



بارم هر سوال ۲/۳۳ می باشد.

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Rod AB.

$$P = 40 + 30 = 70 \text{ kN} = 70 \times 10^3 \text{ N}$$

$$\sigma_{AB} = \frac{P}{A_{AB}} = \frac{P}{\frac{\pi}{4} d_1^2} = \frac{4P}{\pi d_1^2}$$

$$d_1 = \sqrt{\frac{4P}{\pi \sigma_{AB}}} = \sqrt{\frac{(4)(70 \times 10^3)}{\pi(140 \times 10^6)}} = 25.2 \times 10^{-3} \text{ m}$$

$$d_1 = 25.2 \text{ mm} \quad \blacktriangleleft$$

Rod BC

$$P = 30 \text{ kN} = 30 \times 10^3 \text{ N}$$

$$\sigma_{BC} = \frac{P}{A_{BC}} = \frac{P}{\frac{\pi}{4} d_2^2} = \frac{4P}{\pi d_2^2}$$

$$d_2 = \sqrt{\frac{4P}{\pi \sigma_{BC}}} = \sqrt{\frac{(4)(30 \times 10^3)}{\pi(140 \times 10^6)}} = 16.52 \times 10^{-3} \text{ m}$$

$$d_2 = 16.52 \text{ mm} \quad \blacktriangleleft$$



$$\sigma_y = 0 \quad \epsilon_y = 0$$

$$\epsilon_y = \frac{1}{E} (\sigma_y - \nu \sigma_x) = 0 \quad \sigma_y = \nu \sigma_x$$

$$\epsilon_z = \frac{1}{E} (-\nu \sigma_x - \nu \sigma_y) = -\frac{\nu (\sigma_x + \sigma_y)}{E}$$

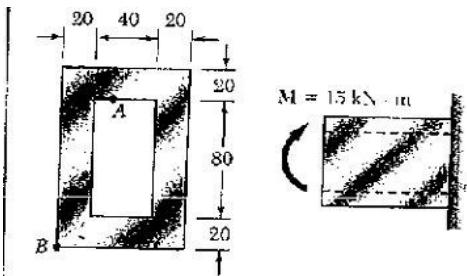
$$\epsilon_x = \frac{1}{E} (\sigma_x - \nu \sigma_y)$$

$$A_0 + \Delta A = L_x (1 + \epsilon_x) L_z (1 + \epsilon_z) = L_x L_z (1 + \epsilon_x + \epsilon_z + \epsilon_x \epsilon_z)$$

$$\text{But } A_0 = L_x L_z$$

$$\Delta A = L_x L_z (\epsilon_x + \epsilon_z + \epsilon_x \epsilon_z)$$

$$\text{Since } L_y \text{ is constant } \Delta V = L_y (\Delta A)$$



Dimensions in mm

For rectangle $I = \frac{1}{12} b h^3$

Outside rectangle: $I_1 = \frac{1}{12} (80)(120)^3$

$I_1 = 11.52 \times 10^6 \text{ mm}^4 = 11.52 \times 10^{-6} \text{ m}^4$

Cutout: $I_2 = \frac{1}{12} (40)(80)^3$

$I_2 = 1.70667 \times 10^6 \text{ mm}^4 = 1.70667 \times 10^{-6} \text{ m}^4$

Section: $I = I_1 - I_2 = 9.81333 \times 10^{-6} \text{ m}^4$

(a) $y_A = 40 \text{ mm} = 0.040 \text{ m}$

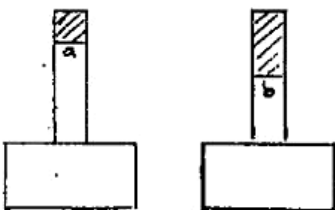
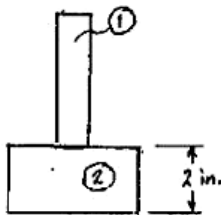
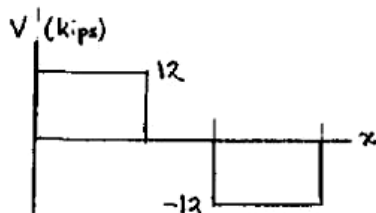
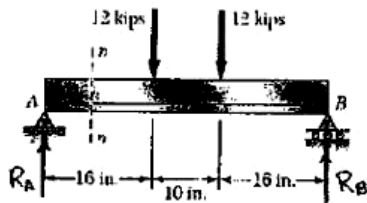
$\sigma_A = -\frac{M y_A}{I} = -\frac{(15 \times 10^3)(0.040)}{9.81333 \times 10^{-6}} = -61.6 \times 10^6 \text{ Pa}$

$\sigma_A = -61.6 \text{ MPa}$

(b) $y_B = -60 \text{ mm} = -0.060 \text{ m}$

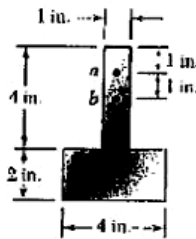
$\sigma_B = -\frac{M y_B}{I} = -\frac{(15 \times 10^3)(-0.060)}{9.81333 \times 10^{-6}} = 91.7 \times 10^6 \text{ Pa}$

$\sigma_B = 91.7 \text{ MPa}$



(a)

(b)



$$R_A = R_B = 12 \text{ kips.}$$

Draw shear diagram.

$$V = 12 \text{ kips}$$

Determine section properties.

Part	A (in ²)	\bar{y} (in.)	A \bar{y} (in ³)	d (in.)	Ad ² (in ⁴)	\bar{I} (in ⁴)
①	4	4	16	2	16	5.333
②	8	1	8	-1	8	2.667
Σ	12		24		24	8.000

$$\bar{y} = \frac{\Sigma A\bar{y}}{\Sigma A} = \frac{24}{12} = 2 \text{ in.}$$

$$I = \Sigma Ad^2 + \Sigma \bar{I} = 32 \text{ in}^4$$

$$(a) \quad A = 1 \text{ in}^2 \quad \bar{y} = 3.5 \text{ in.} \quad Q_a = A\bar{y} = 3.5 \text{ in}^3$$

$$t = 1 \text{ in.}$$

$$\tau_a = \frac{VQ_a}{It} = \frac{(12)(3.5)}{(32)(1)} = 1.3125 \text{ ksi} \quad \blacktriangleleft$$

$$(b) \quad A = 2 \text{ in}^2 \quad \bar{y} = 3 \text{ in.} \quad Q_b = A\bar{y} = 6 \text{ in}^3$$

$$t = 1 \text{ in.}$$

$$\tau_b = \frac{VQ_b}{It} = \frac{(12)(6)}{(32)(1)} = 2.25 \text{ ksi} \quad \blacktriangleleft$$



$$\sigma_{\max, \min} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2} \quad \tan 2\theta_p = \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

$$\tau_{\max} = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$\sigma' = \sigma_{\text{ave}} = \frac{\sigma_x + \sigma_y}{2}$$