.60 |
| Capronitrile | $\mathrm{C}_{6} \mathrm{H}_{11} \mathrm{~N}$ | 156 | 88.15 |
| Carbon disulfide | $\mathrm{CS}_{2}$ | 0 | 89.35 |
|  |  | 46.25 | 84.09 |
|  |  | 100 | 75.49 |
|  |  | 140 | 67.37 |
| Carbon tetrachloride | $\mathrm{CCI}_{4}$ | 0 | 52.06 |
|  |  | 76.75 | 46.42 |
|  |  | 200 | 32.73 |
| Carvacrol | $\mathrm{C}_{10} \mathrm{H}_{14} \mathrm{O}$ | 237 | 68.09 |
| Chloral | $\mathrm{C}_{2} \mathrm{HCl}_{3} \mathrm{O}$ | - | 53.99 |
| Chloral hydrate | $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{Cl}_{3} \mathrm{O}_{2}$ | 96 | 131.87 |
| Chlorobenzene | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ | 130.6 | 77.59 |
| Chloroethyl alcohol (2-) | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{ClO}$ | 126.5 | 122.94 |
| Chloroethyl acetate ( $\beta$-) | $\mathrm{C}_{4} \mathrm{H}_{7} \mathrm{ClO}_{2}$ | 141.5 | 80.75 |
| Chloroform | $\mathrm{CHCl}_{3}$ | 0 | 64.74 |
|  |  | 40 | 60.92 |
|  |  | 61.5 | 59.01 |
|  |  | 100 | 55.19 |
|  |  | 260 | 0 |
| Chlorotoluene (o-) | $\mathrm{C}_{7} \mathrm{H}_{7} \mathrm{Cl}$ | 158.1 | 72.63 |
| Chlorotoluene ( $p$-) | $\mathrm{C}_{7} \mathrm{H}_{7} \mathrm{Cl}$ | 160.4 | 73.13 |
| Cresol (m-) | $\mathrm{C}_{7} \mathrm{H}_{8} \mathrm{O}$ | 202 | 100.58 |
| Cyanogen | $(\mathrm{CN})_{2}$ | 0 | 102.97 |
| Cyanogen chloride | CNCl | 13 | 134.98 |
| Cyclohexanol | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}$ | 161.1 | 108.22 |
| Cycohexyl chloride | $\mathrm{C}_{6} \mathrm{H}_{11} \mathrm{Cl}$ | 142.0 | 74.78 |
| Dichloroacetic acid | $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2} \mathrm{O}_{2}$ | 194.4 | 77.16 |
| Dichlorodifluormethane | $\mathrm{CCl}_{2} \mathrm{~F}_{2}$ | -29.8 | 40.40 |
| Diethylamine | $\mathrm{C}_{4} \mathrm{H}_{11} \mathrm{~N}$ | 58 | 91.02 |
| Diethylamine carbonate | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{3}$ | 126 | 73.10 |
| Diethylamine ketone | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}$ | 101 | 90.78 |
| Diethylamine oxalate | $\mathrm{C}_{6} \mathrm{H}_{10} \mathrm{O}_{4}$ | 185 | 67.61 |
| Di-isobutylamine | $\mathrm{C}_{8} \mathrm{H}_{19} \mathrm{~N}$ | 134 | 65.70 |
| Dimethyl aniline | $\mathrm{C}_{8} \mathrm{H}_{11} \mathrm{~N}$ | 193 | 80.75 |
| Dimethyl carbonate | $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}_{3}$ | 90 | 88.15 |
| Dipropyl ketone | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}$ | 143.5 | 75.73 |
| Dipropylamine ( $n$-) | $\mathrm{C}_{6} \mathrm{H}_{15} \mathrm{~N}$ | 108 | 75.73 |
| Ethyl acetate | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$ | 0.0 | 102.01 |
| Ethyl alcohol | $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$ | 78.3 | 204.26 |
| Ethylamine | $\mathrm{C}_{2} \mathrm{H}_{7} \mathrm{~N}$ | 15 | 145.97 |
| Ethyl benzoate | $\mathrm{C}_{9} \mathrm{H}_{10} \mathrm{O}_{2}$ | 213 | 64.50 |
| Ethyl bromide | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Br}$ | 38.4 | 59.92 |

Table A. 17 (Continued)

|  | Formula | Temperature ( ${ }^{\circ} \mathrm{C}$ ) | $\lambda$ (cal./g) |
| :---: | :---: | :---: | :---: |
| Ethyl butyrate ( $n$-) | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 118.9 | 74.68 |
| Ethyl caprylate | $\mathrm{C}_{10} \mathrm{H}_{20} \mathrm{O}_{2}$ | 207 | 60.44 |
| Ethyl chloride | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}$ | 4.7 | 92.93 |
|  |  | 15.0 | 92.45 |
|  |  | 20.0 | 92.22 |
|  |  | 25.0 | 91.98 |
| Ethylene bromide | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Br}_{2}$ | 130.8 | 46.23 |
| Ethylene chloride | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Cl}_{2}$ | 0 | 85.29 |
|  |  | 82.3 | 77.33 |
| Ethylene glycol | $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}$ | 197 | 191.12 |
| Ethylene oxide | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}$ | 13 | 138.56 |
| Ethyl ether | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ | 34.6 | 83.85 |
| Ethyl formate | $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}_{2}$ | 53.3 | 97.18 |
| Ethyl iodide | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{I}$ | 71.2 | 45.61 |
| Ethylidine chloride | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Cl}_{2}$ | 0.0 | 76.69 |
|  |  | 60 | 67.13 |
| Ethyl isobutyl ether | $\mathrm{C}_{6} \mathrm{H}_{14} \mathrm{O}$ | 79.0 | 74.78 |
| Ethyl isobutyrate | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 109.2 | 72.05 |
| Ethyl isovalerate | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ | 144 | 67.85 |
| Ethyl methyl ketone | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}$ | 78.2 | 105.93 |
| Ethyl methyl ketoxime | $\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{NO}$ | 182 | 115.87 |
| Ethyl nonylate | $\mathrm{C}_{11} \mathrm{H}_{22} \mathrm{O}_{2}$ | 227 | 58.05 |
| Ethyl propionate | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$ | 97.6 | 80.08 |
| Ethyl propyl ether | $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}$ | 60 | 82.66 |
| Ethyl valerate ( $n$-) | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ | 98 | 77.16 |
| Formic acid | $\mathrm{CH}_{2} \mathrm{O}_{2}$ | 101 | 119.93 |
| Furane | $\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{O}$ | 31 | 95.32 |
| Furfural | $\mathrm{C}_{5} \mathrm{H}_{4} \mathrm{O}_{2}$ | 160.5 | 107.51 |
| Heptyl alcohol ( $n$-) | $\mathrm{C}_{7} \mathrm{H}_{16} \mathrm{O}$ | 176 | 104.88 |
| Hexylmethyl ketone | $\mathrm{C}_{8} \mathrm{H}_{16} \mathrm{O}$ | 173 | 74.06 |
| Hydrogen cyanide | HCN | 20 | 210.23 |
| Isoamyl acetate | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ | 143.6 | 69.04 |
| Isoamyl alcohol | $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}$ | 130.2 | 119.78 |
| Isoamyl butyrate ( $n$-) | $\mathrm{C}_{9} \mathrm{H}_{18} \mathrm{O}_{2}$ | 169 | 61.88 |
| Isoamyl formate | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 123 | 73.58 |
| Isoamyl isobutyrate | $\mathrm{C}_{9} \mathrm{H}_{18} \mathrm{O}_{2}$ | 168 | 57.57 |
| Isoamyl propionate | $\mathrm{C}_{8} \mathrm{H}_{16} \mathrm{O}_{2}$ | 161 | 65.22 |
| Isoamyl valerate ( $n$-) | $\mathrm{C}_{10} \mathrm{H}_{20} \mathrm{O}_{2}$ | 187 | 56.14 |
| Isobutyl acetate | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 115.3 | 73.75 |
| Isobutyl alcohol | $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ | 106.9 | 138.08 |
| Isobutyl butyrate ( $n$-) | $\mathrm{C}_{8} \mathrm{H}_{16} \mathrm{O}_{2}$ | 157 | 64.50 |
| Isobutyl formate | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$ | 97 | 78.50 |
| Isobutyl isovalerate | $\mathrm{C}_{9} \mathrm{H}_{18} \mathrm{O}_{2}$ | 169 | 60.44 |
| Isobutyl isobutyrate | $\mathrm{C}_{8} \mathrm{H}_{16} \mathrm{O}_{2}$ | 148 | 63.31 |
| Isobutyl propionate | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ | 137 | 65.94 |
| Isobutyl valerate ( $n$-) | $\mathrm{C}_{9} \mathrm{H}_{18} \mathrm{O}_{2}$ | 169 | 57.81 |
| Isobutyric acid | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$ | 154 | 111.57 |
| Isopropyl alcohol | $\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}$ | 82.3 | 159.35 |

Table A. 17 (Continued)

|  | Formula | Temperature ( ${ }^{\circ} \mathrm{C}$ ) | $\lambda$ (cal./g) |
| :---: | :---: | :---: | :---: |
| Isopropyl methyl ketone | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}$ | 92 | 89.83 |
| Isovaleric acid | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$ | 176.3 | 101.05 |
| Limonene | $\mathrm{C}_{10} \mathrm{H}_{16}$ | 165 | 69.52 |
| Mesityl oxide | $\mathrm{C}_{6} \mathrm{H}_{10} \mathrm{O}$ | 128 | 85.77 |
| Methyl acetate | $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}_{2}$ | 0.0 | 113.96 |
|  |  | 56.3 | 98.09 |
| Methylal | $\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}_{2}$ | 42 | 89.83 |
| Methyl alcohol | $\mathrm{CH}_{4} \mathrm{O}$ | 0 | 284.29 |
|  |  | 64.7 | 262.79 |
|  |  | 100 | 241.29 |
|  |  | 160 | 193.51 |
|  |  | 200 | 148.12 |
|  |  | 220 | 109.89 |
|  |  | 240 | , |
| Methyl amyl ketone ( $n$-) | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}$ | 149.2 | 82.66 |
| Methyl aniline | $\mathrm{C}_{7} \mathrm{H}_{9} \mathrm{~N}$ | 194 | 95.56 |
| Methyl butyl ketone ( $n$-) | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 127 | 82.42 |
| Methyl butyrate ( $n$-) | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$ | 102.6 | 79.79 |
| Methyl chloride | $\mathrm{CH}_{3} \mathrm{Cl}$ | -23.8 | 102.25 |
|  |  | 15.0 | 96.04 |
|  |  | 20.0 | 95.32 |
|  |  | 25.0 | 94.60 |
| Methyl ethyl ketone | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}$ | 78.2 | 105.93 |
| Methyl ethyl ketoxime | $\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{NO}$ | 182 | 115.87 |
| Methyl formate | $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}_{2}$ | 31.3 | 112.35 |
| Methyl hexyl ketone | $\mathrm{C}_{8} \mathrm{H}_{16} \mathrm{O}$ | 173 | 74.06 |
| Methyl iodide | $\mathrm{CH}_{3} \mathrm{I}$ | 42 | 45.87 |
| Methyl isobutyrate | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$ | 91.1 | 78.12 |
| Methyl isopropyl ketone | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}$ | 92 | 89.83 |
| Methyl isovalerate | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 116 | 72.39 |
| Methyl phenyl ether | $\mathrm{C}_{7} \mathrm{H}_{8} \mathrm{O}$ | 153 | 81.46 |
| Methyl propionate | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$ | 79.0 | 87.56 |
| Methyl valerate ( $n$-) | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 116 | 70.00 |
| Naphthalene | $\mathrm{C}_{10} \mathrm{H}_{8}$ | 218 | 75.49 |
| Nitrobenzene | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NO}_{2}$ | 210 | 79.08 |
| Nitromethane | $\mathrm{CH}_{3} \mathrm{NO}_{2}$ | 99.9 | 134.98 |
| Octyl alcohol ( $n$-) | $\mathrm{C}_{8} \mathrm{H}_{18} \mathrm{O}$ | 196 | 97.47 |
| Octyl alcohol (dl-) (sec-) | $\mathrm{C}_{8} \mathrm{H}_{18} \mathrm{O}$ | 180 | 94.37 |
| Phenyl methyl ether | $\mathrm{C}_{7} \mathrm{H}_{8} \mathrm{O}$ | 153 | 81.46 |
| Picoline ( $\alpha$-) | $\mathrm{C}_{6} \mathrm{H}_{7} \mathrm{~N}$ | 129 | 90.78 |
| Piperidine | $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{~N}$ | 106 | 89.35 |
| Propionic acid | $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}_{2}$ | 139.3 | 98.81 |
| Propionitrile | $\mathrm{C}_{3} \mathrm{H}_{5} \mathrm{~N}$ | 97 | 134.26 |
| Propyl acetate ( $n$-) | $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$ | 100.4 | 80.27 |
| Propyl alcohol ( $n$-) | $\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}$ | 97.2 | 164.36 |
| Propyl butyrate ( $n$-) | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ | 143.6 | 68.33 |
| Propyl formate ( $n$-) | $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$ | 80.0 | 88.13 |

Table A. 17 (Continued)

|  | Formula | Temperature $\left({ }^{\circ} \mathrm{C}\right)$ | $\lambda(\mathrm{cal} . / \mathrm{g})$ |
| :--- | :--- | :--- | ---: |
| Propyl isobutyrate $(n-)$ | $\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}$ | 134 | 63.79 |
| Propyl isovalerate $(n-)$ | $\mathrm{C}_{8} \mathrm{H}_{16} \mathrm{O}_{2}$ | 156 | 64.50 |
| Propyl propionate $(n-)$ | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$ | 120.6 | 73.15 |
| Pyridine | $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$ | 114.1 | 107.36 |
| Salicylaldehyde | $\mathrm{C}_{7} \mathrm{H}_{6} \mathrm{O}_{2}$ | 196 | 74.78 |
| Tetrachloroethane $(1,1,2,2-)$ | $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{4}$ | 145 | 55.07 |
| Tetrachloroethylene | $\mathrm{C}_{2} \mathrm{Cl}_{4}$ | 120.7 | 50.05 |
| Toluidine $(o-)$ | $\mathrm{C}_{7} \mathrm{H}_{9} \mathrm{~N}$ | 198 | 95.08 |
| Trichloroethylene | $\mathrm{C}_{2} \mathrm{HCl}_{3}$ | 85.7 | 57.24 |
| Valeronitrile $(n-)$ | $\mathrm{C}_{5} \mathrm{H}_{9} \mathrm{~N}$ | 129 | 96.28 |



Figure A. 1 Viscosities of liquids at atmospheric pressure (Source: Ref. [11]).

Table A. 18 Coordinates to be Used with Figure A. 1

| Liquid | $X$ | $Y$ | Liquid | $X$ | $Y$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Acetaldehyde | 15.2 | 4.8 | Ethyl alcohol, 95\% | 9.8 | 14.3 |
| Acetic acid, 100\% | 12.1 | 14.2 | Ethyl alcohol, 40\% | 6.5 | 16.6 |
| Acetic acid, 70\% | 9.5 | 17.0 | Ethyl benzene | 13.2 | 11.5 |
| Acetic anhydride | 12.7 | 12.8 | Ethyl bromide | 14.5 | 8.1 |
| Acetone, 100\% | 14.5 | 7.2 | 2-Ethyl butyl acrylate | 11.2 | 14.0 |
| Acetone, 35\% | 7.9 | 15.0 | Ethyl chloride | 14.8 | 6.0 |
| Acetonitrile | 14.4 | 7.4 | Ethyl ether | 14.5 | 5.3 |
| Acrylic acid | 12.3 | 13.9 | Ethyl formate | 14.2 | 8.4 |
| Allyl alcohol | 10.2 | 14.3 | 2-Ethyl hexyl acrylate | 9.0 | 15.0 |
| Allyl bromide | 14.4 | 9.6 | Ethyl iodide | 14.7 | 10.3 |
| Allyl iodide | 14.0 | 11.7 | Ethyl propionate | 13.2 | 9.9 |
| Ammonia, 100\% | 12.6 | 2.0 | Ethyl propyl ether | 14.0 | 7.0 |
| Ammonia, 26\% | 10.1 | 13.9 | Ethyl sulfide | 13.8 | 8.9 |
| Amyl acetate | 11.8 | 12.5 | Ethylene bromide | 11.9 | 15.7 |
| Amyl alcohol | 7.5 | 18.4 | Ethylene chloride | 12.7 | 12.2 |
| Aniline | 8.1 | 18.7 | Ethylene glycol | 6.0 | 23.6 |
| Anisole | 12.3 | 13.5 | Ethylidene chloride | 14.1 | 8.7 |
| Arsenic trichloride | 13.9 | 14.5 | Fluorobenzene | 13.7 | 10.4 |
| Benzene | 12.5 | 10.9 | Formic acid | 10.7 | 15.8 |
| Brine, $\mathrm{CaCL}_{2}$, 25\% | 6.6 | 15.9 | Freon-11 | 14.4 | 9.0 |
| Brine, $\mathrm{NaCl}, 25 \%$ | 10.2 | 16.6 | Freon-12 | 16.8 | 15.6 |
| Bromine | 14.2 | 13.2 | Freon-21 | 15.7 | 7.5 |
| Bromotoluene | 20.0 | 15.9 | Freon-22 | 17.2 | 4.7 |
| Butyl acetate | 12.3 | 11.0 | Freon-113 | 12.5 | 11.4 |
| Butyl acrylate | 11.5 | 12.6 | Glycerol, 100\% | 2.0 | 30.0 |
| Butyl alcohol | 8.6 | 17.2 | Glycerol, 50\% | 6.9 | 19.6 |
| Butyric acid | 12.1 | 15.3 | Heptane | 14.1 | 8.4 |
| Carbon dioxide | 11.6 | 0.3 | Hexane | 14.7 | 7.0 |
| Carbon disulfide | 16.1 | 7.5 | Hydrochloric acid, 31.5\% | 13.0 | 16.6 |
| Carbon tetrachloride | 12.7 | 13.1 | Iodobenzene | 12.8 | 15.9 |
| Chlorobenzene | 12.3 | 12.4 | Isobutyl alcohol | 7.1 | 18.0 |
| Chloroform | 14.4 | 10.2 | Isobutyric acid | 12.2 | 14.4 |
| Chlorosulfonic acid | 11.2 | 18.1 | Isopropyl alcohol | 8.2 | 16.0 |
| Chlorotoluene, ortho | 13.0 | 13.3 | Isopropyl bromide | 14.1 | 9.2 |
| Chlorotoluene, meta | 13.3 | 12.5 | Isopropyl chloride | 13.9 | 7.1 |
| Chlorotoluene, para | 13.3 | 12.5 | Isopropyl iodide | 13.7 | 11.2 |
| Cresol, meta | 2.5 | 20.8 | Kerosene | 10.2 | 16.9 |
| Cyclohexanol | 2.9 | 24.3 | Linseed oil, raw | 7.5 | 27.2 |
| Cyclohexane | 9.8 | 12.9 | Mercury | 18.4 | 16.4 |
| Dibromomethane | 12.7 | 15.8 | Methanol, 100\% | 12.4 | 10.5 |
| Dichloroethane | 13.2 | 12.2 | Methanol, 90\% | 12.3 | 11.8 |
| Dichloromethane | 14.6 | 8.9 | Methanol, 40\% | 7.8 | 15.5 |
| Diethyl ketone | 13.5 | 9.2 | Methyl acetate | 14.2 | 8.2 |
| Diethyl oxalate | 11.0 | 16.4 | Methyl acrylate | 13.0 | 9.5 |
| Diethylene glycol | 5.0 | 24.7 | Methyl $i$-butyrate | 12.3 | 9.7 |
| Diphenyl | 12.0 | 18.3 | Methyl $n$-butyrate | 13.2 | 10.3 |
| Dipropyl ether | 13.2 | 8.6 | Methyl chloride | 15.0 | 3.8 |
| Dipropyl oxalate | 10.3 | 17.7 | Methyl ethyl ketone | 13.9 | 8.6 |
| Ethyl acetate | 13.7 | 9.1 | Methyl formate | 14.2 | 7.5 |
| Ethyl acrylate | 12.7 | 10.4 | Methyl iodide | 14.3 | 9.3 |
| Ethyl alcohol, 100\% | 10.5 | 13.8 | Methyl propionate | 13.5 | 9.0 |

Table A. 18 (Continued)

| Liquid | $X$ |  | Liquid | $X$ | $Y$ |
| :--- | ---: | ---: | :--- | ---: | ---: |
| Methyl propyl ketone | 14.3 | 9.5 | Sodium hydroxide, $50 \%$ | 3.2 | 25.8 |
| Methyl sulfide | 15.3 | 6.4 | Stannic chloride | 13.5 | 12.8 |
| Napthalene | 7.9 | 18.1 | Succinonitrile | 10.1 | 20.8 |
| Nitric acid, $95 \%$ | 12.8 | 13.8 | Sulfur dioxide | 15.2 | 7.1 |
| Nitric acid, $60 \%$ | 10.8 | 17.0 | Sulfuric acid, $110 \%$ | 7.2 | 27.4 |
| Nitrobenzene | 10.6 | 16.2 | Sulfuric acid, $100 \%$ | 8.0 | 25.1 |
| Nitrogen dioxide | 12.9 | 8.6 | Sulfuric acid, $98 \%$ | 24.8 |  |
| Nitrotoluene | 11.0 | 17.0 | Sulfuric acid, $60 \%$ | 7.0 | 21.3 |
| Octane | 13.7 | 10.0 | Sulfuryl chloride | 10.2 | 15.2 |
| Octyl alcohol | 6.6 | 21.1 | Tetrachloroethane | 11.9 | 15.4 |
| Pentachloroethane | 10.9 | 17.3 | Thiophene | 13.2 | 11.0 |
| Pentane | 14.9 | 5.2 | Titanium tetrachloride | 14.4 | 12.3 |
| Phenol | 6.9 | 20.8 | Toluene | 10.4 |  |
| Phosphorus tribromide | 13.8 | 16.7 | Trichloroethylene | 14.8 | 10.5 |
| Phosphorus trichloride | 16.2 | 10.9 | Triethylene glycol | 4.7 | 24.8 |
| Propionic acid | 12.8 | 13.8 | Turpentine | 11.5 | 14.9 |
| Propyl acetate | 13.1 | 10.3 | Vinyl acetate | 14.0 | 8.8 |
| Propyl alcohol | 9.1 | 16.5 | Vinyl toluene | 13.4 | 12.0 |
| Propyl bromide | 14.5 | 9.6 | Water | 13.0 |  |
| Propyl chloride | 14.4 | 7.5 | Xylene, ortho | 13.2 | 12.1 |
| Propyl formate | 13.1 | 9.7 | Xylene, meta | 13.5 | 13.9 |
| Propyl iodide | 14.1 | 11.6 | Xylene, para | 10.9 |  |
| Sodium | 16.4 | 13.9 |  | 13.9 | 10.9 |

Source: Ref. [11].

Temperature



| No. | Gas | X | Y | No. | Gas | X | Y | No. | Gas | X | Y | No. | Gas | X | Y |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Acetic acid | 7.7 | 14.3 | 15 | Chloroform | 8.9 | 15.7 | 29 | Freon-113 | 11.3 | :14.0 | 43 | Nitric oxide | 10.9 | 20.5 |
| 2 | Acetone | 8.9 | 13.0 | 16 | Cyanogen | 9.2 | 15.2 | 30 | Helium | 10.9 | 20.5 | 44 | Nitrogen | 10.6 | 20.0 |
| 3 | Acetylene | 9.8 | 14.9 | 17 | Cyclohexane | 9.2 | 12.0 | 31 | Hexane | 8.6 | 11.8 | 45 | Nitrosyl chloride | 8.0 | 17.6 |
| 4 | Air | 11.0 | 20.0 | 18 | Ethane | 9.1 | 14.5 | 32 | Hydrogen | 11.2 | 12.4 | 46 | Nitrous oxide | 8.8 | 19.0 |
| 5 | Ammonia | 8.4 | 16.0 | 19 | Ethyl acetate | 8.5 | 13.2 | 33 | $3 \mathrm{H}_{2}+\mathrm{IN}_{2}$ | 11.2 | 17.2 | 47 | Oxygen | 11.0 | 21.3 |
| 6 | Argon | 10.5 | 22.4 | 20 | Ethyl alcohol | 9.2 | 14.2 | 34 | Hydrogen bromide | 8.8 | 20.9 | 48 | Pentane | 7.0 | 12.8 |
| 7 | Benzene | 8.5 | 13.2 | 21 | Ethyl chloride | 8.5 | 15.6 | 35 | Hydrogen chloride | 8.8 | 18.7 | 49 | Propane | 9.7 | 12.9 |
| 8 | Bromine | 8.9 | 19.2 | 22 | Ethyl ether | 8.9 | 13.0 | 36 | Hydrogen cyanide | 9.8 | 14.9 | 50 | Propyl alcohol | 8.4 | 13.4 |
| 9 | Butene | 9.2 | 13.7 | 23 | Ethylene | 9.5 | 15.1 | 37 | Hydrogen iodide | 9.0 | 21.3 | 51 | Propylene | 9.0 | 13.8 |
| 10 | Butylene | 8.9 | 13.0 | 24 | Fluorine | 7.3 | 23.8 | 38 | Hydrogen sulfide | 8.6 | 18.0 | 52 | Sulfur dioxide | 9.6 | 17.0 |
| 11 | Carbon dioxide | 9.5 | 18.7 | 25 | Freon-11 | 10.6 | 15.1 | 39 | lodine | 9.0 | 18.4 | 53 | Toluene | 8.6 | 12.4 |
| 12 | Carbon disulfide | 8.0 | 16.0 | 26 | Freon-12 | 11.1 | 16.0 | 40 | Mercury | 5.3 | 22.9 | 54 | 2,3,3-Trimethylbutane | 9.5 | 10.5 |
| 13 | Carbon monoxide | 11.0 | 20.0 | 27 | Freon-21 | 10.8 | 15.3 | 41 | Methane | 9.9 | 15.6 | 55 | Water | 8.0 | 16.0 |
| 14 | Chlorine | 9.0 | 18.4 | 28 | Freon-22 | 10.1 | 17.0 | 42 | Methyl alcohol | 8.5 | 15.6 | 56 | Xenon | 9.3 | 23.0 |

Figure A. 2 Viscosities of gases at atmospheric pressure (Source: Ref. [11]).


Figure A. 3 Specific heats of liquids (Source: Ref. [12]).

## Appendix B: Dimensions of Pipe and Tubing

Table B. 1 Dimensions of Heat Exchanger and Condenser Tubing
(a) The Birmingham Wire Gage Scale

| BWG | Thickness (in.) |
| :---: | :--- |
| 7 | 0.180 |
| 8 | 0.165 |
| 10 | 0.134 |
| 11 | 0.120 |
| 12 | 0.109 |
| 13 | 0.095 |
| 14 | 0.083 |
| 15 | 0.072 |
| 16 | 0.065 |
| 17 | 0.058 |
| 18 | 0.049 |
| 20 | 0.035 |
| 22 | 0.028 |
| 24 | 0.022 |
| 26 | 0.018 |

Table B. 1 Dimensions of Heat Exchanger and Condenser Tubing (b) Tubing Dimensions

| Tube OD (in.) | BWG | $\begin{aligned} & \text { Tube } \mathrm{ID}^{\mathrm{a}} \\ & \text { (in.) } \end{aligned}$ | Internal area ${ }^{\text {b }}$ $\text { (in. } \left.{ }^{2}\right)$ | External surface per foot length ${ }^{\mathrm{c}}$ ( $\mathrm{ft}^{2} / \mathrm{ft}$ ) | $\frac{\mathrm{OD}}{\mathrm{ID}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1/2 | 16 | 0.370 | 0.1075 | 0.1309 | 1.351 |
|  | 18 | 0.402 | 0.1269 | 0.1309 | 1.244 |
|  | 20 | 0.430 | 0.1452 | 0.1309 | 1.163 |
|  | 22 | 0.444 | 0.1548 | 0.1309 | 1.126 |
| 5/8 | 12 | 0.407 | 0.1301 | 0.1636 | 1.536 |
|  | 13 | 0.435 | 0.1486 | 0.1636 | 1.437 |
|  | 14 | 0.459 | 0.1655 | 0.1636 | 1.362 |
|  | 15 | 0.481 | 0.1817 | 0.1636 | 1.299 |
|  | 16 | 0.495 | 0.1924 | 0.1636 | 1.263 |
|  | 17 | 0.509 | 0.2035 | 0.1636 | 1.228 |
|  | 18 | 0.527 | 0.2181 | 0.1636 | 1.186 |
|  | 19 | 0.541 | 0.2299 | 0.1636 | 1.155 |
|  | 20 | 0.555 | 0.2419 | 0.1636 | 1.126 |
| 3/4 | 10 | 0.482 | 0.1825 | 0.1963 | 1.556 |
|  | 11 | 0.510 | 0.2043 | 0.1963 | 1.471 |
|  | 12 | 0.532 | 0.2223 | 0.1963 | 1.410 |
|  | 13 | 0.560 | 0.2463 | 0.1963 | 1.339 |
|  | 14 | 0.584 | 0.2679 | 0.1963 | 1.284 |
|  | 15 | 0.606 | 0.2884 | 0.1963 | 1.238 |
|  | 16 | 0.620 | 0.3019 | 0.1963 | 1.210 |
|  | 17 | 0.634 | 0.3157 | 0.1963 | 1.183 |
|  | 18 | 0.652 | 0.3339 | 0.1963 | 1.150 |
|  | 20 | 0.680 | 0.3632 | 0.1963 | 1.103 |
| 7/8 | 10 | 0.607 | 0.2894 | 0.2291 | 1.442 |
|  | 11 | 0.635 | 0.3167 | 0.2291 | 1.378 |
|  | 12 | 0.657 | 0.3390 | 0.2291 | 1.332 |
|  | 13 | 0.685 | 0.3685 | 0.2291 | 1.277 |
|  | 14 | 0.709 | 0.3948 | 0.2291 | 1.234 |
|  | 15 | 0.731 | 0.4197 | 0.2291 | 1.197 |
|  | 16 | 0.745 | 0.4359 | 0.2291 | 1.174 |
|  | 17 | 0.759 | 0.4525 | 0.2291 | 1.153 |
|  | 18 | 0.777 | 0.4742 | 0.2291 | 1.126 |
|  | 20 | 0.805 | 0.5090 | 0.2291 | 1.087 |
| 1.0 | 8 | 0.670 | 0.3526 | 0.2618 | 1.493 |
|  | 10 | 0.732 | 0.4208 | 0.2618 | 1.366 |
|  | 11 | 0.760 | 0.4536 | 0.2618 | 1.316 |
|  | 12 | 0.782 | 0.4803 | 0.2618 | 1.279 |
|  | 13 | 0.810 | 0.5153 | 0.2618 | 1.235 |
|  | 14 | 0.834 | 0.5463 | 0.2618 | 1.199 |
|  | 15 | 0.856 | 0.5755 | 0.2618 | 1.168 |
|  | 16 | 0.870 | 0.5945 | 0.2618 | 1.149 |
|  | 18 | 0.902 | 0.6390 | 0.2618 | 1.109 |
|  | 20 | 0.930 | 0.6793 | 0.2618 | 1.075 |

## Table B. 1 (Continued)

| Tube OD <br> (in.) | BWG | Tube ID <br> (in.) | Internal area ${ }^{\text {b }}$ <br> (in. ${ }^{2}$ ) | External surface per <br> foot length ${ }^{\mathrm{c}}\left(\mathrm{ft}^{2} / \mathrm{ft}\right.$ ) | OD <br> 1.25 |
| :--- | :---: | :--- | :--- | :--- | :--- |
|  | 7 | 0.890 | 0.6221 | 0.3272 | 1.404 |
|  | 8 | 0.920 | 0.6648 | 0.3272 | 1.359 |
|  | 10 | 0.982 | 0.7574 | 0.3272 | 1.273 |
|  | 11 | 1.010 | 0.8012 | 0.3272 | 1.238 |
|  | 12 | 1.032 | 0.8365 | 0.3272 | 1.211 |
|  | 13 | 1.060 | 0.8825 | 0.3272 | 1.179 |
|  | 14 | 1.084 | 0.9229 | 0.3272 | 1.153 |
|  | 16 | 1.120 | 0.9852 | 0.3272 | 1.116 |
|  | 18 | 1.152 | 1.0423 | 0.3272 | 1.085 |
|  | 20 | 1.180 | 1.0936 | 0.3272 | 1.059 |
|  | 10 | 1.232 | 1.1921 | 0.3927 | 1.218 |
|  | 12 | 1.282 | 1.2908 | 0.3927 | 1.170 |
|  | 14 | 1.334 | 1.3977 | 0.3927 | 1.124 |
|  | 16 | 1.370 | 1.4741 | 0.3927 | 1.095 |
|  | 11 | 1.760 | 2.4328 | 0.5236 | 1.136 |
|  | 12 | 1.782 | 2.4941 | 0.5236 | 1.122 |
|  | 13 | 1.810 | 2.5730 | 0.5236 | 1.105 |
|  | 14 | 1.834 | 2.6417 | 0.5236 | 1.091 |

[^11]Table B. 2 Properties of Steel Pipe.

| Nominal pipe size (in.) | Outside diameter (in.) | Schedule <br> No. | Wall thickness (in.) | Inside <br> diameter <br> (in.) | Cross-sectional area |  | Circumference (ft) or surface ( $\mathrm{ft}^{2} / \mathrm{ft}$ of length) |  | Capacity at $1 \mathrm{ft} / \mathrm{s}$ velocity |  | Weight of plain-end pipe (lb/ft) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Metal <br> (in. ${ }^{2}$ ) | Flow <br> ( $\mathrm{ft}^{2}$ ) | Outside | Inside | US gal/min | lb/h water |  |
| $\frac{1}{8}$ | 0.405 | 10S | 0.049 | 0.307 | 0.055 | 0.00051 | 0.106 | 0.0804 | 0.231 | 115.5 | 0.19 |
|  |  | 40ST, 40S | 0.068 | 0.269 | 0.072 | 0.00040 | 0.106 | 0.0705 | 0.179 | 89.5 | 0.24 |
|  |  | 80XS, 80S | 0.095 | 0.215 | 0.093 | 0.00025 | 0.106 | 0.0563 | 0.113 | 56.5 | 0.31 |
| $\frac{1}{4}$ | 0.540 | 10S | 0.065 | 0.410 | 0.097 | 0.00092 | 0.141 | 0.107 | 0.412 | 206.5 | 0.33 |
|  |  | 40ST, 40S | 0.088 | 0.364 | 0.125 | 0.00072 | 0.141 | 0.095 | 0.323 | 161.5 | 0.42 |
|  |  | 80XS, 80S | 0.119 | 0.302 | 0.157 | 0.00050 | 0.141 | 0.079 | 0.224 | 112.0 | 0.54 |
| $\frac{3}{8}$ | 0.675 | 10S | 0.065 | 0.545 | 0.125 | 0.00162 | 0.177 | 0.143 | 0.727 | 363.5 | 0.42 |
|  |  | 40ST, 40S | 0.091 | 0.493 | 0.167 | 0.00133 | 0.177 | 0.129 | 0.596 | 298.0 | 0.57 |
|  |  | 80XS, 80S | 0.126 | 0.423 | 0.217 | 0.00098 | 0.177 | 0.111 | 0.440 | 220.0 | 0.74 |
| $\frac{1}{2}$ | 0.840 | 5S | 0.065 | 0.710 | 0.158 | 0.00275 | 0.220 | 0.186 | 1.234 | 617.0 | 0.54 |
|  |  | 10S | 0.083 | 0.674 | 0.197 | 0.00248 | 0.220 | 0.176 | 1.112 | 556.0 | 0.67 |
|  |  | 40ST, 40S | 0.109 | 0.622 | 0.250 | 0.00211 | 0.220 | 0.163 | 0.945 | 472.0 | 0.85 |
|  |  | 80XS, 80S | 0.147 | 0.546 | 0.320 | 0.00163 | 0.220 | 0.143 | 0.730 | 365.0 | 1.09 |
|  |  | 160 | 0.188 | 0.464 | 0.385 | 0.00117 | 0.220 | 0.122 | 0.527 | 263.5 | 1.31 |
|  |  | XX | 0.294 | 0.252 | 0.504 | 0.00035 | 0.220 | 0.066 | 0.155 | 77.5 | 1.71 |
| $\frac{3}{4}$ | 1.050 | 5S | 0.065 | 0.920 | 0.201 | 0.00461 | 0.275 | 0.241 | 2.072 | 1036.0 | 0.69 |
|  |  | 10S | 0.083 | 0.884 | 0.252 | 0.00426 | 0.275 | 0.231 | 1.903 | 951.5 | 0.86 |
|  |  | 40ST, 40S | 0.113 | 0.824 | 0.333 | 0.00371 | 0.275 | 0.216 | 1.665 | 832.5 | 1.13 |
|  |  | 80XS, 80S | 0.154 | 0.742 | 0.433 | 0.00300 | 0.275 | 0.194 | 1.345 | 672.5 | 1.47 |
|  |  | 160 | 0.219 | 0.612 | 0.572 | 0.00204 | 0.275 | 0.160 | 0.917 | 458.5 | 1.94 |
|  |  | XX | 0.308 | 0.434 | 0.718 | 0.00103 | 0.275 | 0.114 | 0.461 | 230.5 | 2.44 |
| 1 | 1.315 | 5S | 0.065 | 1.185 | 0.255 | 0.00768 | 0.344 | 0.310 | 3.449 | 1725 | 0.87 |
|  |  | 10S | 0.109 | 1.097 | 0.413 | 0.00656 | 0.344 | 0.287 | 2.946 | 1473 | 1.40 |
|  |  | 40ST, 40S | 0.133 | 1.049 | 0.494 | 0.00600 | 0.344 | 0.275 | 2.690 | 1345 | 1.68 |
|  |  | 80XS, 80S | 0.179 | 0.957 | 0.639 | 0.00499 | 0.344 | 0.250 | 2.240 | 1120 | 2.17 |
|  |  | 160 | 0.250 | 0.815 | 0.836 | 0.00362 | 0.344 | 0.213 | 1.625 | 812.5 | 2.84 |
|  |  | XX | 0.358 | 0.599 | 1.076 | 0.00196 | 0.344 | 0.157 | 0.878 | 439.0 | 3.66 |



Table B. 2 (Continued)

| Nominal pipe size (in.) | Outside diameter (in.) | ScheduleNo. | Wall thickness (in.) | Inside diameter (in.) | Cross-sectional area |  | Circumference (ft) or surface ( $\mathrm{ft}^{2} / \mathrm{ft}$ of length) |  | Capacity at $1 \mathrm{ft} / \mathrm{s}$ velocity |  | Weight of plain-end pipe (lb/ft) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Metal <br> (in. ${ }^{2}$ ) | $\begin{aligned} & \text { Flow } \\ & \left(\mathrm{ft}^{2}\right) \end{aligned}$ | Outside | Inside | US <br> gal/min | lb/h water |  |
| 4 | 4.5 | 5 S | 0.083 | 4.334 | 1.152 | 0.10245 | 1.178 | 1.135 | 46.0 | 23,000 | 3.92 |
|  |  | 10S | 0.120 | 4.260 | 1.651 | 0.09898 | 1.178 | 1.115 | 44.4 | 22,200 | 5.61 |
|  |  | 40ST, 40S | 0.237 | 4.026 | 3.17 | 0.08840 | 1.178 | 1.054 | 39.6 | 19,800 | 10.79 |
|  |  | 80XS, 80S | 0.337 | 3.826 | 4.41 | 0.07986 | 1.178 | 1.002 | 35.8 | 17,900 | 14.98 |
|  |  | 120 | 0.438 | 3.624 | 5.58 | 0.07170 | 1.178 | 0.949 | 32.2 | 16,100 | 18.98 |
|  |  | 160 | 0.531 | 3.438 | 6.62 | 0.06647 | 1.178 | 0.900 | 28.9 | 14,450 | 22.52 |
|  |  | XX | 0.674 | 3.152 | 8.10 | 0.05419 | 1.178 | 0.825 | 24.3 | 12,150 | 27.54 |
| 5 | 5.563 | 5 S | 0.109 | 5.345 | 1.87 | 0.1558 | 1.456 | 1.399 | 69.9 | 34,950 | 6.36 |
|  |  | 10S | 0.134 | 5.295 | 2.29 | 0.1529 | 1.456 | 1.386 | 68.6 | 34,300 | 7.77 |
|  |  | 40ST, 40S | 0.258 | 5.047 | 4.30 | 0.1390 | 1.456 | 1.321 | 62.3 | 31,150 | 14.62 |
|  |  | 80XS, 80S | 0.375 | 4.813 | 6.11 | 0.1263 | 1.456 | 1.260 | 57.7 | 28,850 | 20.78 |
|  |  | 120 | 0.500 | 4.563 | 7.95 | 0.1136 | 1.456 | 1.195 | 51.0 | 25,500 | 27.04 |
|  |  | 160 | 0.625 | 4.313 | 9.70 | 0.1015 | 1.456 | 1.129 | 45.5 | 22,750 | 32.96 |
|  |  | XX | 0.750 | 4.063 | 11.34 | 0.0900 | 1.456 | 1.064 | 40.4 | 20,200 | 38.55 |
| 6 | 6.625 | 5 S |  | 6.407 | 2.23 | 0.2239 | 1.734 | 1.677 | 100.5 | 50,250 | 7.60 |
|  |  | 10 S | 0.134 | 6.357 | 2.73 | 0.2204 | 1.734 | 1.664 | 98.9 | 49,450 | 9.29 |
|  |  | 40ST, 40S | 0.280 | 6.065 | 5.58 | 0.2006 | 1.734 | 1.588 | 90.0 | 45,000 | 18.97 |
|  |  | 80XS, 80S | 0.432 | 5.761 | 8.40 | 0.1810 | 1.734 | 1.508 | 81.1 | 40,550 | 28.57 |
|  |  | 120 | 0.562 | 5.501 | 10.70 | 0.1650 | 1.734 | 1.440 | 73.9 | 36,950 | 36.42 |
|  |  | 160 | 0.719 | 5.187 | 13.34 | 0.1467 | 1.734 | 1.358 | 65.9 | 32,950 | 45.34 |
|  |  | XX | 0.864 | 4.897 | 15.64 | 0.1308 | 1.734 | 1.282 | 58.7 | 29,350 | 53.16 |
| 8 | 8.625 | 5 S | 0.109 | 8.407 | 2.915 | 0.3855 | 2.258 | 2.201 | 173.0 | 86,500 | 9.93 |
|  |  | 10 S | 0.148 | 8.329 | 3.941 | 0.3784 | 2.258 | 2.180 | 169.8 | 84,900 | 13.40 |
|  |  | 20 | 0.250 | 8.125 | 6.578 | 0.3601 | 2.258 | 2.127 | 161.5 | 80,750 | 22.36 |
|  |  | 30 | 0.277 | 8.071 | 7.265 | 0.3553 | 2.258 | 2.113 | 159.4 | 79,700 | 24.70 |
|  |  | 40ST, 40S | 0.322 | 7.981 | 8.399 | 0.3474 | 2.258 | 2.089 | 155.7 | 77,850 | 28.55 |
|  |  | 60 | 0.406 | 7.813 | 10.48 | 0.3329 | 2.258 | 2.045 | 149.4 | 74,700 | 35.66 |
|  |  | 80XS, 80S | 0.500 | 7.625 | 12.76 | 0.3171 | 2.258 | 1.996 | 142.3 | 71,150 | 43.39 |
|  |  | 100 | 0.594 | 7.437 | 14.99 | 0.3017 | 2.258 | 1.947 | 135.4 | 67,700 | 50.93 |


|  |  | 120 | 0.719 | 7.187 | 17.86 | 0.2817 | 2.258 | 1.882 | 126.4 | 63,200 | 60.69 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 140 | 0.812 | 7.001 | 19.93 | 0.2673 | 2.258 | 1.833 | 120.0 | 60,000 | 67.79 |  |
|  |  | XX | 0.875 | 6.875 | 21.30 | 0.2578 | 2.258 | 1.800 | 115.7 | 57,850 | 72.42 |  |
|  |  | 160 | 0.906 | 6.813 | 21.97 | 0.2532 | 2.258 | 1.784 | 113.5 | 56,750 | 74.71 |  |
| 10 | 10.75 | 5S | 0.134 | 10.842 | 4.47 | 0.5993 | 2.814 | 2.744 | 269.0 | 134,500 | 15.19 |  |
|  |  | 10S | 0.165 | 10.420 | 5.49 | 0.5922 | 2.814 | 2.728 | 265.8 | 132,900 | 18.65 |  |
|  |  | 20 | 0.250 | 10.250 | 8.25 | 0.5731 | 2.814 | 2.685 | 257.0 | 128,500 | 28.04 |  |
|  |  | 30 | 0.307 | 10.136 | 10.07 | 0.5603 | 2.814 | 2.655 | 252.0 | 126,000 | 34.24 |  |
|  |  | 40ST, 40S | 0.365 | 10.020 | 11.91 | 0.5475 | 2.814 | 2.620 | 246.0 | 123,000 | 40.48 |  |
|  |  | 80S, 60XS | 0.500 | 9.750 | 16.10 | 0.5185 | 2.814 | 2.550 | 233.0 | 116,500 | 54.74 |  |
|  |  | 80 | 0.594 | 9.562 | 18.95 | 0.4987 | 2.814 | 2.503 | 223.4 | 111,700 | 64.40 |  |
|  |  | 100 | 0.719 | 9.312 | 22.66 | 0.4729 | 2.814 | 2.438 | 212.3 | 106,150 | 77.00 |  |
|  |  | 120 | 0.844 | 9.062 | 26.27 | 0.4479 | 2.814 | 2.372 | 201.0 | 100,500 | 89.27 |  |
|  |  | 140, XX | 1.000 | 8.750 | 30.63 | 0.4176 | 2.814 | 2.291 | 188.0 | 94,000 | 104.13 |  |
|  |  | 160 | 1.125 | 8.500 | 34.02 | 0.3941 | 2.814 | 2.225 | 177.0 | 88,500 | 115.65 |  |
| 12 | 12.75 | 5S | 0.156 | 12.438 | 6.17 | 0.8438 | 3.338 | 3.26 | 378.7 | 189,350 | 20.98 |  |
|  |  | 10S | 0.180 | 12.390 | 7.11 | 0.8373 | 3.338 | 3.24 | 375.8 | 187,900 | 24.17 |  |
|  |  | 20 | 0.250 | 12.250 | 9.82 | 0.8185 | 3.338 | 3.21 | 367.0 | 183,500 | 33.38 |  |
|  |  | 30 | 0.330 | 12.090 | 12.88 | 0.7972 | 3.338 | 3.17 | 358.0 | 179,000 | 43.77 |  |
|  |  | ST, 40S | 0.375 | 12.000 | 14.58 | 0.7854 | 3.338 | 3.14 | 352.5 | 176,250 | 49.56 |  |
|  |  | 40 | 0.406 | 11.938 | 15.74 | 0.7773 | 3.338 | 3.13 | 349.0 | 174,500 | 53.56 |  |
|  |  | XS, 80S | 0.500 | 11.750 | 19.24 | 0.7530 | 3.338 | 3.08 | 338.0 | 169,000 | 65.42 |  |
|  |  | 60 | 0.562 | 11.626 | 21.52 | 0.7372 | 3.338 | 3.04 | 331.0 | 165,500 | 73.22 |  |
|  |  | 80 | 0.688 | 11.374 | 26.07 | 0.7056 | 3.338 | 2.98 | 316.7 | 158,350 | 88.57 |  |
|  |  | 100 | 0.844 | 11.062 | 31.57 | 0.6674 | 3.338 | 2.90 | 299.6 | 149,800 | 107.29 |  |
|  |  | 120, XX | 1.000 | 10.750 | 36.91 | 0.6303 | 3.338 | 2.81 | 283.0 | 141,500 | 125.49 |  |
|  |  | 140 | 1.125 | 10.500 | 41.09 | 0.6013 | 3.338 | 2.75 | 270.0 | 135,000 | 139.68 |  |
|  |  | 160 | 1.312 | 10.126 | 47.14 | 0.5592 | 3.338 | 2.65 | 251.0 | 125,500 | 160.33 |  |
| 14 | 14 | 5S | 0.156 | 13.688 | 6.78 | 1.0219 | 3.665 | 3.58 | 459 | 229,500 | 23.07 |  |
|  |  | 10S | 0.188 | 13.624 | 8.16 | 1.0125 | 3.665 | 3.57 | 454 | 227,000 | 27.73 | $\xrightarrow{\square}$ |
|  |  | 10 | 0.250 | 13.500 | 10.80 | 0.9940 | 3.665 | 3.53 | 446 | 223,000 | 36.71 | 0 |
|  |  | 20 | 0.312 | 13.376 | 13.42 | 0.9750 | 3.665 | 3.50 | 438 | 219,000 | 45.68 | \% |
|  |  | 30, ST | 0.375 | 13.250 | 16.05 | 0.9575 | 3.665 | 3.47 | 430 | 215,000 | 54.57 |  |
|  |  | 40 | 0.438 | 13.124 | 18.66 | 0.9397 | 3.665 | 3.44 | 422 | 211,000 | 63.37 | $\overline{\times}$ |
|  |  | XS | 0.500 | 13.000 | 21.21 | 0.9218 | 3.665 | 3.40 | 414 | 207,000 | 72.09 |  |
|  |  | 60 | 0.594 | 12.812 | 25.02 | 0.8957 | 3.665 | 3.35 | 402 | 201,000 | 85.01 | - |
|  |  |  |  |  |  |  |  |  |  |  | (continued) | N |

Table B. 2 (Continued)


|  |  | 120 | 1.375 | 15.250 | 71.82 | 1.2684 | 4.712 | 3.99 | 569 | 284,500 | 244.14 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 140 | 1.562 | 14.876 | 80.66 | 1.2070 | 4.712 | 3.89 | 540 | 270,000 | 274.30 |
|  |  | 160 | 1.781 | 14.438 | 90.75 | 1.1370 | 4.712 | 3.78 | 510 | 255,000 | 308.55 |
| 20 | 20 | 5 S | 0.188 | 19.624 | 11.70 | 2.1004 | 5.236 | 5.14 | 943 | 471,500 | 39.78 |
|  |  | 10S | 0.218 | 19.564 | 13.55 | 2.0878 | 5.236 | 5.12 | 937 | 467,500 | 46.06 |
|  |  | 10 | 0.250 | 19.500 | 15.51 | 2.0740 | 5.236 | 5.11 | 930 | 465,000 | 52.73 |
|  |  | 20, ST | 0.375 | 19.250 | 23.12 | 2.0211 | 5.236 | 5.04 | 902 | 451,000 | 78.60 |
|  |  | 30, XS | 0.500 | 19.000 | 30.63 | 1.9689 | 5.236 | 4.97 | 883 | 441,500 | 104.13 |
|  |  | 40 | 0.594 | 18.812 | 36.21 | 1.9302 | 5.236 | 4.92 | 866 | 433,000 | 123.06 |
|  |  | 60 | 0.812 | 18.376 | 48.95 | 1.8417 | 5.236 | 4.81 | 826 | 413,000 | 166.50 |
|  |  | 80 | 1.031 | 17.938 | 61.44 | 1.7550 | 5.236 | 4.70 | 787 | 393,500 | 208.92 |
|  |  | 100 | 1.281 | 17.438 | 75.33 | 1.6585 | 5.236 | 4.57 | 744 | 372,000 | 256.15 |
|  |  | 120 | 1.500 | 17.000 | 87.18 | 1.5763 | 5.236 | 4.45 | 707 | 353,500 | 296.37 |
|  |  | 140 | 1.750 | 16.500 | 100.3 | 1.4849 | 5.236 | 4.32 | 665 | 332,500 | 341.10 |
|  |  | 160 | 1.969 | 16.062 | 111.5 | 1.4071 | 5.236 | 4.21 | 632 | 316,000 | 379.14 |
| 24 | 24 | 5 S | 0.218 | 23.564 | 16.29 | 3.0285 | 6.283 | 6.17 | 1359 | 679,500 | 55.37 |
|  |  | 10, 10S | 0.250 | 23.500 | 18.65 | 3.012 | 6.283 | 6.15 | 1350 | 675,000 | 63.41 |
|  |  | 20, ST | 0.375 | 23.250 | 27.83 | 2.948 | 6.283 | 6.09 | 1325 | 662,500 | 94.62 |
|  |  | XS | 0.500 | 23.000 | 36.90 | 2.885 | 6.283 | 6.02 | 1295 | 642,500 | 125.49 |
|  |  | 30 | 0.562 | 22.876 | 41.39 | 2.854 | 6.283 | 5.99 | 1281 | 640,500 | 140.80 |
|  |  | 40 | 0.688 | 22.624 | 50.39 | 2.792 | 6.283 | 5.92 | 1253 | 626,500 | 171.17 |
|  |  | 60 | 0.969 | 22.062 | 70.11 | 2.655 | 6.283 | 5.78 | 1192 | 596,000 | 238.29 |
|  |  | 80 | 1.219 | 21.562 | 87.24 | 2.536 | 6.283 | 5.64 | 1138 | 569,000 | 296.53 |
|  |  | 100 | 1.531 | 20.938 | 108.1 | 2.391 | 6.283 | 5.48 | 1073 | 536,500 | 367.45 |
|  |  | 120 | 1.812 | 20.376 | 126.3 | 2.264 | 6.283 | 5.33 | 1016 | 508,000 | 429.50 |
|  |  | 140 | 2.062 | 19.876 | 142.1 | 2.155 | 6.283 | 5.20 | 965 | 482,500 | 483.24 |
|  |  | 160 | 2.344 | 19.312 | 159.5 | 2.034 | 6.283 | 5.06 | 913 | 456,500 | 542.09 |
| 30 | 30 | 5 S | 0.250 | 29.500 | 23.37 | 4.746 | 7.854 | 7.72 | 2130 | 1,065,000 | 79.43 |
|  |  | 10, 10S | 0.312 | 29.376 | 29.10 | 4.707 | 7.854 | 7.69 | 2110 | 1,055,000 | 98.93 |
|  |  | ST | 0.375 | 29.250 | 34.90 | 4.666 | 7.854 | 7.66 | 2094 | 1,048,000 | 118.65 |
|  |  | 20, XS | 0.500 | 29.000 | 46.34 | 4.587 | 7.854 | 7.59 | 2055 | 1,027,500 | 157.53 |
|  |  | 30 | 0.625 | 28.750 | 57.68 | 4.508 | 7.854 | 7.53 | 2020 | 1,010,000 | 196.08 |

[^12]Table B. 3 Dimensions of Selected Radial Low-Fin Tubing (Type S/T Trufin ${ }^{\ominus}$ ): 16 fpi Tubing

| Catalog number | Nominal outside diameter (in. (mm)) | Average plain end wall thickness (in. (mm)) | Minimum wall thickness under fin (in. (mm)) | Finned section nominal root diameter (in. (mm)) | Nominal inside diameter (in. (mm)) | Actual outside area ( $\mathrm{ft}{ }^{2} / \mathrm{ft}\left(\mathrm{m}^{2} / \mathrm{m}\right)$ ) | Area ratio actual outside/ actual inside | Approximate weight per unit length ( $\mathrm{lb} / \mathrm{ft}(\mathrm{kg} / \mathrm{m})$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 60-163049 | 1/2 (12.70) | 0.065 (1.65) | 0.044 (1.118) | 0.375 (9.53) | 0.277 (7.04) | 0.261 (0.080) | 3.60 | 0.288 (0.428) |
| 60-164065 | 5/8 (15.88) | 0.085 (2.16) | 0.058 (1.473) | 0.500 (12.70) | 0.370 (9.40) | 0.340 (0.104) | 3.51 | 0.471 (0.701) |
| 60-165065 | 3/4 (19.05) | 0.085 (2.16) | 0.058 (1.473) | 0.625 (15.89) | 0.495 (12.57) | 0.418 (0.127) | 3.23 | 0.478 (0.711) |
| 60-165083 | 3/4 (19.05) | 0.095 (2.41) | 0.074 (1.880) | 0.625 (15.89) | 0.459 (11.66) | 0.418 (0.127) | 3.48 | 0.659 (0.981) |
| 60-166065 | 7/8 (22.23) | 0.085 (2.16) | 0.058 (1.473) | 0.750 (19.05) | 0.620 (15.75) | 0.496 (0.151) | 3.06 | 0.681 (1.014) |
| 60-166083 | 7/8 (22.23) | 0.095 (2.41) | 0.074 (1.880) | 0.750 (19.05) | 0.584 (14.83) | 0.496 (0.151) | 3.24 | 0.791 (1.176) |
| 60-167083 | 1 (25.40) | 0.095 (2.41) | 0.074 (1.880) | 0.875 (22.23) | 0.709 (18.01) | 0.574 (0.175) | 3.09 | 0.899 (1.338) |

[^13]Table B. 4 Dimensions of Selected Radial Low-Fin Tubing (Type S/T Trufin ${ }^{\circledR}$ ): 19 fpi Tubing

| Catalog number | Nominal outside diameter (in. (mm)) | Average plain end wall thickness (in. (mm)) | Minimum wall thickness under fin (in. (mm)) | Finned section nominal root diameter (in. (mm)) | Nominal inside diameter (in. (mm)) | Actual outside area ( $\mathrm{ft}^{2} / \mathrm{ft}\left(\mathrm{m}^{2} / \mathrm{m}\right)$ ) | Area ratio actual outside/ actual inside | Approximate weight per unit length ( $\mathrm{lb} / \mathrm{ft}(\mathrm{kg} / \mathrm{m})$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 60-193042 | 1/2 (12.70) | 0.060 (1.52) | 0.037 (0.940) | 0.375 (9.53) | 0.291 (7.39) | 0.319 (0.097) | 4.19 | 0.239 (0.355) |
| 60-193049 | 1/2 (12.70) | 0.065 (1.65) | 0.044 (1.118) | 0.375 (9.53) | 0.277 (7.04) | 0.319 (0.097) | 4.40 | 0.284 (0.423) |
| 60-193058 | 1/2 (12.70) | 0.075 (1.91) | 0.049 (1.245) | 0.375 (9.53) | 0.259 (6.58) | 0.319 (0.097) | 4.71 | 0.286 (0.425) |
| 60-194049 | 5/8 (15.88) | 0.065 (1.65) | 0.044 (1.118) | 0.500 (12.70) | 0.402 (10.21) | 0.414 (0.126) | 3.94 | 0.362 (0.538) |
| 60-194058 | 5/8 (15.88) | 0.075 (1.91) | 0.049 (1.245) | 0.500 (12.70) | 0.384 (9.75) | 0.414 (0.126) | 4.12 | 0.396 (0.589) |
| 60-194065 | 5/8 (15.88) | 0.085 (2.16) | 0.058 (1.473) | 0.500 (12.70) | 0.370 (9.40) | 0.414 (0.126) | 4.27 | 0.456 (0.679) |
| 60-194072 | 5/8 (15.88) | 0.090 (2.29) | 0.065 (1.651) | 0.500 (12.70) | 0.356 (9.04) | 0.414 (0.126) | 4.44 | 0.447 (0.665) |
| 60-195049 | 3/4 (19.05) | 0.065 (1.65) | 0.044 (1.118) | 0.625 (15.88) | 0.527 (13.39) | 0.507 (0.155) | 3.67 | 0.447 (0.666) |
| 60-195058 | 3/4 (19.05) | 0.075 (1.91) | 0.049 (1.245) | 0.625 (15.88) | 0.509 (12.93) | 0.507 (0.155) | 3.80 | 0.485 (0.722) |
| 60-195065 | 3/4 (19.05) | 0.085 (2.16) | 0.058 (1.473) | 0.625 (15.88) | 0.495 (12.57) | 0.507 (0.155) | 3.91 | 0.568 (0.845) |
| 60-195072 | 3/4 (19.05) | 0.090 (2.29) | 0.065 (1.651) | 0.625 (15.88) | 0.481 (12.22) | 0.507 (0.155) | 4.03 | 0.592 (0.881) |
| 60-195083 | 3/4 (19.05) | 0.095 (2.41) | 0.074 (1.880) | 0.625 (15.88) | 0.459 (11.66) | 0.507 (0.155) | 4.22 | 0.618 (0.920) |
| 60-196058 | 7/8 (22.23) | 0.075 (1.91) | 0.049 (1.245) | 0.750 (19.05) | 0.634 (16.10) | 0.588 (0.179) | 3.54 | 0.595 (0.885) |
| 60-196065 | 7/8 (22.23) | 0.085 (2.16) | 0.058 (1.473) | 0.750 (19.05) | 0.620 (15.75) | 0.588 (0.179) | 3.62 | 0.675 (1.004) |
| 60-196072 | 7/8 (22.23) | 0.090 (2.29) | 0.065 (1.651) | 0.750 (19.05) | 0.606 (15.39) | 0.588 (0.179) | 3.71 | 0.689 (1.024) |
| 60-196083 | 7/8 (22.23) | 0.095 (2.41) | 0.074 (1.880) | 0.750 (19.05) | 0.584 (14.83) | 0.588 (0.179) | 3.85 | 0.762 (1.134) |
| 60-196095 | 7/8 (22.23) | 0.110 (2.79) | 0.084 (2.134) | 0.750 (19.05) | 0.560 (14.22) | 0.588 (0.179) | 4.01 | 0.835 (1.243) |
| 60-197058 | 1 (25.40) | 0.075 (1.91) | 0.049 (1.245) | 0.875 (22.23) | 0.759 (19.28) | 0.695 (0.212) | 3.50 | 0.697 (1.037) |
| 60-197065 | 1 (25.40) | 0.085 (2.16) | 0.058 (1.473) | 0.875 (22.23) | 0.745 (18.92) | 0.695 (0.212) | 3.56 | 0.757 (1.126) |
| 60-197072 | 1 (25.40) | 0.090 (2.29) | 0.065 (1.651) | 0.875 (22.23) | 0.731 (18.57) | 0.695 (0.212) | 3.63 | 0.813 (1.210) |
| 60-197083 | 1 (25.40) | 0.095 (2.41) | 0.074 (1.880) | 0.875 (22.23) | 0.709 (18.01) | 0.695 (0.212) | 3.74 | 0.873 (1.299) |
| 60-197095 | 1 (25.40) | 0.110 (2.79) | 0.084 (2.134) | 0.875 (22.23) | 0.685 (17.40) | 0.695 (0.212) | 3.88 | 0.988 (1.471) |
| 60-197109 | 1 (25.40) | 0.125 (3.18) | 0.097 (2.464) | 0.875 (22.23) | 0.657 (16.69) | 0.695 (0.212) | 4.04 | 1.135 (1.688) |

[^14]Source: Wolverine Tube, Inc., www.wlv.com

Table B. 5 Dimensions of Selected Radial Low-Fin Tubing (Type 3 Fine-Fin ${ }^{\circledR}$ ): 26 fpi Tubing

| Part number | Plain section average diameter (in. (mm)) | Plain section average wall (in. (mm)) | Wall under fin, average (in. (mm)) | Wall under fin, minimum (in. (mm)) | Nominal root diameter (in. (mm)) | Fin section ID (in. (mm)) | Outside area, $\mathrm{A}_{0}$ $\left(\mathrm{ft}^{2} / \mathrm{ft}\left(\mathrm{m}^{2} / \mathrm{m}\right)\right)$ | Inside area, $\mathrm{A}_{\mathrm{i}}$ $\left(\mathrm{ft}^{2} / \mathrm{ft}\left(\mathrm{m}^{2} / \mathrm{m}\right)\right.$ ) | Area ratio $\mathrm{A}_{0} / \mathrm{A}_{\mathrm{i}}$ | ID cross <br> sectional area $\left(\text { in. }{ }^{2}\left(\mathrm{~cm}^{2}\right)\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 264028 | 0.625 (15.875) | 0.049 (1.245) | 0.028 (0.711) | 0.025 (0.635) | 0.527 (13.386) | 0.471 (11.963) | 0.492 (0.150) | 0.123 (0.037) | 4.000 | 0.174 (1.124) |
| 264035 | 0.625 (15.875) | 0.058 (1.473) | 0.035 (0.889) | 0.031 (0.787) | 0.527 (13.386) | 0.457 (11.608) | 0.492 (0.150) | 0.120 (0.037) | 4.100 | 0.164 (1.058) |
| 264042 | 0.625 (15.875) | 0.065 (1.651) | 0.042 (1.067) | 0.037 (0.940) | 0.527 (13.386) | 0.443 (11.252) | 0.492 (0.150) | 0.116 (0.035) | 4.241 | 0.154 (0.994) |
| 264049 | 0.625 (15.875) | 0.072 (1.829) | 0.049 (1.245) | 0.044 (1.118) | 0.527 (13.386) | 0.429 (10.897) | 0.492 (0.150) | 0.112 (0.034) | 4.393 | 0.145 (0.933) |
| 264065 | 0.625 (15.875) | 0.083 (2.108) | 0.065 (1.651) | 0.058 (1.473) | 0.527 (13.386) | 0.397 (10.084) | 0.492 (0.150) | 0.104 (0.032) | 4.731 | 0.124 (0.799) |
| 265028 | 0.750 (19.050) | 0.049 (1.245) | 0.028 (0.711) | 0.025 (0.635) | 0.652 (16.561) | 0.596 (15.138) | 0.596 (0.182) | 0.156 (0.048) | 3.821 | 0.279 (1.800) |
| 265035 | 0.750 (19.050) | 0.058 (1.473) | 0.035 (0.889) | 0.031 (0.787) | 0.652 (16.561) | 0.582 (14.783) | 0.596 (0.182) | 0.152 (0.046) | 3.921 | 0.266 (1.716) |
| 265042 | 0.750 (19.050) | 0.065 (1.651) | 0.042 (1.067) | 0.037 (0.940) | 0.652 (16.561) | 0.568 (14.427) | 0.596 (0.182) | 0.149 (0.045) | 4.000 | 0.253 (1.635) |
| 265049 | 0.750 (19.050) | 0.072 (1.829) | 0.049 (1.245) | 0.044 (1.118) | 0.652 (16.561) | 0.554 (14.072) | 0.596 (0.182) | 0.145 (0.044) | 4.110 | 0.241 (1.555) |
| 265065 | 0.750 (19.050) | 0.083 (2.108) | 0.065 (1.651) | 0.058 (1.473) | 0.652 (16.561) | 0.522 (13.259) | 0.596 (0.182) | 0.137 (0.042) | 4.350 | 0.214 (1.381) |
| 265083 | 0.750 (19.050) | 0.109 (2.769) | 0.083 (2.108) | 0.074 (1.880) | 0.652 (16.561) | 0.486 (12.344) | 0.596 (0.182) | 0.127 (0.039) | 4.693 | 0.186 (1.197) |
| 266028 | 0.875 (22.225) | 0.049 (1.245) | 0.028 (0.711) | 0.025 (0.635) | 0.777 (19.736) | 0.721 (18.313) | 0.704 (0.215) | 0.189 (0.058) | 3.725 | 0.408 (2.634) |
| 266035 | 0.875 (22.225) | 0.058 (1.473) | 0.035 (0.889) | 0.031 (0.787) | 0.777 (19.736) | 0.707 (17.958) | 0.704 (0.215) | 0.185 (0.056) | 3.805 | 0.393 (2.533) |
| 266042 | 0.875 (22.225) | 0.065 (1.651) | 0.042 (1.067) | 0.037 (0.940) | 0.777 (19.736) | 0.693 (17.602) | 0.704 (0.215) | 0.181 (0.055) | 3.890 | 0.377 (2.433) |
| 266049 | 0.875 (22.225) | 0.072 (1.829) | 0.049 (1.245) | 0.044 (1.118) | 0.777 (19.736) | 0.679 (17.247) | 0.704 (0.215) | 0.178 (0.054) | 3.955 | 0.362 (2.336) |
| 266065 | 0.875 (22.225) | 0.083 (2.108) | 0.065 (1.651) | 0.058 (1.473) | 0.777 (19.736) | 0.647 (16.434) | 0.704 (0.215) | 0.169 (0.052) | 4.166 | 0.329 (2.121) |
| 266083 | 0.875 (22.225) | 0.109 (2.769) | 0.083 (2.108) | 0.074 (1.880) | 0.777 (19.736) | 0.611 (15.519) | $0.704(0.215)$ | 0.160 (0.049) | 4.400 | 0.293 (1.892) |
| 267035 | 1.000 (25.400) | 0.058 (1.473) | 0.035 (0.889) | 0.031 (0.787) | 0.902 (22.911) | 0.832 (21.133) | 0.811 (0.247) | 0.218 (0.066) | 3.720 | 0.544 (3.508) |
| 267042 | 1.000 (25.400) | 0.065 (1.651) | 0.042 (1.067) | 0.037 (0.940) | 0.902 (22.911) | 0.818 (20.777) | 0.811 (0.247) | 0.214 (0.065) | 3.790 | 0.526 (3.391) |
| 267049 | 1.000 (25.400) | 0.072 (1.829) | 0.049 (1.245) | 0.044 (1.118) | 0.902 (22.911) | 0.804 (20.422) | 0.811 (0.247) | 0.210 (0.064) | 3.862 | 0.508 (3.275) |
| 267065 | 1.000 (25.400) | 0.083 (2.108) | 0.065 (1.651) | 0.058 (1.473) | 0.902 (22.911) | 0.772 (19.609) | 0.811 (0.247) | 0.202 (0.062) | 4.015 | 0.468 (3.020) |
| 267083 | 1.000 (25.400) | 0.109 (2.769) | 0.083 (2.108) | 0.074 (1.880) | 0.902 (22.911) | 0.736 (18.694) | 0.811 (0.247) | 0.193 (0.059) | 4.202 | 0.425 (2.745) |

[^15]
## Appendix C:Tube-Count Tables

Source for this Appendix: Nooter Corporation, St. Louis, MO. Orginally published in Ref. [11].

Table C. 1 Tube Counts for 5/8-in. OD Tubes on 13/16-in. Square Pitch

| Shell ID (in.) | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 55 | 48 | 34 | 24 | 52 | 40 | 32 |
| 10 | 88 | 78 | 62 | 56 | 90 | 80 | 74 |
| 12 | 140 | 138 | 112 | 100 | 140 | 128 | 108 |
| 13.25 | 178 | 172 | 146 | 136 | 180 | 164 | 148 |
| 15.25 | 245 | 232 | 208 | 192 | 246 | 232 | 216 |
| 17.25 | 320 | 308 | 274 | 260 | 330 | 312 | 292 |
| 19.25 | 405 | 392 | 352 | 336 | 420 | 388 | 368 |
| 21.25 | 502 | 484 | 442 | 424 | 510 | 488 | 460 |
| 23.25 | 610 | 584 | 536 | 508 | 626 | 596 | 562 |
| 25 | 700 | 676 | 618 | 600 | 728 | 692 | 644 |
| 27 | 843 | 812 | 742 | 716 | 856 | 816 | 780 |
| 29 | 970 | 942 | 868 | 840 | 998 | 956 | 920 |
| 31 | 1127 | 1096 | 1014 | 984 | 1148 | 1108 | 1060 |
| 33 | 1288 | 1250 | 1172 | 1148 | 1318 | 1268 | 1222 |
| 35 | 1479 | 1438 | 1330 | 1308 | 1492 | 1436 | 1388 |
| 37 | 1647 | 1604 | 1520 | 1480 | 1684 | 1620 | 1568 |
| 39 | 1840 | 1794 | 1700 | 1664 | 1882 | 1816 | 1754 |
| 42 | 2157 | 2112 | 2004 | 1968 | 2196 | 2136 | 2068 |
| 45 | 2511 | 2458 | 2326 | 2288 | 2530 | 2464 | 2402 |
| 48 | 2865 | 2808 | 2686 | 2656 | 2908 | 2832 | 2764 |
| 54 | 3656 | 3600 | 3462 | 3404 | 3712 | 3624 | 3556 |
| 60 | 4538 | 4472 | 4310 | 4256 | 4608 | 4508 | 4426 |

Table C. 2 Tube Counts for 3/4-in. OD Tubes on 15/16-in. Triangular Pitch

| Shell ID <br> (in.) | TEMA L or M |  |  |  | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 64 | 48 | 34 | 24 | 34 | 32 | 16 | 18 | 32 | 24 | 24 |
| 10 | 85 | 72 | 52 | 50 | 60 | 62 | 52 | 44 | 64 | 52 | 52 |
| 12 | 122 | 114 | 94 | 96 | 109 | 98 | 78 | 68 | 98 | 88 | 78 |
| 13.25 | 151 | 142 | 124 | 112 | 126 | 120 | 106 | 100 | 126 | 116 | 108 |
| 15.25 | 204 | 192 | 166 | 168 | 183 | 168 | 146 | 136 | 180 | 160 | 148 |
| 17.25 | 264 | 254 | 228 | 220 | 237 | 228 | 202 | 192 | 238 | 224 | 204 |
| 19.25 | 332 | 326 | 290 | 280 | 297 | 286 | 258 | 248 | 298 | 280 | 262 |
| 21.25 | 417 | 396 | 364 | 348 | 372 | 356 | 324 | 316 | 370 | 352 | 334 |
| 23.25 | 495 | 478 | 430 | 420 | 450 | 430 | 392 | 376 | 456 | 428 | 408 |
| 25 | 579 | 554 | 512 | 488 | 518 | 498 | 456 | 444 | 534 | 500 | 474 |
| 27 | 676 | 648 | 602 | 584 | 618 | 602 | 548 | 532 | 628 | 600 | 570 |
| 29 | 785 | 762 | 704 | 688 | 729 | 708 | 650 | 624 | 736 | 696 | 668 |
| 31 | 909 | 878 | 814 | 792 | 843 | 812 | 744 | 732 | 846 | 812 | 780 |
| 33 | 1035 | 1002 | 944 | 920 | 962 | 934 | 868 | 840 | 978 | 928 | 904 |
| 35 | 1164 | 1132 | 1062 | 1036 | 1090 | 1064 | 990 | 972 | 1100 | 1060 | 1008 |
| 37 | 1304 | 1270 | 1200 | 1168 | 1233 | 1196 | 1132 | 1100 | 1238 | 1200 | 1152 |
| 39 | 1460 | 1422 | 1338 | 1320 | 1365 | 1346 | 1266 | 1244 | 1390 | 1336 | 1290 |
| 42 | 1703 | 1664 | 1578 | 1552 | 1611 | 1580 | 1498 | 1464 | 1632 | 1568 | 1524 |
| 45 | 1960 | 1918 | 1830 | 1800 | 1875 | 1834 | 1736 | 1708 | 1882 | 1820 | 1770 |
| 48 | 2242 | 2196 | 2106 | 2060 | 2132 | 2100 | 1998 | 1964 | 2152 | 2092 | 2044 |
| 54 | 2861 | 2804 | 2682 | 2660 | 2730 | 2684 | 2574 | 2536 | 2748 | 2680 | 2628 |
| 60 | 3527 | 3476 | 3360 | 3300 | 3395 | 3346 | 3228 | 3196 | 3420 | 3340 | 3286 |
| 66 | 4292 | 4228 | 4088 | 4044 |  |  |  |  |  |  |  |
| 72 | 5116 | 5044 | 4902 | 4868 |  |  |  |  |  |  |  |
| 78 | 6034 | 5964 | 5786 | 5740 |  |  |  |  |  |  |  |
| 84 | 7005 | 6934 | 6766 | 6680 |  |  |  |  |  |  |  |
| 90 | 8093 | 7998 | 7832 | 7708 |  |  |  |  |  |  |  |
| 96 | 9203 | 9114 | 8896 | 8844 |  |  |  |  |  |  |  |
| 108 | 11696 | 11618 | 11336 | 11268 |  |  |  |  |  |  |  |
| 120 | 14459 | 14378 | 14080 | 13984 |  |  |  |  |  |  |  |

Table C. 3 Tube Counts for 3/4-in. OD Tubes on 1-in. Square Pitch

| Shell ID (in.) | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 28 | 26 | 16 | 12 | 28 | 24 | 12 |
| 10 | 52 | 48 | 44 | 24 | 52 | 44 | 32 |
| 12 | 80 | 76 | 66 | 56 | 78 | 72 | 70 |
| 131/4 | 104 | 90 | 70 | 80 | 96 | 92 | 90 |
| 151/4 | 136 | 128 | 128 | 114 | 136 | 132 | 120 |
| 171/4 | 181 | 174 | 154 | 160 | 176 | 176 | 160 |
| 191/4 | 222 | 220 | 204 | 198 | 224 | 224 | 224 |
| 211/4 | 289 | 272 | 262 | 260 | 284 | 280 | 274 |
| $23^{1 / 4}$ | 345 | 332 | 310 | 308 | 348 | 336 | 328 |
| 25 | 398 | 386 | 366 | 344 | 408 | 392 | 378 |
| 27 | 477 | 456 | 432 | 424 | 480 | 468 | 460 |
| 29 | 554 | 532 | 510 | 496 | 562 | 548 | 530 |
| 31 | 637 | 624 | 588 | 576 | 648 | 636 | 620 |
| 33 | 730 | 712 | 682 | 668 | 748 | 728 | 718 |
| 35 | 828 | 812 | 780 | 760 | 848 | 820 | 816 |
| 37 | 937 | 918 | 882 | 872 | 952 | 932 | 918 |
| 39 | 1048 | 1028 | 996 | 972 | 1056 | 1044 | 1020 |
| 42 | 1224 | 1200 | 1170 | 1140 | 1244 | 1224 | 1212 |
| 45 | 1421 | 1394 | 1350 | 1336 | 1436 | 1408 | 1398 |
| 48 | 1628 | 1598 | 1548 | 1536 | 1640 | 1628 | 1602 |
| 54 | 2096 | 2048 | 2010 | 1992 | 2108 | 2084 | 2068 |
| 60 | 2585 | 2552 | 2512 | 2476 | 2614 | 2584 | 2558 |

Table C. 4 Tube Counts for 3/4-in. OD Tubes on 1-in. Triangular Pitch

| Shell ID <br> (in.) | TEMA L or M |  |  |  | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 42 | 40 | 26 | 24 | 31 | 26 | 16 | 12 | 32 | 24 | 24 |
| 10 | 73 | 66 | 52 | 44 | 56 | 48 | 42 | 40 | 52 | 48 | 40 |
| 12 | 109 | 102 | 88 | 80 | 88 | 78 | 62 | 68 | 84 | 76 | 74 |
| $13^{1 / 4}$ | 136 | 128 | 112 | 102 | 121 | 106 | 94 | 88 | 110 | 100 | 98 |
| $15^{1 / 4}$ | 183 | 172 | 146 | 148 | 159 | 148 | 132 | 132 | 152 | 140 | 136 |
| $17^{1 / 4}$ | 237 | 228 | 208 | 192 | 208 | 198 | 182 | 180 | 206 | 188 | 182 |
| 191/4 | 295 | 282 | 258 | 248 | 258 | 250 | 228 | 220 | 266 | 248 | 234 |
| $21^{1 / 4}$ | 361 | 346 | 318 | 320 | 320 | 314 | 290 | 276 | 330 | 316 | 296 |
| $23^{1 / 4}$ | 438 | 416 | 382 | 372 | 400 | 384 | 352 | 336 | 400 | 384 | 356 |
| 25 | 507 | 486 | 448 | 440 | 450 | 442 | 400 | 392 | 472 | 440 | 424 |
| 27 | 592 | 574 | 536 | 516 | 543 | 530 | 488 | 468 | 554 | 528 | 502 |
| 29 | 692 | 668 | 632 | 604 | 645 | 618 | 574 | 556 | 648 | 616 | 588 |
| 31 | 796 | 774 | 732 | 708 | 741 | 716 | 666 | 648 | 744 | 716 | 688 |
| 33 | 909 | 886 | 836 | 812 | 843 | 826 | 760 | 740 | 852 | 816 | 788 |
| 35 | 1023 | 1002 | 942 | 920 | 950 | 930 | 878 | 856 | 974 | 932 | 908 |
| 37 | 1155 | 1124 | 1058 | 1032 | 1070 | 1052 | 992 | 968 | 1092 | 1056 | 1008 |
| 39 | 1277 | 1254 | 1194 | 1164 | 1209 | 1184 | 1122 | 1096 | 1224 | 1180 | 1146 |
| 42 | 1503 | 1466 | 1404 | 1372 | 1409 | 1378 | 1314 | 1296 | 1434 | 1388 | 1350 |
| 45 | 1726 | 1690 | 1622 | 1588 | 1635 | 1608 | 1536 | 1504 | 1652 | 1604 | 1560 |
| 48 | 1964 | 1936 | 1870 | 1828 | 1887 | 1842 | 1768 | 1740 | 1894 | 1844 | 1794 |
| 54 | 2519 | 2466 | 2380 | 2352 | 2399 | 2366 | 2270 | 2244 | 2426 | 2368 | 2326 |
| 60 | 3095 | 3058 | 2954 | 2928 | 2981 | 2940 | 2832 | 2800 | 3006 | 2944 | 2884 |
| 66 | 3769 | 3722 | 3618 | 3576 |  |  |  |  |  |  |  |
| 72 | 4502 | 4448 | 4324 | 4280 |  |  |  |  |  |  |  |
| 78 | 5309 | 5252 | 5126 | 5068 |  |  |  |  |  |  |  |
| 84 | 6162 | 6108 | 5964 | 5900 |  |  |  |  |  |  |  |
| 90 | 7103 | 7040 | 6898 | 6800 |  |  |  |  |  |  |  |
| 96 | 8093 | 8026 | 7848 | 7796 |  |  |  |  |  |  |  |
| 108 | 10260 | 10206 | 9992 | 9940 |  |  |  |  |  |  |  |
| 120 | 12731 | 12648 | 12450 | 12336 |  |  |  |  |  |  |  |

Table C. 5 Tube Counts for 1-in. OD Tubes on 1.25-in. Square Pitch

| Shell ID (in.) | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 17 | 12 | 8 | 12 | 14 | 8 | 6 |
| 10 | 30 | 30 | 16 | 18 | 30 | 24 | 12 |
| 12 | 52 | 48 | 42 | 24 | 44 | 40 | 32 |
| $13^{1 / 4}$ | 61 | 56 | 52 | 50 | 60 | 48 | 44 |
| $15^{1 / 4}$ | 85 | 78 | 62 | 64 | 80 | 72 | 74 |
| $171 / 4$ | 108 | 108 | 104 | 96 | 104 | 100 | 100 |
| 191/4 | 144 | 136 | 130 | 114 | 132 | 132 | 120 |
| $21^{1 / 4}$ | 173 | 166 | 154 | 156 | 172 | 168 | 148 |
| 231/4 | 217 | 208 | 194 | 192 | 212 | 204 | 198 |
| 25 | 252 | 240 | 230 | 212 | 244 | 240 | 230 |
| 27 | 296 | 280 | 270 | 260 | 290 | 284 | 274 |
| 29 | 345 | 336 | 310 | 314 | 340 | 336 | 328 |
| 31 | 402 | 390 | 366 | 368 | 400 | 384 | 372 |
| 33 | 461 | 452 | 432 | 420 | 456 | 444 | 440 |
| 35 | 520 | 514 | 494 | 484 | 518 | 504 | 502 |
| 37 | 588 | 572 | 562 | 548 | 584 | 576 | 566 |
| 39 | 661 | 640 | 624 | 620 | 664 | 644 | 640 |
| 42 | 776 | 756 | 738 | 724 | 764 | 748 | 750 |
| 45 | 900 | 882 | 862 | 844 | 902 | 880 | 862 |
| 48 | 1029 | 1016 | 984 | 972 | 1028 | 1008 | 1004 |
| 54 | 1310 | 1296 | 1268 | 1256 | 1320 | 1296 | 1284 |
| 60 | 1641 | 1624 | 1598 | 1576 | 1634 | 1616 | 1614 |

Table C. 6 Tube Counts for 1-in. OD Tubes on 1.25-in. Triangular Pitch

| Shell ID (in.) | TEMA L or M |  |  |  | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 27 | 26 | 8 | 12 | 18 | 14 | 8 | 12 | 14 | 12 | 6 |
| 10 | 42 | 40 | 34 | 24 | 33 | 28 | 16 | 18 | 28 | 24 | 24 |
| 12 | 64 | 66 | 52 | 44 | 51 | 48 | 42 | 44 | 52 | 40 | 40 |
| $13^{1 / 4}$ | 81 | 74 | 62 | 56 | 73 | 68 | 52 | 44 | 64 | 56 | 52 |
| $151 / 4$ | 106 | 106 | 88 | 92 | 93 | 90 | 78 | 76 | 90 | 80 | 78 |
| $171 / 4$ | 147 | 134 | 124 | 114 | 126 | 122 | 112 | 102 | 122 | 112 | 102 |
| 191/4 | 183 | 176 | 150 | 152 | 159 | 152 | 132 | 136 | 152 | 140 | 136 |
| $211 / 4$ | 226 | 220 | 204 | 186 | 202 | 192 | 182 | 172 | 196 | 180 | 176 |
| $231 / 4$ | 268 | 262 | 236 | 228 | 249 | 238 | 216 | 212 | 242 | 224 | 216 |
| 25 | 316 | 302 | 274 | 272 | 291 | 278 | 250 | 240 | 286 | 264 | 246 |
| 27 | 375 | 360 | 336 | 324 | 345 | 330 | 298 | 288 | 340 | 320 | 300 |
| 29 | 430 | 416 | 390 | 380 | 400 | 388 | 356 | 348 | 400 | 380 | 352 |
| 31 | 495 | 482 | 452 | 448 | 459 | 450 | 414 | 400 | 456 | 436 | 414 |
| 33 | 579 | 554 | 520 | 504 | 526 | 514 | 484 | 464 | 526 | 504 | 486 |
| 35 | 645 | 622 | 586 | 576 | 596 | 584 | 548 | 536 | 596 | 572 | 548 |
| 37 | 729 | 712 | 662 | 648 | 672 | 668 | 626 | 608 | 668 | 636 | 614 |
| 39 | 808 | 792 | 744 | 732 | 756 | 736 | 704 | 692 | 748 | 728 | 700 |
| 42 | 947 | 918 | 874 | 868 | 890 | 878 | 834 | 808 | 890 | 856 | 830 |
| 45 | 1095 | 1068 | 1022 | 1000 | 1035 | 1008 | 966 | 948 | 1028 | 992 | 972 |
| 48 | 1241 | 1220 | 1176 | 1148 | 1181 | 1162 | 1118 | 1092 | 1180 | 1136 | 1100 |
| 54 | 1577 | 1572 | 1510 | 1480 | 1520 | 1492 | 1436 | 1416 | 1508 | 1468 | 1442 |
| 60 | 1964 | 1940 | 1882 | 1832 | 1884 | 1858 | 1800 | 1764 | 1886 | 1840 | 1794 |
| 66 | 2390 | 2362 | 2282 | 2260 |  |  |  |  |  |  |  |
| 72 | 2861 | 2828 | 2746 | 2708 |  |  |  |  |  |  |  |
| 78 | 3368 | 3324 | 3236 | 3216 |  |  |  |  |  |  |  |
| 84 | 3920 | 3882 | 3784 | 3736 |  |  |  |  |  |  |  |
| 90 | 4499 | 4456 | 4370 | 4328 |  |  |  |  |  |  |  |
| 96 | 5144 | 5104 | 4986 | 4936 |  |  |  |  |  |  |  |
| 108 | 6546 | 6494 | 6360 | 6300 |  |  |  |  |  |  |  |
| 120 | 8117 | 8038 | 7870 | 7812 |  |  |  |  |  |  |  |

Table C. 7 Tube Counts for 1.25-in. OD Tubes on 19/16-in. Square Pitch

| Shell ID (in.) | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 12 | 12 | 4 | 0 | 4 | 4 | 6 |
| 10 | 21 | 12 | 8 | 12 | 12 | 8 | 12 |
| 12 | 29 | 28 | 16 | 18 | 26 | 20 | 12 |
| $13^{1 / 4}$ | 38 | 34 | 34 | 24 | 36 | 28 | 15 |
| 151/4 | 52 | 48 | 44 | 48 | 44 | 44 | 32 |
| $171 / 4$ | 70 | 66 | 56 | 50 | 60 | 60 | 56 |
| 191/4 | 85 | 84 | 70 | 80 | 82 | 76 | 79 |
| $21^{1 / 4}$ | 108 | 108 | 100 | 96 | 100 | 100 | 100 |
| $23^{1 / 4}$ | 136 | 128 | 128 | 114 | 128 | 120 | 120 |
| 25 | 154 | 154 | 142 | 136 | 154 | 148 | 130 |
| 27 | 184 | 180 | 158 | 172 | 176 | 172 | 160 |
| 29 | 217 | 212 | 204 | 198 | 212 | 204 | 198 |
| 31 | 252 | 248 | 234 | 236 | 242 | 240 | 234 |
| 33 | 289 | 276 | 270 | 264 | 280 | 280 | 274 |
| 35 | 329 | 316 | 310 | 304 | 324 | 312 | 308 |
| 37 | 372 | 368 | 354 | 340 | 358 | 352 | 350 |
| 39 | 420 | 402 | 402 | 392 | 408 | 400 | 392 |
| 42 | 485 | 476 | 468 | 464 | 480 | 476 | 464 |
| 45 | 565 | 554 | 546 | 544 | 558 | 548 | 550 |
| 48 | 653 | 636 | 628 | 620 | 644 | 628 | 632 |
| 54 | 837 | 820 | 812 | 804 | 824 | 808 | 808 |
| 60 | 1036 | 1028 | 1012 | 1008 | 1028 | 1016 | 1008 |

Table C. 8 Tube Counts for 1.25-in. OD Tubes on 19/16-in. Triangular Pitch

| Shell ID <br> (in.) | TEMA L or M |  |  |  | TEMA P or S |  |  |  | TEMA U |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of passes |  |  |  | Number of passes |  |  |  | Number of passes |  |  |
|  | 1 | 2 | 4 | 6 | 1 | 2 | 4 | 6 | 2 | 4 | 6 |
| 8 | 15 | 10 | 8 | 12 | 13 | 10 | 4 | 0 | 6 | 4 | 6 |
| 10 | 27 | 22 | 16 | 12 | 18 | 20 | 8 | 12 | 14 | 12 | 12 |
| 12 | 38 | 36 | 26 | 24 | 33 | 26 | 26 | 18 | 28 | 20 | 18 |
| $13^{1 / 4}$ | 55 | 44 | 42 | 40 | 38 | 44 | 34 | 24 | 34 | 28 | 30 |
| $15^{1 / 4}$ | 66 | 64 | 52 | 50 | 57 | 58 | 48 | 44 | 52 | 48 | 40 |
| 171/4 | 88 | 82 | 78 | 68 | 81 | 72 | 62 | 68 | 72 | 68 | 64 |
| 191/4 | 117 | 106 | 98 | 96 | 100 | 94 | 86 | 80 | 90 | 84 | 78 |
| $21^{1 / 4}$ | 136 | 134 | 124 | 108 | 126 | 120 | 116 | 102 | 118 | 112 | 102 |
| 231/4 | 170 | 164 | 146 | 148 | 159 | 146 | 132 | 132 | 148 | 132 | 120 |
| 25 | 198 | 188 | 166 | 168 | 183 | 172 | 150 | 148 | 172 | 160 | 152 |
| 27 | 237 | 228 | 208 | 192 | 208 | 206 | 190 | 180 | 200 | 188 | 180 |
| 29 | 268 | 266 | 242 | 236 | 249 | 238 | 224 | 220 | 242 | 228 | 216 |
| 31 | 312 | 304 | 284 | 276 | 291 | 282 | 262 | 256 | 282 | 264 | 250 |
| 33 | 357 | 346 | 322 | 324 | 333 | 326 | 298 | 296 | 326 | 308 | 292 |
| 35 | 417 | 396 | 372 | 364 | 372 | 368 | 344 | 336 | 362 | 344 | 336 |
| 37 | 446 | 446 | 422 | 408 | 425 | 412 | 394 | 384 | 416 | 396 | 384 |
| 39 | 506 | 490 | 472 | 464 | 478 | 468 | 442 | 432 | 472 | 444 | 428 |
| 42 | 592 | 584 | 552 | 544 | 558 | 546 | 520 | 512 | 554 | 524 | 510 |
| 45 | 680 | 676 | 646 | 632 | 646 | 634 | 606 | 596 | 636 | 624 | 592 |
| 48 | 788 | 774 | 736 | 732 | 748 | 732 | 704 | 696 | 736 | 708 | 692 |
| 54 | 1003 | 980 | 952 | 928 | 962 | 952 | 912 | 892 | 946 | 916 | 890 |
| 60 | 1237 | 1228 | 1188 | 1152 | 1194 | 1182 | 1144 | 1116 | 1176 | 1148 | 1116 |
| 66 | 1520 | 1496 | 1448 | 1424 |  |  |  |  |  |  |  |
| 72 | 1814 | 1786 | 1736 | 1724 |  |  |  |  |  |  |  |
| 78 | 2141 | 2116 | 2068 | 2044 |  |  |  |  |  |  |  |
| 84 | 2507 | 2470 | 2392 | 2372 |  |  |  |  |  |  |  |
| 90 | 2861 | 2840 | 2764 | 2744 |  |  |  |  |  |  |  |
| 96 | 3275 | 3246 | 3158 | 3156 |  |  |  |  |  |  |  |
| 108 | 4172 | 4136 | 4046 | 4020 |  |  |  |  |  |  |  |
| 120 | 5164 | 5128 | 5038 | 5000 |  |  |  |  |  |  |  |

## Appendix D: Equivalent Lengths of Pipe Fittings

Source for this appendix: Ref. [13].
Table D. 1 Equivalent Lengths (ft) of Elbows, Tees and Bends

| Nominal pipe size (in.) | $90^{\circ}$ elbows* |  | $90^{\circ}$ bends* |  | Tee |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Short radius, $R=1 D$ | Long radius, $R=1.5 \mathrm{D}$ | $R=5 D$ | $R=10 \mathrm{D}$ | Flowthrough branch $\xlongequal{\prime \prime}$ | Flowthrough $\qquad$ |
| $11 / 2$ | 4.5 | 3 | 2.5 | 4 | 8 | 3 |
| 2 | 5.25 | 3.5 | 3 | 5 | 11 | 3.5 |
| $2^{1 / 2}$ | 6 | 4 | 3.5 | 6 | 13 | 4 |
| 3 | 7.5 | 5 | 4 | 7.5 | 16 | 5 |
| 4 | 10.5 | 7 | 5.5 | 10 | 20 | 7 |
| 6 | 15 | 10 | 8.5 | 15 | 30 | 10 |
| 8 | 21 | 14 | 11 | 20 | 40 | 14 |
| 10 | 24 | 16 | 14 | 25 | 50 | 16 |
| 12 | 32 | 21 | 16 | 30 | 60 | 21 |
| 14 | 33 | 22 | 19 | 33 | 65 | 22 |
| 16 | 39 | 26 | 21 | 38 | 75 | 26 |
| 18 | 44 | 29 | 24 | 42 | 86 | 29 |
| 20 | 48 | 32 | 27 | 50 | 100 | 32 |
| 24 | 57 | 38 | 32 | 60 | 120 | 38 |

[^16]Table D. 2 Equivalent Lengths (ft) for Valves

| Nominal pipe <br> size <br> (in.) | Gate fully open | Globe* fully open bevel or plug seat |  |  | Check |  | Straightthrough cock ${ }^{1}$ | Three-way cock $^{2}$ |  | Butterfly fully open |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Swin | Ball |  | Straight- |  |  |
|  |  | $+90^{\circ}$ |  |  |  |  |  | through flows | through branch |  |
| $11 / 2$ | 1.75 | 46 | 23 | 18 | 17 | 20 | 2.5 | 6 | 20 | 6 |
| 2 | 2.25 | 60 | 30 | 24 | 22 | 25 | 3.5 | 7.5 | 24 | 8 |
| $2^{1 / 2}$ | 2.75 | 70 | 38 | 30 | 27 | 30 | 4 | 9 | 30 | 10 |
| 3 | 3.5 | 90 | 45 | 38 | 35 | 38 | 5 | 12 | 36 | 12 |
| 4 | 4.5 | 120 | 60 | 48 | 45 | 50 | 6.5 | 15 | 48 | 15 |
| 6 | 6.5 | 175 | 88 | 72 | 65 | 75 | 10 | 22 | 70 | 23 |
| 8 | 9 | 230 | 120 | 95 | 90 | 100 | 13 | 30 | 95 | 27 |
| 10 | 12 | 280 | 150 | 130 | 120 | 130 | 16 | 38 | 120 | 35 |
| 12 | 14 | 320 | 170 | 145 | 140 | 150 | 19 |  |  | 40 |
| 14 | 15 | 380 | 190 | 160 | 150 | 170 | 20 |  |  | 45 |
| 16 | 17 | 420 | 220 | 180 | 170 | 190 | 22 |  |  | 50 |
| 18 | 18 | 480 | 250 | 205 | 180 | 210 | 24 |  |  | 58 |
| 20 | 20 | 530 | 290 | 240 | 200 | 240 | 27 |  |  | 64 |
| 24 | 32 | 630 | 330 | 270 | 250 | 290 | 33 |  |  | 78 |

[^17]Table D. 3 Equivalent Lengths (ft) of Inlets and Outlets

| Resistance coefficient | $K=1.0$ | $K=0.78$ | $K=0.5$ | $K=0.23$ |
| :---: | :---: | :---: | :---: | :---: |
| Nominal pipe size (in.) | $\stackrel{\square}{\vec{Z}}$ | $\frac{1}{\rightarrow}$ | $\stackrel{\bigsqcup}{\stackrel{L}{\Gamma}}$ |  |
| 1/2 | 2 | 1.5 | 1 | 0.5 |
| $3 / 4$ | 3 | 2.5 | 1.5 | 0.75 |
| 1 | 4 | 3 | 2 | 1 |
| $11 / 2$ | 7 | 5.5 | 3.5 | 1.75 |
| 2 | 9 | 7 | 4.5 | 2.25 |
| 3 | 15 | 12 | 7.5 | 3.75 |
| 4 | 20 | 16 | 10 | 5 |
| 6 | 36 | 29 | 18 | 9 |
| 8 | 48 | 38 | 24 | 12 |
| 10 | 62 | 49 | 31 | 15 |
| 12 | 78 | 60 | 39 | 19 |
| 14 | 88 | 70 | 44 | 22 |
| 16 | 100 | 78 | 50 | 25 |
| 18 | 120 | 95 | 60 | 30 |
| 20 | 136 | 107 | 68 | 34 |
| 24 | 170 | 135 | 85 | 42 |

Table D. 4 Equivalent Lengths (ft) of Expanders and Reducers

| Nominal sizes (in.) |  | $\begin{aligned} & D_{2} \xlongequal{\square} D_{1} \\ & D_{2} \longmapsto D_{1} \end{aligned}$ | $\begin{aligned} & D_{1} \frac{\square}{\rightleftarrows} D_{2} \\ & D_{1} \square D_{2} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| $D_{1}$ | $D_{2}$ |  |  |
| $3 / 4$ | 1/2 | 0.6 | 0.5 |
| 1 | 1/2 | 1.2 | 0.7 |
|  | $3 / 4$ | 0.6 | 0.6 |
| $11 / 2$ | $3 / 4$ | 1.6 | 1.0 |
|  | 1 | 1.2 | 0.9 |
| 2 | 1 | 2.2 | 1.3 |
|  | $1^{1 / 2}$ | 1.3 | 1.3 |
| 3 | $11 / 2$ | 3.8 | 2.4 |
|  | 2 | 2.7 | 2.3 |
| 4 | 2 | 5 | 3.2 |
|  | 3 | 3 | 3 |
| 6 | 3 | 8 | 5 |
|  | 4 | 4 | 4 |
| 8 | 4 | 12 | 7 |
|  | 6 | 7 | 7 |
| 10 | 4 | 15 | 8 |
|  | 6 | 14 | 9.5 |
|  | 8 | 6 | 6 |
| 12 | 6 | 19 | 12 |
|  | 8 | 14 | 12 |
|  | 10 | 6.5 | 6.5 |
| 14 | 6 | 22 | 14 |
|  | 8 | 22 | 14 |
|  | 10 | 15 | 13 |
|  | 12 | 6 | 6 |
| 16 | 8 | 27 | 17 |
|  | 10 | 23 | 17 |
|  | 12 | 15 | 15 |
|  | 14 | 7 | 7 |
| 18 | 10 | 30 | 19 |
|  | 12 | 23 | 19 |
|  | 14 | 15 | 15 |
|  | 16 | 4 | 4 |
| 20 | 12 | 30 | 23 |
|  | 14 | 21 | 23 |
|  | 16 | 13 | 13 |
|  | 18 | 5 | 5 |
| 24 | 18 | 25 | 25 |
|  | 20 | 12 | 12 |

Note: Add these equivalent lengths to the equivalent length of the smaller pipe and its components.

## Appendix E: Properties of Petroleum Streams

Crude oils and petroleum fractions are complex mixtures containing large numbers of chemical species, primarily hydrocarbons. Methods have been devised for correlating the physical properties of these mixtures in terms of readily measurable parameters. Flowsheet simulators such as HEXTRAN have built-in correlations that are used to estimate the physical properties needed for simulation purposes. Assay data in the form of ASTM boiling curves can be used as input for petroleum streams. However, physical properties can also be estimated with just two pieces of information, namely, the standard density and the average normal boiling point of the liquid. This information is usually supplied in the form of two parameters commonly used in petroleum correlations, the API gravity and the Watson characterization factor (also called the UOP characterization factor).

The API gravity is defined as follows:

$$
\begin{equation*}
{ }^{\circ} A P I=\frac{141.5}{s}-131.5 \tag{E.1}
\end{equation*}
$$

where $s$ is the liquid specific gravity of the material at $60^{\circ} \mathrm{F}$ referenced to water at $60^{\circ} \mathrm{F}$. The inverse relation is:

$$
\begin{equation*}
s=\frac{141.5}{{ }^{\circ} A P I+131.5} \tag{E.2}
\end{equation*}
$$

The API gravity ranges from less than zero for heavy residual oils to $340^{\circ}$ for methane (liquid specific gravity of 0.30 at $60^{\circ} \mathrm{F}$ ). A range of $10-70^{\circ}$ is typical of many petroleum liquids. Note that a specific gravity of 1.0 corresponds to $10^{\circ} \mathrm{API}$. Fluids that are denser than water have lower API gravities, while a value above $10^{\circ} \mathrm{API}$ indicates that the liquid hydrocarbon is less dense than water.

The Watson (or UOP) characterization factor, $K_{w}$, is defined as follows:

$$
\begin{equation*}
K_{w}=\frac{T_{\mathrm{B}}^{1 / 3}}{s} \tag{E.3}
\end{equation*}
$$

where
$T_{\mathrm{B}}=$ average normal boiling point ( ${ }^{\circ} \mathrm{R}$ )
$s=$ liquid specific gravity at $60^{\circ} \mathrm{F}$
Values of $K_{w}$ typically fall in the range 10-13, although lower and higher values also occur. The value of the characterization factor is an indication of the aromatic content of the hydrocarbon mixture, with lower values generally corresponding to greater aromatic content. Benzene, for example, has a characterization factor of 10.0 , while hexane has a value of 12.8 .

## Example E. 1

A $40^{\circ}$ API hydrocarbon mixture has a Watson characterization factor of 12.0 . Use HEXTRAN to estimate the liquid and vapor properties of the mixture at $350^{\circ} \mathrm{F}$ and $500^{\circ} \mathrm{F}$ and a pressure of 50 psia .

## Solution

Two runs are made, one each for liquid and vapor properties. A flowsheet is constructed consisting of a feed stream, a heater and a product stream. The feed is defined as a bulk property stream, and values of the API gravity and characterization factor are entered on the Specifications form, along with the stream temperature $\left(350^{\circ} \mathrm{F}\right)$ and pressure ( 50 psia ). The flow rate is (arbitrarily) specified as $1000 \mathrm{lb} / \mathrm{h}$ of liquid (run 1) or vapor (run 2). The outlet temperature of the heater is specified to
be $500^{\circ} \mathrm{F}$ and the pressure drop is set to zero. After running the simulations, the following values are obtained from the output files.

| Property | Liquid |  |  | Vapor |  |
| :--- | :---: | :---: | :--- | :--- | :---: |
|  | $350^{\circ} \mathrm{F}$ | $500^{\circ} \mathrm{F}$ |  | $350^{\circ} \mathrm{F}$ | $500^{\circ} \mathrm{F}$ |
| $\rho\left(\mathrm{lbm} / \mathrm{ft}^{3}\right)$ | 43.674 | 39.227 |  | 1.909 | 1.278 |
| $C_{P}\left(\mathrm{Btu} / \mathrm{lbm} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.630 | 0.715 |  | 0.523 | 0.599 |
| $k\left(\mathrm{Btu} / \mathrm{h} \cdot \mathrm{ft} \cdot{ }^{\circ} \mathrm{F}\right)$ | 0.0561 | 0.0471 |  | 0.0114 | 0.0160 |
| $\mu(\mathrm{cp})$ | 0.416 | 0.226 |  | 0.00283 | 0.00399 |
| $\sigma(\mathrm{dyne} / \mathrm{cm})$ | 16.98 | 10.79 |  | - | - |

## References

1. Kreith, F. and M. S. Bohn, Principles of Heat Transfer, 6th edn, Brooks/Cole, Pacific Grove, CA, 2001.
2. Eckert, E. R. G. and R. M. Drake, Analysis of Heat and Mass Transfer, McGraw-Hill, New York, 1972.
3. Raznjevič, K., Handbook of Thermodynamic Tables and Charts, Hemisphere Publishing Corp., New York, 1976.
4. Touloukian, Y. S., ed., Thermophysical Properties of High Temperature Solid Materials, vol. 1: Elements, The MacMillan Company, New York, 1967.
5. Holman, J. P., Heat Transfer, 7th edn, McGraw-Hill, New York, 1990.
6. Brown, A. I. and S. M. Marco, Introduction to Heat Transfer, 3rd edn, McGraw-Hill, New York, 1958.
7. Anonymous, ASME Steam Tables, American Society of Mechanical Engineers, New York, 1967.
8. Anonymous, Flow of Fluids Through Valves, Fittings and Pipe, Technical Paper 410, Crane Company, New York, 1988.
9. Incropera, F. P. and D. P. DeWitt, Introduction to Heat Transfer, 4th edn, Wiley, New York, 2002.
10. Vargaftik, N. B., Tables of Thermophysical Properties of Liquids and Gases, 2nd edn, Hemisphere Publishing Corp., New York, 1975.
11. R. H. Perry and C. H. Chilton, eds, Chemical Engineers' Handbook, 5th edn, McGraw-Hill, New York, 1973.
12. McCabe, W.L., J. C. Smith and P. Harriott, Unit Operations of Chemical Engineering, 4th edn, McGraw-Hill, New York, 1985.
13. Kern, R., How to compute pipe size, Chem. Eng., 82, No. 1, 115-120, 1975.

This page intentionally left blank

## Index

## Note: Page numbers in italics refer to figures and tables

A-frame condenser, 660
Acceleration loss, 478, 510
Acetic acid, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Acetone, properties of liquid at $20^{\circ} \mathrm{C}, 699$
ACOL, 311, 659-660, 662, 664
AES floating-head heat exchanger, 88-89
Air, properties of, 659, 678, 687
Air-cooled heat exchangers, 629
air-side heat-transfer coefficient, 637-638
air-side pressure drop, 638-640
computer software, 653
description, 630-637
equipment for cold climates, 636-637
fans and drivers, 635-636
high-fin tubing, types, 632-633
overall configuration, 630-632
tube bundle construction, 633-635
design
guidelines, 643-644
strategy, 644-653
fan and motor sizing, 640-643
LMTD correction factors, 643, 669-674
overall heat-transfer coefficient, 640
standard US motor sizes, 675
Air density correction, for elevation, 675
Air-side heat-transfer coefficient, 637-638, 645, 648
Air-side pressure drop, 633, 638-640, 660, 665, 667
Air temperature, design value, 644
Akers-Rosson correlation, 620-621
Alloys, 31, 197
thermophysical properties, 684
Ammonia vapor, at atmospheric pressure
thermophysical properties, 697
Aniline, 106, 141
properties of liquid at $20^{\circ} \mathrm{C}, 699$
Annular fins, 47, 51, 192, 632
Annular flow regimes, 402, 404, 416, 430, 562, 564
API gravity, 740
API method for liquid density, 489, 497, 595
API Standard 661, 644
APLE, 311
Approach, see Temperature approach
Area targets
for HEN, 353-356
Arithmetic mean temperature difference, 56
Aspen Plus, 170, 295, 311
Aspen Pinch, 361
Aspen Technology, Inc., 170, 311, 361, 371
Assay data for petroleum streams, 495-496

Assay stream, 152, 496, 497
ASTM distillation, 496

Baffle cut, 89, 196, 218, 307, 308
Baffle leakage streams, 282, 288 correction factor, 249, 259
Baffle pitch, see Pitch, baffle
Baffle space, 206, 580, 588
central baffle space, 251, 260, 261
entrance and exit baffle space, 253
inlet and outlet baffle space, 250, 253, 289
Baffle spacers, 196, 200, 579
Baffle window flow, 246, 252
correction factor, 249, 259
ideal pressure drop
correction factor, 249, 259
for laminar flow, 252
for turbulent flow, 252
Baffles
disk and doughnut, 91
helical, 197
rod, 197, 541
segmental, 89, 199
thickness of, 199, 200
window-cut, 91
Balance equation, thermal energy, 6, 7, 48, 114, 361
Balanced composite curve, 373
Balanced pressure drop requirement, 279
Beatty-Katz correlation, 568, 569
Bell-Delaware method, see Delaware method
Bell-Ghaly method, 591-592
BEM fixed tube-sheet heat exchanger, 88,89
Benzene, 106, 141, 175
properties of liquid at $20^{\circ} \mathrm{C}, 699$
Bimetallic tubing, 632, 633
Birmingham Wire Gage, 90, 717-718
B-JAC, 218
Boiling curve, 386, 387, 540
Boiling heat transfer, 385
convective boiling, in tubes, 416-428
boiling, in vertical tube, 416-417
Chen correlation, 417-418
critical heat flux, 424-428
Gungor-Winterton correlation, 418-419
Liu-Winterton correlation, 419
film boiling, 428-431
nucleate boiling, correlations for
critical heat flux, 399-402
mixture effects, 394-398

Boiling heat transfer (continued)
nucleate boiling, correlations for (continued)
pure component heat-transfer coefficients, 387-394
tube bundles, convective effects in, 398-399
pool boiling, 386-387
two-phase flow
flow regimes, 402-404
pressure drop correlations, 404-412
recommendations, 416
void fraction and two-phase density, 412-416
Boiling number, 419, 422
Boiling range, 395, 397, 470
Box header, 634, 635
Boyko-Kruzhilin method, 558, 564
Brake power, 642, 652
Brazed-fin tubing, 632
Breber et al. correlation, 564, 567
Breber et al. method for determination of condensing flow regime, 562
Briggs and Young correlation, 637-638
Bromley equation, 429, 430
Bubble diameter, theoretical, 393
Bubble point, 397, 489, 496
Bubbly flow regime, 402, 404, 413, 416, 570
Building materials properties of, 685-686
R -value for, 18-19
Bulk property stream, 152, 496
Bulk temperature, 53
Bundle bypass flow, 258
correction factor, 249-250, 259-260
Bundle bypass flow area, 258, 268
n-Butyl alcohol, properties of liquid at $20^{\circ} \mathrm{C}, 699$
BWG, see Birmingham Wire Gage
Bypass flow resistance, 288
Capital cost recovery factor, 358
Carbon dioxide at one atmosphere thermophysical properties, 697
Carpenter-Colburn correlation, 619-620
Central-tube-limit diameter, 253, 254, 255
Chen correlation, 417-418
Chisholm correlation, 406-407, 413
for two-phase density, 413, 416, 453
for two-phase pressure drop in pipes, 406
for two-phase pressure drop in shell-side condensers, 570
Chisholm parameter, 408, 410, 483
Chloroform, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Churn flow, 402
Churn flow regime, 402, 416
CISE correlation, 413-414
Circulation rate
in horizontal thermosyphon reboiler, 467
in kettle reboiler, 449
in Vertical thermosyphon reboiler, 478
Clearances, estimation of, 260-268
shell-to-baffle clearance, 261
shell-to-bundle diametral clearance, 261, 262
tube-to-baffle clearance, 261
Co-current flow, 86, 98, 117
Coefficient of volume expansion
calculation of, 66, 130
definition of, 66
Colburn j-factor, 274, 561
Composite curve
balanced, 373
grand, 334-335, 374
Composite curves, HEN, 331-334
cold composite curve, 331
hot composite curve, 331
Compositional stream, 152, 489, 654
Computer software
for air-cooled heat exchangers, 653
for double-pipe heat exchangers, 152
for heat exchanger networks, 361
for shell-and-tube heat exchanger, 218
for stream analysis method, 295
HEXTRAN
air-cooled heat exchangers, 653-659
condensers, 595-602
double-pipe heat exchangers, 152-169
heat exchanger networks, 361-371
reboilers, 488-502
Shell-and-tube heat exchangers, 218-231
HTFS Suite
air-cooled heat exchangers, 659-664
COMThermo, 175-179
Condensers, 595
double-pipe heat exchangers, 170
mechanical design calculations, 170,311 , 659
reboilers, 502-515
shell-and-tube heat exchangers, 170
tube layouts, 311, 318-320, 507
tube vibration analysis, 311
HTRI Xchanger Suite
air-cooled heat exchangers, 664-668
condensers, 595
reboilers, 515-526
shell-and-tube heat exchangers, 295
tube layouts, 295, 307
tube vibration analysis, 295
VMG Thermo, 295
HX-Net, 371-374
COMThermo, 175-179, 505, 509, 596-597
Condensate nozzles, sizing for gravity drainage, 614-615
Condensate subcooling, 553-557
Condensation, 540
on finned tubes, 568-569
on horizontal tubes, 549-552
inside horizontal tubes, 562-568
annular flow, 564
flow regimes, 562-563
stratified flow, 563-564
multi-component, 590-595
Bell-Ghaly method, 591-592
general problem, 590-591
on vertical surface
plane wall, 545-549
vertical tubes, 549
Condensers, 539
A-frame, 631, 660
air-cooled, 631
computer software, 595-607
condensation
on finned tubes, 568-569
on horizontal tubes, 549-552
inside horizontal tubes, 562-568
multi-component, 590-595
on vertical surface, 545-549
design considerations, 614-615
mean temperature difference, 571-590
Nusselt theory, 545-549
modifications, 552-562
pressure drop, 540, 569-571
types, 540-545
horizontal shell-side condenser, 540-541, 542
horizontal tube-side condenser, 541, 542
reflux condenser, 544-545
vertical shell-side condenser, 541-542, 543
vertical tube-side downflow condenser, 542-544, 543
Condensing curve, 540, 571, 572
Conduction
and convection, 44-46
Conduction shape factor, 19-24
Configurations of hairpins, series/parallel of double-pipe exchangers, 131-132
Contact angle, 390, 393
Contact resistance, 18, 632, 640
Convective boiling, in tubes, 416-428
boiling, in vertical tube, 416-417
Chen correlation, 417-418
critical heat flux, 424-428
Gungor-Winterton correlation, 418-419
Liu-Winterton correlation, 419
Convective heat transfer, 43
conduction and convection, combined, 44-46
forced convection, 44
in external flow, 62-64
in pipes and ducts, $53-56,61-62$
free convection, 44, 65-68
heat transfer fins, 47-53
Cooper correlation, 389
Corrected fin height, 142
Corrected fin radius, 51, 192, 586, 649
Correction factors, correlations
for baffle leakage, 259
for baffle window flow, 259
for bundle bypass flow, 259-260
laminar flow, 260
for unequal baffle spacing, 260

Counter-current flow, 86, 117, 592
Counter flow exchangers, 114, 353, 355
CP difference, 338-339, 342
CP inequality, 338, 339, 342
CP table, 339, 342
Critical heat flux, 471-472, 488
convective boiling
for horizontal tubes, 426-428
for vertical tubes, 424-426
nucleate boiling, 399-402
in pool boiling, 386, 387
in tube bundles, 399-400, 457
Cross-flow
over finned tube banks
heat transfer in, 282
pressure drop in, 251
over plain tube banks
heat transfer and pressure drop in, 246
over single cylinders, 63
Cross-flow area, 254-255, 263
Cross-flow resistance, 287, 289
Cross-flow (X-shell) heat exchanger, 467, 610, 643
Cross passes, 298, 303
Cylinder
critical heat flux for, in pool boiling, 399
forced convection from, 63
free convection from, 67, 399
un-steady state heat transfer in, 28, 29

Darcy friction factor, 55,128
Delaware method, 110, 191, 245
clearances, estimation of, 260-261
correction factors, correlations
baffle leakage, 259
baffle window flow, 259
bundle bypass flow, 259-260
laminar flow, 260
unequal baffle spacing, 260
flow areas
bundle bypass flow area, 258
cross-flow area, 254-255
shell-to-baffle leakage area, 257-258
tube-to-baffle leakage area, 255-257
window flow area, 258-259
ideal tube bank correlations, 246-248
shell-side heat-transfer coefficient, 248-250
shell-side pressure drop, 250-254
Design
double-pipe heat exchangers, 127
horizontal thermosyphon reboilers, 467-473
kettle reboilers, 449
shell-and-tube heat exchangers, 187
vertical thermosyphon reboilers, 473
Design guidelines
for air-cooled heat exchangers
air flow distribution, 644
air velocity, 644
construction standards, 644
design air temperature, 644

Design guidelines (continued)
for air-cooled heat exchangers (continued)
outlet air temperature, 644
tubing, 643
for horizontal thermosyphon reboilers, 467-473
for shell-and-tube heat exchangers
baffles and tubesheets, 199
fluid placement, 197
nozzles, 199-201
sealing strips, 201
shell and head types, 198-199
tube layout, 198
tube passes, 198
tubing selection, 198
Design strategy
for air-cooled heat exchangers, 644-645
for heat-exchanger networks, 339-340
for horizontal thermosyphon reboilers, 467
for kettle reboilers, 449-450
for shell-and-tube heat exchangers, 201
for vertical thermosyphon reboilers, 477-488
Design targets, HEN, 329
Desuperheating, 569, 571
Dew point, 395, 453, 534, 535, 536, 537
Diehl-Koppany correlation, 615
Diffuser, 636
Dittus-Boelter correlation, 419, 486, 564
Dome segment area, 451
Double-pipe heat exchanger, 86-87, 93, 131, 141
analysis, 101-106
multi-tube exchanger, 86,87
simple double-pipe exchanger, 86,87
Double-pipe heat exchangers, design, 127
computer software, 152-177
exchangers without fins
heat-transfer coefficients, 128
hydraulic calculations, 128-131
finned-pipe exchangers, 141-143
characteristics, 141
efficiency, 141-143
flow area and equivalent diameter, 143
overall heat-transfer coefficient, 143
heat-transfer coefficients and friction factors
for finned annuli, 143-145
hydraulic equations, in SI units, 178-179
incremental analysis, 179-180
multi-tube exchangers, 132
standard configuration, 142
over-surface and over-design, 133
series/parallel configurations of hairpins, 131-132
single finned inner pipes, standard configuration, 142
wall temperature, for finned pipes, 145-146
Draft
forced, 630-632, 636, 644
induced, 630-632, 636, 644

Driving force plot, HEN, 356-358
Dry air at atmospheric pressure
thermophysical properties
English units, 687
SI units, 687
Dryout, see Critical heat flux

## E-fin, see Bimetallic tubing

E-shell condenser, 540, 571
Eddy transport mechanism, of heat transfer, 44
Edge-wound/I-fin, 632
Effective mean temperature difference, 454, 469
Effectiveness
heat exchanger, see Heat exchanger effectiveness
of shell-side streams for heat transfer, 282
Efficiency
fan, 665
fin, 50, 53, 141-143, 213, 586
motor, 643
speed reducer, 642
weighted, 142, 148, 663
Elbows, tees and bends, equivalent lengths of, 737
EMAT, see Exchanger Minimum Approach
Temperature
Embedded fin tubing, 632
Emissivity, 431
Engine oil, properties of, 700
Enhancement factor in convective boiling, 418
Enthalpy interval, 351, 354
Equilibrium ratios, 590
Equivalent diameter, 132, 143, 246, 252, 288, 568
Equivalent hydraulic network, 278-279
equations, 279-280
balanced pressure drop requirement, 279
flow resistance coefficient, correlation, 280
mass conservation, 279
stream pressure drops, 279
window friction factor, 280
window pressure drop, 280
Equivalent length concept, 416
Error function (erf), 25
Ethyl acetate, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Ethyl alcohol, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Ethylene glycol, properties of liquid at $20^{\circ} \mathrm{C}, 699$
EXCEL solver, 360
Excess temperature, 386
Exchanger Minimum Approach Temperature
(EMAT), 361
Exchangers without fins
heat-transfer coefficients, 128
hydraulic calculations, 128-131
Expanders and reducers, equivalent lengths of, 739
Expansion joint, 199
Extended surface, see Heat-transfer fins

F-shell heat exchanger, 92
Face area, 644, 646

Face velocity
typical values of, 637, 646, 647
Fan
bay, 635
casing, 636
efficiency, 642
guard, 660
noise, 643
power, 642
ring, 642
selection, 643
shroud, 636
static pressure, 640, 641, 651
Fan and motor sizing
in air-cooled heat exchanger, 640-643
Fan static pressure (FSP), 640, 641-642
Fanning friction factor, 143, 246, 638
Film boiling, 386, 428-431
Film temperature, 63, 64, 552
Fin efficiency, 50, 141-143, 192
Fin geometry, 665
Fin spacing, 568, 569, 637
Finned-pipe exchangers, 141-143
characteristics, 141
dimensions of, 142
efficiency, 141-143
flow area and equivalent diameter, 143
overall heat-transfer coefficient, 143
wall temperature, 145-146, 148
Finned tubing, 192-194
condensation on, 568-569
high-fin
bimetallic (E-fin), 632, 633
brazed, 632
embedded (G-fin), 632, 633
integrally finned (K-fin), 632, 640
shoulder-grooved, 632, 633
tension wound (I-fin, L-fin, LL-fin), 632-633
in kettle reboilers design, 452
radial low-fin, 452
rectangular-fin, 47, 141
in shell-and-tube heat exchangers, 192-194
tension-wound, 632
Fixed-tubesheet heat exchanger, 198-199
Flat plate
forced convection from, 62-63
free convection from, 66
Floating-head heat exchanger, 89, 90
externally sealed (Type W), 88
outside packed (Type P), 88
pull through (Type T), 88
split ring (Type S), 88
Floating head types
comparison, 236
Flooding in reflux condenser
Diehl-Koppany correlation for, 615
Flooding velocity, 615

Flow areas
bundle bypass flow area, 258, 308
bypass flow area, 284
cross-flow area, 254-255
in finned-pipe exchangers, 143
shell-to-baffle leakage area, 257-258
tube-to-baffle leakage area, 255-257
window flow area, 258-259
Flow instability, see Vertical thermosyphon reboilers
Flow regimes, 552
for condensation inside horizontal tubes, 562-565
two-phase flow regimes, 402-403, 404, 504, 541
Flow resistance coefficient, correlation, 280
Fluid placement, 197
criteria for, 106
Forced convection
in external flow, 62-65
and free convection effects, relative importance, 68
in pipes and ducts, 53-62
Forced-draft operation, 635-636
Forced flow reboilers, 446
Forster-Zuber correlation, 388, 418
Fouling factors, 93, 94-96
in kettle reboilers designing, 450
Fourier number (Fo), 26, 28
Fourier's law of heat conduction, 2-6
FRAN, 311
Free convection, 65-70
and forced convection effects, relative importance, 68
Freon 12, properties of saturated liquid, 698
Friction factor
for exchangers without fins
laminar flow, 129-130
turbulent flow, 130
for finned annuli, 143-145
tube-side pressure drops
laminar flow, 189
turbulent flow, 189
Friedel correlation, 407-408
Froude number, 408, 419

G-fin, see Embedded fin tubing
G-shell heat exchanger, 467
Ganguli et al. correlation
for air-side heat transfer, 638
for air-side pressure drop, 639
Gas oil, 115
Gasoline, 124, 641, 701
Glycerine, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Gnielinski
correlation for laminar flow in annulus, 55
correlation for pipe flow, 55
Gorenflo correlation, 439-440
Grand composite curves, HEN, 334-335
Grashof number, 65-66

Gravity controlled condensation
on horizontal tubes, 558-562
inside horizontal tubes, 562, 563
Nusselt theory of, 545, 557-558, 563
on vertical surfaces, 545
on vertical tube banks, 549
Gravity drainage of condensate, 614-615
Groeneveld correlation, 429-430
Gungor-Winterton correlation, 418-419

Hairpin configuration, 86, 131-132
Hairpin heat exchanger, see Double-pipe heat exchanger
Hausen correlation, 54, 128, 566
Head types, comparison of, 235-236
Headers
for air-cooled heat exchangers, 634-635
for shell-and-tube heat exchangers, $92,189,190$, 235-236
Heat capacity flow rate, $315,328,338,669,676$
Heat capacity of liquids, nomograph for, 556
Heat conduction, 1
conduction shape factor, 19-24
equation, 6-15
Fourier's law, 2-6
mechanisms, 31
thermal resistance, 15-19
unsteady-state conduction, 24-31
Heat exchanger effectiveness, 114-116
Heat-exchanger networks (HENs), 327
area targets, 353-356
capital cost, 358
composite curves, 331-334
computer software, 361
design strategy, 339-340
design targets, 329
driving force plot, 356-358
feasibility criteria, at pinch, 337-339
heat capacity flow rate difference, 338-339
heat capacity flow rate inequality, 338
heat capacity flow rate table, 339
process streams and branches, number of, 338
grand composite curve, 334-335
linear programming, targeting by, 359-361
network simplification, 344-347
heat load loops, 344-346
heat load paths, 346-347
operating cost, 358
pinch, significance, 335-337
problem table, 329-331
required shells, 347-348
super targeting, 358-359
targeting, for required shells
analytical method, 350-352
graphical method, 348-350
TC3, 328
minimum-utility design, 340-344
threshold problems and utility pinches, 337

Heat exchanger tubing
high-fin, 632-633
radial low-fin, 192-194
dimensions of, 726-728
rectangular (longitudinal) finned, 47, 141
un-finned, dimensions of, 132, 152
Heat exchangers, 85
air-cooled heat exchangers, 629
and condenser tubing, dimensions, 717
double-pipe exchanger, 86-87
analysis, 102-106
design, 127
effectiveness, 114-116
LMTD
correction factor, 98-101
derivation, 117-118
overall heat-transfer coefficient, 93-98
shell-and-tube exchanger, 87-93
preliminary design, 106-109
rating, 109-114
Heat load loops, in HEN, 344-346
Heat load paths, in HEN, 346-347
Heat Recovery Approach Temperature (HRAT), 361
Heat-transfer coefficients, 44, 398, 416, 548, 550
air-side, in air-cooled heat exchangers, 637-638
for boiling
convective boiling, 416, 417
film boiling, 429
on horizontal tubes, 387-390
of mixtures, 394
nucleate boiling, 387
in tube bundles, 398
in vertical tubes, 420
for condensation
on finned tubes, 568-569
on horizontal tubes, 550
on inclined surfaces, 552
inside horizontal tubes, 563
on vertical surfaces, 552,553
on vertical tube banks, 558
for cross flow, 558
definition of, 44
for double-pipe heat exchangers, 102
for exchangers without fins, 128
for finned annuli, 143-145
for forced convection
over circular cylinder, 63
over flat plate, 62
over non-circular cylinder, 63-64
over sphere, 63
in pipes and ducts, $53,54,55$
for free convection
on horizontal cylinder, 67
on horizontal plate, 67
on sphere, 67
on vertical cylinder, 67
on vertical plate, 67
for laminar flow in annuli, 128
overall
for air-cooled heat exchangers, 630, 640
clean, 111
definition of, 93
design, 94
for finned-tube heat exchangers, 630
required, 111
typical values of
for air-cooled heat exchangers, 641
for shell-and-tube heat exchangers, 107
for shell-and-tube heat exchangers, 188-189
shell-side
Delaware method for, 248-250
simplified Delaware method for, 188-189
stream Analysis method for, 281-282
for steam as heating medium, 452
tube-side, 188
for window flow, 260
Heat-transfer fins, 47-53
annular fins, 47
rectangular fins, 47
Heat-transfer fluids, $17,38,44,45,73,121,533$
Heat Transfer Research, Inc. (HTRI), 110, 278, 295, 515, 664
Helical baffles, 197
n -Heptane, properties of liquid at $20^{\circ} \mathrm{C}, 699$
n -Hexane, properties of liquid at $20^{\circ} \mathrm{C}, 699$
HEXTRAN, 152-169, 218, 267, 268, 295, 361-371, 488-502, 595, 596, 653-659, 740
accessing input and output files for, 157-161, 220-231, 363-369, 490-495, 496-501
design mode, 218, 653
double-pipe heat exchanger (DPE) module, 152
example problems using, 161-169, 218
keyword file, 154, 159, 165, 221, 227, 364, 368, 492, 499, 599, 657
multi-tube hairpin exchanger (MTE) module, 152
rating mode, 152, 218, 295, 297, 653
stream types in, 152-157, 218-219, 295, 361-362, 488-490, 595-597, 653
streams, 152-153
synthesis mode, 361,367
targeting mode, 361
High-fin tubing, 631-633
arrays, characteristics, 634
types, 632, 640
bimetallic, 632
brazed-fin, 632
embedded fin, 632
integrally finned, 632
tension-wound fin, 632
High-torque-drive (HTD) belt, 635
Homogeneous flow model, 404, 412-413, 414
Homogeneous two-phase density, 413, 431, 570
Horizontal shell-side condenser, 540-541, 542, 568
Horizontal thermosyphon reboilers, 445-446, 446
design, 467
guidelines, 467-468
strategy, 467
Horizontal tube-side condenser, 541, 542
Hot air recirculation, 630-631
HRAT, see Heat Recovery Approach Temperature
HTFS, 170, 284, 311
HTFS/Aspen, 170, 218, 311, 595, 659-660
for kettle reboilers, 502
TASC, 502, 595
mechanical, 170, 311
thermal, 170, 311
for thermosyphon reboilers, 503-504
HTRI software, 295, 303, 515-516, 664-665
for air-cooled heat exchangers, 664-665
for kettle reboilers, 515
for thermosyphon reboilers, 515
Xace module, 664-665
Xist module, 295, 296, 515, 595
HTRI Xchanger Suite, 152, 218, 595
HX-Net, 371-374
Hydraulic calculations, 86
for condensers
shell-side condensing, 540-542
tube-side condensing, 542-543
for double-pipe heat exchangers
minor losses, 130
nozzle losses, 130-131
in SI units, 178-179
with fins, 141-143
without fins, 128-131
for exchangers without fins, 128-131
for reboiler systems
kettle, 449
vertical thermosyphon, 502
for shell-and-tube heat exchangers, 189
minor losses, 190, 232
nozzle losses, 232-233
shell side
for baffle window, 250
for cross flow, 281
Delaware method for, 250-253
for end baffle spaces, 281
simplified Delaware method for, 191
stream Analysis method for, 279-280
in SI units, 232-233
tube side, 189-190
of shell-side pressure drop, 191-192
in SI units, 232-233
of tube-side pressure drop, 189-190
Hydraulic equations, 279-281
balanced pressure drop requirements, 279
flow resistance coefficient, correlations, 280
mass conservation, 279
in SI units, 178-179, 232-233
stream pressure drops, 279
window friction factor, 280
window pressure drop, 280
Hydraulic network, 279-281

Hydrocarbon stream, 595, 596
Hyprotech Ltd, 170, 371
HYSYS process simulator, 170, 295, 300, 311, 371

I-fin tubing, 632, 633
Ideal heat-transfer coefficient for mixture boiling, 438
Ideal tube bank correlations, 246-248, 280, 285, 287
Ideal tube bank pressure drop, 250-251, 254
Impingement plate, 201, 515, 596
Impingement protection, 201, 209, 216, 317, 540
Incremental analysis, 179-180, 311, 592, 595, 659
Induced-draft operation, 630-631, 636, 644
Inlet and outlet
baffle spaces, 234, 250, 289
equivalent lengths of, 738
Instability in two-phase flow, see Vertical thermosyphon reboiler
Insulations and building materials, 18-19
thermophysical properties, 685-686
Integrally finned tubing, 632
Interfacial shear, 557-562
condensation in vertical tubes
with vapor downflow, 558
with vapor upflow, 558-559
condensation outside horizontal tubes, 558-559
Internal reboilers, 447
Inverted annular flow, 429, 430
Isobutyl alcohol, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Isothermal flow, 128
j-factor, 274, 561
J-shell condenser, 541, 570, 595-596, 604, 613

K-fin, see Integrally finned tubing
Kandlikar correlation, 420
Kattan correlation, 420
Katto-Ohno correlation, 424-425
Kerosene, 115, 202, 219, 224
Kettle reboilers, 444, 445, 507, 515
design, 449-466
fin tubes, 452
fouling factors, 450
heating medium, 452-453
liquid overflow reservoir, 452
mean temperature difference, 450
nozzles use, 450
shell diameter, 451-452
two-phase density calculation, 453
Kinematic viscosity, 64, 66, 72, 252, 270
Kinetic energy correction factor, 641
Knockback condenser, see Reflux condenser

L-fin tubing, 632, 633
Laminar flow, 128, 129, 130, 189, 252
correction factor, 250, 260

Laplacian operator, 7, 33
Lapse rate, 675
Latent heats of vaporization, organic compounds
hydrocarbon compounds
alkyl benzenes, 705-706
alkyl cyclohexanes, 706
alkyl cyclopentanes, 706
monoolefins, 707
paraffins, 704-705
non-hydrocarbon compounds, 707-711
Leakage flows, see Shell-side streams
Level control, 445, 446, 447
Liedenfrost point, 386
Linear programming, HEN, 359-361
Liquid metals, 554
Liquid overflow reservoir, see Kettle reboilers
Liquid water at saturation pressure
thermophysical properties, 688
Liu-Winterton correlation, 419
LL-fin tubing, 632
Lockhart-Martinelli correlation, 404-406, 413
Lockhart-Martinelli parameter, 421, 558, 562
Logarithmic mean temperature difference (LMTD), 55-56, 131, 347, 450, 571, 643
correction factor
for air-cooled heat exchangers, 643, 669
in multi-pass shell-and-tube exchangers, 98-101, 353
for TEMA J- and X- shells, 612, 613-614
in temperature profile distortion, 282-284
derivation, 117-118
Louvers, 636-637, 651, 660
Low-fin tubing, 192-193
Lube oil, 194, 125, 326
Mass conservation, 279
Mass-transfer coefficient, 395, 590
MATHCAD, 613
Maximum tube-side fluid velocities, 233-234
Maximum unsupported tube lengths, 234
McNaught correlation, 558-559
Mean temperature difference, 93, 571-590
in air-cooled heat exchangers, 643
in double-pipe heat exchangers, 138,282
in horizontal thermosyphon reboilers, 467-468, 469
in kettle reboilers, 450
in shell-and-tube condensers, 550
in shell-and-tube heat exchangers, 198
Merilo correlation, 426
Metallic elements
thermophysical properties, 682
Methane hydrates, 636
Methyl alcohol, properties of liquid at $20^{\circ} \mathrm{C}, 699$
MILP, see Mixed Integer Linear Programming
Minimum utility design
for TC3, 340-343
Minor losses, see Hydraulic calculations
Mist flow, 402, 404

Mist flow limit, 477, 485
Mist flow regime, 402, 404, 413, 416, 429, 477, 478
Mixed integer linear program (MILP), 361, 371
Mostinski correlation, 388-389, 400
for critical heat flux, 388-389
for nucleate boiling, 422-423
Motor size, standard, 675
Multi-component condensation, 590-595
Bell-Ghaly method, 591-595
general problem, 590-591
Multi-pass shell-and-tube exchanger, 98, 347, 350, 353, 355
Multi-tube exchangers, 86, 87, 132
standard configuration, 142
MUSE, 311
Müller-Steinhagen and Heck (MSH) correlation, 408, 416

Natural convection, 44, 386, 660
see also Free convection
Navier-Stokes equation, 546
Newton's Law of Cooling, 44
No-tubes-in-window configuration, 197, 199, 218
Non-Newtonian fluids, 44
Nozzles, 453
Annular, 564
intermediate, in TASC, 172
sizing guidelines for, 199-201, 200
sizing of, for gravity drainage of condensate, 614-615
standard, 130-131
Nozzles, sizing, 199-201
NTU, 115-116
Nucleate boiling, correlations for, 387-402
critical heat flux, 399-401
mixture effects, 394-398
pure component heat-transfer coefficients, 387-394
Cooper correlation, 389
Forster-Zuber correlation, 388
Mostinski correlation, 388-389
Stephan-Abdelsalam correlation, 389-390
tube bundles, convective effects in, 398-399
Nusselt Number
definition of, 54
Nusselt theory, 545-549
modifications of, 552-562
condensate subcooling, 553-557
inclined surfaces, 552
interfacial shear, 557-562
superheated vapor, 553
turbulence, in condensate film, 552-553
variable fluid properties, 552
n-Octane, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Ohm's Law of Electricity, 15
Once-through thermosyphon reboiler system, 447-448

Onset of nucleate boiling (ONB), 386
Outer-tube-limit diameter, 253, 254
Over-design, 133
Over-surface, 133
Overall heat-transfer coefficient, 93-98, 143, 641 fouling, 94
for high-fin tubing, 640
in tubular heat exchanger, 107-108
Overflow reservoir, see Kettle reboilers

## Palen correlation

for convective film boiling, 428, 430
for critical heat flux in convective boiling, 424
for critical heat flux in tube bundles, 398, 400, 401, 426
Palen's method
for boiling in tube bundles, 398, 400
for critical heat flux in convective boiling, 424
for critical heat flux in tube bundles, 400, 401, 426
for heat transfer coefficient, 395
for mixture boiling, 396, 398, 471
Parallel flow, see Co-current flow
Partial condenser, 570
Peng-Robinson equation, 595, 596
n -Pentane, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Petroleum streams, properties of, 740
Pinch
design strategy, 339-340
feasibility criteria at, 337-339
heat capacity flow rate difference, 338-339
heat capacity flow rate inequality, 338
heat capacity flow rate table, 339
process streams and branches, number of, 338
significance, 335-337
threshold problems and utility pinches, 337
Pinch design method, 328, 337
Pipe and tubing, dimensions of
heat exchanger and condenser tubing, 717
radial low-fin tubing
16 fpi tubing, 726
19 fpi tubing, 727
26 fpi tubing, 728
steel pipe, properties, 720
Pipe fittings, equivalent lengths of
elbows, tees and bends, 737
expanders and reducers, 739
inlets and outlets, 738
values, 738
Pitch, 92
baffle, 206, 511
tube, 89
longitudinal, 653
transverse, 653
Plenum, 636
Plug flow regime, 404, 477, 562
Plug header, 634, 645
Pool boiling, 386-387
Prandtl number, 63, 430, 553, 554
definition of, 54

Pressure balance, 474-475
Pressure drop, 569-571
shell-side pressure drop, 191-192, 250-254, 281
affecting factors, 196-197
and stream flow rates, 285-287
tube-side pressure drop affecting factors, 195
Pressure drop correlations, in separated flow model, 404-412
Chisholm correlation, 405-406
Friedel correlation, 406-407
Lockhart-Martinelli correlation, 404-406
Müller-Steinhagen and Heck (MSH) correlation, 408
Pressure gradient, 406, 476, 481
Prime surface, 47, 145, 194, 585, 649
PRO II, 152, 295, 300
Problem table algorithm, HEN, 329-331
ProMax, 218
Pseudo components, 395
Pseudo-critical pressure, 397-398, 455
Pseudo-reduced pressure, 398, 455, 470
Pull-through floating head, 261

Quality of vapor, 429, 558-559

R-value, 18-19
Radial fins, 192, 193, 452, 568, 632, 726-728
Radial low-fin tubing, 192, 193, 726, 727, 728
Radiative heat transfer, in film boiling, 429-431
Rating of heat exchangers
role in design strategy, 339-340
thermal, procedure for, 112-114
using computer software, 295, 311
Reboiler design
fouling factors, 450
Reboilers
computer software, 488
selection, 448-449
types, 444-449
forced flow reboilers, 446
horizontal thermosyphon reboilers, 445-446, 466
internal reboilers, 447
kettle reboilers, 444, 449-466
recirculating versus once-through operation, 447-448
vertical thermosyphon reboilers, 444-445, 473-488
Recirculating thermosyphon reboiler system, 447
Rectangular fins, 47, 141
Reduced pressure, 389
Reflux condenser, 544, 545, 595, 615
Refrigerants, 419, 420
Regression analysis, 389, 570
Relative humidity, 643
Resistance, thermal, see Thermal resistance
Reynolds number, 64, 65, 145, 157, 198, 246, 268

Robinson-Briggs correlation, 639
Rod baffles, see Baffles, rod
Root tube diameter
Effective, 194
Rose-Briggs method, 595
Rotated square pitch, 92 , 198, 248

Saturated liquid Freon-12
thermophysical properties, 698
Saturated liquids
thermophysical properties
at $20^{\circ} \mathrm{C}, 699$
engine oil, 700
ethylene glycol, 700
glycerin, 700
Saturated steam and water
thermophysical properties, 689
viscosities of, 696
Saturation temperature, 386
Schlünder method
for heat transfer coefficient, 394-395
Sealing strips, 92, 201, 219, 307, 603
Segmental baffle geometry, 253
Seider-Tate correlation, 54, 55, 57, 558
Seider-Tate equation, 102, 128, 250, 418
Self-venting line, 614
Semi-infinite solid, transient conduction in, 24
Sensible heat duty, 572
Sensible heating zone, see Vertical thermosyphon reboilers
Series/parallel configurations of hairpins, 131-132
Shah correlation, 420, 567-568
for condensation, 564
for convective boiling, 420
Shape factor, see Heat conduction
Shear controlled condensation, 558, 620
Shell-and-tube exchanger, 87-93
head types comparison
floating head types, 236
stationary head types, 235
preliminary design, 106-109
rating, 109-114
mechanical features of, 91
baffles, 92, 199
head types, 88, 198-199
sealing strips, 92,201
shell types, 88, 198-199
tie rods, $90,307,308$
tube bundles, 92, 198
tubesheets, 89, 199
Shell-and-tube heat exchangers, design
computer software, 218
design guidelines, 197-201
design strategy, 201, 311
finned tubing, 192-194
heat-transfer coefficients, 188-189
hydraulic calculations, 189-192
pressure drop, factors affecting, 195-197
tube-count tables, 194-195

Shell-side heat-transfer coefficient, 248-250, 281-282, 585
Shell-side pressure drop, 191-192, 196-197, 250-254, 281
$\Delta P_{c}$ calculation, 250-251
$\Delta P_{e}$ calculation, 253
$\Delta P_{w}$ calculation, 251-252
Shell-side streams
baffle-to-shell leakage, 282
bundle bypass, 249-250
cross flow, 282
tube-pass-partition bypass, 278
tube-to-baffle leakage, 255-257, 284
Shell-to-baffle clearance, 261, 283
Shell-to-baffle leakage area, 257-258, 259, 268, 282
Shell-to-baffle leakage flow resistance, 288, 292
Shell-to-bundle diametral clearance, 261
Short-pipe correction factor, 54,57
Simple double-pipe exchanger, 86-87
Simplified Delaware method, 188, 191, 201, 219, 267, 560, 577
Slip ratio, 412, 413-414, 415, 482, 566
Slug flow regime, 402, 404, 416, 477, 562
Specific gravity of liquids, 129
Specific heat of liquids, nomograph for, 716
Speed reducer
efficiency of, 642, 652
Sphere
correlation for forced convection from, 68
correlation for natural convection from, 67-68
Split-ring floating head, 541
Standard US motor sizes, 675
Static head, 445, 446, 453, 460, 569
Stationary head types
comparison, 235
STE module, 218
Steam, properties of, 688
Steam at atmospheric pressure
thermophysical properties, 688
Steam coil, 637
Steel pipe, properties, 720
Stefan-Boltzman constant, 429
Steiner-Taborek correlation, 420
Stephan-Abdelsalam correlation, 389-390, 395
Stratified flow regime, 404, 562, 563-564, 570
Stream analysis method, 111, 277, 570
computer software, 295
equivalent hydraulic network, 278-279
equations, 279-281
shell-side heat-transfer coefficient, 281-282
shell-side pressure drop, 281
temperature profile distortion, 282-284
Wills-Johnston method, 284-294, 304
flow resistances, 287-289
inlet and outlet baffle spaces, 289
pressure drops and stream flow rates, 285-287
streams and flow areas, 284-285
total shell-side pressure drop, 289-290
Stream pressure drops, 279, 358

Streams
and flow areas, 284-285
Subcooled boiling, 419, 475
Subcooling
of condensate, 506, 553-557
parameter in Katto-Ohno correlation, 424-425
Super targeting, HEN, 334, 358-359, 371, 372
Superheated vapor, 553
Support plates, 197, 444, 454, 583, 604
Suppression factor in convective boiling, 417-418
Targeting
for minimum heat-transfer area, 353-356
for minimum number of shells, 348-359
for minimum number of units, 340-344
for minimum utilities, 341, 343, 344
super, 358-359
TASC, 176, 296, 502, 504, 505, 506, 595, 596, 597, 603-607
TASC Mechanical, 170, 311, 318, 511
TASC Thermal, 170, 311
thermosyphon reboiler, configuration, 503
TEMA, see Tubular Exchanger Manufacturers Association
TEMA Standards, 200, 234
Temperature approach, 304, 361
Temperature cross, 347-349
Temperature difference, 2, 93, 282, 356
arithmetic mean, 56
effective mean, 454, 469
logarithmic mean, 55-56, 117-118
Temperature gradient, $2,47-48,417,476$, 481-482
Temperature profile distortion, 282-284
Tension-wound finned tubing, 632
Test Case Number 3 (TC3), 328
minimum-utility design
cold end design, 341-343
complete network design, 343-344
hot end design, 340-341
Theoretical bubble diameter, 390, 393
Thermal conductivities, 2-3
of liquids, 701
of tubing materials, 703
Thermal diffusivity, 7
Thermal energy, 6-7, 31, 48
Thermal resistance, 15-19, 21-22
Therminol ${ }^{\circledR}$, 468, 469, 496
Thermodynamic methods
in HEXTRAN, 488-495, 595-603
in HTFS Suite, 170, 311, 502
in HTRI Xchanger Suite, 296, 515-520
Thermodynamic packages
COMThermo, 170, 175-177, 505, 596, 597
VMGThermo, 295, 300, 517, 596
Thermophysical properties, of materials, 682 alloys, 684
ammonia vapor, at atmospheric pressure, 697
carbon dioxide, at one atmosphere, 697

Thermophysical properties, of materials (continued)
dry air, at atmospheric pressure
English units, 687
SI units, 687
insulations and building materials, 685-686
latent heats of vaporization
of organic compounds, 704-711
liquid water, at saturation pressure
SI units, 688
metallic elements, 682-683
saturated liquid Freon 12, 698
saturated liquids
at $20^{\circ} \mathrm{C}, 699$
engine oil, 700
ethylene gylcol, 700
gylcerin, 700
saturated steam and water English units, 689
steam and water, viscosities of English units, 696
steam, at atmospheric pressure, 688
thermal conductivities
of liquids, 701-702
of tubing materials, 703
Thermosyphon reboilers, 541
horizontal thermosyphon reboilers, 445-446 design, 467-473
once through types, 447-448
recirculating type, 447-448
vertical thermosyphon reboilers, 444-445 design, 473-488
Thome and Shakir method
for heat transfer coefficient, 395
Threshold problems and utility pinches, HEN, 337
Tick-off heuristic, 340
Tie rods, $90,307,308$
Toluene properties, 437
of liquid at $20^{\circ} \mathrm{C}, 699$
Total shell-side pressure drop, 281, 289-290
Transient heat conduction
in infinite cylinder, 20, 28, 29-30
in rectangular solid, 24, 28, 40
in semi-infinite solid, 24-29
in sphere, 28, 29
Transition region
In pool boiling, 386-387
Transition region, flow in, 54, 128
Transport properties, 152, 489, 497, 595, 654
Transverse fins, 47
Tube bundle diameter, 254
Tube bundles
in air-cooled heat exchangers, 633-635
boiling in, 398-399
condensation in, 541-542
finned, 189
plain, 189
in cross flow
heat-transfer and pressure-drop correlations for, 254-255

Tube-count tables, 194-195, 729-736
Tube layout
H-banded, 308, 312, 313, 315, 321
Quadrant, 308
ribbon-banded, 308, 312, 313-314
rotated square, $92,110,254,287$
square, 198, 293
triangular, 198, 284
Tube outstand, 320-321
Tube pitch, 88, 196
Tube side, minor losses on, 207
velocity heads, 190
Tube-side pressure drop, 111, 189-190, 195, 464-465
Tube-to-baffle clearance, 261
Tube-to-baffle leakage area, 255-257
Tube-to-baffle leakage flow resistance, 288
Tubesheets, 89, 199, 634
Tubing dimensions
high-fin, 632-633
low-fin, 192-194, 726-728
plain (un-finned), 132, 152
Tubular Exchanger Manufacturers Association (TEMA), 88, 261
E-shell, 444, 445, 446
fouling factors, $95-96$
G-shell, 467
H-shell, 467
J - and X-shells
LMTD correction factors, 609-613
K-shell, 444
Tubular heat exchanger
overall heat exchanger coefficient typical values, 107-108
Turbulent flow, 44, 54, 128, 129, 130, 131, 189, 190, 198, 641
in condensate film, 558
in finned annuli, 143-145
in pipes and ducts friction factor correlations for, 55-56
heat transfer correlations for, 54-55
Turpentine, properties of liquid at $20^{\circ} \mathrm{C}, 699$
Two-phase flow, 386, 402-416
flow regimes, 402-404 for horizontal tubes, 403, 404
for vertical tubes, 402, 403
pressure drop correlations, 404-412
recommendations, 416
void fraction and two-phase density, 412-416
Two-phase multiplier
for heat transfer, 405, 406-407
for pressure drop, 407-408
U-bend supports, 604
U-tubes
in air-cooled heat exchangers, 199, 444, 445
as alternative to floating head, 236
minor losses in, 190
tube counts for, 468

Unequal baffle spacing
correction factor,249, 260
Unmixed-unmixed cross flow, 613
Unsteady-state conduction, 24-31
UOP characterization factor, 740
Utility pinches, 337
Utility stream, 152-153, 362
Utility usage
targets for, 372

V-belt, 635
Vapor blanketing, 429
Vapor loading in kettle reboilers, 451-452
Vapor pressure, 481
Vaporizers, 444
Velocity heads, 130, 131, 190
Velocity pressure, 652
Vent condenser, see Reflux condenser
Vents, 540, 541, 542, 604
Vertical shell-side condenser, 541-542, 543
Vertical thermosyphon reboilers, 416, 444-445
configuration for, 445
design, 473-488
flow instability, 477
mist flow limit, 477
pressure balance, 474-475
sensible heating zone, 475-476
size limitations, 477
strategy, 477-478
Vertical tube-side downflow condenser, 542-544
Vibration analysis, 603, 604
Viscosity
of gases, 715
of liquids, 712
of steam and water, 696
Viscosity correction factor, 102, 129, 145
VMGThermo, 295, 517
Void fraction, 412
and two-phase density, 412-416
Chisholm correlation, 413
CISE correlation, 413-414
homogeneous flow model, 412-413
Lockhart-Martinelli correlation, 413

Wall temperature
for finned pipes, 145-151
Water, properties of, 689-690
Water/steam stream, 152
Watson characterization factor, 740
Watson correlation, 396, 740
Wavy flow regime, 403, 552
Weber number, 414, 415
Wegstein's method, 59
Weighted efficiency of finned surface, 142, 148, 586, 649
Wetted perimeter, 132, 143
Wills-Johnston method, 284-294
flow resistances, 287-289
bypass flow, 288
cross-flow, 287
shell-to-baffle leakage flow, 288
tube-to-baffle leakage flow, 288
window flow, 289
inlet and outlet baffle spaces, 289
pressure drops and stream flow rates, 285-287
streams and flow areas, 284-285
total shell-side pressure drop, 289-290
Window flow area, 258-259
Window flow resistance, 289
Window friction factor, 280
Window pressure drop, 280
Wispy annular flow, 402

X-shell condenser, 541, 605
Xace, 295, 664-668
Xchanger Suite, 295, 664
Xfh, 295
Xhpe, 295
Xist, 295-310, 515-526, 595-597
Xjpe, 295
Xtlo, 295
Xvib, 295

Zone analysis, 478, 485, 488, 571
Zuber equation for critical heat flux, 399, 400


[^0]:    * Class R exchangers are for the generally severe requirements of petroleum and related processing applications.

    Source: HEXTRAN and TEAMS computer programs.

[^1]:    ${ }^{\text {a Area-weighted average over first five zones; subcooled condensate zone not included. }}$
    ${ }^{\mathrm{b}}$ Friction and acceleration, excluding nozzle losses.
    ${ }^{\text {c }}$ Based on specified duty.

[^2]:    ${ }^{\text {a }}$ Area-weighted average of values for sensible heating and boiling zones.
    ${ }^{\mathrm{b}}$ Value for boiling zone.
    ${ }^{\mathrm{c}}$ Friction and acceleration, excluding nozzle losses.

[^3]:    $h$ : height; $D$ : diameter; and $A$ : area.
    Rules for using table: (1) Divide height of segment by the diameter; multiply the area in the table corresponding to the quotient, height/diameter, by the diameter squared. When segment exceeds a semicircle, its area is: area of circle minus the area of a segment whose height is the circle diameter minus the height of the given segment. (2) To find the diameter when given the chord and the segment height: the diameter $=\left[(1 / 2 \text { chord })^{2} /\right.$ height $]+$ height.
    Source: Ref. [18]

[^4]:    Source: Refs. [1] and [2].

[^5]:    Source: Refs. [5] and [6].

[^6]:    Data generated using the PRO II process simulator

[^7]:    Source: Ref. [7].

[^8]:    Source: Refs. [9] and [10].

[^9]:    Source: Refs. [1] and [2].

[^10]:    Source: Refs. [2] and [9].

[^11]:    ${ }^{\mathrm{a}} \mathrm{ID}=\mathrm{OD}-2 \times$ wall thickness from part (a) of table
    ${ }^{\mathrm{b}}$ Internal area $=(\pi / 4)(\mathrm{ID})^{2}$
    ${ }^{\text {c }}$ External surface per foot length $=\pi(\mathrm{OD} / 12)$

[^12]:    Source: Reprinted from ASME B36.10-1959 and B36.19-1965, by permission of the American Society of Mechanical Engineers; all rights reserved.

[^13]:    For S/T Trufin ${ }^{\circledR} 16$ fpi, the average fin height is 0.053 in . $(1.35 \mathrm{~mm})$ and the average fin width is $0.010 \mathrm{in} .(0.254 \mathrm{~mm})$.
    Source: Wolverine Tube, Inc., www.wlv.com

[^14]:    For S/T Trufin ${ }^{\circledR} 19$ fpi, the minimum fin height is 0.050 in . $(1.27 \mathrm{~mm}$ ) and the average fin width is 0.011 in . ( 0.279 mm ).

[^15]:    Type 326 FPI Fine-Fin ${ }^{\circledR}$ Materials: Ferritic Stainless Steel, Carbon Steel, Copper-Nickel Alloys, Monel. For Type 326 FPI Fine-Fin ${ }^{\circledR}$, the average fin height is 0.049 in. ( 1.245 mm ) and the average fin thickness is 0.013 in . $(0.330 \mathrm{~mm})$.
    Source: High Performance Tube, Inc., www.highperformancetube.com

[^16]:    * For $45^{\circ}$ elbows and bends, estimate $50 \%$ of tabulated values. For $180^{\circ}$ returns, double the tabulated values.

[^17]:    * For partially closed globe valves, multiply tabulated values by 3 for three-quarters open, by 12 for one-half open, and by 70 for one-quarter open.
    ${ }^{1}$ With port area open. Port area $=$ pipe area
    ${ }^{2}$ Port area equals $80 \%$ of pipe area.

